

21/8/2023

## Greedy

Greedy  $\rightarrow$  Max profit / Min loss.

A  
iphone  $\rightarrow$  70k

B  
iphone  $\rightarrow$  60k ✓

(10k      shoes      5k)  $\rightarrow$  multiple factors

Q There is a limited time sale going on for toys,

$A[i] \rightarrow$  sale end time for  $i$ th toy

$B[i] \rightarrow$  beauty of  $i$ th toy.

It takes 1 unit of time to buy a toy & toy can only be bought if current time for  $i$ th toy  $\leq A[i]$ .

Buy toys s.t. sum of beauty is maximized.

	1	2	3	4	5
$A =$	3	1	3	2	3
$B =$	6	5	3	1	9
$T =$	1	0		2	

$$\text{Ans} = 5 + 6 + 9 = 20$$

	toy	$B[i]$
$T=0$	5	9
$T=1$	1	6
$T=2$	3	3
$T=3$		<u>18</u>

	1	2
$A =$	1	2
$B =$	3	1500
	$\uparrow$	$\uparrow$

$$T \rightarrow 0 \quad 1 \quad \text{Ans} = 1503$$

Select toys w.r.t sale end time.

	1	2	3	4	5	6	7
$A =$	1	3	3	3	5	5	5
$B =$	5	2	7	1	4	3	8
$T =$	0	1	2		3	4	5

$$\text{Ans} = 5 + 2 + 7 + 4 + 3 = 21$$

high beauty toy  $\Rightarrow$  purchase it  $\Rightarrow$  remove a previously purchased toy.  
mini beauty toy.  
mini heap.

	1	2	3	4	5	6	7	8	
A =	1	3	3	3	5	5	5	6	
B =	5	2	7	1	4	3	8	10	
T →	0	1	2		3	4		5	

Beauty of selected toys.

	1	2	3	4	5	6	7	8	9
A =	1	3	3	3	3	5	5	5	6
B =	5	2	7	1	100	4	3	8	10
T =	0	1	2		3	4		5	6

$100$   
 $1000$   
 $10000$   
 $1$

$100$   
 $1000$   
 $10K$

$7 + 100 + 8 + 10 = \dots$

// sort w.r.t A[i]

t=0

for i → 0 to (N-1) {

if (A[i] > t) {

h.insert(B[i]);

t++;

}

else { // sale ended for the product

if (h.peek() < B[i]) {

h.getmin();

h.insert(B[i]);

}

}

Ans =  $\sum$  elements present in heap.

TC:  $O(N \log N)$   
 SC:  $O(N)$

// replace with min  
 beauty toy already  
 bought.

Q2 There are  $N$  children with marks, teacher has to give them candies. s.t.

- a) Every child has atleast one candy.
- b) Children with higher marks have more candies than their neighbours  $(i-1)$   $i$   $(i+1)$

Find min candies required to do so.

$$A = [1 \ 5 \ 2 \ 1]$$

$$C \Rightarrow [1 \ 3 \ 2 \ 1]$$

$$\text{Ans} = 1 + 3 + 2 + 1 = 7$$

$$A = [4 \ 4 \ 4 \ 4 \ 4]$$

$$C = [1 \ 1 \ 1 \ 1 \ 1]$$

$$\text{Ans} = 5.$$

$$1) \forall i \ C[i] \geq 1$$

$$2) \text{ if } A[i] > A[i-1] \\ C[i] > C[i-1] \\ C[i] = C[i-1] + 1$$

$$3) \text{ if } A[i] > A[i+1] \\ C[i] > C[i+1]$$

$$C[i] = \max(C[i+1] + 1, C[i])$$

$$A = [1 \ 5 \ 2]$$

$$C = [1 \ 2 \ 1] \rightarrow \text{Ans} = 4$$

$$A = \begin{matrix} & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \\ \begin{bmatrix} 1 & 6 & 3 & 1 & 10 & 12 & 20 & 5 & 2 \end{bmatrix} \end{matrix}$$

$$C = \begin{bmatrix} 1 & 2 & 2 & 1 & 2 & 3 & 4 & 1 & 1 \end{bmatrix}$$

L  $\rightarrow$  R

$$\begin{matrix} 3 & 2 \end{matrix}$$

$$2$$

R  $\rightarrow$  L

$\forall c[i] = 1.$

```
for i = 1 to (N-1) {  
  if (A[i] > A[i-1]) {  
    c[i] = c[i-1] + 1; ← greedy.  
  }  
}
```

