

TITEL: MANHATTAN DISTANCE

```
import heapq

class PuzzleState:
    def __init__(self, board, g, h):
        self.board = board # The current state of the board
        self.g = g # Cost to reach this node (depth)
        self.h = h # Heuristic cost (Manhattan distance)
        self.f = g + h # Total cost (f(n) = g(n) + h(n))

    def __lt__(self, other):
        return self.f < other.f # For priority queue to sort by f(n)

def print_board(board):
    """Print the current board state."""
    for row in board:
        print(" ".join(str(num) for num in row))
    print() # Empty line for better readability

def get_blank_position(board):
    for i in range(3):
        for j in range(3):
            if board[i][j] == 0: # Find the blank space (0)
                return (i, j)

def get_successors(state):
    successors = []
    x, y = get_blank_position(state.board) # Get position of blank tile
    directions = [(-1, 0), (1, 0), (0, -1), (0, 1)] # Possible moves
    for dx, dy in directions:
        new_x, new_y = x + dx, y + dy
        if 0 <= new_x < 3 and 0 <= new_y < 3: # Valid move
            new_board = [row[:] for row in state.board] # Copy the current board
            new_board[x][y], new_board[new_x][new_y] = new_board[new_x][new_y], new_board[x][y]
    # Swap
    successors.append(PuzzleState(new_board, state.g + 1, 0)) # Create new state
    return successors

def heuristic_manhattan_distance(board):
    distance = 0
    for i in range(3):
        for j in range(3):
            if board[i][j] != 0:
                target_x = (board[i][j] - 1) // 3
                target_y = (board[i][j] - 1) % 3
                distance += abs(i - target_x) + abs(j - target_y)
```

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    return distance

def is_goal_state(board):
    return board == [[1, 2, 3],
                     [8, 0, 4],
                     [7, 6, 5]] # Check if the board is in the goal state

def a_star_search_manhattan_distance(start_board):
    start_state = PuzzleState(start_board, 0, heuristic_manhattan_distance(start_board))
    open_set = []
    heapq.heappush(open_set, start_state)
    closed_set = set()

    while open_set:
        current_state = heapq.heappop(open_set)

        # Print current board state and details
        print("Current board state:")
        print_board(current_state.board)
        print(f"g(n): {current_state.g}, h(n): {current_state.h}, f(n): {current_state.f}\n")

        # Check if we've reached the goal
        if is_goal_state(current_state.board):
            print("Goal state reached!")
            return current_state.g # Return the cost to reach the goal

        closed_set.add(tuple(map(tuple, current_state.board)))

        for successor in get_successors(current_state):
            successor.h = heuristic_manhattan_distance(successor.board)
            successor.f = successor.g + successor.h

            if tuple(map(tuple, successor.board)) in closed_set:
                continue

            heapq.heappush(open_set, successor)

    return None # No solution found

def get_user_input():
    board = []
    for i in range(3):
        while True:
            row = input(f"Enter row {i + 1} (3 numbers separated by space): ")
            nums = list(map(int, row.split()))
            if len(nums) == 3 and all(0 <= num <= 8 for num in nums):
                board.append(nums)
                break

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    else:
        print("Invalid input. Please enter 3 numbers between 0 and 8.")
    return board
```

```
if __name__ == "__main__":
    start_board = get_user_input()
    steps = a_star_search_manhattan_distance(start_board)
    print(f"Steps to solve with Manhattan Distance heuristic: {steps}")
```

output:

```
Enter row 1 (3 numbers separated by space): 2 8 3
Enter row 2 (3 numbers separated by space): 1 6 4
Enter row 3 (3 numbers separated by space): 7 0 5
Current board state:
2 8 3
1 6 4
7 0 5
```

g(n): 0, h(n): 9, f(n): 9

```
Current board state:
2 8 3
1 6 4
7 5 0
```

g(n): 1, h(n): 8, f(n): 9

```
Current board state:
2 8 3
1 6 4
0 7 5
```

g(n): 1, h(n): 10, f(n): 11

```
Current board state:
2 8 3
1 0 4
7 6 5
```

g(n): 1, h(n): 10, f(n): 11

```
Current board state:
2 8 3
1 6 0
7 5 4
```

g(n): 2, h(n): 9, f(n): 11

```
Current board state:
2 0 3
```

1 8 4
7 6 5

$g(n): 2, h(n): 9, f(n): 11$

Current board state:

2 8 3
1 0 6
7 5 4

$g(n): 3, h(n): 8, f(n): 11$

Current board state:

0 2 3
1 8 4
7 6 5

$g(n): 3, h(n): 8, f(n): 11$

Current board state:

2 0 3
1 8 6
7 5 4

$g(n): 4, h(n): 7, f(n): 11$

Current board state:

2 8 3
1 4 0
7 6 5

$g(n): 2, h(n): 9, f(n): 11$

Current board state:

2 8 3
1 5 6
7 0 4

$g(n): 4, h(n): 7, f(n): 11$

Current board state:

1 2 3
0 8 4
7 6 5

$g(n): 4, h(n): 7, f(n): 11$

Current board state:

2 8 3
1 5 6
7 4 0

$g(n): 5, h(n): 6, f(n): 11$

Current board state:

2 8 3

1 4 5

7 6 0

$g(n): 3, h(n): 8, f(n): 11$

Current board state:

0 2 3

1 8 6

7 5 4

$g(n): 5, h(n): 6, f(n): 11$

Current board state:

2 8 3

1 4 5

7 0 6

$g(n): 4, h(n): 7, f(n): 11$

Current board state:

1 2 3

0 8 6

7 5 4

$g(n): 6, h(n): 5, f(n): 11$

Current board state:

2 8 3

0 6 4

1 7 5

$g(n): 2, h(n): 11, f(n): 13$

Current board state:

2 8 3

0 1 6

7 5 4

$g(n): 4, h(n): 9, f(n): 13$

Current board state:

2 8 3

1 4 5

0 7 6

$g(n): 5, h(n): 8, f(n): 13$

Current board state:

1 2 3

7 8 6

0 5 4

$g(n): 7, h(n): 6, f(n): 13$

Current board state:

1 2 3

8 0 6

7 5 4

$g(n): 7, h(n): 6, f(n): 13$

Current board state:

2 3 0

1 8 4

7 6 5

$g(n): 3, h(n): 10, f(n): 13$

Current board state:

2 8 3

1 0 5

7 4 6

$g(n): 5, h(n): 8, f(n): 13$

Current board state:

1 2 3

7 8 4

0 6 5

$g(n): 5, h(n): 8, f(n): 13$

Current board state:

2 8 0

1 4 3

7 6 5

$g(n): 3, h(n): 10, f(n): 13$

Current board state:

2 8 3

1 5 6

0 7 4

$g(n): 5, h(n): 8, f(n): 13$

Current board state:

2 8 3
1 5 0
7 4 6

$g(n): 6, h(n): 7, f(n): 13$

Current board state:

2 8 3
1 5 0
7 4 6

$g(n): 6, h(n): 7, f(n): 13$

Current board state:

2 8 0
1 6 3
7 5 4

$g(n): 3, h(n): 10, f(n): 13$

Current board state:

2 3 0
1 8 6
7 5 4

$g(n): 5, h(n): 8, f(n): 13$

Current board state:

1 2 3
8 0 4
7 6 5

$g(n): 5, h(n): 8, f(n): 13$

Goal state reached!

Steps to solve with Manhattan Distance heuristic: 5