AIMA: Chapter 3 (Sections 3.4)

Introduction to Artificial Intelligence CSCE 476-876, Fall 2017

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function GENERAL-SEARCH(*problem*, *strategy*) **returns** a solution, or failure initialize the search tree using the initial state of *problem* **loop do**

if there are no candidates for expansion then return failure choose a leaf node for expansion according to *strategy*if the node contains a goal state then return the corresponding solution else expand the node and add the resulting nodes to the search tree
end

Essence of search: which node to expand first?

 \longrightarrow search strategy

A strategy is defined by picking the order of node expansion

Heuristic: exploits some knowledge of the domain

Uninformed search strategies

1. Breadth-first search

2. Uniform-cost search

3. Depth-first search

4. Depth-limited search

5. Iterative deepening depth-first search

6. Bidirectional search

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Search strategies

Criteria for evaluating search:

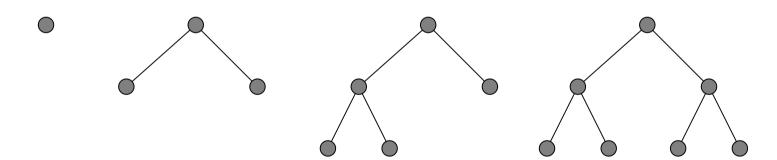
- 1. Completeness: does it always find a solution if one exists?
- 2. Time complexity: number of nodes generated/expanded
- 3. Space complexity: maximum number of nodes in memory
- 4. Optimality: does it always find a least-cost solution?

Time/space complexity measured in terms of:

- b: maximum branching factor of the search tree
- d: depth of the least-cost solution
- m: maximum depth of the search space (may be ∞)

Breadth-first search (I)

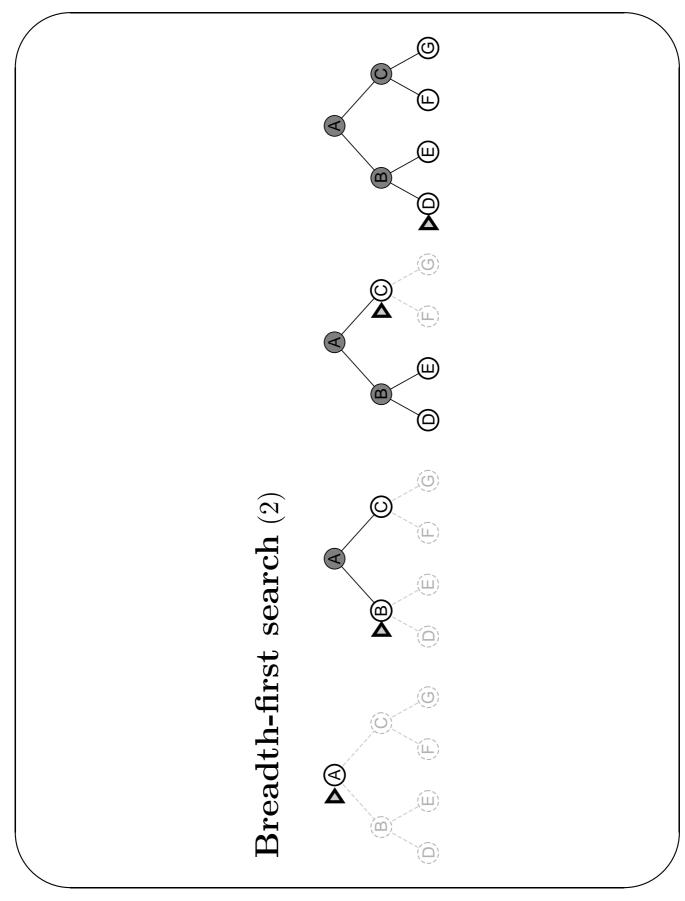
- \rightarrow Expand root node
- \rightarrow Expand <u>all</u> children of root
- \rightarrow Expand each child of root
- \rightarrow Expand successors of each child of root, etc.



- \longrightarrow Expands nodes at depth d before nodes at depth d+1
- → Systematically considers all paths length 1, then length 2, etc.
- → Implement: put successors at end of queue.. FIFO

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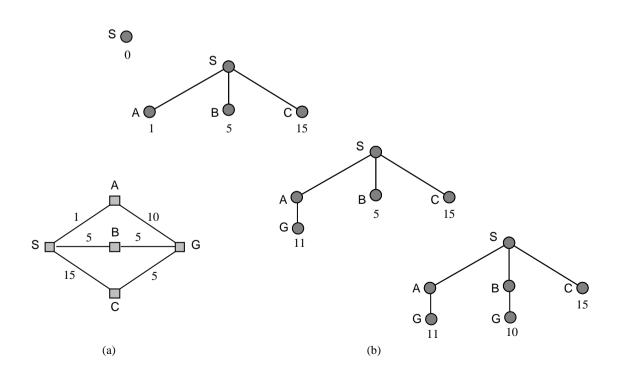
Breadth-first search (3)

