# PLUMED 2.4.0-dev

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## **Chapter 1**

## Introduction

PLUMED is a plugin that works with a large number of molecular dynamics codes (Codes interfaced with PLUMED). It can be used to analyse features of the dynamics on-the-fly or to perform a wide variety of free energy methods. PLUMED can also work as a Command Line Tools to perform analysis on trajectories saved in most of the existing formats. If PLUMED is useful for your work please read and cite ?, if you are interested in the PLUMED 1 original publication please read and cite ?.

To follow the development of PLUMED 2, you can look at the detailed Change Log .

To install PLUMED, see this page: Installation , while in Getting started you can find a brief introduction on how to write your first PLUMED input file.

Tutorials are available to introduce basic as well as more advanced features of PLUMED.

## 1.1 About this manual

This manual has been compiled from PLUMED version **2.4.0-dev** (git version: **1423483** ). Manual built on Travis CI for branch tutorial-lugano2017.

Regtest results for this version can be found here.

This is the user manual - if you want to modify PLUMED or to understand how it works internally, have a look at the developer manual .

## 1.2 Codes interfaced with PLUMED

PLUMED can be incorporated into an MD code and used to analyse or bias a molecular dynamics run on the fly. Some MD code could already include calls to the PLUMED library and be PLUMED-ready in its original distribution. As far as we know, the following MD codes can be used with PLUMED out of the box:

- AmberTools, sander module, since version 15.
- CP2K, since Feb 2015.
- $\bullet$  ESPResSo, in a Plumedized version that can be found here.
- PINY-MD, in its plumed branch.

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- IPHIGENIE.
- AceMD.
- OpenMM, using the openmmp-plumed plugin.
- DL\_POLY4.

Please refer to the documentation of the MD code to know how to use it with the latest PLUMED release. If you maintain another MD code that is PLUMED-ready let us know and we will add it to this list.

Additionally, we provide patching procedures for the following codes:

- amber14
- · gromacs-2016-1
- gromacs-4-5-7
- gromacs-5-1-4
- · lammps-6Apr13
- namd-2-8
- namd-2-9
- qespresso-5-0-2

Alternatively, one can use PLUMED as a Command Line Tools for postprocessing the results from molecular dynamics or enhanced sampling calculations. Notice that PLUMED can be used as an analysis tool also from the following packages:

- PLUMED-GUI is a VMD plugin that computes PLUMED collective variables.
- HTMD can use PLUMED collective variables for analysis.

## **Chapter 2**

## **Change Log**

Here you can find a history of changes across different PLUMED versions. The future releases are expected to follow more or less the pace of the old release. This means:

- Approximately once per year, after summer, a new release (2.X). These releases typically group together all the features that were contributed during the year.
- Approximately every three month, we announce a patch (e.g. 2.2.X). This typically contains bug fixes, and could occasionally contain a new feature.

A few months before each new release we provide a beta release. We typically maintain release branches until the fifth patch release (2.X.5), which should come out approximately 15 month after the original release (2.X). After that, branches are not supported anymore.

Notice that occasionally we publish patches on the mailing list. These patches are always included in the following release, but we encourage users that want to be up to date to follow the mailing list.

Below you can find change logs for all the published releases. We mostly add new features without breaking existing ones. However, some of the changes lead to incompatible behavior. In the Change Log we try to give as much visibility as possible to these changes to avoid surprises.

We also log changes that are relevant if you are developing the code. These change lists are however not complete, and if you want to put your hands in the code and maintain your own collective variables we suggest you to follow the development on github.

- Changes for Version 2.0
- Changes for Version 2.1
- Changes for Version 2.2
- Changes for Version 2.3
- Changes for Unreleased changes

#### 2.1 Version 2.0

#### Version 2.0.0 (Sep 27, 2013)

Version 2.0 is a complete rewrite, so there is no way to write a complete set of difference with respect to plumed 1.3. Here is a possibly incomplete summary of the difference:

- The input is simpler, more flexible, and more error proof. Many checks are now performed and in this way common errors are avoided.
- The units are now the same for all MD codes. If you want to use a different unit than the default you set it in the input file.
- The analysis tools are now much more flexible. As an example of this it is now possible to write different collective variables with different frequencies.
- Many complex collective variables are considerably faster than they were in plumed1. In particular, all variables based on RMSD distances.
- Centers of mass can be used as if they were atoms. Hence, unlike plumed 1.3, you can use center of mass positions in ALL collective variables.
- The virial contribution is now computed and passed to the MD code. Plumed can thus now be used to perform biased NPT simulations.
- · Variables can be dumped on different files, and are computed only when this is necessary.
- PLUMED is now compiled as a separate library. This simplifies the patching procedure, but might require some extra work to configure PLUMED properly. Since PLUMED can be loaded as a shared library, it is possible to setup everything such that PLUMED and MD codes can be updated independently from each other.

In addition, it is now much easier to contribute new functionality to the code because:

- There is a much simpler interface between plumed and the base MD codes. This makes it much easier to
  add plumed to a new MD code. Hopefully, in the future, interfaces with MD codes will be maintained by the
  developers of the MD codes independently from PLUMED developers. This will allow more MD codes to be
  compatible with PLUMED.
- There is C++ object oriented programming and full compatibility with the C++ standard library
- · A modular structure.
- · New collective variables and methods can be released independently.
- · There is an extensive developer documentation.
- User documentation is provided together inside the implementation files.

## Caveats:

- PLUMED 2 input file (plumed.dat) has a syntax which is not compatible with PLUMED 1. Transition should be easy, but cannot be done just using the new version with the old input file.
- PLUMED 2 is written in C++, thus requires a C++ compiler
- PLUMED 2 may not include all the features that were available in PLUMED 1.

A tutorial explaining how to move from PLUMED 1 to PLUMED 2 is available (see Moving from PLUMED 1 to PLUMED 2).

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## Version 2.0.1 (Nov 14, 2013)

#### For users:

 Fixed a bug in HISTOGRAM with REWEIGHT\_BIAS. Reweighting was only done when also temperaturereweighting was enabled.

- Fixed a bug that was sometime crashing code with domain decomposition and non-dense simulation boxes (e.g. implicit solvent).
- Performance improvements for GYRATION.
- · Flush all files every 10000 steps by default, without need to use FLUSH
- · Errors when writing input for switchingfunction are now properly recognized.
- Added message when simplemd is used on a non-existing file.
- Fixed plumed mklib such that it deletes the target shared library in case of compilation error.
- · Several small fixes in documentation and log file.

#### For developers:

- Added possibility to setup replica exchange from MD codes in fortran (commands "GREX setMPIFIntercomm" and "GREX setMPIFIntracomm").
- cmd("setStopFlag") should now be called after PLUMED initialization.
- · Several small fixes in documentation.

## Version 2.0.2 (Feb 11, 2014)

#### For users:

- Fixed bug with METAD with INTERVAL and replica exchange, including bias exchange. Now the bias is correctly computed outside the boundaries. Notice that this is different from what was done in PLUMED 1.3. Also notice that INTERVAL now works correctly with grids and splines.
- · Fixed bug with READ and periodic variables.
- Fixed bug with HISTOGRAM (option USE\_ALL\_DATA was not working properly).
- · Gromacs patch updated to 4.6.5.
- Gromacs patch for 4.6 has been modified to allow for better load balancing when using GPUs.
- · Added option 'plumed info -long-version' and 'plumed info -git-version'.
- · Added full reference (page/number) to published paper in doc and log.
- Fixed a bug in file backups (only affecting Windows version thanks to T. Giorgino).
- Added possibility to search in the documentation.
- · Several small fixes in documentation and log file.

### For developers:

- Fixed makefile dependencies in some auxiliary files in src/lib (\*cmake and \*inc).
- Changed way modules are linked in src/. E.g. src/colvar/tools/ is not anymore a symlink to src/colvar but
  a real directory. (Notice that this introduces a regression: when using plumed as an external library some
  include files could not work this only applies when plumed is installed; also notice that this is fixed in 2.0.3)
- Patch for gromacs 4.6 now also include original code so as to simplify its modification.
- · Added option 'plumed patch -save-originals'.
- Fixed regtest regtest/secondarystructure/rt32 to avoid problems with NUMERICAL\_DERIVATIVES.
- · Removed include graphs in the documentation (too large).
- · Several small fixes in documentation.

## Version 2.0.3 (June 30, 2014)

#### For users:

- · Now compiles on Blue Gene Q with IBM compilers.
- · Fixed bug in CENTER where default WEIGHTS were missing.
- Fixed broken CONTACTMAP with SUM
- Fixed DUMPATOMS with gro file and more than 100k atoms.
- Added CMDIST in CONTACTMAP to emulate plumed1 CMAP.
- · Several small fixes in documentation and log file.

#### For developers:

- Fixed cmd("getBias") to retrieve bias. It was not working with single precision codes and it was not converting
  units properly.
- Fixed a regression in 2.0.2 concerning include files from installed plumed (see commit 562d5ea9dfc3).
- Small fix in tools/Random.cpp that allows Random objects to be declared as static.
- · Small fix in user-doc compilation, so that if plumed is not found the sourceme.sh file is sourced
- · Fixed non-ansi syntax in a few points and a non-important memory leakage.
- Split cltools/Driver.cpp to make parallel compilation faster.

## Version 2.0.4 (Sep 15, 2014)

## For users:

- Fixed a bug in BIASVALUE that could produce wrong acceptance with replica exchange simulations.
- Fixed a few innocuous memory leaks.
- Fixed reader for xyz files, that now correctly detects missing columns. Also a related regtest has been changed.
- · Several small fixes in documentation and log file.

## For developers:

Renamed Value.cpp to BiasValue.cpp

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Version 2.0.5 (Dec 15, 2014)

Notice that branch 2.0 will not be longer maintained! All users are invited to switch to version 2.1.

For users:

• Fixed a bug in replica exchange with different Hamiltonians (either lamdba-dynamics or plumed XX-hrex branch) possibly occuring when using charge or mass dependent variables.

- Fixed a bug in analysis (e.g. HISTOGRAM) leading to wrong accumulation of statistics when running a replica exchange simulation.
- Fixed a bug in the calculation of derivatives in histograms. This should be harmless since people usually only consider the value in histograms and not the derivatives.
- Fixed an issue in Makefile that could results in problems when patching an MD code with –shared option (pointed out by Abhi Acharya). This fixes a regression introduced in 2.0.2.
- · Small fixes in documentation.

#### For developers:

· Added warning when performing regtests using an instance of plumed from a different directory

#### 2.2 Version 2.1

Version 2.1.0 (Sep 15, 2014)

Version 2.1 contains several improvements with respect to 2.0. Users currently working with 2.0 should have a look at the section "Changes leading to incompatible behavior" below and might need tiny adjustments in their input files. In 2.1 we restored more features of 1.3 that were missing in 2.0, so users still working with 1.3 could opt for an upgrade. A tutorial explaining how to move from PLUMED 1 to PLUMED 2 is available (see Moving from PLUMED 1 to PLUMED 2).

Below you find a list of all the changes with respect to version 2.0. Notice that version 2.1 includes already all the fixes in branch 2.0 up to 2.0.4.

Changes from version 2.0 which are relevant for users:

- · Changes leading to incompatible behavior:
  - COORDINATION now skips pairs of one atom with itself.
  - Labels of quantities calculated by BIASVALUE have changed from label.bias.argname to label.argname bias, which is more consistent with steered MD
  - Labels of quantities calculated by ABMD have change from label.min\_argname to label.argname\_min, which is more consistent with steered MD
  - Labels of quantities calculated by PIECEWISE have change from label.argnumber to label.argname
     — pfunc, which is more consistent with steered MD
  - For multicolvars components calculated with LESS\_THAN and MORE\_THAN keywords are now labelled less than and more than. This change is necessary as the underscore character now has a special usage in component names.
  - In CONTACTMAP components are now labelled *label*.contact- n.

- The command SPHERE has been replaced by UWALLS.
- New configuration system based on autoconf (use ./configure from root directory). Optional packages are
  detected at compile time and correctly enabled or disabled. An internal version of lapack and blas will be
  used if these libraries are not installed.
- · New actions:
  - SPRINT topological collective variables.
  - CH3SHIFTS collective variable.
  - POSITION collective variable.
  - FIT\_TO\_TEMPLATE.
  - COMMITTOR analysis.
  - LOCAL AVERAGE.
  - NLINKS.
  - DIHCOR.
  - NOE.
  - RDC.
  - CLASSICAL MDS.
  - XDISTANCES.
  - YDISTANCES.
  - ZDISTANCES.
  - DUMPMULTICOLVAR.
  - Crystallization module, including Q3, LOCAL\_Q3, Q4, Q6, LOCAL\_Q4, LOCAL\_Q6, MOLECULES, SIMPLECUBIC, TETRAHEDRAL and FCCUBIC.
  - ENSEMBLE to perform Replica-Averaging on any collective variable.
- · New features for existing actions:
  - METAD: WALKERS\_MPI flag (multiple walkers in a mpi-based multi-replica framework), ACCELE 
    RATION flag (calculate on the fly the Metadynamics acceleration factor), TAU option (alternative way to set Gaussian height in well-tempered metadynamics), GRID\_SPACING (alternative to GRID\_BIN to set grid spacing). Notice that now one can also omit GRID\_BIN and GRID\_SPACING when using fixed size Gaussian, and the grid spacing will be automatically set.
  - DISTANCE: added SCALED\_COMPONENTS
  - COORDINATION: if a single group is provided, it avoids permuted atom indexes and runs at twice the speed.
  - DUMPATOMS: PRECISION option to set number of digits in output file.
  - GROUP: NDX\_FILE and NDX\_GROUP options to import atom lists from ndx (gromacs) files.
  - In many multicolvars, MIN and MAX options can be used.
  - HISTOGRAM: GRID\_SPACING (alternative to GRID\_BIN to set grid spacing), FREE-ENERGY flags
    in addition to standard probability density, additional option for KERNEL=DISCRETE to accumulate
    standard histograms.
  - sum\_hills: added options -spacing (alternative to -bin to set grid spacing) and -setmintozero to translate the minimum of the output files to zero.
  - CONTACTMAP: parallelised and added weights.
- · New features in MD patches (require repatch):
  - New patch for Gromacs 5.0
  - Gromacs 4.6.X patch updated to 4.6.7
  - Gromacs 4.6.7 supports COMMITTOR analysis; can be now be used to perform energy minimization; now passes temperature to PLUMED (this allows temperature to be omitted in some actions, namely METAD and analysis actions).

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Notice that if you use runtime binding it is not compulsory to repatch, and that all combinations should work correctly (new/old PLUMED with repatched/non-repatched MD code).

#### · Other new features:

- driver can now read trajectories in many formats using VMD molfile plugin (requires VMD plugins to be compiled and installed). In case VMD plugins are not installed, the configuration system falls back to an internal version which implements a minimal list of plugins (gromacs and dcd) (kindly provided by T. Giorgino).
- switchingfunction: added STRETCH flag.
- Negative strides in atom ranges (e.g. ATOMS=10-1:-3 is expanded to ATOMS=10,7,4,1).
- COORDINATION and DHENERGY with NLIST now work correctly in replica exchange simulations.
- Multicolvars with neighbor lists now work correctly in replica exchange simulations.
- Improved multicolvar neighbor lists.

#### · Optimizations:

- Root-mean-square devations with align weights different from displace weights are now considerably faster. This will affect RMSD calculations plus other variables based on RMSD.
- WHOLEMOLECULES is slighlty faster.
- COORDINATION is slighlty faster when NN and MM are even and D\_0=0.
- Atom scattering with domain decomposition is slightly faster.
- Link cells are now exploited in some multicolvars.
- Derivatives are not calculated unless they are specifically required, because for instance you are adding a bias.

#### · Documentation:

- All tutorial material from the recent plumed meeting in Belfast is now in the manual
- Improvements to documentation, including lists of referenceable quantities outputted by each action
- Manual has been re-organized following suggestions received at the plumed meeting.
- An experimental PDF version of the manual is now provided (a link can be found in the documentation homepage).

#### Changes from version 2.0 which are relevant for developers:

- Added regtests for plumed as a library (e.g. basic/rt-make-0). plumed command has an additional flag (
   is-installed) to probe if running from a compilation directory or from a fully installed copy (this is needed for
   regtests to work properly).
- Improved class Communicator. Many operations can now be done directly on Vectors, Tensors, std::vector and PLMD::Matrix.
- · Modified class RMSD.
- Patches for GPL codes (QuantumEspresso and Gromacs) now also include original code so as to simplify their modification.
- colvar/CoordinationBase.cpp has been changed to make it faster. If you devised a class which inherits from here, consider that CoordinationBase::pairing now needs *squared* distance instead of distance
- It is possible to run "make install" from subdirectories (e.g. from src/colvar)
- There is a small script which disables/enables all optional modules (make mod-light/mod-heavy/mod-reset)

- · Added "-q" option to plumed patch
- You can now create new metrics to measure distances from a reference configurations. If you do so such metrics can then be used in paths straightforwardly
- · You can now use multicolvars in tandem with manyrestraints in order to add a large numbers of restraints.
- · Can now do multicolvar like things in which each colvar is a vector rather than a scalar.
- Updated script that generated header files so that they properly show years. Notice that the script should new be run from within a git repository

This list is likely incompleted, if you are developing in PLUMED you are encouraged to follow changes on github.

Version 2.1.1 (Dec 15, 2014)

This release includes all the fixes available in branch 2.0 until 2.0.5.

For users:

- New patch for AMBER 14 (sander module only). This patch should be compatible with any PLUMED 2 version (including 2.0). It includes most PLUMED features with the notable exception of multi-replica framework.
- Changed definition in arbitrary phase of eigenvectors. This will change the result of some analysis method where the phase does matter (e.g. CLASSICAL\_MDS) and make some regression test better reproducible.
- Fixed a portability issue in BG/P where gettimeofday is not implemented. Notice that this fix implies that one should execute again ./configure to have plumed timing working correctly.
- CS2Backbone: fixed a bug that resulted in only a fraction of the chemical shifts being printed with WRITE\_CS
  and parallel simulations (requires to get the last almost updated from SVN)
- NOE: fixed a bug in the replica-averaging
- Fixed a linking issue with ALMOST, where bz2 was always used to link ALMOST to PLUMED even if it is not compulsory to build ALMOST.
- · Fixed a wrong include in the GMX5 patch.
- FUNCPATHMSD can now be used together with CONTACTMAP to define pathways in contactmaps space
- Configuration is more verbose, a warning is given if a default option cannot be enabled and an error is given if an option explicitly enabled cannot be enabled.
- · Compilation is less verbose (use "make VERBOSE=1" to have old behavior)
- · Small fixes in documentation.

## For developers:

- · Tests are now performed at every single push on travis-ci.org
- · Manual is built and pushed to the online server from travis-ci.org (see developer doc)
- · Fixes in developer doc.

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## Version 2.1.2 (Mar 16, 2015)

#### For users:

- · Added two new short tutorials to the manual (Cambridge tutorial and Munster tutorial).
- Fixed a severe bug on DRMSD cutoff values were ignored by PLUMED. Notice that this bug was introduced in 2.1.0, so that it should not affect the 2.0.x series.
- Fixed a bug affecting LAMMPS patch used with a single processor. Notice that the fix is inside PLUMED, thus it does not necessarily requires repatching.
- Sander patch now works with multiple replica (no replica exchange yet). It also contains some fix from J. Swails.
- GMX5 patch was not working for bias-exchange like cases
- · Patching system now checks for the availabity of shared/static/runtime version of plumed before patching
- Configure now check better if compiler flag are accepted by the compiler. This makes configure on bluegene
  more robust.
- · Sourceme.sh now sets proper library path in linux also.

