



UNIVERSIDADE ESTADUAL DE CAMPINAS
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OTIMIZAÇÃO ONLINE DA ABERTURA DINÂMICA DO SIRIUS

ONLINE OPTIMIZATION OF SIRIUS DYNAMIC APERTURE

CAMPINAS
2023

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Dissertação apresentada ao Instituto de Física Gleb Wataghin da Universidade Estadual de Campinas como parte dos requisitos exigidos para a obtenção do título de MESTRE EM FÍSICA, na Área de FÍSICA.

Thesis presented to the Gleb Wataghin Institute of Physics of the University of Campinas in partial fulfillment of the requirements for the degree of MASTER IN PHYSICS, in the area of PHYSICS.

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ESTE TRABALHO CORRESPONDE À VERSÃO FINAL DA TESE DEFENDIDA PELO ALUNO MATHEUS MELO SANTOS VELLOSO E ORIENTADA PELO PROF. DR. LIU LIN.

CAMPINAS

2023

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FOLHA DA APROVAÇÃO

Acknowledgements

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Abstract

Beam accumulation into the SIRIUS storage ring occurs in the off-axis scheme, for which the efficiency depends on a sufficiently large dynamic aperture (DA) - the region comprising stable transverse oscillations. In the design phase, SIRIUS DA was numerically optimized in the accelerator model using various techniques and during commissioning the optimized lattice was implemented in the machine. Recent measurements indicate that SIRIUS DA, although sufficiently large for an injection efficiency of around 85%, can be yet increased upon fine-tuning of sextupole magnets strengths, which govern the beam nonlinear dynamics and determine the DA. In this master's project, the student will carry out online optimization experiments to tune the ring nonlinear lattice and improve the DA and injection efficiency into the storage ring.

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CHAPTER 1

Introduction

This dissertation concerns the work performed on the SIRIUS storage ring sextupole magnets with the objective to optimize the ring's Dynamic Aperture (DA) and injection efficiency. The text is organized as follows:

- The present chapter introduces synchrotron light sources, the SIRIUS project, the main components and subsystems found in electron storage rings and the problem addressed during the execution of the student's masters project;
- Chapter 2 introduces the theoretical and scientific background on the dynamics of particles in accelerators. The optics functions, the tunes, chromatic effects, field errors and perturbations and the dynamic aperture are discussed;
- Chapter 3 introduces and justifies online optimization of nonlinear dynamics in accelerators and presents the Robust Conjugate Direction Search (RCDS) algorithm;
- Chapter 4 describes the experimental methods and setup for the online optimization experiments and the results achieved;
- Chapter 5 concludes this dissertation presenting the final remarks.

1.1 Storage ring-based synchrotron light sources

Synchrotron radiation (SR) is the electromagnetic radiation emitted by charged relativistic particles when accelerated perpendicularly to their motion. The phenomenon was theoretically predicted in the early 1900s when Liénard and Wiechert calculated the retarded potentials for point particles. The first experimental observation occurred at General Electric's synchrotron accelerator, justifying the adoption of the term "synchrotron" in its name [3].

Synchrotron light is extremely colimated and has a broad spectral distribution, covering from infrared to hard X-rays. These properties make synchrotron light ideal for imaging experiments in crystallography and spectroscopy in a wide variety of scientific disciplines.

Modern synchrotron light sources primarily rely on two particle acceleration technologies: free-electron lasers and electron storage rings. Here, we focus on storage ring-based synchrotron light source facilities. In these facilities, ultra-relativistic electron beams are stored for extended periods within a chamber in ultra-high vacuum to produce synchrotron light. The beams are maintained in stable orbits by the fields of an array of magnets which provide both bending and focusing of the trajectories. The beam is also periodically influenced by radiofrequency cavities, which replenish the energy radiated away in the form of light.

The main figure of merit for the quality of a SR source is the *brightness* [4], defined as the photon flux in six-dimensional phase space [5]:

$$B(\omega) = \frac{1}{\Delta\omega/\omega} \frac{F(\omega)}{\Sigma_x(\omega)\Sigma_y(\omega)}, \quad (1.1)$$

where $F(\omega)$ is the photon flux at energy $E = \hbar\omega$, Σ_u is the photon beam volume in the $u = x, y$ phase space, and $\Delta\omega/\omega$ is the frequency bandwidth, which is typically about 0.1%. The photon phase space volume depends on the convolution of the electron beam distribution with the distribution of the photons emitted by a single electron. The latter depends on the photon energy and the emission process, while the former is related to the average phase space volume of the electron beam: the *emittance*, which depends on the magnetic lattice and has units of the transverse phase space areas (length times angle). Increasing brightness depends on maximizing the photon flux, reducing the electron beam emittances and optimizing the matching between photon and electron beams for maximizing their distributions convolution [3].

Synchrotron light sources can be classified based on their brightness/emittance. In the early 1960s, the community interested in SR for imaging experiments obtained SR parasitically from high-energy and nuclear physics machines such as DESY and DORIS in Germany and ADA in Italy [6], marking the era of first-generation synchrotron light sources [7]. The second-generation machines emerged in the 1980s and consisted on machines designed exclusively for SR production, such as BESSY, DORIS II and III, ELSA in Germany, SUPERACO in France, MAX I in Sweden [6] and UVX in Brazil.

The 1990s saw a growing demand for higher brightness, leading to the development of third-generation machines [7]. These machines introduced insertion devices such as wigglers and undulators, significantly enhancing brightness by increasing radiative damping. Additionally, these devices allowed precise control over radiation energy and polarization. Typical emittances for third-generation machines is of the order of units to tens of nm rad. Most of currently operating machines pertain to the third-generation, such as ALBA in Spain, ESRF and SOLEIL in France, Diamond in the United Kingdom and ELETTRA, in Italy [6].

The era of the fourth-generation of storage rings (4GSR) commenced with the

commissioning of the MAX-IV machine in Lund, Sweden, in 2015 [5, 7]. Fourth-generation machines achieved a notable reduction in emittance, reaching sub-nm rad values thanks to recent technological advancements in computer simulations, vacuum technology, machining and mechanical alignment [5, 7]. Following MAX-IV, an upgrade of the ESRF facility, the ESRF-EBS, and the launch of SIRIUS in Campinas marked significant milestones for the fourth-generation. Today, several 4GSR projects are being planned, designed and constructed.

1.2 The SIRIUS project

SIRIUS is a 4GSR synchrotron light source. It was designed, built, and is operated by the Brazilian Synchrotron Light Laboratory (LNLS), on the campus of the Center of Research in Energy and Materials (CNPEM), in Campinas, Brazil. The storage ring operating energy is 3 GeV, and the ring has 518 m in circumference. The natural emittance of the lattice is 250 pm rad and it is expected to reach 150 pm rad with the installation of its definitive insertion devices [8]¹.

SIRIUS succeeded the first synchrotron light source in Brazil, the UVX machine, which opened to users in 1997 and served the community until its shutdown, in the beginning of SIRIUS commissioning, in August 2019² [8]. The project started in 2009, initially planned and designed as a third-generation machine. By 2012, it evolved into the project of a fourth-generation machine [8]. Construction was finished in 2018, the LINAC and Booster commissioning soon followed. In November 2019 the first beam was stored in the storage ring.

Check these statements. Get more info about main milestones

SIRIUS finished its Phase-0 commissioning in 2022 and since March 2023 is receiving its first external users. At the time of this writing, it has 6 operating beamlines, 4 beamlines in commissioning and 4 under construction and installation. It is currently storing 100 mA current, with frequent beam injections throughout the day, a scheme known as “top-up” mode. SIRIUS is expected to achieve 350 mA current when the system of two superconducting radiofrequency cavities is installed [9, 10].

more info on the phases. which phase are we in?

Presently, SIRIUS stands as the most complex scientific infrastructure ever constructed in Brazil, with the ambitious goal of positioning the country at the forefront of global leadership in synchrotron light sources. This state-of-the-art synchrotron was

¹SIRIUS is currently operating with provisional insertion devices for providing light to the first users and allowing scientific commissioning of the beamlines

²The UVX project led to the creation of LNLS, which marked a new model for scientific research in Brazil, based on social organizations under contracts with the Ministry of Science Technology and Innovations. LNLS paved the way for national labs (NL), including labs on biosciences (LNBio), nanotechnology (LNNano), and bio-renewables (LNBR), which are also located at the CNPEM campus.



Figure 1.1: Schematic view of the SIRIUS installations. 1) Linear accelerator (LINAC); 2) Concrete tunnel housing the booster accelerator and the storage ring; 3) storage ring; 4) beamlines. From [LNLS website](#).

meticulously designed to shine as the brightest in its energy category, and has the capacity to host up to 40 beamlines. As of the time of this writing, SIRIUS holds the distinction of being the sole fourth-generation synchrotron light source in the southern hemisphere and one of merely three 4GSRs in operation across the globe (still true?).

1.3 Subsystems and components of a storage ring-based light source facility

Typical systems comprising a storage ring synchrotron light source facility include:

- an injection system: including the electrons source, beam transport lines, the linear accelerator and the booster circular accelerator. At SIRIUS, the linear accelerator provides the booster ring with a 150 MeV beam. The booster further ramps the beam energy up to 3 GeV, which is the storage ring operation energy;
- storage ring: where the ultra-relativistic beam of electrons is kept in stable orbits for hours within the vacuum-chamber, producing synchrotron light at the bending magnets and insertion devices;
- beamlines which steer the photon beams towards the experimental cabins where samples are placed for the experiments based on light-matter interaction, such as spectroscopy, crystallography, tomography and others.

A schematic view of the SIRIUS building is shown in Fig. 1.1.

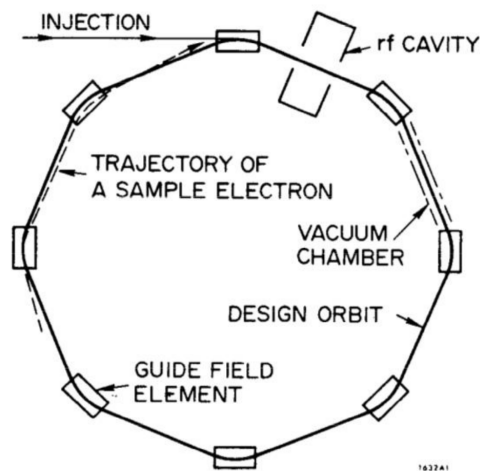


Figure 1.2: Storage ring typical configuration. From [?]

Storage ring magnets and RF cavity

draw my own figure

Figure 1.2 sketches the typical layout of a synchrotron accelerator. The electron beam is stored within a vacuum chamber, oscillating in proximity to a reference design closed orbit under the influence of an array of magnets. The orbit is determined by the strengths of the deflection magnets, the dipoles, and the operation energy of the beams. A pure dipole magnet provides a uniform and homogeneous magnetic field perpendicular to the facility floor and bends the electron's trajectory in the direction parallel to the floor. For the trajectories resulting in a closed orbit, the overall bending angle provided by the dipoles along the entire ring must equal 2π radians. The field profile of a dipole magnet is depicted in the left side sketch of Fig. 1.3. Imagining a beam directed inward the screen, the trajectory will be bent to the right.

To maintain electrons in close proximity to the reference orbit, focusing of the trajectories is required. Focusing is attained by employing gradient fields, primarily generated by quadrupole magnets at SIRIUS. The strength of such fields increases linearly with deviations from the closed orbit, which lies in the magnet's center. Gradient fields effectively act as spring forces. The magnet's poles and the field profile of a quadrupole magnet are depicted in the center sketch of Fig. 1.3.

Focusing and deflection are energy-dependent, which means small deviations from the nominal operating energy can result in differential focusing. Drawing an analogy from geometric optics, the beam's focusing behavior at the "lens" (quadrupoles) depends on its "color" (energy). To correct for these chromatic aberrations, the use of "glasses" becomes necessary. In the context of accelerators, sextupole fields serve as these corrective lenses. They introduce geometric aberrations to counteract the chromatic ones, resulting in approximately uniform, energy-independent focusing, up to the linear approximation

theory. The magnets poles and the field profile of a sextupole magnet are depicted in the right sketch of Fig. 1.3.

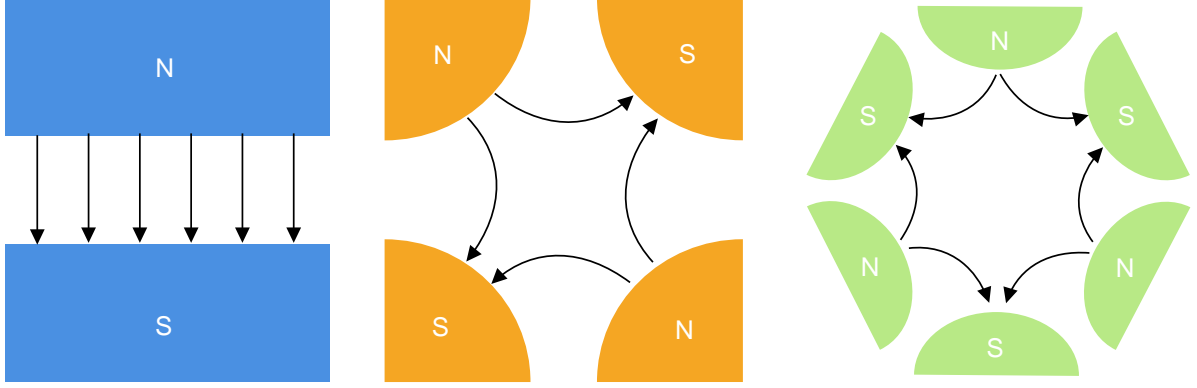


Figure 1.3: Schematic representation of the magnets comprising SIRIUS lattice and their fields profile. From left to right: dipole magnet, quadrupole magnet and sextupole magnet.

Besides dipoles, quadrupoles and sextupoles, additional dipole actuators magnets for orbit/trajectory correction and pulsed magnets for beam injection are also part of the ring. The beam is also periodically subject to longitudinal time-dependent electromagnetic radiofrequency fields which do work on the beam to replenish its energy. The goal is to compensate for the energy carried away in the form of synchrotron light.

1.4 The problem addressed in this work

The pursuit of low emittances and high brightness has driven the accelerator community toward the fourth-generation of storage rings. Achieving such low emittances was possible because of series of technological advances which enabled the use of the multi-bend achromat (MBA) lattice [5, 7]. MBA lattices require intense gradient fields provided by quadrupole magnets, which, in turn, demands the presence of strong sextupolar fields to compensate for chromatic effects. Since sextupoles provide nonlinear fields, the dynamics in fourth-generation storage rings has become increasingly nonlinear [7].

A quasi-periodic nonlinear dynamics, when subjected to even the slightest perturbations—such as small field errors stemming from rotation, alignment, or fields excitation errors—can potentially become unstable at large oscillation amplitudes. These instabilities impose constraints on the maximum transverse oscillation amplitudes that the machine can accommodate. The specific amplitude below which motion is stable is referred to as the Dynamic Aperture (DA) of the ring. Exceeding the DA results in irregular and often chaotic motion and beam loss.

Under normal operating conditions, the equilibrium beam size and typical oscillation amplitudes are considerably smaller than the DA, and the dynamics can be well studied and analyzed using a linear approximation theory, without worrying about the DA. However, there are specific scenarios where the DA becomes crucial for the operation, notably during the injection process.

During injection into the storage ring for beam accumulation, the beam is extracted from the booster accelerator and guided toward the storage ring through a transport line. As soon as it enters the ring, the beam is deflected by the field of a pulsed nonlinear magnet, which makes the beam almost parallel to the storage ring tangent direction, albeit with a horizontal offset of approximately $x = -8$ mm [11]. If the DA is smaller than this initial amplitude, it imposes limitations on the injection efficiency.

