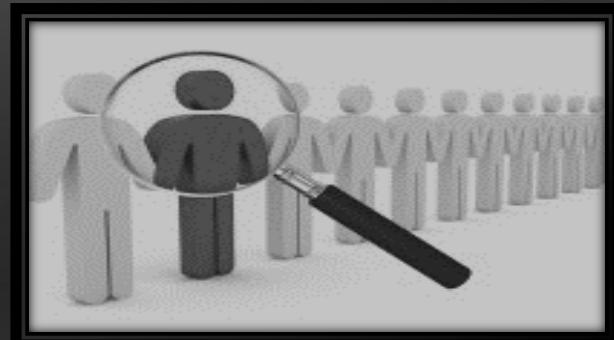
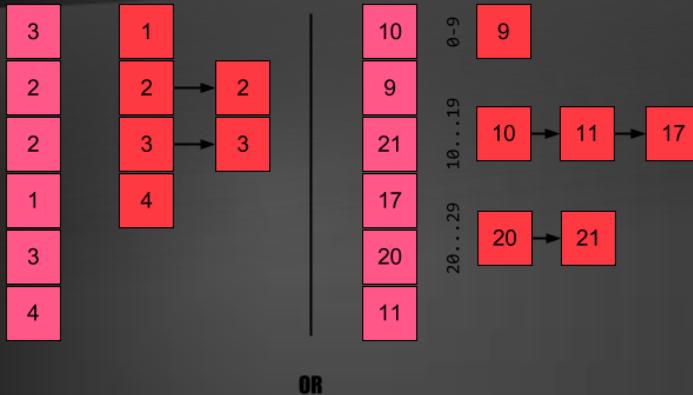


BUCKET SORT



Sorting and Searching Algorithms

Data Structures and Algorithms

Telerik Software Academy

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Sorting



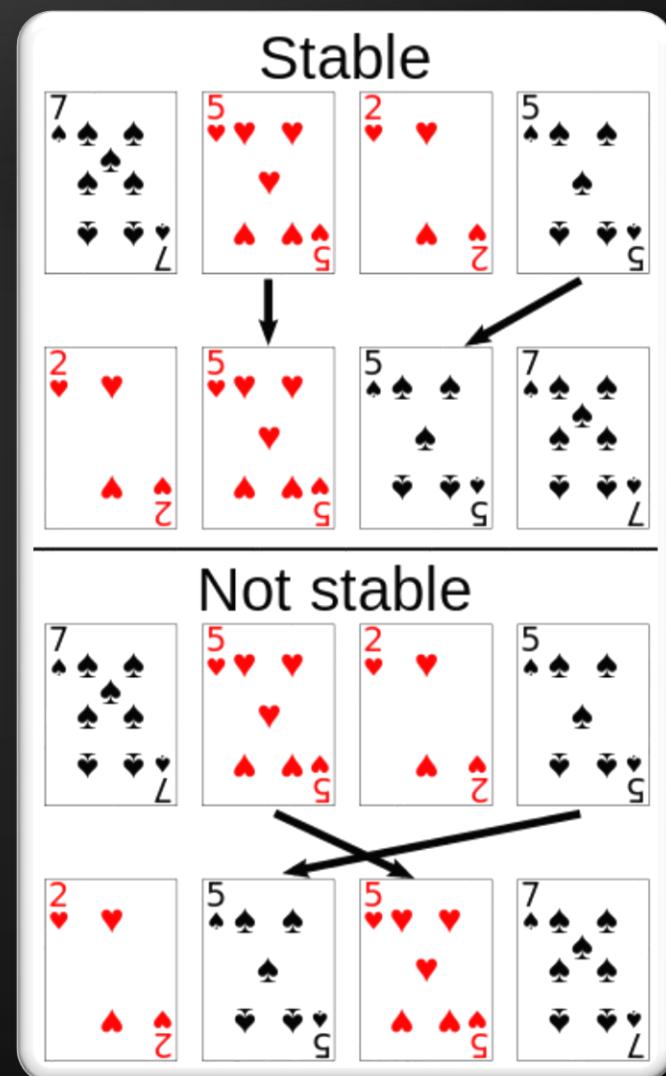
What is a Sorting Algorithm?

