# Debt Issuance Impact Factor and the Cross Section of Stock Returns

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#### Abstract

This paper studies the asset pricing implications of Debt Issuance Impact Factor (DIF), and its robustness in predicting returns in the cross-section of equities using the protocol proposed by Novy-Marx and Velikov (2023). A value-weighted long/short trading strategy based on DIF achieves an annualized gross (net) Sharpe ratio of 0.39 (0.28), and monthly average abnormal gross (net) return relative to the Fama and French (2015) five-factor model plus a momentum factor of 16 (13) bps/month with a t-statistic of 2.25 (1.75), respectively. Its gross monthly alpha relative to these six factors plus the six most closely related strategies from the factor zoo (Net debt financing, Change in financial liabilities, Net external financing, Inventory Growth, Cash-based operating profitability, Inventory Growth) is 15 bps/month with a t-statistic of 2.04.

## 1 Introduction

The efficient market hypothesis suggests that asset prices should fully reflect all available information, making it difficult to systematically earn abnormal returns. However, a growing body of literature documents various market anomalies that appear to contradict this notion (Stambaugh and Yuan, 2017). Among these, corporate financing decisions have emerged as particularly powerful predictors of future stock returns (Bradshaw et al., 2006). Despite extensive research on equity issuance and general external financing, the specific role of debt financing decisions in predicting cross-sectional stock returns remains incompletely understood.

While prior work has examined aggregate measures of external financing (Bradshaw et al., 2006) and net debt issuance (Baker and Wurgler, 2003), these broad measures may mask important variations in how different types of debt financing decisions affect future returns. The literature has yet to fully explore how the relative impact of debt issuance on a firm's capital structure - what we term the 'Debt Issuance Impact Factor' (DIF) - influences subsequent stock performance.

We develop our hypothesis based on three key theoretical frameworks. First, the market timing theory of capital structure (Baker and Wurgler, 2002) suggests that managers issue securities when they believe their prices are high relative to fundamental value. This implies that substantial debt issuance may signal management's view that equity is overvalued, predicting lower future returns. Second, agency theory (Jensen and Meckling, 1976) indicates that significant increases in leverage can exacerbate agency conflicts between shareholders and debtholders, potentially leading to suboptimal investment decisions.

Third, the trade-off theory of capital structure (Myers and Majluf, 1984) suggests that firms balance the tax benefits of debt against bankruptcy costs to determine optimal leverage. Significant deviations from optimal leverage through large debt issuances may signal future adjustment costs that the market does not fully appre-

ciate. These theoretical perspectives collectively suggest that the magnitude of debt issuance relative to existing capital structure may contain important information about future stock returns.

Based on these frameworks, we hypothesize that firms with high DIF scores - those whose debt issuance represents a larger proportional impact on their capital structure - will underperform firms with low DIF scores. This relationship should persist after controlling for known risk factors and related anomalies, as it captures a distinct aspect of corporate financing decisions not fully reflected in existing measures.

Our empirical analysis reveals strong support for our hypothesis. A value-weighted long/short trading strategy based on DIF achieves an annualized gross Sharpe ratio of 0.39, with monthly average abnormal returns of 16 basis points relative to the Fama-French five-factor model plus momentum (t-statistic = 2.25). The strategy's performance remains robust after accounting for transaction costs, with a net Sharpe ratio of 0.28.

Importantly, the predictive power of DIF persists among large-cap stocks, with the strategy earning average returns of 25 basis points per month (t-statistic = 2.72) among firms above the 80th percentile of market capitalization. This suggests that the effect is not limited to small, illiquid stocks where trading costs might prohibit implementation.

Further supporting our hypothesis, the DIF strategy generates an alpha of 15 basis points per month (t-statistic = 2.04) even after controlling for six closely related anomalies and the Fama-French six factors. This indicates that DIF captures unique information about future returns not contained in existing measures of external financing or profitability.

Our paper makes several important contributions to the literature on corporate financing decisions and asset pricing. First, we extend the work of (Bradshaw et al., 2006) and (Baker and Wurgler, 2003) by introducing a novel measure that specifically

captures the relative impact of debt issuance on capital structure. While these earlier studies focused on aggregate external financing measures, our DIF metric provides new insights into how the magnitude of debt financing decisions relative to existing capital structure affects future returns.

Second, we contribute to the growing literature on factor investing by documenting a new robust predictor of cross-sectional stock returns. Our findings complement recent work by (Stambaugh and Yuan, 2017) on mispricing factors and (Green et al., 2013) on the characteristics of reliable stock return predictors. The DIF strategy's performance among large-cap stocks and after transaction costs suggests it could be particularly valuable for institutional investors.

Finally, our results have important implications for corporate finance theory and practice. The strong predictive power of DIF supports market timing theories of capital structure and suggests that markets may not fully incorporate the information content of significant changes in leverage. These findings should be of interest to both academics studying market efficiency and practitioners making portfolio allocation decisions.

## 2 Data

Our study investigates the predictive power of a financial signal derived from accounting data for cross-sectional returns, focusing specifically on the Debt Issuance Impact Factor. We obtain accounting and financial data from COMPUSTAT, covering firm-level observations for publicly traded companies. To construct our signal, we use COMPUSTAT's item DLTIS for long-term debt issuance and item AOX for total assets. Long-term debt issuance (DLTIS) represents the cash proceeds from issuance of long-term debt during the fiscal year, while total assets (AOX) provides a comprehensive measure of a firm's size and economic resources. The construction

of the signal follows a difference-in-levels approach scaled by firm size, where we subtract the previous year's DLTIS from the current year's DLTIS and divide this difference by the previous year's total assets (AOX). This scaled difference captures the relative magnitude of changes in debt issuance activity, normalized by firm size to ensure comparability across different-sized firms. By focusing on the year-over-year changes in debt issuance relative to firm size, the signal aims to capture significant shifts in a firm's financing activities that may signal future performance or strategic changes. We construct this measure using end-of-fiscal-year values for both DLTIS and AOX to ensure consistency and comparability across firms and over time.

