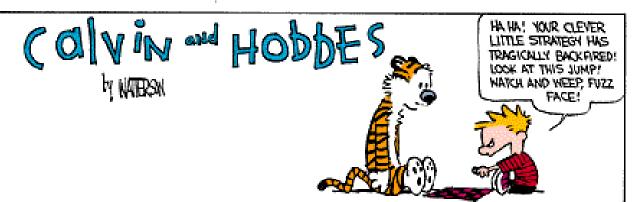
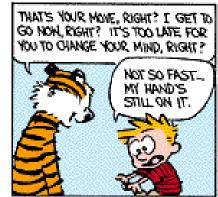
Adversarial Search Chapter 5

Mausam

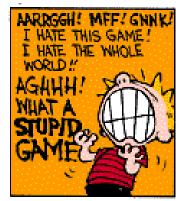
(Based on slides of Stuart Russell, Andrew Parks, Henry Kautz, Linda Shapiro, Diane Cook)





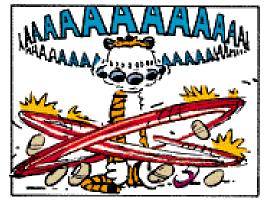
















Game Playing

Why do AI researchers study game playing?

- 1. It's a good reasoning problem, formal and nontrivial.
- 2. Direct comparison with humans and other computer programs is easy.

What Kinds of Games?

Mainly games of strategy with the following characteristics:

- 1. Sequence of moves to play
- 2. Rules that specify possible moves
- 3. Rules that specify a payment for each move
- 4. Objective is to maximize your payment

Games vs. Search Problems

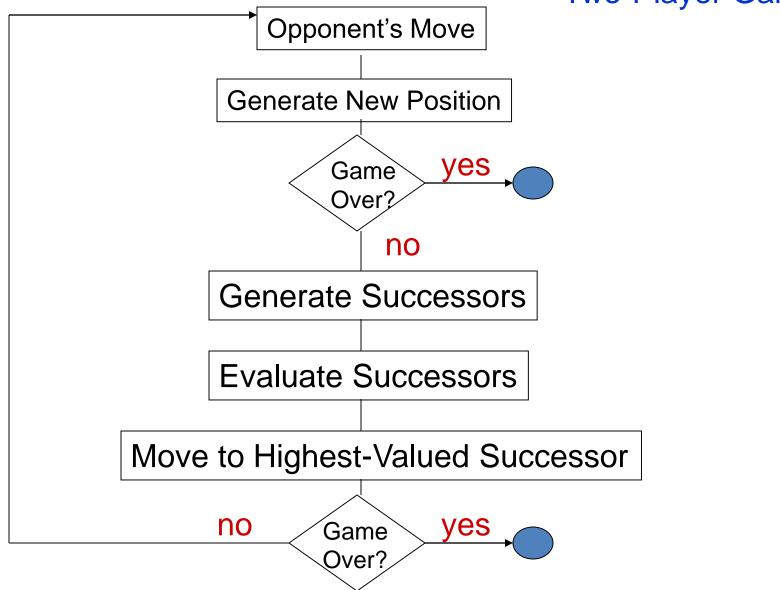
Unpredictable opponent

 specifying a move for every possible opponent reply

Time limits

unlikely to find goal, must approximate

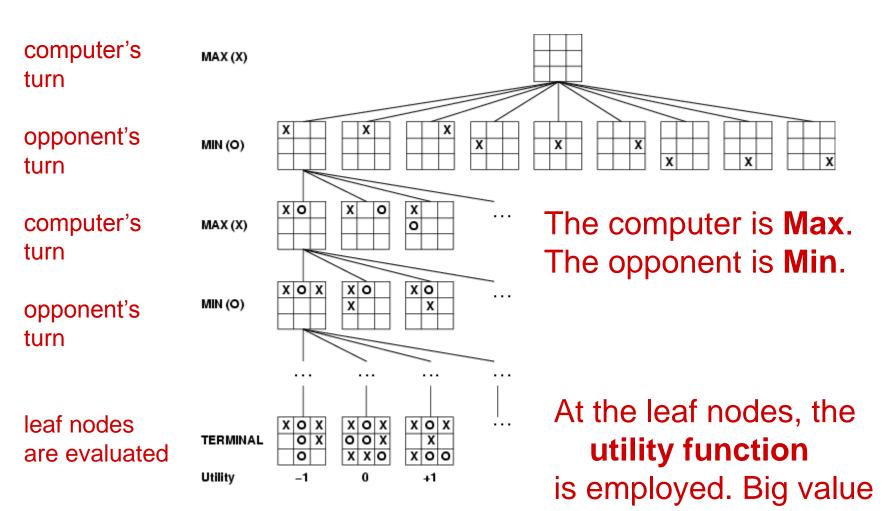
Two-Player Game



Games as Adversarial Search

- States:
 - board configurations
- Initial state:
 - the board position and which player will move
- Successor function:
 - returns list of (move, state) pairs, each indicating a legal move and the resulting state
- Terminal test:
 - determines when the game is over
- Utility function:
 - gives a numeric value in terminal states(e.g., -1, 0, +1 for loss, tie, win)

Game Tree (2-player, Deterministic, Turns)



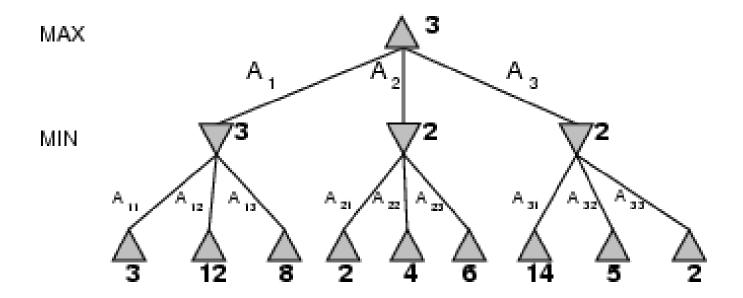
means good, small is bad.

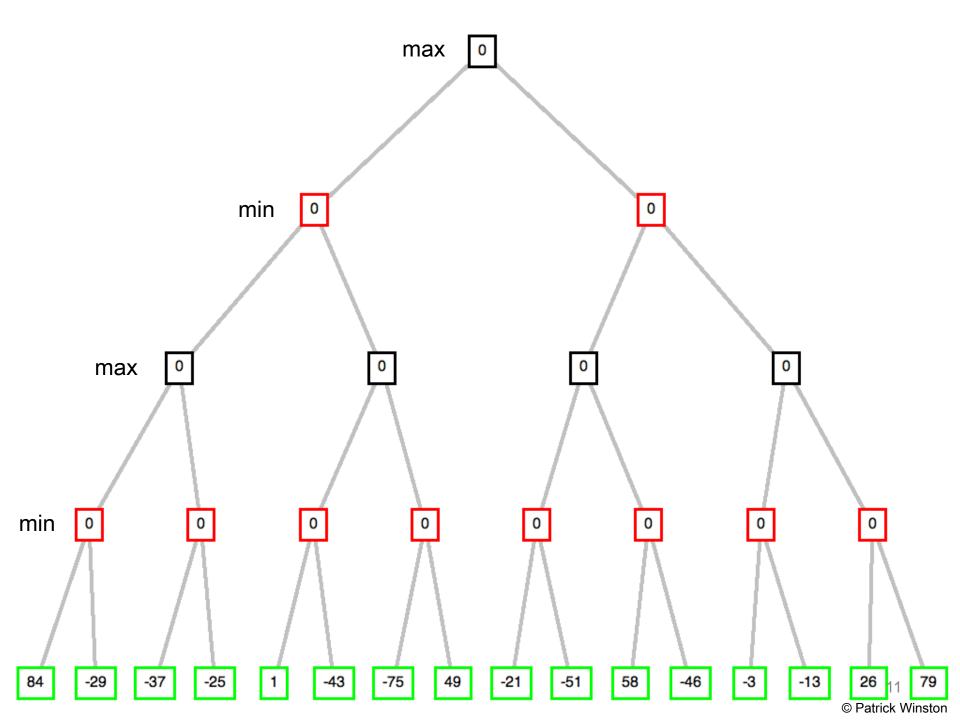
Mini-Max Terminology

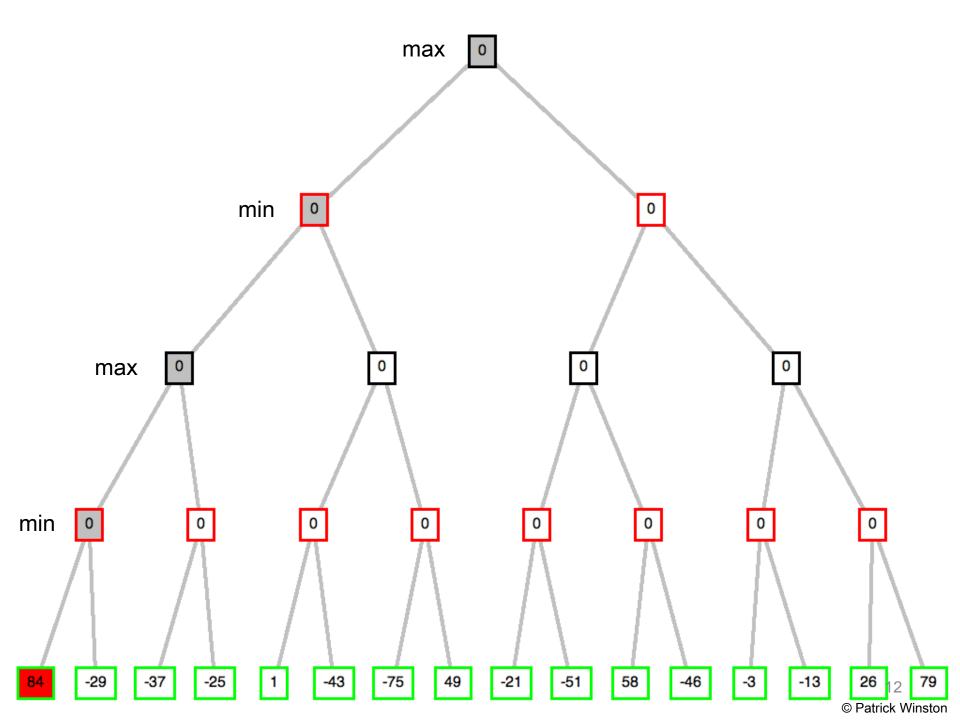
- move: a move by both players
- ply: a half-move
- utility function: the function applied to leaf nodes
- backed-up value
 - of a max-position: the value of its largest successor
 - of a min-position: the value of its smallest successor
- minimax procedure: search down several levels; at the bottom level apply the utility function, back-up values all the way up to the root node, and that node selects the move.

