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Multistage Capital Budgeting with Delayed Consumption of Slack

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apital budgeting frequently involves multiple stages at which firms can continue or abandon ongoing projects. In this paper, we study a project requiring two stages of investment. Failure to fund Stage 1 of the investment precludes investment in Stage 2, whereas failure to fund Stage 2 results in early termination. In contrast to the existing literature, we assume that the firm can limit the manager's informational rents with the early termination of the project. In this setting, we find that the firm optimally commits to a capital allocation scheme whereby it forgoes positive net present value (NPV) projects at Stage 1 (capital rationing), whereas at Stage 2, depending on the manager's previous report, it sometimes implements projects with a negative continuation NPV but in other situations forgoes implementing projects with positive continuation NPVs.

Key words: accounting; capital budgeting; resource allocation; multistaged financing; abandonment options; milestone-contingent investments

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Introduction

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In the presence of privately informed managers, a firm's capital budgeting policies balance investment efficiency against informational rents, or slack, such as managers' consumption of perquisites. To limit the opportunities for managers to divert capital funds for private benefit, firms use their managerial accounting systems as well as audits of their capital projects. For example, these systems can easily uncover, and thereby preclude, the manager's diversion of capital funds from appropriate investments to private uses such as vacations or excess compensation. However, it is more difficult for these systems to distinguish between investments in necessary and unnecessary assets, provided that both fall within the general class of appropriate purchases. For instance, it may be difficult to detect that a manager is engaging in empire building (acquiring unnecessary hard assets such as research equipment, cars, or offices, or unnecessary soft assets such as staff and consulting services) from which he derives private benefits. Thus, at best the firm's accounting and auditing systems may mitigate a manager's informational rent by constraining the set of assets into which he can divert capital funds for private benefit. One possible implication of restricting

investment to specific asset classes is that the private benefit provided to the manager can be consumed over time. For example, the private benefit of lavish offices is consumed over the time that the manager actually uses these offices (as compared to excess compensation or vacations, whose benefits are consumed immediately). As a result of constraining a manager's asset diversions, a principal can deny the manager the full consumption of such private benefits by abandoning the project before completion. However, by abandoning the project, the principal may be unable to fully recoup her initial investment. We study the implications of this abandonment option and "delayed slack consumption" on optimal capital allocation schemes.

We consider a multistage capital budgeting setting in which a privately informed manager proposes an initial research budget to develop a new project that the principal either accepts or rejects. If the principal accepts, the funds are made available to the manager who engages in the research required to discover the feasibility and net benefit of implementing the project of interest. If the research stage is successful, the continuation value of the project becomes known to both the principal and manager at the end of Stage 1. The



principal determines whether to implement or abandon the project in Stage 2. Consistent with the above discussion, we assume that the manager cannot consume all the slack in Stage 1 that may arise from the investment. As a result, if the project is abandoned at Stage 2, the manager forgoes consuming some of the associated informational rent. Likewise, if the project is abandoned at Stage 2, the principal cannot fully recoup her initial investment. Thus, if the investment is abandoned, a deadweight loss is incurred. For simplicity, and without loss of generality, we assume that the early abandonment of the project leads to the manager consuming no slack and the principal receiving a zero salvage value for his Stage 1 investment.

Our model of "delayed slack consumption" gives rise to an optimal capital allocation scheme that is qualitatively different from that found in the previous literature but is consistent with empirical findings. For example, we find that whereas the optimal capital allocation scheme uses a single Stage 1 hurdle rate that results in underinvestment or capital rationing at Stage 1 (the research stage), at Stage 2 it applies different hurdle rates depending on the manager's previous Stage 1 cost report and the outcome of his Stage 1 research. In fact, we find that it is optimal for the principal to commit to continue some projects at Stage 2 even if they have a negative continuation value (i.e., Stage 2 overinvestment), and it is also optimal to commit to forgo other projects that have a positive continuation value (i.e., Stage 2 underinvestment). Our results are consistent with the empirical evidence of both over- and underinvestment across firms found by Richardson (2006) and Driver and Temple (2009). However, our results are most closely related to those of Poterba and Summers (1995), who found multiple hurdle rates within individual firms, some of which are below and some of which are above their cost of capital.

Whereas our model is descriptive of a large class of capital budgeting problems, we believe that it is particularly descriptive of the capital budgeting process for research and development (R&D) projects that tend to span multiple stages; require highlyspecialized investments whose salvage values, if abandoned early, are significantly lower than their initial costs; and for which the general categories of assets to be funded can be agreed upon ahead of time and audited. For example, R&D investments often require multiple investment stages because additional technological information (regarding cost, reliability and scalability) or market information (regarding availability of suppliers or demand) can only be acquired after constructing a prototype plant or product.1 Another applicable R&D setting is one where

¹For a discussion of multistage capital budgeting, see Gompers (1995) and Gitman and Mercurio (1982).

regulatory obligations must be satisfied sequentially, as is the case with newly developed drugs undergoing U.S. Food and Drug Administration approval.

2. Literature Review

Our paper builds on the single-period, adverse selection capital budgeting model of Antle and Eppen (1985) in which the project cost is commonly known, and the rate of return is privately known by the manager. Because the manager can immediately consume any allocated funds above and beyond those required for the project, his incentive is always to understate the project's true rate of return. To mitigate the manager's misreporting incentives, the optimal capital allocation scheme provides the same budget for all projects and specifies a single required rate of return or hurdle rate that exceeds the firm's cost of capital, causing the firm to forgo some positive net present value (NPV) projects (i.e., underinvest).²

Antle and Fellingham (1990), Fellingham and Young (1990), and Arya et al. (1994) extended the model to a repeated game, where the manager privately observes and reports on a new and independent investment opportunity in each period. Similarly, Antle et al. (2006) considered the value of giving the privately informed manager an option to postpone the investment to a later period, at which time he may discover and report on a new and unrelated investment opportunity. In contrast, we consider projects where the Stage 2 investment opportunity arises only if the firm invested in Stage 1; i.e., the former can be viewed as a continuation of the latter. Furthermore, the above-mentioned literature assumes that the manager can immediately consume any slack provided by the principal, whereas we assume that the manager consumes the slack across multiple stages.

Most closely related to our work is the abandonment options literature. Levitt and Snyder (1997) considered a two-stage setting where the manager is subject to moral hazard in Stage 1, and his efforts affect both an interim signal received between the two stages and the likelihood of the project succeeding at the end of Stage 2.³ If the principal abandons the project upon receiving the interim signal, she eliminates the possibility of conditioning the manager's compensation on the project outcome, thereby exacerbating the Stage 1 moral hazard problem. Consequently, the principal optimally continues projects with a negative continuation value (overinvests) when the Stage 1



² Bockem and Schiller (2009) found report-contingent budgets, which were used to motivate the manager to engage in costly information gathering. A similar extension was considered by Kim (2006).

³ We thank an anonymous referee for referring us to Levitt and Snyder (1997).

moral hazard problem is sufficiently severe.⁴ Unlike Levitt and Snyder (1997), we find instances of both under- and overinvestment. Furthermore, because the manager in our model takes no productive actions but has private information, the principal uses her Stage 2 abandonment/continuation decision to control the manager's Stage 1 reporting incentives.

The structure of our model is most closely related to that of Pfeiffer and Schneider (2007). In both papers, the principal makes a Stage 1 investment decision based on the manager's report and later makes her Stage 2 continuation decision based on information revealed at Stage 2.⁵ The major difference between our paper and Pfeiffer and Schneider (2007) concerns the informational rent. In Pfeiffer and Schneider (2007), the principal incurs an informational rent (and the manager consumes it) only if the project is continued.⁶ In our model, the principal incurs the informational rent upfront at the time of the Stage 1 funding. If the project is not continued, there is a deadweight loss in that the principal has already incurred the informational rent but the manager cannot consume it.

Our finding of Stage 2 overinvestment is also related to the literature on "escalation errors" (Staw 1976, Berg et al. 2009). This literature identifies settings in which a person who has previously invested in a project subsequently finds out that the continuation value of the project is negative but still chooses not to abandon it, resulting in overinvestment. Kanodia et al. (1989) provides a rational economic explanation for such behavior based on reputational concerns. In that model, abandoning the project would indicate that the person did not have "foresight" at the time he initially invested in the project, causing the labor market to revise downward his value and future outside opportunity wage. The present paper and Kanodia et al. (1989) explain two very different overinvestment phenomena. Kanodia et al. (1989) examines a single-actor, labor market setting in which it is optimal for the single actor to continue a negative NPV project. The present paper examines an optimal contracting, principal-agent setting in which it is optimal for the principal to commit to continue a negative NPV project to mitigate the manager's Stage 1 reporting incentives.