## Version 2.1.3 (June 30, 2015)

#### For users:

- · Fixed bug in ENSEMBLE derivatives when more than 1 argument was provided
- · Fixed bug in GHOST: virial is now computed correctly.
- Fixed a serious bug in virial communicated from plumed to gromacs, for both gromacs versions 4.6 and 5.

   O. See #132. This fix requires gromacs to be repatched and could be very important if you run biased simulations in the NPT ensemble.
- Fixed a bug in the virial computed with FIT\_TO\_TEMPLATE when the reference pdb had center non located at the origin.
- Fixed a bug in the the forces computed with FIT\_TO\_TEMPLATE when used in combination with COM, CENTER, or GHOST
- Fixed a bug that could lead plumed to be stuck with domain decomposition in some extreme case (one domain with all atoms, other domains empty).
- Fixed a bug when COMBINE or MATHEVAL are used with PERIODIC keyword. Now when PERIODIC keyword is used the result of the calculation is brought within the periodicity domain. See #139.
- Fixed a bug related to RANDOM\_EXCHANGES followed by INCLUDE
- · Fixed bug in derivatives of histogram bead with triangular kernels
- Updated gromacs patch 4.5.5 to 4.5.7
- · Updated internal molfile plugins to VMD 1.9.2.
- · Included crd and crdbox formats to internal molfile.
- Added –natoms to driver. This is required to read coordinate files with VMD plugins when number of atoms is not present (e.g. amber crd files)
- Added the checks in the driver to detect cases where molinfo does not provide box information (e.g. pdb).

- · Added support for readdir\_r when available, which makes opening files thread safe.
- · CFLAGS now include -fPIC by default
- Added a warning when using METAD without grids with a large number of hills.
- · Fixes in user documentation.

#### For developers:

- Allow external VMD plugins to be detected with –has-external-molfile. This is required to enable some regtest with amber files.
- · Added -dump-full-virial to driver
- Allow definition of variables where some of the components have derivatives and some haven't (#131).
- · Improved travis tests with more debug options.
- · Improved some regtest to check out-of-diagonal virial components
- · Improved make cppcheck options.
- · Fixes in developer documentation.

## Version 2.1.4 (Oct 13, 2015)

#### For users:

- Fixed NAMD patch. Masses and charges were not passed correctly, thus resulting in wrong COM or CE←
   NTER with MASS. This fix required repatching NAMD. Notice that this bug was present also in v2.0 but in a
   different form. More information here (#162), including a workaround that allows masses to be fixed without
   repatching.
- When installing with PLUMED\_LIBSUFFIX an underscore is used as separator instead of a dash. E.g. make install PLUMED\_LIBSUFFIX=2.1 will result in an executable named plumed\_v2.1. This fix a potential problem (see Installation).
- Fixed erroneously reported message about MPI at the end of ./configure.
- · Changed warning message about undocumented components.
- · PLUMED now says in the log file if it was compiled from a dirty git repository.
- Fixed a problem leading to rare random crashes when using METAD with WALKERS\_MPI and multiple processors per replica.
- Small change in numerical accuracy of lattice reduction. Should be more robust when running with highly optimizing compilers.
- Fixed a bug in normalisation of kernel functions. This affects HISTOGRAM If these actions were used with previous versions of the code care should be taken when analysing the results.
- Fixed a bug in derivatives of kernel functions with non-diagonal covariances. This affects the derivatives output by sum\_hills

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Version 2.1.5 (Jan 18, 2016)

Notice that branch 2.1 will not be longer maintained! All users are invited to switch to version 2.2.

For users:

 PLUMED now reports an error when using HISTOGRAM with FREE-ENERGY without USE\_ALL\_DATA. See #175

· Fixed a bug in configure together with -enable-almost. The check for lbz2 library was not working properly.

#### 2.3 Version 2.2

Version 2.2 (Oct 13, 2015)

Version 2.2 contains several improvements with respect to 2.1. Users currently working with 2.1 should have a look at the section "Changes leading to incompatible behavior" below and might need tiny adjustments in their input files. In 2.2 we restored more features of 1.3 that were missing in 2.1, so users still working with 1.3 could opt for an upgrade. A tutorial explaining how to move from PLUMED 1 to PLUMED 2 is available (see Moving from PLUMED 1 to PLUMED 2).

Below you find a list of all the changes with respect to version 2.1. Notice that version 2.2 includes already all the fixes in branch 2.1 up to 2.1.4 indicated in Version 2.1.

Changes from version 2.1 which are relevant for users:

- · Changes leading to incompatible behavior:
  - Labels of quantities calculates by SPRINT have changed from label.coord num to label.coord-num
  - METAD with WALKERS\_MPI now writes a single hills file, without suffixes
  - removed the ./configure.sh script of v2.0.x, now plumed can only be configured using autotools (./configure)
  - COM, CENTER, and GYRATION now automatically make molecules whole. In case you do not want them to do it, use NOPBC flag, which recovers plumed 2.1 behavior
  - Some MD code could now automatically trigger restart (e.g. gromacs when starting from cpt files). This
    can be overwritten using RESTART NO.
  - Replica suffixes are now added by PLUMED before extension (e.g. use plumed.0.dat instead of plumed.dat.0)
  - When using switchingfunction the STRETCH keyword is now implicit. NOSTRETCH is available to enforce the old behavior.
- Module activation can now be controlled during configure with --enable-modules option.
- Almost complete refactoring of installation procedure. Now DESTDIR and other standard autoconf directories (e.g. bindir) are completely supported. Additionally, everything should work properly also when directory names include spaces (#157). Finally, compiler is not invoked on install unless path are explicitly changed (#107).
- Related to installation refactoring, upon install a previusly installed plumed is not removed. This is to avoid data loss if prefix variable is not properly set
- Several changes have been made in the Makefile.conf that makes it not compatible with those packaged with plumed 2.0/2.1. Please use ./configure to generate a new configuration file.

- Added partial OpenMP parallelization, see OpenMP
- Added multiple time step integration for bias potentials, see Multiple time stepping
- Link cells are now used in all multicolvars that involve switchingfunction. The link cell cutoff is set equal to 2.\*  $d_{\mathrm{max}}$ . Where  $d_{\mathrm{max}}$  is the (user-specified) point at which the switching function goes to zero. Users should always set this parameter when using a switching function in order to achieve optimal performance.
- DHENERGY option is no longer possible within DISTANCES. You can still calculate the DHENERGY colvar by using DHENERGY
- Reweighting in the manner described in  $\bf ?$  is now possible using a combination of the METAD and HISTOG RAM actions. The relevent keywords in METAD are REWEIGHTING\_NGRID and REWEIGHTING\_NHILLS. The c(t) and the appropriate weight to apply to the configurations are given by the values labeled rct and rbias.
- · News in configure and install:
  - ./configure now allows external blas to be used with internal lapack. This is done automatically if only blas are available, and can be enforced with -disable-external-lapack.
  - ./configure supports -program-prefix, -program-suffix, and -program-transform-name.
  - make install supports DESTDIR and prefix.
  - Environment variables PLUMED\_LIBSUFFIX and PLUMED\_PREFIX are deprecated and will be removed in a later version.

#### · New actions

- DUMPMASSCHARGE to dump a file with mass and charges during MD.
- EFFECTIVE\_ENERGY\_DRIFT to check that plumed forces are not screwing the MD integrator.
- EXTENDED\_LAGRANGIAN: in combination with METAD it implements metadynamics with Extended Lagrangian; standalone it implements TAMD/dAFED.
- DFSCLUSTERING calculate the size of clusters
- DUMPMULTICOLVAR print out a multicolvar
- MFILTER LESS filter multicolvar by the value of the colvar
- MFILTER MORE
- MFILTER BETWEEN
- PCARMSD pca collective variables using OPTIMAL rmsd measure
- PCAVARS pca collective variables using any one of the measures in reference
- GRADIENT can be used to calculate the gradient of a quantity. Used to drive nucleation
- CAVITY
- PUCKERING implemented for 5-membered rings (thanks to Alejandro Gil-Ley).
- WRAPAROUND to fix periodic boundary conditions.
- · New features for existing actions:
  - Keywords UPDATE\_FROM and UPDATE\_UNTIL to limit update step in a defined time window, available only for actions where it would be useful.
  - Keyword UNNORMALIZED for HISTOGRAM.
  - Possibility to use Tiwary-Parrinello reweighting for METAD
  - Keywords for GROUP (REMOVE, SORT, UNIQUE) to allow more flexible editing of groups.
  - DUMPATOMS now supports dumping xtc and trr files (requires xdrfile library).
  - driver can now read xtc and trr files also with xdrfile library.
  - driver accepts a –mc flag to read charges and masses from a file produced during molecular dynamics with DUMPMASSCHARGE

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 Possibility to enable or disable RESTART on a per action basis, available only for actions where it would be useful.

- MOLINFO now supports many more special names for rna and dna (thanks to Alejandro Gil-Ley).
- VMEAN and VSUM allow one to calculate the sum of a set of vectors calculated by VectorMultiColvar.
   Note these can also be used in tandem with AROUND or MFILTER\_MORE to calculate the average vector within a particular part of the cell or the average vector amonst those that have a magnitude greater than some tolerance
- New way of calculating the minimum value in multicolvars (ALT\_MIN). This is less succetible to overflow for certain values of β.
- New keywords for calculating the LOWEST and HIGHEST colvar calculated by a multicolvar
- Added components to DIPOLE (#160).
- · Other changes:
  - File reader now supports dos newlines as well as files with no endline at the end.

#### For developers:

- In order to be able to use openmp parallelism within multcolvar, secondarystructure, manyrestraints and crystallisation we had to make some substantial changes to the code that underlies these routines that is contained within vesselbase. In particular we needed to get rid of the derivatives and buffer private variables in the class ActionWithVessel. As a consequence the derivatives calculated in the various performTask methods are stored in an object of type MultiValue. Within multicolvar this is contained within an object of type Atom
  ValuePack, which stores information on the atom indices. If you have implemented a new multicolvar it should be relatively straightforward to translate them so they can exploit this new version of the code. Look at what has been done to the other multicolvars in there for guidance. Sorry for any inconvenience caused.
- Changed the logic of several PLUMED ifdef macros so as to make them consistent. Now every feature based on external libraries is identified by a \_\_PLUMED\_HAS\_\* macro.

#### Version 2.2.1 (Jan 18, 2016)

#### For users:

- PBMETAD implement the new Parallel Bias Metadynamics flavor of the Metadynamics sampling method.
- PLUMED now reports an error when using HISTOGRAM with UNNORMALIZED without USE\_ALL\_DATA.
   See #175
- Fixed a bug in configure together with -enable-almost. The check for lbz2 library was not working properly.
- Fixed a bug in install procedure that was introducing an error in linking with CP2K.
- Fixed a bug that sometimes was preventing the printing of a usefull error message.

#### For developers:

- Vector and Tensor now support direct output with <<.
- Added some missing matmul operation Vector and Tensor.
- ./configure is automatically relaunched when changing ./configure or Makefile.conf. This makes it more robust to switch between branches.

## Version 2.2.2 (Apr 13, 2016)

#### For users:

- MOLINFO for RNA accepts more residue names, see #180.
- · added two mpi barries (one was missing in PBMetaD for multiple walkers) to help syncronise initialisation
- Fixed a bug in internal stopwatches that was making DEBUG logRequestedAtoms not working
- Some multicolvars (including BRIDGE, ANGLES, and INPLANEDISTANCES) now crashes if one asks for too many atoms, see #185.
- Optimisations (activation of the dependencies, secondary structures, DRMSD)
- · Fixed a performance regression with RMSD=OPTIMAL-FAST
- Fixed a bug in the normalization of kernel functions (relevant for HISTOGRAM).
- Fixed a regression introduced in v2.2 that was making METAD with non-MPI multiple walkers crash if reading frequently. See #190
- Updated patch for gromacs 5.x. Patches for gromacs 5.0 and 5.1 have been fixed so as to allow patching in runtime mode.
- Possibility to control manual generation (including pdf) from ./configure. Pdf manual is now off by default.
   Notice that on travis CI it is still generated.

#### For developers:

- Fixed a bug in the interpretation of cmd strings. Namely, an erroneous string was not triggering an error. This
  is harmless for MD codes properly patched, but could have introduced problems in MD codes with typoes in
  cmd strings.
- ./configure is not automatically relaunched anymore when doing make clean.

## Version 2.2.3 (Jun 30, 2016)

#### For users:

- Updated patches for gromacs 5.1.x and 5.0.x to fix a problem when plumed was trying to write to an already closed gromacs log file.
- When looking for a value outside the GRID now the error include the name of the responsible collective variable
- Numerical check in LatticeReduction made less picky. This should solve some of the internal errors reported by LatticeReduction.cpp when using aggressive compilers.
- Files are now flushed at the correct step. Before this fix, they were flushed at the step before the requested one (e.g. with FLUSH STRIDE=100 at step 99, 199, etc).
- In METAD, INTERVAL with periodic variables now report an error.
- LOAD now works also when plumed is installed with a suffix.
- Added --md-root option to plumed patch which allows it to be run from a directory different from the one where the md code is located.
- Wham script in Munster tutorial tutorial now writes weights in scientific notation.

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#### For developers:

- ./configure checks if dependencies can be generated. If not, they are disabled.
- · Added -disable-dependency-tracking to ./configure
- Added a make target all\_plus\_doc that builds both code and docs.
- Added possibility to set a default location for plumed library in runtime binding. If the plumed wrapped is compiled with -D\_\_PLUMED\_DEFAULT\_KERNEL=/path/libplumedKernel.so, then if the env var PLUMED KERNEL is undefined or empty PLUMED will look in the path at compile time.
- Tentative port files are now available at this link. They can be used to install PLUMED using MacPorts.

Version 2.2.4 (Dec 12, 2016)

#### For users:

- Fix a bug in PBMETAD when biasing periodic and not periodic collective variables at the same time
- GSL library is now treated by ./configure in the same way as other libraries, that is -lgsl-lgslcblas are only added if necessary.
- Fix a bug in METAD when using INTERVAL and ADAPTIVE gaussians at the same time
- Updated gromacs patch for 5.1.x to 5.1.4
- Fix a performance regression in the calculate loop where derivatives and forces were set to zero even if an action was not active, this is relevant for postprocessing and for the on-the-fly analysis
- Torsion calculation has been made slightly faster and improved so as to provide correct derivatives even for special angles (e.g. +pi/2 and -pi/2).

For developers:

· Macports portile is now tested on travis at every plumed push.

Version 2.2.5

See branch v2.2 on git repository.

For users:

- Fixed a problem with large step numbers in driver (see #209).
- Fixed a problem leading to crashes when using switching functions without cutoff with some compiler (see #210).
- Root dir is logged to allow easier debugging of problems.

#### 2.4 Version 2.3

Version 2.3 (Dec 12, 2016)

Version 2.3 contains several improvements with respect to 2.2. Users currently working with 2.2 should have a look at the section "Changes leading to incompatible behavior" below and might need tiny adjustments in their input files.

Below you find a list of all the changes with respect to version 2.2. Notice that version 2.3 includes already all the fixes in branch 2.2 up to 2.2.3 indicated in Version 2.2.

Changes from version 2.2 which are relevant for users:

- · Changes leading to incompatible behavior:
  - COMMITTOR can now be used to define multiple basins, but the syntax has been changed
  - Syntax for SPRINT and DFSCLUSTERING has changed. We have separated the Actions that calculate the contact matrix from these actions. These actions thus now take a contact matrix as input. This means that we these actions can be used with contact matrices that measures whether or not a pair of atoms are hydrogen bonded. For more details on this see Exploiting contact matrices. For clustering the output can now be passed to the actions CLUSTER\_PROPERTIES, CLUSTER\_DIAMETER, CLUSCOMERNATIONS, OUTPUT\_CLUSTER and CLUSTER\_DISTRIBUTION. These provide various different kinds of information about the connected components found by clustering
  - In driver masses and charges are set by default to NaN. This makes it less likely to do mistakes trying to compute centers of mass or electrostatic-dependent variables when masses or charges were not set.
     To compute these variables from the driver you are now forced to use --pdb or --mc.
  - In rational switching functions, by default MM is twice NN. This is valid both in switchingfunction with expanded syntax and when specifying MM on e.g. COORDINATION
  - Patch script plumed patch now patches by default with --shared. This should make the procedure more robust (see #186).
  - Faster GYRATION but new default behavior is not mass weighted
  - When using HISTOGRAM you now output the accumulated grid using DUMPGRID or DUMPCUBE to
    get the free energy you use the method CONVERT\_TO\_FES. These changes allow one to use grids
    calculated within PLUMED in a work flow of tasks similarly to the way that you can currently use Values.
  - The way that reweighting is performed is now different. There are three separate actions REWEIGHT ← \_BIAS, REWEIGHT\_TEMP and REWEIGHT\_METAD. These actions calculate the quantities that were calculated using the keywords REWEIGHT\_BIAS and REWEIGHT\_TEMP that used to appear in the old HISTOGRAM method. Now those these methods can be used in any methods that calculate ensemble averages for example HISTOGRAM and AVERAGE
  - Manual is now build with locally compiled plumed
  - Removed CH3SHIFT
  - CS2BACKBONE is now native in PLUMED removing the need to link ALMOST, small syntax differences
  - CS2BACKBONE, NOE, RDC, removed the keyword ENSEMBLE: now ensemble averages can only be calculated using ENSEMBLE
  - RDC, syntax changes
  - It is not possible anymore to select modules using modulename.on and modulename.off files.
     Use ./configure --enable-modules instead.
  - Removed IMD modules. In case someone is interested in restoring it, please contact the PLUMED developers.
- · New actions:
  - FIXEDATOM
  - HBOND MATRIX

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- CLUSTER\_PROPERTIES
- CLUSTER\_DIAMETER
- CLUSTER\_NATOMS
- OUTPUT\_CLUSTER
- CLUSTER\_DISTRIBUTION
- ROWSUMS
- COLUMNSUMS
- UPDATE\_IF
- DUMPGRID
- DUMPCUBE
- CONVERT TO FES
- INTERPOLATE GRID
- FIND\_CONTOUR
- FIND\_SPHERICAL\_CONTOUR
- FIND\_CONTOUR\_SURFACE
- AVERAGE
- REWEIGHT\_BIAS
- REWEIGHT TEMP
- REWEIGHT\_METAD
- PCA
- PRE
- STATS
- METAINFERENCE
- LOCALENSEMBLE
- FRET
- RESET CELL
- JCOUPLING
- ERMSD
- · New features in MD patches (require repatch):
  - Patch for amber 14 now passes charges with appropriate units (fixes #165). Notice that the patch is still backward compatible with older PLUMED version, but the charges will only be passed when using PLUMED 2.3 or later.
  - Patch for GROMACS 5.1 incorporates Hamiltonian replica exchange, see Using Hamiltonian replica exchange with GROMACS
  - Gromacs 2016, 5.1.x, 5.0.x, flush the plumed output files upon checkpointing
  - Added patch for Gromacs 2016.1
  - gromacs 5.1.x patch updated to 5.1.4
  - Removed the patch for Gromacs 4.6.x
  - LAMMPS patch updated to support multiple walkers and report plumed bias to LAMMPS (thanks to Pablo Piaggi).
- New features for existing actions:
  - The SPECIES and SPECIESA keyword in MultiColvars can now take a multicolvar as input. This allows
    one to calculate quantities such as the Q4 parameters for those atoms that have a coordination number
    greater than x.
  - Added MATHEVAL type in switchingfunction

- Added Q type native contacts in switchingfunction (thanks to Jan Domanski).
- COMMITTOR can now be used to define multiple basins
- The number of atoms admitted in BRIDGE has been significantly increased, see #185.
- driver now allows –trajectory-stride to be set to zero when reading with –ixtc/–itrr. In this case, step number is read from the trajectory file.
- METAD and PBMETAD can now be restarted from a GRID
- Added keywords TARGET and DAMPFACTOR in METAD
- When using METAD with file-based multple walkers and parallel jobs (i.e. mpirun) extra suffix is not added (thanks to Marco De La Pierre).
- ENSEMBLE added keywords for weighted averages, and calculation of higher momenta
- MOLINFO now allows single atoms to be picked by name.
- FIT\_TO\_TEMPLATE now supports optimal alignment.
- CONSTANT added the possibility of storing more values as components with or without derivatives
- PUCKERING now supports 6 membered rings.
- Extended checkpoint infrastracture, now METAD and PBMETAD will write GRIDS also on checkpoint step (only the GROMACS patch is currently using the checkpointing interface)

#### · Other features:

- Added a plumed-config command line tool. Can be used to inspect configuration also when cross compiling.
- Added a --mpi option to plumed, symmetric to --no-mpi. Currently, it has no effect (MPI is initialized by default when available).
- PLUMED now generate a VIM syntax file, see Using VIM syntax file
- The backward cycle is now parallelised in MPI/OpenMP in case many collective variables are used.
- GSL library is now searched by default during ./configure.
- Tutorials have been (partially) updated to reflect some of the changes in the syntax
- Parser now reports errors when passing numbers that cannot be parsed instead of silently replacing their default value. See #104.
- More and more documentation
- · Bug fixes:
- · Fixed a bug in PBMETAD that was preventing the writing of GRIDS if a hill was not added in that same step

#### For developers:

- IMPORTANT: BIAS can now be BIASED as well, this changes can lead to some incompatibility: now the "bias" component is always defined automatically by the constructure as a componentWithDerivatives, derivatives are automatically obtained by forces. The main change is that you don't have to define the bias component anymore in your constructor and that you can use setBias(value) to set the value of the bias component in calculate.
- Added new strings for plumed cmd: setMDMassUnits, setMDChargeUnits, readInputLine, performCalcNo←
   Update, update and doCheckPoint.
- · Easier to add actions with multiple arguments
- New functions to access local quantities in domain decomposition
- Active modules to enable regtests are chosen using plumed config.
- A script is available to check if source code complies plumed standard. Notice that this script is run together with cppcheck on travis-ci.
- Cppcheck on travis-ci has been updated to 1.75. Several small issues triggering errors on 1.75 were fixed (e.g. structures passed by value are now passed by const ref) and false positives marked as such.
- · Added coverage scan.

