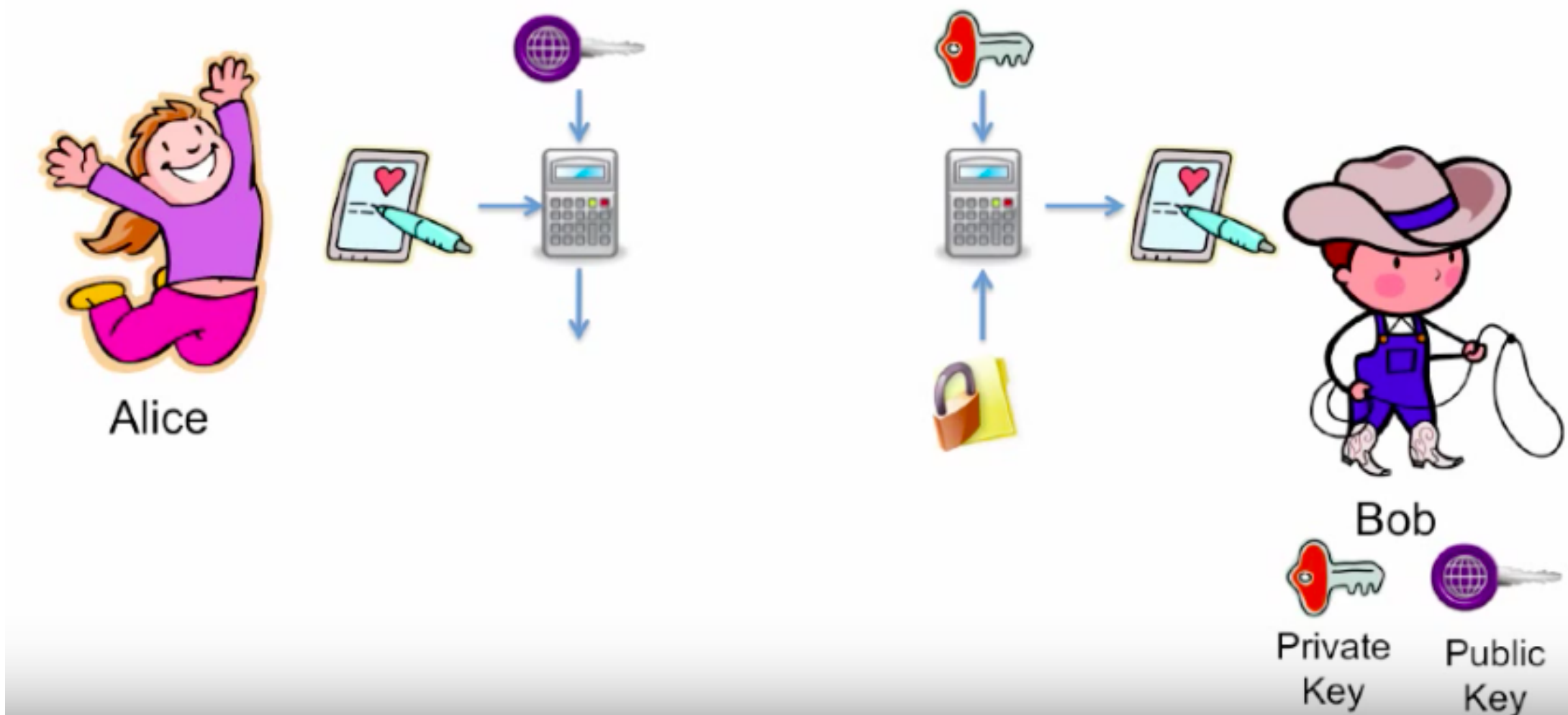


- Public key crypto allows you encrypt with one key and have someone else decrypt the message *with a different key*
- This has two uses:
  - Confidentiality
    - Send secret messages to someone
  - Integrity:
    - Ensure something wasn't modified
    - Prove who created it

- A cryptographic technique where both parties in the communication use *different keys*



Public and Private Keys

- Mathematically related keys that allow you to encrypt with one and decrypt with the other
  - Similar to the mathematics used in the Diffie-Hellman key exchange
- Every user has two keys: A public key and a private key
  - Public key: Not a secret. Anyone can have it
  - Private key: Secret. Only the owner can have it

- If we encrypt with the Alice public key - Decrypt with Alice's private key.