3. Model

We study an adverse selection model encompassing two stages. At Stage 1, the manager requests a budget to investigate a potential new project. The cost required to successfully conduct this investigation is privately known by the manager. If funded, the manager's investigative or research work generates a public signal at the end of Stage 1 that reveals the continuation value of implementing the project. At the start of Stage 2, after the public signal is revealed, the principal decides whether to abandon or to implement the project. We label Stage 1 the research stage and Stage 2 the implementation stage, as the project is assumed to end without any payoff in Stage 2 unless the principal makes the Stage 2 investment to implement the project. Consistent with the two stages, we refer to an investment in Stage 1 as "funding" research and an investment in Stage 2 as "implementing" the project.

The timeline is as follows (see Figure 1). At time t = 1, a risk-neutral firm (the principal) hires a riskneutral manager to oversee the research activity associated with a potential new project. The principal offers a contract to the manager that fully specifies the compensation scheme and capital budgeting rules (as discussed below). At t = 0, prior to being hired, the manager privately observes the level of funding required to conduct the research in Stage 1. We assume that the research stage requires a minimum investment of $c_i \in C = \{c_1, \dots, c_n\}$, where $c_i < c_{i+1} \,\forall i$, is privately observed by the manager. Any Stage 1 investment greater than or equal to the observed c_i generates a contractible signal, $g_i \in G = \{g_1, \dots, g_k\},\$ where $g_i > g_{i+1} \,\forall j$, which denotes the net continuation value of implementing the project at t = 4.7 To highlight the role of the abandonment decision and delayed slack consumption in mitigating inefficiencies, we assume that at time t = 1, the principal can commit to a t = 4 implementation schedule based on the contractible continuation signal, g_i . The interim signal being contractible allows us to ignore additional issues that arise when information asymmetry occurs at two different points in time. Without loss of generality, any Stage 1 investment less than the observed c_i will cause the research stage to fail with certainty, which we assume to be a contractible event. The probability densities of c_i and g_i are common knowledge, independent, and represented by $f(c_i)$ and $f(g_i) \equiv \rho_i$, respectively.⁸ To facilitate the



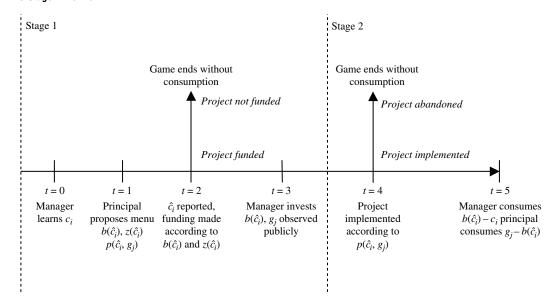
⁴ Dutta and Fan (2009) and Bernardo et al. (2009) also study moral hazard models that give rise to instances of overinvestment.

⁵ The interim signal is privately observed by the manager in Pfeiffer and Schneider (2007), whereas it is publicly observed in our model. ⁶ Furthermore, in Pfeiffer and Schneider (2007), the abandonment decision creates information in the sense that it allows the principal to perfectly observe the agent's subsequent effort choice. In contrast, in Arya and Glover (2003) abandonment destroys information about the agent's prior choice of effort. In our model, the Stage 2 decision has no effect on the information available to the principal.

⁷The ordering of c_i 's and g_j 's implies that the principal prefers smaller indices for both c_i and g_j .

⁸ The model could also accommodate correlated random variables, *c* and *g*, although doing so would complicate the interpretation of our results, because one would then have to distinguish between the effects caused by statistical dependence versus those arising from the delayed consumption of slack.

Figure 1 Two-Stage Timeline



exposition, we assume that the discrete costs, c_i , are evenly spaced, with $c_i - c_{i-1} = \delta$ for i > 1, $c_1 = \delta$, and that these costs are uniformly distributed: $f(c_i) = 1/n$. The assumptions placed on the probability distributions of the Stage 1 costs and Stage 2 continuation values significantly simplify the characterization of the manager's informational rent. However, we believe that all qualitative results would continue to hold with more general distributions.

We next specify the budgeting and compensation processes. At time t = 2, the manager uses his private information to submit a report, \hat{c}_i , to the principal regarding his research costs, and the latter funds the project according to the contract agreed to at time t=1; with probability $z(\hat{c}_i) \in [0,1]$ the research is funded, and with probability $1 - z(\hat{c}_i)$ it is not. If the project is not funded, the game ends and both parties receive their reservation utility of zero. On the other hand, if the project is funded, the manager receives the contractually specified budget of $b(\hat{c}_i)$ to fund his research at t = 3. We assume that the manager's spending is imperfectly audited, as discussed in the introduction, so that he cannot immediately divert any funds in excess of that required to conduct the Stage 1 research (i.e., $b(\hat{c}_i) - c_i$) into consumption. Hence, the manager invests his entire budget in research-related assets; however, only c_i is necessary to conduct the Stage 1 research. The remainder generates no benefit to the firm but provides the manager with personal utility in Stage 2-so long as the project is implemented.9 The principal's implementation decision at t = 4 accords with the contract agreed to at t = 1: she implements the project with probability $p(\hat{c}_i, g_j) \in [0, 1]$, and abandons it with probability $1 - p(\hat{c}_i, g_j)$. We assume that if the project is abandoned at t = 4, the principal cannot recoup the earlier investment, b_i . On the other hand, if the project is implemented at t = 4, then at t = 5, the principal consumes the residual project surplus, $g_j - b(\hat{c}_i)$, and the manager consumes the excess funding, or slack, procured in Stage 1: $b(\hat{c}_i) - c_i$.

As a managerial example of our setting, consider a firm that is interested in entering a new geographical market with uncertain market potential. The firm decides to delay the large upfront costs required to fully enter the market by hiring a manager to conduct a trial experiment in a representative fraction of the market. To do so, the manager needs to hire people familiar with the new market and invest in facilities. The manager is privately informed as to the cost of running the trial. Although the firm can audit the manager's spending, it cannot distinguish between necessary and excessive investments in people and facilities. The manager can only consume the full private benefits provided by excess Stage 1 funding if the trial is successful and the firm decides to fully enter the market. Again, if the project is abandoned, the salvage value of the unconsumed assets is likely to be zero.

Although we have outlined an extensive list of assumptions above, the three critical assumptions required for our results are that (1) the manager does not consume all the slack in Stage 1, (2) the principal cannot recoup all of the unconsumed funding if the project is abandoned, and (3) the principal and manager cannot contract on the price of salvaged assets if the project is abandoned. Assumptions (1) and (2) guarantee that a deadweight loss



⁹ Bolton and Dewatripont (1994) make a similar assumption.

is incurred if the project is abandoned, whereas (3) assures that the principal cannot fully resolve the Stage 1 adverse selection problem by abandoning the project in Stage 2.

4. Two Benchmark Models

Before formally stating our problem, we introduce two benchmark models that will help us analyze the efficiency implications of our model (referred to as the commitment model). The first-best (FB) model is identical to the commitment model, but without adverse selection; that is, we assume that the manager's research cost, c_i , is common knowledge. Accordingly, the principal provides a budget of b_i = c_i . Let $c_{h^{\text{FB}}}$ be the largest research cost realization that the principal agrees to fund, i.e., $c_{h^{FB}} \leq E[g_i]$ and $c_{h^{\text{FB}}+1} > E[g_i]$. At Stage 2, the principal optimally implements all projects with positive continuation values; i.e., a project is implemented if and only if $g_i \ge 0$, regardless of the (sunk) Stage 1 expenditures. As with the definition of $c_{h^{\text{FB}}}$, let w^{FB} be the continuation value index such that $g_{w^{\text{FB}}} \ge 0$ but $g_{w^{\text{FB}}+1} <$ 0. Comparing the results from the commitment and first-best models will allow us to identify overinvestment, underinvestment, and the agency costs associated with eliciting the manager's private information. We define underinvestment at Stage 1 relative to the first-best model as any allocation policy where profitable projects are not funded, i.e., $z_i < 1$ for some $\hat{c}_i \le$ $c_{h^{\rm FB}}$. We define underinvestment at Stage 2 if some projects with a positive continuation value are abandoned, i.e., $p(\hat{c}_i, g_i) < 1$ for some $g_i \ge g_{w^{\text{FB}}}$ and i. Overinvestment is similarly defined.