## 3 Signal diagnostics

Figure 1 plots descriptive statistics for the DIF signal. Panel A plots the time-series of the mean, median, and interquartile range for DIF. On average, the cross-sectional mean (median) DIF is -5.51 (-0.00) over the 1974 to 2023 sample, where the starting date is determined by the availability of the input DIF data. The signal's interquartile range spans -3.89 to 2.70. Panel B of Figure 1 plots the time-series of the coverage of the DIF signal for the CRSP universe. On average, the DIF signal is available for 5.46% of CRSP names, which on average make up 6.67% of total market capitalization.

## 4 Does DIF predict returns?

Table 1 reports the performance of portfolios constructed using a value-weighted, quintile sort on DIF using NYSE breaks. The first two lines of Panel A report monthly average excess returns for each of the five portfolios and for the long/short portfolio that buys the high DIF portfolio and sells the low DIF portfolio. The rest of Panel A reports the portfolios' monthly abnormal returns relative to the five most

common factor models: the CAPM, the Fama and French (1993) three-factor model (FF3) and its variation that adds momentum (FF4), the Fama and French (2015) five-factor model (FF5), and its variation that adds momentum factor used in Fama and French (2018) (FF6). The table shows that the long/short DIF strategy earns an average return of 0.20% per month with a t-statistic of 2.76. The annualized Sharpe ratio of the strategy is 0.39. The alphas range from 0.16% to 0.26% per month and have t-statistics exceeding 2.25 everywhere. The lowest alpha is with respect to the FF6 factor model.

Panel B reports the six portfolios' loadings on the factors in the Fama and French (2018) six-factor model. The long/short strategy's most significant loading is 0.23, with a t-statistic of 4.72 on the CMA factor. Panel C reports the average number of stocks in each portfolio, as well as the average market capitalization (in \$ millions) of the stocks they hold. In an average month, the five portfolios have at least 449 stocks and an average market capitalization of at least \$1,255 million.

Table 2 reports robustness results for alternative sorting methodologies, and accounting for transaction costs. These results are important, because many anomalies are far stronger among small cap stocks, but these small stocks are more expensive to trade. Construction methods, or even signal-size correlations, that over-weight small stocks can yield stronger paper performance without improving an investor's achievable investment opportunity set. Panel A reports gross returns and alphas for the long/short strategies made using various different protfolio constructions. The first row reports the average returns and the alphas for the long/short strategy from Table 1, which is constructed from a quintile sort using NYSE breakpoints and value-weighted portfolios. The rest of the panel shows the equal-weighted returns to this same strategy, and the value-weighted performance of strategies constructed from quintile sorts using name breaks (approximately equal number of firms in each portfolio) and market capitalization breaks (approximately equal total market capit

talization in each portfolio), and using NYSE deciles. The average return is lowest for the quintile sort using name breakpoints and value-weighted portfolios, and equals 18 bps/month with a t-statistics of 2.40. Out of the twenty-five alphas reported in Panel A, the t-statistics for twenty-two exceed two, and for thirteen exceed three.

Panel B reports for these same strategies the average monthly net returns and the generalized net alphas of Novy-Marx and Velikov (2016). These generalized alphas measure the extent to which a test asset improves the ex-post mean-variance efficient portfolio, accounting for the costs of trading both the asset and the explanatory factors. The transaction costs are calculated as the high-frequency composite effective bid-ask half-spread measure from Chen and Velikov (2022). The net average returns reported in the first column range between -8-17bps/month. The lowest return, (-8 bps/month), is achieved from the quintile sort using NYSE breakpoints and equal-weighted portfolios, and has an associated t-statistic of -1.21. Out of the twenty-five construction-methodology-factor-model pairs reported in Panel B, the DIF trading strategy improves the achievable mean-variance efficient frontier spanned by the factor models in twenty cases, and significantly expands the achievable frontier in twelve cases.

Table 3 provides direct tests for the role size plays in the DIF strategy performance. Panel A reports the average returns for the twenty-five portfolios constructed from a conditional double sort on size and DIF, as well as average returns and alphas for long/short trading DIF strategies within each size quintile. Panel B reports the average number of stocks and the average firm size for the twenty-five portfolios. Among the largest stocks (those with market capitalization greater than the 80<sup>th</sup> NYSE percentile), the DIF strategy achieves an average return of 25 bps/month with a t-statistic of 2.72. Among these large cap stocks, the alphas for the DIF strategy relative to the five most common factor models range from 15 to 30 bps/month with t-statistics between 1.61 and 3.22.

## 5 How does DIF perform relative to the zoo?

Figure 2 puts the performance of DIF in context, showing the long/short strategy performance relative to other strategies in the "factor zoo." It shows Sharpe ratio histograms, both for gross and net returns (Panel A and B, respectively), for 212 documented anomalies in the zoo.<sup>1</sup> The vertical red line shows where the Sharpe ratio for the DIF strategy falls in the distribution. The DIF strategy's gross (net) Sharpe ratio of 0.39 (0.28) is greater than 81% (88%) of anomaly Sharpe ratios, respectively.

Figure 3 plots the growth of a \$1 invested in these same 212 anomaly trading strategies (gray lines), and compares those with the growth of a \$1 invested in the DIF strategy (red line).<sup>2</sup> Ignoring trading costs, a \$1 invested in the DIF strategy would have yielded \$2.06 which ranks the DIF strategy in the top 11% across the 212 anomalies. Accounting for trading costs, a \$1 invested in the DIF strategy would have yielded \$1.18 which ranks the DIF strategy in the top 9% across the 212 anomalies.

