

23/8/2023

## Backtracking - 1

Recursion  $\rightarrow$  Solving a problem using its subproblem.

Backtracking  $\rightarrow$  Trying all possibilities with recursion.

Bruteforce.

3 boxes  $\rightarrow$  Find box with max chocolates  $\rightarrow$  check all 3

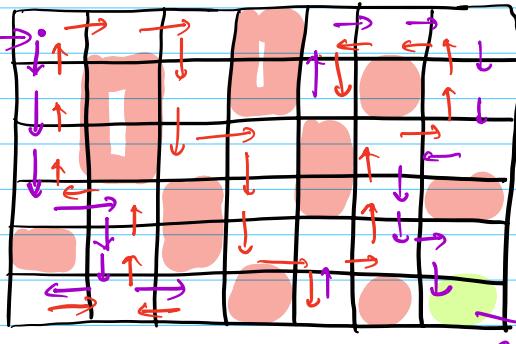
Q

Rat in a maze  $\rightarrow$  check if it is possible to go from top-left to bottom-right cell in a maze with some blocked cells.

I/P  $\rightarrow$   $A[][], \rightarrow 0$  (empty)

$\hookrightarrow 1$  (blocked)

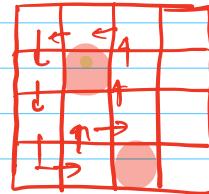
Rat



$(i-1, j)$  Move.  
 $(i, j-1) \leftarrow (i, j) \rightarrow (i, j+1)$   
 $(i+1, j)$

ans = true

Exit



1> Rat is always inside the maze.

2> Rat is not going to any visited cell.

3> Rat is not going to any blocked cell.

II  $A[][], N, M$

if ( $A(N-1)[M-1] == 1$ ) return false;  $A[][], \rightarrow 0$  (empty)

boolean check( $i, j$ ) {

[if ( $i == N-1 \ \&\& j == M-1$ )

$\hookrightarrow 1$  (blocked)

$\hookrightarrow 2$  (visited)

return true //reached exit.

[if ( $i < 0 \ || i > N \ || j < 0 \ || j > M$ ) {  
return false;  
}]

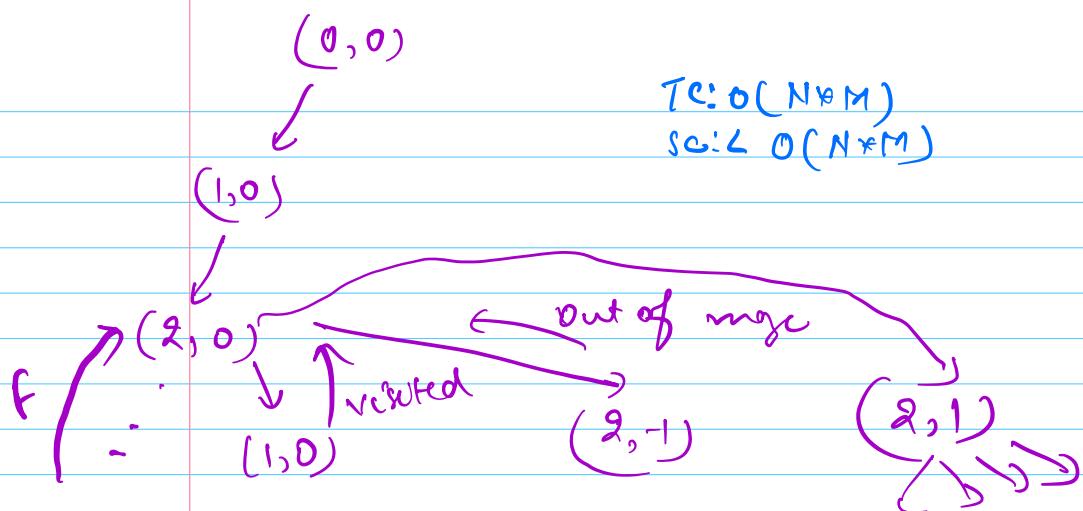
[if ( $A[i][j] == 1 \ || A[i][j] == 2$ )  
return false // blocked or visited