To illustrate how our results differ from prior capital budgeting research, we introduce a second benchmark: the no-commitment (NC) model is identical to our commitment model (including delayed slack consumption), but where the principal cannot commit to her Stage 2 implementation rule at the contracting period, t = 1. Instead, the principal follows a sequentially rational Stage 2 implementation rule that implements all projects with nonnegative continuation values $(g_i \ge 0)$, regardless of the Stage 1 expenditure. Therefore the no-commitment solution has the same Stage 2 implementation policy as the first-best solution, i.e., $g_{w^{\rm NC}} = g_{w^{\rm FB}} \ge 0$. Because the principal cannot commit to an implementation rule when she proposes a contract in the no-commitment setting, her only available controls are the probability of providing a budget, $z(\hat{c}_i)$, and the size of the allocated budget, $b(\hat{c}_i)$. However, because the sequentially rational Stage 2 implementation rule is independent of the manager's Stage 1 cost report, we can still invoke the revelation principle, which implies $\hat{c}_i = c_i$. To simplify what follows, let $z_i \equiv z(c_i)$, $b_i \equiv b(c_i)$, and $p_{i,j} \equiv p(c_i, g_j)$. The optimal solution to the no-commitment model thus solves

$$U_{P} = \max_{b_{i}, z_{i}, p_{i,j}} \frac{1}{n} \sum_{i=1}^{n} z_{i} \left(\sum_{j=1}^{k} \rho_{j} p_{i,j} g_{j} - b_{i} \right)$$

subject to:

$$z_{i} \sum_{j=1}^{k} \rho_{j} p_{i,j}(b_{i} - c_{i}) \ge z_{s} \sum_{j=1}^{k} \rho_{j} p_{s,j}(b_{s} - c_{i}),$$

$$i, s = 1, \dots, n; \qquad (TT^{NC})$$

$$z_i \sum_{j=1}^k \rho_j p_{i,j}(b_i - c_i) \ge 0, \quad i = 1, \dots, n;$$
 (IR^{NC})

$$p_{i,j} = \begin{cases} 1 & \text{for } j \le w^{\text{FB}}, \\ 0 & \text{for } j > w^{\text{FB}}, \end{cases} \quad \forall i.$$
 (SR^{NC})

Sequential rationality ensures that the principal will only implement Stage 2 projects with nonnegative continuation values, regardless of the reported Stage 1 cost (SR^{NC}). The (TT^{NC}) constraints ensure that the manager's report is truthful. The (IR^{NC}) constraints assure that the manager is given sufficient funds to conduct his Stage 1 research. Note that the delayed slack consumption plays no role in the principal's Stage 2 implementation decision because she cannot recoup any of the unconsumed budget if she abandons the project at Stage 2. Delayed slack consumption only shows up in the manager's (TT^{NC}) constraints.

LEMMA 1. The optimal funding and implementation rules in the no-commitment benchmark exhibit the following characteristics:

- (i) They define a Stage 1 hurdle cost, $c_{h^{NC}}$, with $h^{NC} \in \{1, \ldots, n\}$, such that projects are always funded $(z_i = 1)$ when the Stage 1 cost is less than or equal to the hurdle $c_i \leq c_{h^{NC}}$ and are always rejected $(z_i = 0)$ when the Stage 1 cost exceeds the hurdle, $c_i > c_{h^{NC}}$.
- (ii) They provide the manager with a fixed Stage 1 budget, $b_i^{NC} = c_{h^{NC}}$, for any funded Stage 1 cost, $c_i \leq c_{h^{NC}}$.

Note that the structure of the optimal Stage 1 funding rule is the same as in the Antle and Eppen (1985) model, because the sequential rationality of the Stage 2 implementation decision makes the Stage 1 funding decision essentially a one-period problem. Comparing our results with those obtained in the nocommitment model will thus allow us to compare our results with the prior literature and to isolate the roles of delayed slack consumption and commitment in the optimal capital allocation rule.

5. Commitment Model Results

Returning to our *commitment* model, and again invoking the revelation principle, the manager's expected



utility upon observing Stage 1 cost c_i is given by:

$$U_A = z_i \sum_{j=1}^k \rho_j p_{i,j} (b_i - c_i).$$

When the manager reports c_i , the principal funds the project in the amount b_i , with probability z_i , and commits to a Stage 2 implementation rule, $p_{i,j}$. Thus, at time t = 1, we can express the principal's commitment program as

$$\begin{aligned} U_{p} &= \max_{b_{i}, z_{i}, p_{i, j}} \frac{1}{n} \sum_{i=1}^{n} z_{i} \left(\sum_{j=1}^{k} \rho_{j} p_{i, j} g_{j} - b_{i} \right) \\ \text{subject to:} \quad z_{i} \sum_{j=1}^{k} \rho_{j} p_{i, j} (b_{i} - c_{i}) \geq z_{s} \sum_{j=1}^{k} \rho_{j} p_{s, j} (b_{s} - c_{i}), \\ i, s &= 1, \dots, n; \end{aligned}$$

$$z_i \sum_{j=1}^k \rho_j p_{i,j}(b_i - c_i) \ge 0, \quad i = 1, ..., n.$$
 (IR^C)

Note that because the principal can now commit to a Stage 2 implementation rule, the sequential rationality constraints from the no-commitment problem can be dropped. The manager's truth-telling constraints, (TT^C), ensure that the manager truthfully reports his cost, c_i . The manager's individual rationality constraints, (IR^C), guarantee that the manager receives sufficient funds to conduct his Stage 1 research whenever the principal agrees to fund it.¹⁰ Conditional on a Stage 1 cost c_i , the manager's expected utility only depends on the interim information, g_i , to the extent that it affects the probability of implementing the project in Stage 2, or equivalently, the probability that he consumes his informational rent. With commitment, the principal has three choice variables to control the manager's incentives: the set of cost reports that receive Stage 1 funding (the set of c_i for which $z_i > 0$), the associated budgets (b_i) , and the Stage 2 implementation rule $(p_{i,j})$. Proposition 1 below characterizes the principal's optimal funding and implementation rules, where $p_i \equiv \sum_{j=1}^k \rho_j p_{i,j}$ denotes the probability of Stage 2 implementation following a cost observation c_i .

Proposition 1. The optimal funding and implementation rules (denoted by superscript asterisks) of the commitment model exhibit the following characteristics:

(i) They define a Stage 1 hurdle cost, c_{h^*} , with $h^* \in \{1, ..., n\}$, such that projects are always funded $(z_i^* = 1)$ when the cost is less than or equal to the hurdle $c_i \le c_{h^*}$

Without loss of generality, we ignore the possibility that the principal compensates the manager when (a) the principal does not invest in the research stage and (b) the principal does invest in the research stage, but chooses not implement the project. The proof of this assertion is relatively long but follows from the assumed risk neutrality of the manager and lack of any additional agency problems.

and are always rejected ($z_i^* = 0$) when the cost exceeds the hurdle, $c_i > c_{h^*}$.

- (ii) They provide the manager with a Stage 1 budget, $b_i^* = c_i + \delta \sum_{q=i+1}^{h^*} (p_q^*/p_i^*)$, that weakly increases in the manager's cost, c_i .
- (iii) They define a Stage 2 continuation value hurdle, $g_{w_i^*}$, for every funded Stage 1 cost, $c_i \leq c_{h^*}$, such that projects are implemented for $g_j \geq g_{w_i^*}$ and are abandoned for $g_j < g_{w_i^*}$.
- (iv) The Stage 2 continuation value hurdle $g_{w_i^*}$ is weakly increasing in the manager's Stage 1 cost.
 - (v) The Stage 2 implementation probability:
- (a) for any Stage 2 project, $p_{i,j}^*$ is weakly decreasing in the manager's Stage 1 cost, c_i , and increasing in the Stage 2 continuation value, g_j ;
- (b) for all Stage 2 projects, $p_i^* \equiv \sum_{j=1}^k \rho_j p_{i,j}^*$, is weakly decreasing in the manager's Stage 1 cost, c_i .

Proposition 1(i) finds that the familiar Stage 1 hurdle-rate contracts from the prior capital budgeting literature and the no-commitment model remain optimal in the presence of Stage 2 commitment and delayed slack consumption. As in the prior literature, the hurdle is used to discourage the manager from overstating his cost. The optimal funding probabilities, z_i^* , also follow the earlier models in that they are binary.¹¹

Part (ii) provides the first instance of how our assumptions of delayed slack consumption and commitment to Stage 2 implementation result in novel capital allocation rules. We find that the size of the manager's Stage 1 budget, b_i^* , increases in his cost. To derive the optimal Stage 1 budgets, we use standard techniques to establish that only the adjacent upward (TT^C) constraints are binding (preventing a manager with cost c_i from reporting cost c_{i+1}). This gives rise to the recursive equation $b_i = (p_{i+1}/p_i)(b_{i+1}$ $c_i(1-p_i/p_{i+1}))$, which yields the optimal budgets, $b_i^* =$ $c_i + \delta \sum_{q=i+1}^{h^*} (p_q/p_i)$. In the prior literature and the nocommitment model, the budget is constant for all funded cost reports and equal to the highest funded cost, i.e., $b_i^{NC} = c_{h^{NC}}$, and the principal mitigates the manager's informational rent by choosing a hurdle below the first best, $c_{h^{\rm NC}} < c_{h^{\rm FB}}$. In contrast, the optimal budgets in our commitment model increase in the manager's cost because, with delayed slack consumption and Stage 2 commitment, the manager is interested not only in $b_i - c_i$ as in the no-commitment model, but also in the probability with which he is able to consume it (p_i) , which the principal controls.¹²



 $^{^{11}}$ Our results on the behavior of b_i^* , p_i^* , and z_i^* in Proposition 1 are "weak" because of the discreteness of our densities. Our results would be "strict" if we assumed that the supports of Stage 1 and Stage 2 costs were sufficiently dense.