Figure 4 plots percentile ranks for the 212 anomaly trading strategies in terms of gross and Novy-Marx and Velikov (2016) net generalized alphas with respect to the CAPM, and the Fama-French three-, four-, five-, and six-factor models from Table 1, and indicates the ranking of the DIF relative to those. Panel A shows that the DIF strategy gross alphas fall between the 48 and 63 percentiles across the five factor models. Panel B shows that, accounting for trading costs, a large fraction of anomalies have not improved the investment opportunity set of an investor with access to the factor models over the 197406 to 202306 sample. For example, 45%

 $<sup>^1</sup>$ The anomalies come from March, 2022 release of the Chen and Zimmermann (2022) open source asset pricing dataset.

<sup>&</sup>lt;sup>2</sup>The figure assumes an initial investment of \$1 in T-bills and \$1 long/short in the two sides of the strategy. Returns are compounded each month, assuming, as in Detzel et al. (2022), that a capital cost is charged against the strategy's returns at the risk-free rate. This excess return corresponds more closely to the strategy's economic profitability.

(53%) of the 212 anomalies would not have improved the investment opportunity set for an investor having access to the Fama-French three-factor (six-factor) model. The DIF strategy has a positive net generalized alpha for five out of the five factor models. In these cases DIF ranks between the 65 and 82 percentiles in terms of how much it could have expanded the achievable investment frontier.

#### 6 Does DIF add relative to related anomalies?

With so many anomalies, it is possible that any proposed, new cross-sectional predictor is just capturing some combination of known predictors. It is consequently natural to investigate to what extent the proposed predictor adds additional predictive power beyond the most closely related anomalies. Closely related anomalies are more likely to be formed on the basis of signals with higher absolute correlations. Figure 5 plots a name histogram of the correlations of DIF with 209 filtered anomaly signals.<sup>3</sup> Figure 6 also shows an agglomerative hierarchical cluster plot using Ward's minimum method and a maximum of 10 clusters.

A closely related anomaly is also more likely to price DIF or at least to weaken the power DIF has predicting the cross-section of returns. Figure 7 plots histograms of t-statistics for predictability tests of DIF conditioning on each of the 209 filtered anomaly signals one at a time. Panel A reports t-statistics on  $\beta_{DIF}$  from Fama-MacBeth regressions of the form  $r_{i,t} = \alpha + \beta_{DIF}DIF_{i,t} + \beta_X X_{i,t} + \epsilon_{i,t}$ , where Xstands for one of the 209 filtered anomaly signals at a time. Panel B plots t-statistics on  $\alpha$  from spanning tests of the form:  $r_{DIF,t} = \alpha + \beta r_{X,t} + \epsilon_t$ , where  $r_{X,t}$  stands for the returns to one of the 209 filtered anomaly trading strategies at a time. The strategies employed in the spanning tests are constructed using quintile sorts, value-

<sup>&</sup>lt;sup>3</sup>When performing tests at the underlying signal level (e.g., the correlations plotted in Figure 5), we filter the 212 anomalies to avoid small sample issues. For each anomaly, we calculate the common stock observations in an average month for which both the anomaly and the test signal are available. In the filtered anomaly set, we drop anomalies with fewer than 100 common stock observations in an average month.

weighting, and NYSE breakpoints. Panel C plots t-statistics on the average returns to strategies constructed by conditional double sorts. In each month, we sort stocks into quintiles based one of the 209 filtered anomaly signals. Then, within each quintile, we sort stocks into quintiles based on DIF. Stocks are finally grouped into five DIF portfolios by combining stocks within each anomaly sorting portfolio. The panel plots the t-statistics on the average returns of these conditional double-sorted DIF trading strategies conditioned on each of the 209 filtered anomalies.

Table 4 reports Fama-MacBeth cross-sectional regressions of returns on DIF and the six anomalies most closely-related to it. The six most-closely related anomalies are picked as those with the highest combined rank where the ranks are based on the absolute value of the Spearman correlations in Panel B of Figure 5 and the  $R^2$  from the spanning tests in Figure 7, Panel B. Controlling for each of these signals at a time, the t-statistics on the DIF signal in these Fama-MacBeth regressions exceed 1.01, with the minimum t-statistic occurring when controlling for Net debt financing. Controlling for all six closely related anomalies, the t-statistic on DIF is -0.10.

Similarly, Table 5 reports results from spanning tests that regress returns to the DIF strategy onto the returns of the six most closely-related anomalies and the six Fama-French factors. Controlling for the six most-closely related anomalies individually, the DIF strategy earns alphas that range from 16-17bps/month. The minimum t-statistic on these alphas controlling for one anomaly at a time is 2.13, which is achieved when controlling for Net debt financing. Controlling for all six closely-related anomalies and the six Fama-French factors simultaneously, the DIF trading strategy achieves an alpha of 15bps/month with a t-statistic of 2.04.

#### 7 Does DIF add relative to the whole zoo?

Finally, we can ask how much adding DIF to the entire factor zoo could improve investment performance. Figure 8 plots the growth of \$1 invested in trading strategies that combine multiple anomalies following Chen and Velikov (2022). The combinations use either the 156 anomalies from the zoo that satisfy our inclusion criteria (blue lines) or these 156 anomalies augmented with the DIF signal.<sup>4</sup> We consider one different methods for combining signals.

Panel A shows results using "Average rank" as the combination method. This method sorts stocks on the basis of forecast excess returns, where these are calculated on the basis of their average cross-sectional percentile rank across return predictors, and the predictors are all signed so that higher ranks are associated with higher average returns. For this method, \$1 investment in the 156-anomaly combination strategy grows to \$935.00, while \$1 investment in the combination strategy that includes DIF grows to \$1005.20.

