

Assignment Four

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Our Goal: In this assignment we will read a given file and create graphs based on the listed instructions. Once a graph is done being described and built, we will print the graphs adjacency list as well as it's matrix form. Then we will print the vertex ids in breadth first order as well as in depth first order. We will do this for each graph described. We will also look at Binary Search trees. We will construct a tree of magic item strings, print out the path to insert them into the tree, perform an in order traversal which will print the items in alphabetical order, then search for 42 items in the tree and look at the number of comparisons needed to locate each one. Lastly, we will look at the average number of comparisons for the 42 lookup items and establish why that is the case.

1 Vertex Class

```
1 public class Vertex {
2     //Vertexes are made up of an id, a boolean is processed to
3     //aid with traversals and a list of neighbors
4     private int id;
5     private boolean processed;
6     public ArrayList<Vertex> neighbors;
7
8     public Vertex()
9     {
10         id = 0;
11         processed = false;
12         neighbors = new ArrayList<Vertex>();
13     } //Vertex
14
15     public Vertex(int newid)
16     {
17         id = newid;
18         processed = false;
19         neighbors = new ArrayList<Vertex>();
20     } //Vertex
21
22     public ArrayList<Vertex> getNeighbors()
23     {
24         return neighbors;
25     } //getNeighbors
26
27     public void setNeighbors(ArrayList<Vertex> newNeighbors)
28     {
29         neighbors = newNeighbors;
30     } //setNeighbors
31
32     public boolean getprocessed()
33     {
34         return processed;
35     } //getprocessed
36
37     public void setprocessed(boolean newprocessed)
38     {
39         processed = newprocessed;
40     } //setprocessed
41
42     //getter for id
43     public int getid()
```

```

44     {
45         return id;
46     } //getid
47
48
49     //setter for myData
50     public void setid(int newid)
51     {
52         id = newid;
53     } //setid
54
55     //add vertex to other vertex's list of neighbors to create an edge
56     public void addEdge(Vertex destination)
57     {
58         //System.out.println("... destination is vertex " + destination.id);
59         this.neighbors.add(destination);
60         //System.out.println("added destination vertex " + destination.id
61         + "from Vertex_" + this.id);
62     } //add edge
63 } //Vertex

```

First we must look at the vertex class. The vertices are what make up the graph and allow edges to be formed. Vertices are made up of an id or integer value, a Boolean isProcessed to aid with traversals, and an array list of neighbors to the given vertex. In addition to constructors and getters and setters for each of the mentioned attributes, we also have a method named addEdge() which when called takes the vertex it is called on and adds the vertex in parenthesis to the list of neighbors of the first vertex. This must be called in main twice since the graph is undirected – if vertex a is neighbors with vertex b, then vertex b must be neighbors with vertex a. By adding these two as neighbors we are essentially creating an edge between them.

2 Graph Class

```

1     public class Graph {
2
3     private int numOfVertices;
4     public ArrayList<Vertex> theVertices;
5
6     public Graph()
7     {
8         theVertices = new ArrayList<>();
9         numOfVertices = 0;
10
11     } //Graph
12
13     public void addVertex(int num)
14     {
15         Vertex newVertex = new Vertex(num);
16         theVertices.add(newVertex);
17         numOfVertices++;
18     } //addVertex
19
20     public int getnumOfVertices()
21     {
22         return numOfVertices;