- Encryption with the public key

- $C = E_{\text{PUB-Alice}}(M)$
- $M = D_{\text{PRIV-Alice}}(C)$

- Encryption with the private key

- $C = E_{\text{PRIV-Alice}}(M)$
- $M = D_{\text{PUB-Alice}}(C)$

- Other encryption/decryption pairs *don't work*

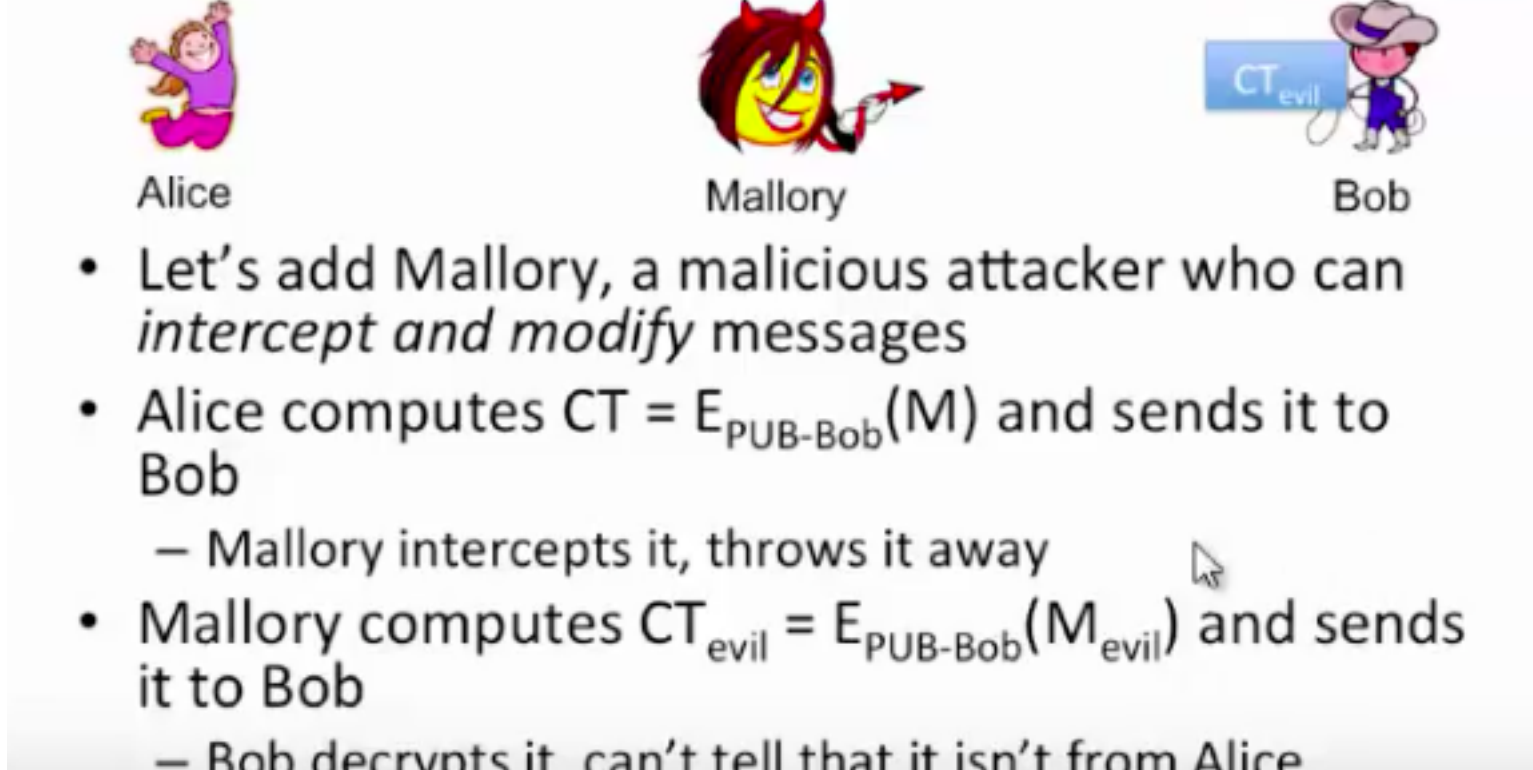
## Public Key Crypto for Confidentiality



- If Alice wants to send a message, M, to Bob...
  - She computes  $CT = E_{\text{PUB-Bob}}(M)$  and sends it to Bob
  - Bob decrypts it by calculating  $M = D_{\text{PRIV-Bob}}(C)$
- Who can perform the decryption?
  - Only Bob, with his private key
- Who can perform the encryption?
  - Anyone, because Bob's public key is public



- If Alice wants to send a message, M, to Bob that proves it is from her
  - She computes  $DS = E_{\text{PRIV-Alice}}(M)$  and sends it to Bob
  - Bob decrypts it by calculating  $M = D_{\text{PUB-Alice}}(DS)$
- Who can perform the encryption?
  - Only Alice, with her private key
- Who can perform the decryption?
  - Anyone, because Alice's public key is public



- Let's add Mallory, a malicious attacker who can *intercept and modify* messages
- Alice computes  $CT = E_{\text{PUB-Bob}}(M)$  and sends it to Bob
  - Mallory intercepts it, throws it away
- Mallory computes  $CT_{\text{evil}} = E_{\text{PUB-Bob}}(M_{\text{evil}})$  and sends it to Bob
  - Bob decrypts it, can't tell that it isn't from Alice

## Public Key Crypto for Integrity

- Bob knows the message is from Alice because *only Alice could have produced it*
- Notice this doesn't guarantee confidentiality
- We call this a *digital signature*
  - Alice is simply signing the message to prove it is from her

## RSA

- The first public key cryptosystem
- Invented by Rivest, Shamir, and Adleman
- Any bit size is ok
  - 512 was standard when it was released
  - 2048 or 4096 is standard now
- Based on prime numbers and factoring
  - The public key is the product of two primes
  - The private key is those two primes

## Note on Bit Size

- In symmetric key crypto, the *key size* is given in bits:
  - AES-128 means AES with a 128-bit key
  - 128-bits measures the keyspace (number of possible keys)
- In RSA asymmetric key crypto, the *prime number size* is given in bits:
  - RSA-2048 means RSA is using 2048-bit prime numbers to create the public and private keys
- Comparisons between symmetric and asymmetric security cannot be done based just on bit size

Asymmetric algorithm is roughly 1000 times slower than symmetric encryption algorithm.