#### 8 Conclusion

This study provides compelling evidence for the predictive power of the Debt Issuance Impact Factor (DIF) in explaining cross-sectional stock returns. Our findings demonstrate that a value-weighted long/short strategy based on DIF generates economically and statistically significant returns, with an annualized gross Sharpe ratio of 0.39 (0.28 net of transaction costs). The strategy's robustness is particularly noteworthy, maintaining significant abnormal returns even after controlling for established factors and related anomalies.

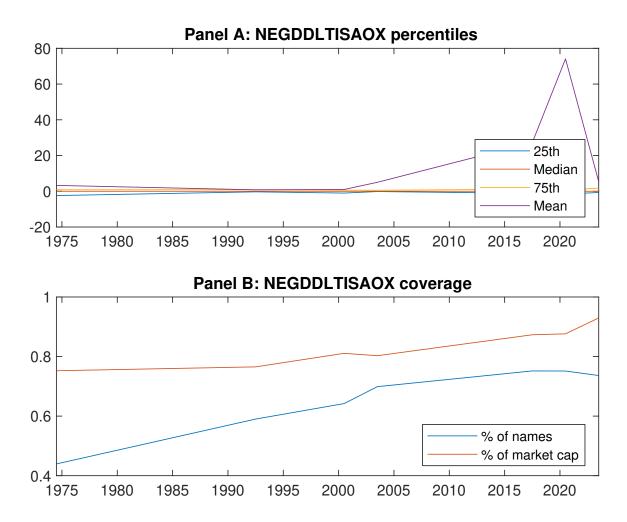
The persistence of DIF's predictive power, evidenced by monthly abnormal re-

<sup>&</sup>lt;sup>4</sup>We filter the 207 Chen and Zimmermann (2022) anomalies and require for each anomaly the average month to have at least 40% of the cross-sectional observations available for market capitalization on CRSP in the period for which DIF is available.

turns of 16 basis points (gross) and 13 basis points (net) relative to the Fama-French five-factor model plus momentum, suggests that this signal captures unique information about firm value not fully reflected in existing factor models. Furthermore, the signal's ability to generate a significant alpha of 15 basis points monthly, even when controlling for six closely related strategies, underscores its distinctive contribution to the asset pricing literature.

However, several limitations warrant consideration. The study's findings may be sensitive to the specific time period examined, and the signal's effectiveness could vary across different market conditions or economic cycles. Future research could explore the signal's performance in international markets, its interaction with other established anomalies, and its underlying economic mechanisms. Additionally, investigating the signal's behavior during various market regimes and its potential application in different investment strategies could provide valuable insights for both academics and practitioners.

In conclusion, while DIF demonstrates promising results as a return predictor, further investigation into its practical implementation challenges, scalability, and economic drivers would enhance our understanding of its role in asset pricing and portfolio management.



**Figure 1:** Times series of DIF percentiles and coverage. This figure plots descriptive statistics for DIF. Panel A shows cross-sectional percentiles of DIF over the sample. Panel B plots the monthly coverage of DIF relative to the universe of CRSP stocks with available market capitalizations.

Table 1: Basic sort: VW, quintile, NYSE-breaks

This table reports average excess returns and alphas for portfolios sorted on DIF. At the end of each month, we sort stocks into five portfolios based on their signal using NYSE breakpoints. Panel A reports average value-weighted quintile portfolio (L,2,3,4,H) returns in excess of the risk-free rate, the long-short extreme quintile portfolio (H-L) return, and alphas with respect to the CAPM, Fama and French (1993) three-factor model, Fama and French (1993) three-factor model augmented with the Carhart (1997) momentum factor, Fama and French (2015) five-factor model, and the Fama and French (2015) five-factor model augmented with the Carhart (1997) momentum factor following Fama and French (2018). Panel B reports the factor loadings for the quintile portfolios and long-short extreme quintile portfolio in the Fama and French (2015) five-factor model. Panel C reports the average number of stocks and market capitalization of each portfolio. T-statistics are in brackets. The sample period is 197406 to 202306.

Panel A: Ex	cess returns	and alphas of	on DIF-sorted	l portfolios		
	(L)	(2)	(3)	(4)	(H)	(H-L)
$r^e$	0.68 [3.12]	$0.65 \\ [3.47]$	$0.73 \\ [3.57]$	$0.77 \\ [4.05]$	0.87 [4.25]	$0.20 \\ [2.76]$
$\alpha_{CAPM}$	-0.08 [-1.49]	-0.00 [-0.05]	$0.02 \\ [0.38]$	0.11 [2.20]	0.16 [2.83]	0.24 [3.39]
$\alpha_{FF3}$	-0.08 [-1.50]	-0.01 [-0.26]	0.08 [1.42]	0.11 [2.33]	0.18 [3.19]	0.26 [3.56]
$\alpha_{FF4}$	-0.06 [-1.12]	-0.01 [-0.20]	0.13 [2.38]	0.08 [1.73]	0.16 [2.86]	0.22 [3.03]
$lpha_{FF5}$	-0.08 [-1.44]	-0.10 [-2.28]	0.12 [2.04]	0.03 [0.58]	0.10 [1.89]	0.18 [2.51]
$\alpha_{FF6}$	-0.06 [-1.19]	-0.09 [-2.03]	0.15 [2.68]	0.02 [0.32]	0.10 [1.80]	0.16 [2.25]
Panel B: Fa	ma and Fren	nch (2018) 6-1	factor model	loadings for l	DIF-sorted po	ortfolios
$\beta_{ ext{MKT}}$	1.07 [86.10]	1.01 [95.43]	1.00 [77.31]	$1.00 \\ [89.35]$	1.03 [80.57]	-0.04 [-2.09]
$\beta_{ m SMB}$	$0.15 \\ [7.91]$	-0.08 [-5.04]	-0.02 [-0.77]	-0.03 [-1.46]	0.14 [7.29]	-0.01 [-0.28]
$eta_{ m HML}$	-0.02 [-0.95]	$0.00 \\ [0.05]$	-0.14 [-5.80]	-0.08 [-3.70]	-0.14 [-5.88]	-0.12 [-3.78]
$\beta_{\mathrm{RMW}}$	0.07 [2.78]	0.16 [7.78]	-0.01 [-0.54]	0.10 [4.33]	0.10 [3.93]	$0.03 \\ [0.95]$
$\beta_{\mathrm{CMA}}$	-0.10 [-2.66]	0.12 [3.95]	-0.08 [-2.09]	0.18 [5.58]	0.13 [3.62]	$0.23 \\ [4.72]$
$\beta_{\mathrm{UMD}}$	-0.02 [-1.85]	-0.02 [-1.72]	-0.06 [-4.71]	0.02 [1.93]	0.01 [0.58]	0.03 [1.81]
Panel C: Av	verage numb	er of firms (n	and market	capitalizatio	on (me)	
n	627	449	910	488	606	
me $(\$10^6)$	1339	2665	2004	2754	1255	