- ◆ **Sorting algorithm**
 - ◆ An algorithm that puts elements of a list in a certain order (most common lexicographically)
- ◆ **More formally:**
 - ◆ The output is in some (non-decreasing) order
 - ◆ The output is a permutation of the input
- ◆ **Efficient sorting is important for**
 - ◆ Producing human-readable output
 - ◆ Canonicalizing data
 - ◆ Optimizing the use of other algorithms
- ◆ **Sorting presents many important techniques**

- ◆ Sorting algorithms are often classified by
 - ◆ Computational complexity
 - ◆ worst, average and best behavior
 - ◆ Memory usage
 - ◆ Recursive or non-recursive
 - ◆ Stability
 - ◆ Whether or not they are a comparison sort
 - ◆ General method
 - ◆ insertion, exchange (bubble sort and quicksort), selection (heapsort), merging, serial or parallel...

Stability of Sorting

- ◆ Stable sorting algorithms
 - ◆ Maintain the relative order of records with equal values
 - ◆ If two items compare as equal, then their relative order will be preserved
 - ◆ When sorting only part of the data is examined when determining the sort order



- ◆ Very simple and very inefficient algorithm
 - ◆ Best, worst and average case: n^2
 - ◆ Memory: 1 (constant, only for the min element)
 - ◆ Stable: No
 - ◆ Method: Selection

```
for (j = 0; j < n-1; j++) {  
    /* find the min element in the unsorted a[j .. n-1] */  
    iMin = j;  
    for ( i = j+1; i < n; i++) {  
        if (a[i] < a[iMin]) iMin = i;  
    }  
    if (iMin != j) swap(a[j], a[iMin]);  
}
```

- ◆ http://en.wikipedia.org/wiki/Selection_sort

- ♦ Repeatedly stepping through the list, comparing each pair of adjacent items and swap them if they are in the wrong order
 - ♦ Best case: n , worst and average case: n^2
 - ♦ Memory: 1, Stable: Yes, Method: Exchanging

```
procedure bubbleSort( A : list of sortable items )
    repeat
        swapped = false
        for i = 1 to length(A) - 1 inclusive do:
            /* if this pair is out of order */
            if A[i-1] > A[i] then
                /* swap them and remember something changed */
                swap( A[i-1], A[i] )
                swapped = true
            end if
        end for
        until not swapped
    end procedure
```

- ♦ http://en.wikipedia.org/wiki/Bubble_sort

- ◆ Builds the final sorted array one item at a time
 - ◆ Best case: n, worst and average case: n^2
 - ◆ Memory: 1, Stable: Yes, Method: Insertion

```
for i ← 1 to i ← length(A)-1
{
    valueToInsert ← A[i]
    holePos ← i
    while holePos > 0 and valueToInsert < A[holePos - 1]
    {
        A[holePos] ← A[holePos - 1] // shift the larger value up
        holePos ← holePos - 1      // move the hole position down
    }
    A[holePos] ← valueToInsert
}
```

- ◆ http://en.wikipedia.org/wiki/Insertion_sort

- ◆ First divides a large list into two smaller sub-lists then recursively sort the sub-lists
 - ◆ Best and average case: $n * \log(n)$, worst: n^2
 - ◆ Memory: $\log(n)$ stack space
 - ◆ Stable: Depends
 - ◆ Method: Partitioning

Stable implementation

```
function quicksort ('array')
    if length('array') ≤ 1
        return 'array' // an array of zero or one elements is already sorted
    select and remove a pivot value 'pivot' from 'array'
    create empty lists 'less' and 'greater'
    for each 'x' in 'array'
        if 'x' ≤ 'pivot' then append 'x' to 'less'
        else append 'x' to 'greater'
    return concatenate(quicksort('less'), 'pivot', quicksort('greater'))
```

- ◆ <http://en.wikipedia.org/wiki/Quicksort>

- ◆ Conceptually, a merge sort works as follows
 - ◆ Divide the unsorted list into n sublists, each containing 1 element (list of 1 element is sorted)
 - ◆ Repeatedly merge sublists to produce new sublists until there is only 1 sublist remaining
- ◆ Best, average and worst case: $n * \log(n)$
- ◆ Memory: Depends; worst case is n
- ◆ Stable: Yes; Method: Merging
- ◆ Highly parallelizable (up to $O(\log(n))$) using the Three Hungarian's Algorithm
- ◆ http://en.wikipedia.org/wiki/Merge_sort