```

```

23     }//getNumOfVertices
24
25     public void printAdjList(Graph graph)
26     {
27         for(int j = 0; j < graph.numOfVertices; j++)
28         {
29             System.out.print(graph.theVertices.get(j).getId()+ "└┐");
30             for(int q = 0; q < graph.theVertices.get(j).neighbors.size()
31             ; q++)
32             {
33                 System.out.print(graph.theVertices.get(j).neighbors
34                 .get(q).getId() + "└┐");
35             }//for
36             System.out.println();
37         }//for
38
39     }//printAdjList
40
41
42     public void printMatrix(Graph graph)
43     {
44         boolean [][] matrix = new boolean [numOfVertices][numOfVertices];
45
46         //initialize matrix to false
47         for (int i = 0; i < numOfVertices; i++)
48         {
49             for( int k= 0; k< numOfVertices; k++)
50                 matrix[i][k] = false;
51         }//for
52
53         //change from false to true if in list of neighbors
54         //if vertex id's start a 0 we do not have to adjust for the
55         //matix positions
56         if(graph.theVertices.get(0).getId() == 0)
57         {
58             for (int h = 0; h < graph.theVertices.size() ; h++)
59                 for (int p = 0; p < graph.theVertices.get(h)
60                 .getNeighbors().size(); p++)
61                     matrix[h][graph.theVertices.get(h)
62                     .getNeighbors().get(p).getId()] = true;
63         }//if
64         else
65         {
66             for (int h = 0; h < graph.theVertices.size() ; h++)
67                 for (int p = 0; p < graph.theVertices.get(h)
68                 .getNeighbors().size(); p++)
69                     matrix[h][graph.theVertices.get(h).getNeighbors()
70                     .get(p).getId()-1] = true;
71         }//else
72
73         //print out 1 for true and 0 for false
74         for (int i = 0; i < graph.numOfVertices; i++)
75         {
76             System.out.println( );
77             for (int j = 0; j < graph.numOfVertices; j++)
78             {
79                 if(matrix[i][j] == true)
80                     System.out.print("└1┐");

```

```

81         else
82             System.out.print("_0_");
83     } //for
84 } //for
85
86 } //printGraph
87
88 //depth first traversal
89 public void depthFT(Vertex v)
90 {
91     if(v.getprocessed() == false)
92     {
93         v.setprocessed(true);
94         System.out.print(v.getid() + "_");
95
96     } // if
97     for (int n = 0; n < v.neighbors.size(); n++)
98     {
99         if(v.neighbors.get(n).getprocessed() == false)
100         {
101             //recursion
102             depthFT(v.neighbors.get(n));
103         } //if
104     } //for
105 } //DepthFT
106
107 //breadth first traversal
108 public void breadthFT(Vertex v)
109 {
110     Queue q = new Queue();
111     q.enqueue(v);
112     v.setprocessed(true);
113     Vertex cv;
114     while(!q.isEmpty())
115     {
116         cv = q.dequeue();
117         System.out.print(cv.getid() + "_");
118         for(int n = 0; n < cv.neighbors.size(); n++)
119         {
120             if(cv.neighbors.get(n).getprocessed() == false)
121             {
122                 q.enqueue(cv.neighbors.get(n));
123                 cv.neighbors.get(n).setprocessed(true);
124             } //if
125         } //for
126     } //while
127 } //breadthFT
128
129 //reset processed to be false again after one traversal has been done
130 //so second traversal and start fresh
131 public void reset(Vertex v)
132 {
133     if(v.getprocessed() == true)
134     {
135         v.setprocessed(false);
136     } // if
137
138     for (int n = 0; n < v.neighbors.size(); n++)

```

```

139         {
140             if (v.neighbors.get(n).getprocessed() == true)
141             {
142                 reset(v.neighbors.get(n));
143             } //if
144         } //for
145     } //reset
146
147     //reset number of vertices and the vertices when we are moving to next graph
148     public void resetGraph(Graph graph)
149     {
150         graph.numOfVertices = 0;
151         graph.theVertices.clear();
152     } //resetGraph
153 } //Graph

```

The graph class holds most of the methods to manipulate and traverse the graph. First we have `addVertex()` which creates a new vertex, adds it to the list of vertices and increments the counter for the number of vertices. Next we have a method to print the adjacency list for the graph. To do this we have a nested for loop where the first loop goes through the list of theVertices and for each vertex we print the list of neighbors for that vertex. We then print a blank line to properly align the list. Next we have `printMatrix()` which is responsible for constructing and printing the matrix form of the graph. To do this we initialize a two dimensional array of boolean's the size of the number of vertices for the graph. We then have a nested for loop to initialize the entire matrix to false. Next we have an if else statement that determines if the vertices start at zero (meaning we done have to adjust for a zero based list) or if they start at one (we will have to subtract one from the id value of the vertex to account for zero based arrays). Once this is determined, we have another nested for loop that goes through the list of vertices and for each we go through the list of neighbors and set the appropriate matrix block to be true where the vertex has a neighbor. Lastly, we have yet another nested for loop that goes through the entire matrix printing one if the cell is true and zero if the cell is false. As a result we have a matrix the size of the number of vertices in the graph where we can use zeros and ones to determine if the vertex is neighbors with the other vertices. Next is `depthFT()` which gets passed a vertex to start at and recursively calls itself until all the vertices in theVertices list have processed values that are now true. We start with the first vertex and go through its list of neighbors calling `depthFT()` on each of them until they are all processed and printing their id out as they are processed. In other words, depth first traversals will go as deep in the graph as possible before back tracking to the width of the graph. Conversely, we have breadth first traversals. This works by first processing all the one step away vertices before moving to the two steps away vertices and so on. This works by queuing the neighbors of the vertices and processing them in that order. Once the queue is empty all the vertices have been processed and printed and the traversal is complete. To aid with these two traversals we also have `reset()` which goes through the graph yet again undoing the traversal and setting all processed boolean's back to false. This will be called between `depthFT()` and `breadthFT()` to allow the second traversal to start fresh with all processed boolean's set to false. Lastly for the Graph Class we have `resetGraph()` which is called when the adjacency list, matrix form and both traversals have been completed and we are ready to move to the next graph. This sets the number of vertices to be zero and clears the list of theVertices so