} order is  
important

$A[i][j] = 2$

return check( $i+1, j$ ) || check( $i-1, j$ ) ||  
check( $i, j-1$ ) || check( $i, j+1$ );

}



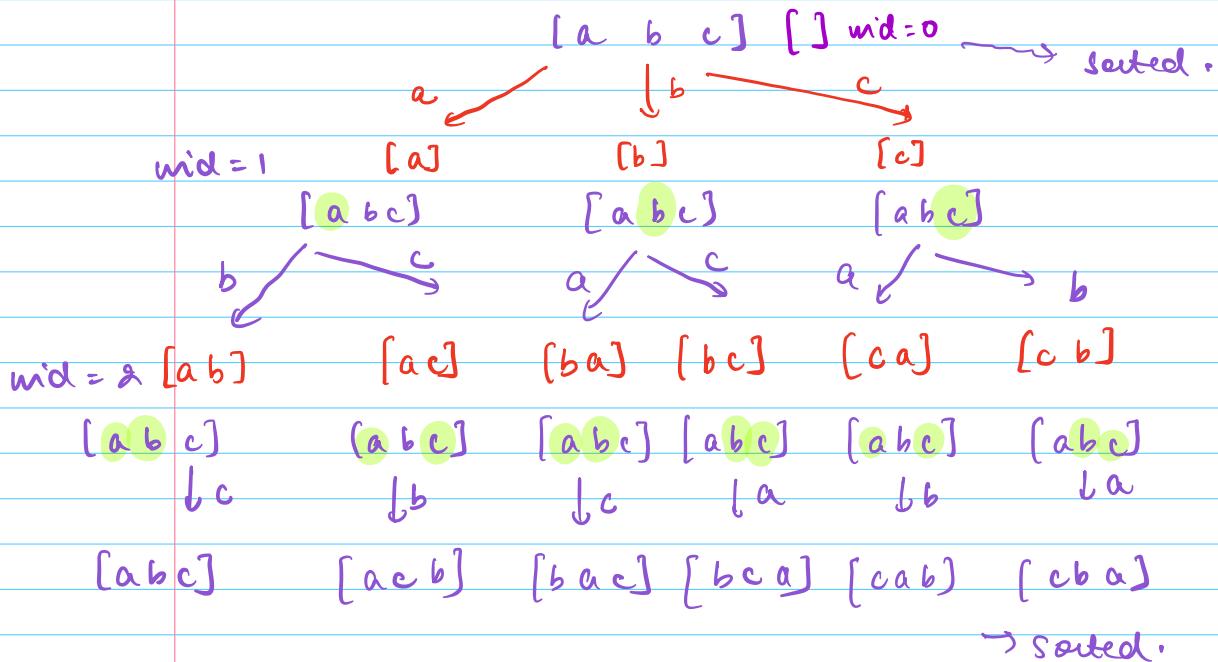
Q

Given a char array with **distinct elements**. Print all the permutations of the array without modifying the input array.

$A = [a \ b \ c]$  o/p  $\Rightarrow abc \quad bac \quad cab$   
 $acb \quad bca \quad cba$

$$3 \times 2 \times 1 = 3! = 6$$

// Permutation with distinct chars  $\Rightarrow N!$



```

void permutation (A[], vst[], ans[], mid) { N → A.length
    if (mid == N) { // Base case
        print array (ans);
        return;
    }

    for (i = 0 to (N-1)) { // All possibilities.
        if (!vst[i]) { // Valid possibility
            vst[i] = true; // do
            ans[mid] = A[i];

            permutation (A, vst, ans, mid+1); // Recursion

            vst[i] = false; // undo
        }
    }
}

```

TC:  $O(N! * N)$

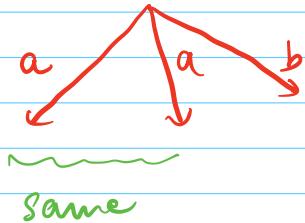
SC:  $O(N)$

Print the permutations in sorted order  $\Rightarrow$  initially sort the input array.

Meet at 8:35 am IST

Q = Print all unique permutations of the given char array.

