

BOARD

PERCENTAGES

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Introduction

- ▶ What is percentage?

In mathematics, a **percentage** is a number or ratio expressed as a fraction of 100..

- ▶ Why percentage?

It helps in comparison by making the same base value for every comparison.

Basic Question Types

- ▶ Almost all the questions which come from Percentages can be broadly classified into 4 categories-

If $A=50$ and $B=40$, then

Q1. A is what percent of B?

Q2. B is what percent of A?

Q3. A is what percent more than B?

Q4. B is what percent less than A?

Solution

$$\frac{\text{What we compare}}{\text{to whom/which value we compare}} \times 100$$

1. $A/B \times 100$ ----- 125%

2. $B/A \times 100$ ----- 80%

3. $(A-B)/B \times 100$ ----- 25%

4. $(A-B)/A \times 100$ ----- 20%

Shortcuts

Shortcut 1: Splitting of values

a) 20% of 80 = ?

100% of 80 = 80

10% of 80 = 8

20% of 80 = 16

Try 30% of 60

b) 15% of 80 = ?

10% of 80 = 8

5% of 80 = 4

15% of 80 = 12

Try 15% of 60

c) 12% of 80 = ?

10% of 80 = 8

1% of 80 = 0.8

2% of 80 = 1.6

12% of 80 = 9.6

Try 13% of 60

d) 45% of 80 = ?

50% of 80 = 40

5% of 80 = 4

45% of 80 = 36

Try 45% of 60

Shortcut 2:

How do you solve **12.5% of 80 = ?**

10% + 2% + 0.5% ?

How much time will the following question take?

12.5% of 8.8 = ?

Now this

16.66% of 3.6 = ?

12.5% of 80 = ?

$$1 = 100\%$$

$$1/2 = 50\%$$

$$1/4 = 25\%$$

$$1/8 = 12.5\%$$

$$\begin{aligned}\therefore 12.5\% \text{ of } 80 &= 1/8 \text{ of } 80 \\ &= \mathbf{10}\end{aligned}$$

Similarly **12.5% of 8.8** = $1/8$ of 8.8
= **1.1**

16.66% of 3.6 = $1/6$ of 3.6
= **0.6**

Lets learn to convert few more fraction values

1 = 100%

$1/2 = 50\%$

$1/3 = 33.33\%$

$1/4 = 25\%$ (half of $1/2$)

$1/5 = 20\%$

$1/6 = 16.66\%$ (half of $1/3$)

$1/7 = 14.28\%$

$1/8 = 12.5\%$ (half of $1/4$)

$1/9 = 11.11\%$ ($1/3^{\text{rd}}$ of $1/3$)

$1/10 = 10\%$

$1/11 = 9.09\%$

Note: $1/9$ x will be in the multiples of 11
 $1/11$ x will be in the multiples of 9



▶ $1/9 = 11.11\%$, $2/9 = 22.22\%$, $3/9 = 33.33\%$

▶ $1/11 = 9.09\%$ $2/11 = 18.18\%$, $3/11 = 27.27\%$

▶

Shortcut 3:

How do you solve **62% of 150 = ?**

10% to 60%

1% to 2%

Then 60% + 2% ?


No

a% of b can be written as b% of a

Proof: $a\% \text{ of } b = b\% \text{ of } a$

$$a/100 \times b = b/100 \times a$$

$$ab/100 = ab/100$$


$$\begin{aligned}\therefore 62\% \text{ of } 150 &= 150\% \text{ of } 62 \\ &= 100\% + 50\% \text{ of } 62 \\ &= 62 + 31 \\ &= 93\end{aligned}$$

Why should we interchange 62 and 150?

Because splitting 150 is easier than splitting 62

So whenever the right hand side value is easier, interchange the values.

Try 84% of 250

Try 72% of 90

Percentage Change


► PERCENTAGE INCREASE and PERCENTAGE DECREASE

EXAMPLE- Lets say you have a factory which produced 20 cars in Year 1 and 25 cars in Year 2.

What is the percentage increase from the 1st year to the 2nd ?

What is the increase? 5

From where it is increasing? 20


$$\begin{aligned}\text{Percentage increase} &= 5/20 * 100 \\ &= 1/4 * 100 \\ &= 25\%\end{aligned}$$

What is the percentage decrease from the 2nd year to the 1st?