The placement, symmetry and strength of sextupoles magnets—the nonlinear lattice—were determined through a multi-objective optimization process, primarily focused on improving the simulated DA and beam lifetime of the machine’s computer model [12,13]. This optimization work considered the average performance of the lattice configurations while accounting for various magnet errors that simulate the expected errors in the actual machine [12]. Several models, with several errors distribution among the magnets were generated, and the DA and lifetime for a given lattice configuration was calculated by simulating the electron beams motion for several turns (tracking simulations). The final figure of merit for a lattice consisted on the average DA and lifetime it provided to the ensemble of machines. The best-performing machine lattice found during this process was adopted as the nominal lattice which was subsequently deployed during the commissioning phase of the machine.

The operating machine consists on a practical realization of a specific error configuration, which defines the physically realized magnetic lattice and determines the dynamics overall performance. The best-performing lattice on average, found in the simulations, is not necessarily the optimum lattice for this specific errors realization.

Assuming the realized lattice closely approximates the optimum setup, i.e. that the errors are small, it is reasonable to assume that by making minor tweaks and adjustments to the strengths of the sextupoles one can adapt the nonlinear lattice to match the actual distribution of errors in the physical system. This fine-tuning process can result in improved nonlinear dynamics performance, expanding the DA, and ultimately enhancing both injection efficiency and its stability. This process has already been demonstrated in other machines. It has proven to be a successful approach and became known as *Online optimization*. If one thinks of the errors as agents that deteriorate the DA from its optimum, online optimization can be seen as an attempt to compensate for such deterioration.

Online optimization of the machine nonlinear dynamics consists on employing computer-automated search strategies to systematically explore various sextupole configurations with the goal of identifying the ones that yields the largest DA while not interfering

in other machine parameters, such as chromaticity and beam lifetime. The key ingredient in online optimization is the choice of a robust optimization algorithm based on direct or indirect search in the parameter space. The most widely used is the Robust Conjugate Direction Search (RCDS) algorithm, which is based on a noise robust one-dimensional optimizer along with a clever strategy, known as Powell's method, for choosing directions in the search space. Chapter 3 addresses the RCDS algorithm.

Besides improving the DA and injection efficiency in nominal operation conditions, it is also interesting to do so in different machine *working points*, with different *tunes*. As chapter 2 shows, if one fixes one's attention to a specific point of the ring, and measure the beam position in horizontal and vertical planes for consecutive turns, one realizes the motion is a sampled sinusoid and the tunes ν_x and ν_y are the fundamental frequencies of such harmonic motion. They are important operation parameters since they affect over the response of the system in the presence of perturbations. Tunes close to integer numbers result in large *orbit amplification factors* making the dynamics particularly sensitive to perturbations.

The fractional parts of SIRIUS nominal tunes are quite low and increasing them would distance the tunes away from integer numbers, reducing the orbit amplification factors and improving the orbit stability. Changing the tunes can be achieved by actuating with the quadrupole magnets, but doing so takes the machine to a different operating optics, in which the DA can, and often is, smaller than the DA in nominal optics. In different working points, thus, online optimization is essential to find a new sextupole configuration to adapt the nonlinear magnets to the new optics and achieve a good DA and acceptable injection efficiencies for operation.

In agreement with the experience in other facilities, it is shown in Chapter 4 that online optimization using RCDS can successfully improve the dynamics performance and lead to DA and injection efficiency improvements. This was observed for the SIRIUS storage ring both in the machine nominal tunes as well as in other working points. SIRIUS experience with online optimization is a valuable demonstration of this tool's efficiency in fourth-generation rings with such a large search space.

At the time of this writing, SIRIUS is operating with the sextupole configurations found during one of the experiments carried out during the execution of this project. The configuration was found by online optimization carried out with increased tunes optics. The higher tunes led a reduction in orbit amplification factors resulting in unprecedented orbit stability.

In the next chapter, the dynamics of electrons in storage rings is examined. The linear approximation motion is introduced and nonlinear dynamics is treated as a perturbation to the linear theory. Chapter 3 gives the reader a brief overview of optimization strategies and focuses on familiarizing the reader with the Robust Conjugate Direction Search (RCDS) algorithm. Chapter 4 presents the methods and results of the online

optimization experiments carried during the execution of this project.

CHAPTER 2

Theoretical Background

This chapter provides the bare minimum theoretical knowledge on electron storage ring physics and particles dynamics needed to state to the reader the optimization problem and the constraints which are involved. A qualitative description of the physics of electron storage rings is presented, followed by a more detailed and more quantitative treatment of single particle dynamics in storage rings.

2.1 The physics of electron storage rings

As mentioned previously, a storage ring is designed to confine bunches of electrons and steer them along a reference closed orbit. The orbit is defined by the bending magnets, the dipoles. The trajectories consist on oscillations about the closed orbit, and focusing of such oscillations toward the closed orbit is provided by gradient fields, mostly coming from quadrupole magnets. Additionally, to correct chromatic aberrations in the beam's motion, i.e. a dependence of focusing with the beam's energy, and guarantee correct focusing despite energy deviations from the nominal value, sextupolar magnetic fields are also introduced, providing fields depending quadratically on the deviations from the nominal orbit. These fields introduce strong nonlinearities in the dynamics.

When having its trajectory bent at the dipoles and insertion devices, the beam loses energy in the form of synchrotron radiation. To maintain the beam stored, the energy lost must be replenished. To this aim, radio-frequency (RF) cavities are placed along the ring to provide oscillating electric fields parallel to the longitudinal direction. The work done in the beam by the fields restore its energy.

The radiated photons are emitted in a narrow cone with angular aperture of $1/\gamma$, γ being the relativistic Lorentz factor (~ 6000 at SIRIUS storage ring). The photons carry away a fraction of the beam's energy and momentum in both the longitudinal and transverse directions. When passing through RF cavities, only momentum in the longitudinal direction is replenished. The combined effect of radiating photons and passing through RF cavities leads to an overall damping of transverse amplitudes.

On the other hand, the quantum nature of the emitted radiation leads to the excitation of transverse oscillations, which is known as quantum excitation. When a

photon carries away energy, it depletes the electrons energy by the same amount. It thus changes the reference orbit of the electron in certain regions of the ring (dispersive regions), inducing oscillations. Eventually, equilibrium between radiative damping and quantum excitation is achieved, leading the rms values of each electron's amplitudes to reach a stationary regime.

include the case of nondispersive and vertical amplitudes damping

Each one of the beam's degrees of freedom defines an acceptance: limits which if exceeded can result in instabilities and eventually beam losses. The most obvious acceptance is the transverse acceptance: the beam motion is bounded by a vacuum chamber and colliding with the chamber's physical aperture leads to losses. Additionally, the beam also has an energy acceptance: a tolerance for energy deviations from the nominal value that when exceeded can lead to a suboptimal energetic balance, which, in turn, leads to significant deviations from the nominal orbit and eventually collisions with the vacuum chamber.

The beam is also subject to elastic and inelastic collisions with residual gas molecules within the chamber and also the collisions between electrons within the same bunch, besides other kinds of interactions with wake-fields from other bunches. All these effects can lead to beam-losses and the overall beam loss rate resulting from these combined mechanisms defines the characteristic time scale at which a given electron current survives in the ring. This is the beam lifetime and determines the rate at which injections into the storage ring are required.

Because of the nonlinearities introduced by the sextupole magnets, the transverse acceptances can be limited not solely by the physical aperture available in the vacuum chamber but rather by the amplitudes above which motion is irregular, unstable and unbounded. As already mentioned before, this limiting amplitude is known as the dynamic aperture (DA), a term that can be used to refer to amplitudes in the transverse space x, y or to the phase space coordinates x, p_x and y, p_y .

Despite the complicated physics of a fully-coupled dynamics involving the transverse and the energy oscillations and also the damping and the excitation of amplitudes, collective effects and instabilities, for the purpose of this dissertation, it is sufficient to model the motion of a single electron, neglecting radiation losses (and thus the existence of the RF cavities) and any other collective interactions.

In this picture, the electron travels along the ring at the speed of light and executes transverse oscillations in two orthogonal planes. The dynamics takes place in a 4-dimensional phase space which is the dynamics of two independent quasi-periodic oscillators. These simplifications are justified for our immediate purposes because:

- radiation losses/gains and energy oscillations are only significant over a time scale of a couple of turns. Over this period, tens of transverse oscillations take place

- the linear and uncoupled dynamics this modeling renders serves as a building block upon which elaborate modeling can be carried out, incorporating coupling, nonlinearities and perturbations with perturbation theory
- why is it ok to ignore collective effects and instabilities?

Next, the single-particle dynamics is presented with the aim of defining quantitatively the dynamic aperture and the characteristics of the dynamics in electron storage rings. Throughout the modelling, optical functions and parameter for the SIRIUS storage rings are also presented.

2.2 Motion of charged particles in magnetic fields

An electron of charge e and momentum of magnitude p follows a circular orbit of radius ρ when interacting with an uniform and time-independent magnetic field of magnitude B directed perpendicularly to the orbit plane. In such conditions, the Lorentz force law predicts that the relevant quantities are related by

$$R(p) \equiv B\rho = \frac{p}{e}. \quad (2.1)$$

Consider now an electron traveling along a curve parametrized by the arclength s with respect to an arbitrary reference point. The interaction with fields $B_x(x, y, s)$ and $B_y(x, y, s)$, both perpendicular to the electron's motion, results in deflections of the trajectory. The deflection angles are given by

$$d\theta_u = \frac{ds}{\rho_u(s)} = \frac{e}{p} B_v(x, y, s) ds = \frac{1}{R(p)} B_v(x, y, s) ds, \quad u, v = x, y \quad \text{or} \quad y, x. \quad (2.2)$$

Where (2.1) has been used to replace the p/e ratio by the *magnetic rigidity* $R(p)$, which is defined as the product of the uniform field strength needed for a beam with momentum p and charge e to perform circular orbit with radius ρ . The rigidity depends solely on the electron's momentum/energy and gives the appropriate normalization to evaluate the instantaneous angular deflections in the electron's trajectory caused by magnetic fields.

Add deflection figures

2.3 The coordinate system for storage ring dynamics

As sketched by Figure 1.2, electrons in a storage ring perform a prescribed nearly circular trajectory close to a reference orbit. A convenient coordinate frame to describe the dynamics in storage rings can be constructed by imagining a reference particle traveling along a curve drawn by the tip of a vector \mathbf{r}_0 , as Fig. 2.1 shows. The idea is that

this particle samples exactly the reference nominal orbit. The particle travels a distance s along the ring, which can be used to parametrize the motion. The triad of direction vectors consists of a vector $\hat{\mathbf{s}}$, tangent to the trajectory, a vector $\hat{\mathbf{x}}$ normal to it, pointing in the direction at which $\hat{\mathbf{s}}$ changes and a vector $\hat{\mathbf{y}} = \hat{\mathbf{x}} \times \hat{\mathbf{s}}$, bi-normal to the trajectory. This construction leads to a Frenet-Serret reference frame. The deviations from the nominal orbit can be measured in units of the unit vectors in the normal and bi-normal directions, characterizing the transverse dynamics. One may also be concerned with the distance of a given particle from the reference particle itself along the curve. Such differences may arise due to differences in the energy two particles. Since no radiation loss nor gain will be considered in our modeling, the energy and longitudinal deviations from the reference particle are not dynamical quantities, but rather parameters of the dynamics.

Assuming no curvature in the y plane, i.e. that the accelerator defines a curve whose plane is parallel to the facility flat floor, then the unit vectors defining the frame can be calculated by [14]

$$\hat{\mathbf{s}} = \frac{d\mathbf{r}_0}{ds}, \quad \hat{\mathbf{x}} = -\rho \frac{d\hat{\mathbf{s}}}{ds}, \quad \hat{\mathbf{y}} = \hat{\mathbf{x}} \times \hat{\mathbf{s}}. \quad (2.3)$$

where $\rho(s) = \|d\hat{\mathbf{s}}/ds\|^{-1}$ is the local curvature radius¹. The vectors evolve along s as prescribed by the Frenet-Serret equations:

$$\frac{d\hat{\mathbf{s}}}{ds} = -\frac{1}{\rho(s)}\hat{\mathbf{x}}, \quad \frac{d\hat{\mathbf{x}}}{ds} = \frac{1}{\rho(s)}\hat{\mathbf{s}}, \quad \frac{d\hat{\mathbf{y}}}{ds} = 0, \quad (2.4)$$

The frame thus depends solely on the geometry of the specified path. Since the curvature is defined by the dipolar fields $B_0(s)$ in the y direction, then, eq. (2.2) leads to

$$\frac{1}{\rho(s)} = \frac{B_0(s)}{R_0}, \quad (2.5)$$

where R_0 is the rigidity for the beam at the nominal energy.

2.4 Hamiltonian for the relativistic electron

The dynamics of relativistic electrons influenced by electromagnetic fields (Φ, \mathbf{A}) is encapsulated by the Hamiltonian [15]

$$H = \sqrt{m^2c^4 + (\mathbf{P} - q\mathbf{A})^2c^2} + e\Phi,$$

¹For a circular trajectory, $\mathbf{r}_0 = (R \cos(s/R), R \sin(s/R), 0)$, $0 \leq s \leq L$ (check), in the cartesian laboratory frame. $\hat{\mathbf{s}} = (-\sin(s/R), \cos(s/R), 0)$, $d\hat{\mathbf{s}}/ds = -R^{-1}(\cos(s/R), \sin(s/R), 0)$ and $\rho(s) = R$, justifying the interpretation as curvature radius.



Figure 2.1: The Frenet-Serret coordinate system. From [1].

e being the elementary charge and $\mathbf{P} = \mathbf{p} + e\mathbf{A}$ the canonical momentum. The following steps are followed to obtain equations of motion for electrons in the storage ring:

- A canonical transformation to change coordinates is applied in order to describe the motion in terms of the Frenet-Serret frame variables x, y ;
- Instead of time t , the Hamiltonian and the dynamical variables are described as functions of s , the longitudinal position along the ring;
- Paraxial approximation: the transverse momenta are assumed to be way smaller than the momentum along the trajectory's tangent direction. This allows the expansion of the square root in the Hamiltonian as a power series, revealing the expression for an approximate Hamiltonian which can be more easily handled;
- Geometric quantities are used: in the paraxial approximation, the canonical momenta for on-energy particles are identified with the derivatives with respect to the parameter s $x' = dx/ds$ and $y' = dy/ds$, which represent the divergence angles from the nominal orbit;

All of the transformations and manipulations summarized above can be found in detail in the literature, such as in Refs. [2,3,14]. As mentioned previously, by neglecting RF cavities ($\Phi = 0$) and radiation losses, the energy will be a constant parameter and the dynamics will consist solely on the transverse degrees of freedom. In this 4-dimensional dynamics, the set of canonical variables are (x, p_x, y, p_y) , where the momenta are given by

$$p_x = x'(1 + \delta), \quad p_y = y'(1 + \delta) \quad (2.6)$$

and δ is the relative deviation from the nominal energy-momentum:

$$\delta \equiv \frac{P - P_0}{P_0} \approx \frac{E - E_0}{E_0}. \quad (2.7)$$

The ultra-relativistic approximation $E \approx pc$ was used.

Hamilton's equations for the paraxial-approximated Hamiltonian reveals the equations of motion for the x and y Frenet-Serret coordinates, which read:

$$x'' = -\frac{(1 + Gx)^2}{1 + \delta} \frac{B_y}{R_0} + G(1 + Gx), \quad y'' = \frac{(1 + Gx)^2}{1 + \delta} \frac{B_x}{R_0}, \quad (2.8)$$

where $R_0 = p_0/e$ is the magnetic rigidity of the beam at the nominal energy and $G(s) \equiv \rho^{-1}(s)$ is the inverse local radius of curvature, related to the dipole field as in Eq. (2.5).

