# Reinforcement Learning Intelligent Systems Series Lecture 3

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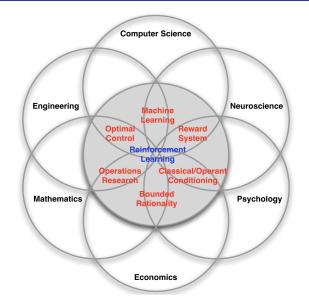




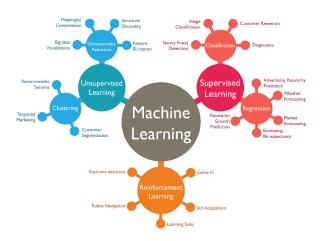


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# Many Types and Areas of Reinforcement Learning



#### Reminder: Branches of Machhine Learning



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## **Characteristics of Reinforcement Learning**

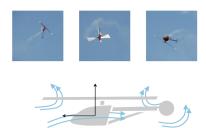
What makes reinforcement learning different from other machine learning paradigms?

- There is no supervisor, only a reward signal
- Feedback is delayed, not instantaneous
- Time really matters (sequential, non i.i.d data)
- Agent's actions affect the subsequent data it receives

## **Examples of Reinforcement Learning**

- Fly stunt manoeuvres in a helicopter
- Defeat the world champion at Backgammon
- Manage an investment portfolio
- Control a power station
- Make a humanoid robot walk
- Play many different Atari games better than humans
- Beat the best human player in Go

# Examples – Helicopter Manoeuvres



https://www.youtube.com/watch?v=0JL04JJjocc

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# Examples – Bipedal Robots



https://www.youtube.com/watch?v=No-JwwPbSLA

## **Examples – Atari Games**



https://www.youtube.com/watch?v=Vr5MR51KOc8

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#### **Rewards**

- $\bullet$  A reward  $R_t$  is a scalar feedback signal
- Indicates how well agent is doing at step t
- The agent's job is to maximize cumulative reward

Reinforcement learning is based on the reward hypothesis

#### **Definition (Reward Hypothesis)**

All goals can be described by the maximization of expected cumulative reward

Do you agree with this statement?

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## **Sequential Decision Making**

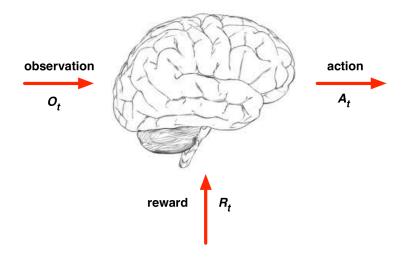
- Goal: select actions to maximize total future reward
- Actions may have long term consequences
- Reward may be delayed
- It may be better to sacrifice immediate reward to gain more long-term reward
- Examples:
  - A financial investment (may take months to mature)
  - Refueling a helicopter (might prevent a crash in several hours)
  - Blocking opponent moves (might help winning chances many moves from now)

#### **Examples of Rewards**

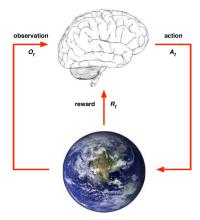
- Fly stunt manoeuvres in a helicopter
  - +ve reward for following desired trajectory
  - -ve reward for crashing
- Defeat the world champion at Backgammon
  - +/-ve reward for winning/losing a game
- Manage an investment portfolio
  - +ve reward for each \$ in bank
- Control a power station
  - +ve reward for producing power
  - -ve reward for exceeding safety thresholds
- Make a humanoid robot walk
  - +ve reward for forward motion
  - -ve reward for falling over
- Play many different Atari games better than humans
  - +/-ve reward for increasing/decreasing score

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## **Agent and Environment**



## **Agent and Environment**



- At each step t the agent:
  - Executes action A<sub>t</sub>
  - Receives observation O<sub>t</sub>
  - Receives scalar reward  $R_t$
- The environment:
  - Receives action At
  - ullet Emits observation  $O_{t+1}$
  - ullet Emits scalar reward  $R_{t+1}$
- t increments at env. step

**History and State** 

• The history is the sequence of observations, actions, rewards

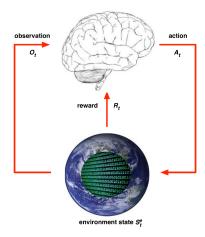
$$H_t = O_1, R_1, A_1, ..., A_{t-1}, O_t, R_t$$