¹² Note that if, instead, the manager could consume all his informational rent in Stage 1, then the principal would optimally

Hereafter we will refer to $b_i - c_i$ as "budgetary slack" and to $p_i(b_i - c_i)$ as the "informational rent."

By increasing the manager's budget in his cost report, the principal achieves two efficiency gains over the NC capital budgeting setting. First, for a given Stage 1 cost hurdle, c_h , the manager's budgetary slack is less than in the NC and prior models where $b_i^{\text{NC}} = c_{h^{\text{NC}}}, \ \forall i \leq h^{\text{NC}}$. This gives rise to the second benefit in that it allows the principal to increase the Stage 1 funding hurdle closer to the first best (see Proposition 2(ii)) and thereby reduce Stage 1 underinvestment. However, the disadvantage of an increasing budget is that it provides the manager with additional incentives to overstate his cost. To mitigate this incentive, the principal commits to a Stage 2 implementation rule, $p_{i,j}$, that decreases in the manager's Stage 1 cost (Proposition 1(v)(a)). The manager's situation is similar to an auction where the bidder trades off the surplus $(b_i - c_i)$ in our case) were he to win with a bid b_i against the probability of winning with that bid (p_i) . Although the probability of "winning" an auction is exogenously determined by the distribution of bidders but is optimally chosen by the principal in our setting, the trade-offs the bidder and manager face are identical.

As Proposition 1(iii) points out, Stage 2 implementation follows a (Stage 1 report-contingent) hurdle policy in that all projects with a continuation value below the hurdle, $g_{w_i^p}$, are abandoned and projects with a continuation value strictly greater than the hurdle are implemented with probability 1. Because of the assumed discreteness of g_j , projects whose continuation value is exactly the hurdle may be implemented with a probability less than 1.

To further isolate the role of delayed slack consumption, the following proposition compares the Stage 1 relative efficiency between our model and both the first-best and no-commitment benchmarks.

Proposition 2. The optimal capital allocation mechanism in the commitment model results in Stage 1 investment whereby the principal

- (i) underinvests in research at Stage 1 relative to the first-best benchmark and
- (ii) underinvests less in research at Stage 1 than the nocommitment benchmark.

With delayed slack consumption and Stage 2 commitment, the optimal allocation involves capital rationing at Stage 1 ($h^* \le h^{\text{FB}}$), which is consistent with the previous adverse-selection models of capital allocation (Antle and Eppen 1985 and others). However, Proposition 2(ii) finds that this underinvestment

adopt the first-best Stage 2 implementation rule with constant p_i 's, which, when plugged into the above recursive equation, would imply $b_i = b_{i+1}$, consistent with the constant budget obtained in the extant literature and the no-commitment benchmark of Lemma 1.

is less severe in the commitment model than in the nocommitment model. To see why, suppose that (1) there are three Stage 1 cost realizations (c_1, c_2, c_3) , (2) all Stage 2 projects have nonnegative continuation values, (3) the principal funds all three Stage 1 managers and implements all Stage 2 projects under the firstbest model, (4) the Stage 1 hurdle for both the commitment and the no-commitment models is c_1 , and (5) that the principal optimally implements all Stage 2 projects conditional on c_1 in both settings. Because only c_1 is funded, no manager earns rent. Now, consider increasing the Stage 1 hurdle to c_2 . In the no-commitment model, the principal optimally continues to implement all Stage 2 projects (now for both c_1 and c_2) and must therefore provide a budget of c_2 to both managers. Thus, for the NC model, the increase in informational rent to the c_1 manager from increasing the Stage 1 hurdle is $c_2 - c_1 = \delta$. In the commitment model, the principal would still implement all Stage 2 projects for the c_1 manager, but could impose a lower implementation probability for the c_2 manager (as shown in Proposition 1). This allows the principal to pay a smaller informational rent to the c_1 manager than in the no-commitment model, but at the cost of incurring a Stage 2 implementation inefficiency. Thus, the resulting *net* cost of reducing Stage 1 underinvestment may be less with commitment than without. In this example, we reduced the c_1 manager's informational rent by choosing an implementation probability for the c_2 manager less than 1, thereby incurring Stage 2 underinvestment. Alternatively, if there were Stage 2 projects with negative continuation values, then instead of imposing an inefficient implementation schedule on manager c_2 , we could have limited the c_1 manager's misreporting incentives by increasing his implementation probability for one or more of the negative continuation value projects, thereby incurring Stage 2 overinvestment. In fact, as we show in Proposition 3, we find that the optimal Stage 2 distortions may include both underinvestment and overinvestment.

Proposition 3. The principal's optimal contract in the commitment model results in the following Stage 2 distortions relative to the first-best and no-commitment models:

- (i) weak underinvestment on average;
- (ii) weak overinvestment for small Stage 1 costs;
- (iii) weak underinvestment for large Stage 1 costs.

Recall that in both the first-best and no-commitment solutions, the principal's Stage 2 implementation rules are efficient in that they ignore the sunk costs from Stage 1.¹³ However, in the commitment model, the

¹³ Overinvestment from the principal's point of view and the society's point of view are identical in the first-best model. In the no-commitment model and in our model, overinvestment from the principal's point of view occurs when any project with a negative



principal uses the Stage 2 implementation rules to trade off her project profits (g_j) and the manager's compensation. To see this, consider the principal's unconstrained optimization problem after substituting the optimal budgets from Proposition 1(ii) into the principal's objective function:

$$U_{P} = \max_{p_{i,j}} \frac{1}{n} \sum_{i=1}^{h^{*}} \sum_{j=1}^{k} \left(\rho_{j} p_{i,j} g_{j} - c_{i} - \delta \frac{\sum_{s=i+1}^{h^{*}} \sum_{m=1}^{k} \rho_{m} p_{s,m}}{\sum_{m=1}^{k} \rho_{m} p_{i,m}} \right).$$

From the principal's objective function it is straightforward that the more Stage 1 projects that are funded, the more slack the principal has to provide the managers, as the last term in brackets increases in h^* . Furthermore, changing the implementation probability $p_{i,j}$ has three effects for the principal, one direct and two indirect. These three effect can be seen in the principal's marginal payoff to raising the implementation probability $p_{i,j}$, holding fixed the number of funded managers, h^* :

$$\frac{\partial U_{p}}{\partial p_{i,j}} = \frac{\rho_{j}}{n} \left(g_{j} + \delta \sum_{s=i+1}^{h^{*}} \frac{p_{s}}{p_{i}^{2}} - \delta \sum_{t=1}^{i-1} \frac{1}{p_{t}} \right). \tag{1}$$

By changing $p_{i,j}$, the principal changes the probability with which she implements a project with continuation value g_i . For a positive continuation value, increasing $p_{i,j}$ directly increases the principal's utility by reducing the level of Stage 2 underinvestment. The two indirect effects change the principal's utility by affecting the budgetary slack $b_i - c_i =$ $\delta \sum_{s=i+1}^{h^*} (p_s/p_i)$ required to satisfy the manager's truthtelling constraints. From (1), the first indirect effect, $\delta \sum_{s=i+1}^{h^*} (p_s/p_i^2)$, represents the amount of manager i's budgetary slack that the principal can reduce via a marginal increase in $p_{i,j}$, while leaving the manager's reporting incentives unchanged. However, the final term in (1), $-\delta \sum_{t=1}^{i-1} (1/p_t)$, represents a second, countervailing indirect effect. In equilibrium the upward truth-telling conditions are binding. This implies that when increasing the probability of implementation for manager c_i , the principal must also increase the informational rents paid to for all managers whose cost is less than c_i ; that is, by increasing the implementation probability for one manager, the payoff to overreporting increases for all managers with lower Stage 1 cost; therefore, the principal must also

continuation value is implemented. This need not be overinvestment from a social welfare point of view because the loss to the principal from continuing a negative continuation value project may be compensated by the slack which the agent gains from such implementation. We define overinvestment from the principal's point of view. Note that this is consistent with what empiricists are able to document, as the slack arising from earlier stage investments cannot be observed. We thank an anonymous referee for raising this issue. increase the rents paid to them to maintain their truthtelling incentives.

