



Comprehensive Revision Notes on Linear Regression: Assumptions and Techniques

Introduction

In this session, we focused on understanding the assumptions underlying linear regression and techniques for handling scenarios where these assumptions might be violated. The class was structured around practical examples and emphasized the importance of concept comprehension over code memorization. Below are the detailed notes covering all the concepts discussed.

Key Concepts and Assumptions in Linear Regression

1. Multicollinearity

- **Definition:** Multicollinearity occurs when two or more independent variables in a regression model are highly correlated, meaning that one variable can be linearly predicted from the others with a substantial degree of accuracy **【4:9+transcript.txt】** .
- **Detection:**
 - **Variance Inflation Factor (VIF):** An indicator of multicollinearity. A VIF value above 5 suggests a potential problem, and above 10 indicates a critical issue **【4:14+transcript.txt】** .
- **Handling Multicollinearity:**
 - Remove variables with high VIF to reduce multicollinearity without significantly affecting the model's predictive power, as indicated by the stability of the R-squared value **【4:0+transcript.txt】** .

2. Handling Errors



predicted values (Error = $Y_{\text{actual}} - Y_{\text{predicted}}$)

【4:18+transcript.txt】 .

- **Error Plots:** Useful for visualizing how errors vary with independent variables. These plots help in identifying patterns or trends in errors, which can signal model inadequacies
【4:18+transcript.txt】 .

3. Outliers

- **Impact on Regression Models:** Outliers can drastically skew regression lines, leading to less accurate models. They affect both the slope and intercept, causing significant model errors
【4:3+transcript.txt】 .
- **Solutions:**
 - Removal or correction can help in realigning the regression model.
 - Switching to models that handle outliers better, such as tree-based models like Random Forest or XGBoost, can also be effective
【4:13+transcript.txt】 .

4. Assumptions of Normality of Errors

- **Concept:** In linear regression, it is assumed that errors are normally distributed. This assumption ensures that inaccuracies in data prediction are symmetrically distributed about zero
【4:7+transcript.txt】 .
- **Violation Indication:** Non-normally distributed errors suggest potential underfitting or overfitting, meaning the model may not be capturing all underlying data patterns 【4:8+transcript.txt】 .

5. Autocorrelation in Errors

- **Relevance:** Particularly significant in time series data, autocorrelation in errors suggests that the model errors are correlated over time, indicating a model's deficiency in capturing time-related trends 【4:2+transcript.txt】 .



6. Heteroskedasticity

- **Explanation:** This is when the variance of errors is not constant across all levels of the independent variable, leading to inefficiencies in predictions `【4:13+transcript.txt】` .
- **Impact and Detection:**
 - Can be spotted using residual plots; a non-random pattern signals heteroskedasticity.
 - Leads to inefficient parameter estimates, affecting the validity of hypothesis tests `【4:13+transcript.txt】` .

Conclusion

This class session provided an in-depth exploration of linear regression assumptions and methods to mitigate common issues such as multicollinearity, non-normal distribution of errors, and the presence of outliers. Understanding these concepts is crucial for building robust predictive models in data science. The focus on practical applications and interpretations ensures that learners can effectively apply these strategies in industry scenarios without being bogged down by syntactic details.