Merge Sort Pseudocode

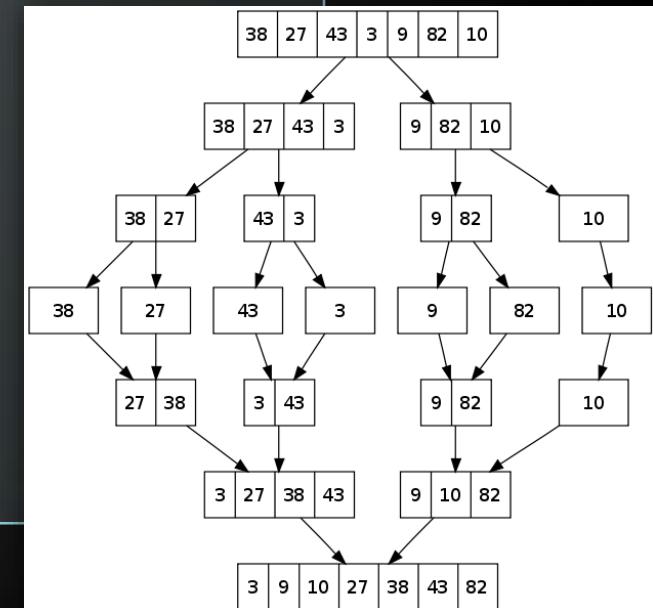
```
function merge_sort(list m)
    // if list size is 0 (empty) or 1, consider it sorted
    // (using less than or equal prevents infinite recursion for a
zero length m)
    if length(m) <= 1
        return m
    // else list size is > 1, so split the list into two sublists
    var list left, right
    var integer middle = length(m) / 2
    for each x in m before middle
        add x to left
    for each x in m after or equal middle
        add x to right
    // recursively call merge_sort() to further split each sublist
    // until sublist size is 1
    left = merge_sort(left)
    right = merge_sort(right)
    // merge the sublists returned from prior calls to merge_sort()
    // and return the resulting merged sublist
    return merge(left, right)
```

Merge Sort Pseudocode (2)

```

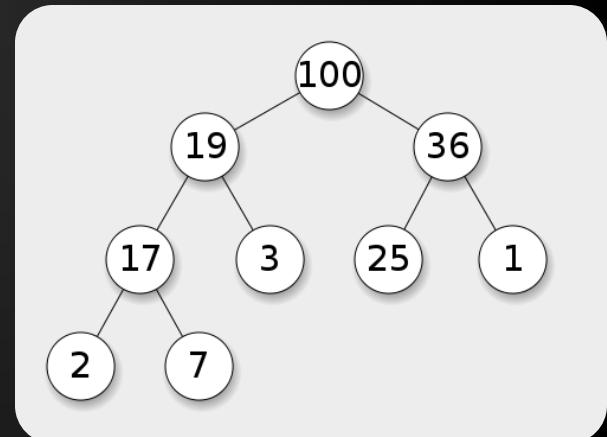
function merge(left, right)
    var list result
    while length(left) > 0 or length(right) > 0
        if length(left) > 0 and length(right) > 0
            if first(left) <= first(right)
                append first(left) to result
                left = rest(left)
            else
                append first(right) to result
                right = rest(right)
        else if length(left) > 0
            append first(left) to result
            left = rest(left)
        else if length(right) > 0
            append first(right) to result
            right = rest(right)
    end while
    return result

```



- ◆ Specialized tree-based data structure that satisfies the heap property:
 - ◆ Parent nodes are always greater (less) than or equal to the children
 - ◆ No implied ordering between siblings or cousins

find-min	$\Theta(1)$
delete-min	$\Theta(\log n)$
insert	$\Theta(\log n)$
decrease-key	$\Theta(\log n)$
merge	$\Theta(n)$



- ◆ [en.wikipedia.org/wiki/Heap_\(data_structure\)](https://en.wikipedia.org/wiki/Heap_(data_structure))