Taking these three effects together illustrates how the optimal allocation rule may result in Stage 2 overinvestment for relatively low Stage 1 cost realizations and underinvestment for relatively high Stage 1 cost realizations. For example, because there are no managers with a lower Stage 1 cost than manager c_1 , the second indirect effect is absent. As a result, the firstorder condition (FOC) for manager c_1 demonstrates how the first indirect effect can lead to overinvestment because $\partial U_p/\partial p_{1,j}=(\rho_j/n)(g_j+\delta\sum_{s=2}^h(p_s/p_1^2))$ can be positive, resulting in $p_{1,j} > 0$, even when $g_j < 0$. Similarly, for manager c_h there are no managers with a higher Stage 1 cost; hence, the first indirect effect is absent. This FOC shows how the second indirect effect can lead to underinvestment because $\partial U_P/\partial p_{h,j} = (\rho_j/n)(g_j - \delta \sum_{t=1}^{h-1} (1/p_t))$ can be negative, resulting in $p_{h,j} = 0$, even when $g_j > 0$. Proposition 3(i) shows that, on average, the effect of increasing the slack of other managers dominates the effect of reducing the slack of any one manager so that the principal commits to underinvestment at Stage 2. Notice, however, that if either the principal could not commit to her Stage 2 implementation rule or if the manager consumed all of his informational rents in Stage 1, then $\partial U_P/\partial p_{i,j} = (\rho_i/n)g_i$, in which case there would be no indirect effects at Stage 2, and the principal would instead follow the sequential rational implementation rule used both in the first-best and nocommitment models,

$$p_{i,j} = \begin{cases} 1 & g_j \ge 0, \\ 0 & g_j < 0. \end{cases}$$

Recall that in our model there is a deadweight loss from abandonment. The first indirect effect, which gives rise to overinvestment, is entirely caused by this deadweight loss. To see this formally, suppose the principal could recoup the budgetary slack b_i-c_i if she abandons the project. The objective function then becomes

$$U_{p} = \max_{b_{i}, z_{i}, p_{i,j}} \frac{1}{n} \sum_{i=1}^{n} z_{i} \left(\sum_{j=1}^{k} \rho_{j} p_{i,j} g_{j} - b_{i} + (1 - p_{i})(b_{i} - c_{i}) \right),$$

and the associated FOC then becomes $\partial U_P/\partial p_{i,j} = (\rho_j/n)(g_j - \delta \sum_{q=1}^{i-1} 1)$, precluding overinvestment.

To further show how the direct and indirect effects discussed above interact, we next consider the effect of an exogenous shock to a single Stage 2 continuation value g_j on the implementation probabilities. The above discussed first-order condition $\partial U_p/\partial p_{i,j}$ illustrates the direct effect on the optimal $p_{i,j}$ of a change in the continuation value g_j . However, in equilibrium, varying $p_{i,j}$ affects the budgetary slack $b_i - c_i$ and



Table 1 Implementation Probabilities in an Example

	g_1	g_2	g_3	g_4
c_1 c_2 c_3	$p_{1,1} = 1$ $p_{2,1} = 1$ $p_{3,1} = 1$	$p_{1,2} = 1$ $p_{2,2} = 1$ $p_{3,2} = 0$	$p_{1,3} = 1$ $p_{2,3} = 0$ $p_{3,3} = 0$	$ \begin{array}{l} p_{1,4} = 0 \\ p_{2,4} = 0 \\ p_{3,4} = 0 \end{array} $

consequently the manager's (TT^C) constraints. As a result, a change in any *one* g_j may have an indirect effect on *all* implementation probabilities. This comparative static analysis is illustrated in the following proposition.

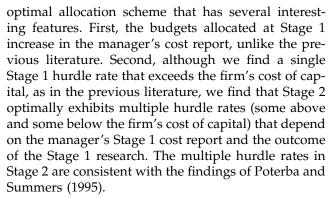
PROPOSITION 4. For a fixed h^* , increases (decreases) in a continuation value, g_j to g_j' such that $g_{j+1} < g_j' < g_{j-1}$, will result in larger (smaller) optimal implementation probabilities, $p_i^{*'}$, relative to p_i^* , for all $i \le h^*$.

Increasing the continuation value g_j to g_j' changes the principal's Stage 2 expected payoff whenever $g_j \geq g_{w_i^*}$, i.e., whenever the manager observes a cost c_i for which this specific Stage 2 project is actually implemented. To capitalize on the increased continuation value, intuition suggests that the principal should weakly increase $p_{i,j}$, which has two indirect effects. To illustrate these two effects, consider the following example. Assume there are three potential Stage 1 costs, c_1 , c_2 , and c_3 , as well as four potential Stage 2 continuation values g_1 , g_2 , g_3 , and g_4 . Further assume that the optimal $p_{i,j}$ values are represented in Table 1.

Now assume that g_3 increases to g_3' . This makes increasing $p_{2,3}$ worthwhile to the principal due to the direct effect. However, increasing $p_{2,3}$ now makes it more valuable for manager c_1 to misrepresent himself as a c_2 manager. To maintain manager c_1 's truth-telling incentive, the principal weakly increases $p_{1,4}$ (as long as g_4 is not too negative).¹⁴ In addition, increasing $p_{2,3}$ relaxes the upward (TTC) constraint for manager c_2 , which the principal exploits by weakly increasing $p_{3,2}$. Therefore, the principal weakly increases all values of $p_{i,j}$ following the increase in g_3 .

6. Conclusion

Capital investment decisions often involve multiple stages. Such investments are particularly prone to problems of adverse selection, because the firm must initially rely on managers with relevant prior experience or expertise. These informed managers thus stand to collect informational rents. We highlight the role that abandonment options and the delayed consumption of slack have on the optimal design of capital allocation schemes. These features result in an



Our model makes a number of assumptions. For example, we assume that the interim information available at Stage 2 is independent of the manager's Stage 1 cost. If instead the manager's cost information is correlated with the Stage 2 continuation cost, then the principal could further reduce the manager's informational rents by exploiting this statistical relation. However, to the extent that the Stage 2 information does not *perfectly* reveal the manager's cost, the same tensions examined in this study would continue to hold.

Our formulation also assumes that the manager only derives utility from excessive investment in assets if the project is implemented in Stage 2 and that the salvage value of the Stage 1 investment is zero if the project is abandoned. Although these assumptions are relatively strong, they are not critical to our results. All of our results continue to hold provided that (1) at least part of the manager's slack consumption depends on the project implementation and that (2) at least part of the remaining slack cannot be recouped by the principal if the project is abandoned. In other words, a necessary condition for our findings is that there be a deadweight loss associated with the Stage 1 funding (unconsumed excess assets) and that the deadweight loss depend on the manager's reported cost. Thus, in addition to the traditional trade-off between production efficiencies and informational rents, our principal is also concerned with the deadweight loss attributed to the cancelation of previously funded projects.¹⁵

Another assumption is that whereas the manager privately observes the Stage 1 cost, the Stage 2 information is publicly observed. As long as the manager cannot leave the firm after having observed the Stage 2 information (as in Pfeiffer and Schneider 2007), he would not earn any rents on that private information, and our results would continue to hold. If instead the manager could leave, the principal would design the contract to limit the additional informational rents,



 $^{^{14}}$ If $g_3 > 0$ and $g_4 < 0$, then this change results in optimal overinvestment for $c_1.$

¹⁵ Trading off productive efficiency and deadweight loss, although not informational rent, arises in the implicit contracting literature (e.g., MacLeod 2003, Rajan and Reichelstein 2009).

thereby introducing additional distortions. Alternatively, if the principal privately observes the continuation value, her ability to commit to a multistage funding rule would be limited, possibly leading to the use of implicit contracts.

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Appendix. Proofs.

Proof of Proposition 1 (i) (Stage 1 Hurdle). Note that the manager's utility does not depend on $p_{i,j}$ per-se, but only on the total implementation probability $p_i = \sum_{j=1}^k \rho_j p_{i,j}$. Therefore, in evaluating the manager's expected utility, it suffices to consider the total implementation probabilities, p_i , instead of the individual probabilities, p_i , instead of the individual probabilities, p_i , p_i . Thus, we can write the expected utility of a manager who observes and reports c_i as $z_i p_i (b_i - c_i)$. We first show that if $z_i p_i > 0$, then $b_{i-1} \leq b_i$, which will allow us to establish that $z_i \in \{0,1\}$ and that the optimal contract employs a hurdle rule for Stage 1 funding decisions.