2.5 Specification of magnetic fields

To study the motion, we need to specify the fields $B_x(s)$ and $B_y(s)$ acting on the beam. Since in a storage ring the magnets are arranged as arrays of dipoles, quadrupoles and sextupoles which usually have some symmetry and periodicity, the $B_x(s)$ and $B_y(s)$ functions are generally periodic. If $\ell_d, \ell_s, \ell_{\text{se}}$ are the lengths of dipoles, quadrupoles and sextupoles magnets in a ring, respectively, the magnetic fields are sectionally defined and have the following functional forms

- Horizontal Dipole

$$B_x(s) = 0, \quad B_y(s) = B_0, \quad s \in (0, \ell_d), \quad (2.9)$$

- Normal quadrupole

$$B_x = B_1 y, \quad B_y = B_1 x, \quad s \in (0, \ell_q), \quad (2.10)$$

- Normal sextupole

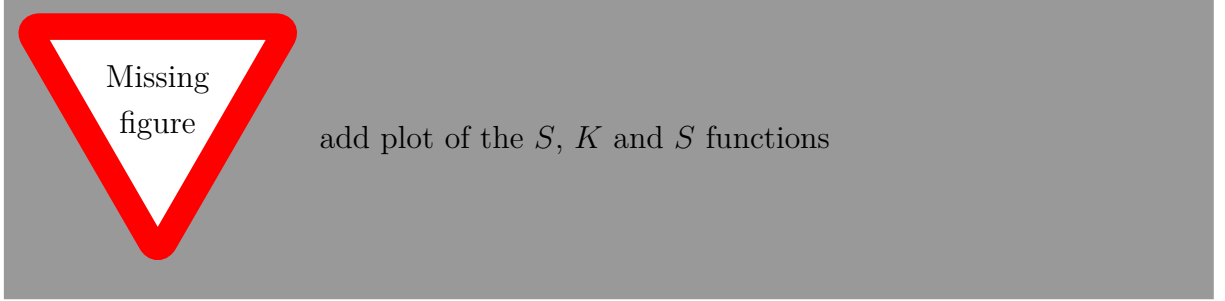
$$B_x = B_2 xy, \quad B_y = \frac{1}{2} B_2 (x^2 - y^2), \quad s \in (0, \ell_s), \quad (2.11)$$

and zero everywhere else, neglecting the fields of insertion devices. Fields (2.9)–(2.11) are the so-called *normal multipole fields*. There are also *skew multipole fields*, which couple the horizontal and vertical dynamics. We will neglect skew fields and coupling for now. They can be treated as perturbations in perturbation theory schemes.

In eqs. (2.8), the magnetic rigidity normalizes all the fields. We therefore define

the normalized dipolar, quadrupolar and sextupolar fields as the functions

$$G(s) = \frac{B_0(s)}{R_0}, \quad K(s) = \frac{B_1(s)}{R_0}, \quad S(s) = \frac{B_2(s)}{R_0}. \quad (2.12)$$



2.6 Linear Dynamics

The linear equations of motion

Expansion of eqs. (2.8) up to first order in the x, y, δ variables leads to [16]

$$x'' + (G^2 + K)x = G\delta, \quad y'' - Ky = 0. \quad (2.13)$$

For on-momentum particles, $\delta = 0$, both equations are instances of Hill's equations

$$u'' + K_u(s)u = 0, \quad (2.14)$$

i.e, a pair of parametric oscillators for $u = x, y$, with s -dependent and periodic focusing functions

$$K_x(s) = G^2(s) + K(s), \quad K_y(s) = -K(s),$$

the analogues to an oscillator's spring force per unit mass. Motion in the linear approximation thus consists on oscillations around the closed orbit, known as *betatron oscillations*.

Pseudoharmonic description

Betatron motion can be cast in a amplitude-phase form. One can show that

$$u(s) = \sqrt{2\beta_u(s)J_u} \cos(\phi_u(s) + \phi_0), \quad u = x, y, \quad (2.15)$$

is a solution to (2.14) as long as the $\beta_u(s)$ function satisfies the boundary-value problem

$$\frac{1}{2}\beta_u'' + \beta_u K_u(s) - \frac{1}{\beta_u} \left(\frac{1}{4}\beta_u'^2 + 1 \right) = 0, \quad \begin{cases} \beta_u(0) = \beta_u(L) \\ \beta_u'(0) = \beta_u'(L) \end{cases} \quad (2.16)$$

and the phase advance is given by

$$\phi_u(s) = \int_0^s \frac{1}{\beta_u(\sigma)} d\sigma. \quad (2.17)$$

The motion is oscillatory, non-harmonic and non-periodic. The oscillations envelope is the square-root of the beta functions $\beta_u(s)$, which for the SIRIUS storage ring are shown in Fig. 2.2.

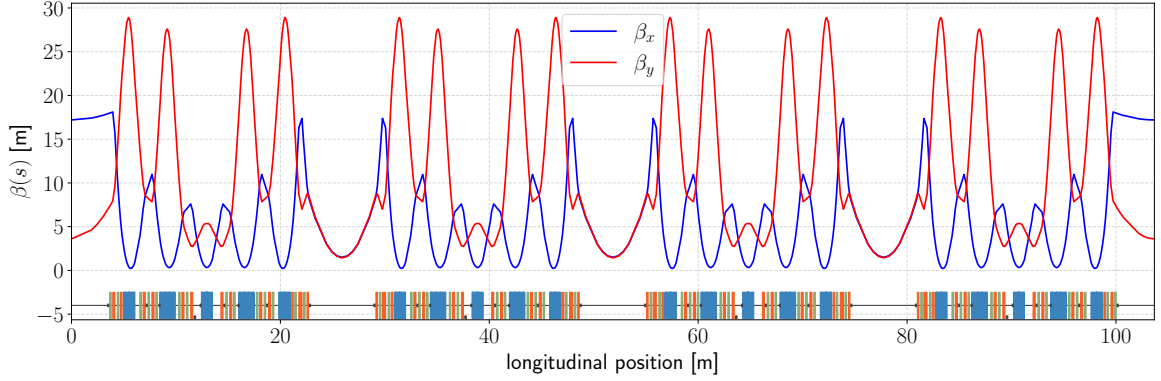


Figure 2.2: Betatron functions for the SIRIUS storage ring. Colored blocks represent the magnets of the accelerator lattice: blue for dipoles, orange for quadrupoles and green for sextupoles. The ring has a 5-fold symmetry, with the lattice and betatron function repeating the same pattern shown above five times up to $s = 518$ m

The tune

An important feature of the dynamics is the *tune*: the phase advance over a revolution along the ring

$$\nu_u = \frac{1}{2\pi} \int_s^{s+L} \frac{d\sigma}{\beta_u(\sigma)} \equiv \frac{1}{2\pi} \oint \frac{ds}{\beta_u(s)}.$$

The tune reveals the number of transverse oscillations per revolution. The nominal tunes for SIRIUS storage ring are $(\nu_x, \nu_y) = (49.08, 14.14)$.

When studying the effects of perturbations and nonlinearities acting on the beam, one finds the tunes are a critical variables in determining the beam's response. More specifically, the tunes impact over disturbances amplification factors, which are greatest when tunes are close to integer numbers.

Turn-by-turn motion

If one keeps track of the time evolution of the the u, u' variables at a fixed position along the ring, plotting them in a phase space, one realizes the the quasi-periodic motion traces out ellipses in such plane. This fact can be analytically verified by calculating

the derivative

$$u'(s) = -\sqrt{\frac{2J_u}{\beta_u}} \left[\sin(\phi_u(s) + \phi_0) + \frac{1}{2}\beta'_u(s) \cos(\phi_u(s) + \phi_0) \right], \quad (2.18)$$

defining the functions $\alpha_u = \frac{\beta'_u}{2}$ and $\gamma_u = \frac{(1+\alpha_u^2)}{\beta_u}$ and checking that u, u' satisfy the quadratic form

$$2J_u = \gamma_u u^2 + 2\alpha_u u u' + \beta_u u'^2. \quad (2.19)$$

The ellipse properties are ruled by the $\beta_u(s), \alpha_u(s)$ and $\gamma_u(s)$ functions, also known as Courant-Snyder (C-S) parameters or Twiss parameters. Since the parameters are functions of the position s , then, at each point along the accelerator, the Poincaré Section u, u' displays a different ellipse. Although different in shape, their areas are proportional to J_u , an invariant quantity determined by the particle's initial condition. The areas are thus conserved along the ring [3, 14].

Since the phase advance over a turn is $2\pi\nu + \phi_0$, the phase advance after the j -th turn is $2\pi\nu j + \phi_0$, and thus sampling the transverse motion at a fixed $s = s_0$ position reveals a harmonic displacement, which at the j -th turn reads

$$u_j(s_0) = \sqrt{2\beta_u(s_0)J_u} \cos(2\pi\nu_u j + \phi_u(s_0)). \quad (2.20)$$

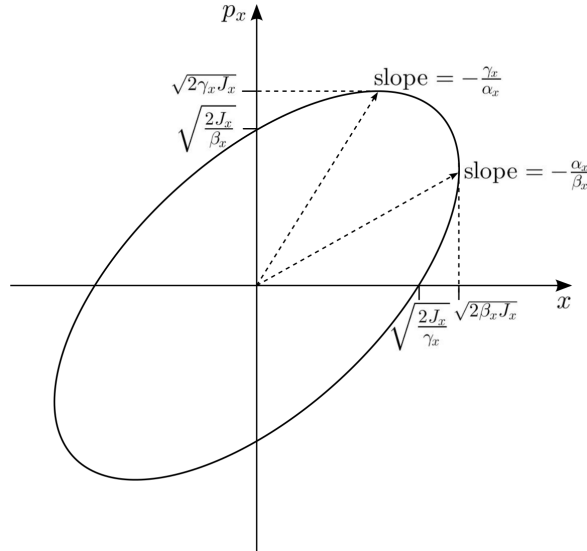


Figure 2.3: Phase space ellipse traced by tur-by-turn (TbT) motion in the (x, p_x) phase space. Optics functions determine the principal axes ratios and the inclination of the ellipse at each longitudinal position along the ring. From [2].

2.7 Dispersive & Chromatic Effects and Linear Perturbations

Dispersion

The equation of motion for off-momentum particles in the horizontal plane, the first of eqs. (2.13), is a non-homogeneous Hill's equation. The solution consists on the linear combination of the homogeneous solution (betatron motion) plus the particular solution: $x = x_\beta + x_\delta$. Since the non-homogeneous term, $G(s)\delta$, is proportional to δ , we can assume $x_\delta = \eta(s)\delta$ where $\eta(s)$ is the *dispersion function*, which should satisfy

$$\eta'' + (G^2 + K)\eta = G, \quad \begin{cases} \eta(0) = \eta(L), \\ \eta'(0) = \eta'(L). \end{cases}$$

The periodicity in the $\eta(s)$ function is required if we want to interpret it as a closed orbit distortion per relative momentum deviation. Thus, off-momentum particles perform betatron oscillations around a dispersive orbit, displaced from the nominal orbit by $\eta(s)\delta$. The dispersion function for the SIRIUS storage ring is shown in Fig. 2.4

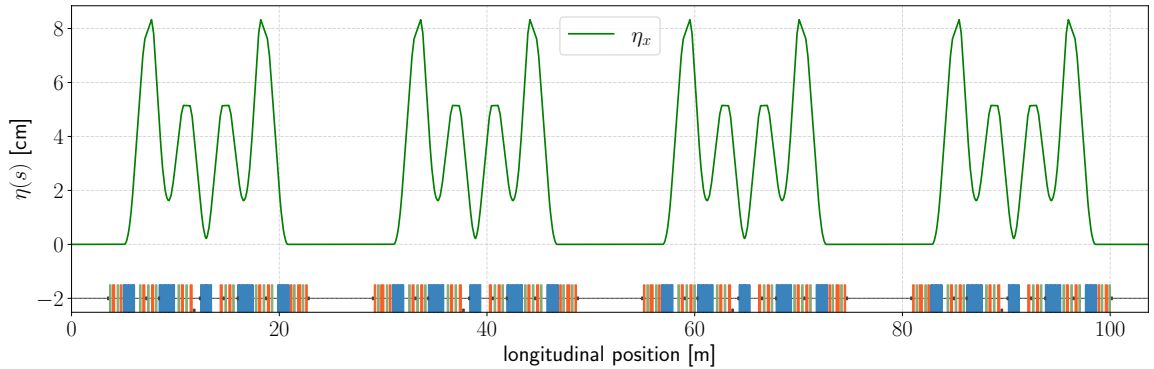


Figure 2.4: Dispersion function for SIRIUS superperiod.

Linear Field Errors

In the presence of additional dipolar and quadrupolar fields representing field errors and deviations from the nominal fields, the orbit and focusing of the beam are changed. Assuming these are small perturbations and not sufficiently strong to kill the beam, we can evaluate the disturbances to the unperturbed dynamics. The details and derivations can be found in the literature, such as in chapter 2 of Ref. [14]. Here we highlight the main results.

For dipole errors $\Delta G_y(s) = -\Delta B_{0x}(s)/R_0$ and $\Delta G_x(s) = \Delta B_{0y}(s)/R_0$, the

equations of motion read

$$x'' + K_x(s)x = G\delta + \Delta G_x(s), \quad y'' + K_y(s)y = \Delta G_y(s). \quad (2.21)$$

The solution consists on the combinations of the betatron motion plus the dispersive orbit (for the horizontal plane) plus the closed orbit distortion u_{co} induced by the additional bending terms due to the dipole errors. For a single thin bending error ΔG_u in the $u = x, y$ plane, acting for a length Δs around $s = s_0$, the closed orbit distortion u_{co} reads

$$u_{\text{co}}(s) = \frac{\sqrt{\beta_u(s)\beta_u(s_0)}}{2 \sin \pi \nu_u} \Delta G_u \cos(\pi \nu_u - |\phi_u(s) - \phi_u(s_0)|) \Delta s. \quad (2.22)$$

For a distribution $\Delta G_u(s)$ of dipolar perturbations along the ring, we sum over the contributions:

$$u_{\text{co}}(s) = \frac{\sqrt{\beta_u(s)}}{2 \sin \pi \nu_u} \int_s^{s+L} \Delta G_u(\sigma) \sqrt{\beta_u(\sigma)} \cos(\pi \nu_u + \phi_u(s) - \phi_u(\sigma)) d\sigma. \quad (2.23)$$

The prefactor involving the sine of the tune shows how ν_u close to an integer can amplify the effects of the dipolar perturbations on orbit distortions. At first sight, aiming for tunes half-integer tunes $\nu = k/2, k \in \mathbb{Z}$ might seem desirable to minimize the distortions. Choosing so, however, increases the sensitivity to gradient errors, which we examine next.

Gradient errors can be modeled as corrections to the focusing functions in the equations of motion: $K_u(s) \rightarrow K_u(s) + \Delta K_u(s)$, for $\Delta K_x(s) = \Delta B_{1y}(s)/R_0$ and $\Delta K_y(s) = -\Delta B_{1x}(s)/R_0$. The changes in beam focusing lead to changes in the beta-functions, phase advances and consequently the betatron tunes. One can show the tune-shift as a consequence of a gradient error acting over a small extent Δs around $s = s_0$ is [14]

$$\Delta \nu_u = \frac{1}{4\pi} \beta(s_0) \Delta K_u \Delta s. \quad (2.24)$$

For a distribution of errors we sum over the ring:

$$\Delta \nu = \frac{1}{4\pi} \oint \beta(s) \Delta K(s) ds, \quad (2.25)$$

where the closed integration sign refers to a complete circulation along the ring, i.e., integration from s_0 to $s_0 + L$, for any $s_0 \in [0, L)$.