- \longrightarrow One solution?
- → Many solutions? Finds shallowest goal first
 - 1. Complete? Yes, if b is finite
 - 2. Optimal? provided cost increases monotonically with depth, not in general (e.g., actions have same cost)
 - 3. Time? $1+b+b^2+b^3+\ldots+b^d+b(b^d-1)=O(b^{d+1})$ $O(b^{d+1}) \begin{cases} \text{branching factor } b \\ \text{depth } d \end{cases}$
- 4. Space? same, $O(b^{d+1})$, keeps every node in memory, big problem can easily generate nodes at 10MB/sec so 24hrs = 860GB

Uniform-cost search (I)

- \longrightarrow Breadth-first does not consider path cost g(x)
- → Uniform-cost expands first lowest-cost node on the fringe
- → Implement: sort queue in decreasing cost order

When $g(x) = \text{Depth}(x) \longrightarrow \text{Breadth-first} \equiv \text{Uniform-cost}$



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Uniform-cost search (2)

- 1. Complete? Yes, if $\cos t \ge \epsilon$
- 2. Optimal?

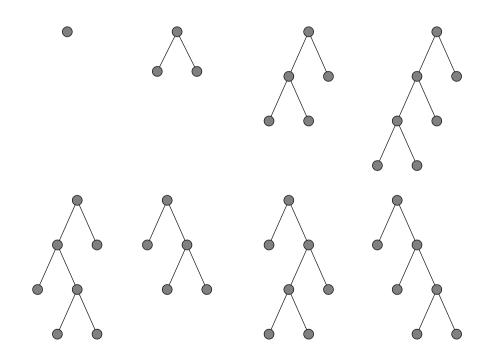
 If the cost is a monotonically increasing function

 When cost is added up along path, an operator's cost?
- 3. Time? # of nodes with $g \leq \text{cost of optimal solution}$, $O(b^{\lceil C^*/\epsilon \rceil})$ where C^* is the cost of the optimal solution
- 4. Space? # of nodes with $g \leq \text{cost of optimal solution}$, $O(b^{\lceil C^*/\epsilon \rceil})$

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Depth-first search (I)

- → Expands nodes at deepest level in tree
- → When dead-end, goes back to shallower levels
- → Implement: put successors at front of queue.. LIFO



→ Little memory: path and unexpanded nodes

For b: branching factor, m: maximum depth, space?

Depth-first search (3)

Time complexity:

We may need to expand all paths, $O(b^m)$

When there are many solutions, DFS may be quicker than BFS When m is big, much larger than d, ∞ (deep, loops), .. troubles

→ Major drawback of DFS: going deep where there is no solution...

Properties:

- 1. Complete? Not in infinite spaces, complete in finite spaces
- 2. Optimal?
- 3. Time? $O(b^m)$ Woow..

 terrible if m is much larger than d, but if solutions are dense,
 may be much faster than breadth-first
- 4. Space? O(bm), linear!

Woow..

Depth-limited search (I)

- → DFS is going too deep, put a threshold on depth!

 For instance, 20 cities on map for Romania, any node deeper than 19 is cycling. Don't expand deeper!
- \longrightarrow Implement: nodes at depth l have no successor

Properties:

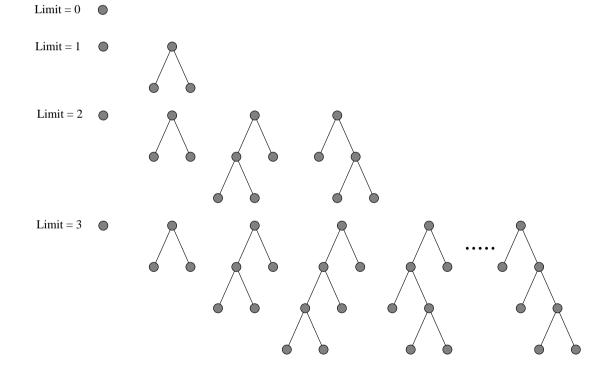
- 1. Complete?
- 2. Optimal?
- 3. Time? (given l depth limit)
- 4. Space? (given l depth limit)

Problem: how to choose l?

Iterative-deepening search (I)

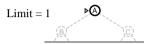
→ Combines benefits of DFS and BFS

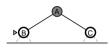
- \rightarrow DLS with depth = 0
- \rightarrow DLS with depth = 1
- \rightarrow DLS with depth = 2
- \rightarrow DLS with depth = 3...

