

$$\Gamma(p) := \int_0^{\infty} t^{p-1} e^{-t} dt, \quad p > 0$$

$$N(m, \sigma^2) \rightarrow f(x) = \frac{1}{\sigma \sqrt{2\pi}} e^{-\frac{(x-m)^2}{2\sigma^2}}$$

$$\Gamma\left(\frac{1}{2}\right) = \int_0^{\infty} t^{\frac{1}{2}-1} e^{-t} dt = \int_0^{\infty} \frac{e^{-t}}{\sqrt{t}} dt = \left[ \begin{array}{l} t = \frac{x^2}{2} \\ dt = x dx \end{array} \right] = \int_0^{\infty} \frac{e^{-\frac{x^2}{2}}}{\frac{x}{\sqrt{2}}} x dx$$

$$= \sqrt{2} \int_0^{\infty} e^{-\frac{x^2}{2}} dx = 2 \sqrt{\pi} \int_0^{\infty} \underbrace{\frac{e^{-\frac{x^2}{2}}}{\sqrt{2\pi}}}_{\text{gęstość } N(0,1) \text{ na } [0, \infty)} dx = 2 \sqrt{\pi} \cdot \frac{1}{2} = \sqrt{\pi}$$

mnożenie przez 1

gęstość  $N(0,1)$  na  $[0, \infty)$