As for the induced error on the beta-functions, it is possible to show that the relative error, known as betabeat, can be expressed as

$$\frac{\Delta \beta_u(s)}{\beta_u(s)} = -\frac{1}{2 \sin(2\pi \nu_u)} \int_s^{s+L} \Delta K_u(\sigma) \cos[2(\phi_u(\sigma) - \phi_u(s) - \pi \nu)] d\sigma. \quad (2.26)$$

which is the largest for $2\nu_u$ closest to an integer. This means we must avoid tunes close to

half-integers if we want to avoid the coherent build-up of betatron amplitudes, which can eventually lead to beam loss. Integer or half-integer tunes are the simplest instances of resonances the beam can be subject to. A more general overview of resonances is presented in section 2.8.



Chromaticity

We know the bending angles at the dipoles is different for electrons with different energies. This is the origin of dispersive orbits. The energy deviations affect not only the closed orbit by means of the dispersion effect, but affect also the focusing of the trajectories, since a more/less energetic beam has higer/lower rigidity and thus is focused differently when passing through gradient fields. Expanding the equations of motion, eqs. (2.8), for off-energy particles up to the order of terms $u\delta$, for $u = x, y$, reveals additional higher-order gradient errors. The focusing functions are corrected by $K_u(s) \rightarrow K_u(s) + \Delta K_u(s)$ [1, 14], where

$$\Delta K_x = -(K + 2G^2)\delta \approx -K_x\delta \quad (2.27)$$

$$\Delta K_y = K\delta = -K_y\delta \quad (2.28)$$

This means there exists an energy-dependent tune-shift effect caused by the gradient error. Using eq. (2.25), the tune-shift reads

$$\Delta\nu_u = -\frac{1}{4\pi} \oint \beta_u K_u \delta \, ds, \quad (2.29)$$

for the $u = x, y$ planes. We can define the *linear chromaticity* in the $u = x, y$ direction as tune-shift $\Delta\nu_u$ per relative energy deviation δ :

$$\xi_u = \frac{d\nu_u}{d\delta}. \quad (2.30)$$

This uncorrected chromaticity is also called natural chromaticity. Using expression (2.29) for the tune-shift, the natural chromaticity reads

$$\xi_{u,\text{nat}} = -\frac{1}{4\pi} \oint K_u \beta_u \, ds. \quad (2.31)$$

This chromatic aberration effect needs to be corrected to guarantee energy-independent focusing. Correction can be attained with the insertion of geometric aberrations provided by sextupolar fields, specifically in the dispersive sections of the storage ring. In such regions, off-energy particles follow a dispersive orbit, and their position reads $x(s) = x_\beta(s) + \eta(s)\delta$, where $x_\beta(s)$ consists on the betatron oscillations. Since sextupolar fields are of the form

$$B_x = B_2xy, \quad B_y = \frac{B_2}{2}(x^2 - y^2),$$

then, the off-momentum particles "see" the fields

$$B_x = B_2(x_\beta y + \eta\delta y), \quad B_y = \frac{B_2}{2}(x_\beta^2 - y^2) + B_2x_\beta\eta\delta + \frac{B_2}{2}(\eta\delta)^2,$$

So, to lowest order in eqs. (2.8), they feel a dipolar perturbation (which contributes to orbit distortions) and the gradient perturbation

$$\Delta K_{x,y}(\delta) = \pm S\eta\delta,$$

recalling that $S(s) = B_2/R_0$.

Considering the contributions from both the errors induced by energy deviations and also the lowest order sextupole gradient effect, we have a total error of $\Delta K_u = -(K_u \mp S\eta)\delta$ to be inserted in eq. (2.25). The chromaticity in a lattice with sextupoles thus reads

$$\xi_u = -\frac{1}{4\pi} \oint \beta_u (K_u \mp S\eta) ds, \quad (2.32)$$

with the minus sign for $u = x$ and the plus sign for $u = y$. The chromaticity depends linearly on sextupole strengths, allowing for its correction to desired values. Since the effect of the sextupole field focuses in a given plane but defocuses in the other, at least two sextupole families are required for chromaticity correction: one family where $\beta_x > \beta_y$ and other where $\beta_y < \beta_x$. The cost of correcting chromaticity is the insertion of perturbations and nonlinearities in the dynamics. To allow for more control over the nonlinear dynamics effects, usually some families of sextupoles are also placed in non-dispersive sections. They are called achromatic families, since they have no effect over chromaticity.



show chromatic aberrations and their correction with geometric aberrations

2.8 Nonlinear Dynamics, Perturbations, Ressonances and Tune-Shifts

Action-Angle Variables

The betatron equations of motion, Eqs. (2.14), can be obtained as Hamilton's equations for an effective, linear Hamiltonian

$$\mathcal{H}_u = \frac{1}{2}u'^2 + \frac{1}{2}K_u(s)u^2, \quad (2.33)$$

summed over $u = x, y$. A transformation $(u, u') \rightarrow (\psi_u, J_u)$ to Action-angle variables is implicitly implemented by the type-1 generating function [14]

$$F_1(u, \phi_u) = \int u' du = -\frac{u^2}{2\beta_u} \left(\tan \phi_u - \frac{\beta'_u}{2} \right). \quad (2.34)$$

The action variable reads

$$J_u = -\frac{\partial F_1}{\partial \phi_u} = \frac{u^2}{2\beta_u} \sec^2 \phi_u = \frac{1}{2\beta_u} [u^2 + (\beta_u u' + \alpha_u u^2)], \quad (2.35)$$

from which we can recover the pseudo-harmonic form $u = \sqrt{2\beta_u J_u} \cos(\phi_u(s) + \phi_0)$. In the J, ϕ variables, the new hamiltonian is $H_0(\phi, J)$, given by

$$H_u = \mathcal{H}_u + \frac{\partial F_1}{\partial s} = \frac{J_u}{\beta_u}. \quad (2.36)$$

Performing the change to action-angle variable in both the horizontal and vertical planes we find the action-angle Hamiltonian for 4D dynamics

$$H_0 = \frac{J_x}{\beta_x} + \frac{J_y}{\beta_y}. \quad (2.37)$$

Hamilton's equations read

$$\phi'_u = \frac{1}{\beta_u(s)}, \quad J'_u = 0. \quad (2.38)$$

Perturbations and tune-shifts

Linear motion is integrable, since it can be written in terms of the action variable only (angle-independent Hamiltonian). This leads to the action variable being a constant of motion, and the phase advance behaving just as the pseudo-harmonic motion anticipated.

Linear motion, though, is only a useful first approximation. In reality, in an storage ring, there are higher order multipole magnets, such as sextupole magnets, and

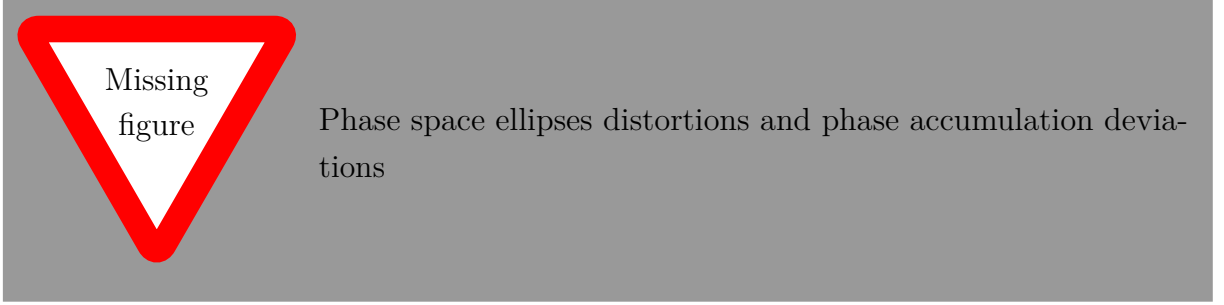
also multipole, alignment and excitation errors, all acting as perturbations to linear motion. Generically referring to perturbations as $V(J, \phi)$, we can write the perturbed motion Hamiltonian

$$H(J, \phi) = H_0 + V(J, \phi), \quad (2.39)$$

For which Hamilton's equations read

$$\phi'_u = \frac{1}{\beta_u(s)} + \frac{\partial V(J, \phi)}{\partial J_u}, \quad J'_u = \frac{\partial V(J, \phi)}{\partial \phi_u}. \quad (2.40)$$

The action is no longer an invariant and the phase advance rate deviates from the linear betatron phase advance.



Focusing on the effects on the tunes, we can express the tunes in terms of the nonlinear chromatic and amplitude-dependent tune-shifts

$$\nu_u = \nu_{u0} + \xi_u(\delta)\delta + \alpha_{uu}J_u + \alpha_{uv}J_v \quad (2.41)$$

where ξ_u represents the energy-dependent tune-shifts (higher order generalization of the linear chromaticity), and the other components consist on the amplitude-dependent tune-shifts, up to first order in the actions.

Resonances

4D linear and unperturbed motion consists on the motion of two uncoupled parametric oscillators. As a quasi-periodic, integrable system, the phase-space is diffeomorphic to the 2-Torus, \mathbb{T}^2 , and there are an infinite number of such tori covering phase space, corresponding to the different choices of initial conditions J_u .

Canonical perturbation theory applied to perturbed motion fails to converge whenever the ratio of tunes is sufficiently rational. The Poincare-Birkhoff theorem states that under such conditions, almost all the periodic phase-space orbits disappear. An even number of tori survives, half of which are stable and half unstable. Unstable motion in a storage ring can eventually lead to beam loss.

The condition for sufficiently rational tunes can be expressed as

$$m\nu_x + n\nu_y = \ell, \quad (2.42)$$

for $n, m, \ell \in \mathbb{Z}$. This condition defines lines in tune-space corresponding to the locus in which perturbation theory fails and motion can become unstable. These are resonance lines and $|n| + |m|$ is the order of the resonance. Particular resonances arising from linear field errors, such as dipolar errors, $\nu_x, \nu_y = n \in \mathbb{Z}$, and gradient field errors, $2\nu_x, 2\nu_y = n \in \mathbb{Z}$, are contained in condition (2.42). Resonances coupling both planes arise when considering perturbations the skew multipole magnets, which can be treated by perturbation theory. Linear coupling resonances are the famous sum and difference resonances $\nu_x + \nu_y = \ell, \nu_x - \nu_y = \ell$, excited by skew quadrupoles magnets.

more details, and the resonances induced by sextupoles

Figure 2.5 shows resonance lines for the resonances up to second, third and fourth order respectively. First order resonances can be excited by dipolar fields, 2nd order resonances can be excited by quadrupole fields and 3rd order resonances can be driven by sextupolar fields.

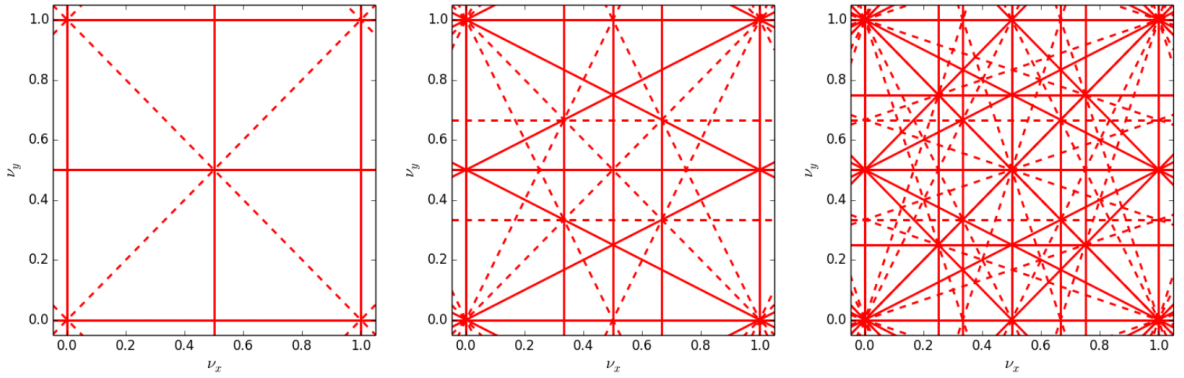


Figure 2.5: Resonance lines in tune space up to 2nd, 3rd and 4th order, respectively.

Dynamic Aperture

Nonlinear dynamics can become sensitive to initial conditions when the amplitudes are large. Because of the tune-shifts, specially the amplitude-dependent tune shifts, the tunes can wander in tune space, eventually crossing resonance conditions that may lead to instabilities, chaotic motion and beam loss. The dynamics can impose limitations to the maximum transverse deviations in which the beam can oscillate while displaying regular and bounded motion. This is a dynamic restriction to the motion known as the *dynamic aperture*.

Exceeding the dynamic aperture eventually leads to beam loss. During injection of the beam, if the transverse offsets are larger than the dynamic aperture, the beam is not captured into the storage ring. This is specially important for off-axis injection, such as in the case for SIRIUS.

More discussion on DA.

CHAPTER 3

Online Optimization

This chapter defines, introduces and justifies online optimization in the context of accelerators. A brief overview of optimization algorithms and their classifications is presented. The Robust Conjugate Direction Search (RCDS) algorithm is introduced as well as the other routines from which it was derived from.

This chapter adds no novelty to the literature in optimization. It is just an overview for merely pedagogic purposes. It is mostly based on the discussion presented by the classic Numerical Recipes, as well as Refs.

3.1 Defining Online Optimization

Suppose we have a machine (we do) in which there is some sort of figure of merit depending on the collective state of some set of relevant components, parts or operation modes—our parameters. There is no mechanistic/deterministic or probabilistic model for the dependence of the figure of merit on the reparameters state, but we do know the parameters affect the figure of merit. We may call these relevant parameters as knobs, since we can use them to tune the figure of merit.,

Now suppose we want to tune the knobs so the figure of merit reaches a certain value, or so that it is minimized or maximized. This is an optimization problem, and we might as well call the figure of merit our objective function. Since the whole system is a black-box, to measure different values for the objective function, i.e., to sample it, we need to change the knobs and measure it again. The tuning procedure is thus based on trial-and-error.

If we are able to devise a computer-automated strategy to seek for the desired value or extremum of the objective function, then running this program while the machine is up and working is what we define as online optimization. The program must measure the objective function and read the current state of the knobs, calculate/decide and apply the changes on the knobs, measure the objective again and evaluate and judge the quality of the changes carried out. The process is iterated until the desired outcome is reached.

This black-box, heuristic optimization problem describes the Dynamic Aperture optimization problem very well. The DA is a figure of merit related to the nonlinear

dynamics—in SIRIUS’ case, the sextupole magnets. There is no analytical/statistical¹ model predicting DA changes given sextupole nudges so we cannot invert the problem and tune sextupoles to A desired DA value. The tuning procedure must be based on trial-and-error.

3.2 Justifying Online Optimization

Running online optimization in a machine will find the nearest extremum (minimum/maximum). In other words, if no stochasticity element is brought into the routine to diversify the search along the parameter space, it will find local, not global extrema. How can we be sure the local minima are the best solution for the optimization problem?

It seems that we will never know, but it actually does not matter. A good-performing solution is all we care about as long as other operation parameters are not affected (more details on the next chapter). But there are reasons to believe the local minima found are actually the global ones and it has to do with how accelerators are designed and the origins of deterioration of the dynamic aperture in the machine.

