

DAY 5

INTERVIEW BIT PROBLEMS :

1. Matrix Median

Given a matrix of integers A of size $N \times M$ in which each row is sorted.

Find and return the overall median of the matrix A .

Note: No extra memory is allowed.

Note: Rows are numbered from top to bottom and columns are numbered from left to right.

Input Format

The first and only argument given is the integer matrix A .

Output Format

Return the overall median of the matrix A .

Constraints

$1 \leq N, M \leq 10^5$

$1 \leq N \times M \leq 10^6$

$1 \leq A[i] \leq 10^9$

$N \times M$ is odd

For Example

Input 1:

```
A = [ [1, 3, 5],
       [2, 6, 9],
       [3, 6, 9] ]
```

Output 1:

5

Explanation 1:

$A = [1, 2, 3, 3, 5, 6, 6, 9, 9]$

Median is 5. So, we return 5.

Input 2:

```
A = [ [5, 17, 100] ]
```

Output 2:

Matrix=17

CODE:

C++

```
int Solution::findMedian(vector<vector<int> > &A) {
    int n=A.size();
    int m=A[0].size();
    int med=n*m/2;
    vector<int>out;
    for(int i=0;i<n;i++){
        for(int j=0;j<m;j++){
            out.push_back(A[i][j]);
        }
    }
    std :: nth_element(out.begin(),out.begin()+med,out.end());
    return out[med];
}
```

PYTHON

```
class Solution:
    # @param A : list of list of integers
    # @return an integer
    def findMedian(self, A):
        out=[num for rows in A for num in rows]
        out.sort()
        return out[len(out)//2]
```

2. Sorted Insert Position

Given a sorted array and a target value, return the index if the target is found. If not, return the index where it would be if it were inserted in order.

You may **assume no duplicates** in the array.

Here are few examples.

[1,3,5,6], 5 \rightarrow 2

[1,3,5,6], 2 \rightarrow 1

[1,3,5,6], 7 \rightarrow 4

[1,3,5,6], 0 \rightarrow 0

CODE :

C++

```
int Solution::searchInsert(vector<int> &A, int B) {  
    // Do not write main() function.  
    // Do not read input, instead use the arguments to the  
    function.  
    // Do not print the output, instead return values as  
    specified
```

```
    int l=0,h=A.size()-1;  
    while(l<=h){  
        int m=(l+h)/2;  
        if(A[m]==B){  
            return m;  
        }  
        else if(A[m]<B){  
            l=m+1;  
        }  
        else{  
            h=m-1;  
        }  
    }  
    return l;  
}
```

PYTHON

class Solution:

 # @param A : list of integers

 # @param B : integer

 # @return an integer

 def searchInsert(self, A, B):

 l=0

 h=len(A)-1

 while(l<=h):

 m=(l+h)//2

 if A[m]==B:

 return m

 elif A[m]<B:

 l=m+1

 else:

 h=m-1

 return l

3. Search for a Range

Given a sorted array of integers A(0 based index) of size N, find the starting and ending position of a given integer B in array A.

Your algorithm's runtime complexity must be in the order of $O(\log n)$.

Return an array of size 2, such that first element = starting position of B in A and second element = ending position of B in A, if B is not found in A return [-1, -1].

Input Format

The first argument given is the integer array A.

The second argument given is the integer B.

Output Format

Return an array of size 2, such that first element = starting position of B in A and second element = ending position of B in A, if B is not found in A return [-1, -1].

Constraints

$1 \leq N \leq 10^6$

$1 \leq A[i], B \leq 10^9$

For Example

Input 1:

A = [5, 7, 7, 8, 8, 10]

B = 8

Output 1:

[3, 4]

Explanation 1:

First occurrence of 8 in A is at index 3

Second occurrence of 8 in A is at index 4

ans = [3, 4]

Input 2:

A = [5, 17, 100, 111]

B = 3

Output 2:

[-1, -1]

CODE :

PYTHON

class Solution:

@param A : tuple of integers

@param B : integer

@return a list of integers

def searchRange(self, A, B):

output=[-1,-1]

A=list(A)

h=len(A)-1

```

l=0
while l<=high:
    mid=l+(h-l)//2
    if A[mid]>=B:
        h=mid-1
    if A[mid]<B:
        l=mid+1
if A[l]==B:
    output[0]=l
l=0
h=len(A)-1
while l<=h:
    mid=l+(h-l)//2
    if A[mid]>B:
        h=mid-1
    if A[mid]<=B:
        l=mid+1
if A[h]==B:
    output[1]=h
return output

```

C++

```

vector<int> Solution::searchRange(const vector<int> &A, int B) {
    int n=A.size();
    int l=0,h=n-1;
    vector<int>out(2,-1);
    while(l<=h){
        int m=l+(h-l)/2;
        if(A[m]>=B){
            h=m-1;
        }
        if(A[m]<B){
            l=m+1;
        }
    }
}

```

```

    }
    if(A[l]==B){
        out[0]=l;
    }
    l=0;
    h=n-1;
    while(l<=h){
        int m=l+(h-l)/2;
        if(A[m]>B){
            h=m-1;
        }
        if(A[m]<=B){
            l=m+1;
        }
    }
    if(A[h]==B){
        out[1]=h;
    }
    return out;
}

```

4. Implement Power Function

Implement $\text{pow}(x, n) \% d$.

In other words, given x , n and d ,
find $(x^n \% d)$

Note that remainders on division cannot be negative.

In other words, make sure the answer you return is non negative.

Input : $x = 2, n = 3, d = 3$

Output : 2

$$2^3 \% 3 = 8 \% 3 = 2.$$

CODE :

PYTHON

class Solution:

```
# @param x : integer
# @param n : integer
# @param d : integer
# @return an integer
def pow(self, x, n, d):
    power= 1%d
    while n > 0:
        if n & 1:
            power= (power * x) % d
        x = x**2 % d
        n >>= 1
    return power
```