they are not added twice when the construction of the next graph begins. This completes everything needed for the graph portion of the assignment. The actual construction of the graphs and reading of the file will happen in main, so we will look at that later.

3 Binary Search Tree

```
1 public class BinarySearchTree
2 {
3
4     //comparison counter
5     public static float BSTComparisons;
6
7     class Node
8     {
9         String key;
10        Node left , right;
11
12        public Node(String item)
13        {
14            key = item;
15            left = right = null;
16        } //Node
17    } //Node
18
19    Node root;
20
21    BinarySearchTree()
22    {
23        root = null;
24    } //BinarySearchTree
25
26    public void insert (String key)
27    {
28        root = insertRecurssive( root , key);
29    } //insert
30
31    public Node insertRecurssive(Node root , String key)
32    {
33        if (root == null)
34        {
35            root = new Node(key);
36            return root;
37        } //if
38
39        if (key.compareToIgnoreCase(root.key)<0)
40        {
41            root.left = insertRecurssive(root.left , key);
42            System.out.print("L");
43        } //if
44        else if (key.compareToIgnoreCase(root.key)>=0)
45        {
46            root.right = insertRecurssive(root.right , key);
47            System.out.print("R");
48        } //elseif
49        return root;
50    } //insertRecurssive
```

```

51
52     public void inOrder()
53     {
54         inOrderRecurissive(root);
55     }//inOrder
56
57     public void inOrderRecurissive(Node root)
58     {
59         if(root != null)
60         {
61             inOrderRecurissive(root.left);
62             System.out.println(root.key);
63             inOrderRecurissive(root.right);
64         }//inOrderRecurissive
65     }//inOrderRecurissive
66
67     public Node search( Node root , String key)
68     {
69         //if the tree is empty or the one we are looking at matches the one
70         //we are searching for return the one we are looking at (root)
71         if(root == null || root.key.compareToIgnoreCase(key) == 0)
72         {
73             BSTComparisons++;
74             return root;
75         }//if
76
77         //if key comes after the one we are looking at go the right
78         if (root.key.compareToIgnoreCase(key)< 0)
79         {
80             BSTComparisons++;
81             System.out.print("R");
82             return search(root.right , key);
83         }//if
84
85         //if key comes before the one we are looking at go the left
86         else
87         {
88             BSTComparisons++;
89             System.out.print("L");
90             return search(root.left , key);
91         }//else
92     }//search
93
94     public float countComps()
95     {
96         return BSTComparisons;
97     }//countComps
98
99     public void resetComps()
100    {
101        BSTComparisons = 0;
102    }//resetComps
103 }//BinarySearchTree