Because there are correction schemes for the linear dynamics in accelerators, the Dynamic Aperture, i.e. limitations to the allowed oscillation amplitudes, arises because of perturbations acting in a nonlinear dynamics. Other than that, the only limitation would be the physical aperture². The strength and symmetry of the whole magnets lattice is decided based on simulating several possible machine lattice configurations and evaluating parameters such as the dynamic aperture and the beam-lifetime. The best performing and viable solution (lattice) is implemented in the real machine.

In the real machine, additional errors arising from magnets misalignment or any fields deviations can (and will) introduce additional perturbations and can deteriorate the DA. The simulating procedure actually does take into consideration the existence of errors: they are introduced in the model during evaluation of the figure of merit parameters and the best performing lattice on average is chosen.

In the machine, a particular error configuration is physically realized, and we are thus dealing with one possible lattice realization, for which the optimum configuration is not that with the largest average DA or lifetime. But we expect it to be not too far from that reference configuration chosen and applied to the machine. Online optimization thus consists on adjusting the sextupole lattice to the physically realized machine lattice so that it reaches its best-performing configuration.

¹in principle, a surrogate model could be trained to reproduce dynamic aperture given the sextupole strengths as inputs. This is not what we have done so far

²Unperturbed nonlinear motion can display no limitations to oscillation amplitudes

3.3 Robust Conjugate Direction Search

Optimization routines and algorithms are usually classified according to whether they rely on the calculation of derivatives (gradient-based) or solely on the comparison of the objective function values (gradient-free). The latter can yet be classified into direct- or indirect-search methods, depending on whether the search of the extremum relies on direct comparisons of the objective function itself or from a mathematical model of it, respectively [?].

Both gradient-based and gradient-free strategies rely on the comparison of the objective function at different points of the parameter space. If the objective function suffers from noise this can significantly reduce the efficiency of the optimization routine [?, ?]. In Chap. 7 of Ref. [?], a review of the most popular optimization algorithms shows how most of them suffer to find minima to, at least, the precision of the noise- σ the objective function is subjected to.

The Robust Conjugate Direction Search (RCDS) algorithm is a indirect-search, gradient-free optimization algorithm introduced in Ref. [?]. The algorithm consists of a main loop for constructing and managing optimal search directions along the knobs space (Powell’s Method) and a one-dimensional optimizer responsible for a noise-aware search for the minimum along a given direction. The algorithm is capable of optimizing the objective function (find its local maximum/minimum) to at least the precision of the objective-function noise [?, ?], being thus adequate for online optimization problems. Specifically, for accelerator controls and optimization, the algorithm has been successfully applied to optimize beam steering and optics matching during injection [?], reducing horizontal emittance [?, ?] and optimization of dynamic aperture [?, ?, ?, ?, ?].

RCDS actually consists on small modifications of well-known indirect-search routines. To grasp how it works, a brief overview on its predecessors is presented next.

3.3.1 Line methods

Let us incorporate the role of an accelerator operator and suppose we are seeking the configuration of a single knob rendering the best performance, say, the minimum of a certain figure of merit. We nudge the knobs slowly and measure the objective, scanning for the minimum. We might scan tuning the knobs up while the objective goes downhill, and stop when starts increasing. The knobs lives over the real line, so this is basically a line-scan, the basis of line optimization methods. How to teach a computer do the same?

Let $f(x) \in \mathbb{R}$ be the objective function depending on the single parameter $x \in \mathbb{R}$. The task of optimizing f is achieved by a direct search over its domain. Since maximizing a function equals to minimizing the same function multiplied by -1 , in what follows, we shall refer to minimization only.

The search for the minimum is usually preceeded by initially *bracketing* the

minimum. We seek for points $a < b < c$ in the domain such that $f(b)$ is smaller than both $f(a)$ and $f(c)$. If f is reasonably smooth, we are certain there will be a minimum in the interval (a, c) . Standard bracket routines for well-behaved, noiseless objective functions can be found in the literature, and mostly consists on, starting from an initial point, scanning the line “downhill” until the function stops decreasing.

We can see the bracketing procedure as a coarse-grained scan initially performed by the operator. The minimum is then finely searched on a second line-search scan. Given an initial bracketed interval, the most common line-search methods are

- Golden Section Search: which progressively scans within the brackets, updating it at each iteration so that it shrinks at each round until it spans only a small interval specified by the user. The machine precision ϵ is often indicated. The guess for the minimum is taken as the mid-point along the interval. The minimum point is found to within the precision of $\epsilon/2$.
- Parabolic Interpolation: where a parabola is fitted to the values $f(a), f(b), f(c)$ the function takes along the brackets. Moving along the parabola minimum takes us to f ’s minimum or pretty close to it in a single leap.

The brackets routine and the line-search methods presented rely on the comparison of the objective function at different points in the parameter space. They assume the functions to be deterministic and trust the behaviour and are completely unaware of the experimental noise.

In what follows, we assume what we actually measure in the control-room is $\hat{f}(x) = f(x) + \xi$, where $\xi \sim \mathcal{N}(\mu = 0, \sigma)$ is a random variable modeling the experimental noise, with σ being expected noise error, $\sigma^2 = \text{Var}[\xi]$.

For the optimization of noisy objective functions, RCDS introduces a noise-aware bracketing routine and a parabolic interpolation scan over the bracket interval. For the brackets, instead of seeking for points $a < b < c$ satisfying $f(b) < f(a), f(b) < f(c)$, RCDS requires a more strict condition $f(b) < f(a) + 3\sigma, f(b) < f(c) + 3\sigma$. This increases the likelihood the observed trend consists on real trends of the objection itself, rather than random errors.

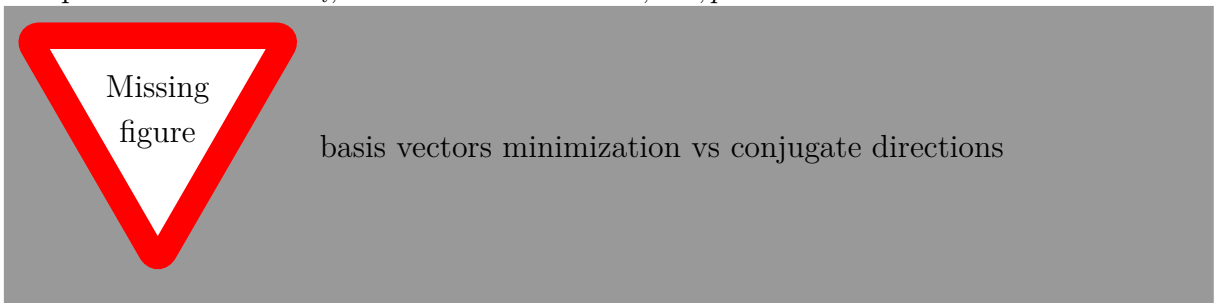
During the line-search, a parabola is fitted within the brackets and its minimum is taken as the objective function minimum. Additionally there is a comparison of the available (previously evaluated) points within the brackets used for the fitting of the parabola. If any of them is considered an outlier, it is discarded and the fitting is repeated without it.



3.3.2 Powell's conjugate direction set

How could we optimize an objective function $f(\mathbf{x}) \in \mathbb{R}$ depending on the set of p parameters $\{x_i\}_{i=1,\dots,p}$? The simplest idea is to iteratively optimize nudging each knob individually: optimize f by changing x_1 , while the other knobs remain fixed. Next, optimize by changing x_2 only, and so forth. In other words, each one of the knobs defines a direction whose basis vector is $\hat{\mathbf{e}}_i$, corresponding to a unit change of the knob. This is easy to automate with the noise-robust line-optimizer introduced in the previous section.

Formally, we are reducing a multi-dimensional optimization problem into a series of line-searches. That is, given an initial configuration of the parameters (an initial position) \mathbf{x}_0 , and a direction $\hat{\mathbf{n}}$, we have the one-dimensional problem to minimize $g(\delta) = f(\mathbf{x}_0 + \delta\hat{\mathbf{n}})$. The minimum is then $f(\mathbf{x}_0 + \delta_*\hat{\mathbf{n}})$, where $\delta_* = \arg \min_{\delta} g(\delta)$. In the previous paragraph, we specialized to $\mathbf{n} = \hat{\mathbf{e}}_i$, and iterated for $i = 1, \dots, p$.



As can be seen in figure, scanning along each orthogonal direction can be time-consuming, specially for some functions with long narrow valleys at some angle with the coordinates basis vectors. This strategy thus is suboptimal when evaluation of the objective function is expensive.

The reason why using unit basis vectors can be so inefficient is because optimizing along a given basis vector spoils down minimization carried out in the any other of them. So the processes needs to be iterated. A more efficient strategy consists on constructing a set of special non-interfering direction vectors for which the minimizations are preserved when optimizing in a different direction.

The necessary condition for direction vectors \mathbf{u} and \mathbf{v} to be non-interfering is (proof in the appendix)

$$\mathbf{v} \cdot \mathbf{H} \cdot \mathbf{u} = 0, \quad (3.1)$$

where $(\mathbf{H})_{ij} = \partial^2 f(\mathbf{x}_0) / \partial x_i \partial x_j$ is the Hessian matrix for function f . The \mathbf{u} and \mathbf{v} directions are said to be conjugate directions.

The problem now consists on finding an appropriate set of p conjugate directions, so we can optimize $f(\mathbf{x})$ along them. Let $\{\mathbf{u}_i\}$ denote our directions set. Powell proved conjugate directions can be constructed as follows

1. Set the initial directions as the basis vectors: $\hat{\mathbf{u}}_i = \hat{\mathbf{e}}_i, i = 1, \dots, p$.
2. Save the starting point (initial parameters state) as \mathbf{x}_0 ;
3. For $i = 1, \dots, p$ minimize along $\hat{\mathbf{u}}_i$. Save the minimum as \mathbf{x}_i .
4. For $i = 1, \dots, p - 1$ set $\hat{\mathbf{u}}_i \leftarrow \hat{\mathbf{u}}_{i+1}$
5. Set $\mathbf{u}_p = \mathbf{x}_p - \mathbf{x}_0$. Normalize to obtain $\hat{\mathbf{u}}_p$.
6. Minimize along $\hat{\mathbf{u}}_p$. Name the found minimum as the new \mathbf{x}_0 and repeat the procedure until reaching a certain number of evaluations or until some stopping condition is reached.

That is, from steps 1–3. we optimize along each one of the unit basis vectors, updating the minimum. When finishing optimization along x_p , the current minimum will be \mathbf{x}_p . In step 4 we discard the first direction, rename directions \mathbf{u}_{i+1} to \mathbf{u}_i , and set as our new p th direction the vector from the starting point \mathbf{x}_0 to the the current minimum.

Powell proved that repeating this procedure k times for a quadratic form produces a set of directions whose last k vectors are mutually, pairwise conjugate, in the sense of the Hessian matrix. So p iterations exactly minimizes the quadratic form. The method is also quadratically convergent: each iteration doubles the number of significant figures of the candidate minimum for the quadratic form.

There is a problem in throwing away for $\hat{\mathbf{u}}_1$ for $\mathbf{x}_p - \mathbf{x}_0$ every iteration: at some point the lines start to fold up on each other and lose linear independence. As a result the function can end up minimized only within a subspace of parameter space. To fix this, you can reinitialize the directions to the basis vectors after an iteration along the p directions, or use any new set of orthogonal directions.

The somewhat counterintuitive solution suggested by Powell is to discard not necessarily $\hat{\mathbf{u}}_1$ in favor of the new direction, but the direction along which f had its largest decrease so far. This is justified because this direction is likely have a largest component along the new proposed conjugate direction. Accepting this advice results in a set of p directions which are no longer mutually conjugate by the end of p iterations. As a result, the method will no longer be quadratically convergent

Powell also posits some conditions in which is best not to add any new directions, keeping the old set from the previous iteration. These are presented in the appendix, as well as the pseudo-code for the Powell loop.

In summary, Powell's direction set loop calculates and manages directions adaptatively, deciding when to change old directions in favor of newly calculated conjugated vectors, and when to avoid the changes to control build-up of linear dependence

In practice, using conjugate directions accounts to finding a good set of directions in which the number of steps along the vectors is reduced. They provide “shortcuts” towards the minimum in the objective landscape.

CHAPTER 4

Diagnostics tools, measurements processes & experimental setup

This is a "methods" chapter. Its first section presents the available beam diagnostics at the storage ring and describes the experimental measurements of relevant quantities such as beam positions, trajectories and orbits, beam current and lifetime, the tunes and chromaticity and how these are dialed at our will during a study. The last two sections discuss the choice of objective functions to probe the Dynamic Aperture and the appropriate selection of sextupole families as the optimization knobs.

4.1 Diagnostics and measurements at the control room

4.1.1 Beam Position Monitors

To probe the beam's position along the ring, a diagnostic tool consisting on a set of four pick-up antennas placed within the vacuum chamber are used. These are known as Beam-position-monitors (BPMs), and are sketched in the Figure. The antennas are placed in such a manner so the electron beam deposits mirror charges when passing by then and triggers the antenna a certain voltage signal. The determination of the beam displacements is based on the differential signal induced on the antennas when the beam is not at the geometric center, in which case the induced charges are equal. The signal of the antennas is processed in the so-called "Delta/Sigma" scheme, which gives the horizontal and vertical beam displacements according to the following algebra:

$$x = K_x \frac{(A + D) - (B + C)}{\Sigma}, \quad y = K_y \frac{(A + B) - (C + D)}{\Sigma}, \quad (4.1)$$

where A, B, C, D refers to the intensity of the induced signal over the corresponding antenna, $\Sigma = A + B + C + D$ is the sum signal, proportional to the beam's current, and K_x and K_y are calibration factors, which depend on the BPM geometry and distances between the antennas. SIRIUS has 160 BPMs distributed along the storage ring. They

allow for the determination of the centroid's positions at a turn-by-turn acquisition rate, which is needed for probing of the betatron motion. The signal can also be processed in other acquisition rates, which renders an averaging of the signal and allows to probe information about the orbit.



BPMS antennas diagram

4.1.2 Beam Current and Injection Efficiency

Direct-Current Current Transformers (DCCTs) enable the measurement of the stored beam current within accelerator rings (booster or storage ring). A DCCT current monitor works by surrounding the beam of charged particles in the accelerator ring with a magnetic core. The magnetic field induced by the beam current flowing by the core is then measured, allowing for an accurate determination of the current itself.

Utilizing the current measurement and the beam revolution period in the respective ring, one can assess the stored charge, and calculate the injection efficiency during storage ring injections. By estimating the charge in the booster or transport line just before injection into the storage ring and the storage ring charge immediately after the injection pulse, it is possible to deduce the efficiency of the injection process. The efficiency of the injection can also be estimated from the sum-signal of the BPMs, since it is proportional to the stored current.

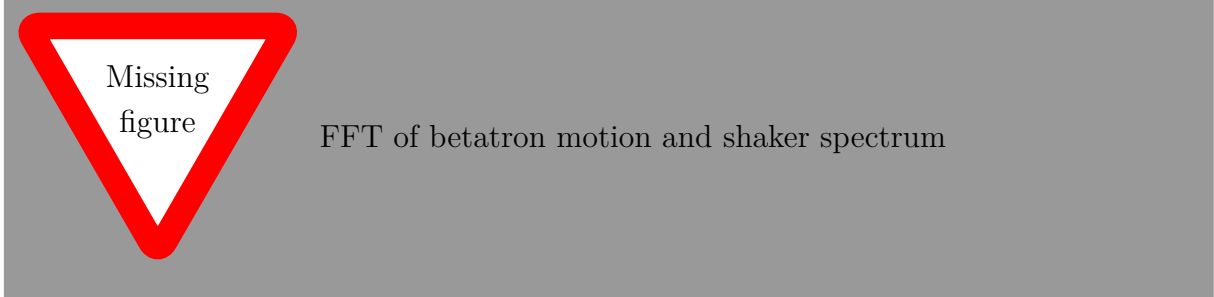
what is the accuracy and precision of the current measurements with the DCCT? what are its limitations? what about the sum-signal

4.1.3 Tunes measurement & control

When turn-by-turn motion is viewed at a fixed longitudinal position s , it consists on the sampling of a harmonic motion. Its fundamental frequency is the tune ν . Any observation of Turn-by-turn (TbT) motion can reveal the tunes upon the appropriate signal processing. For instance, the betatron motion can be Fourier-transformed (discrete Fourier transform via fast-fourier transform algorithm), revealing the BPM signal spectrum. Alternatively the time-domain signal can be fitted to a sinusoid, allowing the determination of the tune as the fundamental frequency.