## Version 2.3.1

See branch v2.3 on git repository.

- small change in CS2BACKBONE to symmetrise the ring current contribution with respect to ring rotations (also faster)
- fixed plumed-config that was not working.
- log file points to the config.txt files to allow users to check which features were available in that compiled version.
- make clean in root dir now also cleans vim subdirectory.

## For developers:

- Cppcheck on travis-ci has been updated to 1.77.
- Doxygen on travis-ci has been updated to 1.8.13

## 2.5 Unreleased changes

This page contains changes that will end up in 2.4

Changes from version 2.3 which are relevant for users:

- PBMETAD : multiple walkers using files (thanks to Marco De La Pierre).
- PBMETAD : adaptive gaussians
- PBMETAD : default names for GRID and FILE (usefull with many collective variables)
- IMPLICIT: EEF1-SB implicit solvent solvation energy

## **Chapter 3**

## Installation

In this page you can learn how to configure, compile, and install PLUMED. For those of you who are impatient, the following might do the job:

```
> ./configure --prefix=/usr/local
> make -j 4
> make doc # this is optional and requires proper doxygen version installed
> make install
```

Notice that make install is not strictly necessary as plumed can be used from the compilation directory. This is very useful so as to quickly test the implementation of new features. However, we strongly recommend to perform a full install.

Once the above is completed the plumed executable should be in your execution path and you will be able to use PLUMED to analyze existing trajectories or play with the Lennard-Jones code that is included. However, because PLUMED is mostly used to bias on the fly simulations performed with serious molecular dynamics packages, you can find instructions about how to patch your favorite MD code so that it can be combined with PLUMED below. Again, if you are impatient, something like this will do the job:

```
> cd /md/root/dir
> plumed patch -p
```

Then compile your MD code. For some MD codes these instructions are insufficient. It is thus recommended that you read the instructions at the end of this page. Notice that MD codes could in principle be "PLUMED ready" in their official distribution. If your favorite MD code is available "PLUMED ready" you will have to compile PLUMED first, then (optionally) install it, then check the MD codes' manual to discover how to link it.

If you are using a Mac, notice that we are providing tentative port files to install PLUMED with MacPorts. Follow the instructions at this link and report feedbacks on the mailing list.

## 3.1 Configuring PLUMED

The ./configure command just generates a Makefile.conf file and a sourceme.sh file. In PLUMED 2.0 these files were pre-prepared and stored in the directory configurations/. The new ones generated by ./configure are similar to the old ones but are not completely compatible. In particular, some of the -D options have been changed in version 2.2, and several new variables so as to specify the installation directories have been added. For this reason, you now should run ./configure again. Anyway, it should be easy to enforce a similar setup with autoconf by passing the proper arguments on the command line. If you have problems on your architecture, please report them to the mailing list.

Useful command line options for ./configure can be found by typing

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```
> ./configure --help
```

PLUMED is made up of modules. Some of them are on by default, some others aren't. Since version 2.2, the activation of modules can be made during configuration using the --enable-modules option (see List of modules).

Notice that some functionalities of PLUMED depend on external libraries which are looked for by configure. You can typically avoid looking for a library using the "disable" syntax, e.g.

```
> ./configure --disable-mpi --disable-matheval
```

Notice that when mpi search is enabled (by default) compilers such as "mpic++" and "mpicxx" are searched for first. On the other hand, if mpi search is disabled ("./configure --disable-mpi") non-mpi compilers are searched for. Notice that only a few of the possible compiler name are searched. Thus, compilers such as "g++-mp-4.8" should be explicitly requested with the CXX option.

You can better control which compiler is used by setting the variables CXX and CC. E.g., to use Intel compilers use the following command:

```
> ./configure CXX=icpc CC=icc
```

Notice that we are using icpc in this example, which is not an mpi compiler as a result mpi will not be enabled. Also consider that this is different with respect to what some other configure script does in that variables such as MPICXX are completely ignored here. In case you work on a machine where CXX is set to a serial compiler and MPICXX to a MPI compiler, to compile with MPI you should use

```
> ./configure CXX="$MPICXX"
```

#### Warning

This procedure could be somehow confusing since many other programs behave in a different way. The flag <code>--enable-mpi</code> is perfectly valid but is not needed here. Autoconf will check if a code containing MPI calls can be compiled, and if so it will enable it. <code>--disable-mpi</code> could be used if you are using a compiler that supports MPI but you don't want PLUMED to be compiled with MPI support. Thus the correct way to enable MPI is to pass to ./configure the name of a C++ compiler that implements MPI using the CXX option. In this way, MPI library is treated similarly to all the other libraries that PLUMED tries to link by default.

To tune the compilation options you can use the CXXFLAGS variable:

```
> ./configure CXXFLAGS=-03
```

If you are implementing new functionality and want to build with debug flags in place so as to do some checking you can use

```
> ./configure --enable-debug
```

This will perform some extra check during execution (possibly slowing down PLUMED) and write full symbol tables in the executable (making the final executable much larger).

The main goal of the automatic configure is to find the libraries. When they are stored in unconventional places it is thus sensible to tell autoconf where to look! To do this there are some environment variable that can be used to instruct the linker which directories it should search for libraries inside. These variables are compiler dependent, but could have been set by the system administrator so that libraries are found without any extra flag. Our suggested procedure is to first try to configure without any additional flags and to then check the log so as to see whether or not the libraries were properly detected.

If a library is not found during configuration, you can try to use options to modify the search path. For example if your matheval libraries is in /opt/local (this is where MacPorts put it) and configure is not able to find it you can try

```
> ./configure LDFLAGS=-L/opt/local/lib CPPFLAGS=-I/opt/local/include
```

Notice that PLUMED will first try to link a routine from say matheval without any additional flag, and then in case of failure will retry adding "-Imatheval" to the LIBS options. If also this does not work, the matheval library will be disabled and some features will not be available. This procedure allows you to use libraries with custom names. So, if your matheval library is called /opt/local/lib/libmymatheval.so you can link it with

```
> ./configure LDFLAGS=-L/opt/local/lib CPPFLAGS=-I/opt/local/include LIBS=-lmymatheval
```

In this example, the linker will directly try to link /opt/local/lib/libmymatheval.so. This rule is true for all the libraries, so that you will always be able to link a specific version of a library by specifying it using the LIBS variable.

#### Warning

On Linux you might have problems using the LDFLAGS option. In particular, if makefile complaints that it cannot link the file 'src/lib/plumed-shared', try to set correctly the runtime path by using

```
> ./configure LDFLAGS="-L/opt/local/lib -Wl,-rpath,/opt/local/lib" \
    CPPFLAGS=-I/opt/local/include LIBS=-lmymatheval
```

Notice that although the file 'src/lib/plumed-shared' is not necessary, being able to produce it means that it will be possible to link PLUMED dynamically with MD codes later.

PLUMED needs blas and lapack. These are treated slighty different from other libraries. The search is done in the usual way (i.e., first look for them without any link flag, then add "-lblas" and "-llapack", respectively). As such if you want to use a specific version of blas or lapack you can make them available to configure by using

```
> ./configure LDFLAGS=-L/path/to/blas/lib LIBS=-lnameoflib
```

If the functions of these libraries are not found, the compiler looks for a version with a final underscore added. Finally, since blas and lapack are compulsory in PLUMED, you can use a internal version of these libraries that comes as part of PLUMED. If all else fails the internal version of BLAS and LAPACK are the ones that will be used by PLUMED. If you wish to disable any search for external libraries (e.g. because the system libraries have problems) this can be done with

```
> ./configure --disable-external-blas
```

Notice that you can also disable external lapack only, that is use internal lapack with external blas using

```
> ./configure --disable-external-lapack
```

Since typically it is the blas library that can be heavily optimized, this configuration should not provide significant slowing down and could be used on systems where native lapack libraries have problems.

As a final resort, you can also edit the resulting Makefile.conf file. Notable variables in this file include:

- DYNAMIC\_LIB: these are the libraries needed to compile the PLUMED library (e.g. -L/path/to/matheval lmatheval etc). Notice that for the PLUMED shared library to be compiled properly these should be dynamic libraries. Also notice that PLUMED preferentially requires BLAS and LAPACK library; see BLAS and LAPACK for further info. Notice that the variables that you supply with configure LIBS=something will end up in this variable. This is a bit misleading but is required to keep the configuration files compatible with PLUMED 2.0.
- LIBS: these are the libraries needed when patching an MD code; typically only "-ldl" (needed to have functions for dynamic loading).
- CPPFLAGS: add here definition needed to enable specific optional functions; e.g. use -D\_\_PLUMED\_HA
   S\_MATHEVAL to enable the matheval library
- SOEXT: this gives the extension for shared libraries in your system, typically "so" on unix, "dylib" on mac; If your system does not support dynamic libraries or, for some other reason, you would like only static executables you can just set this variable to a blank ("SOEXT=").

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#### 3.1.1 BLAS and LAPACK

We tried to keep PLUMED as independent as possible from external libraries and as such those features that require external libraries (e.g. Matheval) are optional. However, to have a properly working version of plumed PLUMED you need BLAS and LAPACK libraries. We would strongly recommend you download these libraries and install them separately so as to have the most efficient possible implementations of the functions contained within them. However, if you cannot install blas and lapack, you can use the internal ones. Since version 2.1, PLUMED uses a configure script to detect libraries. In case system LAPACK or BLAS are not found on your system, PLUMED will use the internal replacement.

We have had a number of emails (and have struggled ourselves) with ensuring that PLUMED can link BLAS and LAPACK. The following describes some of the pitfalls that you can fall into and a set of sensible steps by which you can check whether or not you have set up the configuration correctly.

Notice first of all that the DYNAMIC\_LIB variable in the Makefile.conf should contain the flag necessary to load the BLAS and LAPACK libraries. Typically this will be -llapack -lblas, in some case followed by -lgfortran. Full path specification with -L may be necessary and on some machines the blas and lapack libraries may not be called -llapack and -lblas. Everything will depend on your system configuration.

Some simple to fix further problems include:

- If the linker complains and suggests recompiling lapack with -fPIC, it means that you have static lapack libraries. Either install dynamic lapack libraries or switch to static compilation of PLUMED by unsetting the SOEXT variable in the configuration file.
- If the linker complains about other missing functions (typically starting with "for\_" prefix) then you should also link some Fortran libraries. PLUMED is written in C++ and often C++ linkers do not include Fortran libraries by default. These libraries are required for lapack and blas to work. Please check the documentation of your compiler.
- If the linker complains that dsyevr\_ cannot be found, try adding -DF77\_NO\_UNDERSCORE to CPPFLAGS Notice that "./configure" should automatically try this solution.

## 3.2 Compiling PLUMED

Once configured, PLUMED can be compiled using the following command:

```
> make -j 4
```

This will compile the entire code and produce a number of files in the 'src/lib' directory, including the executable 'src/lib/plumed'. When shared libraries are enabled, a shared libraries called 'src/lib/libKernel.so' should also be present. Notice that the extension could be '.dylib' on a Mac.

In case you want to run PLUMED without installing it (i.e. from the compilation directory), you can use the file 'sourceme.sh' that has been created by the configure script in the main PLUMED directory. This file can be "sourced" (presently only working for bash shell) if you want to use PLUMED before installing it (i.e. from the compilation directory). It is a good idea to source it now, so that you can play with the just compiled PLUMED:

```
> source sourceme.sh
```

Now a "plumed" executable should be in your path. Try to type

```
> plumed -h
```

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#### Warning

If you are cross compiling, the plumed executable will not work. As a consequence, you won't be able to run regtests or compile the manual. This is not a problem.

You can also check if PLUMED is correctly compiled by performing our regression tests. Be warned that some of them fail because of the different numerical accuracy on different machines.

```
> cd regtest
> make
```

Notice that regtests are performed using the "plumed" executable that is currenty in the path. You can check the exact version they will use by using the command

```
> which plumed
```

This means that if you do not source "sourceme.sh", the tests will fails. This does not mean that plumed is not working it just means that you haven't told them shell where to find plumed!

Notice that the compiled executable, which now sits in 'src/lib/plumed', relies on other resource files present in the compilation directory. This directory should thus stay in the correct place. One should thus not rename or delete it. In fact the path to the PLUMED root directory is hardcoded in the plumed executable as can be verified using

```
> plumed info --root
```

In case you try to use the plumed executable without the compilation directory in place (e.g. you move away the src/lib/plumed static executable and delete or rename the compilation directory) PLUMED will not work correctly and will give you an error message

```
> plumed help
ERROR: I cannot find /xxx/yyy/patches directory
```

You can force plumed to run anyway by using the option -standalone-executable:

```
> plumed --standalone-executable help
```

Many features will not be available if you run in this way. However, this is currently the only way to use the PLUMED static executable on Windows.

## 3.3 Installing PLUMED

It is strongly suggested to install PLUMED in a predefined location. This is done using

```
> make install
```

This will allow you to remove the original compilation directory, or to recompile a different PLUMED version in the same place.

To install PLUMED one should first decide the location. The standard way to do it is during the configure step:

```
> ./configure --prefix=$HOME/opt
> make
> make install
```

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However, you can also change it after compilation setting the variable prefix.

```
> ./configure
> make
> make install prefix=$HOME/opt
```

If you didn't specify the <code>--prefix</code> option during configure, and you did not set the <code>prefix</code> variable when installing, PLUMED will be installed in /usr/local. The install command should be executed with root permissions (e.g. "sudo make install") if you want to install PLUMED on a system directory.

Notice that upon installation PLUMED might need to relink a library. This was always true until version 2.1, but in version 2.2 libraries should only be relinked if one changes the install prefix during when typing make install. If root user does not have access to compilers, "sudo -E make install" might solve the issue.

Upon install, executables are copied to \$prefix/bin, libraries to \$prefix/lib, include files to \$prefix/include, and documentation to \$prefix/shared/doc/plumed. Additionally, a directory \$prefix/lib/plumed is created containing several other files, including patch files, object files (for static patches), etc. Notice also that these path can be further customized using standard autoconf directories (e.g. ./configure --bindir=/usr/bin64).

One should then set the environment properly. We suggest to do it using the module framework (http-://modules.sourceforge.net). An ad hoc generated module file for PLUMED can be found in \$pre-fix/lib/plumed/src/lib/modulefile Just edit it as you wish and put it in your modulefile directory. This will also allow you to install multiple PLUMED versions on your machine and to switch amongst them. If you do not want to use modules, you can still have a look at the modulefile we did so as to know which environment variables should be set for PLUMED to work correctly.

If the environment is properly configured one should be able to do the following things:

- use the "plumed" executable from the command line. This is also possible before installing.
- link against the PLUMED library using the "-lplumed" flag for the linker. This allows one to use PLUMED library in general purpose programs
- use the PLUMED internal functionalities (C++ classes) including header files such as "#include <plumed/tools/Vector.h>". This is useful as it may be expedient to exploit the PLUMED library in general purpose programs

As a final note, if you want to install several PLUMED versions without using modules then you should provide a different suffix and/or prefix at configure time:

```
> ./configure prefix=$HOME/opt --program-suffix=_2.2 --program-prefix=mpi-
> make install
```

This will install a plumed executable named "mpi-plumed\_2.2". All the other files will be renamed similarly, e. ← g. the PLUMED library will be loaded with "-lmpi-plumed\_2.2" and the PLUMED header files will be included with "#include <mpi-plumed\_2.2/tools/Vector.h>". Notice that you can also use arbitrary scripts to edit the name of the executable with the option –program-transform-name=PROGRAM (see autoconf documentation for more info). These options are useful if you do not want to set up modules, but we believe that using modules as described above is more flexible.

## 3.4 Patching your MD code

A growing number of MD codes can use PLUMED without any modification. If you are using one of these codes, refer to its manual to know how to activate PLUMED. In case your MD code is not supporting PLUMED already, you should modify it. We provide scripts to adjust some of the most popular MD codes so as to provide PLUMED support. At the present times we support patching the following list of codes:

- amber14
- · gromacs-2016-1
- · gromacs-4-5-7
- gromacs-5-1-4
- · lammps-6Apr13
- namd-2-8
- namd-2-9
- · qespresso-5-0-2

In the section Code specific notes you can find information specific for each MD code.

To patch your MD code, you should have already installed PLUMED properly. This is necessary as you need to have the command "plumed" in your execution path. As described above this executible will be in your paths if plumed was installed or if you have run sourceme.sh

Once you have a compiled and working version of plumed, follow these steps to add it to an MD code

- Configure and compile your MD enginge (look for the instructions in its documentation).
- · Test if the MD code is working properly.
- Go to the root directory for the source code of the MD engine.
- · Patch with PLUMED using:

```
> plumed patch -p
```

The script will interactively ask which MD engine you are patching.

Once you have patched recompile the MD code (if dependencies are set up properly in the MD engine, only
modified files will be recompiled)

There are different options available when patching. You can check all of them using