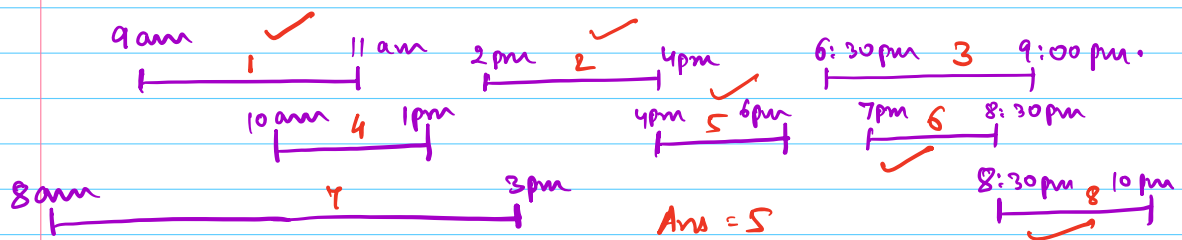
```
ans = c[N-1];  
for i = (N-2) to 0 {  
  if (A[i] > A[i+1]) {  
    c[i] = max(c[i+1] + 1, c[i]);  
  }  
  ans += c[i]  
}  
return ans;
```

Tc:  $O(N)$

Sc:  $O(N)$

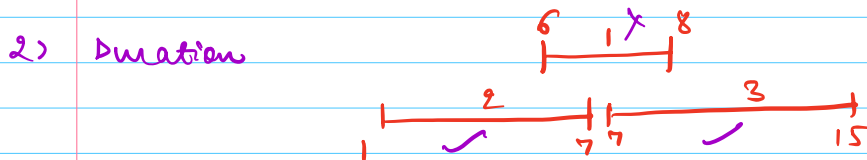
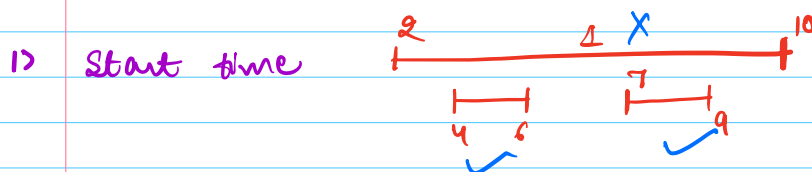
Break tile 8:49 am IST.

Q3 Given  $N$  jobs with start & end time. And max jobs that can be completed if only one job can be done at a time.

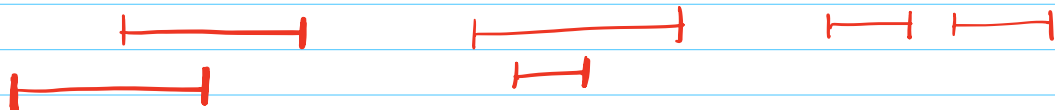


$S = [1, 5, 8, 7, 12, 13]$   
 $E = [2, 10, 10, 11, 20, 19]$

Jobs 1, 5, and 12 are highlighted in green. The answer is 3.



3) End time  $\rightarrow$  early start time & less duration



// sort w.r.t E[i] // sorting  
ans = 1, e = E[0]

```
for i → 1 to (N-1) {  
    if (S[i] >= e) {  
        ans++;  
        e = E[i];  
    }  
}
```

TC:  $O(N \log N)$   
SC:  $O(1)$

return ans;