Assuming $z_ip_i > 0$, adding the (TT^C) constraints for i and i-1 yields $z_{i-1}p_{i-1}(c_i-c_{i-1}) \ge z_ip_i(c_i-c_{i-1})$ or $z_ip_i \le z_{i-1}p_{i-1}$. To satisfy (TT^C) for i, we must have $z_ip_i(b_i-c_i) \ge z_{i-1}p_{i-1}(b_{i-1}-c_i)$; thus, $(b_i-c_i) \ge (b_{i-1}-c_i)$, or equivalently, $b_i \ge b_{i-1}$.

Note that projects are funded in Stage 1 with probability 1 or 0 ($z_i \in \{0, 1\}$) because the principal's problem is linear in z_i .

To complete the proof to Proposition 1(i) and establish the existence of a hurdle research cost, c_h , suppose a manager reporting \hat{c}_i is funded; then $z_i=1$, implying $p_i>0$ (otherwise the allocated budget is wasted). Because z_ip_i was shown to decrease in i, we have $z_{i-1}p_{i-1}>0$. Therefore, if a manager receives Stage 1 funding, all managers with lower reported costs also receive funding, which establishes the existence of a Stage 1 hurdle rule. This together with $0 < z_ip_i \le z_{i-1}p_{i-1}$ implies that $p_i \le p_{i-1}$.

(ii) (Optimal Budgets). We first show that expected rents are strictly decreasing in the reported cost, \hat{c}_i . We then prove that the upward (TT^C) constraints must bind in equilibrium, which enables us to derive the optimal budgets.

From (TT^C) for any i, l such that p_i , $p_l > 0$ and $c_i < c_l$, we have $p_i(b_i - c_i) \ge p_l(b_l - c_i) > p_l(b_l - c_l)$; that is, the manager's expected rent is decreasing in his cost observation if (TT^C) holds. If c_h is the greatest research cost observation for which $p_h > 0$, then it must be that $b_h = c_h$; i.e., when the manager truthfully reports the largest allowable research cost, he earns no expected rents. If not, the principal could increase her expected payoff by decreasing all b_i for i < h by $b_h - c_h > 0$. All (IR^C) constraints continue to be satisfied because we have already shown that $p_h > 0 \Rightarrow p_i(b_i - c_i) \ge p_h(b_h - c_h) \ \forall i < h$, and the (TT^C) constraints are unaffected because all budgets are decreased equally.

We next show that only the adjacent upward (TT^C) constraints bind at optimality. First, it is straightforward to establish that satisfying the adjacent upward constraints implies that all other upward constraints are satisfied provided that the budgets are monotonic (which was shown above). In addition, it is also straightforward to show that, given that the p_i values are weakly decreasing, satisfying the upward constraints implies that the downward constraints are also satisfied. Accordingly, we restrict our attention to adjacent upward constraints. If $p_i > 0$, then, if the upward adjacent (TT^C) constraint binds for i, we must have $p_i(b_i - c_i) = p_{i+1}(b_{i+1} - c_i)$ or, equivalently, $b_i = (p_{i+1}/p_i)(b_{i+1} - c_i)(1 - (p_i/p_{i+1}))$. Solving iteratively, we obtain $b_i = c_i + \delta \sum_{q=i+1}^{h} (p_q/p_i)$ as stated in part (ii).

To see that the adjacent upward (TTC) constraints must bind, suppose that the (TTC) constraint for a manager truthfully reporting c_i does not bind; i.e., $p_i(b_i - c_i)$ – $p_{i+1}(b_{i+1} - c_i) = \varepsilon > 0$. Consider a change wherein we reduce the budget for a manager with cost c_i by $\gamma = \varepsilon/p_i$ so that his adjacent upward (TTC) constraint now binds. The change relaxes the adjacent upward (TTC) constraint of a manager with c_{i-1} but leaves unchanged the adjacent upward (TT^C) constraints of all other managers. Because all the upward adjacent (TTC) constraints continue to hold, it is again straightforward to show that the downward constraints continue to be satisfied. Furthermore, the (IR^C) constraint for manager i+1 assures that his utility is at least 0; therefore, $p_i(b_i - c_i) - \varepsilon = p_{i+1}(b_{i+1} - c_i) > p_{i+1}(b_{i+1} - c_{i+1}) \ge 0$, and hence the new contract continues to satisfy manager i's (IR^C) constraint. Finally, we showed previously in the proof of part (i) that b_i is weakly increasing in the manager's Stage 1 cost report.

(iii)–(v). We show that the desired properties of $p_{i,j}$ follow from the first-order conditions.¹⁶ Using the optimal budgets from part (ii), we can express the principal's problem as $(1/n) \sum_{i=1}^{h} \sum_{j=1}^{k} (\rho_{j} p_{i,j} g_{j} - c_{i} - \sum_{s=i+1}^{h} (p_{s}/p_{i}) \delta)$. Differentiating with respect to $p_{i,j}$ yields $\partial U^h/\partial p_{i,j} = (\rho_j/n)[g_j +$ $\sum_{s=i+1}^{h} (p_s/p_i^2)\delta - \sum_{t=1}^{i-1} (1/p_t)\delta$]. The principal will optimally set $p_{i,j}$ such that $\partial U^h/\partial p_{i,j}=0$. If equality cannot be met with $p_{i,j} \in [0,1]$, then the principal sets $p_{i,j}^* = 1$ if $(1/\delta)g_j > \sum_{t=1}^{i-1}(1/p_t) - \sum_{s=i+1}^{h}(p_s/p_i^2)$ and $p_{i,j}^* = 0$ if $(1/\delta)g_j < 1/2$ $\sum_{t=1}^{i-1} (1/p_t) - \sum_{s=i+1}^{h} (p_s/p_i^2)$. Because g_j/δ is decreasing in j, if $p_{i,j}^* = 1$, then $p_{i,l}^* = 1$ for l < j, that is, the optimal Stage 2 implementation probabilities are weakly decreasing (increasing) in the Stage 2 index j (continuation value g_i), which establishes (iii) and the second part of (v)(a). From above, we know that $p_i \leq p_{i-1}$, which proves (iv) and (v)(b) and, together with the Stage 2 hurdle rule, implies that $p_{i,j}$ is weakly decreasing in i, which proves the first part of (v)(a). \square

PROOF OF PROPOSITION 2. To facilitate what follows, we exploit the result that the $p_{i,j}$ values are decreasing in j. Therefore, if for any given funded c_i , $p_i \leq \rho_1$, the principal only implements g_1 . Likewise, if for any given funded c_i , $\rho_1 < p_i \leq \rho_1 + \rho_2$, the principal only implements g_1 and g_2 . Therefore, we can express the principal's revenues



¹⁶ A proof that the first-order approach yields a maximum is available from the authors upon request.

associated with implementing a Stage 2 project with probability p_i as

$$\gamma(p_i) = \begin{cases} p_i g_1 & \text{for } p_i \leq \rho_1, \\ \rho_1 g_1 + (p_i - \rho_1) g_2 & \text{for } \rho_1 < p_i \leq \rho_1 + \rho_2, \\ \vdots & \vdots \\ \sum_{j=1}^{k-1} \rho_j g_j + (p_i - \sum_{j=1}^{k-1} \rho_j) g_h & \text{for } \sum_{j=1}^{k-1} \rho_j < p_i \leq \sum_{j=1}^k \rho_j. \end{cases}$$

Define the principal's utility as a function of the implementation probability vector $P = (p_1, \ldots, p_h) \in [0, 1]^h$ and budget vector $B = (b_1, \ldots, b_h)$ as $U^h(P, B) = (1/n) \sum_{i=1}^h (\gamma(p_i) - c_i - b_i)$ or as $U^h(P) = U^h(P, B^*(h))$, where $B^*(h)$ denotes the optimal budgets obtained in Proposition 1, with $b_i^* = c_i + \delta \sum_{q=i+1}^h (p_q^*/p_i^*)$.

 $\delta \sum_{q=i+1}^{h} (p_q^*/p_i^*)$. We label the least profitable (in terms of the continuation value) Stage 2 project that the principal implements with positive probability after funding a manager with reported Stage 1 cost c_i as g_{w_i} ; i.e., $p_{i,j} > 0 \Leftrightarrow j \leq w_i$.

Part (i). We first show that overinvestment relative to the first-best model in Stage 1 is never optimal.