```
> plumed patch --help
```

Particularly interesting options include:

-static (default) just link PLUMED as a collection of object files. This is only suggested if for external reasons
you absolutely need a static executable. Notice that with this setting it is often more complicated to configure
properly the MD code, since all the libraries that PLUMED depends on should be properly specified. The
./configure script does its best in this sense, but sometime it cannot solve the problem. Additionally, this
patching mode has been reported not to work properly on OSX.

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-shared allows you to link PLUMED as a shared library. As a result when PLUMED is updated, there will be
no need to recompile the MD code. This is way better than -static since the libraries that PLUMED depends
on should be automatically linked. Notice that if you later remove the directory where PLUMED is installed
also the MD code will not run anymore.

-runtime allows you to choose the location of the PLUMED library at runtime by setting the variable PLUM←
ED\_KERNEL. This is probably the most flexible option, and we encourage system administrators to use this
option when installing PLUMED on shared facilities. Indeed, using this setting it will be possible to update
separately the PLUMED library and the MD code, leaving to the user the possibility to combine different
versions at will. We also recommend to use the provided modulefile (see above) to properly set the runtime
environment.

Notice that it is not currently possible to link PLUMED as a static library (something like 'libplumed.a'). The reason for this is that PLUMED heavily relies on C++ static constructors that do not behave well in static libraries. For this reason, to produce a static executable with an MD code + PLUMED we link PLUMED as a collection of object files.

If your MD code is not supported, you may want to implement an interface for it. Refer to the developer manual

## 3.5 Cross compiling

If you are compiling an executable from a different machine, then plumed executable will not be available in the compilation environment. This means that you won't be able to perform regtests on the machine nor to compile the manual. You can try to run the regtests on the computing nodes, but this might require some tweak since often machines where people do cross compiling have architectures with limited capabilities on the compute nodes. Also notice that many of the plumed options (e.g. patch) are implemented as shell scripts launched from within the plumed executable. If the compute nodes have some limitation (e.g. they do not allow to fork new processes) these options will not work. Anyway, the PLUMED library in combination with an MD software should work if both PLUMED and the MD software have been properly compiled.

Also notice that it will not be possible to use the command plumed patch on the machine where you are compiling. You should thus use plumed-patch instead of plumed patch (notice that it should be written as a single word).

Try e.g.:

> plumed-patch --help

This script provides a "shell only" implementation of plumed patch that will skip the launch of the plumed executable.

Notice that other command line tools will be available in the directory <code>prefix/lib/progname/</code>. If configuring with default values this would be <code>/usr/local/lib/plumed/plumed-\*</code>. These files are not included in the execution path (prefix/bin) to avoid clashes, but can be executed also when plumed is cross compiled and the main plumed executable cannot be launched.

## 3.6 Installing PLUMED on a cluster

If you are installing PLUMED on a cluster and you want several users to take advantage of it consider the following suggestions.

First of all, we highly recommend using the module file that PLUMED provides to set up the environment. Just edit it as necessary to make it suitable for your environment.

Notice that PLUMED can take advantage of many additionaly features if specific libraries are available upon compiling it. Install libraries and check if PLUMED ./configure is detecting it. Libraries a must have with PLUMED. If someone uses gromacs, install libraries first and check if PLUMED ./configure is detecting it. PLUMED will be able to write trr/xtc file, simplifying analysis.

Try to patch all MD codes with the —runtime option. This will allow independent update of PLUMED and MD codes. Users will be able to combine any of the installed gromacs/amber/etc versions with any of the installed PLUMED versions. Notice that it is sometime claimed that statically linked codes are faster. In our experience, this is not true. In case you absolutely need a static executable, be ready to face non trivial linking issues. PLUMED is written in C++, thus required the appropriate C++ library to be linked, and might require additional libraries (e.g. libmatheval).

Sometime we make small fixes on the patches. For this reason, keep track of which version of PLUMED you used to patch each of the MD code. Perhaps you can call the MD code modules with names such as gromacs/4.6.7p1, gromacs/4.6.7p2 and write somewhere in the module file which version of PLUMED you used. Alternatively, call them something like gromacs/4.6.7p2.2.0. In this way, when we report a bug on the mailing list, users will know if the version they are using is affected by it.

Usually it is not necessary to install both a MPI and a non-MPI PLUMED version. PLUMED library only calls MPI functions when the MD code is compiled with MPI. PLUMED executable calls MPI functions only when it is invoked without --no-mpi. In many machines it is thus sufficient to run the plumed executable on the login node as

```
> plumed --no-mpi
```

even though PLUMED was compiled with MPI and the login node does not support MPI. The only case where you might need two different PLUMED installation for compute and login node is when you are cross compiling.

PLUMED needs to be well optimized to run efficiently. If you need a single PLUMED binary to run efficiency on machines with different levels of hardware (e.g.: some of your workstations support AVX and some do not), with intel compiler you can use something like

```
./configure CXX=mpicxx CXXFLAGS="-03 -axSSE2,AVX"
```

It will take more time to compile but it will allow you to use a single module. Otherwise, you should install two PLUMED version with different optimization levels.

Using modules, it is not necessary to make the PLUMED module explicitly dependent on the used library. Imagine a scenario where you first installed a module libmatheval, then load it while you compile PLUMED. If you provide the following option to configure LDFLAGS="-Wl,-rpath,\$LD\_LIBRARY\_PATH", the PLUMED executable and library will remember where libmatheval is, without the need to load libmatheval module at runtime. Notice that this trick often does not work for fundamental libraries such as C++ and MPI library. As a consequence, usually the PLUMED module should load the compiler and MPI modules.

## Attention

In case you found out how to compile PLUMED on some fancy architecture please share your tricks! You can either post it in your blog, send it to the mailing list, or ask as to update this paragraph in the manual, we will be happy to do so.

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## 3.7 Other hints

We here collect a list of suggestions that might be useful on particular machines.

• On Blue Gene Q (likely on AIX) the prelinking made with ld -r is not working properly. There is no easy way to detect this at configure time. If during make you receive an error in the form

```
ld: TOC section size exceeds 64k

please configure plumed again with the following flag
./configure --disable-ld-r
```

## 3.8 Code specific notes

Here you can find instructions that are specific for patching each of the supported MD codes. Notice that MD codes with native PLUMED support are not listed here.

- amber14
- gromacs-2016.1
- gromacs-4.5.7
- gromacs-5.1.4
- · lammps-6Apr13
- namd-2.8
- namd-2.9
- qespresso-5.0.2

### 3.8.1 amber14

PLUMED can be incorporated into amber (sander module) using the standard patching procedure. Patching must be done in the root directory of amber *before* compilation.

To enable PLUMED in a sander simulation one should use add to the cntrl input namelist these two fields:

```
plumed=1 , plumedfile='plumed.dat'
```

The first is switching plumed on, the second is specifying the name of the plumed input file.

This patch is compatible with the MPI version of sander and support multisander. However, replica exchange is not supported. Multisander can thus only be used for multiple walkers metadynamics or for ensemble restraints.

For more information on amber you should visit http://ambermd.org

## 3.8.2 gromacs-2016.1

PLUMED can be incorporated into gromacs using the standard patching procedure. Patching must be done in the gromacs root directory *before* the cmake command is invoked.

On clusters you may want to patch gromacs using the static version of plumed, in this case building gromacs can result in multiple errors. One possible solution is to configure gromacs with these additional options:

```
cmake -DBUILD_SHARED_LIBS=OFF -DGMX_PREFER_STATIC_LIBS=ON
```

To enable PLUMED in a gromacs simulation one should use mdrun with an extra -plumed flag. The flag can be used to specify the name of the PLUMED input file, e.g.:

gmx mdrun -plumed plumed.dat

For more information on gromacs you should visit http://www.gromacs.org

## 3.8.3 gromacs-4.5.7

PLUMED can be incorporated into gromacs using the standard patching procedure. Patching must be done in the gromacs source directory *after* gromacs has been configured but *before* gromacs is compiled. Gromcas should be configured with ./configure (not cmake).

To enable PLUMED in a gromacs simulation one should use mdrun with an extra -plumed flag. The flag can be used to specify the name of the PLUMED input file, e.g.:

mdrun -plumed plumed.dat

For more information on gromacs you should visit http://www.gromacs.org

## 3.8.4 gromacs-5.1.4

PLUMED can be incorporated into gromacs using the standard patching procedure. Patching must be done in the gromacs root directory *before* the cmake command is invoked.

On clusters you may want to patch gromacs using the static version of plumed, in this case building gromacs can result in multiple errors. One possible solution is to configure gromacs with these additional options:

```
cmake -DBUILD_SHARED_LIBS=OFF -DGMX_PREFER_STATIC_LIBS=ON
```

To enable PLUMED in a gromacs simulation one should use mdrun with an extra -plumed flag. The flag can be used to specify the name of the PLUMED input file, e.g.:

gmx mdrun -plumed plumed.dat

This patch also implements the -hrex keyword for gromacs. See Using Hamiltonian replica exchange with GROM ← ACS

For more information on gromacs you should visit http://www.gromacs.org

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# 3.8.5 lammps-6Apr13

PLUMED can be incorporated into LAMMPS using a simple patching procedure. Patching must be done *before* LAMMPS is configured. After patching, one should enable PLUMED using the command make yes-user-plumed In the same way, before reverting one should disable PLUMED using the command make no-user-plumed

Also notice that command "fix plumed" should be used in lammps input file *after* the relevant input parameters have been set (e.g. after "timestep" command)

See also http://lammps.sandia.gov/doc/Section\_commands.html for further info on processing LAMMPS input, as well as this discussion on github: http://github.com/plumed/plumed2/issues/67.

For more information on LAMMPS you should visit http://lammps.sandia.gov/

## 3.8.6 namd-2.8

**Bug** NAMD does not currently take into account virial contributions from PLUMED. Please use constant volume simulations only

For more information on NAMD you should visit http://www.ks.uiuc.edu/Research/namd/

## 3.8.7 namd-2.9

**Bug** NAMD does not currently take into account virial contributions from PLUMED. Please use constant volume simulations only

For more information on NAMD you should visit http://www.ks.uiuc.edu/Research/namd/

## 3.8.8 qespresso-5.0.2

For more information on Quantum Espresso you should visit http://www.quantum-espresso.org

# **Chapter 4**

# **Getting started**

To run PLUMED you need to provide one input file. In this file you specify what it is that PLUMED should do during the course of the run. Typically this will involve calculating one or more collective variables, perhaps calculating a function of these CVs and then doing some analysis of values of your collective variables/functions or running some free energy method. A very brief introduction to the syntax used in the PLUMED input file is provided in this 10-minute video.

Within this input file every line is an instruction for PLUMED to perform some particular action. This could be the calculation of a colvar, an occasional analysis of the trajectory or a biassing of the dynamics. The first word in these lines specify what particular action is to be performed. This is then followed by a number of keywords which provide PLUMED with more details as to how the action is to be performed. These keywords are either single words (in which they tell PLUMED to do the calculation in a particular way - for example NOPBC tells PLUMED to not use the periodic bounadry conditions when calculating a particular colvar) or they can be words followed by an equals sign and a comma separated list *with no spaces* of numbers or characters (so for example ATOMS=1,2,3,4 tells PLUMED to use atom numbers 1,2,3 and 4 in the calculation of a particular colvar). Space separated lists can be used instead of commma separated list if the entire list is enclosed in curly braces (e.g. ATOMS={1 2 3 4}). Please note that you can split commands over multiple lines by using Continuation lines.

The most important of these keywords is the label keyword as it is only by using these labels that we can pass data from one action to another. As an example if you do:

DISTANCE ATOMS=1,2

(see DISTANCE)

Then PLUMED will do nothing other than read in your input file. In contrast if you do:

DISTANCE ATOMS=1,2 LABEL=d1
PRINT ARG=d1 FILE=colvar STRIDE=10

(see PRINT)

then PLUMED will print out the value of the distance between atoms 1 and 2 every 10 steps to the file colvar as you have told PLUMED to take the value calculated by the action d1 and to print it. You can use any character string to label your actions as long as it does not begin with the symbol @. Strings beginning with @ are used by within PLUMED to reference special, code-generated groups of atoms and to give labels to any Actions for which the user does not provide a label in the input.

Notice that if a word followed by a column is added at the beginning of the line (e.g. pippo:), PLUMED automatically removes it and adds an equivalent label (LABEL=pippo). Thus, a completely equivalent result can be obtained with the following shortcut:

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```
d1: DISTANCE ATOMS=1,2
PRINT ARG=d1 FILE=colvar STRIDE=10
```

Also notice that all the actions can be labeled, and that many actions besides normal collective variables can define one or more value, which can be then referred using the corresponding label.

Actions can be referred also with POSIX regular expressions (see Regular Expressions) if regex library is available on your system and detected at configure time. You can also add Comments to the input or set up your input over multiple files and then create a composite input by Including other files.

More information on the input syntax as well as details on the the various trajectory analisys tools that come with PLUMED are given in:

- · Collective variables tells you about the ways that you can calculate functions of the positions of the atoms.
- Analysis tells you about the various forms of analysis you can run on trajectories using PLUMED.
- · Bias tells you about the methods that you can use to bias molecular dynamics simulations with PLUMED.

## 4.1 Plumed units

By default the PLUMED inputs and outputs quantities in the following units:

- · Energy kJ/mol
- Length nanometers
- · Time picoseconds

Unlike PLUMED 1 the units used are independent of the MD engine you are using. If you want to change these units you can do this using the UNITS keyword.

## 4.2 UNITS

This is part of the setup module

This command sets the internal units for the code. A new unit can be set by either specifying how to convert from the plumed default unit into that new unit or by using the shortcuts described below. This directive MUST appear at the BEGINNING of the plumed.dat file. The same units must be used throughout the plumed.dat file.

Notice that all input/output will then be made using the specified units. That is: all the input parameters, all the output files, etc. The only exceptions are file formats for which there is a specific convention concerning the units. For example, trajectories written in .gro format (with DUMPATOMS) are going to be always in nm.

**Options** 

4.2 UNITS 37

| NATURAL | ( default=off ) use natural units  |
|---------|--|
| LENGTH  | the units of lengths. Either specify a conversion factor from the default, nm, or A (for angstroms) or um  |
| ENERGY  | the units of energy. Either specify a conversion factor from the default, kj/mol, or use j/mol or kcal/mol |
| TIME    | the units of time. Either specify a conversion factor from the default, ps, or use ns or fs                |
| MASS    | the units of masses. Specify a conversion factor from the default, amu                                     |
| CHARGE  | the units of charges. Specify a conversion factor from the default, e                                      |

# Examples

```
# this is using nm - kj/mol - fs
UNITS LENGTH=nm TIME=fs
If a number, x, is found, the new unit is equal to x (default units)
# this is using nm - kj/mol - fs
UNITS LENGTH=nm TIME=0.001
```

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# **Chapter 5**

# **Collective variables**

Chemical systems contain an enormous number atoms, which, in most cases makes it simply impossible for us to understand anything by monitoring the atom postions directly. Consquentially, we introduce Collective variables (CVs) that describe the chemical processes we are interested in and monitor these simpler quantities instead. These CVs are used in many of the methods implemented in PLUMED - there values can be monitored using PRI NT, Functions of them can be calculated or they can be analyzed or biased using the Analysis and Biasing methods implemented in PLUMED. Before doing any of these things however we first have to tell PLUMED how to calculate them.

The simplest collective variables that are implemented in PLUMED take in a set of atomic positions and output one or multiple scalar CV values. Information on these variables is given on the page entitled CV Documentation while information as to how sets of atoms can be selected can be found in the pages on Groups and Virtual Atoms. Please be aware that PLUMED contains implementations of many other collective variables but that the input for these variables may be less transparent when it is first encourntered. In particular, the page on Distances from reference configurations describes the various ways that you can calculate the distance from a particular reference configuration. So you will find instructions on how to calculate the RMSD distance from the folded state of a protein here. Meanwhile, the page on Functions describes the various functions of collective variables that can be used in the code. This is a very powerful feature of PLUMED as you can use the Functions commands to calculate any function or combination of the simple collective variables listed on the page CV Documentation. Lastly the page on MultiColvar describes MultiColvars. MultiColvars allow you to use many different colvars and allow us to implement all these collective variables without implementing having an unmanigiably large ammount of code. For some things (e.g. DISTANCES GROUPA=1 GROUPB=2-100 LESS\_THAN={RATIONAL R\_0=3}) there are more computationally efficient options available in plumed (e.g. COORDINATION). However, MultiColvars are worth investigating as they provide a flexible syntax for many quite-complex CVs.

- · Groups and Virtual Atoms
- CV Documentation
- · Distances from reference configurations
- Functions
- MultiColvar
- Exploiting contact matrices

# 5.1 Groups and Virtual Atoms

## 5.1.1 Specifying Atoms

The vast majority of the CVs implemented in PLUMED are calculated from a list of atom positions. Within PLUMED atoms are specified using their numerical indices in the molecular dynamics input file.

In PLUMED lists of atoms can be either provided directly inside the definition of each collective variable, or predefined as a GROUP that can be reused multiple times. Lists of atoms can be written as:

- comma separated lists of numbers (GROUP ATOMS=10,11,15,20 LABEL=g1)
- numerical ranges. So GROUP ATOMS=10-20 LABEL=g2 is equivalent to GROUP ATOMS=10,11,12,13,14,15,16,17,18,19,20 LABEL=g2
- numerical ranges with a stride. So GROUP ATOMS=10-100:10 LABEL=g3 is equivalent to GROUP ATO
   MS=10,20,30,40,50,60,70,80,90,100 LABEL=g3
- atoms ranges with a negative stride. So GROUP ATOMS=100-10:-10 LABEL=g4 is equivalent to GROUP ATOMS=100,90,80,70,60,50,40,30,20,10 LABEL=g4
- all the above methods together. For example GROUP ATOMS=1,2,10-20,40-60:5,100-70:-2 LABEL=g5.

Some collective variable must accept a fixed number of atoms, for example a DISTANCE is calculated using two atoms only, an ANGLE is calculated using either 3 or 4 atoms and TORSION is calculated using 4 atoms.

Additional material and examples can be also found in the tutorial Belfast tutorial: Analyzing CVs.

#### 5.1.1.1 Molecules

In addition, for certain colvars, pdb files can be read in using the following keywords and used to select ATOMS:

| MOLINFO | This command is used to provide information on the molecules that are present in your system. |
|---------|---|
|---------|---|

The information on the molecules in your system can either be provided in the form of a pdb file or as a set of lists of atoms that describe the various chains in your system using MOLINFO. If a pdb file is used plumed the MOLINFO command will endeavor to recognize the various chains and residues that make up the molecules in your system using the chainIDs and resnumbers from the pdb file. You can then use this information in commands where this has been implemented to specify atom lists. One place where this is particularly useful is when using the commands ALPHARMSD, ANTIBETARMSD and PARABETARMSD.

MOLINFO also introduces special groups that can be used in atom selection. These special groups always begin with a @ symbol. The following special groups are currently available in PLUMED:

| Symbol | Topology type | Despription  |
|--------|---------------|--|
| @phi-# | protein       | The torsional angle defined by the C, CA, N and C atoms of the protein back- |
|        |               | bone in the #th residue. See http://en.wikipedia.org/wiki/↔                  |
|        |               | Ramachandran_plot  |
| @psi-# | protein       | The torsional angle defined by the N, C, CA and N atoms of the protein back- |
|        |               | bone in the #th residue. See http://en.wikipedia.org/wiki/↔                  |
|        |               | Ramachandran_plot  |

| @omega-# | protein | The torsional angle defined by the CA, N, C and CA atoms of the protein backbone in the #th residue. See http://en.wikipedia.org/wiki/ Ramachandran_plot                               |
|----------|---------|--|
| @chi1-#  | protein | The first torsional angle of the sidechain of the #th residue. Be aware that this angle is not defined for GLY or ALA residues. See http://en.com/wikipedia.org/wiki/Ramachandran_plot |

The following example shows how to use MOLINFO with TORSION to calculate the torsion angles phi and psi for the first and fourth residue of the protein:

```
MOLINFO MOLTYPE=protein STRUCTURE=myprotein.pdb
t1: TORSION ATOMS=@phi-3
t2: TORSION ATOMS=@psi-4
PRINT ARG=t1,t2 FILE=colvar STRIDE=10
```

#### 5.1.1.2 Broken Molecules and PBC

PLUMED is designed so that for the majority of the CVs implemented the periodic boundary conditions are treated in the same manner as they would be treated in the host code. In some codes this can be problematic when the colvars you are using involve some property of a molecule. These codes allow the atoms in the molecules to become separated by periodic boundaries, a fact which PLUMED could only deal with were the topology passed from the MD code to PLUMED. Making this work would involve a lot laborious programming and goes against our original aim of having a general patch that can be implemented in a wide variety of MD codes. Consequentially, we have implemented a more pragmatic solution to this probem - the user specifies in input any molecules (or parts of molecules) that must be kept in tact throughout the simulation run. In PLUMED 1 this was done using the ALIGN\_ATOMS keyword. In PLUMED 2 the same effect can be achieved using the WHOLEMOLECULES command.