- i.e. all observable variables up to time t
- i.e. the sensorimotor stream of a robot or embodied agent
- What happens next depends on the history:
  - The agent selects actions
  - The environment selects observations/rewards
- State is the information used to determine what happens next
- Formally, state is a function of the history:

$$S_t = f(H_t)$$

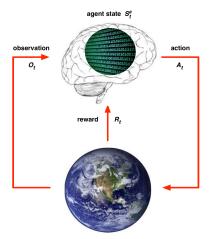
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## **Environment/World State**



- The environment state  $S_t^e$  is the environment's private representation
- i.e. whatever data the environment uses to pick the next observation/reward
- The environment state is not usually visible to the agent
- Even if  $S_t^e$  is visible, it may contain irrelevant information

## **Agent State**



- The agent state  $S_t^a$  is the agent's internal representation
- i.e. whatever information the agent uses to pick the next action
- i.e. it is the information used by reinforcement learning algorithms
- It can be any function of the history:

$$S_t^a = f(H_t)$$

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#### **Information State**

An information state (a.k.a. Markov state) contains all useful information from the history.

#### Definition

A state  $S_t$  is Markov if and only if

$$P(S_{t+1} \mid S_t) = P(S_{t+1} \mid S_1, ..., S_t)$$

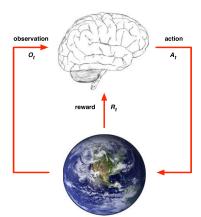
• The future is independent of the past given the present

$$H_{1:t} \rightarrow S_t \rightarrow H_{t+1:\infty}$$

- Once the state is known, the history may be thrown away
- i.e. the state is a sufficient statistic of the future
- The environment state  $S_t^e$  is Markov
- The history  $H_t$  is Markov

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#### **Fully Observeable Environments**



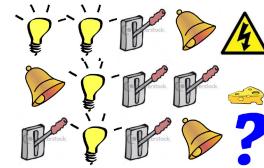
Full observability: agent directly observes environment state

$$O_t = S_t^a = S_t^e$$

- Agent state = environment state = information state
- Formally, this is a Markov decision process (MDP)

#### Rat Example





- What if agent state = last 3 items in sequence?
- What if agent state = counts for lights, bells and levers?
- What if agent state = complete sequence?

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#### **Partially Observable Environments**

- Partial observability: agent indirectly observes environment:
  - A robot with camera vision isn't told its absolute location
  - A trading agent only observes current prices
  - A poker playing agent only observes public cards
- Now agent state  $\neq$  environment state
- Formally this is a partially observable Markov decision process (POMDP)
- Agent must construct its own state representation  $S_t^a$ , e.g.
  - Complete history:  $S_t^a = H_t$
  - Beliefs of environment state:  $S_t^a = (P(S_t^e = s^1), ..., P(S_t^e = s^n))$
  - Recurrent neural network:  $S_t^a = \sigma(S_{t-1}^a W_s + O_t W_o)$

#### Major Components of an RL Agent

An RL agent may include one or more of these components:

Policy: agent's behaviour function

• Value function: how good is each state and/or action

• Model: agent's representation of the environment

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#### **Value Function**

- Value function is a prediction of future reward
- Used to evaluate the goodness/badness of states
- pused to select which action to take
- e.g. models the expected discounted future reward

$$v_{\pi}(s) = \mathbb{E}_{\pi}[R_{t+1} + \gamma R_{t+2} + \gamma^2 R_{t+3} + \cdots \mid S_t = s]$$

#### **Policy**

- A policy defines the agent's behaviour
- It is a map from state to action, e.g.
- Deterministic policy:  $a = \pi(s)$
- Stochastic policy:  $\pi(a|s) = P(A_t = a|S_t = s)$

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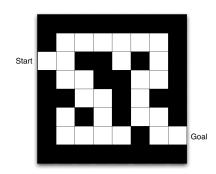
#### Model

- A model predicts what the environment will do next
- ullet  ${\cal P}$  predicts the next state
- $\bullet$   $\mathcal{R}$  predicts the next (immediate) reward, e.g.