Precise measurement and online monitoring of the tunes in an accelerator ring can be achieved with the aid of a stripline shaker, which constantly drives the beam with an

alternating electric field in a narrow of frquencies, leading to sub-nanometer displacements and inducing small-amplitude, noninterfering with operation betatron motion. The same system also reads back the beam response at that same frequency range. The peak of the beam response signal is identified with the betatron tune.



As for changing and manipulating the tunes, formula (2.24) reveals that changes in the quadrupoles strengths, specially at the quadrupoles at large β -function sections, allow for the control of the tunes. Since the tune response to quadrupole strength changes is linear, a tune-response matrix can be constructed, i.e. the Jacobian of the tunes with respect to changes in quadrupoles, so that tune changes can be expressed as

$$\Delta\nu = \mathbf{J}_\nu \Delta\mathbf{K}, \quad (4.2)$$

where $\Delta\nu = [\Delta\nu_x \ \Delta\nu_y]^\top$ is the tune-shifts vector, $\Delta\mathbf{K}$ is the vector containing the changes in strengths across all the quadrupole families, and the Jacobian or response matrix has entries

$$(\mathbf{J}_\nu)_{ij} = \frac{\partial \nu_i}{\partial K_j} \approx \frac{\Delta \nu_i}{\Delta K_j}, \quad i = x, y, \quad j \in \text{quadrupole families}. \quad (4.3)$$

The system can pseudo-inverted, allowing for the determination of quadrupoles changes required for a desired tune change

$$\Delta\mathbf{K} = \mathbf{J}_\nu^+ \Delta\nu \quad (4.4)$$

where $\mathbf{J}_\nu^+ = (\mathbf{J}_\nu^\top \mathbf{J}_\nu)^{-1} \mathbf{J}_\nu^\top$ is the Moore-Penrose pseudoinverse.

which families are used when changing tunes? add discussion on chaging the optics when changing tunes

4.1.4 Chromaticity measurements & control

Chromaticity characterizes the energy-dependent tune-shift. To measure it, we need to calculate the numerical derivative

$$\xi_u = \frac{\partial \nu_u}{\partial \delta} \approx \frac{\Delta \nu_u}{\delta},$$

that is, measure the tune-shift $\Delta\nu_u$ induced by the energy-shift δ . A direct manner to induce a particular energy-shift is to change the RF cavities frequency (see annexes for brief overview of longitudinal dynamics and details about momentum compaction). A relation can be established between energy deviations δ and relative RF frequency changes with the aid of a quantity α , known as *momentum compaction factor* [14, 16]:

$$\delta = -\frac{1}{\alpha} \frac{\Delta f}{f}. \quad (4.5)$$

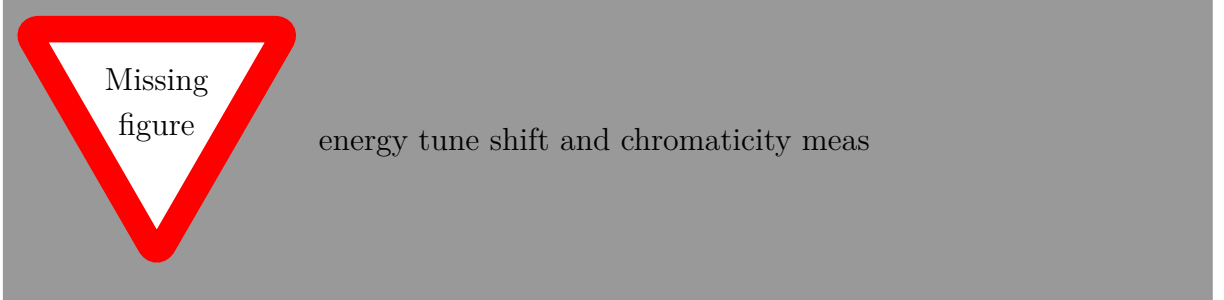
The momentum compaction factor relates changes in orbit length with energy deviations and is defined by

$$\alpha = \frac{1}{L} \oint G(s)\eta(s) ds. \quad (4.6)$$

Therefore, in practice, when measuring chromaticity we are interested in the numerical derivative

$$\xi_u = -\frac{f}{\alpha} \frac{\Delta\nu_u}{\Delta f} \quad (4.7)$$

which is obtained as the first-degree coefficient (properly normalized by α/f) of the polynomial fitting of the tune-shift vs. RF frequency curve. A typical tune-shift curve is shown by Fig.



As eq. (2.32) shows, chromaticity depends linearly on the chromatic sextupole families strengths. It can thus be dialed to certain desired values according to the same pseudo-inversion procedure described above for the tunes. We relate the chromaticity changes $\Delta\xi \in \mathbb{R}^2$ to the sextupole families strength changes $\Delta\mathbf{S} \in \mathbb{R}^{d_s}$ by

$$\Delta\xi = \mathbf{J}_\xi \Delta\mathbf{S}, \quad (4.8)$$

where $\Delta\xi = [\Delta\xi_x \ \Delta\xi_y]^\top$ and the Jacobian matrix $\mathbf{J} \in \mathbb{R}^{2 \times d_s}$ has entries

$$(\mathbf{J}_\xi)_{ij} = \frac{\partial \xi_i}{\partial S_j} \approx \frac{\Delta \xi_i}{\Delta S_j}, \quad i = x, y, \quad j \in \text{sextupole families}. \quad (4.9)$$

d_s refers to cardinality of the set of sextupole families used in the chromaticity change process. In principle, at least two families are required for correcting/tuning chromaticity in the machine: one family for each plane. Since the chromatic sextupole families are the only ones effectively changing chromaticity to leading order, then, at most, $d_s = 15$.

If we wish to change chromaticity by a $\Delta\xi$ amount, the jacobian can be pseudo-inverted to calculate the required sextupole strength changes:

$$\Delta\mathbf{S} = \mathbf{J}_\xi^+ \Delta\xi. \quad (4.10)$$

In practice the chromaticity jacobian was never actually measured in the real machine, due to the time-consuming process of varying a single sextupole family, carrying out the chromaticity measurement and repeating the process for the 15 chromatic families. The "measurement" is instead carried out in the SIRIUS storage ring computer model. The model-calculated jacobian renders a satisfactory correction or tuning of the chromaticity in the actual machine.

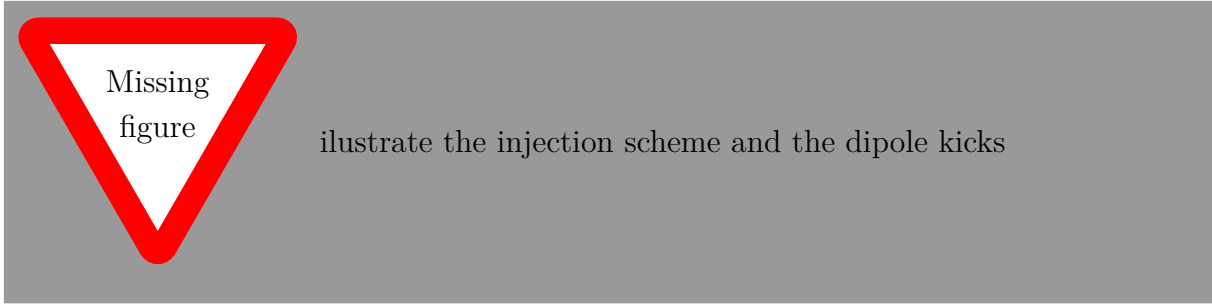
which families are used for correcting

4.2 The choice of objective function & optimization knobs

4.2.1 The objective function

There is no analytical formula relating the storage ring linear or nonlinear optics to the Dynamic Aperture (DA). The optimization procedure must be a heuristic search procedure: changes are performed to the knobs (nonlinear magnets) and the effect on the DA is evaluated. Additionally, one cannot measure the DA in a practical and straightforward measurement procedure sufficiently fast to be run online. Direct measurements of DA can take several iterations of acquiring trajectories of the beam with increasingly higher transverse displacements. The acquisitions are then processed to access the DA. For online optimization, one must choose a practical, easy-to-measure objective function to act as a probe to the DA: a figure of merit related to the dynamic aperture to represent it and to be used to evaluate the quality of the changes performed during the online tuning process.

In our experiments, we studied using two practical objectives as the probes for DA: the **injection efficiency** and the **beam's resilience to dipolar perturbations**. The former is quite self-explanatory: the larger the dynamic aperture, larger the space for the beam to be captured into the storage ring during the injection pulse, and thus the larger the injection efficiency. The latter is related to the DA by the following: the larger the horizontal dipolar kicks the beam can survive, the larger the orbit distortions towards the positive or negative horizontal plane (depending on the kick direction). So the larger the amplitudes the beam explores as it oscillates, probing the DA borders. If the beam survives to large kicks, it means the ring can accommodate larger orbit distortions because of an increased DA.



In summary, the dynamic aperture optimization procedure must consist on the exploration of sextupole (knobs) configurations yielding the largest dynamic aperture as accessed by as objective function such as injection efficiency or beam kick-resiliency.

4.2.2 The optimization knobs

The DA is determined by the quality of the beam dynamics in terms of perturbations. Given that a linear optics correction scheme is already in place and regularly implemented in the machine, effectively addressing optics functions and phase advances, the primary factor impacting SIRIUS DA likely stems from nonlinear dynamics and/or remaining uncorrected and previously inaccessible deviations and errors. This may include sextupole field errors or other minor nonlinear multipoles.

If the limitation of the DA is likely associated with nonlinear dynamics, the actuation knobs must unexpectedly be composed of the controllable nonlinear magnets available at the SIRIUS storage ring, namely the sextupoles. However, it is important to note that sextupole strengths cannot be changed arbitrarily. Sextupoles are originally introduced into the lattices as actuators for correcting chromaticity, which refers to the energy-dependent aberrations in the focusing of the beam. Care must be taken when varying the sextupole strengths, as it can alter the chromaticity. A strategy needs to be devised to select the sextupole family in a way that allows for the simultaneous correction of chromaticity and the online tuning of magnet strengths to optimize the DA. In simpler terms, the optimization processes for DA should be conducted while preserving the machine's chromaticity. The natural question that arises is how to implement these isochromatic changes to the sextupoles.

SIRIUS has 21 sextupole families: magnets powered by the same power supply. 6 of them are achromatic sextupoles. They are placed where the dispersion is zero. The 15 other families are chromatic families. Table 4.1 shows the 21 sextupole families names.

add figure of each family for a superperiod, add the number of magnets for each family

In principle, thus, the optimization parameter space is 21-dimensional. In reality, as mentioned, we would like to change sextupoles without changing chromaticity. Since we need at least one degree of freedom for correcting chromaticity in the horizontal

Table 4.1: SIRIUS sextupole families

| | |
|------------|-------------|
| achromatic | SFA0, SDA0, |
| | SFB0, SDB0, |
| | SDP0, SFP0 |
| chromatic | SDA1, SFA1, |
| | SDA2, SFA2, |
| | SDA3, |
| | SDB1, SFB1 |
| | SDB2, SFB2, |
| | SDB3, |
| | SFP1, SDP1, |
| | SDP2, SFP2 |
| | SDP3 |

plane and one degree of freedom for correcting the chromaticity in vertical plane, there are 19 independent knobs available. The dimensionality of the search space can be further reduced by imposing additional constraints to certain families variations.

Throughout the experiments, two strategies were adopted to select the sextupole optimization knobs. A comapensation scheme and the constrained-families Jacobian null-space knobs.

Compensation scheme

The idea is the following: at least two chromatic sextupole families are labeled "correction" or "compensation" families and are not freely varied during the experiment. The other 13 chromatic families can be varied arbitraly, respecting their linear (non-saturation) regime. Alongside these, the achromatic sextupole families are also free knobs. Everytime the free families strengths are changes, the chromaticity change caused by this action is anticipated: the reduced Jacobian, $\tilde{\mathbf{J}}_{\xi}$, whose columns contain only the "free" knobs columns, is used to calculate the chromaticity change $\Delta\xi$. Another reduced Jacobian, \mathbf{J}'_{ξ} containig only the columns corresponding to the "correction" or "compensation" families is used to conteract the predicted chromaticity build-up, i.e. to correct produce sextupole changes leading to $-\Delta\xi$ chromtaticity change. The required strength changes in the compensation families is determined by $\Delta\mathbf{S} = \mathbf{J}'_{\xi}{}^{+}(-\Delta\xi)$. Therefore,

Jacobian nullspace knobs

Here the idea is to identify the nullspace of the Jacobian. That is, we are intereseted in the set of vectors $\mathbf{x}_i, i = 1, \dots, 13$ such that $\mathbf{J}_{\xi}\mathbf{x}_i = \mathbf{0}$, so that if we change the strengths along the subspace (nullspace) spanned by them, $\Delta\mathbf{S} \in \text{span}\{\mathbf{x}_i\}$ then the resulting changes in chromaticity are null.

A straightforward way to identify the nullspace of the jacobian is to calulate

its full singular value decomposition, which expresses the jacobian as

$$\mathbf{J}_\xi = \mathbf{U}\mathbf{\Sigma}\mathbf{V}^\top$$

$$= \underbrace{\begin{bmatrix} \vdots & \vdots \\ \mathbf{u}_1 & \mathbf{u}_2 \\ \vdots & \vdots \end{bmatrix}}_{2 \times 2} \underbrace{\begin{bmatrix} \sigma_1 & 0 & \dots & 0 \\ 0 & \sigma_2 & \dots & 0 \end{bmatrix}}_{2 \times 21} \underbrace{\begin{bmatrix} \dots & \mathbf{v}_1^\top & \dots \\ \dots & \mathbf{v}_2^\top & \dots \\ \dots & \mathbf{v}_3^\top & \dots \\ \vdots & \vdots & \vdots \\ \dots & \mathbf{v}_{21}^\top & \dots \end{bmatrix}}_{21 \times 21}$$

Note that the singular-values matrix has only two non-vanishing singular values σ_1 and σ_2 . This is because there are only two independent modes in the Jacobian matrix responsible for the changes in the chromaticity, corresponding to the two degrees of freedom to change the horizontal and vertical chromaticity. The matrix product can be rewritten as

$$\mathbf{J}_\xi = \sum_{i=1}^{21} \sigma_i \mathbf{u}_i \mathbf{v}_i^\top = \sigma_1 \mathbf{u}_1 \mathbf{v}_1^\top + \sigma_2 \mathbf{u}_2 \mathbf{v}_2^\top \quad (4.11)$$

Given the interpretation that the column vectors of the \mathbf{U} matrix, the so-called right-singular vectors, span the Jacobian row-space, the chromaticity space, and that the row vectors of the \mathbf{V}^\top matrix, the left-singular vectors, span the Jacobian column-space, the sextupole families space, then we can easily identify the sextupoles living in the left nullspace of the Jacobian. They must be the ones associated with the vanishing singular values: $\ker(\mathbf{J}_\xi) = \{\mathbf{v}_i | i = 3, \dots, 21\}$.