Define h^{FB} as the optimal Stage 1 hurdle in the first-best model that funds all managers with cost less than or equal to $c_{h^{\text{FB}}}$. Fixing $h = h^{\text{FB}} + 1$ in the commitment model and optimizing over P yields the solution $P^*(h^{\text{FB}} + 1) = \{p_1^*(h^{\text{FB}} + 1), p_2^*(h^{\text{FB}} + 1), \dots, p_{h^{\text{FB}}+1}^*(h^{\text{FB}} + 1)\}$. The principal's expected utility is thus

$$U^{h^{\text{FB}}+1}(P^*(h^{\text{FB}}+1))$$

$$= \frac{1}{n} \sum_{i=1}^{h^{\text{FB}}+1} \left(\gamma(p_i^*(h^{\text{FB}}+1)) - c_i - \frac{\delta}{p_i^*(h^{\text{FB}}+1)} \sum_{s=i+1}^{h^{\text{FB}}+1} p_s^*(h^{\text{FB}}+1) \right).$$

Now, consider an alternative allocation policy where the principal does not fund the manager with reported Stage 1 cost $c_{h^{\rm FB}+1}$, but retains the all other aspects of the $P^*(h^{\rm FB}+1)$ policy. For this alternative policy the principal's expected utility is given by (note the $h^{\rm FB}$ superscript on U)

$$\begin{split} & U^{h^{\text{FB}}}(P^*(h^{\text{FB}}+1)) \\ & = \frac{1}{n} \sum_{i=1}^{h^{\text{FB}}} \bigg(\gamma(p_i^*(h^{\text{FB}}+1)) - c_i - \frac{\delta}{p_i^*(h^{\text{FB}}+1)} \sum_{s=i+1}^{h^{\text{FB}}} p_s^*(h^{\text{FB}}+1) \bigg). \end{split}$$

The marginal benefit attributed to the decreased number of funded projects in the commitment model is given by 17

$$\begin{split} U^{h^{\text{FB}}} - U^{h^{\text{FB}}+1} &= \frac{1}{n} \sum_{i=1}^{h^{\text{FB}}} \left(\gamma(p_i^*) - c_i - \frac{\delta}{p_i^*} \sum_{s=i+1}^{h^{\text{FB}}} p_s^* \right) \\ &- \frac{1}{n} \sum_{i=1}^{h^{\text{FB}}+1} \left(\gamma(p_i^*) - c_i - \frac{\delta}{p_i^*} \sum_{s=i+1}^{h^{\text{FB}}+1} p_s^* \right) \\ &= -\frac{1}{n} \left(\gamma(p_{h^{\text{FB}}+1}^*) - c_{h^{\text{FB}}+1} - \sum_{s=i+1}^{h^{\text{FB}}} \frac{\delta p_{h^{\text{FB}}+1}^*}{p_i^*} \right). \end{split}$$

Because the optimal first-best hurdle (Stage 1) cost c_{FB} is defined as the largest c_i such that $(\max_p \gamma(p)) - c_i \ge 0$,

it follows that $\gamma(p_{h^{\rm FB}+1}^*) - c_{h^{\rm FB}+1} < 0$; hence, the difference $U^{h^{\rm FB}}(P^*(h^{\rm FB}+1)) - U^{h^{\rm FB}+1}(P^*(h^{\rm FB}+1))$ is positive and the principal never overinvests in Stage 1 relative to the first-best model.

Next we show the possibility of underinvestment.

Assume that under the first-best model $h^{\rm FB}$ managers receive Stage 1 funding. Now consider the principal's solution to the commitment model assuming that the same $h^{\rm FB}$ managers receive funding in Stage 1: $P^*(h^{\rm FB}) = (p_1^*, p_2^*, \ldots, p_{h^{\rm FB}}^*) \in [0, 1]^{h^{\rm FB}}$ Let $P^{\rm FB}(h^{\rm FB}) = (p_1^{\rm FB}, \ldots, p_{h^{\rm FB}}^{\rm FB}) \in [0, 1]^{h^{\rm FB}}$ denote the first-best solution, and let $U_{\rm FB}^{h^{\rm FB}}(P^{\rm FB}(h^{\rm FB}))$ denote the principal's expected utility under the first-best model employing $h^{\rm FB}$ and $P^{\rm FB}(h^{\rm FB})$. By definition, $U_{\rm FB}^{h^{\rm FB}-1}(P^{\rm FB}(h^{\rm FB})) - U_{\rm FB}^{h^{\rm FB}}(P^{\rm FB}(h^{\rm FB})) < 0$. Comparing the FOC for the first-best and commitment models shows that $p_{h^{\rm FB}}^*(h^{\rm FB}) \leq p_{h^{\rm FB}}^{\rm FB}$; hence $\gamma(p_{h^{\rm FB}}^*(h^{\rm FB})) - c_{h^{\rm FB}} \leq \gamma(p_{h^{\rm FB}}^{\rm FB}) - c_{h^{\rm FB}}$, implying $U_{\rm FB}^{h^{\rm FB}-1}(P^{\rm FB}({\rm FB})) - U_{\rm FB}^{h^{\rm FB}}(P^{\rm FB}(h^{\rm FB})) \leq U_{\rm FB}^{h^{\rm FB}-1}(P^*(h^{\rm FB})) - U_{\rm FB}^{h^{\rm FB}}(P^{\rm FB}(h^{\rm FB}))$. Thus, the cost of underinvestment at Stage 1 is always greater in the first-best setting relative to that in the commitment setting, which implies that the principal weakly underinvests at Stage 1 in the model with commitment.

Part (ii). We next prove that Stage 1 underinvestment is mitigated with the commitment model relative to the no-commitment model. In the commitment case, the principal solves $\max_{P,B} U^h(P,B)$ subject to (IR^C) and (TT^C). Let $\{P^*(h), B^*(h)\}$ denote the principal's solution to the commitment model with h managers receiving Stage 1 funding. Similarly, the NC solution can be specified as $\{P^{NC}(h), B^{NC}(h)\}\$ with $B^{NC}(h) = (c_h, \dots, c_h)$. The NC model assumes that the principal cannot commit to a Stage 2 implementation rule and therefore acts sequentially rationally; consequently, $p_i^{NC}(h) = p^{NC}(h)$ for all i < h. The total expected profit in the NC model given a Stage 1 cost hurdle, c_h , is therefore given by $U^h(P^{NC}(h), B^{NC}(h)) =$ $h/n(\gamma(p^{NC}(h)) - c_h)$. To establish the result, we will show that the incremental profit of funding a manager with cost c_{h+1} in the commitment model is weakly greater than the incremental profit obtained in the NC setting; that is, we will show that

$$U^{h+1}(P^*(h+1), B^*(h+1)) - U^h(P^*(h), B^*(h))$$

$$\geq U^{h+1}(P^{NC}(h+1), B^{NC}(h+1)) - U^h(P^{NC}(h), B^{NC}(h)).$$

The proof is by construction. We begin with the solution $(P^*(h), B^*(h))$ and use it to generate a feasible (P(h+1), B(h+1)) contract to the $\max_{P(h+1), B(h+1)} U^{h+1} \cdot (P(h+1), B(h+1))$ problem, such that

$$\begin{split} & U^{h+1}(P(h+1),B(h+1)) - U^{h}(P^{*}(h),B^{*}(h)) \\ & \geq U^{h+1}(P^{NC}(h+1),B^{NC}(h+1)) - U^{h}(P^{NC}(h),B^{NC}(h)). \end{split}$$

The approach is sufficient, because $U^{h+1}(P^*(h+1), B^*(h+1)) \ge U^{h+1}(P(h+1), B(h+1))$ by definition.

First note that adding an additional manager in the NC model yields incremental profit to the principal of

$$U^{h+1}(P^{NC}(h+1), B^{NC}(h+1)) - U^{h}(P^{NC}(h), B^{NC}(h))$$

= $\frac{1}{n} (\gamma(p^{NC}) - c_{h+1} - h\delta),$

because all managers with cost $c_i < c_{h+1}$ now earn an additional rent of δ dollars.



 $^{^{17}}$ We omit the $(h^{\rm FB}+1)$ notation below because all implementation probabilities below are from $P^*(h^{\rm FB}+1)$.