$$\mathcal{P}_{ss'}^{a} = P(S_{t+1} = s' \mid S_{t} = s, A_{t} = a)$$
  
 $\mathcal{R}_{s}^{a} = \mathbb{E}[R_{t+1} \mid S_{t} = s, A_{t} = a]$ 

• Can be used for planning without actually performing actions

## Maze Example



Environment

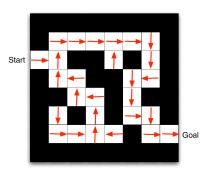
• Rewards: -1 per time-step

• Actions: N, E, S, W

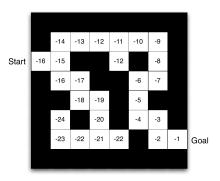
• States: Agent's location

• End at Goal state

### Maze Example: Policy and Value Function



Arrows represent policy  $\pi(s)$ 

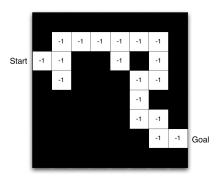


Numbers represent value  $v_{\pi}(s)$ 

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## Maze Example: Model



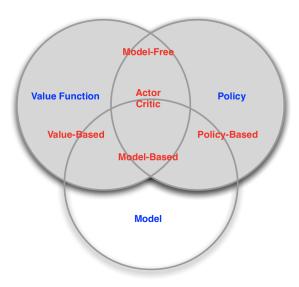
- Agent may have an internal model of the environment
- Dynamics: how actions change the state
- Rewards: how much reward from each state
- The model may be imperfect (most likely is)
- ullet Grid layout represents transition model  $\mathcal{P}^{\mathsf{a}}_{ss'}$
- ullet Numbers represent immediate reward  $\mathcal{R}^a_s$  from each state s (same for all a)

## Categorization of RL agents

- Value Based
  - No Policy (Implicit)
  - Value Function
- Policy Based
  - Policy
  - No Value Function
- Actor Critic
  - Policy
  - Value Function

- Model Free
  - Policy and/or Value Function
  - No Model
- Model Based
  - Policy and/or Value Function
  - Model

## RL Agent Taxonomy



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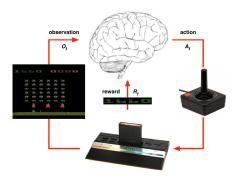
#### **Learning and Planning**

Two fundamental problems in sequential decision making

- Reinforcement Learning:
  - The environment is initially unknown
  - The agent interacts with the environment
  - The agent improves its policy
  - a.k.a. learning by doing, trail and error learning
- Planning:
  - A model of the environment is known
  - The agent performs computations with its model (without any external interaction)
  - The agent improves its policy
  - a.k.a. deliberation, reasoning, introspection, pondering, thought, search

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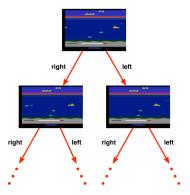
## Atari Example: Reinforcement Learning



- Rules of the game are unknown
- Learn directly from interactive game-play
- Pick actions on joystick, see pixels and scores

## Atari Example: Planning

- Rules of the game are known
- Can query emulator perfect model inside agent's brain
- If I take action a from state s:
  - what would the next state be?
  - what would the score be?
- Plan ahead to find optimal policy e.g. tree search



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## **Exploration and Exploitation**

- Reinforcement learning is like trial-and-error learning
- The agent should discover a good policy
- From its experiences of the environment
- Without losing too much reward along the way
- Exploration finds more information about the environment
- Exploitation exploits known information to maximize reward
- It is usually important to explore as well as exploit

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#### **Prediction and Control**

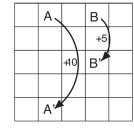
Subproblems within Reinforcement Learning:

- Prediction: evaluate the future
   How do I do given a policy?
- Control: optimize the future Find the best policy

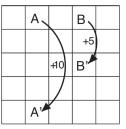
#### **Examples**

- Restaurant Selection
   Exploitation Go to your favorite restaurant
   Exploration Try a new restaurant
- Online Banner Advertisements
   Exploitation Show the most successful advert
   Exploration Show a different advert
- Game Playing
   Exploitation Play the move you believe is best
   Exploration Play an experimental move
- Robot Control Exploitation Do the movement you know works best Exploration Try a different movement

## **Gridworld Example: Prediction**



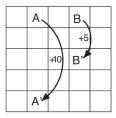






3.3	8.8	4.4	5.3	1.5
1.5	3.0	2.3	1.9	0.5
0.1	0.7	0.7	0.4	-0.4
-1.0	-0.4	-0.4	-0.6	-1.2
-1.9	-1.3	-1.2	-1.4	-2.0

## **Gridworld Example: Control**



22.0	24.4	22.0	19.4	17.5
19.8	22.0	19.8	17.8	16.0
17.8	19.8	17.8	16.0	14.4
16.0	17.8	16.0	14.4	13.0
14.4	16.0	14.4	13.0	11.7

<b>→</b>	$\Rightarrow$	<b>+</b>	<b></b>	<b>←</b>
$\uparrow$	<b>↑</b>	Ţ	<b>←</b>	<b>←</b>
<b>↑</b>	1	<b>_</b>	<b>1</b>	<b>↓</b>
₽	<b>↑</b>	<b>_</b>	<b>↓</b>	<b>↓</b>
<b>_</b>	1	<b>1</b>	<b>†</b>	<b>↓</b>

- a) gridworld
- b)  $v_*$

- c)  $\pi_*$
- What is the optimal value function over all possible policies?
- What is the optimal policy?