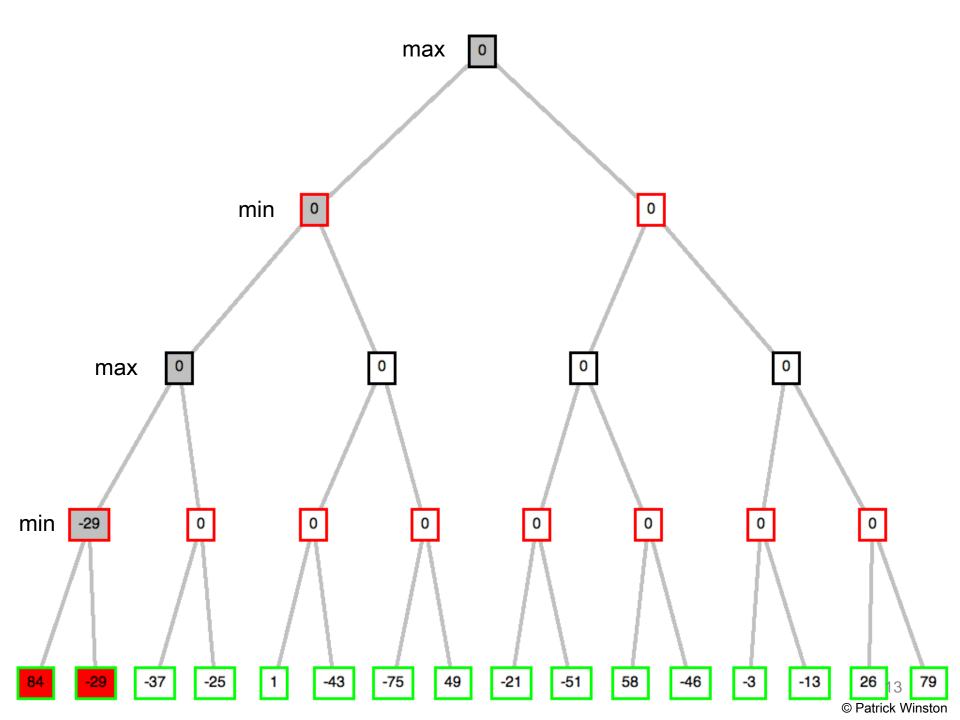
Minimax

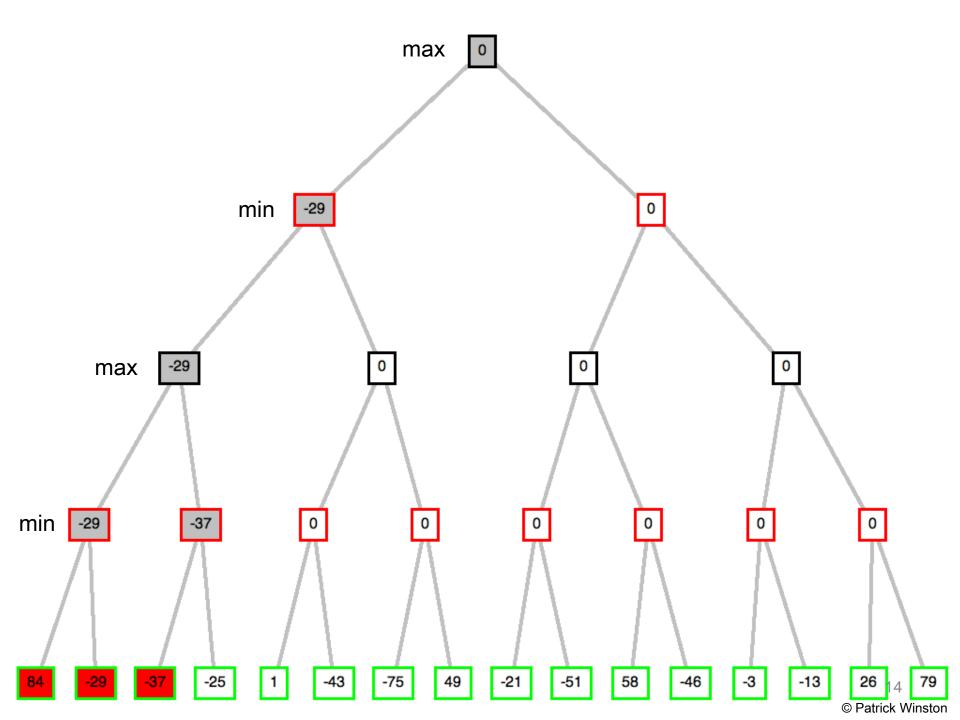
- Perfect play for deterministic games
- Idea: choose move to position with highest minimax value
 best achievable payoff against best play
- E.g., 2-ply game:

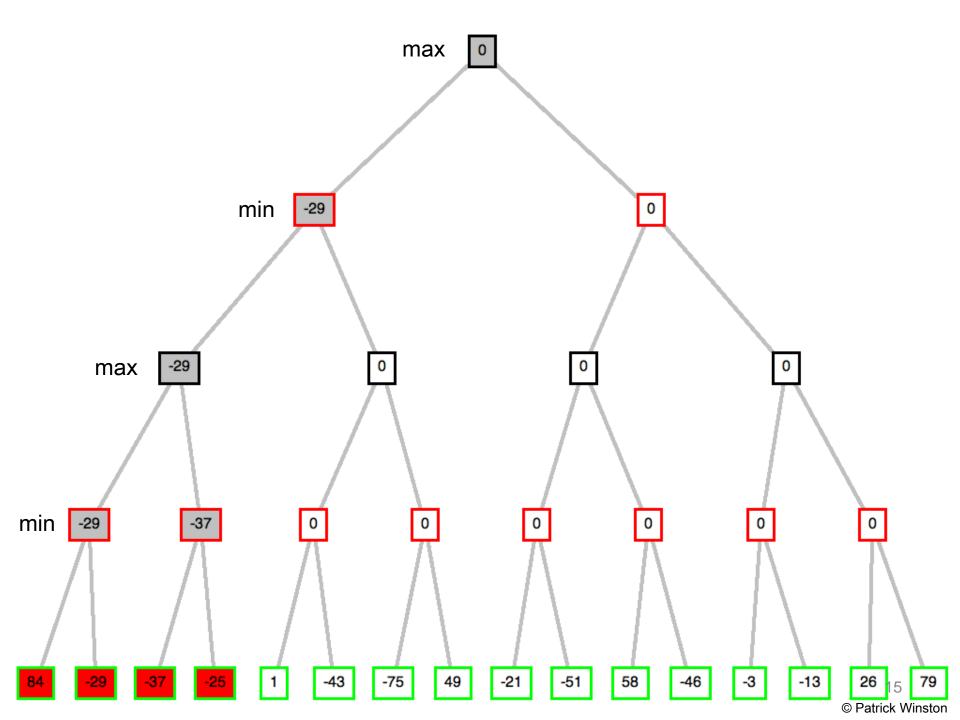


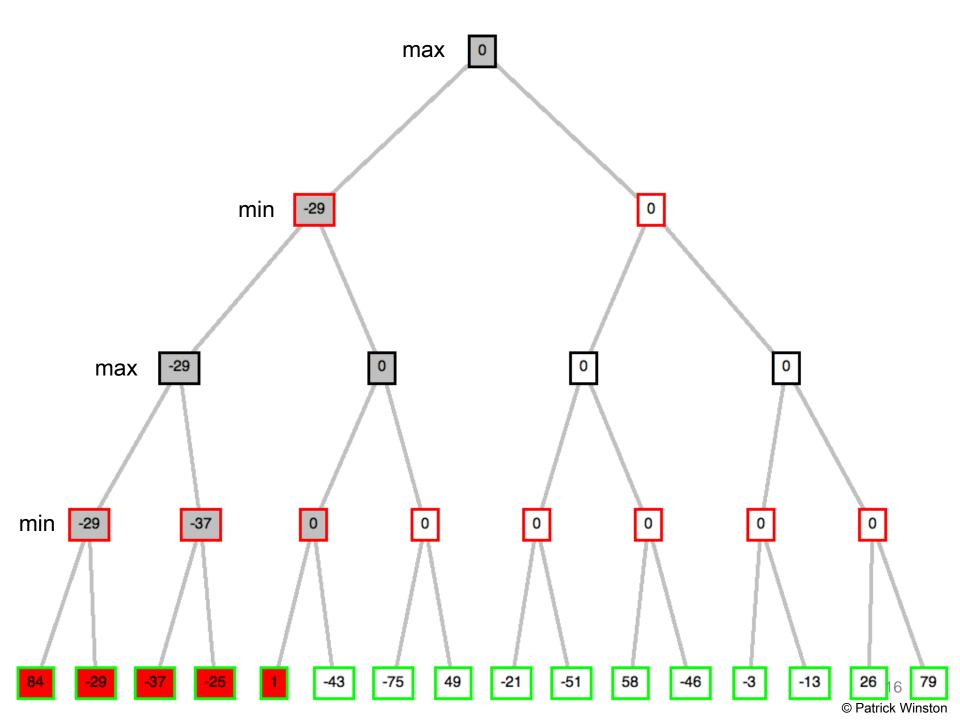


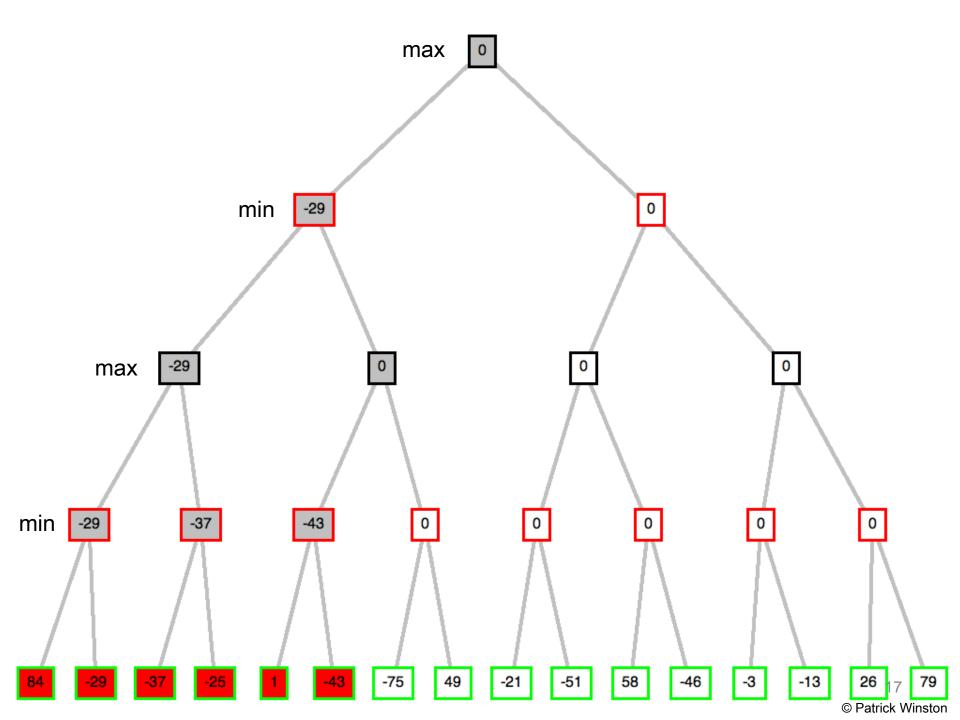


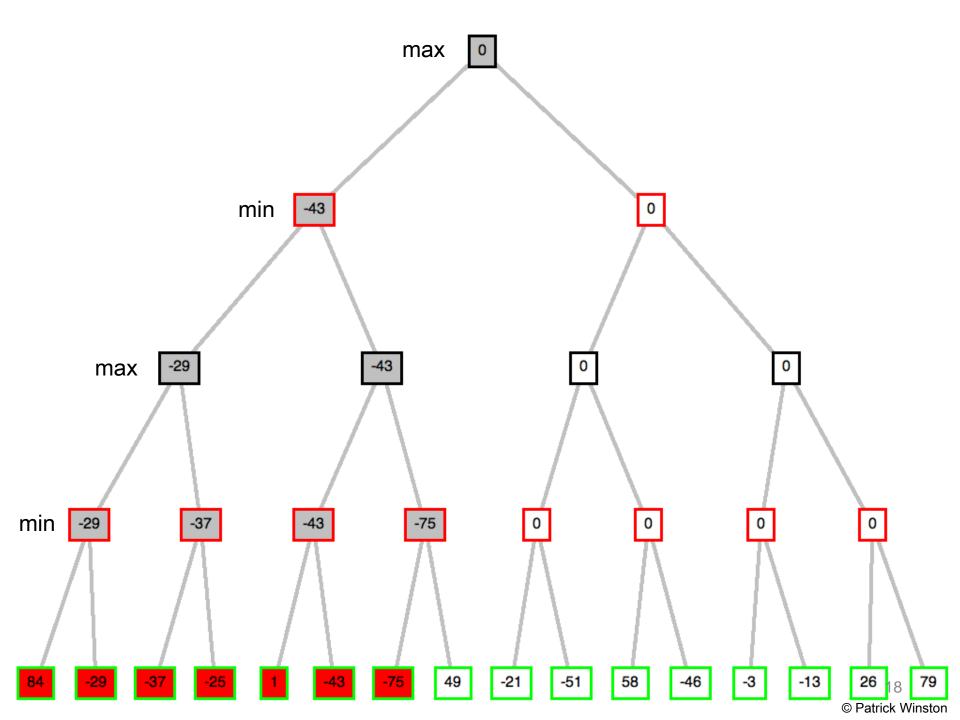


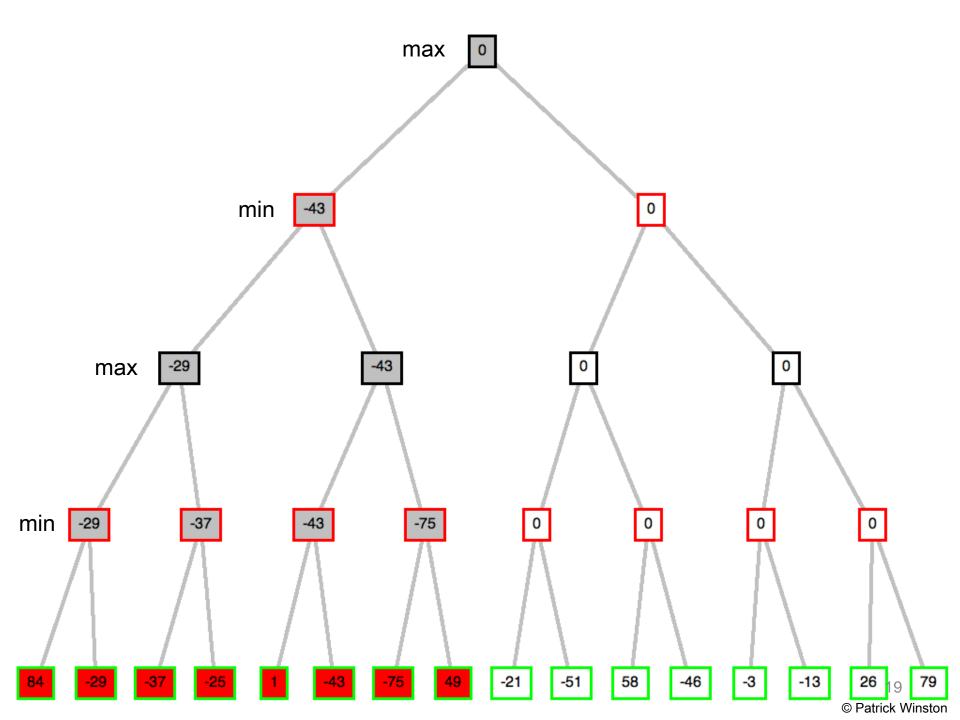


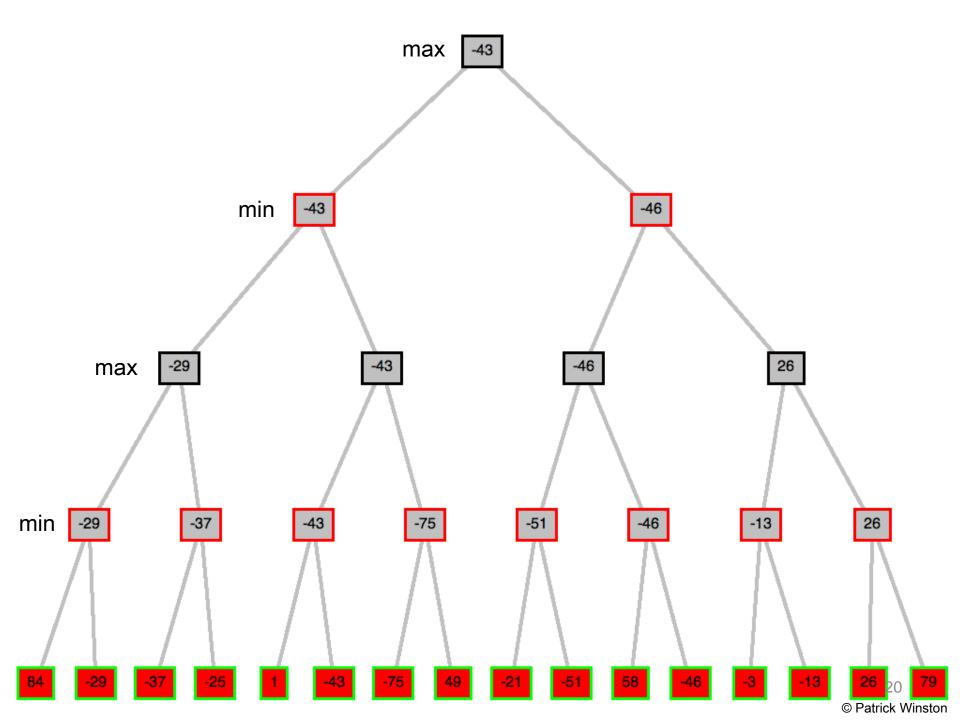


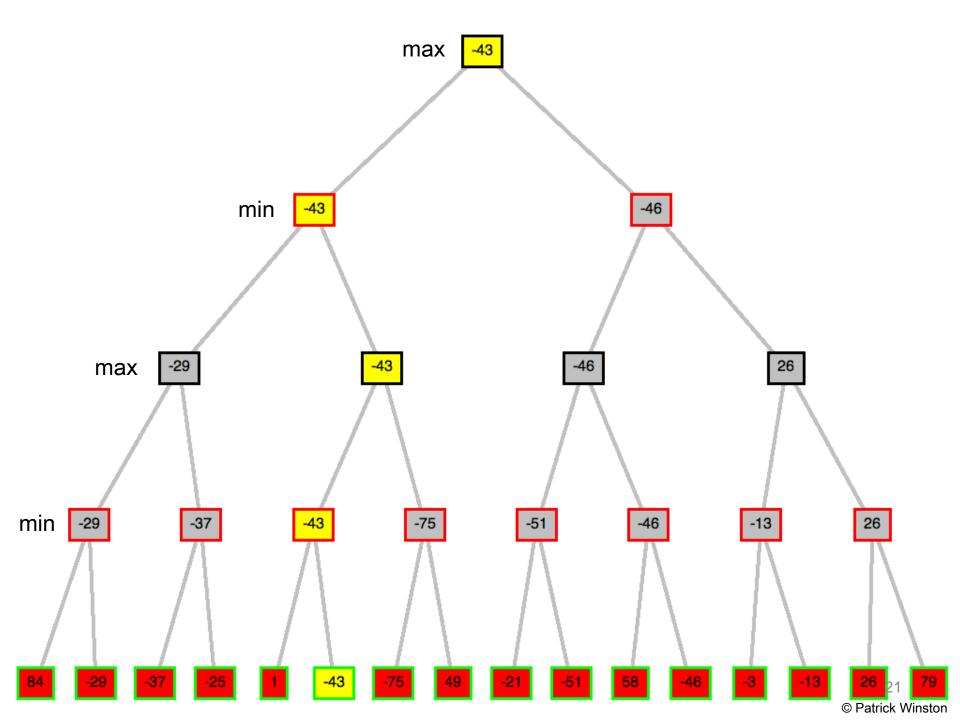












Minimax Strategy

 Why do we take the min value every other level of the tree?

 These nodes represent the opponent's choice of move.

 The computer assumes that the human will choose that move that is of least value to the computer.

Minimax algorithm Adversarial analogue of DFS

```
function Minimax-Decision(state) returns an action
   v \leftarrow \text{MAX-VALUE}(state)
   return the action in Successors(state) with value v
function Max-Value(state) returns a utility value
   if Terminal-Test(state) then return Utility(state)
   v \leftarrow -\infty
   for a, s in Successors(state) do
      v \leftarrow \text{Max}(v, \text{Min-Value}(s))
   return v
function Min-Value(state) returns a utility value
   if Terminal-Test(state) then return Utility(state)
   v \leftarrow \infty
   for a, s in Successors(state) do
      v \leftarrow \text{Min}(v, \text{Max-Value}(s))
   return v
```

Properties of Minimax

- Complete?
 - Yes (if tree is finite)
- Optimal?
 - Yes (against an optimal opponent)
 - No (does not exploit opponent weakness against suboptimal opponent)
- Time complexity?
 - O(b^m)
- Space complexity?
 - O(bm) (depth-first exploration)

Good Enough?