Let s denote the smallest index, such that $p^{NC} \ge p_s^*$ (the existence of s is guaranteed by Proposition 4). Define the proposed probability vector P(h+1) as $P(h+1) = (p_1^*, \ldots, p_{s-1}^*, p^{NC}, p_s^*, \ldots, p_h^*)$ and the proposed budget vector B(h+1) as

$$B(h+1) = \left(c_1 + \delta \sum_{q=2}^{h+1} \frac{p_q}{p_1}, \dots, c_h + \delta \frac{p_{h+1}}{p_h}, c_{h+1}\right).$$

The proposed probability vector for h+1 managers begins with the original solution for h managers and changes the implementation probability for all managers with cost $c_i \ge c_s$. For $c_i = c_s$, the proposed implementation probability is p^{NC} ($p_s = p^{NC}$), and for $c_i > c_s$, the proposed implementation probability is the same probability as for manager c_{i-1} in the original solution $(p_i = p_{i-1}^* \text{ for } i > s)$. Therefore one interpretation for the proposed probability vector is that the additional manager was "inserted" between managers c_{s-1} and c_s in the original solution vector. For example, if $p^{\rm NC}=0.7$, h=4, and $P^*(h)=\{0.9,0.8,0.5,0.4\}$, then s=3, in which case the proposed probability vector is given by $P(h+1) = \{0.9, 0.8, 0.7, 0.5, 0.4\}$. Alternatively, if $p^{NC} = 0.95$, then s = 1, in which case the proposed probability vector is given by $P(h+1) = \{0.95, 0.9, 0.8, 0.5, 0.4\}$. Note that our proposed probability vector increases the overall likelihood of project implementation by $(1/n)p^{NC}$ over the prior solution, $P^*(h)$, which is the same as in the NC setting. Because all Stage 1 cost observations are equally likely, the expected incremental revenue only varies with the overall likelihood of project implementation; therefore, the incremental revenue associated with P(h+1) is identical to that incurred in the NC setting, $(1/n)\gamma(p^{NC})^{.18}$ The proposed budget vector, B(h+1), was chosen according to the optimal budget allocation outlined in Proposition 1; therefore $\{P(h+1), B(h+1)\}$ satisfies the (TT^C) and (IR^C) constraints for all managers.

To complete the proof, we demonstrate that the incremental cost of funding an additional manager in the NC setting, $(1/n)(c_{h+1} + \delta h)$, provides an upper bound for the incremental cost incurred in our proposed solution to the commitment problem. By replacing the h manager optimal contract $\{P^*(h), B^*(h)\}$ with the proposed h+1 manager contract in the commitment setting, $\{P(h+1), B(h+1)\}$, the principal incurs an incremental cost of

$$\frac{1}{n}\sum_{i=1}^{h+1}b_i - \frac{1}{n}\sum_{i=1}^{h}b_i^* = \frac{1}{n}\sum_{i=1}^{s-1}(b_i - b_i^*) + \frac{1}{n}\sum_{i=s}^{h}(b_{i+1} - b_i^*) + \frac{b_s}{n}.$$
 (2)

Because the budgets always provide a manager with cost c_i with his true cost c_i plus slack, the above difference is given by the difference in slack for the preexisting h managers plus the cost of the newly funded manager, $(1/n)c_{h+1}$. Therefore we can rewrite the incremental cost, (2), as

$$\frac{1}{n}c_{h+1} + \frac{\delta}{n} \sum_{i=1}^{s-1} \left(\sum_{q=i+1}^{h+1} \frac{p_q}{p_i} - \sum_{q=i+1}^{h} \frac{p_q^*}{p_i^*} \right) + \frac{\delta}{n} \sum_{i=s}^{h} \left(\sum_{q=i+2}^{h+1} \frac{p_q}{p_i} - \sum_{q=i+1}^{h} \frac{p_q^*}{p_i^*} \right) + \frac{1}{n} \delta \sum_{q=s+1}^{h+1} \frac{p_q}{p_{NC}}.$$
(3)

Since the proposed probability vector, P(h+1), uses (i) the same implementation probabilities as $P^*(h)$, p_i^* , (ii) $p_s = p^{NC}$ for the manager with cost c_s , and (iii) $p_i = p_{i-1}^*$ for managers with cost $c_i > c_s$, we can express the incremental cost, (3), as

$$\begin{split} &\frac{1}{n}c_{h+1} + \frac{\delta}{n}\sum_{i=1}^{s-1} \left(\sum_{q=i+1}^{s-1} \frac{p_q^*}{p_i^*} + \frac{p^{\text{NC}}}{p_i} + \sum_{q=s}^{h} \frac{p_q^*}{p_i^*} - \sum_{q=i+1}^{h} \frac{p_q^*}{p_i^*} \right) \\ &+ \frac{\delta}{n}\sum_{i=s}^{h} \left(\sum_{q=i+1}^{h} \frac{p_q^*}{p_i^*} - \sum_{q=i+1}^{h} \frac{p_q^*}{p_i^*} \right) + \frac{\delta}{n}\sum_{q=s+1}^{h+1} \frac{p_q}{p^{\text{NC}}} \\ &= \frac{1}{n}c_{h+1} + \frac{\delta}{n}\sum_{i=1}^{s-1} \frac{p^{\text{NC}}}{p_i} + \frac{\delta}{n}\sum_{q=s+1}^{h+1} \frac{p_q}{p^{\text{NC}}}. \end{split}$$

By construction, $p_i > p^{\rm NC}$ for i < s, and $p_i < p^{\rm NC}$ for i > s; therefore, we have derived an upper bound for the incremental cost associated with $\{P(h+1), B(h+1)\}$ in the commitment model, namely, $(1/n)c_{h+1} + \delta(h/n)$, which is equal to the incremental cost in the NC model. \square

Proof of Proposition 3 (i) (Weak Overinvestment for 1). To prove part (i), note that if $p_1 > 0$, then

$$\frac{\partial U^h(P^*)}{\partial p_1} = \frac{1}{n} \left(\gamma'(p_1^*) + \frac{\delta}{(p_1^*)^2} \sum_{t=2}^h p_t^* \right) \ge 0,$$

which implies $\gamma'(p_1^*)$ can be negative, even though at the efficient investment level we would have $\gamma'(p_1^{\rm FB}) \geq 0$. Because $\gamma(\cdot)$ is concave and $\partial^2 U^h(P^*)/\partial p_i \partial p_j > 0$ for $i \neq j$, the principal weakly overinvests in the commitment setting relative to the first-best setting. If $g_k \geq 0$, overinvestment is impossible, and therefore this is a mute point. Because the probabilities, p_i^* , are ordered, if overinvestment takes place for the manager with the lowest reported cost, then the principal may also overinvest for managers with greater reported costs.

To prove (ii) (underinvest for h), note that if $p_h > 0$, then the FOC with respect to p_h is

$$\frac{\partial U^h(P^*)}{\partial p_h} = \frac{1}{n} \left(\gamma'(p_h^*) - \delta \sum_{t=1}^{h-1} \frac{1}{p_t^*} \right) \ge 0,$$

which implies $\gamma'(p_h^*) \ge \delta \sum_{t=1}^{h-1} (1/p_t^*) > 0$, i.e., weak underinvestment relative to the first-best model when the manager reports sufficiently large cost realizations.

To prove part (iii) (underinvestment on average), the FOC with respect to p_i for $p_i > 0$ is

$$\frac{\partial U^h(P^*)}{\partial p_i} = \frac{1}{n} \left(\gamma'(p_i^*) - \delta \sum_{s=1}^{i-1} \frac{1}{p_s^*} + \delta \sum_{t=i+1}^h \frac{p_t^*}{(p_i^*)^2} \right) \ge 0.$$

Summing over all FOCs, substituting $\gamma'(p_i^*) = g_{w_i}$, and multiplying by n yields

$$\sum_{i=1}^{h} g_{w_i} - \delta \sum_{i=1}^{h} \left(\frac{(h-i)}{p_i^*} - \sum_{t=i+1}^{h} \frac{p_i^*}{(p_i^*)^2} \right) \ge 0.$$

Because p_i^* is weakly decreasing in i, the term in brackets is nonnegative; therefore, $\sum_{i=1}^h g_{w_i} \ge 0$, and hence, on average, there is weak underinvestment at Stage 2, i.e., $\sum_{i=1}^h (g_{w_i}/h) \ge 0$. \square

PROOF OF PROPOSITION 4. It suffices to show that the principal's objective function, $U^h(P)$, is supermodular and



¹⁸ Our assumption of discrete, rather than continuous, costs simplifies the search for, s, the smallest index, such that $p^{\text{NC}} \ge p_s^*$. Further, our assumption of uniformly distributed costs simplifies the construction of an h+1 probability vector, P(h+1), which attains the same incremental revenues as the NC model.

exhibits increasing differences for the result to hold. A sufficient condition is for all cross partials $\partial^2 U^h(P)/\partial p_i \partial p_j$ with $i \neq j$ and $\partial^2 U^h(P)/\partial p_i \partial g_j$ to carry the same sign (Sundaram 2009). Because $\partial^2 U^h/\partial p_i \partial p_j = \delta/p_j^2$ when j < i, and $\partial^2 U^h/\partial p_i \partial p_j = \delta/p_i^2$ when j > i, we conclude that U^h is supermodular over $X^h \subseteq R^h$. Furthermore, because $\partial^2 U^h/\partial p_i \partial g_j = 1 > 0$, the function U^h is supermodular over the sublattice $\{(p_1, p_2, \ldots, p_h): p_{i+1} < p_i, 0 < p_i \leq 1\} \times \{(g_1, g_2, \ldots, g_k): g_i < g_{i+1}\}$, as was to be shown. \square

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