

## Week 1

Wednesday, October 14, 2020 8:51 PM

- Imagine you're giving a lecture about a 4<sup>th</sup> year topic to a fourth year student.
- 30-50 pgs with title pages @ 12 LaTeX font.
- At least 5 sources, 10 average
- Sec. 6.1, Thm. (5)(a) can be strengthened to  $0 \leq p_{ij} \leq 1$ .

## Questions:

- Discuss title for dissertation - get something in mind, can be changed
  - Searching sources - Don't have to prove possession of sources.
  - How important are examples? - Don't copy others'. Important for complicated or abstract topics.
  - Pg. 215, about the sentence right above Thm. 7, does this fact not follow from the def. of a Markov Chain, also? - No.
  - Can we not strengthen cor(4)(a and b), pg. 221 to an iff?
  - Am I too meticulous? - Yes!
  - Pg. 222 above def. 7: why do we define  $E(T_i | X_0 = i) = \infty$ ?
  - 11 Last sentence of def. 7: How could that be?
- $\hookrightarrow x \cdot \infty = \infty \quad \forall x, \text{ so possibility of going to inf} \Rightarrow E = \infty.$
- Sources mostly books, not papers.

Polya From Hungary transient if summation diverges

Observation:

- Origin Necessarily persistent in 1 and 2 dimensions.  
Not in 3 or more!  
Related to Harmonic series.

Polya's

- 'Almost surely' wikipedia page  
- Lebesgue measure
- Two independent random walks intersecting analogous to one random walk crossing a specific point?
- $\mu_i$  thing (from Stirling's book) being contradictory to intuition.

## Questions:

Proof of 13.2.1 " $f_i$ "s should be " $f_j$ "s, typo?

## Notes:

Get started on writing out the proof and see what's needed as build up.