```

A Binary Search Tree is made up of Nodes of magic items. When constructing the tree, all magic items alphabetically after the root node are found branched to the right while all magic items alphabetically before the root node are found to the left. With every right or

left movement we have a similar construction using each new node as the 'root' and moving left or right depending on the alphabetical order. To insert into the tree we have a recursive method as well as a non recursive method. The non recursive method is what we call in main which then calls the recursive method. When inserting an item we send the item as a string then call the recursive method sending it the root/node we left off at as well as the item were adding. In the recursive method, if the root is null we know the tree is empty and add the item to be the root. If the item were adding is less than the root we print an "L" to signify we are moving to the left and call the recursive insert function on the node to the left of the root, otherwise we do the same on the right if the item were adding comes after the root or is the same word as the root. This is done over and over again until we find the proper null space where we can add the item. We do this for each of the 666 magic items in the file. To print the items in alphabetical order we have inOrder() and inOrderRecurissive(). InOrder() is called in main which then calls inOrderRecurissive() on all the nodes to the left of the root and prints them in order, prints the root node, then calls inOrderRecurissive() on all the nodes to the right of the root node and prints them. This results in all the items printed in alphabetical order. Next we have search(). This is a recursive function that first determines if the root is null (the tree is empty) or if the root is equal to the item we are looking for. For both cases we return the root node to main and increment the global counter to establish the number of comparisons for a binary search tree. If the root/node we are looking for comes before the item we are looking for we increment comparisons, print out an "R" to signify we are moving right and recursively call search on the node to the right of the one we were looking at. We do the same thing to the left if the item we are searching for comes before the root node/the one we are looking at. This is done until the node we send equals the item we are looking for and we can print it along with the number of comparisons used to find it. Lastly, we have two helper methods to aid with counting comparisons. CountComps() is called in main and returns the global variable BSTComparisons. ResetComps() sets BSTComparisons back to zero to start fresh with the next search count.

4 ...In Main Method

```

1 public class main
2 {
3     public static float totalComparisons;
4     public static Graph theGraph = new Graph();
5
6     public static void main(String [] args)
7     {
8         //Read instructions .txt file
9         String fileName = "graphs1.txt";
10        ArrayList<String> commands = new ArrayList<>();
11        try {
12            Scanner readFile = new Scanner (new File (fileName));
13
14            while (readFile.hasNextLine())
15            {
16                commands.add(readFile.nextLine());
17
18            } //while
19        } //try

```

```

20
21     catch (FileNotFoundException ex)
22     {
23         System.out.println("Failed to find file : " + fileName);
24     } // catch
25     catch (InputMismatchException ex)
26     {
27         System.out.println("Type mismatch. ");
28         System.out.println(ex.getMessage());
29     } // catch
30     catch (NumberFormatException ex)
31     {
32         System.out.println("Failed to convert String into integer");
33         System.out.println(ex.getMessage());
34     } // catch
35     catch (NullPointerException ex)
36     {
37         System.out.println("Null pointer exception. ");
38         System.out.println(ex.getMessage());
39     } // catch
40     catch (Exception ex)
41     {
42         System.out.println("Oops, something went wrong. ");
43         ex.printStackTrace();
44     } // catch
45
46     // call makeGraph and send it the ArrayList of instructions
47     // from the .txt file
48     makeGraph(commands);
49
50
51     // For the Binary Search Tree
52     // Read MagicItems
53     String file2Name = "";
54     final int NUMOFITEMS = 666;
55     String [] magicItems = new String [NUMOFITEMS];
56     String theitem = null;
57     file2Name = "magicitems.txt";
58
59     // input item names from file and store in array
60     try
61     {
62         Scanner readFile = new Scanner (new File (file2Name));
63         int g = 0;
64         while (readFile.hasNextLine())
65         {
66             theitem = readFile.nextLine();
67             magicItems[g] = theitem;
68             g++;
69         } // while
70         readFile.close();
71     } // try
72     catch (FileNotFoundException ex)
73     {
74         System.out.println("Failed to find file : " + file2Name);
75     } // catch
76     catch (InputMismatchException ex)
77     {