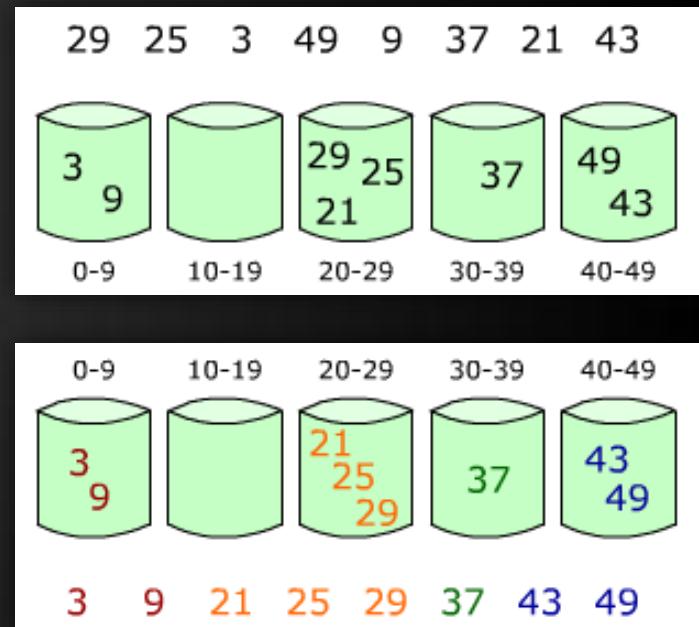
- ◆ Can be divided into two parts
 - ◆ In the first step, a heap is built out of the data
 - ◆ A sorted array is created by repeatedly removing the largest element from the heap
- ◆ Best, average and worst case: $n * \log(n)$
- ◆ Memory: Constant - $O(1)$
- ◆ Stable: No
- ◆ Method: Selection
- ◆ <http://en.wikipedia.org/wiki/Heapsort>

Counting sort

- ◆ Algorithm for sorting a collection of objects according to keys that are small integers
- ◆ Not a comparison sort
- ◆ Average case: $n + r$
- ◆ Worst case: $n + r$
 - r is the range of numbers to be sorted
- ◆ Stable: Yes
- ◆ Memory: $n + r$
- ◆ http://en.wikipedia.org/wiki/Counting_sort

Input Data												
0	4	2	2	0	0	1	1	0	1	0	2	4
Count Array												
0	1	2	3	4								
5	3	4	0	2								
Sorted Data												
0	0	0	0	0	1	1	1	2	2	2	4	4

- ◆ Partitioning an array into a number of buckets
 - ◆ Each bucket is then sorted individually
- ◆ Not a comparison sort
- ◆ Average case: $n + k$
 - ◆ $k = \text{the number of buckets}$
- ◆ Worst case: $n^2 * k$
- ◆ Stable: Yes
- ◆ Memory: $n * k$
- ◆ http://en.wikipedia.org/wiki/Bucket_sort

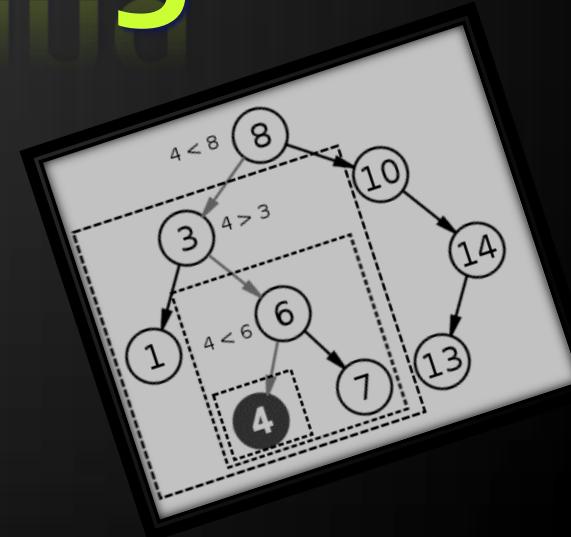
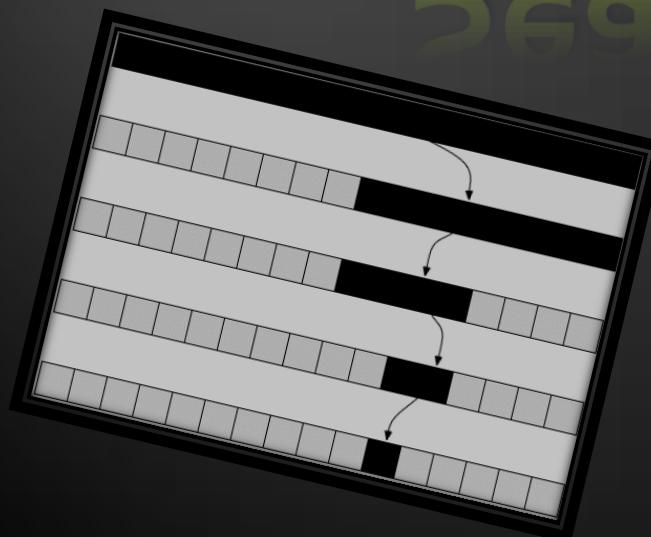