The following input computes the end-to-end distance for a polymer of 100 atoms and keeps it at a value around 5.

```
WHOLEMOLECULES ENTITY0=1-100
e2e: DISTANCE ATOMS=1,100 NOPBC
RESTRAINT ARG=e2e KAPPA=1 AT=5
```

Notice that NOPBC is used to be sure in DISTANCE that if the end-to-end distance is larger than half the simulation box the distance is compute properly. Also notice that, since many MD codes break molecules across cell boundary, it might be necessary to use the WHOLEMOLECULES keyword (also notice that it should be before distance).

Notice that most expressions are invariant with respect to a change in the order of the atoms, but some of them depend on that order. E.g., with WHOLEMOLECULES it could be useful to specify atom lists in a reversed order.

```
# to see the effect, one could dump the atoms as they were before molecule reconstruction:
# DUMPATOMS FILE=dump-broken.xyz ATOMS=1-20
WHOLEMOLECULES STRIDE=1 ENTITY0=1-20
DUMPATOMS FILE=dump.xyz ATOMS=1-20
```

Notice that there are other ways to manipulate the coordinates stored within PLUMED:

- Using the FIT TO TEMPLATE they can be aligned to a template structure.
- Using WRAPAROUND you can bring a set of atom as close as possible to another set of atoms.
- · Using RESET CELL you can rotate the periodic cell.

## 5.1.2 Virtual Atoms

Sometimes, when calculating a colvar, you may not want to use the positions of a number of atoms directly. Instead you may wish to use the position of a virtual atom whose position is generated based on the positions of a collection of other atoms. For example you might want to use the center of mass of a group of atoms. Plumed has a number of routines for calculating the positions of these virtual atoms from lists of atoms:

| CENTER_OF_MULTICOLVAR | Calculate a a weighted average position based on the value of some multi-   |
|-----------------------|---|
|                       | colvar.   |
| CENTER                | Calculate the center for a group of atoms, with arbitrary weights.  |
| COM                   | Calculate the center of mass for a group of atoms.  |
| FIXEDATOM             | Add a virtual atom in a fixed position.   |
| GHOST                 | Calculate the absolute position of a ghost atom with fixed coordinatesin the local reference frame formed by three atoms. The computed ghost atom is stored as a virtual atom that can be accessed inan atom list through the label for the GHOST action that creates it. |

To specify to a colvar that you want to use the position of a virtual atom to calculate a colvar rather than one of the atoms in your system you simply use the label for your virtual atom in place of the usual numerical index. Virtual atoms and normal atoms can be mixed together in the input to colvars as shown below:

COM ATOMS=1,10 LABEL=com1 DISTANCE ATOMS=11,com1

If you don't want to calculate CVs from the virtual atom. That is to say you just want to monitor the position of a virtual atom (or any set of atoms) over the course of your trajectory you can do this using DUMPATOMS.

## 5.1.3 **GROUP**

This is part of the generic module

Define a group of atoms so that a particular list of atoms can be referenced with a single label in definitions of CVs or virtual atoms.

Atoms can be listed as comma separated numbers (i.e. 1,2,3,10,45,7,9,...), simple positive ranges (i.e. 20-40), ranges with a stride either positive or negative (i.e. 20-40:2 or 80-50:-2) or as combinations of all the former methods (1,2,4,5,10-20,21-40:2,80-50:-2).

Moreover, lists can be imported from ndx files (GROMACS format). Use NDX\_FILE to set the name of the index file and NDX\_GROUP to set the name of the group to be imported (default is first one).

It is also possible to remove atoms from a list and or sort them using keywords REMOVE, SORT, and UNIQUE. The flow is the following:

- If ATOMS is present take the ordered list of atoms from the ATOMS keyword.
- If NDX\_FILE is present append the list from the the gromacs group.
- If REMOVE is present remove the first occurrence of each of these atoms from the list. If one tries to remove an atom that was not listed plumed adds a notice in the output.
- · If SORT is present resulting list is sorted.
- If UNIQUE is present the resuling list is sorted and duplicate elements are removed.

Notice that this command just creates a shortcut, and does not imply any real calculation. It is just convenient to better organize input files. Might be used in combination with the INCLUDE command so as to store long group definitions in a separate file.

The atoms involved can be specified using

| ATOMS  | the numerical indexes for the set of atoms in the group. For more information on how to specify lists of atoms see Groups and Virtual Atoms |
|--------|---|
| REMOVE | remove these atoms from the list. For more information on how to specify lists of atoms see Groups and Virtual Atoms                        |

## **Options**

| SORT      | ( default=off ) sort the resulting list  |
|-----------|--|
| UNIQUE    | ( default=off ) sort atoms and remove duplicated ones  |
| NDX_FILE  | the name of index file (gromacs syntax)  |
| NDX_GROUP | the name of the group to be imported (gromacs syntax) - first group found is used by default |

## **Examples**

This command create a group of atoms containing atoms 1,4,7,11 and 14 (labeled 'o'), and another containing atoms 2,3,5,6,8,9,12,13 (labeled 'h'):

```
o: GROUP ATOMS=1,4,7,11,14
h: GROUP ATOMS=2,3,5,6,8,9,12,13
# compute the coordination among the two groups
c: COORDINATION GROUPA=0 GROUPB=h R_0=0.3
# same could have been obtained without GROUP, just writing:
# c: COORDINATION GROUPA=1,4,7,11,14 GROUPB=2,3,5,6,8,9,12,13
# print the coordination on file 'colvar'
PRINT ARG=c FILE=colvar
```

## (see also COORDINATION and PRINT)

Groups can be conveniently stored in a separate file. E.g. one could create a file named 'groups.dat' which reads

```
o: GROUP ATOMS=1,4,7,11,14
h: GROUP ATOMS=2,3,5,6,8,9,12,13
```

and then include it in the main 'plumed.dat' file

```
INCLUDE FILE=groups.dat
# compute the coordination among the two groups
c: COORDINATION GROUPA=o GROUPB=h R_0=0.3
# print the coordination on file 'colvar'
PRINT ARG=c FILE=colvar
```

(see also INCLUDE, COORDINATION, and PRINT). The groups.dat file could be very long and include lists of thousand atoms without cluttering the main plumed.dat file.

A GROMACS index file can also be imported

```
# import group named 'protein' from file index.ndx
pro: GROUP NDX_FILE=index.ndx NDX_GROUP=protein
# dump all the atoms of the protein on a trajectory file
DUMPATOMS ATOMS=pro FILE=traj.gro
```

## (see also DUMPATOMS)

A list can be edited with REMOVE

```
# take one atom every three
ox: GROUP ATOMS=1-90:3
# take the remaining atoms
hy: GROUP ATOMS=1-90 REMOVE=ox
DUMPATOMS ATOMS=ox FILE=ox.gro
DUMPATOMS ATOMS=hy FILE=hy.gro
```

(see also **DUMPATOMS**)

## 5.1.4 MOLINFO

This is part of the setup module

This command is used to provide information on the molecules that are present in your system.

The information on the molecules in your system can either be provided in the form of a pdb file or as a set of lists of atoms that describe the various chains in your system. If a pdb file is used plumed the MOLINFO command will endeavor to recognize the various chains and residues that make up the molecules in your system using the chain ← IDs and resnumbers from the pdb file. You can then use this information in later commands to specify atom lists in terms residues. For example using this command you can find the backbone atoms in your structure automatically.

#### Warning

Please be aware that the pdb parser in plumed is far from perfect. You should thus check the log file and examine what plumed is actually doing whenenver you use the MOLINFO action. Also make sure that the atoms are listed in the pdb with the correct order. If you are using gromacs, the safest way is to use reference pdb file generated with gmx editconf -f topol.tpr -o reference.pdb.

Using MOLINFO with a protein's pdb extend the possibility of atoms selection using the @ special symbol.

Providing MOLTYPE=protein, MOLTYPE=rna, or MOLTYPE=dna will instruct plumed to look for known residues from these three types of molecule (so that any of these three choice can be safely used in a RNA/protein complex).

For protein residues, the following groups are available:

```
@phi-#
@psi-#
@omega-#
@chi1-#
```

that select the appropriate atoms that define each dihedral angle for residue #.

For DNA or RNA residues, the following groups are available:

```
# quadruplets for backbone dihedral angles
@alpha-#
@beta-#
@gamma-#
@delta-#
@epsilon-#
@zeta-#
# quadruplets for sugar dihedral angles
@v0-#
@ \u03c7 1 - #
@v2-#
@v3-#
@v4-#
# backbone, sugar, and base heavy atoms
@sugar-#
@base-#
```

Notice that zeta and epsilon groups should not be used on 3' end residue and alpha and beta should not be used on 5' end residue.

If the chosen group name does not match any of the default ones, the parser looks for a single atom with the same name. This means that it is also possible to pick single atoms using the syntax @atom-residue.

## Warning

If a residue-chain is repeated twice in the reference pdb only the first entry will be selected.

- **Bug** At the moment the HA1 atoms in a GLY residues are treated as if they are the CB atoms. This may or may not be true GLY is problematic for secondary structure residues as it is achiral.
- **Bug** If you use WHOLEMOLECULES RESIDUES=1-10 for a 18 amino acid protein (18 amino acids + 2 terminal groups = 20 residues) the code will fail as it will not be able to interpret terminal residue 1.

The atoms involved can be specified using

| CHAIN | (for masochists (mostly Davide Branduardi)) The atoms involved in each of the chains of interest in |  |
|-------|---|--|
|       | the structure For more information on how to specify lists of atoms see Groups and Virtual Atoms    |  |

## Compulsory keywords

| STRUCTURE | a file in pdb format containing a reference structure. This is used to defines the atoms in the various residues, chains, etc. For more details on the PDB file format visit http://www. |  |
|-----------|--|--|
|           | wwpdb.org/docs.html  |  |
| MOLTYPE   | ( default=protein ) what kind of molecule is contained in the pdb file   |  |

## **Examples**

In the following example the MOLINFO command is used to provide the information on which atoms are in the backbone of a protein to the ALPHARMSD CV.

```
MOLINFO STRUCTURE=reference.pdb ALPHARMSD RESIDUES=all TYPE=DRMSD LESS_THAN={RATIONAL R_0=0.08 NN=8 MM=12} LABEL=a
```

(see also ALPHARMSD)

The following example prints the distance corresponding to the hydrogen bonds in a GC Watson-Crick pair.

```
MOLINFO STRUCTURE=reference.pdb
hb1: DISTANCE ATOMS=@N2-1,@O2-14
hb2: DISTANCE ATOMS=@N1-1,@N3-14
hb3: DISTANCE ATOMS=@O6-1,@N4-14
PRINT ARG=hb1,hb2,hb3
```

(see also DISTANCE).

#### 5.1.5 WHOLEMOLECULES

This is part of the generic module

This action is used to rebuild molecules that can become split by the periodic boundary conditions.

It is similar to the ALIGN\_ATOMS keyword of plumed1, and is needed since some MD dynamics code (e.g. GR← OMACS) can break molecules during the calculation.

Running some CVs without this command can cause there to be discontinuities changes in the CV value and artifacts in the calculations. This command can be applied more than once. To see what effect is has use a variable without pbc or use the DUMPATOMS directive to output the atomic positions.

## Attention

This directive modifies the stored position at the precise moment it is executed. This means that only collective variables which are below it in the input script will see the corrected positions. As a general rule, put it at the top of the input file. Also, unless you know exactly what you are doing, leave the default stride (1), so that this action is performed at every MD step.

The way WHOLEMOLECULES modifies each of the listed entities is this:

- · First atom of the list is left in place
- Each atom of the list is shifted by a lattice vectors so that it becomes as close as possible to the previous one, iteratively.

In this way, if an entity consists of a list of atoms such that consecutive atoms in the list are always closer than half a box side the entity will become whole. This can be usually achieved selecting consecute atoms (1-100), but it is also possible to skip some atoms, provided consecute chosen atoms are close enough.

The atoms involved can be specified using

#### **ENTITY**

the atoms that make up a molecule that you wish to align. To specify multiple molecules use a list of ENTITY keywords: ENTITY0, ENTITY1,... You can use multiple instances of this keyword i.e. ENTITY1, ENTITY2, ENTITY3...

Or alternatively by using

#### **RESIDUES**

this command specifies that the backbone atoms in a set of residues all must be aligned. It must be used in tandem with the MOLINFO action and the MOLTYPE keyword. If you wish to use all the residues from all the chains in your system you can do so by specifying all. Alternatively, if you wish to use a subset of the residues you can specify the particular residues you are interested in as a list of numbers

Compulsory keywords

**STRIDE** 

( default=1 ) the frequency with which molecules are reassembled. Unless you are completely certain about what you are doing leave this set equal to 1!

**Options** 

MOLTYPE

the type of molecule that is under study. This is used to define the backbone atoms

**Examples** 

This command instructs plumed to reconstruct the molecule containing atoms 1-20 at every step of the calculation and dump them on a file.

```
# to see the effect, one could dump the atoms as they were before molecule reconstruction:
# DUMPATOMS FILE=dump-broken.xyz ATOMS=1-20
WHOLEMOLECULES ENTITY0=1-20
DUMPATOMS FILE=dump.xyz ATOMS=1-20
```

## (see also DUMPATOMS)

This command instructs plumed to reconstruct two molecules containing atoms 1-20 and 30-40

```
WHOLEMOLECULES ENTITY0=1-20 ENTITY1=30-40 DUMPATOMS FILE=dump.xyz ATOMS=1-20,30-40
```

## (see also DUMPATOMS)

This command instructs plumed to reconstruct the chain of backbone atoms in a protein

```
MOLINFO STRUCTURE=helix.pdb WHOLEMOLECULES RESIDUES=all MOLTYPE=protein
```

(See also MOLINFO)

## 5.1.6 FIT\_TO\_TEMPLATE

This is part of the generic module

This action is used to align a molecule to a template.

This can be used to move the coordinates stored in plumed so as to be aligned with a provided template in pdb format. Pdb should contain also weights for alignment (see the format of pdb files used e.g. for RMSD). Weights for displacement are ignored, since no displacement is computed here. Notice that all atoms (not only those in the template) are aligned. To see what effect try the DUMPATOMS directive to output the atomic positions.

Also notice that PLUMED propagate forces correctly so that you can add a bias on a CV computed after alignment. For many CVs this has no effect, but in some case the alignment can change the result. Examples are:

- POSITION CV since it is affected by a rigid shift of the system.
- DISTANCE CV with COMPONENTS. Since the alignment could involve a rotation (with TYPE=OPTIMAL) the actual components could be different from the original ones.
- CELL components for a similar reason.

#### Attention

The implementation of TYPE=OPTIMAL is available but should be considered in testing phase. Please report any strange behavior.

This directive modifies the stored position at the precise moment it is executed. This means that only collective variables which are below it in the input script will see the corrected positions. As a general rule, put it at the top of the input file. Also, unless you know exactly what you are doing, leave the default stride (1), so that this action is performed at every MD step.

## Compulsory keywords

| STRIDE    | ( default=1 ) the frequency with which molecules are reassembled. Unless you are completely certain about what you are doing leave this set equal to 1! |
|-----------|---|
| REFERENCE | a file in pdb format containing the reference structure and the atoms involved in the CV.   |
| TYPE      | ( default=SIMPLE ) the manner in which RMSD alignment is performed. Should be OPTIMAL or SIMPLE.  |

### **Examples**

Align the atomic position to a template then print them

```
# to see the effect, one could dump the atoms before alignment
DUMPATOMS FILE=dump-before.xyz ATOMS=1-20
FIT_TO_TEMPLATE STRIDE=1 REFERENCE=ref.pdb TYPE=SIMPLE
DUMPATOMS FILE=dump-after.xyz ATOMS=1-20
```

(see also **DUMPATOMS**)

## 5.1.7 WRAPAROUND

This is part of the generic module

Rebuild periodic boundary conditions around chosen atoms.

Modify position of atoms indicated by ATOMS by shifting them by lattice vectors so that they are as close as possible to the atoms indicated by AROUND. More precisely, for every atom i in the ATOMS list the following procedure is performed:

- The atom j among those in the AROUND list is searched that is closest to atom i.
- The atom i is replaced with its periodic image that is closest to atom j.

This action works similarly to WHOLEMOLECULES in that it replaces atoms coordinate. Notice that only atoms specified with ATOMS are replaced, and that, at variance with WHOLEMOLECULES, the order in which atoms are specified is irrelevant.

This is often convenient at a post processing stage (using the driver), but sometime it is required during the simulation if collective variables need atoms to be in a specific periodic image.

#### Attention

This directive modifies the stored position at the precise moment it is executed. This means that only collective variables which are below it in the input script will see the corrected positions. As a general rule, put it at the top of the input file. Also, unless you know exactly what you are doing, leave the default stride (1), so that this action is performed at every MD step.

Consider that the computational cost grows with the product of the size of the two lists (ATOMS and AROUND), so that this action can become very expensive. If you are using it to analyse a trajectory this is usually not a big problem. If you use it to analyze a simulation on the fly, e.g. with DUMPATOMS to store a properly wrapped trajectory, consider the possibility of using the STRIDE keyword here (with great care).

The atoms involved can be specified using

| AROUND | reference atoms. For more information on how to specify lists of atoms see Groups and Virtual Atoms |
|--------|---|
| ATOMS  | wrapped atoms. For more information on how to specify lists of atoms see Groups and Virtual Atoms   |

## Compulsory keywords

| STRIDE  | ( default=1 ) the frequency with which molecules are reassembled. Unless you are completely |
|---------|---|
|         | certain about what you are doing leave this set equal to 1!                                 |
| GROUPBY | ( default=1 ) group atoms so as not to break molecules                                      |

## **Examples**

This command instructs plumed to move all the ions to their periodic image that is as close as possible to the rna group.

```
rna: GROUP ATOMS=1-100
ions: GROUP ATOMS=101-110
# first make the rna molecule whole
WHOLEMOLECULES ENTITY0=rna
WRAPAROUND ATOMS=ions AROUND=rna
DUMPATOMS FILE=dump.xyz ATOMS=rna,ions
```

#### (see also WHOLEMOLECULES, GROUP and DUMPATOMS)

In case you want to do it during a simulation and you only care about wrapping the ions in the  $\mathtt{dump}$  .  $\mathtt{xyz}$  file, you can use the following:

```
# add some restraint that do not require molecules to be whole:
a: TORSION ATOMS=1,2,10,11
RESTRAINT ARG=a AT=0.0 KAPPA=5

# then do the things that are required for dumping the trajectory
# notice that they are all done every 100 steps, so as not to
# unnecessarily overload the calculation

rna: GROUP ATOMS=1-100
ions: GROUP ATOMS=101-110
# first make the rna molecule whole
WHOLEMOLECULES ENTITY0=rna STRIDE=100
WRAPAROUND ATOMS=ions AROUND=rna STRIDE=100
DUMPATOMS FILE=dump.xyz ATOMS=rna,ions STRIDE=100
```

## (see also TORSION, GROUP, WHOLEMOLECULES and DUMPATOMS)

Notice that if the biased variable requires a molecule to be whole, you might have to put just the WHOLEMOLEC ULES command before computing that variable and leave the default STRIDE=1.

