

40)

$T = \sum X_i$ 是充分完全统计量

$\therefore \bar{X}$ 是 UMVUE, 方差为 θ^2/n

$$I(\theta) = E\left(\frac{\partial}{\partial \theta} \log \theta\right)^2 = E\left(\frac{1}{\theta}\right)^2 = 1/\theta^2$$

$$\therefore D \geq \theta^2/n$$

44)

$$E(\hat{\sigma}) = \sigma$$

由 $\sum (X_i - \bar{X})^2$ 是 σ^2 的充分完全统计量

立得 $\hat{\sigma}$ 是 UMVUE

$$D \geq 2\sigma^4/n$$

$$Var(\hat{\sigma}) = Var\left(\frac{1}{\sqrt{n}} \sum (X_i - \bar{X})^2\right) = 4\sigma^4/n$$

$$\therefore e = 1/2$$