Table 2: Robustness to sorting methodology & trading costs

This table evaluates the robustness of the choices made in the DIF strategy construction methodology. In each panel, the first row shows results from a quintile, value-weighted sort using NYSE break points as employed in Table 1. Each of the subsequent rows deviates in one of the three choices at a time, and the choices are specified in the first three columns. For each strategy construction methodology, the table reports average excess returns and alphas with respect to the CAPM, Fama and French (1993) three-factor model, Fama and French (1993) three-factor model augmented with the Carhart (1997) momentum factor, Fama and French (2015) five-factor model, and the Fama and French (2015) five-factor model augmented with the Carhart (1997) momentum factor following Fama and French (2018). Panel A reports average returns and alphas with no adjustment for trading costs. Panel B reports net average returns and Novy-Marx and Velikov (2016) generalized alphas as prescribed by Detzel et al. (2022). T-statistics are in brackets. The sample period is 197406 to 202306.

Panel A: Gross Returns and Alphas											
Portfolios	Breaks	Weights	$r^e$	$\alpha_{\mathrm{CAPM}}$	$lpha_{ ext{FF3}}$	$lpha_{ ext{FF4}}$	$lpha_{ ext{FF}5}$	$lpha_{ ext{FF}6}$			
Quintile	NYSE	VW	$0.20 \\ [2.76]$	0.24 [3.39]	$0.26 \\ [3.56]$	$0.22 \\ [3.03]$	0.18 [2.51]	0.16 [2.25]			
Quintile	NYSE	EW	0.18 [4.01]	$0.20 \\ [4.45]$	$0.20 \\ [4.27]$	$0.17 \\ [3.75]$	0.18 [3.89]	0.17 [3.60]			
Quintile	Name	VW	0.18 [2.40]	$0.22 \\ [3.02]$	0.23 [3.13]	$0.20 \\ [2.67]$	0.14 [1.86]	$0.13 \\ [1.67]$			
Quintile	Cap	VW	$0.19 \\ [3.00]$	$0.23 \\ [3.57]$	0.23 [3.58]	0.18 [2.72]	0.15  [2.34]	0.12 [1.84]			
Decile	NYSE	VW	0.24 [2.70]	0.26 [2.82]	0.28 [3.04]	$0.23 \\ [2.53]$	$0.23 \\ [2.47]$	$0.20 \\ [2.17]$			
Panel B: N	et Return	ns and Nov	y-Marx a	and Velikov	v (2016) g	generalized	l alphas				
Portfolios	Breaks	Weights	$r_{net}^e$	$\alpha^*_{\mathrm{CAPM}}$	$lpha^*_{ ext{FF3}}$	$lpha^*_{\mathrm{FF4}}$	$lpha^*_{ ext{FF5}}$	$lpha^*_{ ext{FF}6}$			
Quintile	NYSE	VW	0.14 [1.94]	$0.20 \\ [2.70]$	0.21 [2.83]	0.19 [2.58]	$0.14 \\ [1.94]$	$0.13 \\ [1.75]$			
Quintile	NYSE	EW	-0.08 [-1.21]								
Quintile	Name	VW	$0.12 \\ [1.57]$	0.17 [2.33]	0.18 [2.41]	0.16 [2.19]	$0.10 \\ [1.32]$	$0.09 \\ [1.17]$			
Quintile	Cap	VW	0.14 [2.19]	0.19 [2.94]	0.19 [2.93]	0.16 [2.49]	0.12 [1.86]	$0.10 \\ [1.55]$			
Decile	NYSE	VW	0.17 [1.90]	0.19 [2.07]	0.21 [2.23]	0.18 [1.96]	0.16 [1.73]	0.15 [1.53]			

