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Assignment 3

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$\label{lem:abstract} \textbf{Abstract} \textbf{—} \textbf{This document explains the concept of matrix multiplication}$

Download all latex-tikz codes from

https://github.com/venkateshelangovan/IIT— Hyderabad—Assignments/tree/master/ Assignment3 Matrix Theory

If
$$F(x) = \begin{pmatrix} \cos x & -\sin x & 0 \\ \sin x & \cos x & 0 \\ 0 & 0 & 1 \end{pmatrix}$$
, show that $F(x)F(y) = F(x+y)$

2 Solution

Given,

$$F(x) = \begin{pmatrix} \cos x & -\sin x & 0\\ \sin x & \cos x & 0\\ 0 & 0 & 1 \end{pmatrix}$$
 (2.0.1)

Replacing x with y in above equation 2.0.1 F(y) is given as,

$$F(y) = \begin{pmatrix} \cos y & -\sin y & 0\\ \sin y & \cos y & 0\\ 0 & 0 & 1 \end{pmatrix}$$
 (2.0.2)

From the problem statement, Consider the LHS, F(x)F(y)

$$= \begin{pmatrix} \cos x & -\sin x & 0 \\ \sin x & \cos x & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \cos y & -\sin y & 0 \\ \sin y & \cos y & 0 \\ 0 & 0 & 1 \end{pmatrix}$$
 (2.0.3)
$$= \begin{pmatrix} \cos x \cos y - \sin x \sin y & -\cos x \sin y - \sin x \cos y & 0 \\ \sin x \cos y + \cos x \sin y & -\sin x \sin y + \cos x \cos y & 0 \\ 0 & 0 & 1 \end{pmatrix}$$
 (2.0.4)

$$= \begin{pmatrix} \cos(x+y) & -\sin(x+y) & 0\\ \sin(x+y) & \cos(x+y) & 0\\ 0 & 0 & 1 \end{pmatrix}$$
 (2.0.5)

$$= F(x+y) \tag{2.0.6}$$

Equation 2.0.5 is F(x+y) i.e RHS of the problem statement. Here we arrived at RHS by solving the LHS F(x)F(y) Therefore,

F(x)F(y) = F(x+y) (2.0.7)

Hence Proved