```

```

78         System.out.println("Type_mismatch.");
79         System.out.println(ex.getMessage());
80     } //catch
81     catch (NumberFormatException ex)
82     {
83         System.out.println("Failed_to_convert_String_into_integer.");
84         System.out.println(ex.getMessage());
85     } //catch
86     catch (NullPointerException ex)
87     {
88         System.out.println("Null_pointer_exception.");
89         System.out.println(ex.getMessage());
90     } //catch
91     catch (Exception ex)
92     {
93         System.out.println("Oops, something_went_wrong.");
94         ex.printStackTrace();
95     } //catch
96
97     //fill the Binary Search Tree
98     BinarySearchTree tree = new BinarySearchTree();
99     for (int k = 0; k < NUMOFITEMS; k++)
100     {
101         System.out.print(magicItems[k] + ": ");
102         tree.insert(magicItems[k]);
103         System.out.println();
104     } //for
105
106     System.out.println();
107     //Traverse it in order to get an alphabetized list of magic items
108     System.out.println("In-order Traversal:");
109     tree.inOrder();
110     System.out.println();
111     System.out.println("Searches_and_Comparisons:");
112
113     //read the file with 42 items to search for and store in a new array
114     final int NUMOFSEARCHES = 42;
115     String file3Name = "magicitems-find-in-bst.txt";
116     String [] itemsToFind = new String [NUMOFSEARCHES];
117     //input item names from file and store in array
118     try
119     {
120         Scanner readFile = new Scanner (new File (file3Name));
121         int r = 0;
122         while (readFile.hasNextLine())
123         {
124             itemsToFind[r] = readFile.nextLine();
125             r++;
126         } //while
127         readFile.close();
128     } //try
129     catch (FileNotFoundException ex)
130     {
131         System.out.println("Failed_to_find_file:" + file2Name);
132     } //catch
133     catch (InputMismatchException ex)
134     {
135         System.out.println("Type_mismatch.");

```

```

136         System.out.println(ex.getMessage());
137     } //catch
138     catch(NumberFormatException ex)
139     {
140         System.out.println("Failed to convert String into integer.");
141         System.out.println(ex.getMessage());
142     } //catch
143     catch(NullPointerException ex)
144     {
145         System.out.println("Null pointer exception.");
146         System.out.println(ex.getMessage());
147     } //catch
148     catch(Exception ex)
149     {
150         System.out.println("Oops, something went wrong.");
151         ex.printStackTrace();
152     } //catch
153
154     //loop through list of items to search for
155     //search for each one
156     //print it out along with its path and number of comparisons needed
157     //to find it
158     for(int j = 0; j < NUMOFSEARCHES; j++)
159     {
160         System.out.print(itemsToFind[j] + " — ");
161
162         tree.search(tree.root, itemsToFind[j]);
163
164         totalComparisons += tree.countComps();
165         System.out.print(" — ");
166         System.out.println(tree.countComps());
167         tree.resetComps();
168     } //for
169     System.out.println();
170     //Print the average number of comparisons for a Binary Search Tree
171     System.out.println("The average number of comparisons "
172     + totalComparisons / NUMOFSEARCHES);
173
174 } //main
175
176 public static void makeGraph(ArrayList<String> list)
177 {
178     //loop through each line of the array
179     for (int i = 0; i < list.size(); i++)
180     {
181         //if line contains "undirected" we know a graph is being
182         //announced, so we can
183         //print out that line as it acts as a title for the graph
184         if(list.get(i).contains("undirected"))
185         {
186             System.out.println(list.get(i));
187         } //if
188
189         //if line contains "new graph" we know we want to make a new
190         //graph and not add to the last
191         else if(list.get(i).contains("new_graph"))
192         {
193             Graph theGraph = new Graph();

```

```

194     }
195
196     //if line contains "vertex" we want to add a new vertex to
197     //the graph
198     //We locate the last space in the line and take the number
199     //from the string
200     //and convert it to an integer , so it can be added to the
201     //graph of integers
202     else if (list.get(i).contains("vertex"))
203     {
204         int val = Integer.parseInt(list.get(i).substring(
205             list.get(i).lastIndexOf(" ") + 1 ));
206         //System.out.println("Adding Vertex");
207         theGraph.addVertex(val);
208     }//else if
209
210     //if line contains edge we are linking two vertices
211     //start finds the last index of the letter e and the index
212     //of "-" and converts the number between it to an integer
213     //end takes the number after the "-" and converts it
214     //to an integer
215     else if (list.get(i).contains("edge"))
216     {
217         int start = Integer.parseInt(list.get(i).substring(
218             list.get(i).lastIndexOf("e") + 2,
219             list.get(i).indexOf("-") - 1 ));
220         int end = Integer.parseInt(list.get(i).substring(
221             list.get(i).indexOf("-") + 2 ));
222
223         //System.out.println("Adding edge" + start+ " - "
224         //+ end);
225
226         if(theGraph.theVertices.get(0).getId() == 0)
227         {
228             theGraph.theVertices.get(start).addEdge(
229                 theGraph.theVertices.get(end));
230             theGraph.theVertices.get(end).addEdge(
231                 theGraph.theVertices.get(start));
232         }//if
233         else
234         {
235             //System.out.println("Adding edge to vertex"
236             //+ theVertices.get(start - 1 ).getId());
237             theGraph.theVertices.get(start - 1 )
238                 .addEdge(theGraph.theVertices.get(end - 1 ));
239             theGraph.theVertices.get(end - 1 )
240                 .addEdge(theGraph.theVertices.get(start - 1 ));
241         }
242     }//else
243 }//else if
244
245 //if the line is empty we know the graph is done being
246 //described and we can go about
247 //making and printing the matrix and the adjacency list
248 //as well as doing two traversals
249 else if (list.get(i).equals("")) )
250 {
251     System.out.println();