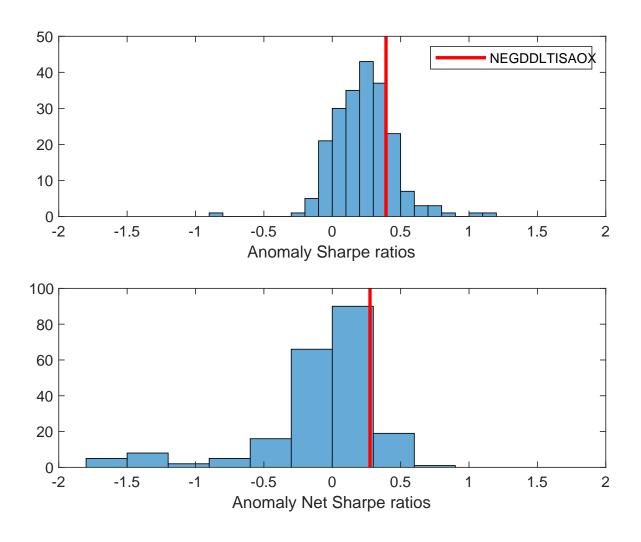
Table 3: Conditional sort on size and DIF

This table presents results for conditional double sorts on size and DIF. In each month, stocks are first sorted into quintiles based on size using NYSE breakpoints. Then, within each size quintile, stocks are further sorted based on DIF. Finally, they are grouped into twenty-five portfolios based on the intersection of the two sorts. Panel A presents the average returns to the 25 portfolios, as well as strategies that go long stocks with high DIF and short stocks with low DIF. Panel B documents the average number of firms and the average firm size for each portfolio. The sample period is 197406 to 202306.

Pan	Panel A: portfolio average returns and time-series regression results											
			D	IF Quintil	es				DIF St	rategies		
		(L)	(2)	(3)	(4)	(H)	$r^e$	$\alpha_{CAPM}$	$\alpha_{FF3}$	$\alpha_{FF4}$	$\alpha_{FF5}$	$\alpha_{FF6}$
	(1)	0.75 [2.59]	0.88 [3.14]	1.02 [3.60]	1.01 [3.31]	0.83 [2.92]	0.09 [1.04]	0.11 [1.27]	0.09 [1.08]	0.06 [0.69]	0.07 [0.79]	$0.05 \\ [0.55]$
iles	(2)	0.80 [2.94]	$0.94 \\ [3.56]$	$0.85 \\ [3.29]$	1.00 [3.88]	0.89 [3.40]	$0.09 \\ [1.03]$	$0.11 \\ [1.37]$	$0.09 \\ [1.09]$	0.11 [1.33]	$0.08 \\ [0.90]$	$0.09 \\ [1.09]$
quintiles	(3)	0.81 [3.11]	$0.90 \\ [3.80]$	$0.92 \\ [3.67]$	0.91 [3.93]	0.96 [3.91]	$0.15 \\ [1.85]$	$0.20 \\ [2.44]$	0.20 [2.39]	0.16 [1.87]	0.18 [2.13]	$0.15 \\ [1.79]$
Size	(4)	$0.80 \\ [3.36]$	$0.83 \\ [3.65]$	0.94 [4.09]	0.84 [3.76]	0.90 [3.87]	$0.09 \\ [1.12]$	$0.12 \\ [1.39]$	0.11  [1.27]	$0.07 \\ [0.85]$	0.10 [1.13]	$0.07 \\ [0.84]$
	(5)	$0.60 \\ [2.95]$	$0.62 \\ [3.31]$	0.66 [3.23]	$0.69 \\ [3.60]$	0.86 [4.35]	$0.25 \\ [2.72]$	$0.29 \\ [3.16]$	$0.30 \\ [3.22]$	0.23 [2.46]	0.19 [2.04]	$0.15 \\ [1.61]$

Panel B: Portfolio average number of firms and market capitalization

DIF Quintiles								DIF Quintiles						
	Average $n$							Average market capitalization $(\$10^6)$						
		(L)	(2)	(3)	(4)	(H)		(L)	(2)	(3)	(4)	(H)		
es	(1)	343	344	344	344	340		32	29	28	29	30		
ntil	(2)	96	97	97	97	96		53	55	52	54	54		
quintil	(3)	68	68	68	68	68		94	96	92	93	95		
Size	(4)	56	57	57	57	56		206	212	207	212	204		
$\infty$	(5)	52	52	52	52	52		1301	1918	1572	2033	1267		



**Figure 2:** Distribution of Sharpe ratios. This figure plots a histogram of Sharpe ratios for 212 anomalies, and compares the Sharpe ratio of the DIF with them (red vertical line). Panel A plots results for gross Sharpe ratios. Panel B plots results for net Sharpe ratios.

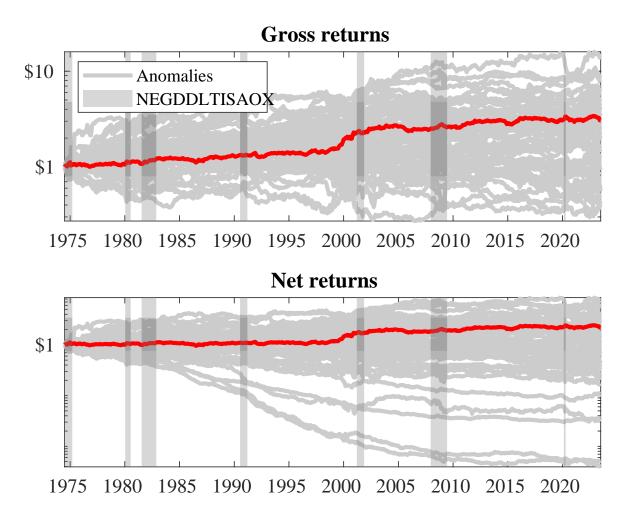
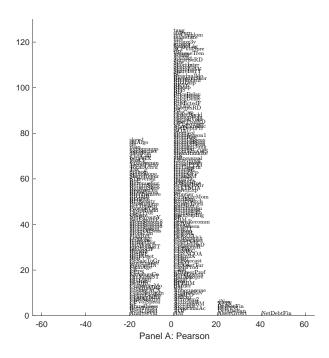
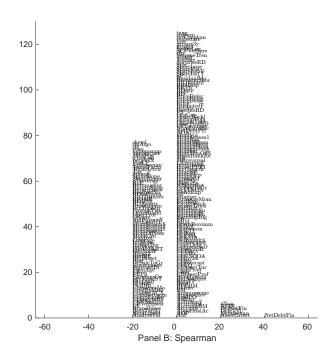


Figure 3: Dollar invested.

