

Q1

XOR is a function which isn't linear.

A single layer perceptron isn't able to classify the non-linear func<sup>n</sup>.

Therefore, by introducing multiple layers of ~~the~~ perceptrons, (MLP) we remove the linearity of the ~~func~~ model, helping us to classify non-linear func<sup>n</sup>.

Q2

A linear relation would be of type :  $\hat{y}_1 = \beta_0 + \beta_1 x$

Multiple layers of same type would result in:

$$\hat{y} = (\beta_0 + \beta'_0 + \beta''_0) + (\beta_1 + \beta'_1 + \beta''_1)x$$

$$= \beta_0 + \beta_1 x + \beta'_0 + \beta'_1 x + \dots$$

$$= \hat{y}_1 + \hat{y}_2 + \dots$$

↳ This is result of just addition

of multiple linear ~~func~~ func<sup>n</sup>.

∴ linear layers stacked on linear layers remain linear.

In deep neural networks, ~~extensive~~ chain rule is used extensively to calculate error (Backprop.)

$$\text{eg: } \frac{\partial L}{\partial w_1} = \frac{\partial L}{\partial a_3} \frac{\partial a_3}{\partial a_2} \dots \frac{\partial a_1}{\partial w_1}$$

Here the partial derivatives are usually ~~of the~~ less than 1, which when multiplied lot of times, result in a very small value, ~~as~~ resulting in gradient shrink.

'sigmoid fun' takes the value and scales it down to  $(0, 1)$  resulting in even smaller derivative.

ReLU is  $\max(0, x)$  which gives this derivative as 1, solving the problem of vanishing grad.

Q3

When transformers use self attention, the tokens ~~are~~ aren't given some number to preserve the original sequence. It doesn't know ~~which~~ what the correct order is. To solve this problem, we use positional encoding.

#### Absolute PE

Gives unique vectors to each index

Initialized randomly and optimized by backprop.

Can only handle seq. of having length less than an assigned val.

#### Sinusoidal PE

Uses sine, cos fun<sup>s</sup> of different frequency

No training happens. Fixed math formula are used

Can be used on any length of sequence

RoPE helps with long-context as it shifts how the model perceive distance from 'absolute slots' to relative rotation.

Unlike ~~previous~~ <sup>other</sup> methods that add vectors together, RoPE rotates the Query & key vectors.

Q4 Query (Q): This represents the "current" word looking for information  
Key (K): This represents a "label" for all words in the sequence.  
Value (V): This is the actual info tied to the word.

$\sqrt{d_k}$  is used for scaling as it gives us stability numerically. When  $d_k$  is too large,  $Q \cdot K^T$  is very big. Hence by dividing by  $\sqrt{d_k}$  val of



$Q \cdot K^T$  is  $\approx 1$  around 1.

In attention weight matrix, the diagonal represents <sup>a</sup> the word attending itself. ~~Since~~<sup>As</sup> the word relates most to itself, the diagonal values are highest.

Q5 If we use single attention head, the model can only focus on one type of relationship at a time for a specific word. By using multiple heads our model can attend <sup>to</sup> different types of relationships at the same time.

$d_{\text{model}}$ : Total size of embedding vector for each word.

$h$ : No. of parallel attention "workers".

$d_{\text{head}}$ : Size of vector processed by each individual head

Q6

Greedy decoding can ~~lead~~ lead the model into a "local optima" trap. By choosing a very likely word now, the model may be forced ~~to~~ into highly unlikely words later to finish the sentence.

Beam search is better as it explores multiple branches/choices simultaneously. If one branch starts with a slightly lower-prob. word but leads to a much more logical and high-prob. conclusion, beam search will preserve that path while greedy would discard ~~it~~ immediately.

	1 <sup>st</sup> Word		2 <sup>nd</sup> Word
lg	Word 1 $\rightarrow$ 0.7 prob	$\Rightarrow$	Word 2 $\rightarrow$ 0.001 prob.
	Word 2 $\rightarrow$ 0.3 prob	$\Rightarrow$	Word 2 $\rightarrow$ 0.9 prob.

1<sup>st</sup> path prob = 0.007  
2<sup>nd</sup> path prob = 0.27

Q1

$$a) d_{mod} = \frac{d_{model}}{h} = 64$$

$$b) \text{Parameter per Matrix} = d_{model}^2 = (768)^2$$

$$\text{for 3 matrices: } 3 d_{model}^2 = 3 \cdot (768)^2$$

Q2

$$\frac{e^{z_i}}{\sum e^{z_i}}$$

$$e^2 = 7.39$$

$$e^1 = 2.71$$

$$e^0 = 1$$

$$\sum e^{z_i} = 11.1$$

$$\sigma_1 = \frac{7.39}{11.1} = 0.6657$$

$$\sigma_2 = \frac{2.71}{11.1} = 0.244$$

$$\sigma_3 = \frac{1}{11.1} = 0.09$$