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EE5600 Assignment 1

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Abstract—This document contains the solution to a Area of triangle problem.

Download all python codes from

https://github.com/venky-p/EE5600/Assignment

1 Problem

Problem Set: Vector2, Example II, Problem 5

1.1. Find the area of the triangle formed by the points (a, c+a), (a, c) and (-a, c-a)

2 Solution

We are going to solve this problem using vectors

$$\mathbf{P} = \begin{pmatrix} a \\ c+a \end{pmatrix}, \mathbf{Q} = \begin{pmatrix} a \\ c \end{pmatrix}, \mathbf{R} = \begin{pmatrix} -a \\ c-a \end{pmatrix}$$
 (2.1.1)

Rewriting P, Q and R as product of a matrix and a vector

$$\mathbf{P} = \mathbf{A}\mathbf{u} = \begin{pmatrix} 1 & 0 \\ 1 & 1 \end{pmatrix} \begin{pmatrix} a \\ c \end{pmatrix} \tag{2.1.2}$$

$$\mathbf{Q} = \mathbf{B}\mathbf{u} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} a \\ c \end{pmatrix} \tag{2.1.3}$$

$$\mathbf{R} = \mathbf{C}\mathbf{u} = \begin{pmatrix} -1 & 0 \\ -1 & 1 \end{pmatrix} \begin{pmatrix} a \\ c \end{pmatrix} \tag{2.1.4}$$

Area of given
$$\triangle le = \frac{1}{2} \|\mathbf{P} - \mathbf{Q} \times \mathbf{P} - \mathbf{R}\|$$
(2.1.5)

$$\mathbf{P} - \mathbf{Q} \times \mathbf{P} - \mathbf{R} = (\mathbf{A}\mathbf{u} - \mathbf{B}\mathbf{u}) \times (\mathbf{A}\mathbf{u} - \mathbf{C}\mathbf{u})$$
(2.1.6)

$$= \mathbf{Au} \times \mathbf{Au} - \mathbf{Au} \times \mathbf{Cu} - \mathbf{Bu} \times \mathbf{Au}$$
 (2.1.7)
+\mathbf{Bu} \times \mathbf{Cu} \tag{(2.1.8)}

$$= \mathbf{Au} \times \mathbf{Bu} + \mathbf{Bu} \times \mathbf{Cu} + \mathbf{Cu} \times \mathbf{Au} \quad (2.1.9)$$

$$= \begin{pmatrix} a \\ c+a \end{pmatrix} \times \begin{pmatrix} a \\ c \end{pmatrix} + \begin{pmatrix} a \\ c \end{pmatrix} \times \begin{pmatrix} -a \\ c-a \end{pmatrix} + \begin{pmatrix} -a \\ c-a \end{pmatrix} \times \begin{pmatrix} a \\ c+a \end{pmatrix}$$
(2.1.10)

$$= ac - a(c+a) + a(c-a) - c(-a)$$
 (2.1.11)
+(-a)(c+a) - (c-a)a (2.1.12)

$$= -2a^2 (2.1.13)$$

By Substituting the above value in (2.1.5), We get

Area of given
$$\triangle le = \frac{1}{2} ||-2a^2||$$
 (2.1.14)

$$= a^2 (2.1.15)$$

$$\therefore Area of given \triangle le = a^2 units^2$$
 (2.1.16)

3 Numerical Example

Let,

$$\mathbf{u} = \begin{pmatrix} a \\ c \end{pmatrix} = \begin{pmatrix} 2 \\ 4 \end{pmatrix} \tag{3.1.17}$$

Solution: By substituting the given values in (2.1.1), We get

$$\mathbf{P} = \begin{pmatrix} 2 \\ 6 \end{pmatrix}, \mathbf{Q} = \begin{pmatrix} 2 \\ 4 \end{pmatrix}, \mathbf{R} = \begin{pmatrix} -2 \\ 2 \end{pmatrix}$$
 (3.1.18)

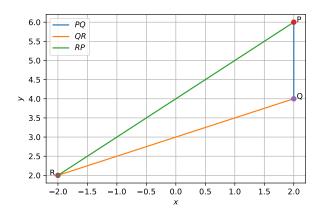


Fig. 3.1: Plot obtained from Python code

Using (2.1.16),

$$Area \ of \ \triangle le = a^2 \tag{3.1.19}$$

$$= 2^2 (3.1.20)$$

$$= 4 units^2$$
 (3.1.21)