

# Frame Assignments

## 1 FRAME DIAGRAM

The Quanser Arm's frame diagram is attached in Figure 1. This was developed using the Standard Denavit Hartenberg (DH) parameters [1].

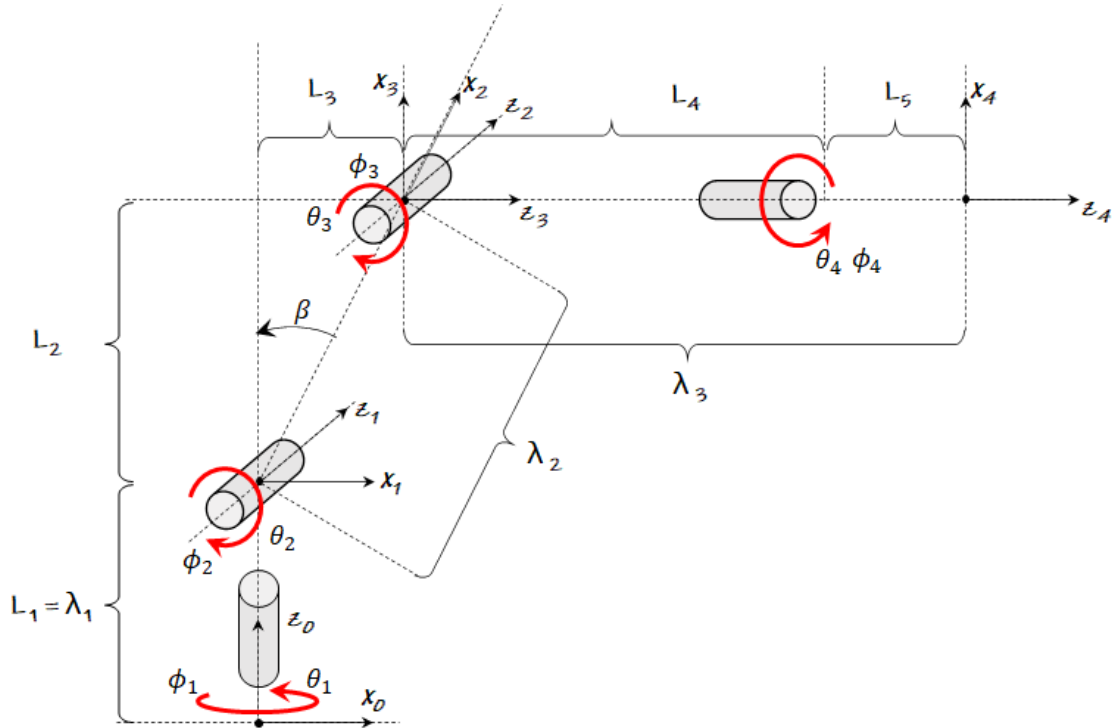


Figure 1. Frame diagram for the Quanser Arm manipulator

Note that the manipulator shown in Figure 1 is currently in its home position. In this state, the joint space vector  $\vec{\theta}$  is,

$$\vec{\theta} = \begin{bmatrix} 0 \\ \beta - \frac{\pi}{2} \\ -\beta \\ 0 \end{bmatrix} \quad (3)$$

The manipulator's encoders and actuators though, are calibrated at this position. Thus, an actuator command of  $[0 \ 0 \ 0 \ 0]^T$  would move the manipulator to the home position, where it's encoders would read a joint position of  $[0 \ 0 \ 0 \ 0]^T$  as well. We can represent this alternate joint space as  $\vec{\phi}$ . A mapping summarized in Table 1 will allow us to describe the manipulator in  $\vec{\phi}$  space, while we carry out the mathematics in  $\vec{\theta}$  space without having to carry around the offset in equation 3. For example, a command of  $\phi_2 = 0$  will imply  $\theta_2 = \beta - \frac{\pi}{2}$  which corresponds to joint 2 in the home position. Algebraically, a reference to  $\theta_2$  in the mathematics already includes this offset.

New parameter	Original Parameter	New parameter	Original Parameter
$\lambda_1$	$L_1$	$\phi_1$	$\theta_1$
$\lambda_2$	$\sqrt{L_2^2 + L_3^2}$	$\phi_2$	$\theta_2 + \frac{\pi}{2} - \beta$
$\lambda_3$	$L_4 + L_5$	$\phi_3$	$\theta_3 + \beta$
$\beta$	$\tan^{-1}(L_3/L_2)$	$\phi_4$	$\theta_4$

Table 1. Linear mapping to simplify the mathematical formulations

## 2 DH TABLE

The DH table corresponding to the frame diagram in Figure 1 is presented in Table 2.

$i$	$a_i$	$\alpha_i$	$d_i$	$\theta_i$
1	0	$-\pi/2$	$\lambda_1$	$\theta_1$
2	$\lambda_2$	0	0	$\theta_2$
3	0	$-\pi/2$	0	$\theta_3$
4	0	0	$\lambda_3$	$\theta_4$

Table 2. DH Table