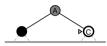


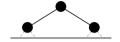
Iterative-deepening search (2)

Limit = 0



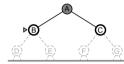






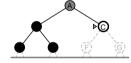
Limit = 2

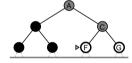


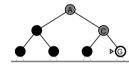


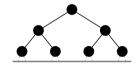




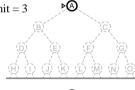


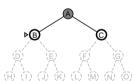




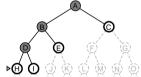


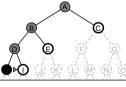
Limit = 3

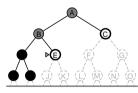


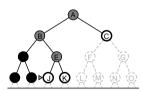


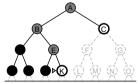


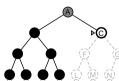


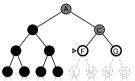


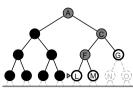


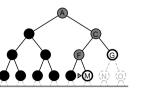












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Iterative-deepening search (3)

→ combines benefits of DFS and BFS

Properties:

1. Time? $(d+1).b^0 + (d).b + (d-1).b^2 + ... + 1.b^d = O(b^d)$

2. Space? O(bd), like DFS

3. Complete? like BFS

4. Optimal? like BFS (if step cost = 1)

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Iterative-deepening search (4)

→ Some nodes are expanded several times, wasteful?

$$N(BFS) = b + b^2 + b^3 + ... + b^d + (b^{d+1} - b)$$

$$N(IDS) = (d)b + (d-1)b^2 + ... + (1)b^d$$

Numerical comparison for b = 10 and d = 5:

$$N(IDS) = 50 + 400 + 3,000 + 20,000 + 100,000 = 123,450$$

$$N(BFS) = 10 + 100 + 1,000 + 10,000 + 100,000 + 999,990 =$$

1,111,100

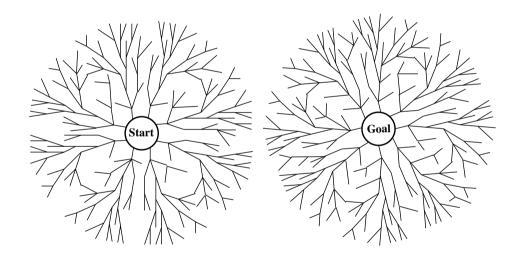
 \longrightarrow IDS is preferred when search space is large and depth unknown

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Bidirectional search (I)

 \rightarrow Given initial state and the goal state, start search from both ends and meet in the middle



 \rightarrow Assume same b branching factor, \exists solution at depth d, time: $O(2b^{d/2}) = O(b^{d/2})$

b = 10, d = 6, DFS = 1,111,111 nodes, BDS = 2,222 nodes!

Bidirectional search (2)

In practice :—(

- Need to define predecessor operators to search backwards If operator are invertible, no problem
- What if \exists many goals (set state)? do as for multiple-state search
- need to check the 2 fringes to see how they match need to check whether any node in one space appears in the other space (use hashing) need to keep all nodes in a half in memory $O(b^{d/2})$
- What kind of search in each half space?

Summary

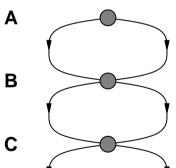
| Criterion | Breadth- | Uniform- | Depth- | Depth- | Iterative |
|-----------|-----------|---------------------------------|--------|--------------------|-----------|
| | First | Cost | First | Limited | Deepening |
| Complete? | Yes* | Yes* | No | Yes, if $l \geq d$ | Yes |
| Time | b^{d+1} | $b^{\lceil C^*/\epsilon ceil}$ | b^m | b^l | b^d |
| Space | b^{d+1} | $b^{\lceil C^*/\epsilon ceil}$ | bm | bl | bd |
| Optimal? | Yes* | Yes* | No | No | Yes |

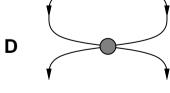
b branching factor d solution depth m maximum depth of tree l depth limit

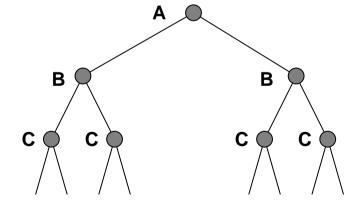
Avoid expanding states that have already been visited

Valid for both infinite and finite trees

Example: $\begin{cases} m \text{ maximum depth} \\ m+1 \text{ states} \\ 2^m \text{ possible branches (paths)} \end{cases}$





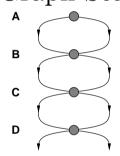


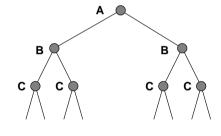
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Keep nodes in two lists:

Open list: Fringe Closed list: Leaf and expansed nodes

Discard a current node that matches a node in the closed list Tree-Search \longrightarrow Graph-Search





Issues:

- 1. Implementation: hash table, access is constant time Trade-off cost of storing+checking vs. cost of searching
- 2. Losing optimality when new path is cheaper/shorter of the one stored
- 3. DFS and IDS now require exponential storage

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Summary

Path: sequence of actions leading from one state to another

Partial solution: a path from an initial state to another state

Search: develop a sets of partial solutions

- Search tree & its components (node, root, leaves, fringe)
- Data structure for a search node
- Search space vs. state space
- Node expansion, queue order
- Search types: uninformed vs. heuristic
- 6 uninformed search strategies
- 4 criteria for evaluating & comparing search strategies