CHAPTER 5

Experiments and Results

This section presents partial results from the optimization experiments carried out up until now. The early experiments were performed in december 2022, and the latest have been happening since february 2023.

5.0.1 Kick resilience optimization - december 2022

The parameter space (knobs) adopted consisted on the SDA0, SDB0, SDP0, SFA0, SFB0, SFP0, SDA1, SDB1, SDP1, SDA3, SDB3, SDP3, SFA1, SFB1, SFP1 sextupole families. The SDA2, SDB2, SDP2 and SFA2, SFB2, SFP2 families were used keep chromaticity constant when varying the optimization knobs. This was implemented in the following manner: RCDS freely proposed strength variations to the knob families. For each proposed change in strength, the corresponding changes in chromaticity were estimated from a chromaticity jacobian matrix constructed from the model. To the "correction" families were applied the strengths needed to cancel these chromaticity changes. In this first attempt, we tested the optimization routine twice, with different objective functions to probe the dynamic aperture.

- Objective function: kick resilience

The first objective function adopted was the beam loss after dipolar kick from the horizontal dipole kicker. The idea was to minimize the loss at a given kick, and progressively increase the kicks, to probe larger acceptances. The BPMs acquisition was fired in synchrony with the dipole kick and beam-loss was calculated by comparing the sum-signal¹ of the beam's first 10 turns with the sum-signal of the last 10 turns. As for the strength of the dipole kick, we set a horizontal kick of $\Delta x' = -0.760$ mrad, which rendered about 35 - 40% of beam-loss.

- Experiment:

With the aforementioned scheme for changing strengths in the sextupole families, RCDS was started to minimize the beam-loss upon the horizontal kick. In the

¹BPMs determine the relative changes in position of the beam centroid from the differential image charges the beam induces in the device's four antennas. The sum-signal consists on the sum of the signal from all the antennas and, up to a scale, represents the total beam current. Relative changes in sum-signal correspond to relative changes in beam current.

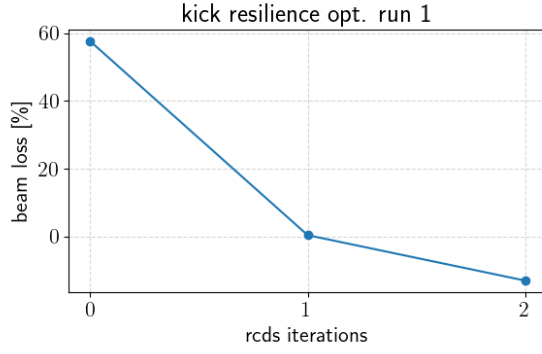


Figure 5.1: Objective function history vs. iterations of the first trial at beam-loss optimization.

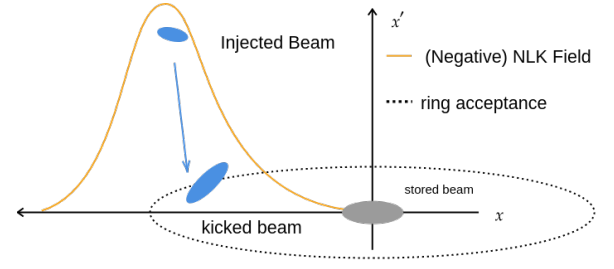


Figure 5.2: Injection conditions for DA optimization

algorithm's first iteration², beam loss dropped from 60% to nearly 0% (Figure 5.1). In the beginning of the 2nd iteration, the objective function took negative values (an artifact) and we stopped the optimization run.

- Results:

The beam-loss minimization significantly improved the beam's resiliency to dipole kicks. After the optimization, it was necessary to kick the beam at approximately $\Delta x' = -0.850$ mrad to achieve the same 30–40% beam-loss rate previously achieved by a $\Delta x' = -0.760$ mrad kick. By the end of this first attempt, the machine magnets were cycled³ and the configurations found during optimization were loaded. When trying to inject in the nominal off-axis scheme, the efficiency was quite low. The improved kick resilience, however, was preserved. This raised the suspicion that the aperture along the negative horizontal direction might have been negatively impacted by the procedure, while the aperture in x' increased. This observation motivated the adoption of injection efficiency to probe the DA.

5.0.2 Injection efficiency optimization - december 2022

The first attempt at optimizing DA by minizing beam-loss revealed that the optimization procedure did not improve injection efficiency. We started another attempt, using the injection efficiency itself as objective function. The knobs (parameter space) used were the same as in the beam-loss optimization.

- Objective function & setup:

The off-axis injection efficiency was worsened by reducing the NLK strength so the

²An RCDS iteration is reached upon completing the one-dimensional optimization along all directions in the parameter space. After each iteration, the algorithm constructs a new (conjugate) direction according to Powell's method and may replace existing directions by this new conjugate direction.

³Cycling or standardizing magnets consists on driving their power supplies with decaying sinusoidal waveforms to remove hysteresis effects and bring the magnets yokes to their standard reference magnetization.

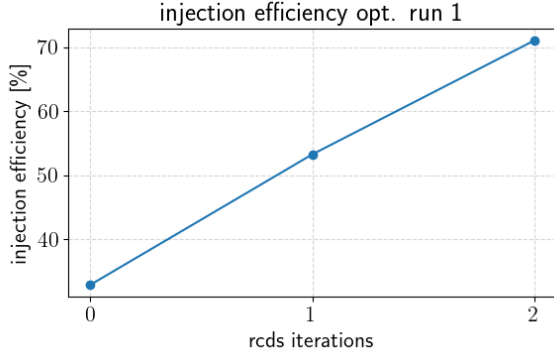


Figure 5.3: Objective function vs iterations during the first run of injection efficiency optimization

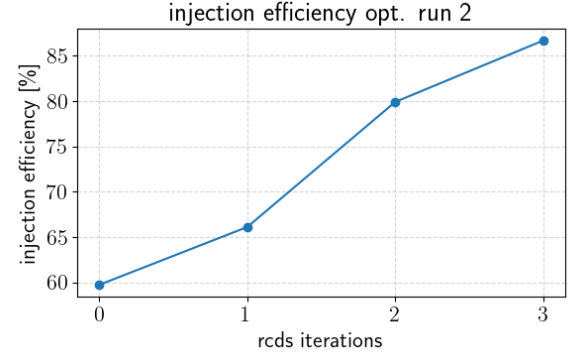


Figure 5.4: Objective function vs iterations during the second run of injection efficiency optimization

beam was injected in the upper-left border of the (x, x') aperture (see Figure 5.2). The efficiency under such conditions was about 30%. The maximization of injection efficiency under such injection conditions should correspond to a maximization of the DA evenly among the x and x' directions, as opposed to the increase on the x' direction only, as seemed to be the case in the previous attempt.

- Experiment:

In the first run, within three iterations the injection efficiency reached 70%, as shown by Fig. 5.3. The algorithm stopped as it reached the maximum number of the objective function evaluations. A second run was launched, starting from the sextupole configurations just found in the first run. In four iterations, 85% efficiency was reached, as Fig. 5.4 shows.

- Results:

When the NLK strength was restored to the reference value, meaning the nominal off-axis injection conditions were restored (in which the beam “lands” not at the border but within the acceptance), the injection efficiency fluctuated around 95–100% with good repeatability. There was a severe reduction in beam lifetime by the end of the last optimization trial. Measurement indicated 54.12 hrs lifetime at 15 mA current, while, the reference (non-optimized) configuration, lifetime at this same current is about 68 hrs.

We carried out chromaticity measurements in the machine loaded with the reference configuration (ref-config) and with the sextupole configurations found at iterations 0, 2, and 3 of the last injection efficiency optimization run (run shown by Fig. 5.4). Table 5.1 presents the measured values, from which we can note the chromaticity changes despite the efforts to anticipate and compensate them when applying changes to the sextupoles. It was later realized, due to the success of the optimization experiments throughout 2023, that the undesired changes in chromaticity are probably not related to this compensation scheme

itself, but rather by the choice of sextupole families operating close to their saturation strengths. Under such conditions, the applied fields are not repeatable, and the excited fields might not correspond to the correct values required to control chromaticity.

| machine configuration | ξ_x | ξ_y |
|-----------------------|-----------------|-------------------|
| ref-config | 2.33 ± 0.02 | 2.531 ± 0.008 |
| iter 0 | 2.59 ± 0.02 | 3.700 ± 0.008 |
| iter 2 | 2.72 ± 0.04 | 3.704 ± 0.008 |
| iter 3 | 2.76 ± 0.05 | 3.510 ± 0.01 |

Table 5.1: Chromaticity measurements for ref-config and sextupole configs. found at the second round of injection optimization

In summary, in these early attempts in december 2022 it was realized that beam-loss minimization/kick resilience maximization does not necessarily leads to injection efficiency improvements. The $x - x'$ phase space seems to be “elastic” and the dynamic aperture can be deformed preferably along x or x' directions, rather than being uniformly increased, as the experiences in other accelerators suggests.

The injection efficiency optimization was successful, but at the expense of a significant decrease in beam lifetime. Undesired chromaticity changes were also observed.

5.0.3 Optimization experiments throughout 2023

In 2023, optimization experiments were carried in the machine configurations with the nominal tunes $(\nu_x, \nu_y) = (49.08, 14.14)$, Working Point 1, as well as in the $(49.20, 14.25)$ and $(49.16, 14.22)$ tunes, Working Points 2 and 3 (WPs 1, 2, 3). Results reported here have also been presented in Ref. [?] (on WPs 1 and 2) and on the presentation delivered at the Optics Tuning and Corrections for Future Colliders Workshop.

The major differences from the previous experiments consisted on

- the use of the average injection efficiency of 5 injection pulses at 2 Hz objective function to reduce the experimental noise sigma from $\sigma = \pm 8\%$ to $\pm 1\%$.
- Families SFP1 and SFB1 were not used as knobs in the optimization experiments since they operate close to their saturation strengths, where hysteresis effects become significant.
- Knobs selection was based in choosing linear combinations spanning null space of the chromaticity response matrix for Working Points 1 and 2. See Ref. [?] for details. Working Point 3 knobs were chosen as described in section 9.1.

Optimization in Working Point 1

Three configurations were found, which resulted from optimizing the objective, loading the best configuration found and continuing the optimization from the previous run's best.

For each one of the best configurations found during runs 1, 2 and 3 and also for the non-optimized reference configuration (ref. config.), turn-by-turn (TbT) BPM data of the stored beam kicked with the horizontal dipolar kicker were acquired. The DCCT current monitor allowed the determination of the current losses as a function of the horizontal kicks, which is shown by Figure 5.5. TbT data also allowed for the reconstruction of the (x, x') phase space of the beam under the influence of the kicks. Using two BPMs at the ends of an empty ID straight section, the position and angle of the beam were determined at each turn. Figure 5.7 shows the measured phase spaces for the ref. config. and the best configurations found during run 1, 2, and 3, at the fifth straight section (SA05), which is a high-beta section with identical optics to the injection point. In the measurement, the beam was under the influence of kicks rendering approximately the same current loss of 12%.

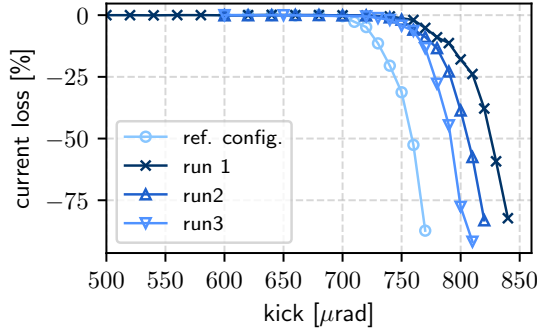


Figure 5.5: Current losses vs. horizontal dipole kick for the ref. config. and for the RCDS solutions at WP 1.

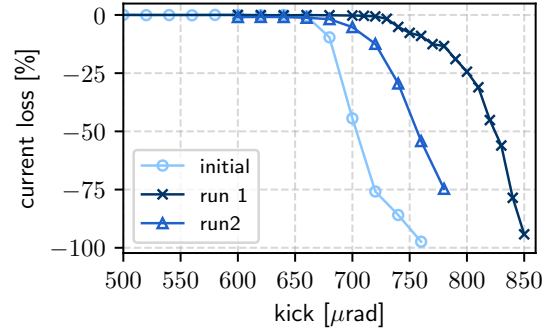


Figure 5.6: Current losses vs. horizontal dipole kick for the initial configuration and the RCDS solutions at WP 2.

Table 5.2 compiles the injection efficiencies (IE) achieved for each configuration during off-axis NLK injection in normal injection conditions ($x \approx -8.5$ mm, $x' \approx 0$). Again we stress that the point regarding the maleability of the phase portrait ellipses deformations: the configuration with the largest kick resilience, that of run 1, is not the one with the largest phase space area and IE performance. This could be explained if the phase space deformations of the ellipse at the kicker location for this sextupole setting resulted in a larger x'/x ratio, which would account for a larger kick acceptance and the worse injection performance compared to run 2.

Lifetime at 60 mA was measured at 20 hr for run 2 best configuration. Lifetime at the same conditions for the reference configuration is 21 hr. No significant chromaticity changes were observed: (2.33, 2.53) in ref. config. vs. (2.24, 2.39) in run 2 best solution.

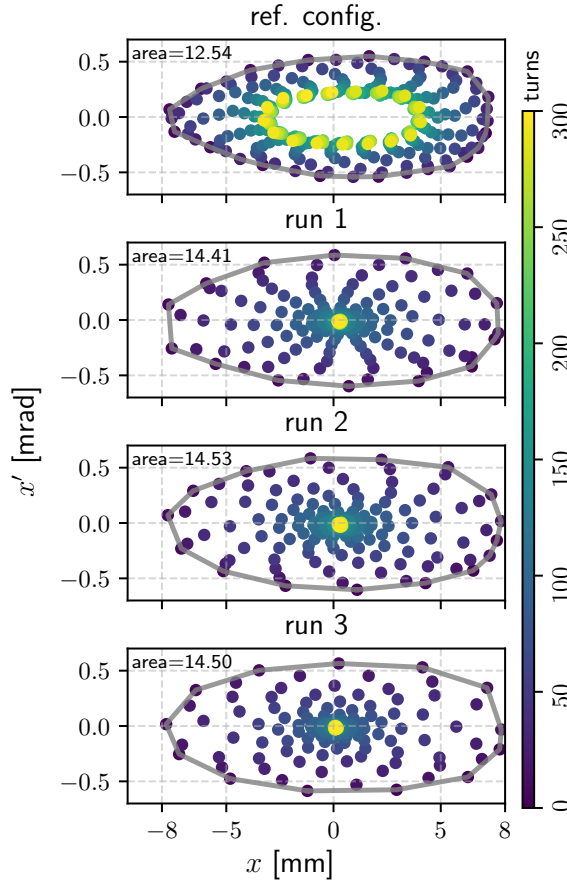


Figure 5.7: Measured phase space at SA05 high-beta straight section for the ref. config. and the best RCDS configurations of runs 1, 2 and 3 in WP 1. Color-map indicates the turns. The areas are in mm mrad. The beam was being kicked horizontally at 730 μ rad in the ref. config, 790 μ rad in run 1, 780 μ rad in run 2, and 770 μ rad, in run 3. Loss rates of 12%, 11%, 13% and 13%.