This command instructs plumed to center all atoms around the center of mass of a solute molecule.

```
solute: GROUP ATOMS=1-100
all: GROUP ATOMS=1-1000
# center of the solute:
# notice that since plumed 2.2 this also works if the
# solute molecule is broken
com: COM ATOMS=solute
# notice that we wrap around a single atom. this should be fast
WRAPAROUND ATOMS=all AROUND=com
DUMPATOMS FILE=dump.xyz ATOMS=all
```

## (see also GROUP COM DUMPATOMS)

Notice that whereas WHOLEMOLECULES is designed to make molecules whole, WRAPAROUND can easily break molecules. In the last example, if solvent (atoms 101-1000) is made e.g. of water, then water molecules could be broken by WRAPAROUND (hydrogen could end up in an image and oxygen in another one). One solution is to use WHOLEMOLECULES on all the water molecules after WRAPAROUND. This is tedious. A better solution is to use the GROUPBY option which is going to consider the atoms listed in ATOMS as a list of groups each of size GROUPBY. The first atom of the group will be brought close to the AROUND atoms. The following atoms of the group will be just brought close to the first atom of the group. Assuming that oxygen is the first atom of each water molecules, in the following examples all the water oxygens will be brought close to the solute, and all the hydrogens will be kept close to their related oxygen.

```
solute: GROUP ATOMS=1-100
water: GROUP ATOMS=101-1000
com: COM ATOMS=solute
# notice that we wrap around a single atom. this should be fast
WRAPAROUND ATOMS=solute AROUND=com
# notice that we wrap around a single atom. this should be fast
WRAPAROUND ATOMS=water AROUND=com GROUPBY=3
DUMPATOMS FILE=dump.xyz ATOMS=solute,water
```

# (see also GROUP COM DUMPATOMS)

5.1.8 RESET\_CELL

This is part of the generic module

This action is used to rotate the full cell

This can be used to modify the periodic box. Notice that this is done at fixed scaled coordinates, so that also atomic coordinates for the entire system are affected. To see what effect try the DUMPATOMS directive to output the atomic positions.

Also notice that PLUMED propagate forces correctly so that you can add a bias on a CV computed after rotation. See also FIT\_TO\_TEMPLATE

Currently, only TYPE=TRIANGULAR is implemented, which allows one to reset the cell to a lower triangular one. Namely, a proper rotation is found that allows rotating the box so that the first lattice vector is in the form (ax,0,0), the second lattice vector is in the form (bx,by,0), and the third lattice vector is arbitrary.

#### Attention

The implementation of this action is available but should be considered in testing phase. Please report any strange behavior.

This directive modifies the stored position at the precise moment it is executed. This means that only collective variables which are below it in the input script will see the corrected positions. Unless you know exactly what you are doing, leave the default stride (1), so that this action is performed at every MD step.

## Compulsory keywords

| STRIDE | ( default=1 ) the frequency with which molecules are reassembled. Unless you are completely certain about what you are doing leave this set equal to 1! |
|--------|---|
| TYPE   | ( default=TRIANGULAR ) the manner in which the cell is reset  |

## **Examples**

Reset cell to be triangular after a rototranslational fit

DUMPATOMS FILE=dump-original.xyz ATOMS=1-20
FIT\_TO\_TEMPLATE STRIDE=1 REFERENCE=ref.pdb TYPE=OPTIMAL
DUMPATOMS FILE=dump-fit.xyz ATOMS=1-20
RESET\_CELL TYPE=TRIANGULAR
DUMPATOMS FILE=dump-reset.xyz ATOMS=1-20

(see also **DUMPATOMS**)

# 5.1.9 CENTER\_OF\_MULTICOLVAR

This is part of the multicolvar module

Calculate a a weighted average position based on the value of some multicolvar.

This action calculates the position of a new virtual atom using the following formula:

$$x_{\alpha} = \frac{1}{2\pi} \arctan \left[ \frac{\sum_{i} w_{i} f_{i} \sin (2\pi x_{i,\alpha})}{\sum_{i} w_{i} f_{i} \cos (2\pi x_{i,\alpha})} \right]$$

Where in this expression the  $w_i$  values are a set of weights calculated within a multicolvar action and the  $f_i$  are the values of the multicolvar functions. The  $x_{i,\alpha}$  values are the positions (in scaled coordinates) associated with each of the multicolvars calculated.

**Bug** The virial contribution for this type of virtual atom is not currently evaluated so do not use in bias functions unless the volume of the cell is fixed

The atoms involved can be specified using

the list of atoms which are involved the virtual atom's definition. For more information on how to specify lists of atoms see Groups and Virtual Atoms

Compulsory keywords

| <b>DATA</b> find the average value for a multicoly | ⁄ar |
|--|-----|
|--|-----|

**Options** 

| COMPONENT | if your input multicolvar is a vector then specify which component you would like to use in |  |
|-----------|---|--|
|           | calculating the weight  |  |
|           |   |  |

**Examples** 

Lets suppose that you are examining the formation of liquid droplets from gas. You may want to determine the center of mass of any of the droplets formed. In doing this calculation you recognise that the atoms in the liquid droplets will have a higher coordination number than those in the surrounding gas. As you want to calculate the position of the droplets you thus recognise that these atoms with high coordination numbers should have a high weight in the weighted average you are using to calculate the position of the droplet. You can thus calculate the position of the droplet using an input like the one shown below:

```
c1: COORDINATIONNUMBER SPECIES=1-512 SWITCH={EXP D_0=4.0 R_0=0.5}
cc: CENTER OF MULTICOLVAR DATA=c1
```

The first line here calclates the coordination numbers of all the atoms in the system. The virtual atom then uses the values of the coordination numbers calculated by the action labelled c1 when it calculates the Berry Phase average described above. (N.B. the  $w_i$  in the above expression are all set equal to 1 in this case)

The above input is fine we can, however, refine this somewhat by making use of a multicolvar transform action as shown below:

```
c1: COORDINATIONNUMBER SPECIES=1-512 SWITCH={EXP D_0=4.0 R_0=0.5}
cf: MTRANSFORM_MORE DATA=c1 SWITCH={RATIONAL D_0=2.0 R_0=0.1} LOWMEM
cc: CENTER_OF_MULTICOLVAR DATA=cf
```

This input once again calculates the coordination numbers of all the atoms in the system. The middle line then transforms these coordinations numbers to numbers between 0 and 1. Essentially any atom with a coordination number larger than 2.0 is given a weight of one and below this value the transformed value decays to zero. It is these transformed coordination numbers that are used to calculate the Berry phase average described in the previous section.

#### 5.1.10 **CENTER**

This is part of the vatom module

Calculate the center for a group of atoms, with arbitrary weights.

The computed center is stored as a virtual atom that can be accessed in an atom list through the label for the CENTER action that creates it. Notice that the generated virtual atom has charge equal to the sum of the charges and mass equal to the sum of the masses. If used with the MASS flag, then it provides a result identical to COM.

When running with periodic boundary conditions, the atoms should be in the proper periodic image. This is done automatically since PLUMED 2.2, by considering the ordered list of atoms and rebuilding PBCs with a procedure that is equivalent to that done in WHOLEMOLECULES. Notice that rebuilding is local to this action. This is different from WHOLEMOLECULES which actually modifies the coordinates stored in PLUMED.

In case you want to recover the old behavior you should use the NOPBC flag. In that case you need to take care that atoms are in the correct periodic image.

The atoms involved can be specified using

| ATOM: | the list of atoms which are involved the virtual atom's definition. For more information on how to |  |
|-------|--|--|
|       | specify lists of atoms see Groups and Virtual Atoms  |  |

#### **Options**

| NOPBC   | PBC (default=off) ignore the periodic boundary conditions when calculating distance |  |
|---------|---|--|
| MASS    | ( default=off ) If set center is mass weighted                                      |  |
| WEIGHTS | Center is computed as a weighted average.   |  |

#### **Examples**

```
\# a point which is on the line connecting atoms 1 and 10, so that its distance \# from 10 is twice its distance from 1: c1: CENTER ATOMS=1,1,10
```

```
# this is another way of stating the same:
clbis: CENTER ATOMS=1,10 WEIGHTS=2,1

# center of mass among these atoms:
c2: CENTER ATOMS=2,3,4,5 MASS
d1: DISTANCE ATOMS=c1,c2

PRINT ARG=d1
```

(See also DISTANCE, COM and PRINT).

## 5.1.11 COM

This is part of the vatom module

Calculate the center of mass for a group of atoms.

The computed center of mass is stored as a virtual atom that can be accessed in an atom list through the label for the COM action that creates it.

For arbitrary weights (e.g. geometric center) see CENTER.

When running with periodic boundary conditions, the atoms should be in the proper periodic image. This is done automatically since PLUMED 2.2, by considering the ordered list of atoms and rebuilding PBCs with a procedure that is equivalent to that done in WHOLEMOLECULES . Notice that rebuilding is local to this action. This is different from WHOLEMOLECULES which actually modifies the coordinates stored in PLUMED.

In case you want to recover the old behavior you should use the NOPBC flag. In that case you need to take care that atoms are in the correct periodic image.

The atoms involved can be specified using

| ATOMS | the list of atoms which are involved the virtual atom's definition. For more info | ormation on how to |
|-------|---|--------------------|
|       | specify lists of atoms see Groups and Virtual Atoms                               |                    |

# **Options**

| NOPBC | ( default=off ) ignore the periodic boundary conditions when calculating distances |
|-------|--|
|       |  |

## **Examples**

The following input instructs plumed to print the distance between the center of mass for atoms 1,2,3,4,5,6,7 and that for atoms 15,20:

COM ATOMS=1-7 LABEL=c1

COM ATOMS=15,20 LABEL=c2
DISTANCE ATOMS=c1,c2 LABEL=d1
PRINT ARG=d1

(See also DISTANCE and PRINT).

## 5.1.12 FIXEDATOM

This is part of the vatom module

Add a virtual atom in a fixed position.

This action creates a virtual atom at a fixed position. The coordinates can be specified in cartesian components (by default) or in scaled coordinats (SCALED\_COMPONENTS). It is also possible to assign a predefined charge or mass to the atom.

## Attention

Similar to POSITION this variable is not invariant for translation of the system. Adding a force on it can create serious troubles.

Notice that the distance between to atoms created using FIXEDATOM is invariant for translation. Additionally, if one first align atoms to a reference using FIT\_TO\_TEMPLATE, then it is safe to add further fixed atoms without breaking translational invariance.

The atoms involved can be specified using

| ATOMS | the list of atoms which are involved the virtual atom's definition. | For more information on how to |
|-------|---|--------------------------------|
|       | specify lists of atoms see Groups and Virtual Atoms                 |                                |

## Compulsory keywords

| AT coordinates of the virtual atom |  |
|------------------------------------|--|
| SET_MASS                           | ( default=1 ) mass of the virtual atom   |
| SET_CHARGE                         | ( default=0 ) charge of the virtual atom |

# **Options**

| SCALED_COMPONENTS | ( default=off ) use scaled components |
|-------------------|---------------------------------------|
|                   |                                       |

# **Examples**

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The following input instructs plumed to compute the angle between distance of atoms 15 and 20 and the z axis and keeping it close to zero.

```
a: FIXEDATOM AT=0,0,0
b: FIXEDATOM AT=0,0,1
an: ANGLE ATOMS=a,b,15,20
RESTRAINT ARG=an AT=0.0 KAPPA=100.0
```

(See also ANGLE and RESTRAINT).

The following input instructs plumed to align a protein on a template and then compute the distance of one of its atom from the point (10,20,30).

```
FIT_TO_TEMPLATE STRIDE=1 REFERENCE=ref.pdb TYPE=SIMPLE
a: FIXEDATOM AT=10,20,30
d: DISTANCE ARG=a,20
PRINT ARG=d FILE=colvar
```

(See also FIT\_TO\_TEMPLATE and DISTANCE).

#### 5.1.13 GHOST

This is part of the vatom module

Calculate the absolute position of a ghost atom with fixed coordinates in the local reference frame formed by three atoms. The computed ghost atom is stored as a virtual atom that can be accessed in an atom list through the the label for the GHOST action that creates it.

The atoms involved can be specified using

| ATOMS       | the list of atoms which are involved the virtual atom's definition. For more information on how to specify lists of atoms see Groups and Virtual Atoms |  |
|-------------|--|--|
| COORDINATES | coordinates of the ghost atom in the local reference frame. For more information on how to specify lists of atoms see Groups and Virtual Atoms         |  |

## **Examples**

The following input instructs plumed to print the distance between the ghost atom and the center of mass for atoms 15,20:

```
GHOST ATOMS=1,5,10 COORDINATES=10.0,10.0,10.0 LABEL=c1
COM ATOMS=15,20 LABEL=c2
DISTANCE ATOMS=c1,c2 LABEL=d1
PRINT ARG=d1
```

(See also DISTANCE and PRINT).

## 5.2 CV Documentation

The following list contains descriptions of a number of the colvars that are currently implemented in PLUMED.

| ALPHABETA             | Measures a distance including pbc between the instantaneous values of a  |
|-----------------------|--|
|                       | set of torsional angles and set of reference values.   |
| ALPHARMSD             | Probe the alpha helical content of a protein structure.  |
| ANGLE                 | Calculate an angle.  |
| ANTIBETARMSD          | Probe the antiparallel beta sheet content of your protein structure.   |
| CELL                  | Calculate the components of the simulation cell  |
| CONSTANT              | Return one or more constant quantitieswith or without derivatives.   |
| CONTACTMAP            | Calculate the distances between a number of pairs of atoms and transform each distance by a switching function. The transformed distance can be compared with a reference value in order to calculate the squared distance tween two contact maps. Each distance can also be weighted for a given value. CONTACTMAP can be used togetherwith FUNCPATHMSD to define a path in the contactmap space. |
| COORDINATION          | Calculate coordination numbers.  |
| CS2BACKBONE           | This collective variable calculates the backbone chemical shifts for a protein.  |
| DHENERGY              | Calculate Debye-Huckel interaction energy among GROUPA and GROUPB.   |
| DIHCOR                | Measures the degree of similarity between dihedral angles.   |
| DIPOLE                | Calculate the dipole moment for a group of atoms.  |
| DISTANCE_FROM_CONTOUR | Calculate the perpendicular distance from a Willard-Chandler dividing surface.   |
| DISTANCE              | Calculate the distance between a pair of atoms.  |
| ENERGY                | Calculate the total energy of the simulation box.  |
| ERMSD                 | Calculate eRMSD with respect to a reference structure.   |
| FAKE                  | This is a fake colvar container used by cltools or various other actions and just support input and period definition  |
| FRET                  | Calculate the FRET efficiency between a pair of atoms. The efficiency is calculated using the Forster relation:  |
| GPROPERTYMAP          | Property maps but with a more flexible framework for the distance metric being used.   |
| GYRATION              | Calculate the radius of gyration, or other properties related to it.   |
| IMPLICIT              |  |
| JCOUPLING             | Calculates $^3J$ coupling constants for a dihedral angle.  |
| NOE                   | Calculates NOE intensities as sums of 1/r^6, also averaging over multiple equivalent atomsor ambiguous NOE.  |
| PARABETARMSD          | Probe the parallel beta sheet content of your protein structure.   |
| PATHMSD               | This Colvar calculates path collective variables.  |
| PATH                  | Path collective variables with a more flexible framework for the distance metric being used.   |
| PCAVARS               | Projection on principal component eigenvectors or other high dimensional linear subspace   |
| POSITION              | Calculate the components of the position of an atom.   |
| PRE                   | Calculates the Paramegnetic Resonance Enhancement intensity ratio between two atoms. The reference atom for the spin label is added with SPI NLABEL, the affected atom(s) are give as numbered GROUPA1, GROUPA2, The additional parameters needed for the calculation are given as INEPT, the inepttime, TAUC the correlation time, OMEGA, the larmor frequency and RTWO for the relaxation time.  |
| PROPERTYMAP           | Calculate generic property maps.   |
| PUCKERING             | Calculate sugar pseudorotation coordinates.  |
| RDC                   | Calculates the (Residual) Dipolar Coupling between two atoms.  |
| TEMPLATE              | This file provides a template for if you want to introduce a new CV.   |
| TORSION               | Calculate a torsional angle.   |
| I                     | ı  |

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| VOLUME | Calculate the volume of the simulation box. |  |
|--------|---|--|
|--------|---|--|

## 5.2.1 ALPHABETA

This is part of the multicolvar module

Measures a distance including pbc between the instantaneous values of a set of torsional angles and set of reference values.

This colvar calculates the following quantity.

$$s = \frac{1}{2} \sum_{i} \left[ 1 + \cos(\phi_i - \phi_i^{\text{Ref}}) \right]$$

where the  $\phi_i$  values are the instantaneous values for the TORSION angles of interest. The  $\phi_i^{Ref}$  values are the user-specified reference values for the torsional angles.

The atoms involved can be specified using

## **ATOMS**

the atoms involved in each of the collective variables you wish to calculate. Keywords like ATOM ← S1, ATOMS2, ATOMS3,... should be listed and one CV will be calculated for each ATOM keyword you specify (all ATOM keywords should define the same number of atoms). The eventual number of quantities calculated by this action will depend on what functions of the distribution you choose to calculate. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3...

Compulsory keywords

| REFERENCE | the reference values for each of the torsional angles. If you use a single REFERENCE value       |
|-----------|--|
|           | the same reference value is used for all torsions You can use multiple instances of this keyword |
|           | i.e. REFERENCE1, REFERENCE2, REFERENCE3  |

**Options** 

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically                |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-             |
|                       | tances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize                          |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation |

#### **Examples**

The following provides an example of the input for an alpha beta similarity.

```
ALPHABETA ...
ATOMS1=168,170,172,188 REFERENCE1=3.14
ATOMS2=170,172,188,190 REFERENCE2=3.14
ATOMS3=188,190,192,230 REFERENCE3=3.14
LABEL=ab
... ALPHABETA
PRINT ARG=ab FILE=colvar STRIDE=10
```

Because all the reference values are the same we can calculate the same quantity using

```
ALPHABETA ...
ATOMS1=168,170,172,188 REFERENCE=3.14
ATOMS2=170,172,188,190
ATOMS3=188,190,192,230
LABEL=ab
... ALPHABETA
PRINT ARG=ab FILE=colvar STRIDE=10
```

Writing out the atoms involved in all the torsions in this way can be rather tedious. Thankfully if you are working with protein you can avoid this by using the MOLINFO command. PLUMED uses the pdb file that you provide to this command to learn about the topology of the protein molecule. This means that you can specify torsion angles using the following syntax:

```
MOLINFO MOLTYPE=protein STRUCTURE=myprotein.pdb
ALPHABETA ...
ATOMS1=@phi-3 REFERENCE=3.14
ATOMS2=@psi-3
ATOMS3=@phi-4
LABEL=ab
... ALPHABETA
PRINT ARG=ab FILE=colvar STRIDE=10
```

Here, @phi-3 tells plumed that you would like to calculate the  $\phi$  angle in the third residue of the protein. Similarly @psi-4 tells plumed that you want to calculate the  $\psi$  angle of the 4th residue of the protein.