Chess:

- branching factor b≈35
- game length m≈100
- search space $b^m \approx 35^{100} \approx 10^{154}$

The Universe:

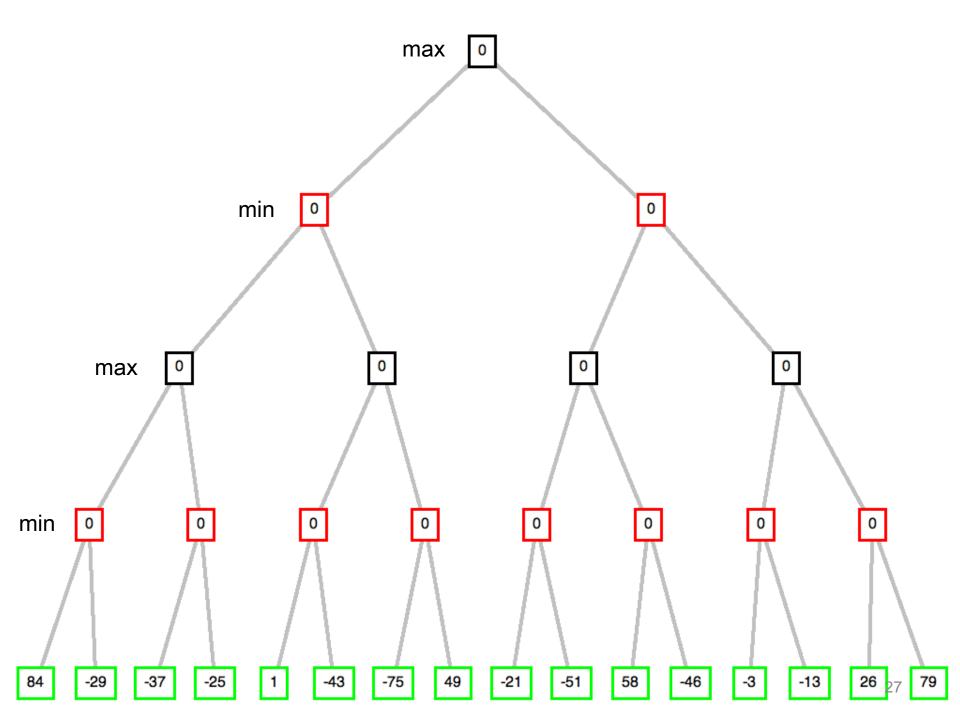
- number of atoms $\approx 10^{78}$
- age ≈ 10^{18} seconds
- -10^8 moves/sec x 10^{78} x 10^{18} = 10^{104}
- Exact solution completely infeasible

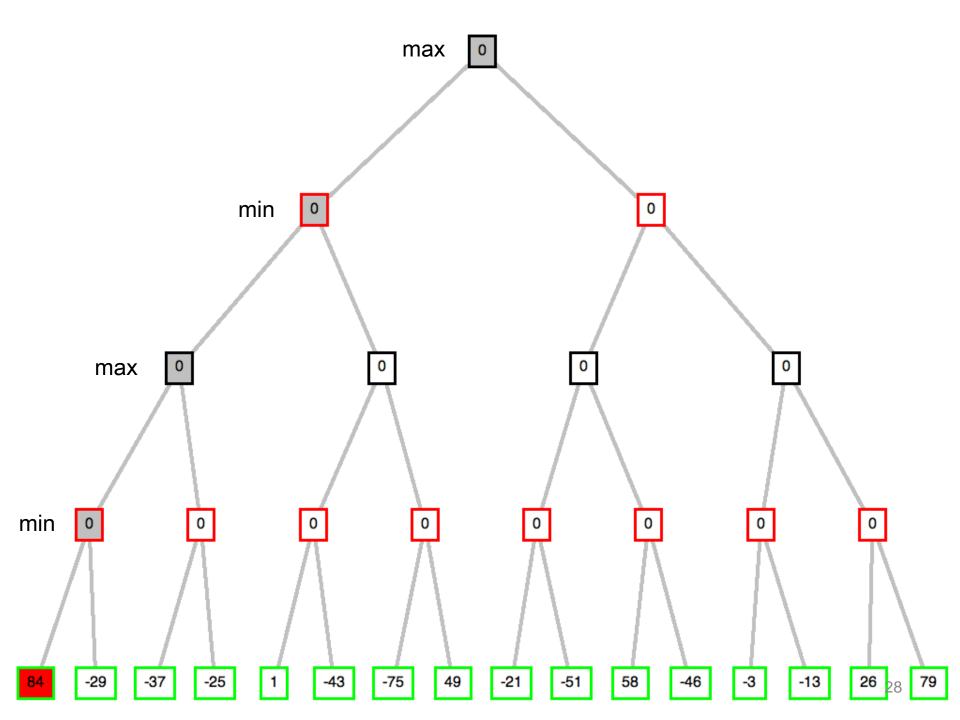
Alpha-Beta Procedure

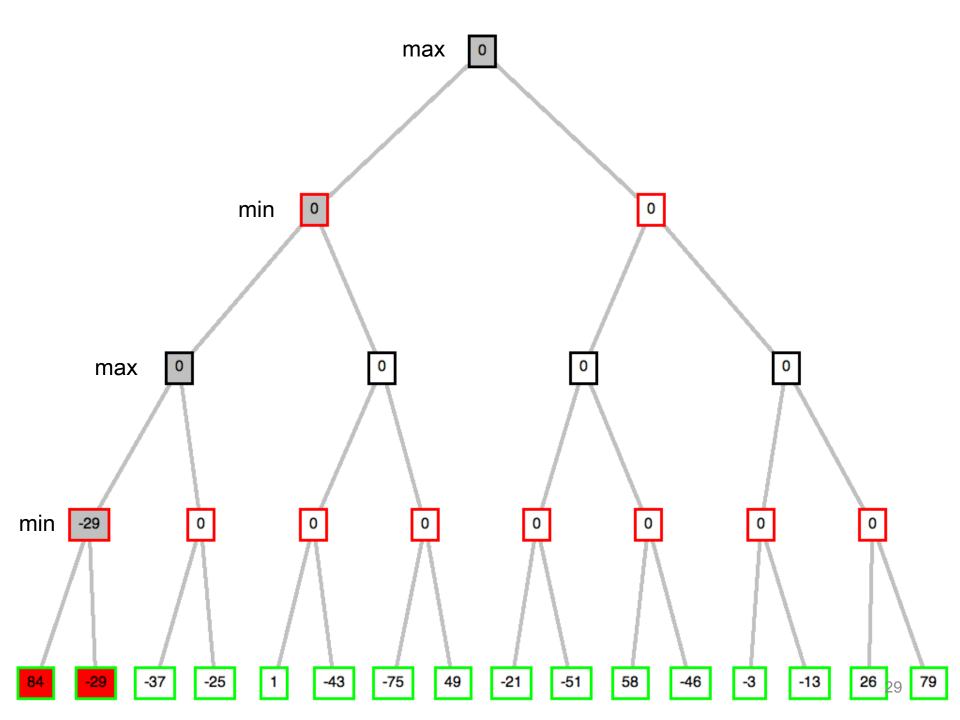
- The alpha-beta procedure can speed up a depth-first minimax search.
- Alpha: a lower bound on the value that a max node may ultimately be assigned

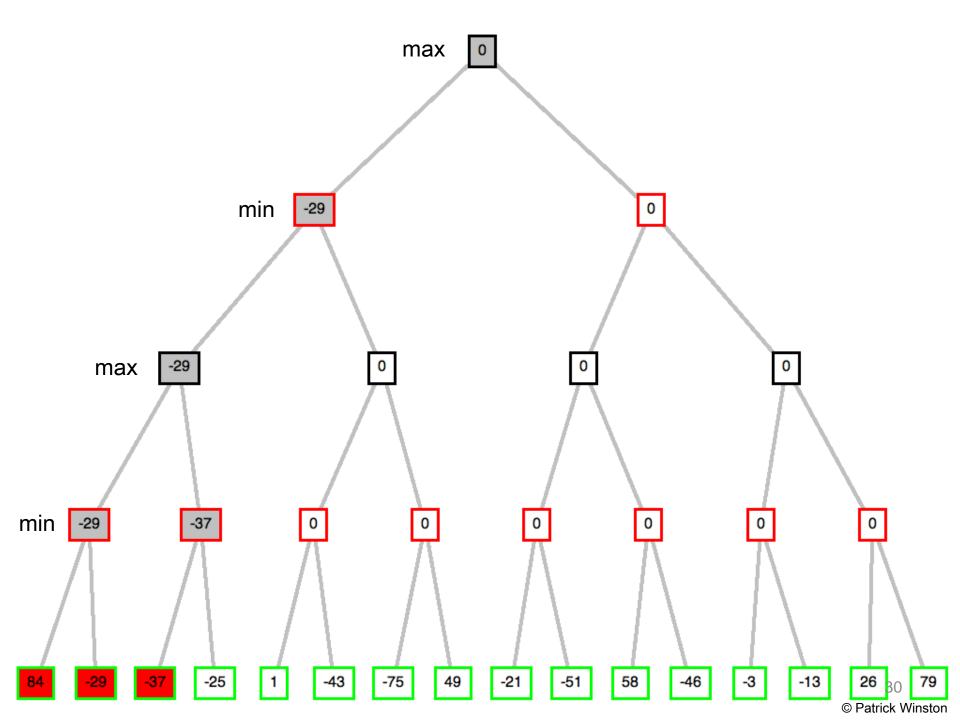
$$V \ge \alpha$$

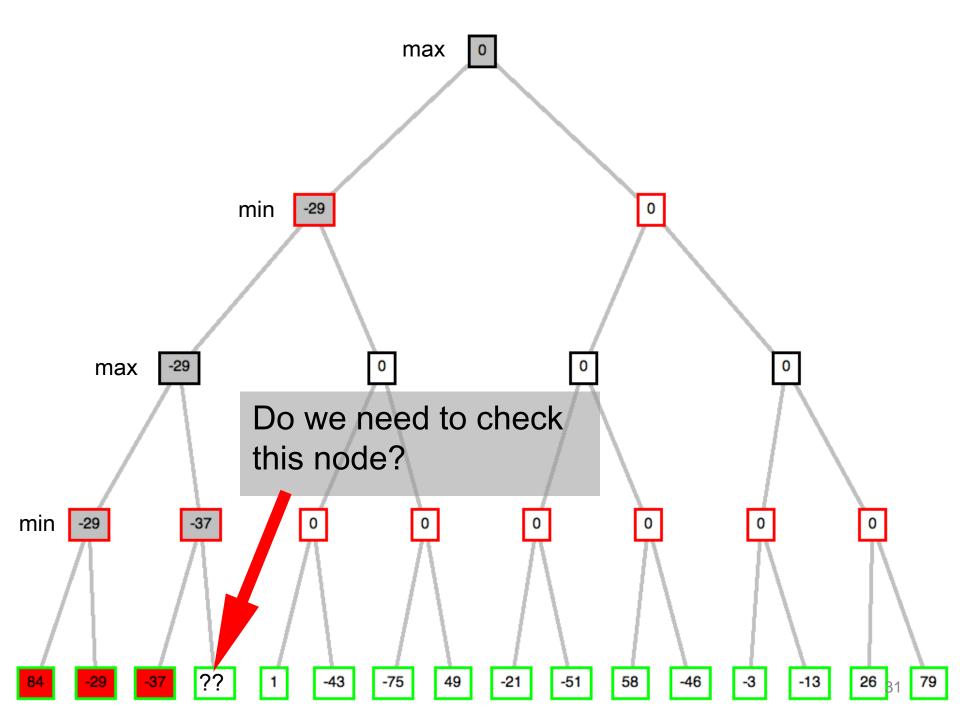
 Beta: an upper bound on the value that a minimizing node may ultimately be assigned