What is the decrease? 5

From where it is decreasing? 25

$$\begin{aligned}\text{Percentage decrease} &= 5/25 * 100 \\ &= 1/5 * 100 \\ &= 20\%\end{aligned}$$



Example: Sachin makes \$5M a week from his job. He earns a raise and now makes \$6M a week. What is the percent increase?

- A. 16.66%
- B. 20%
- C. 25%
- D. 50%

Solution: $\text{Percentage increase} = (1/5) * 100$
 $= 20\%$

Successive Percentage Change

Example: A car is moving at some constant speed. At first it increases its speed by 25% and then again it increases its speed by 20%. What is the overall percentage increase.

Method 1: Initial speed of the car = x

Speed of the car after 1st increase = $x + 25\% \text{ of } x = 1.25x$

Speed of the car after 2nd increase = $1.25x + 20\% \text{ of } 1.25x = 1.50x$

Initial speed = x

Final speed = $1.50x$

Percentage increase = 50%

Method 2:

Assume the initial speed of the car as 100kmph

Initial speed of the car = 100

Speed of the car after the 1st increase = $100 + 25 = 125$

Speed of the car after the 2nd increase = $125 + 2(12.5) = 150$

Initial speed = 100

Final speed = 150

Percentage increase = 50%

Method 3: Shortcut

If the 1st increase/ decrease is **a%** and the 2nd increase/decrease is **b%**, then the overall increase/decrease % will be

$$a + b + ab/100 \%$$

In this question **a = 25%** and **b = 20%**

$$\begin{aligned}\text{Overall increase/decrease} &= 25 + 20 + (25)(20)/100 \\ &= 25 + 20 + 5 \\ &= \mathbf{50 \%}\end{aligned}$$

Note: If a or b is increase, then include +ve sign

If a or b is decrease, then include -ve sign.

Note : The final answer will be in percentage

Example 5: A city's population was 10,000 at the end of 2008. In 2009, it increased by 25% and in 2010, it decreased by 8%. What was the net percentage change city's population at the end of 2010?

Solution:

$$\begin{aligned} & 25 + (-8) + (25)(-8)/100 \% \\ &= 25 - 8 - 200/100 \% \\ &= 25 - 8 - 2 \% \\ &= 15 \% \end{aligned}$$

Question: A fruit seller had some oranges. He sells 70% oranges and still has 420 oranges. How many oranges he had originally?

- A. 1400
- B. 630
- C. 700
- D. 1050

► Solution

From 100% \rightarrow sold 70%.
 \rightarrow remaining = 30%.

A/Q, remaining = 420 oranges

\Rightarrow 30% \rightarrow 420

\Rightarrow 10% $\rightarrow \frac{420}{3} = 140$

\Rightarrow 100% \rightarrow (1400) //



Question: An agent, gets a commission of 5% on the sales of cloth. If on a certain day, he gets Rs. 12.50 as commission, the cloth sold through him on that day is worth

- A. 125
- B. 250
- C. 500
- D. 1000

Solution

Percent commission = 5%, Actual commission = Rs 12.5

∴ 5% of sales \longrightarrow Rs 12.5

10% of sales \longrightarrow Rs 25

100% \longrightarrow Rs 250.

Question:- A student has to obtain 33% of the total marks to pass. He got 125 marks and failed by 40 marks. The maximum marks are-

- A. 400
- B. 500
- C. 600
- D. 800

Solution:

Equate percentage value with the marks to get the answer

Percentage Pass mark = 33%

He got 125 marks and need 40 more marks to pass

$$\therefore \text{Pass mark} = 125 + 40 = 165$$

$$33\% \text{ -----} \rightarrow 165$$

$$\text{Maximum marks} = 100\%$$

$$33\% \text{ -----} \rightarrow 165$$

$$1\% \text{ -----} \rightarrow 165/33 = 5$$

$$100\% = 500$$

Q. In a test A got 15% of the marks and failed by 7 marks whereas B got 28% and got 32 marks more than the pass mark. What was the pass mark?

- A. 45
- B. 52
- C. 84
- D. 300

Solution: Equate percentage value with the price to get the answer

Percentage of A = 15%

Marks of A = -7 (Deviation from pass mark)

Percentage of B = 28%

Marks of B = + 32

Percentage difference b/w A and B = 13%

Marks difference b/w A and B = 39

$\therefore 13\% = 39$ marks

1% = 3 marks