This figure plots the growth of a \$1 invested in 212 anomaly trading strategies (gray lines), and compares those with the DIF trading strategy (red line). The strategies are constructed using value-weighted quintile sorts using NYSE breakpoints. Panel A plots results for gross strategy returns. Panel B plots results for net strategy returns.

Figure 4: Gross and generalized net alpha percentiles of anomalies relative to factor models. This figure plots the percentile ranks for 212 anomaly trading strategies in terms of alphas (solid lines), and compares those with the DIF trading strategy alphas (diamonds). The strategies are constructed using value-weighted quintile sorts using NYSE breakpoints. The alphas include those with respect to the CAPM, Fama and French (1993) three-factor model, Fama and French (1993) three-factor model augmented with the Carhart (1997) momentum factor, Fama and French (2015) five-factor model, and the Fama and French (2015) five-factor model augmented with the Carhart (1997) momentum factor following Fama and French (2018). The left panel plots alphas with no adjustment for trading costs. The right panel plots Novy-Marx and Velikov (2016) net generalized alphas.





**Figure 5:** Distribution of correlations.

This figure plots a name histogram of correlations of 209 filtered anomaly signals with DIF. The correlations are pooled. Panel A plots Pearson correlations, while Panel B plots Spearman rank correlations.

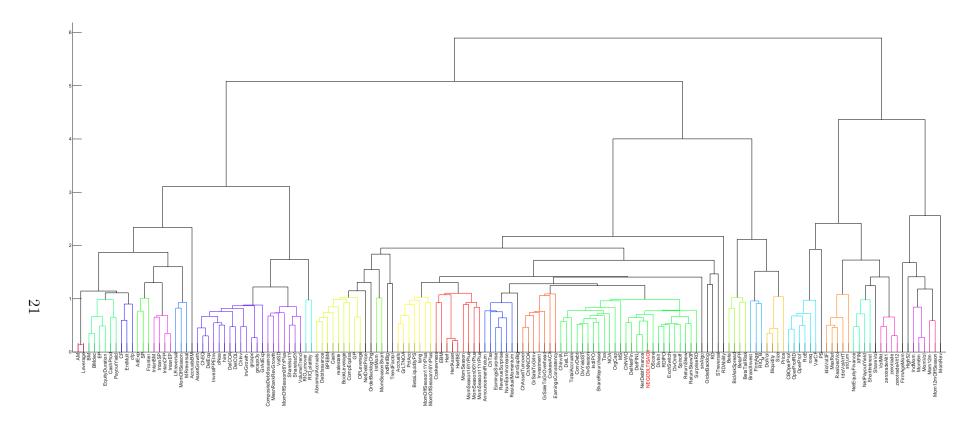
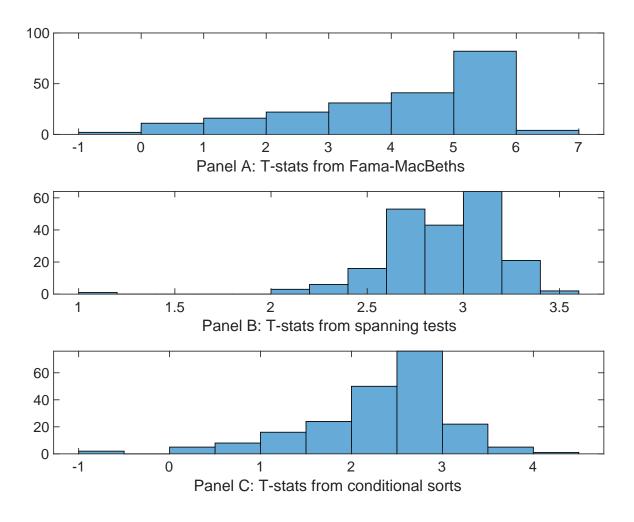


Figure 6: Agglomerative hierarchical cluster plot This figure plots an agglomerative hierarchical cluster plot using Ward's minimum method and a maximum of 10 clusters.



**Figure 7:** Distribution of t-stats on conditioning strategies

This figure plots histograms of t-statistics for predictability tests of DIF conditioning on each of the 209 filtered anomaly signals one at a time. Panel A reports t-statistics on  $\beta_{DIF}$  from Fama-MacBeth regressions of the form  $r_{i,t} = \alpha + \beta_{DIF}DIF_{i,t} + \beta_X X_{i,t} + \epsilon_{i,t}$ , where X stands for one of the 209 filtered anomaly signals at a time. Panel B plots t-statistics on  $\alpha$  from spanning tests of the form:  $r_{DIF,t} = \alpha + \beta r_{X,t} + \epsilon_t$ , where  $r_{X,t}$  stands for the returns to one of the 209 filtered anomaly trading strategies at a time. The strategies employed in the spanning tests are constructed using quintile sorts, value-weighting, and NYSE breakpoints. Panel C plots t-statistics on the average returns to strategies constructed by conditional double sorts. In each month, we sort stocks into quintiles based one of the 209 filtered anomaly signals at a time. Then, within each quintile, we sort stocks into quintiles based on DIF. Stocks are finally grouped into five DIF portfolios by combining stocks within each anomaly sorting portfolio. The panel plots the t-statistics on the average returns of these conditional double-sorted DIF trading strategies conditioned on each of the 209 filtered anomalies.