Comparison of Sorting Algorithms

- ◆ There are hundreds of sorting algorithms

Name	Best	Average	Worst	Memory	Stable	Method
Selection sort	n^2	n^2	n^2	1	No	Selection
Bubble sort	n	n^2	n^2	1	Yes	Exchanging
Insertion sort	n	n^2	n^2	1	Yes	Insertion
Quicksort	$n * \log(n)$	$n * \log(n)$	n^2	$\log(n)$	Depends	Partitioning
Merge sort	$n * \log(n)$	$n * \log(n)$	$n * \log(n)$	Depends worst case is n	Yes	Merging
Heapsort	$n * \log(n)$	$n * \log(n)$	$n * \log(n)$	1	No	Selection
Bogosort	n	$n * n!$	$n * n!$	1	No	Luck
...

Searching



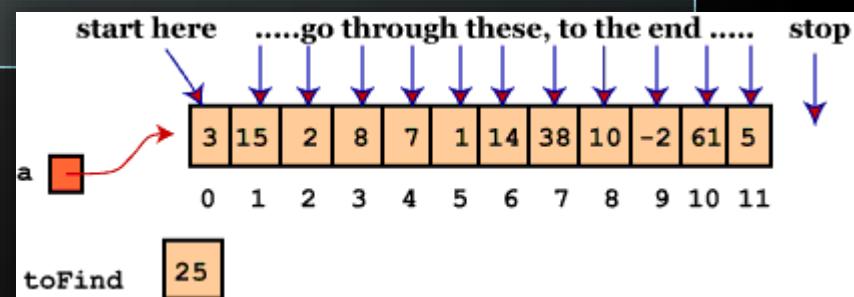
Search Algorithm

- ◆ An algorithm for finding an item with specified properties among a collection of items
- ◆ Different types of searching algorithms
 - ◆ For virtual search spaces
 - ◆ satisfy specific mathematical equations
 - ◆ try to exploit partial knowledge about structure
 - ◆ For sub-structures of a given structure
 - ◆ graph, a string, a finite group
 - ◆ Search for the max (min) of a function
 - ◆ etc.



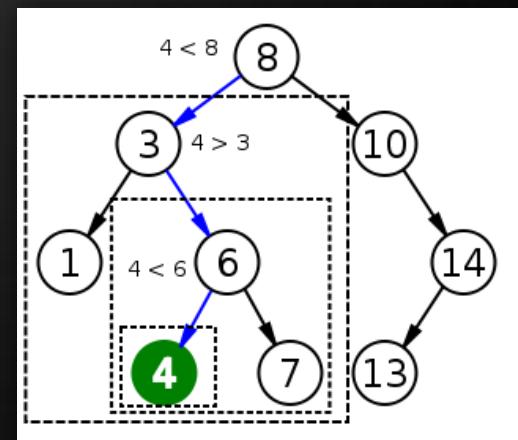
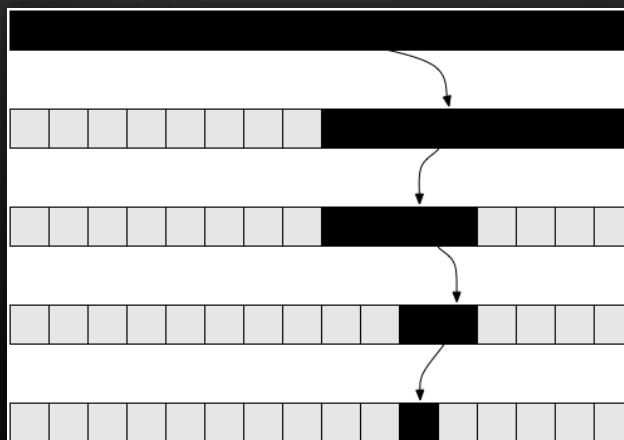
- ◆ Method for finding a particular value in a list
 - ◆ Checking every one of the elements
 - ◆ One at a time in sequence
 - ◆ Until the desired one is found
- ◆ Worst and average performance: $O(n)$

```
for each item in the list:  
    if that item has the desired value,  
        stop the search and return the item's location.  
return nothing.
```



Binary Search

- ◆ Finds the position of a specified value within a sorted data structure
- ◆ In each step, compare the input with the middle
 - The algorithm repeats its action to the left or right sub-structure
- ◆ Average performance: $O(\log(n))$