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#### **Markov Process**

A Markov process is a memoryless random process, i.e. a sequence of random states  $S_1, S_2, \ldots$  with the Markov property.

#### Reminder: Markov property

A state  $S_t$  is Markov if and only if

$$P(S_{t+1} | S_t) = P(S_{t+1} | S_1, ..., S_t)$$

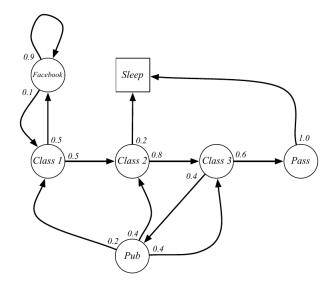
#### Definition (Markov Process/ Markov Chain)

A Markov Process (or Markov Chain) is a tuple  $(\mathcal{S}, \mathcal{P})$ 

- $\bullet$   $\ensuremath{\mathcal{S}}$  is a (finite) set of states
- $\bullet$   $\, \mathcal{P} \,$  is a state transition 0 probability matrix,

$$P_{ss'} = P(S_{t+1} = s' \mid S_t = s)$$

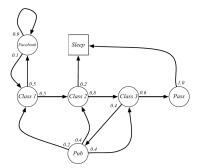
## **Example: Student Markov Chain**



**Markov Decision Processes** 

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#### **Example: Student Markov Chain Episodes**

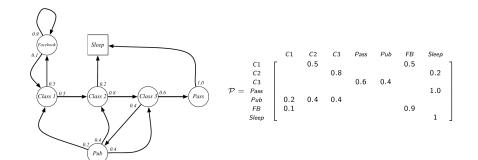


Sample episodes for starting from  $S_1 = C1$ 

$$S_1, S_2, \ldots, S_T$$

- C1 C2 C3 Pass Sleep
- C1 FB FB C1 C2 Sleep
- C1 C2 C3 Pub C2 C3 Pass Sleep
- C1 FB FB C1 C2 C3 Pub C1 FB FB FB C1 C2 C3 Pub C2 Sleep

**Example: Student Markov Chain Transition Matrix** 



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#### **Markov Reward Process**

A Markov reward process is a Markov chain with values.

#### Definition (MRP)

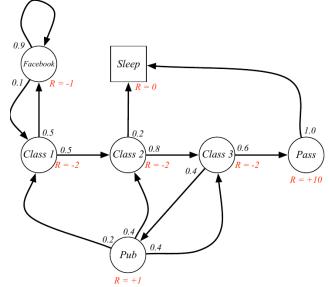
A Markov Reward Process is a tuple  $(S, \mathcal{P}, \mathcal{R}, \gamma)$ 

- ullet  ${\cal S}$  is a finite set of states
- ullet  ${\mathcal P}$  is a state transition probability matrix,

$$P(S_{t+1} | S_t) = P(S_{t+1} | S_1, ..., S_t)$$

- ullet  $\mathcal{R}$  is a reward function,  $\mathcal{R}_s = \mathbb{E}[R_{t+1}|S_t = s]$
- $\bullet \ \gamma$  is a discount factor,  $\gamma \in [0,1]$

## **Example: Student MRP**



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#### Return

#### Definition

The return  $G_t$  is the total discounted reward from time-step t.

$$G_t = R_{t+1} + \gamma R_{t+2} + \dots = \sum_{k=0}^{\infty} \gamma^k R_{t+k+1}$$

- ullet The discount  $\gamma \in [0,1]$  is the present value of future rewards
- The value of receiving reward R after k+1 time-steps is  $\gamma^k R$ .
- This values immediate reward above delayed reward.
  - ullet  $\gamma$  close to 0 leads to "myopic" evaluation
  - ullet  $\gamma$  close to 1 leads to "far-sighted" evaluation

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#### **Next time**

- Continue with MDP's and Bellmann Equation
- Dynamic Programming and Q-Learning

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# Why discount?

Most Markov reward and decision processes are discounted. Why?

- Mathematically convenient to discount rewards
- Avoids infinite returns in cyclic Markov processes
- Uncertainty about the future may not be fully represented
- If the reward is financial, immediate rewards may earn more interest than delayed rewards
- Animal/human behaviour shows preference for immediate reward
- It is sometimes possible to use *undiscounted* Markov reward processes (i.e.  $\gamma=1$ ), e.g. if all sequences terminate.