

#### V.GOKULKUMAR

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ASSIGN-5

## **Contents**

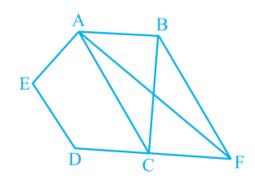
FWC22034

1	Problem	1
2	Solution	1
3	Construction	2

# 1 Problem

ABCDE is a pentagon. A line through B parallel to AC meets DC produced at F. Show that  $\begin{tabular}{ll} \end{tabular} \begin{tabular}{ll} \end{tabular} \begin{tabular}{ll$ 

(i) ar (ACB) = ar (ACF)(ii) ar (AEDF) = ar (ABCDE)



## 2 Solution

Theory:

In pentagon ABCDE,  $AC \parallel BF$ **To Prove:** Ar(ACB)=Ar(ACF)

 $\Delta$  ACB and  $\Delta$  ACF lies on same base AC and are between

same parallel AC and BF

**Theorem**: Two triangles on the same base (or equal bases) and between the same parallels are equal in area.

$$\therefore$$
 Ar( $\triangle$  ACB)=Ar( $\triangle$  ACF).....(1)  
Hence, Proved

To Prove: Ar(AEDF)=Ar(ABCDE)Add Ar(AEDC) to (1) both sides

 $Ar(\Delta ACB) + Ar(AEDC) = Ar(\Delta ACF) + Ar(AEDC)$ 

#### termux commands:

python3 matrix.py

The input parameters for this construction are

Symbol	Value	Description
r1	4	DC
r2	8	DB
r3	6.5	DA
r4	4	DE
$\theta_1$	$17\pi/36$	∠BDC
$\theta_2$	$53\pi/180$	∠ADC
$\theta_3$	$2\pi/3$	∠EDC
D	$\begin{pmatrix} 0 \\ 0 \end{pmatrix}$	Point D

**To Prove:** Ar(ACB)=Ar(ACF)

Area of the triangle  $\Delta ACB$  is given by  $Ar(\Delta ACB) = \frac{1}{2} ||\mathbf{v}\mathbf{1} \times \mathbf{v}\mathbf{2}||.....(2)$ 

Area of the triangle  $\triangle ACF$  is given by  $Ar(\triangle ACF) = \frac{1}{2} ||\mathbf{v}\mathbf{3} \times \mathbf{v}\mathbf{4}||....(3)$ 

**To Prove:** Ar(AEDF)=Ar(ABCDE)

Ar(
$$\triangle$$
AED)=  $\frac{1}{2}$ ||A × E||.....(5)  
Ar( $\triangle$ ADC)=  $\frac{1}{2}$ ||A × C||.....(6)

$$Ar(AEDC)=Ar(\Delta AED)+Ar(\Delta ADC)$$

$$\therefore$$
 Ar(AEDF)=Ar(AEDC)+Ar( $\triangle$ ACF)......(7)

$$\therefore$$
 Ar(ABCDE)=Ar(AEDC)+Ar( $\triangle$ ACB)......(8)

The below python code realizes the above construction:

https://github.com/velicharlagokulkumar/FWC\_module1/tree/main/matrices/lines/codes/matrix.py

# 3 Construction