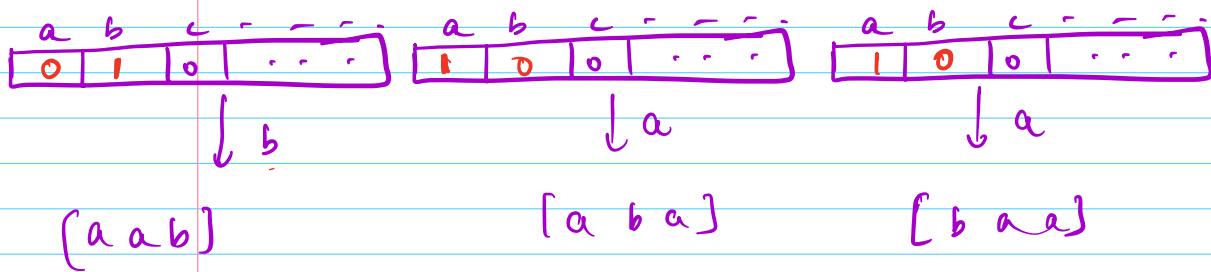
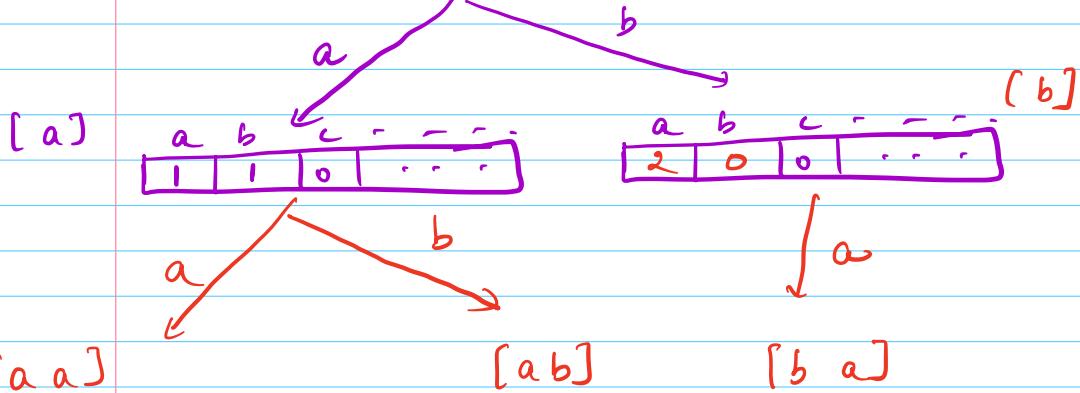
A = [ a a b ] o/p  $\rightarrow$  a a b a b a b a a



```
void permutation (F[], N, ans[], mid) { N  $\rightarrow$  A.length
    if (mid == N) {  $\uparrow 0$ 
        printarray (ans); // Base case
        return;
    }
```

```
for (i = 0 to 25) { // All possibilities.
    if (F[i] > 0) { // Valid possibility
        F[i]--; // do
        ans[mid] = char ('a' + i);
        permutation (A, N, ans, mid + 1); // Recursion
        F[i]++; // undo
    }
}
```

$$f = \begin{bmatrix} a & b & c & \dots & - \\ 0 & 1 & 0 & \dots & \end{bmatrix}$$



$$\begin{aligned} Tc: & O(N! * N!)^{26} \approx O(N!) \\ Sc: & O(N) \end{aligned}$$

Q4 Given a set of distinct integer A, return all possible subsets.

$$A = [1, 2, 3]$$

$$\begin{matrix} \downarrow & \downarrow & \downarrow \\ 2 & 2 & 2 \end{matrix} = 8$$

[ ]  
[1]  
[1, 2]  
[1, 2, 3]  
[1, 3]  
[2]  
[2, 3]  
[3]

a b c ✓  
a b d

a b c ✓  
a b d  
g

a ✓  
a b

0 → [1 2 3]

Tc: O(2^n)  
Sc: O(N)

[1]

[ ]

1 →

[1, 2] [1]

✓ ✓

[2] [ ]

✓ ✓ ✓ ✓

2 →

[1, 2, 3] [1, 2] [1, 3] [1]

[2, 3] [2] [3] [1]

Sorted ans → 1) sort i/p  
2) sort list of answer.