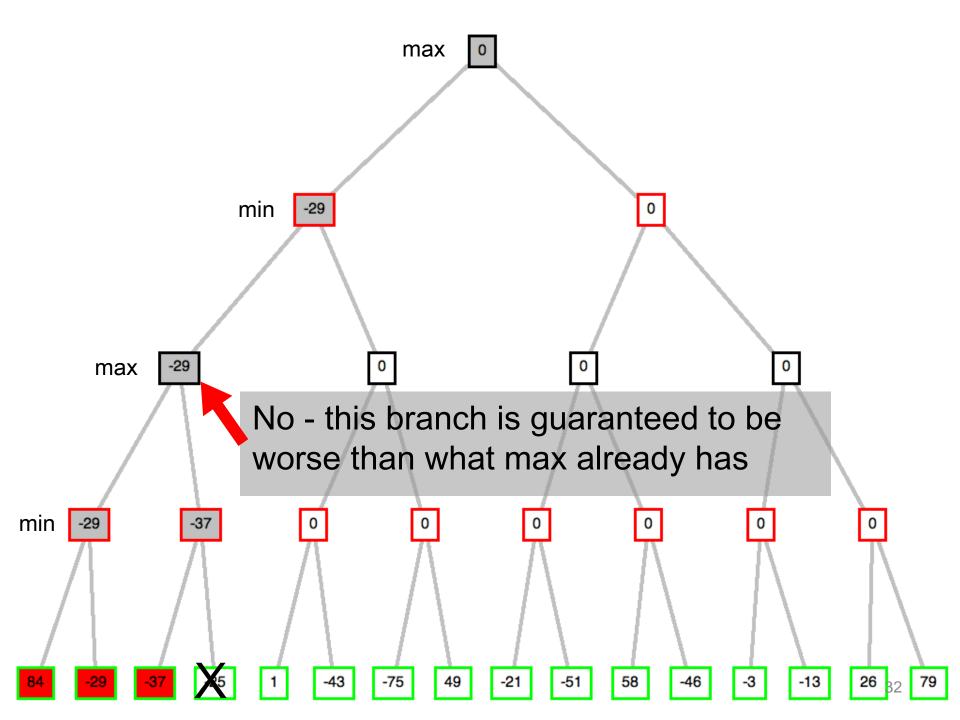






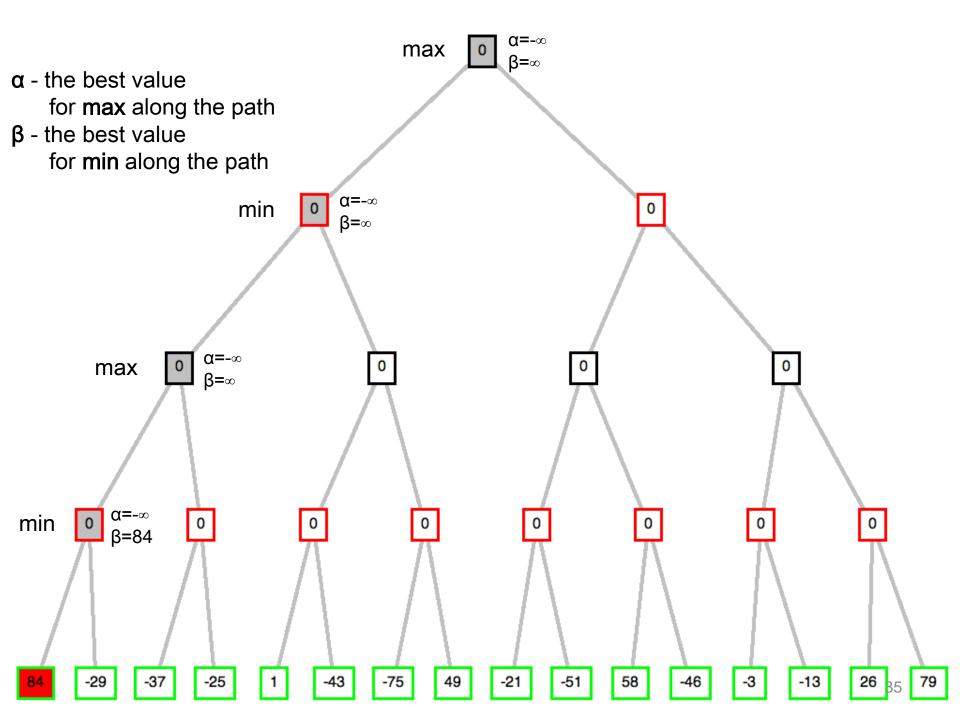


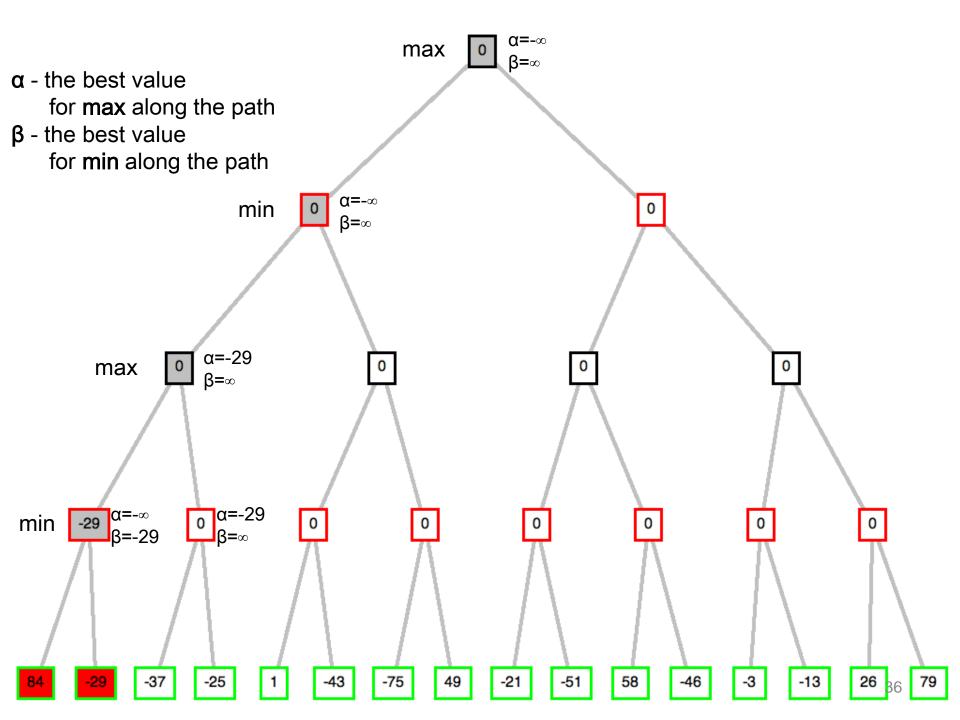


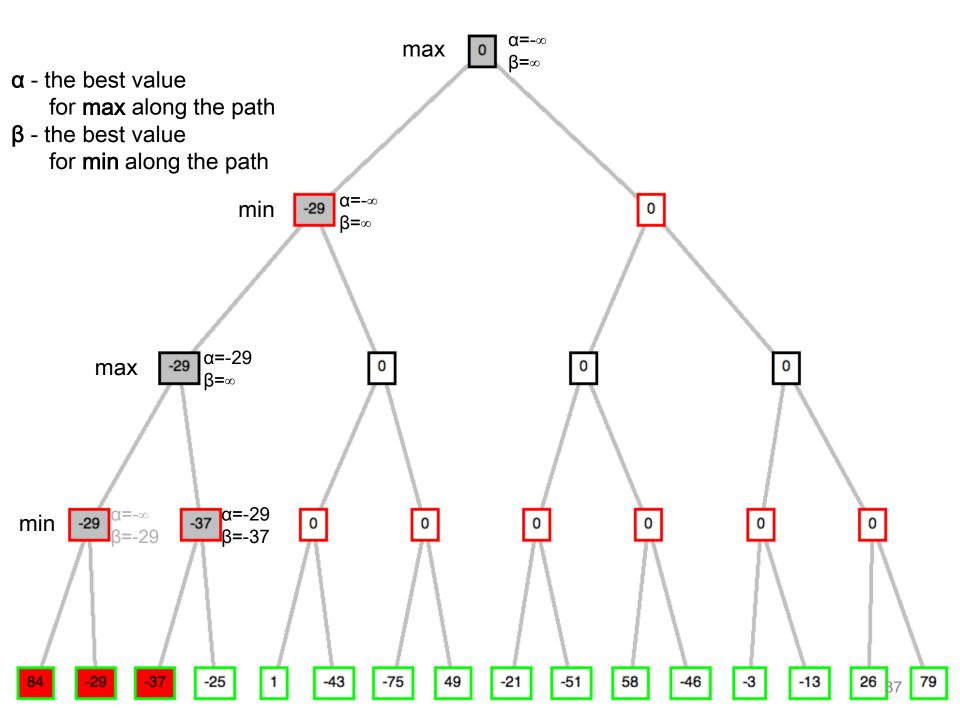


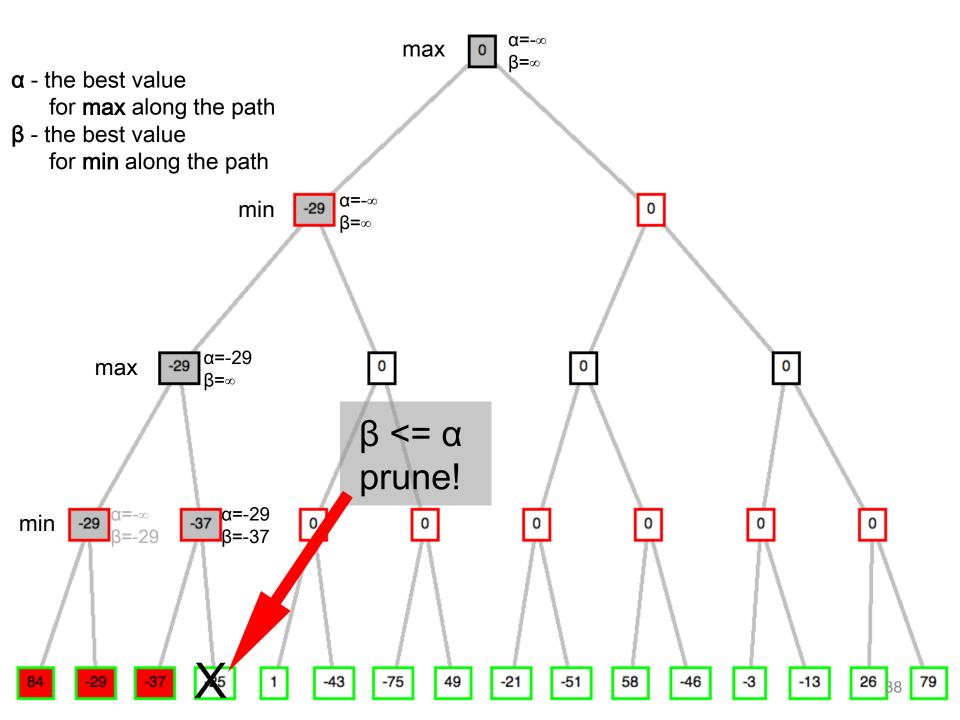
Alpha-Beta

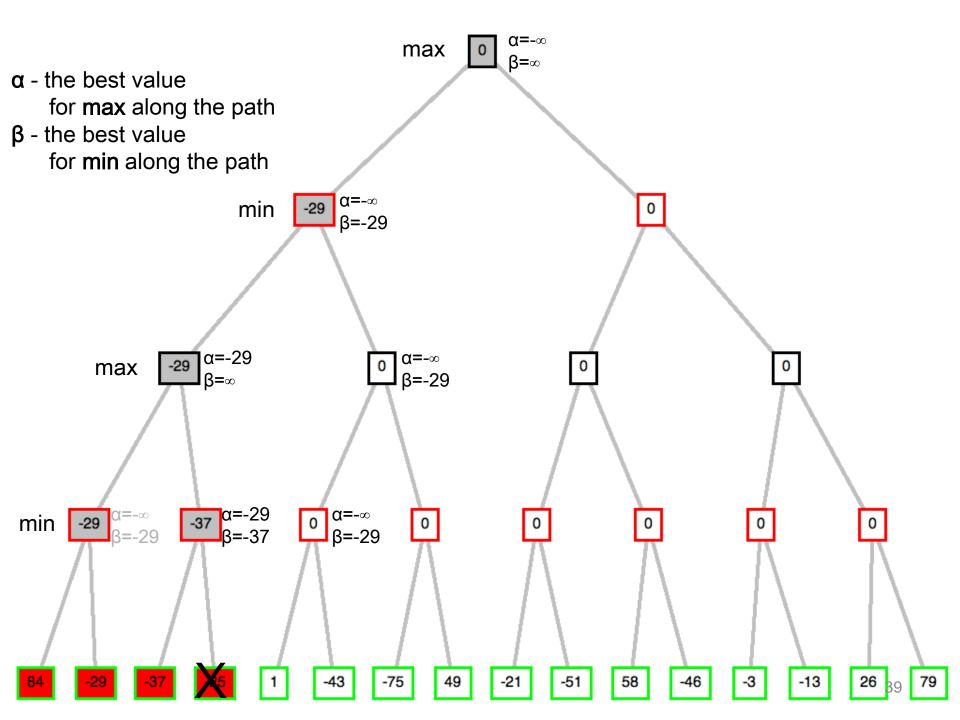
Alpha-Beta

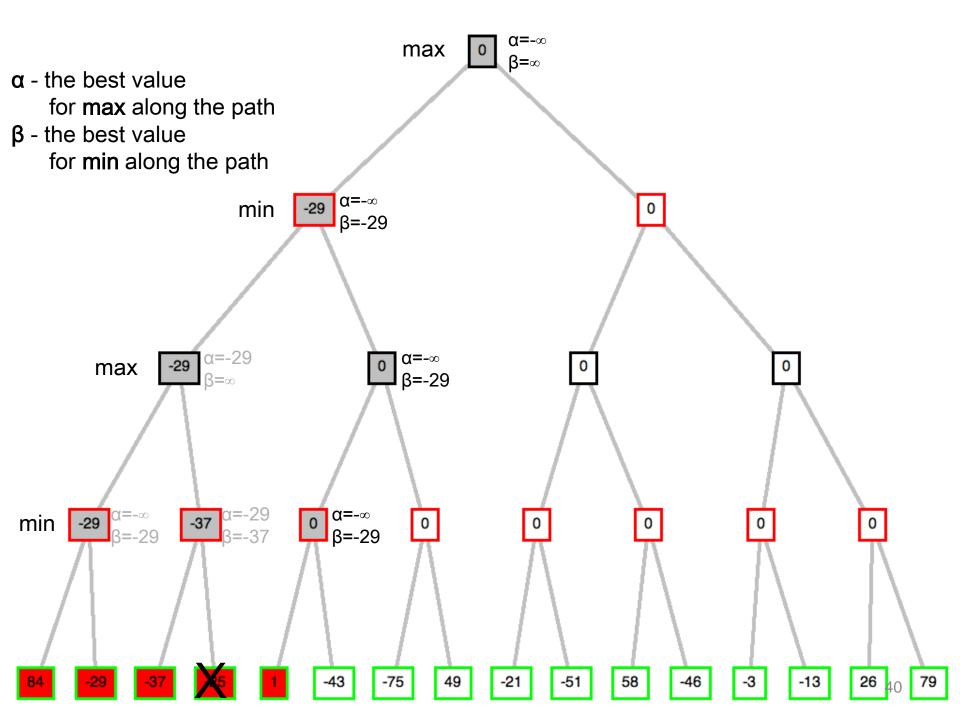


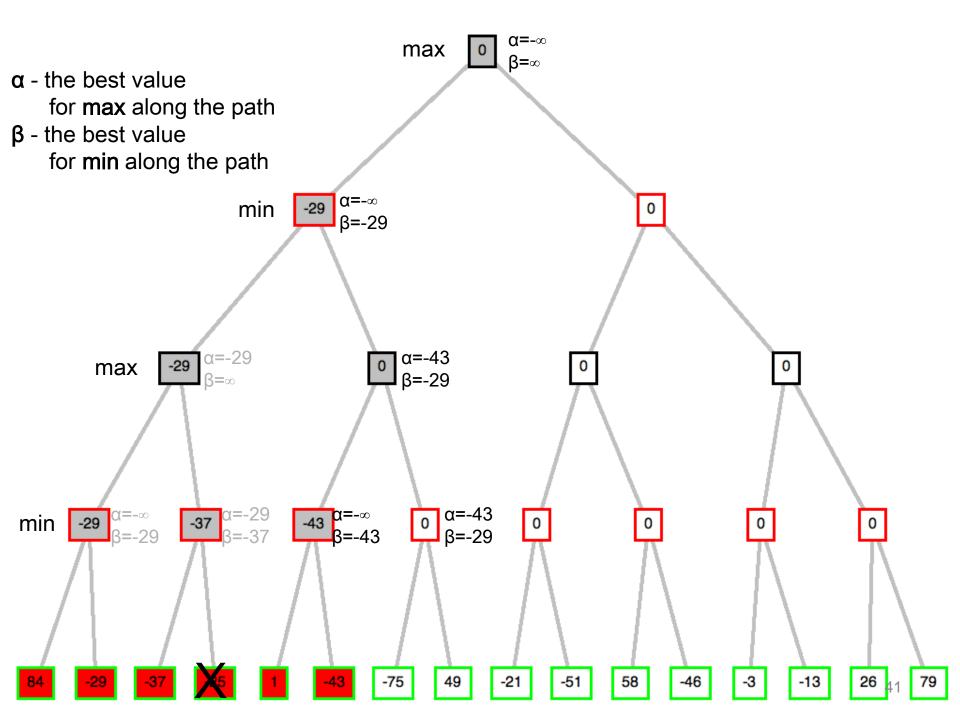


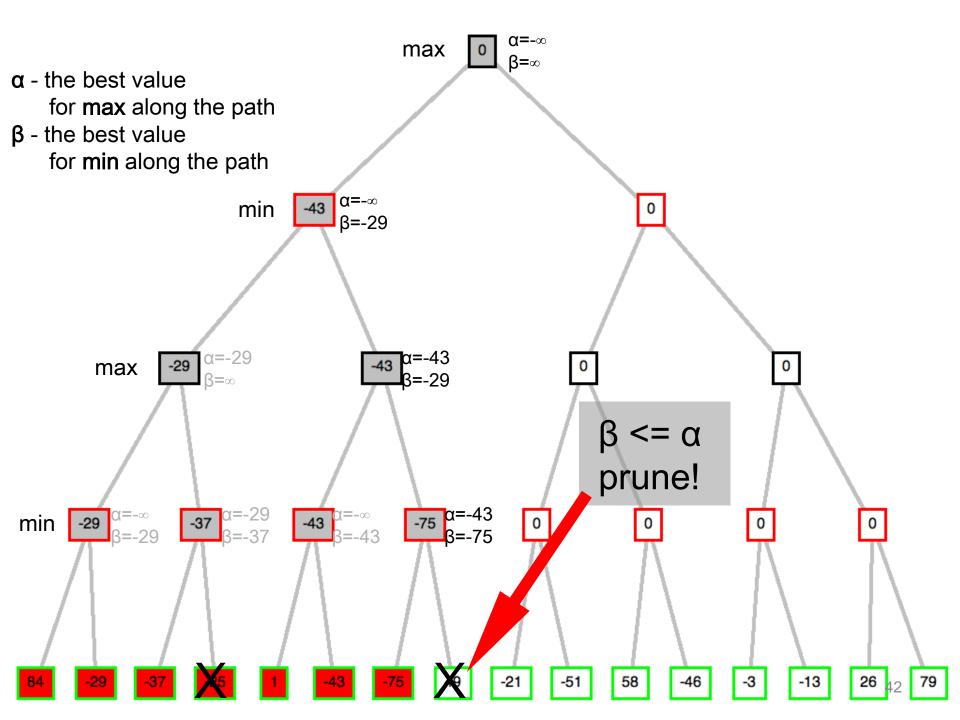


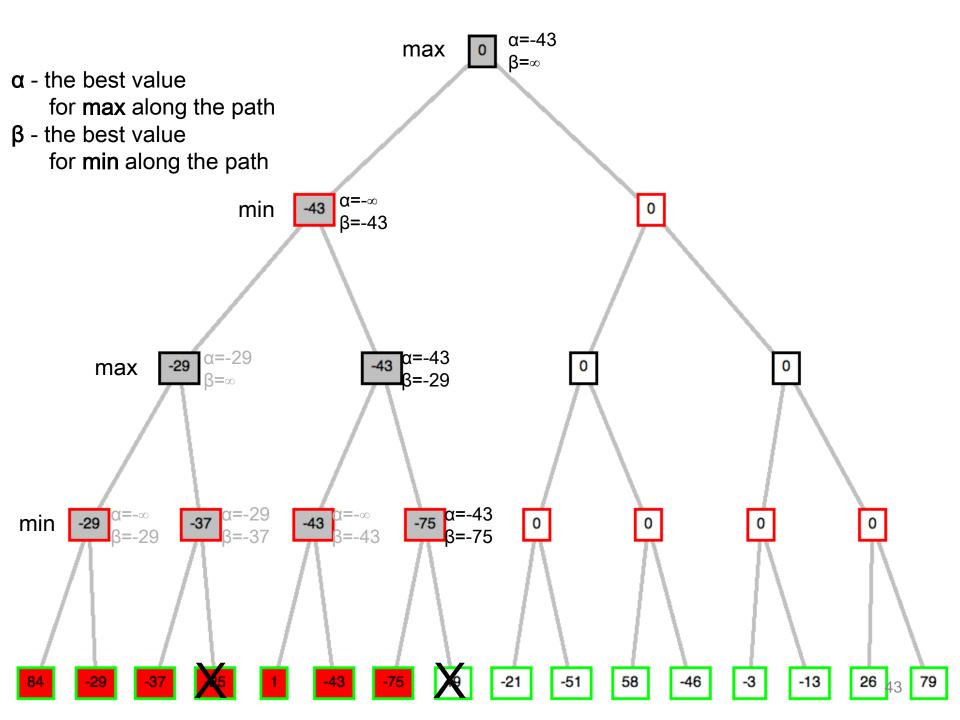


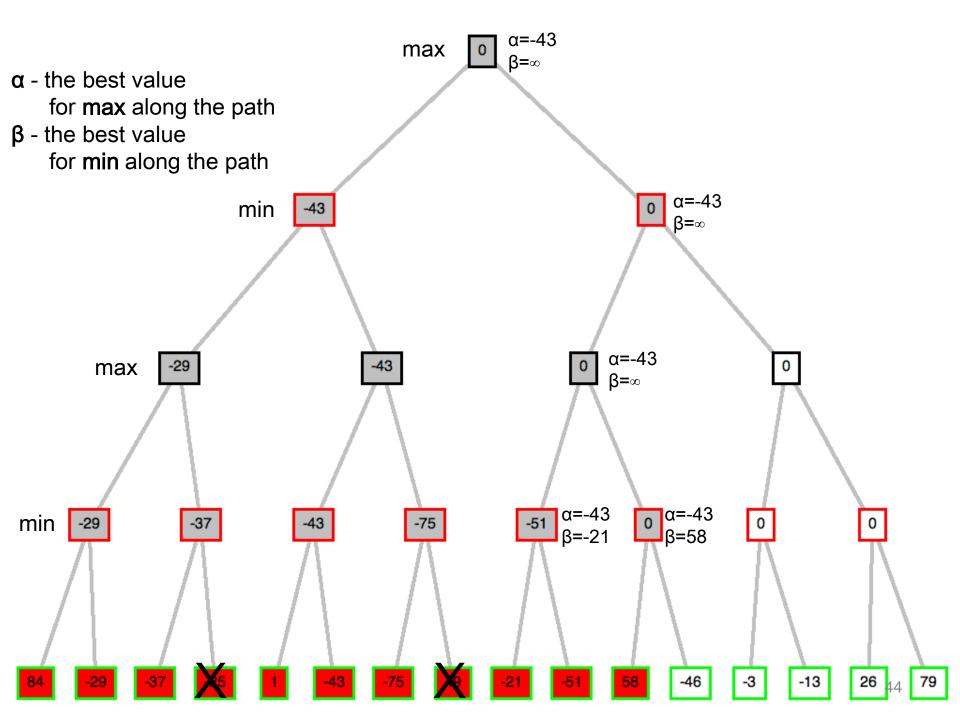


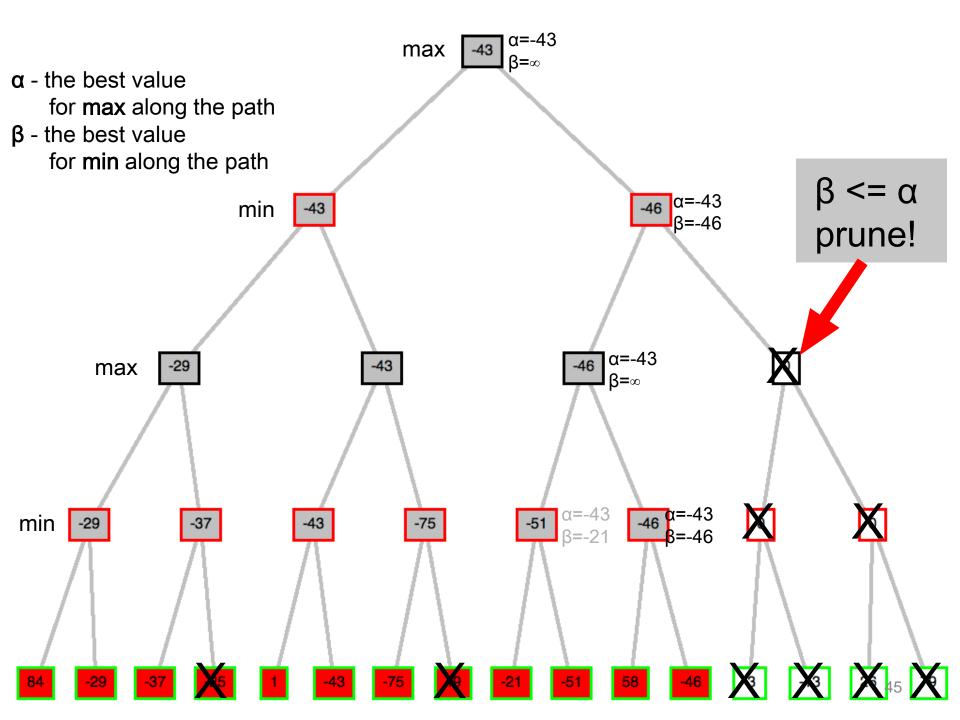






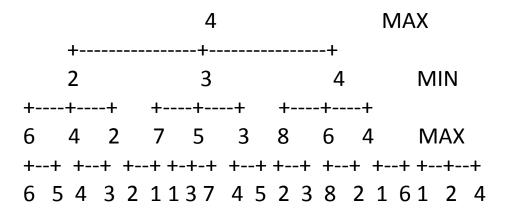






Bad and Good Cases for Alpha-Beta Pruning