```

```

252         System.out.println("The_Adjacency_List_");
253         theGraph.printAdjList(theGraph);
254         System.out.println();
255         System.out.println("The_Matrix_");
256         theGraph.printMatrix(theGraph);
257         System.out.println();
258         System.out.println();
259         System.out.println("Depth_First_Traversal_");
260         theGraph.depthFT(theGraph.theVertices.get(0));
261         System.out.println();
262         //System.out.println(theGraph.theVertices.get(2)
263         //    .getprocessed());
264         theGraph.reset(theGraph.theVertices.get(0));
265         //System.out.println(theGraph.theVertices.get(2)
266         //    .getprocessed());
267         System.out.println();
268         System.out.println("Breadth_First_Traversal_");
269         theGraph.breadthFT(theGraph.theVertices.get(0));
270         System.out.println();
271         theGraph.resetGraph(theGraph);
272         System.out.println();
273         System.out.println();
274         System.out.println();
275
276         }//elseif
277         else
278         {
279             }//else
280     }//for
281 }//makeGraph
282
283 }//main

```

We bring all of these classes together in Main. Main begins by reading the command file for creating the graph and storing it into an Array List. We then call makeGraph() to construct the graph and print the appropriate attributes. Skipping down to makeGraph() we see we loop through the command list and if lines contain certain words we do certain tasks. First, if the line contains "undirected" we know a graph is being announced, so we print it out to label the graph's attributes that will later be printed. Next, if the line contains "new graph" we know we have to construct a new graph, so we do that. If the line contains "vertex" we know we are adding a vertex to the graph, so we locate the id in the line and convert it to an int then add it to the graph. If the line contains "edge" we know we are adding an edge, so we first locate the start and end values of the edge, then if it is the first edge being added we can do so without adjusting with minus one, otherwise we must subtract one from the start and end values before calling add edge. Lastly, if the line is empty we know we are done describing a graph, so we can call methods to print the adjacency list, the matrix form, complete the depth first traversal and breadth first traversal, and lastly reset the entire graph to prepare to make another graph if needed. This completes our exploration of an undirected graph. Moving back to the binary search tree, we start by reading the list of 666 magic items into an array. We then populate the array with those items using the insert() method we discussed earlier. Next we call the inOrder() method from earlier to print the magic items in alphabetical order. Lastly, we read in the text file that contains 42 magic items that we want to look up and count the comparisons of. We store these in

another array. We then call `search()` from the Binary Search Tree class on each of these items, print the number of comparisons needed to find them from `countComps()`, add this to the `totalComparisons` counter, and reset the `countComps()` counter in the Binary Search Tree class. To finish we divide the `totalComparisons` by the number of searches, 42, to find the average look up time for a binary search tree.

5 Conclusion

In terms of complexity for the two graph traversals, we can see that they are both

$$O(\text{ number of edges } + \text{ number of vertices })$$

This is because we of course must reach each vertex, and in order to do so we must travel across each edge to ensure that each vertex is being processed. As a result we have a running time for both depth first traversals and breadth first traversals of $O(e + v)$.

As for Binary Search tree look ups, we have a complexity of

$$O(\log \text{ base } 2 (n))$$

This is the asymptomatic running time for both look ups and insertion. This is because when we move right or left we are cutting out half of the tree. On average we will have a complexity of $\log \text{ base } 2$ of n as sometimes the item will be in the first few levels of the tree and sometimes it will be deeper. $\log \text{ base } 2$ of 666 is about 9.3, so for us getting 10.6 is in the appropriate realm of comparisons.