Table 4: Fama-MacBeths controlling for most closely related anomalies This table presents Fama-MacBeth results of returns on DIF. and the six most closely related anomalies. The regressions take the following form:  $r_{i,t} = \alpha + \beta_{DIF}DIF_{i,t} + \sum_{k=1}^{s} ix\beta_{X_k}X_{i,t}^k + \epsilon_{i,t}$ . The six most closely related anomalies, X, are Net debt financing, Change in financial liabilities, Net external financing, Inventory Growth, Cash-based operating profitability, Inventory Growth. These anomalies were picked as those with the highest combined rank where the ranks are based on the absolute value of the Spearman correlations in Panel B of Figure 5 and the  $R^2$  from the spanning tests in Figure 7, Panel B. The sample period is 197406 to 202306.

Intercept	0.14 [5.44]	0.14 [5.46]	0.14 [5.78]	0.14 [5.46]	0.12 [4.39]	0.14 [5.44]	0.14 [5.11]
DIF	0.58 [1.01]	0.81 [1.44]	0.11 [1.73]	0.23 [3.66]	0.26 [4.61]	0.27 [4.78]	-0.68 [-0.10]
Anomaly 1	0.21 [9.35]	L J	L J	. ,		. ,	0.66 [1.16]
Anomaly 2		0.17 [8.89]					0.16 [0.39]
Anomaly 3			$0.20 \\ [6.58]$				0.13 [2.97]
Anomaly 4				0.41 [7.06]			0.12 [1.85]
Anomaly 5					0.15  [4.19]		0.55 [1.38]
Anomaly 6					L J	0.33 [5.68]	0.16 [1.85]
# months	588	588	588	588	583	588	583
$\bar{R}^2(\%)$	0	0	1	0	1	0	0

Table 5: Spanning tests controlling for most closely related anomalies This table presents spanning tests results of regressing returns to the DIF trading strategy on trading strategies exploiting the six most closely related anomalies. The regressions take the following form:  $r_t^{DIF} = \alpha + \sum_{k=1}^6 \beta_{X_k} r_t^{X_k} + \sum_{j=1}^6 \beta_{f_j} r_t^{f_j} + \epsilon_t$ , where  $X_k$  indicates each of the six most-closely related anomalies and  $f_j$  indicates the six factors from the Fama and French (2015) five-factor model augmented with the Carhart (1997) momentum factor. The six most closely related anomalies, X, are Net debt financing, Change in financial liabilities, Net external financing, Inventory Growth, Cash-based operating profitability, Inventory Growth. These anomalies were picked as those with the highest combined rank where the ranks are based on the absolute value of the Spearman correlations in Panel B of Figure 5 and the  $R^2$  from the spanning tests in Figure 7, Panel B. The sample period is 197406 to 202306.

Intercept	0.16	0.16	0.16	0.17	0.17	0.16	0.15
	[2.17]	[2.19]	[2.22]	[2.36]	[2.29]	[2.13]	[2.04]
Anomaly 1	18.94						16.17
	[4.66]						[2.86]
Anomaly 2		14.28					-0.42
		[3.34]					[-0.07]
Anomaly 3			8.55				1.97
			[2.30]				[0.47]
Anomaly 4				9.41			5.43
· ·				[3.28]			[1.54]
Anomaly 5					7.33		5.27
J					[2.13]		[1.44]
Anomaly 6						7.71	4.90
<i>j</i>						[2.05]	[1.06]
$\operatorname{mkt}$	-3.96	-3.79	-2.80	-4.21	-3.66	-3.78	-3.58
22220	[-2.40]	[-2.27]	[-1.60]	[-2.52]	[-2.16]	[-2.25]	[-2.06]
$\operatorname{smb}$	-2.17	-2.18	1.84	0.05	0.84	-0.04	1.06
	[-0.85]	[-0.84]	[0.65]	[0.02]	[0.30]	[-0.02]	[0.36]
hml	-12.19	-11.72	-11.48	-12.79	-10.71	-12.88	-11.28
111111	[-3.84]	[-3.65]	[-3.54]	[-3.99]	[-3.15]	[-3.99]	[-3.36]
rmw	2.52	2.97	-1.06	5.36	0.36	5.39	0.50
TITIVV	[0.76]	[0.89]	[-0.26]	[1.60]	[0.10]	[1.58]	[0.12]
cma	17.72	17.81	16.84	14.20	20.00	17.33	6.88
Cilia	[3.61]	[3.53]	[3.08]	[2.59]	[4.06]	[3.15]	[1.12]
umd	1.46	1.63	2.97	2.15	2.23	2.63	0.43
umd	[0.86]	[0.94]	[1.76]	[1.26]	[1.31]	[1.54]	[0.45]
// 41							
# months	588	588	588	588	584	588	584
$\bar{R}^{2}(\%)$	11	9	8	9	8	8	11

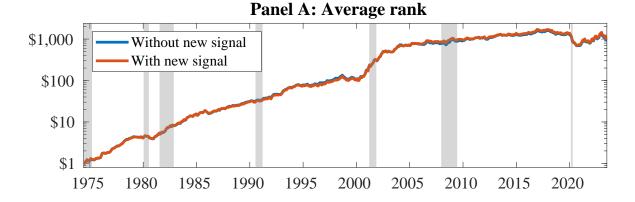


Figure 8: Combination strategy performance

This figure plots the growth of a \$1 invested in trading strategies that combine multiple anomalies following Chen and Velikov (2022). In all panels, the blue solid lines indicate combination trading strategies that utilize 156 anomalies. The red solid lines indicate combination trading strategies that utilize the 156 anomalies as well as DIF. Panel A shows results using "Average rank" as the combination method. See Section 7 for details on the combination methods.

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