Bad: Worst moves encountered first



Good: Good moves ordered first

If we can order moves, we can get more benefit from alpha-beta pruning

Properties of α - β

- Pruning does not affect final result. This means that it gets the exact same result as does full minimax.
- Good move ordering improves effectiveness of pruning
- With "perfect ordering," time complexity = O(b^{m/2})
 - → doubles depth of search
- A simple example of reasoning about 'which computations are relevant' (a form of metareasoning)

Node Ordering

Iterative deepening search

Use evaluations of the previous search for order

Also helps in returning a move in given time

Good Enough?

- Chess:
 - branching factor b≈35
 - –game length m≈100
 - -search space $b^{m/2} \approx 35^{50} \approx 10^{77}$
- The Universe:
 - number of atoms ≈ 10^{78}
 - $-age ≈ 10^{18} seconds$
 - -10^8 moves/sec x 10^{78} x 10^{18} = 10^{104}

The universe

- can we?

can play chess

Cutting off Search

MinimaxCutoff is identical to MinimaxValue except

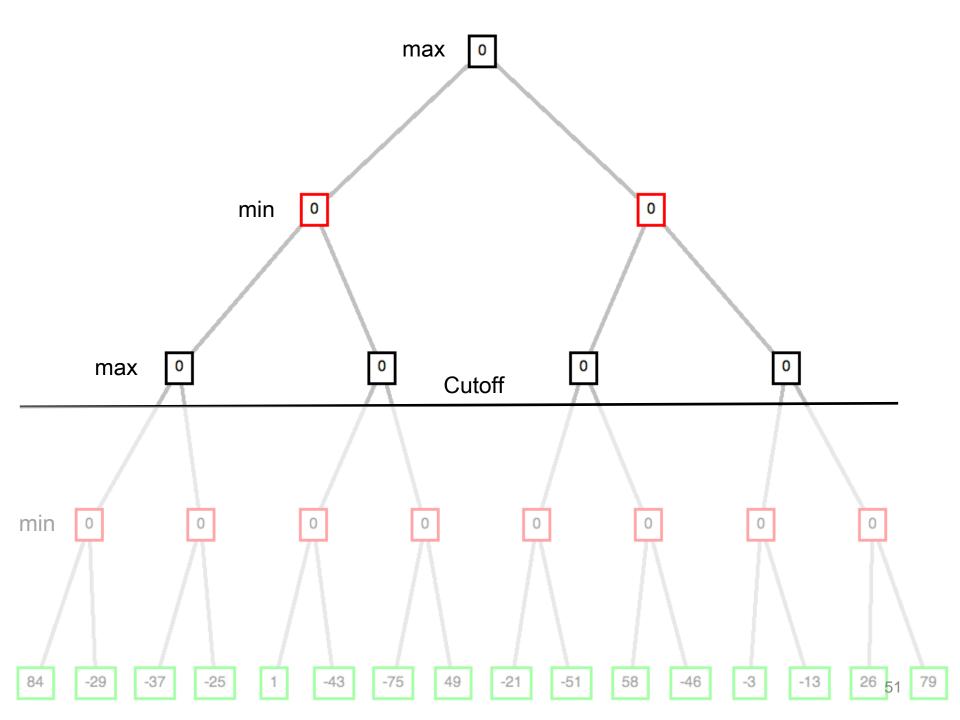
- 1. Terminal? is replaced by Cutoff?
- 2. Utility is replaced by Eval

Does it work in practice?

$$b^{m} = 10^{6}$$
, $b=35 \rightarrow m=4$

4-ply lookahead is a hopeless chess player!