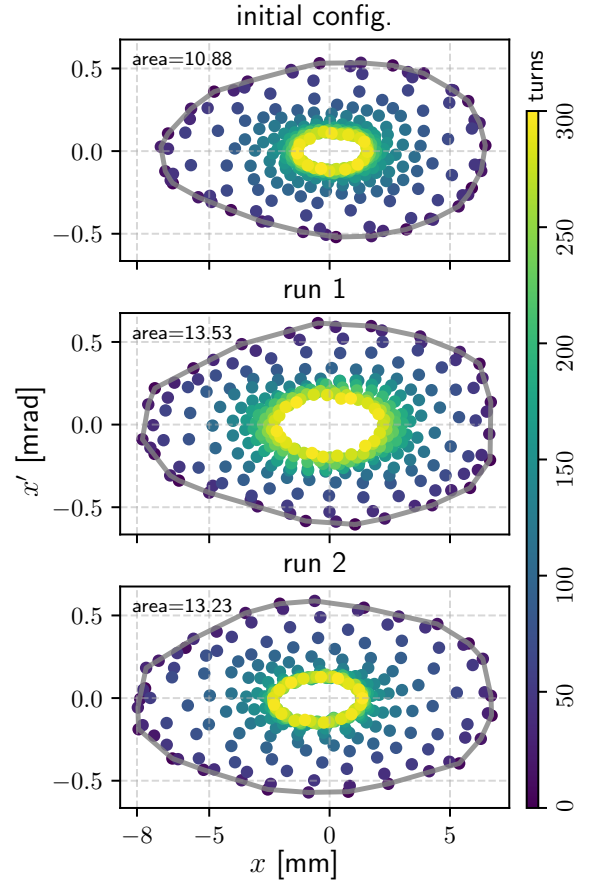


Figure 5.8: Measured phase space at SA05 high-beta straight section for the initial configuration and the best RCDS configurations of runs 1 and 2 in WP 2. Color-map indicates the turns. The areas are in mm mrad. The beam was being kicked horizontally at 680 μ rad, for the initial configuration, 770 μ rad for run 1, and at 720 μ rad for run 2. Loss rates of 10%, 12% and 12%, respectively

Optimization in Working Point 2

In working point 2, two configurations were found: Run 1 and Run 2. The sextupoles were optimized from scratch from a configuration with the new tunes and then, from the best solution found, another round was launched.

TbT BPM data of the kicked stored beam in the initial configuration (non-optimized) and in each run's best solution was acquired and allowed the determination of current losses vs. kicks, shown in Fig. 5.6, and the reconstruction of phase space, shown in Fig. 5.8. Table 5.2 compiles injection efficiencies achieved for the configurations in the new tunes during nominal off-axis injection. The configuration found during run 1 rendered the best IE, the largest kick resilience, a larger lifetime than the initial configuration (21 hrs, run 1 vs. 18 hrs, initial, at 60 mA), and the largest phase-space area increase.

Table 5.2: Injection efficiencies (IE) for configurations found for Working Points 1, 2 and 3.

| working point 1 | | working point 2 | | working point 3 | |
|-----------------|------------|-----------------|------------|-----------------|------------|
| configuration | IE [%] | configuration | IE [%] | configuration | IE [%] |
| ref. config. | 88 ± 8 | initial | 51 ± 1 | initial | |
| run 1 | 91 ± 1 | run 1 | 79 ± 3 | optimized | 93 ± 3 |
| run 2 | 98 ± 1 | run 2 | 65 ± 1 | | |
| run 3 | 87 ± 3 | | | | |

Optimization in Working Point 3

Two optimization runs were carried out, starting from sextupole settings of the reference configuration of the nominal tunes. Best configuration found at run 1 was loaded and run 2 was launched. The resulting configuration displayed injection efficiency of $93 \pm 3\%$ during nominal off-axis injection. Lifetime at 60 mA was measured at 19.5 hrs, so no significant reductions were observed.

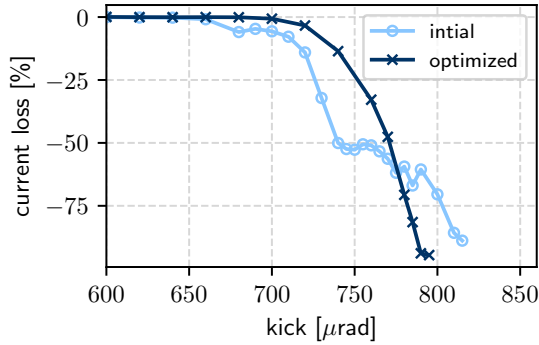


Figure 5.9: Current losses vs. horizontal dipole kick for the initial configuration and the RCDS solution at WP 3

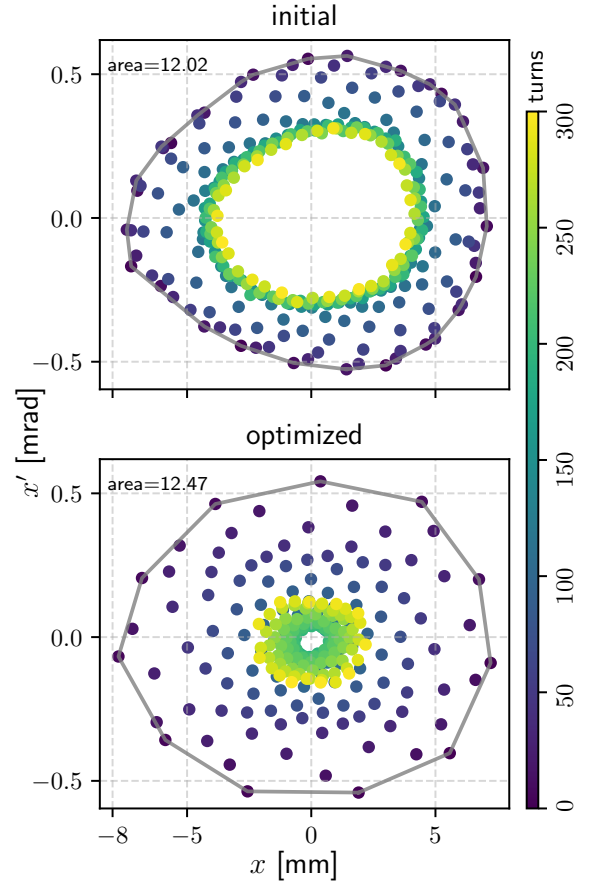


Figure 5.10: Measured phase space at SA05 high-beta straight section for the non-optimized configuration and the best RCDS configuration in WP 3. Color-map indicates the turns. The areas are in mm mrad.

Orbit stability improvements were confirmed by the orbit integrated spectrum density, which decreased by a factor of approximately 2 [?]. Orbit rms variations reached

the record values of less than 1% of the horizontal beam size, in the horizontal plane, and less than 4% of the vertical beam size in the vertical plane.

In summary, in the experiments throughout 2023, the noise in the objective function was reduced and the injection efficiency average was established as the standard objective. No significant chromaticity changes were observed during/after the optimization runs, nor significant changes to beam lifetime, compared to the nominal working point reference configuration.

Excellent configurations were found in WP1, with 98% injection efficiency, but we still believe there is room for further improvements in the higher tunes configurations.

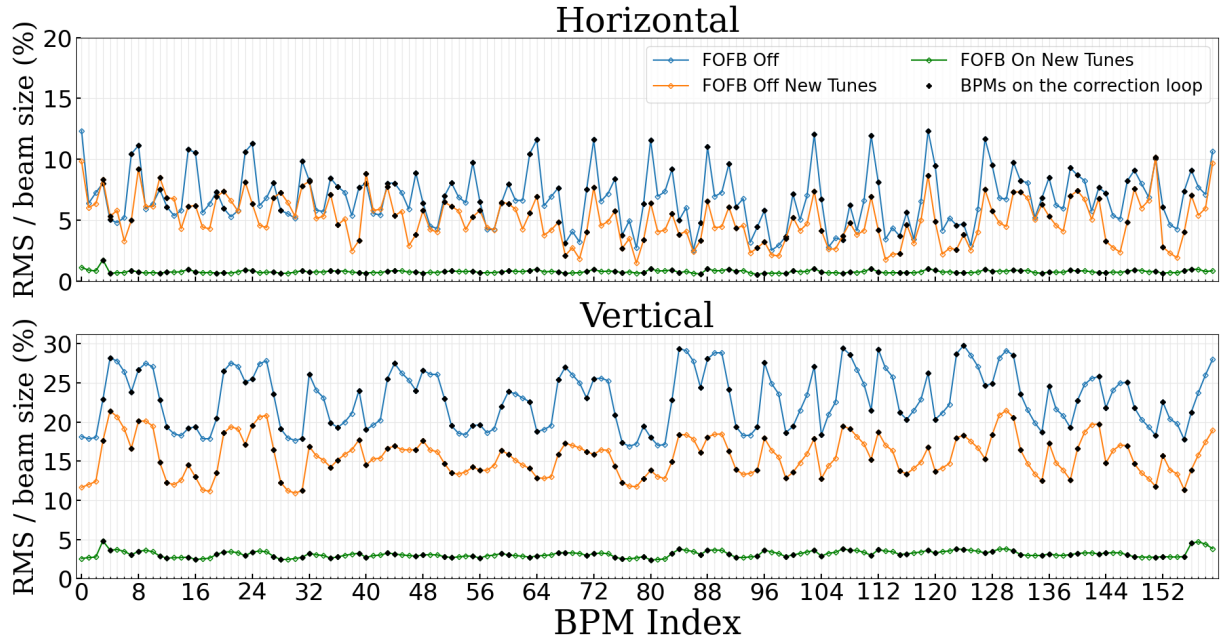


Figure 5.11: Horizontal/Vertical RMS orbit variations in units of the horizontal and vertical beam sizes. Blue curves represents variations in the nominal working point, WP1, orange curves are the orbit variations at WP3, and green curves variations at WP3 plus results of the recent improvements in Fast Orbit Feedback System. From [?]

5.1 Conclusions

The MSc. project is being developed on schedule and should be completed within the stipulated duration of the grant. In the reported period from August 2022 to July 2023 the student has completed the graduate program requirements for course credits, co-authored and collaborated in the writing of computer code for performing machine experiments, participated in the experiments and performed all the analysis of the obtained data. The student has also co-authored and submitted contributions to IPAC'23, the largest conference in the field of particle accelerators, and presented the results achieved so far during the project in the Optics Tuning and Corrections for Future Colliders Workshop, at CERN.

The work developed alongside the LNLS Accelerator Physics Group has contributed to the recent achievements of record orbit stability at the SIRIUS storage ring.

More experiments for further optimization, exploration of working points and characterizations of nonlinear dynamics performance should proceed in the upcoming months up until the end of the year, when the student should then focus in the writing of his dissertation.

CHAPTER 6

Discussion and Conclusions

Bibliography

- [1] Huang, X. *Beam-based Correction and Optimization for Accelerators* (CRC Press, 2019). Google-Books-ID: y0PBDwAAQBAJ.
- [2] Wolski, A. *Beam Dynamics In High Energy Particle Accelerators* (World Scientific, 2014). Google-Books-ID: 8c63CgAAQBAJ.
- [3] Wiedemann, H. *Particle Accelerator Physics*. Graduate Texts in Physics (Springer International Publishing, Cham, 2015). URL <http://link.springer.com/10.1007/978-3-319-18317-6>.
- [4] Huang, Z. Brightness and Coherence of Synchrotron Radiation and FELs. *Free Electron Lasers* (2013).
- [5] Hettel, R. Challenges in the Design of Diffraction-limited Storage Rings. *Proceedings of the 5th Int. Particle Accelerator Conf. IPAC2014*, 5 pages, 0.551 MB (2014). URL <http://jacow.org/ipac2014/doi/JACoW-IPAC2014-MOXBA01.html>. Artwork Size: 5 pages, 0.551 MB ISBN: 9783954501328 Medium: PDF Publisher: JACoW Publishing, Geneva, Switzerland.
- [6] Simoulin, V. The synchrotron generations. *Revue francaise de sociologie* **57**, 503–528 (2016). URL https://www.cairn-int.info/article-E_RFS_573_0503--the-synchrotron-generations.htm. Bibliographie_available: 1 Cairndomain: www.cairn-int.info Cite Par_available: 1 Publisher: Presses de Sciences Po.
- [7] Liu, L. & Jr, H. W. Towards Diffraction Limited Storage Ring Based Light Sources (2017).
- [8] Liu, L., Neuenschwander, R. T. & Rodrigues, A. R. D. Synchrotron radiation sources in Brazil. *Philosophical Transactions of the Royal Society A* (2019). URL <https://royalsocietypublishing.org/doi/10.1098/rsta.2018.0235>. Publisher: The Royal Society Publishing.
- [9] Liu, L. *et al.* Status of Sirius Operation. *Proceedings of the 13th International Particle Accelerator Conference IPAC2022*, 4 pages, 0.882 MB (2022). URL <https://jacow.org/ipac2022/doi/JACoW-IPAC2022-TUPOMS002.html>. Artwork Size: 4 pages, 0.882 MB ISBN: 9783954502271 Medium: PDF Publisher: JACoW Publishing, Geneva, Switzerland.
- [10] Liu, L., Oliveira, A. & Tavares, D. Status of SIRIUS operation with users (2022).

- [11] Liu, L., Resende, X. R. & Rodrigues, A. R. D. Injection Dynamics for Sirius Using a Nonlinear Kicker 3 (2016).
- [12] de Sá, F. H., Liu, L. & Resende, X. R. Optimization of Nonlinear Dynamics for Sirius (2016).
- [13] Dester, P. S., Sá, F. H. & Liu, L. Energy acceptance and on momentum aperture optimization for the Sirius project. *Journal of Physics: Conference Series* **874**, 012068 (2017). URL <https://doi.org/10.1088/1742-6596/874/1/012068>. Publisher: IOP Publishing.
- [14] Lee, S.-Y. *Accelerator Physics* (World Scientific, 2004). Google-Books-ID: VTc8Sdld5S8C.
- [15] Landau, L. D. L. E. M. *The Classical Theory of Fields: Volume 2* (Butterworth-Heinemann, 1975). Google-Books-ID: X18PF4oKyrUC.
- [16] Sands, M. The Physics of Electron Storage Rings: An Introduction. *Conf. Proc. C* **6906161**, 257–411 (1969).

APPENDIX A

Proof of the necessary condition for vectors conjugacy

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APPENDIX B

Algorithms Pseudocode

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APPENDIX C

Momentum Compaction Factor and the relation between energy deviations and RF frequency changes

Momentum compaction factor is the quantity characterizing the energy/momentum dependence of revolution time/frequency of orbits. The path length traversed by a particle reads up to first order reads

$$d\ell = (1 + G(s)x)ds \quad (\text{C.1})$$

where $x(s) = x_\beta(s) + \eta(s)\delta$. For $\delta = 0$ we have simply

$$L = \oint (1 + G(s)x_\beta(s)) ds$$

thus the additional length traversed by an off-energy particle reads

$$\delta\ell = \oint G(s)\eta(s)\delta ds \quad (\text{C.2})$$

thus we can write

$$\frac{\delta\ell}{L} = \alpha\delta$$

by defining the *momentum compaction factor*:

$$\alpha = \frac{1}{L} \oint G(s)\eta(s) ds \quad (\text{C.3})$$

For relativistic electrons, the increase in energy leads to enlargement of orbits with negligible increase of velocity. Thus, the orbit revolution time decreases. This apparently paradoxical result.

$$\frac{\Delta T}{T} = \left(\alpha - \frac{1}{(v/c)^2 \gamma^2} \right) \delta$$

where $\delta = \Delta E/E$. For $v \rightarrow c$, (large γ), we have

$$\frac{\Delta T}{T} = \alpha \frac{\Delta E}{E}$$

or, equivalently

$$\frac{\Delta f}{f} = -\alpha \frac{\Delta E}{E}$$

For non-relativistic electrons, the increase in energy leads to increase of velocity and the orbit time remains fixed. This is what makes cyclotrons possible.