Recursive Binary Search

```
int binary_search(int A[], int key, int imin, int imax)
{
    if (imax < imin)
        // set is empty, so return value showing not found
        return KEY_NOT_FOUND;
    else
    {
        // calculate midpoint to cut set in half
        int imid = midpoint(imin, imax);
        if (A[imid] > key)
            // key is in lower subset
            return binary_search(A, key, imin, imid-1);
        else if (A[imid] < key)
            // key is in upper subset
            return binary_search(A, key, imid+1, imax);
        else
            // key has been found
            return imid;
    }
}
```

Iterative Binary Search

```
int binary_search(int A[], int key, int imin, int imax)
{
    // continue searching while [imin,imax] is not empty
    while (imax >= imin)
    {
        /* calculate the midpoint for roughly equal partition */
        int imid = midpoint(imin, imax);
        // determine which subarray to search
        if (A[imid] < key)
            // change min index to search upper subarray
            imin = imid + 1;
        else if (A[imid] > key)
            // change max index to search lower subarray
            imax = imid - 1;
        else
            // key found at index imid
            return imid;
    }
    return KEY_NOT_FOUND;
}
```

Interpolation Search

- ◆ An algorithm for searching for a given key value in an indexed array that has been ordered by the values of the key
 - ◆ Parallels how humans search through a telephone book
 - ◆ Calculates where in the remaining search space the sought item might be
 - ◆ Binary search always chooses the middle element
- ◆ Average case: $\log(\log(n))$, Worst case: $O(n)$
- ◆ http://youtube.com/watch?v=l1ed_bTv7Hw

Interpolation Search Sample Implementation

```
public int interpolationSearch(int[] sortedArray, int toFind){  
    // Returns index of toFind in sortedArray, or -1 if not found  
    int low = 0;  
    int high = sortedArray.length - 1;  
    int mid;  
    while(sortedArray[low] <= toFind && sortedArray[high] >= toFind) {  
        mid = low + ((toFind - sortedArray[low]) * (high - low)) /  
              (sortedArray[high] - sortedArray[low]);  
        // out of range is possible here  
        if (sortedArray[mid] < toFind)  
            low = mid + 1;  
        else if (sortedArray[mid] > toFind)  
            high = mid - 1;  
        else  
            return mid;  
    }  
    if (sortedArray[low] == toFind) return low;  
    else return -1; // Not found  
}
```



Shuffling

```
// Shuffle using Fisher-Yates (Knuth) algorithm
for (int i = len; i > 0; i--)           - Count DOWN
{
    int j = (int)(Math.random() * i); - Index from 0..i

    int temp = lotteryBalls[j];
    lotteryBalls[j] = lotteryBalls[i];
    lotteryBalls[i] = temp;
}
```

- ◆ A procedure used to randomize the order of items in a collection
 - ◆ Generating random permutation



- ◆ <http://en.wikipedia.org/wiki/Shuffling>

Fisher–Yates shuffle algorithm

```
public static IEnumerable<T> Shuffle<T>(this IEnumerable<T> source)
{
    var array = source.ToArray();
    var n = array.Length;
    for (var i = 0; i < n; i++)
    {
        // Exchange a[i] with random element in a[i..n-1]
        int r = i + RandomProvider.Instance.Next(0, n - i);
        var temp = array[i];
        array[i] = array[r];
        array[r] = temp;
    }
    return array;
}

public static class RandomProvider
{
    private static Random Instance = new Random();
}
```

Sorting and Searching Algorithms

Questions?

- ◆ Open **Sorting-and-Searching-Algorithms-Homework.zip** and:
 1. Implement `SelectionSorter.Sort()` method using selection sort algorithm
 2. Implement `Quicksorter.Sort()` method using quicksort algorithm
 3. Implement `MergeSorter.Sort()` method using merge sort algorithm
 4. Implement `SortableCollection.LinearSearch()` method using linear search
 - Don't use built-in search methods. Write your own.

5. Implement `SortableCollection.BinarySearch()` method using binary search algorithm
6. Implement `SortableCollection.Shuffle()` method using shuffle algorithm of your choice
 - Document what is the complexity of the algorithm
7. * Unit test sorting algorithms
 - `SelectionSorter.Sort()`
 - `Quicksorter.Sort()`
 - `MergeSorter.Sort()`
8. * Unit test searching algorithms
 - `SortableCollection.LinearSearch()`
 - `SortableCollection.BinarySearch()`

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