- 4-ply ≈ human novice
- 8-ply ≈ typical PC, human master
- 12-ply ≈ Deep Blue, Kasparov

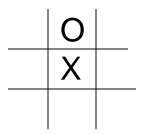


Evaluation Functions Tic Tac Toe

- Let p be a position in the game
- Define the utility function f(p) by
 - f(p) =
 - largest positive number if p is a win for computer
 - smallest negative number if p is a win for opponent
 - RCDC RCDO
 - where RCDC is number of rows, columns and diagonals in which computer could still win
 - and RCDO is number of rows, columns and diagonals in which opponent could still win.

Sample Evaluations

• X = Computer; O = Opponent



x O
rows
cols
diags

X O
rows
cols
diags

Evaluation functions

For chess/checkers, typically linear weighted sum of features

$$Eval(s) = w_1 f_1(s) + w_2 f_2(s) + ... + w_n f_n(s)$$

e.g., $w_1 = 9$ with

 $f_1(s) = (number of white queens) - (number of black queens), etc.$

Example: Samuel's Checker-Playing Program

It uses a linear evaluation function

$$f(n) = a_1x_1(n) + a_2x_2(n) + ... + a_mx_m(n)$$

For example: f = 6K + 4M + U

- K = King Advantage
- M = Man Advantage
- U = Undenied Mobility Advantage (number of moves that Max where Min has no jump moves)

Samuel's Checker Player

In learning mode

- Computer acts as 2 players: A and B
- A adjusts its coefficients after every move
- B uses the static utility function
- If A wins, its function is given to B

Samuel's Checker Player

- How does A change its function?
 - 1. Coefficent replacement

```
/\(\)(node) = backed-up value(node) - initial value(node)
```

if $\triangle > 0$ then terms that contributed **positively** are given more weight and terms that contributed negatively get less weight

if $\triangle < 0$ then terms that contributed **negatively** are given more weight and terms that contributed positively get less weight

Samuel's Checker Player

- How does A change its function?
 - 2. Term Replacement

38 terms altogether

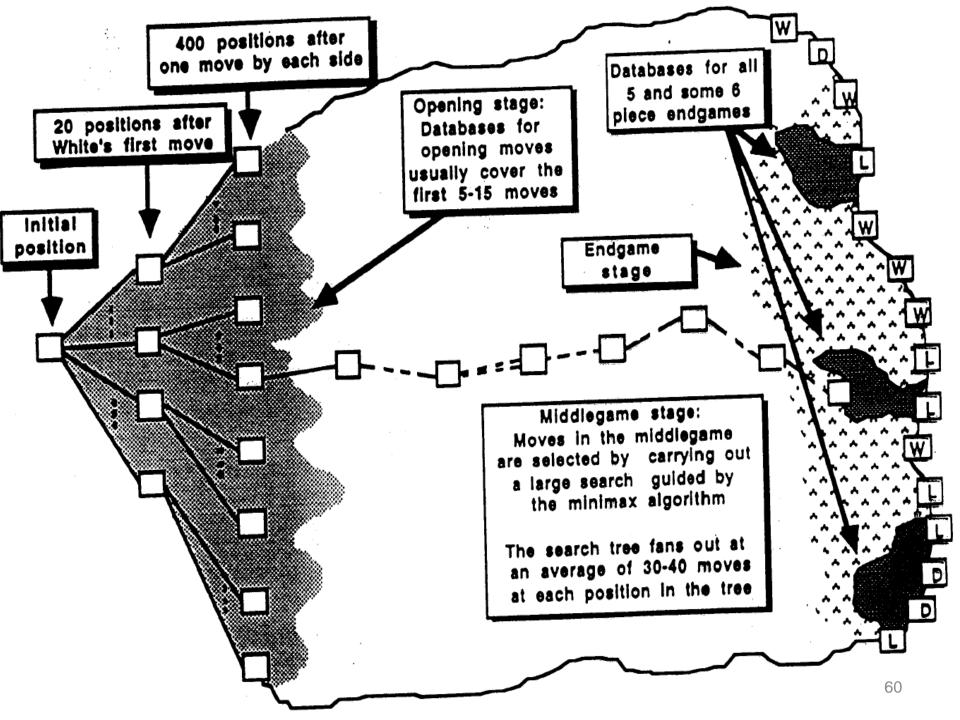
16 used in the utility function at any one time

Terms that **consistently correlate low** with the function value are removed and added to the end of the term queue.

They are replaced by terms from the front of the term queue.

Chess: Rich history of cumulative ideas

- Minimax search, evaluation function learning (1950).
- Alpha-Beta search (1966).
- Transposition Tables (1967).
- Iterative deepening DFS (1975).
- End game data bases ,singular extensions(1977, 1980)
- Parallel search and evaluation(1983, 1985)
- Circuitry (1987)

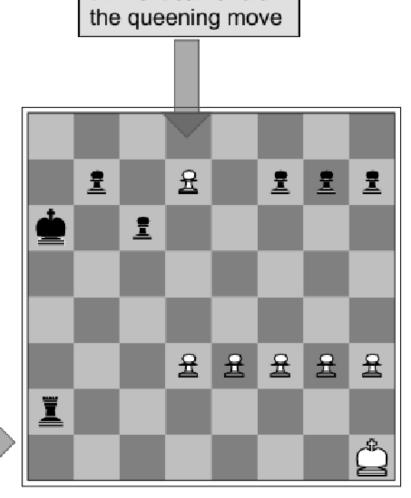


Problem with fixed depth Searches

if we only search n moves ahead, it may be possible that the catastrophy can be delayed by a sequence of moves that do not make any progress

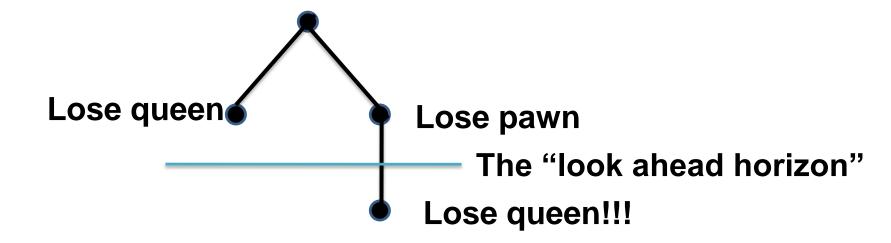
also works in other direction (good moves may not be found)

Black can give many consecutive checks before white escapes



Fixed depth search thinks it can avoid

Problems with a fixed ply: The Horizon Effect



- Inevitable losses are postponed
- Unachievable goals appear achievable
- Short-term gains mask unavoidable consequences (traps)

Solutions

- How to counter the horizon effect
 - Feedover
 - Do not cut off search at non-quiescent board positions (dynamic positions)
 - Example, king in danger
 - Keep searching down that path until reach quiescent (stable) nodes
 - Secondary Search
 - Search further down selected path to ensure this is the best move
 - Progressive Deepening
 - Search one ply, then two ply, etc., until run out of time
 - Similar to IDS

Quiescence Search

This involves searching past the terminal search nodes (depth of 0) and testing all the non-quiescent or 'violent' moves until the situation becomes calm, and only then apply the evaluator.

Enables programs to detect long capture sequences and calculate whether or not they are worth initiating.

Expand searches to avoid evaluating a position where tactical disruption is in progress.

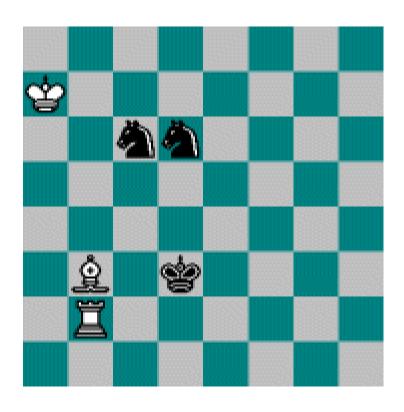
Additional Refinements

- Probabilistic Cut: cut branches probabilistically based on shallow search and global depth-level statistics (forward pruning)
- Openings/Endgames: for some parts of the game (especially initial and end moves), keep a catalog of best moves to make.
- Singular Extensions: find obviously good moves and try them at cutoff.

End-Game Databases

- Ken Thompson all 5 piece end-games
- Lewis Stiller all 6 piece end-games
 - Refuted common chess wisdom: many positions thought to be ties were really forced wins -- 90% for white
 - Is perfect chess a win for white?

The MONSTER



White wins in 255 moves (Stiller, 1991)

Deterministic Games in Practice

- Checkers: Chinook ended 40-year-reign of human world champion Marion Tinsley in 1994. Used a precomputed endgame database defining perfect play for all positions involving 8 or fewer pieces on the board, a total of 444 billion positions. Checkers is now solved!
- Chess: Deep Blue defeated human world champion Garry Kasparov in a six-game match in 1997. Deep Blue searches 200 million positions per second, uses very sophisticated evaluation, and undisclosed methods for extending some lines of search up to 40 ply. Current programs are even better, if less historic!
- Othello: human champions refuse to compete against computers, who are too good.
- Go: human champions refuse to compete against computers, who are too bad. In Go, b > 300, so most programs use pattern knowledge bases to suggest plausible moves, along with aggressive pruning.

Game of Go

human champions refuse to compete against computers, because software is too bad.

	Chess	Go
Size of board	8 x 8	19 x 19
Average no. of moves per game	100	300
Avg branching factor per turn	35	235
Additional complexity		Players can pass

Recent Successes in Go

- MoGo defeated a human expert in 9x9 Go
- Still far away from 19x19 Go.

- Hot area of research
- Leading to development of novel techniques
 - Monte Carlo tree search (UCT)

Other Games

deterministic

chance

perfect information

chess, checkers, go, othello

backgammon, monopoly

imperfect information

stratego

bridge, poker, scrabble

Status of Al Game Players

- Tic Tac Toe
 - Tied for best player in world
- Othello
 - Computer better than any human
 - Human champions now refuse to play computer
- Scrabble
 - Maven beat world champions Joel Sherman and Matt Graham
- Backgammon
 - 1992, <u>Tesauro</u> combines 3-ply search & neural networks (with 160 hidden units) yielding top-3 player
- Bridge
 - Gib ranked among top players in the world

- Poker
 - 2015, Heads-up limit hold'em poker is solved
- Checkers
 - 1994, <u>Chinook</u> ended 40-year reign of human champion Marion Tinsley
- Chess
 - 1997, <u>Deep Blue</u> beat human champion Gary Kasparov in six-game match
 - Deep Blue searches 200M positions/second, up to 40 ply
 - Now looking at other applications (molecular dynamics, drug synthesis)
- Go
 - 2008, MoGo running on 25 nodes (800 cores) beat Myungwan Kim
 - \$2M prize available for first computer program to defeat a top player

Summary

Games are fun to work on!

They illustrate several important points about AI.

Perfection is unattainable

must approximate.

 Game playing programs have shown the world what Al can do.

Quoridor