## 5.2.2 ALPHARMSD

This is part of the secondarystructure module

Probe the alpha helical content of a protein structure.

Any chain of six contiguous residues in a protein chain can form an alpha helix. This colvar thus generates the set of all possible six residue sections and calculates the RMSD distance between the configuration in which the residues find themselves and an idealized alpha helical structure. These distances can be calculated by either aligning the instantaneous structure with the reference structure and measuring each atomic displacement or by calculating differences between the set of interatomic distances in the reference and instantaneous structures.

This colvar is based on the following reference ?. The authors of this paper use the set of distances from the alpha helix configurations to measure the number of segments that have an alpha helical configuration. This is done by calculating the following sum of functions of the rmsd distances:

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$$s = \sum_i \frac{1 - \left(\frac{r_i - d_0}{r_0}\right)^n}{1 - \left(\frac{r_i - d_0}{r_0}\right)^m}$$

where the sum runs over all possible segments of alpha helix. By default the NN, MM and D\_0 parameters are set equal to those used in ?. The R 0 parameter must be set by the user - the value used in ? was 0.08 nm.

If you change the function in the above sum you can calculate quantities such as the average distance from a purely the alpha helical configuration or the distance between the set of residues that is closest to an alpha helix and the reference configuration. To do these sorts of calculations you can use the AVERAGE and MIN keywords. In addition you can use the LESS\_THAN keyword if you would like to change the form of the switching function. If you use any of these options you no longer need to specify NN, R\_0, MM and D\_0.

Please be aware that for codes like gromacs you must ensure that plumed reconstructs the chains involved in your CV when you calculate this CV using anthing other than TYPE=DRMSD. For more details as to how to do this see WHOLEMOLECULES.

**Description of components** 

By default this Action calculates the number of structural units that are within a certain distance of a idealised secondary structure element. This quantity can then be referenced elsewhere in the input by using the label of the action. However, thes Action can also be used to calculate the following quantities by using the keywords as described below. The quantities then calculated can be referened using the label of the action followed by a dot and then the name from the table below. Please note that you can use the LESS\_THAN keyword more than once. The resulting components will be labelled *label*.lessthan-1, *label*.lessthan-2 and so on unless you exploit the fact that these labels are customizable. In particular, by using the LABEL keyword in the description of you LESS\_THAN function you can set name of the component that you are calculating

| Quantity | Keyword   | Description  |
|----------|-----------|--|
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.   |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action   |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.   |

The atoms involved can be specified using

| RESIDUES | this command is used to specify the set of residues that could conceivably form part of the sec-       |
|----------|--|
|          | ondary structure. It is possible to use residues numbers as the various chains and residues            |
|          | should have been identified else using an instance of the MOLINFO action. If you wish to use all       |
|          | · · · · · · · · · · · · · · · · · · ·  |
|          | the residues from all the chains in your system you can do so by specifying all. Alternatively, if you |
|          | wish to use a subset of the residues you can specify the particular residues you are interested in     |
|          | as a list of numbers. Please be aware that to form secondary structure elements your chain must        |
|          | contain at least N residues, where N is dependent on the particular secondary structure you are        |
|          | interested in. As such if you define portions of the chain with fewer than N residues the code will    |
|          | crash.   |

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# Compulsory keywords

| TYPE | ( default=DRMSD ) the manner in which RMSD alignment is performed. Should be OPTIMAL, SIMPLE |
|------|--|
|      | or DRMSD. For more details on the OPTIMAL and SIMPLE methods see RMSD. For more details on   |
|      | the DRMSD method see DRMSD.  |
| R_0  | The r_0 parameter of the switching function.   |
| D_0  | ( default=0.0 ) The d_0 parameter of the switching function                                  |
| NN   | ( default=8 ) The n parameter of the switching function                                      |
| MM   | ( default=12 ) The m parameter of the switching function                                     |

# **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| VERBOSE               | ( default=off ) write a more detailed output  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize  |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation   |
| LESS_THAN             | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.lessthan</code> . You can use multiple instances of this keyword i.e. <code>LESS_THAN1</code> , <code>LESS_THAN2</code> , <code>LESS_THAN3</code> The corresponding values are then referenced using <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-3</code> |
| MIN                   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3                                |
| ALT_MIN               | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3  |
| LOWEST                | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest   |
| HIGHEST               | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest   |

# **Examples**

The following input calculates the number of six residue segments of protein that are in an alpha helical configuration.

MOLINFO STRUCTURE=helix.pdb ALPHARMSD RESIDUES=all TYPE=DRMSD LESS\_THAN={RATIONAL R\_0=0.08 NN=8 MM=12} LABEL=a

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(see also MOLINFO)

## **5.2.3 ANGLE**

This is part of the colvar module

Calculate an angle.

This command can be used to compute the angle between three atoms. Alternatively if four atoms appear in the atom specification it calculates the angle between two vectors identified by two pairs of atoms.

If three atoms are given, the angle is defined as:

$$\theta = \arccos\left(\frac{\mathbf{r}_{21} \cdot \mathbf{r}_{23}}{|\mathbf{r}_{21}||\mathbf{r}_{23}|}\right)$$

Here  $\mathbf{r}_{ij}$  is the distance vector among the i-th and the j-th listed atom.

If four atoms are given, the angle is defined as:

$$\theta = \arccos\left(\frac{\mathbf{r}_{21} \cdot \mathbf{r}_{34}}{|\mathbf{r}_{21}||\mathbf{r}_{34}|}\right)$$

Notice that angles defined in this way are non-periodic variables and their value is limited by definition between 0 and  $\pi$ .

The vectors  $\mathbf{r}_{ij}$  are by default evaluated taking periodic boundary conditions into account. This behavior can be changed with the NOPBC flag.

The atoms involved can be specified using

| ATOMS | the list of atoms involved in this collective variable (either 3 or 4 atoms). For more information on how |
|-------|---|
|       | to specify lists of atoms see Groups and Virtual Atoms  |

**Options** 

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically         |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances |

**Examples** 

This command tells plumed to calculate the angle between the vector connecting atom 1 to atom 2 and the vector connecting atom 2 to atom 3 and to print it on file COLVAR1. At the same time, the angle between vector connecting atom 1 to atom 2 and the vector connecting atom 3 to atom 4 is printed on file COLVAR2.

```
a: ANGLE ATOMS=1,2,3
# equivalently one could state:
# a: ANGLE ATOMS=1,2,2,3
b: ANGLE ATOMS=1,2,3,4

PRINT ARG=a FILE=COLVAR1
PRINT ARG=b FILE=COLVAR2

(see also PRINT)
```

## 5.2.4 ANTIBETARMSD

This is part of the secondarystructure module

Probe the antiparallel beta sheet content of your protein structure.

Two protein segments containing three continguous residues can form an antiparallel beta sheet. Although if the two segments are part of the same protein chain they must be separated by a minimum of 2 residues to make room for the turn. This colvar thus generates the set of all possible six residue sections that could conceivably form an antiparallel beta sheet and calculates the RMSD distance between the configuration in which the residues find themselves and an idealized antiparallel beta sheet structure. These distances can be calculated by either aligning the instantaneous structure with the reference structure and measuring each atomic displacement or by calculating differences between the set of interatomic distances in the reference and instantaneous structures.

This colvar is based on the following reference ?. The authors of this paper use the set of distances from the anti parallel beta sheet configurations to measure the number of segments that have an configuration that resembles an anti parallel beta sheet. This is done by calculating the following sum of functions of the rmsd distances:

$$s = \sum_{i} \frac{1 - \left(\frac{r_i - d_0}{r_0}\right)^n}{1 - \left(\frac{r_i - d_0}{r_0}\right)^m}$$

where the sum runs over all possible segments of antiparallel beta sheet. By default the NN, MM and D\_0 parameters are set equal to those used in ?. The R\_0 parameter must be set by the user - the value used in ? was 0.08 nm.

If you change the function in the above sum you can calculate quantities such as the average distance from a purely configuration composed of pure anti-parallel beta sheets or the distance between the set of residues that is closest to an anti-parallel beta sheet and the reference configuration. To do these sorts of calculations you can use the AVERAGE and MIN keywords. In addition you can use the LESS\_THAN keyword if you would like to change the form of the switching function. If you use any of these options you no longer need to specify NN, R\_0, MM and D\_0.

Please be aware that for codes like gromacs you must ensure that plumed reconstructs the chains involved in your CV when you calculate this CV using anthing other than TYPE=DRMSD. For more details as to how to do this see WHOLEMOLECULES.

**Description of components** 

By default this Action calculates the number of structural units that are within a certain distance of a idealised secondary structure element. This quantity can then be referenced elsewhere in the input by using the label of the action. However, thes Action can also be used to calculate the following quantities by using the keywords as described below. The quantities then calculated can be referened using the label of the action followed by a dot and then the name from the table below. Please note that you can use the LESS\_THAN keyword more than once. The resulting components will be labelled *label*.lessthan-1, *label*.lessthan-2 and so on unless you exploit the fact that these labels are customizable. In particular, by using the LABEL keyword in the description of you LESS\_THAN function you can set name of the component that you are calculating

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| Quantity | Keyword   | Description  |
|----------|-----------|--|
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description   |
|          |           | of the keyword so as to make it continuous.  |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action   |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the   |
|          |           | formula described in the description of the keyword so as to make it continuous.   |
|          |           | You can calculate this quantity multiple times using different parameters.   |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous. |
|          |           | of the Reyword 30 as to make it continuous.  |

The atoms involved can be specified using

| RESIDUES | this command is used to specify the set of residues that could conceivably form part of the sec-       |
|----------|--|
|          | ondary structure. It is possible to use residues numbers as the various chains and residues            |
|          | should have been identified else using an instance of the MOLINFO action. If you wish to use all       |
|          | the residues from all the chains in your system you can do so by specifying all. Alternatively, if you |
|          | wish to use a subset of the residues you can specify the particular residues you are interested in     |
|          | as a list of numbers. Please be aware that to form secondary structure elements your chain must        |
|          | contain at least N residues, where N is dependent on the particular secondary structure you are        |
|          | interested in. As such if you define portions of the chain with fewer than N residues the code will    |
|          | crash.   |

# Compulsory keywords

| TYPE  | ( default=DRMSD ) the manner in which RMSD alignment is performed. Should be OPTIMAL, S↔  |
|-------|---|
|       | IMPLE or DRMSD. For more details on the OPTIMAL and SIMPLE methods see RMSD. For more   |
|       | details on the DRMSD method see DRMSD.  |
| R_0   | The r_0 parameter of the switching function.  |
| D_0   | ( default=0.0 ) The d_0 parameter of the switching function   |
| NN    | ( default=8 ) The n parameter of the switching function   |
| ММ    | ( default=12 ) The m parameter of the switching function  |
| STYLE | ( default=all ) Antiparallel beta sheets can either form in a single chain or from a pair of chains. If STYLE=all all chain configuration with the appropriate geometry are counted. If STYLE=inter only sheet-like configurations involving two chains are counted, while if STYLE=intra only sheet-like configurations involving a single chain are counted |

# Options

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically                |
|-----------------------|---|
| VERBOSE               | ( default=off ) write a more detailed output  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize                          |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation |

| LESS_THAN      | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_THAN2, LESS_THAN3 The corresponding values are then referenced using <i>label</i> .lessthan-1, <i>label</i> .lessthan-2, <i>label</i> .lessthan-3                                  |
|----------------|--|
| MIN            | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label.</i> min-1, <i>label.</i> min-2, <i>label.</i> min-3 |
| ALT_MIN        | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3               |
| LOWEST         | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST        | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |
| STRANDS_CUTOFF | If in a segment of protein the two strands are further apart then the calculation of the actual RMSD is skipped as the structure is very far from being beta-sheet like. This keyword speeds up the calculation enormously when you are using the LESS_THAN option. However, if you are using some other option, then this cannot be used  |

## Examples

The following input calculates the number of six residue segments of protein that are in an antiparallel beta sheet configuration.

```
MOLINFO STRUCTURE=helix.pdb
ANTIBETARMSD RESIDUES=all TYPE=DRMSD LESS_THAN={RATIONAL R_0=0.08 NN=8 MM=12} LABEL=a
```

(see also MOLINFO)

5.2.5 CELL

This is part of the colvar module

Calculate the components of the simulation cell

**Description of components** 

5.2 CV Documentation 67 By default this Action calculates the following quantities. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Description                         |
|----------|-------------------------------------|
| ax       | the ax component of the cell matrix |
| ay       | the ay component of the cell matrix |
| az       | the az component of the cell matrix |
| bx       | the bx component of the cell matrix |
| by       | the by component of the cell matrix |
| bz       | the bz component of the cell matrix |
| сх       | the cx component of the cell matrix |
| су       | the cy component of the cell matrix |
| CZ       | the cz component of the cell matrix |

#### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically |
|-----------------------|--|
|                       |  |

# **Examples**

The following input tells plumed to print the squared modulo of each of the three lattice vectors

(See also COMBINE and PRINT).

# 5.2.6 CONSTANT

Return one or more constant quantities with or without derivatives.

Useful in combination with functions that takes in input constants or parameters.

**Description of components** 

The names of the components in this action can be customized by the user in the actions input file. However, in addition to these customizable components the following quantities will always be output

| Quantity | Description |
|----------|-------------|
| V        | the # value |

Compulsory keywords

| VALUES | ( default=NAN ) The values of the constants |
|--------|---|
| VALUE  | ( default=NAN ) The value of the constant   |

### **Options**

| NOPBC | ( default=off ) ignore the periodic boundary conditions when calculating distances |
|-------|--|
| NODE← | ( default=off ) Set to TRUE if you want values without derivatives.                |
| RIV   |  |

### **Examples**

The following input instructs plumed to compute the distance between atoms 1 and 2. If this distance is between 1.0 and 2.0, it is printed. If it is lower than 1.0 (larger than 2.0), 1.0 (2.0) is printed

```
cn: CONSTANT VALUES=1.0,2.0
dis: DISTANCE ATOMS=1,2
sss: SORT ARG=cn.v_0,dis,cn.v_1
PRINT ARG=sss.2
```

(See also DISTANCE, SORT, and PRINT).

In case you want to pass a single value you can use VALUE:

```
cn: CONSTANT VALUE=1.0
dis: DISTANCE ATOMS=1
sss: SORT ARG=cn, dis
PRINT ARG=sss.1
```

## 5.2.7 CONTACTMAP

This is part of the colvar module

Calculate the distances between a number of pairs of atoms and transform each distance by a switching function. The transformed distance can be compared with a reference value in order to calculate the squared distance between two contact maps. Each distance can also be weighted for a given value. CONTACTMAP can be used together with FUNCPATHMSD to define a path in the contactmap space.

**Description of components** 

By default the value of the calculated quantity can be referenced elsewhere in the input file by using the label of the action. Alternatively this Action can be used to be used to calculate the following quantities by employing the keywords listed below. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Description   |  |
|----------|---|--|
| contact  | By not using SUM or CMDIST each contact will be stored in a component |  |

The atoms involved can be specified using

| <b>ATOMS</b> | the atoms involved in each of the contacts you wish to calculate. Keywords like ATOMS1, ATOMS2, |
|--------------|---|
|              | ATOMS3, should be listed and one contact will be calculated for each ATOM keyword you specify.  |
|              | You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3                      |

## Compulsory keywords

| SWITCH | The switching functions to use for each of the contacts in your map. You can either specify a global |
|--------|--|
|        | switching function using SWITCH or one switching function for each contact. Details of the various   |
|        | switching functions you can use are provided on switchingfunction. You can use multiple instances    |
|        | of this keyword i.e. SWITCH1, SWITCH2, SWITCH3   |

# **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-  |
|                       | tances   |
| SUM                   | ( default=off ) calculate the sum of all the contacts in the input   |
| CMDIST                | ( default=off ) calculate the distance with respect to the provided reference contant map  |
| SERIAL                | ( default=off ) Perform the calculation in serial - for debug purpose  |
| REFERENCE             | A reference value for a given contact, by default is 0.0 You can either specify a global reference value using REFERENCE or one reference value for each contact. You can use multiple instances of this keyword i.e. REFERENCE1, REFERENCE2, REFERENCE3 |
| WEIGHT                | A weight value for a given contact, by default is 1.0 You can either specify a global weight value using WEIGHT or one weight value for each contact. You can use multiple instances of this keyword i.e. WEIGHT1, WEIGHT2, WEIGHT3                      |

# **Examples**

The following example calculates switching functions based on the distances between atoms 1 and 2, 3 and 4 and 4 and 5. The values of these three switching functions are then output to a file named colvar.

The following example calculates the difference of the current contact map with respect to a reference provided. In this case REFERENCE is the fraction of contact that is formed (i.e. the distance between two atoms transformed with the SWITH), while R\_0 is the contact distance. WEIGHT gives the relative weight of each contact to the final distance measure.

```
CONTACTMAP ...
ATOMS1=1,2 REFERENCE1=0.1 WEIGHT1=0.5
ATOMS2=3,4 REFERENCE2=0.5 WEIGHT2=1.0
ATOMS3=4,5 REFERENCE3=0.25 WEIGHT3=1.0
ATOMS4=5,6 REFERENCE4=0.0 WEIGHT4=0.5
SWITCH={RATIONAL R_0=1.5}
LABEL=cmap
CMDIST
... CONTACTMAP
PRINT ARG=cmap FILE=colvar
```

The next example calculates calculates fraction of native contacts (Q) for Trp-cage mini-protein. R\_0 is the distance at which the switch function is guaranteed to be 1.0 – it doesn't really matter for Q and should be something very small, like 1 A. REF is the reference distance for the contact, e.g. the distance from a crystal structure. LAMBDA is the tolerance for the distance – if set to 1.0, the contact would have to have exactly the reference value to be formed; instead for lambda values of 1.5–1.8 are usually used to allow some slack. BETA is the softness of the switch function, default is 50nm. WEIGHT is the 1/(number of contacts) giving equal weight to each contact.

When using native contact Q switch function, please cite?

```
# Full example available in regtest/basic/rt72/

CONTACTMAP ...

ATOMS1=1,67 SWITCH1={Q R_0=0.01 BETA=50.0 LAMBDA=1.5 REF=0.4059} WEIGHT1=0.003597

ATOMS2=1,68 SWITCH2={Q R_0=0.01 BETA=50.0 LAMBDA=1.5 REF=0.4039} WEIGHT2=0.003597

ATOMS3=1,69 SWITCH3={Q R_0=0.01 BETA=50.0 LAMBDA=1.5 REF=0.3215} WEIGHT3=0.003597

[snip]

ATOMS275=183,213 SWITCH275={Q R_0=0.01 BETA=50.0 LAMBDA=1.5 REF=0.355} WEIGHT275=0.003597

ATOMS276=183,234 SWITCH276={Q R_0=0.01 BETA=50.0 LAMBDA=1.5 REF=0.428} WEIGHT276=0.003597

ATOMS277=183,250 SWITCH277={Q R_0=0.01 BETA=50.0 LAMBDA=1.5 REF=0.3832} WEIGHT277=0.003597

ATOMS278=197,220 SWITCH278={Q R_0=0.01 BETA=50.0 LAMBDA=1.5 REF=0.3822} WEIGHT277=0.003597

LABEL=cmap

SUM

... CONTACTMAP

PRINT ARG=cmap FILE=colvar
```

(See also PRINT and switchingfunction)

### 5.2.8 COORDINATION

This is part of the colvar module

Calculate coordination numbers.

