



Manufacturing & Service Operations Management

Publication details, including instructions for authors and subscription information:
<http://pubsonline.informs.org>

Erratum: Optimizing Strategic Safety Stock Placement in Supply Chains

Stephen C. Graves, Sean P. Willems,

To cite this article:

Stephen C. Graves, Sean P. Willems, (2003) Erratum: Optimizing Strategic Safety Stock Placement in Supply Chains. *Manufacturing & Service Operations Management* 5(2):176-177. <http://dx.doi.org/10.1287/msom.5.2.176.16074>

Full terms and conditions of use: <http://pubsonline.informs.org/page/terms-and-conditions>

This article may be used only for the purposes of research, teaching, and/or private study. Commercial use or systematic downloading (by robots or other automatic processes) is prohibited without explicit Publisher approval, unless otherwise noted. For more information, contact permissions@informs.org.

The Publisher does not warrant or guarantee the article's accuracy, completeness, merchantability, fitness for a particular purpose, or non-infringement. Descriptions of, or references to, products or publications, or inclusion of an advertisement in this article, neither constitutes nor implies a guarantee, endorsement, or support of claims made of that product, publication, or service.

© 2003 INFORMS

Please scroll down for article—it is on subsequent pages



INFORMS is the largest professional society in the world for professionals in the fields of operations research, management science, and analytics.

For more information on INFORMS, its publications, membership, or meetings visit <http://www.informs.org>

Correspondence

Erratum: Optimizing Strategic Safety Stock Placement in Supply Chains

Stephen C. Graves • Sean P. Willems

*Leaders for Manufacturing Program and A. P. Sloan School of Management, Massachusetts Institute of Technology,
Cambridge, Massachusetts 02139-4307*

*Boston University, School of Management, Boston, Massachusetts 02215
sgraves@mit.edu • willems@bu.edu*

In Graves and Willems (2000) we consider the problem of finding the optimal placement of safety stocks in a supply chain with bounded demand and guaranteed service times. We develop a dynamic programming algorithm for supply chains that can be modeled as spanning trees.

The intent of this note is to correct an error in the algorithm. Ekaterina Lesnaia of MIT and Dr. Salal Humair of Optiant independently discovered the error. We wish to acknowledge and to thank Ms. Lesnaia and Dr. Humair for uncovering the error and for bringing it to our attention; they have also identified how to correct the error.

To describe the error and its correction, we will repeat part of the algorithm from Graves and Willems (2000). The dynamic program evaluates a functional equation for each node in the spanning tree, in which the nodes have been labeled $1, 2, \dots, N$ by the labeling algorithm in Graves and Willems (2000). We define N_k for each node k to be the subset of nodes $\{1, 2, \dots, k\}$ that are connected to k on the subgraph with node set $\{1, 2, \dots, k\}$. There are two forms for the functional equation. First, the function $f_k(S)$ is the minimum holding cost for safety stock in a subnetwork with node set N_k , where we assume that the outbound service time for node k is S . Second, the function $g_k(SI)$ is the minimum holding cost for safety stock in a subnetwork with node set N_k , where we assume that the inbound service time for node k is SI .

At node k for $1 \leq k \leq N-1$, the algorithm determines either $f_k(S)$ or $g_k(SI)$, depending on the loca-

tion of the node with the higher label that is adjacent to k . If this adjacent node is downstream (upstream) of node k , then we evaluate $f_k(S)$ ($g_k(SI)$). For node N , we can evaluate either functional equation.

To develop the equations for $f_k(S)$ and $g_k(SI)$, we define the function $c_k(S, SI)$ to be the minimum inventory holding cost for the subnetwork with node set N_k , where node k has inbound service time SI and the outbound service time S . In Graves and Willems (2000) the equation for $c_k(S, SI)$ is incorrect as it is based on faulty assumptions, namely the assumptions that $f_k(S)$ is nonincreasing in S and that $g_k(SI)$ is nondecreasing in SI .

The correct expression is as follows:

$$c_k(S, SI) = h_k \{ D_k(SI + T_k - S) - (SI + T_k - S)\mu_k \} \\ + \sum_{\substack{(i,k) \in A \\ i < k}} \min_{0 \leq x \leq SI} [f_i(x)] + \sum_{\substack{(k,j) \in A \\ j < k}} \min_{S \leq y \leq M_j - T_j} [g_j(y)].$$

The first term is the holding cost for the safety stock at node k as a function of S and SI .

The second term corresponds to the nodes in N_k that are upstream of k . For each node i that supplies node k , we include the minimum inventory holding costs for the subnetwork with node set N_i , as a function of SI . Because the inbound service time to node k (SI) is an upper bound for the outbound service time for node i , we need to minimize $f_i(\cdot)$ over the range of feasible service times for node i . In Graves and Willems (2000), we had erroneously assumed that the minimum occurs at $f_i(SI)$.

The third term corresponds to the nodes in N_k that are downstream of k . For each node j , $j \in N_k$ and

$(k, j) \in A$, we include the minimum inventory holding costs for the subnetwork with node set N_j , as a function of S . The outbound service time for node k (S) is a lower bound for the inbound service time for node j . Thus, we now minimize $g_j(\cdot)$ over the range of feasible inbound service times for j . In Graves and Willems (2000), we had erroneously assumed that the minimum occurs at $g_j(S)$.

The rest of the algorithm remains the same. The computational complexity of the algorithm does not increase with this correction, as one can avoid the additional minimizations within the calculation of

$c_k(S, SI)$ by making this part of the determination of the functions $f_k(S)$ and $g_k(SI)$. Thus, the computational complexity of the algorithm remains of order NM^2 where M is the maximum service time, which is bounded by the sum of the production lead-times $\sum_{j=1}^N T_j$.

Reference

Graves, S. C., S. P. Willems. 2000. Optimizing strategic safety stock placement in supply chains. *Manufacturing & Service Oper. Management* 2(1) 68–83.