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GATE 2021 BM.29

EE23BTECH11010 - VENKATESH BANDAWAR*

Question: In the circuit shown below, $V_s = 100V$, $R_1 = 30\Omega$, $R_2 = 60\Omega$, $R_3 = 90\Omega$, $R_4 = 45\Omega$, $R_5 = 30\Omega$ The current flowing through resistor R_3 is _____A. (Gate 2022 BM)

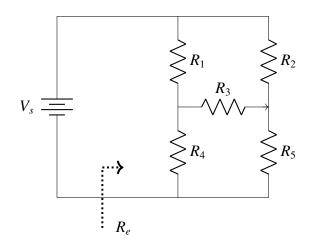


Fig. 1: Circuit Digram

Solution:

Parameter	Value
V_s	100V
R_1	30Ω
R_2	60Ω
R_3	90Ω
R_4	45Ω
R_5	30Ω

TABLE I: Given Parameters

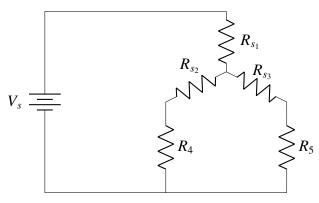


Fig. 2: circuit diagram

$$R_{s_1} = \frac{R_1 R_2}{R_1 + R_2 + R_3} \tag{1}$$

$$=10\Omega \tag{2}$$

$$R_{s_2} = \frac{R_3 R_1}{R_1 + R_2 + R_3} \tag{3}$$

$$=15\Omega \tag{4}$$

$$R_{s_3} = \frac{R_2 R_3}{R_1 + R_2 + R_3} \tag{5}$$

$$=30\Omega \tag{6}$$

$$R_e = R_{s_1} + \frac{(R_{s_2} + R_4)(R_{s_3} + R_5)}{(R_{s_2} + R_4) + (R_{s_3} + R_5)}$$
(7)

$$=40\Omega \tag{8}$$

$$I = \frac{V_s}{R_s} \tag{9}$$

$$=2.5A\tag{10}$$

From Circuit Fig. 2

$$V_{R_4} = \frac{(R_{s_3} + R_5)}{(R_{s_2} + R_4) + (R_{s_3} + R_5)} IR_4$$
 (11)

$$= 56.25V$$
 (12)

By KVL,

$$V_{R_1} = V - V_{R_4} \tag{13}$$

$$=43.75V$$
 (14)

By KCL,

$$I_{R_3} = \frac{V_{R_1}}{R_1} - \frac{V_{R_4}}{R_4} \tag{15}$$

$$= 0.2083A$$
 (16)