This keyword can be used to calculate the number of contacts between two groups of atoms and is defined as

$$\sum_{i \in A} \sum_{i \in B} s_{ij}$$

where  $s_{ij}$  is 1 if the contact between atoms i and j is formed, zero otherwise. In practise,  $s_{ij}$  is replaced with a

switching function to make it differentiable. The default switching function is:

$$s_{ij} = \frac{1 - \left(\frac{\mathbf{r}_{ij} - d_0}{r_0}\right)^n}{1 - \left(\frac{\mathbf{r}_{ij} - d_0}{r_0}\right)^m}$$

but it can be changed using the optional SWITCH option.

To make your calculation faster you can use a neighbor list, which makes it that only a relevant subset of the pairwise distance are calculated at every step.

If GROUPB is empty, it will sum the  $\frac{N(N-1)}{2}$  pairs in GROUPA. This avoids computing twice permuted indexes (e.g. pair (i,j) and (j,i)) thus running at twice the speed.

Notice that if there are common atoms between GROUPA and GROUPB the switching function should be equal to one. These "self contacts" are discarded by plumed (since version 2.1), so that they actually count as "zero".

The atoms involved can be specified using

| GROUPA | First list of atoms. For more information on how to specify lists of atoms see Groups and Virtual Atoms  |  |
|--------|--|--|
| GROUPB | Second list of atoms (if empty, N*(N-1)/2 pairs in GROUPA are counted). For more information on how to specify lists of atoms see Groups and Virtual Atoms |  |

# Compulsory keywords

| NN | ( default=6 ) The n parameter of the switching function                 |
|----|---|
| MM | ( default=0 ) The m parameter of the switching function; 0 implies 2*NN |
| D← | ( default=0.0 ) The d_0 parameter of the switching function             |
| _0 |   |
| R← | The r_0 parameter of the switching function                             |
| _0 |   |

## **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-  |
|                       | tances   |
| SERIAL                | ( default=off ) Perform the calculation in serial - for debug purpose  |
| PAIR                  | ( default=off ) Pair only 1st element of the 1st group with 1st element in the   |
|                       | second, etc  |
| NLIST                 | ( default=off ) Use a neighbour list to speed up the calculation   |
| NL_CUTOFF             | The cutoff for the neighbour list  |
| NL_STRIDE             | The frequency with which we are updating the atoms in the neighbour list   |
| SWITCH                | This keyword is used if you want to employ an alternative to the continuous swiching function defined above. The following provides information on the switchingfunction that are available. When this keyword is present you no longer need the NN, MM, D_0 and R_0 keywords. |
|                       | Generated by Doxygen   |

#### **Examples**

The following example instructs plumed to calculate the total coordination number of the atoms in group 1-10 with the atoms in group 20-100. For atoms 1-10 coordination numbers are calculated that count the number of atoms from the second group that are within 0.3 nm of the central atom. A neighbour list is used to make this calculation faster, this neighbour list is updated every 100 steps.

```
COORDINATION GROUPA=1-10 GROUPB=20-100 R_0=0.3 NLIST NL_CUTOFF=0.5 NL_STRIDE=100
```

The following is a dummy example which should compute the value 0 because the self interaction of atom 1 is skipped. Notice that in plumed 2.0 "self interactions" were not skipped, and the same calculation should return 1.

```
c: COORDINATION GROUPA=1 GROUPB=1 R_0=0.3
PRINT ARG=c STRIDE=10

c1: COORDINATION GROUPA=1-10 GROUPB=1-10 R_0=0.3
x: COORDINATION GROUPA=1-10 R_0=0.3
c2: COMBINE ARG=x COEFFICIENTS=2
# the two variables c1 and c2 should be identical, but the calculation of c2 is twice faster
# since it runs on half of the pairs. Notice that to get the same result you
# should double it
PRINT ARG=c1,c2 STRIDE=10
```

See also PRINT and COMBINE

# 5.2.9 CS2BACKBONE

This is part of the colvar module

This collective variable calculates the backbone chemical shifts for a protein.

The functional form is that of CamShift? The chemical shifts of the selected nuclei/residues are saved as components. Reference experimental values can also be stored as components. The two components can then be used to calculate either a scoring function as in? , using the keyword CAMSHIFT or to calculate ensemble averages chemical shift per chemical shift as in? (see STATS and ENSEMBLE).

CamShift calculation is relatively heavy because it often uses a large number of atoms, in order to make it faster it is currently parallelised with OpenMP.

As a general rule, when using CS2BACKBONE or other experimental restraints it is better to increase the accuracy of the constraint algorithm due to the increased strain on the bonded structure. In the case of GROMACS it is safer to use lincs-iter=2 and lincs-order=6.

In general the system for which chemical shifts are calculated must be completly included in ATOMS and a TEMP LATE pdb file for the same atoms should be provided as well in the folder DATA. The atoms are made automatically whole unless NOPBC is used, in particular if the system is made of by multiple chains it is usually better to use NOPBC and make the molecule whole WHOLEMOLECULES selecting an appropriate order.

In addition to a pdb file one needs to provide a list of chemical shifts to be calculated using one file per nucleus type (CAshifts.dat, CBshifts.dat, Cshifts.dat, Hshifts.dat, Hshifts.dat, Nshifts.dat), all the six files should always be

present. A chemical shift for a nucleus is calculated if a value greater than 0 is provided. For practical purposes the value can correspond to the experimental value. Residues numbers should go from 1 to N irrespectively of the numbers used in the pdb file. The first and last residue of each chain should be preceded by a # character. Termini groups like ACE or NME should be removed from the PDB.

```
CAshifts.dat:
#1 0.0
2 55.5
3 58.4
.
.
#last 0.0
#last+1 (first) of second chain
.
#last of second chain
```

The default behaviour is to store the values for the active nuclei in components (ca\_#, cb\_#, co\_#, ha\_#, hn\_#, nh\_# and expca\_#, expcb\_#, expco\_#, expha\_#, exphn\_#, exp\_nh#) with NOEXP it is possible to only store the backcalculated values.

A pdb file is needed to the generate a simple topology of the protein. For histidines in protonation states different from D the HIE/HSE HIP/HSP name should be used. GLH and ASH can be used for the alternative protonation of GLU and ASP. Non-standard amino acids and other molecules are not yet supported, but in principle they can be named UNK. If multiple chains are present the chain identifier must be in the standard PDB format, together with the TER keyword at the end of each chain.

One more standard file is also needed in the folder DATA: camshift.db. This file includes all the CamShift parameters and can be found in regtest/basic/rt45/data/ .

All the above files must be in a single folder that must be specified with the keyword DATA.

Additional material and examples can be also found in the tutorial Belfast tutorial: NMR restraints

**Description of components** 

The names of the components in this action can be customized by the user in the actions input file. However, in addition to these customizable components the following quantities will always be output

| Quantity | Description                                  |
|----------|--|
| ha       | the calculated Ha hydrogen chemical shifts   |
| hn       | the calculated H hydrogen chemical shifts    |
| nh       | the calculated N nitrogen chemical shifts    |
| ca       | the calculated Ca carbon chemical shifts     |
| cb       | the calculated Cb carbon chemical shifts     |
| СО       | the calculated C' carbon chemical shifts     |
| expha    | the experimental Ha hydrogen chemical shifts |
| exphn    | the experimental H hydrogen chemical shifts  |
| expnh    | the experimental N nitrogen chemical shifts  |
| ехрса    | the experimental Ca carbon chemical shifts   |
| expcb    | the experimental Cb carbon chemical shifts   |
| expco    | the experimental C' carbon chemical shifts   |

The atoms involved can be specified using

| ATOMS | The atoms to be included in the calculation, e.g. the whole protein. For more information on how to |  |
|-------|---|--|
|       | specify lists of atoms see Groups and Virtual Atoms   |  |

### Compulsory keywords

| DATA  | ( default=data/ ) The folder with the experimental chemical shifts.             |
|---|---|
| TEMPLATE  | ( default=template.pdb ) A PDB file of the protein system to initialise ALMOST. |
| NEIGH_FREQ ( default=20 ) Period in step for neighbour list update. |   |
| NRES  | Number of residues, corresponding to the number of chemical shifts.             |

#### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically                           |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-                        |
|                       | tances   |
| CAMSHIFT              | ( default=off ) Set to TRUE if you to calculate a single CamShift score.                             |
| NOEXP                 | ( default=off ) Set to TRUE if you don't want to have fixed components with the experimetnal values. |

### **Examples**

In this first example the chemical shifts are used to calculate a scoring function to be used in NMR driven Metadynamics ? :

```
whole: GROUP ATOMS=2612-2514:-1,961-1:-1,2466-962:-1,2513-2467:-1
WHOLEMOLECULES ENTITYO=whole
cs: CS2BACKBONE ATOMS=1-2612 NRES=176 DATA=../data/ TEMPLATE=template.pdb CAMSHIFT NOPBC
metad: METAD ARG=cs HEIGHT=0.5 SIGMA=0.1 PACE=200 BIASFACTOR=10
PRINT ARG=cs,metad.bias FILE=COLVAR STRIDE=100
```

In this second example the chemical shifts are used as replica-averaged restrained as in ? ?.

```
cs: CS2BACKBONE ATOMS=1-174 DATA=data/ NRES=13
encs: ENSEMBLE ARG=(cs\.hn_.*), (cs\.nh_.*)
stcs: STATS ARG=encs.* SQDEVSUM PARARG=(cs\.exphn_.*), (cs\.expnh_.*)
RESTRAINT ARG=stcs.sqdevsum AT=0 KAPPA=0 SLOPE=24
PRINT ARG=(cs\.hn_.*), (cs\.nh_.*) FILE=RESTRAINT STRIDE=100
```

(See also WHOLEMOLECULES, STATS, METAD, RESTRAINT and PRINT)

## 5.2.10 DHENERGY

This is part of the colvar module

Calculate Debye-Huckel interaction energy among GROUPA and GROUPB.

This variable calculates the electrostatic interaction among GROUPA and GROUPB using a Debye-Huckel approximation defined as

$$\frac{1}{4\pi\epsilon_r\epsilon_0} \sum_{i \in A} \sum_{j \in B} q_i q_j \frac{e^{-\kappa|\mathbf{r}_{ij}|}}{|\mathbf{r}_{ij}|}$$

This collective variable can be used to analyze or induce electrostatically driven reactions ?. Notice that the value of the DHENERGY is returned in plumed units (see UNITS).

If GROUPB is empty, it will sum the N\*(N-1)/2 pairs in GROUPA. This avoids computing twice permuted indexes (e.g. pair (i,j) and (j,i)) thus running at twice the speed.

Notice that if there are common atoms between GROUPA and GROUPB their interaction is discarded.

The atoms involved can be specified using

| GROUPA | First list of atoms. For more information on how to specify lists of atoms see Groups and Virtual Atoms  |
|--------|--|
| GROUPB | Second list of atoms (if empty, N*(N-1)/2 pairs in GROUPA are counted). For more information on how to specify lists of atoms see Groups and Virtual Atoms |

# Compulsory keywords

| I       | ( default=1.0 ) Ionic strength (M)              |
|---------|---|
| TEMP    | ( default=300.0 ) Simulation temperature (K)    |
| EPSILON | ( default=80.0 ) Dielectric constant of solvent |

# **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically                 |  |
|-----------------------|--|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-              |  |
|                       | tances   |  |
| SERIAL                | ( default=off ) Perform the calculation in serial - for debug purpose                      |  |
| PAIR                  | ( default=off ) Pair only 1st element of the 1st group with 1st element in the second, etc |  |
| NLIST                 | ( default=off ) Use a neighbour list to speed up the calculation                           |  |
| NL_CUTOFF             | The cutoff for the neighbour list  |  |
| NL_STRIDE             | The frequency with which we are updating the atoms in the neighbour list                   |  |

## **Examples**

# this is printing the electrostatic interaction between two groups of atoms
dh: DHENERGY GROUPA=1-10 GROUPB=11-20 EPSILON=80.0 I=0.1 TEMP=300.0
PRINT ARG=dh
(see also PRINT)

## 5.2.11 DIHCOR

This is part of the multicolvar module

Measures the degree of similarity between dihedral angles.

This colvar calculates the following quantity.

$$s = \frac{1}{2} \sum_{i} \left[ 1 + \cos(\phi_i - \psi_i) \right]$$

where the  $\phi_i$  and  $\psi$  values and the instantaneous values for the TORSION angles of interest.

The atoms involved can be specified using

| ATOMS | the atoms involved in each of the collective variables you wish to calculate. Keywords like ATOM←       |
|-------|---|
|       | S1, ATOMS2, ATOMS3, should be listed and one CV will be calculated for each ATOM keyword                |
|       | you specify (all ATOM keywords should define the same number of atoms). The eventual number             |
|       | of quantities calculated by this action will depend on what functions of the distribution you choose to |
|       | calculate. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3                   |

**Options** 

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically                |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-             |
|                       | tances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize                          |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation |

# **Examples**

The following provides an example input for the dihcor action

DIHCOR ...

```
ATOMS1=1,2,3,4,5,6,7,8

ATOMS2=5,6,7,8,9,10,11,12

LABEL=dih

... DIHCOR

PRINT ARG=dih FILE=colvar STRIDE=10
```

In the above input we are calculating the correction between the torsion angle involving atoms 1, 2, 3 and 4 and the torsion angle involving atoms 5, 6, 7 and 8. This is then added to the correlation between the torsion angle involving atoms 5, 6, 7 and 8 and the correlation angle involving atoms 9, 10, 11 and 12.

Writing out the atoms involved in all the torsions in this way can be rather tedious. Thankfully if you are working with protein you can avoid this by using the MOLINFO command. PLUMED uses the pdb file that you provide to this command to learn about the topology of the protein molecule. This means that you can specify torsion angles using the following syntax:

```
MOLINFO MOLTYPE=protein STRUCTURE=myprotein.pdb
DIHCOR ...
ATOMS1=@phi-3,@psi-3
ATOMS2=@psi-3,@phi-4
ATOMS4=@phi-4,@psi-4
... DIHCOR
PRINT ARG=dih FILE=colvar STRIDE=10
```

Here, @phi-3 tells plumed that you would like to calculate the  $\phi$  angle in the third residue of the protein. Similarly @psi-4 tells plumed that you want to calculate the  $\psi$  angle of the 4th residue of the protein.

### 5.2.12 **DIPOLE**

This is part of the colvar module

Calculate the dipole moment for a group of atoms.

**Description of components** 

By default the value of the calculated quantity can be referenced elsewhere in the input file by using the label of the action. Alternatively this Action can be used to be used to calculate the following quantities by employing the keywords listed below. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Keyword    | Description                   |
|----------|------------|-------------------------------|
| X        | COMPONENTS | the x-component of the dipole |
| у        | COMPONENTS | the y-component of the dipole |
| Z        | COMPONENTS | the z-component of the dipole |

The atoms involved can be specified using

the group of atoms we are calculating the dipole moment for. For more information on how to specify lists of atoms see Groups and Virtual Atoms

#### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| COMPONENTS            | ( default=off ) calculate the x, y and z components of the dipole separately and store them as label.x, label.y and label.z |

### **Examples**

The following tells plumed to calculate the dipole of the group of atoms containing the atoms from 1-10 and print it every 5 steps

```
d: DIPOLE GROUP=1-10
PRINT FILE=output STRIDE=5 ARG=5
(see also PRINT)
```

#### Attention

If the total charge Q of the group in non zero, then a charge Q/N will be subtracted to every atom, where N is the number of atoms. This implies that the dipole (which for a charged system depends on the position) is computed on the geometric center of the group.

## 5.2.13 DISTANCE FROM CONTOUR

This is part of the multicolvar module

Calculate the perpendicular distance from a Willard-Chandler dividing surface.

Suppose that you have calculated a multicolvar. By doing so you have calculated a set of colvars,  $s_i$ , and each of these colvars has a well defined position in space  $(x_i, y_i, z_i)$ . You can use this information to calculate a phase-field model of the colvar density using:

$$p(x, y, x) = \sum_{i} s_{i} K\left[\frac{x - x_{i}}{\sigma_{x}}, \frac{y - y_{i}}{\sigma_{y}}, \frac{z - z_{i}}{\sigma_{z}}\right]$$

In this expression  $\sigma_x, \sigma_y$  and  $\sigma_z$  are bandwidth parameters and K is one of the kernelfunctions. This is what is done within MULTICOLVARDENS

The Willard-Chandler surface is a surface of constant density in the above phase field p(x, y, z). In other words, it is a set of points, (x', y', z'), in your box which have:

$$p(x', y', z') = \rho$$

where  $\rho$  is some target density. This action caculates the distance projected on the x,y or z axis between the position of some test particle and this surface of constant field density.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity  | Description   |
|-----------|---|
| dist      | the distance between the reference atom and the contour                   |
| thickness | the distance between the two contours on the line from the reference atom |

In addition the following quantities can be calculated by employing the keywords listed below

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| gradient | GRADIENT  | the gradient  |
| vmean    | VMEAN     | the norm of the mean vector. The output component can be refererred to elsewhere in the input file by using the label.vmean   |
| vsum     | VSUM      | the norm of sum of vectors. The output component can be refererred to elsewhere in the input file by using the label.vsum   |
| spath    | SPATH     | the position on the path  |
| gspath   | GPATH     | the position on the path calculated using trigonometry  |
| gzpath   | GPATH     | the distance from the path calculated using trigonometry  |
| zpath    | ZPATH     | the distance from the path  |
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| sum      | SUM       | the sum of values   |

The atoms involved can be specified using

| ATOM | The atom whose perpendicular distance we are calculating from the contour. For more information on |  |
|------|--|--|
|      | how to specify lists of atoms see Groups and Virtual Atoms   |  |

## Compulsory keywords

| DATA      | The input base multicolvar which is being used to calculate the contour  |
|-----------|--|
| BANDWIDTH | the bandwidths for kernel density esimtation   |
| KERNEL    | ( default=gaussian ) the kernel function you are using. More details on the kernels available in plumed plumed can be found in kernelfunctions.  |
| DIR       | the direction perpendicular to the contour that you are looking for  |
| CONTOUR   | the value we would like for the contour  |
| TOLERANCE | ( default=0.1 ) this parameter is used to manage periodic boundary conditions. The problem here is that we can be between contours even when we are not within the membrane because of periodic boundary conditions. When we are in the contour, however, we should have it so that the sums of the absoluate values of the distances to the two contours is approximately the distance between the two contours. There can be numerical errors in these calculations, however, so we specify a small tolerance here |

## **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically                |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-             |
|                       | tances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize                          |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation |

# **Examples**

In this example atoms 2-100 are assumed to be concentraed along some part of the z axis so that you an interface between a liquid/solid and the vapour. The quantity dc measures the distance between the surface at which the density of 2-100 atoms is equal to 0.2 and the position of the test particle atom 1.

```
dens: DENSITY SPECIES=2-100
dc: DISTANCE_FROM_CONTOUR DATA=dens ATOM=1 BANDWIDTH=0.5,0.5,0.5 DIR=z CONTOUR=0.2
```

## 5.2.14 DISTANCE

This is part of the colvar module

Calculate the distance between a pair of atoms.

By default the distance is computed taking into account periodic boundary conditions. This behavior can be changed with the NOPBC flag. Moreover, single components in cartesian space (x,y, and z, with COMPONENTS) or single components projected to the three lattice vectors (a,b, and c, with SCALED\_COMPONENTS) can be also computed.

Notice that Cartesian components will not have the proper periodicity! If you have to study e.g. the permeation of a molecule across a membrane, better to use SCALED\_COMPONENTS.

**Description of components** 

By default the value of the calculated quantity can be referenced elsewhere in the input file by using the label of the action. Alternatively this Action can be used to be used to calculate the following quantities by employing the keywords listed below. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Keyword           | Description   |
|----------|-------------------|---|
| x        | COMPONENTS        | the x-component of the vector connecting the two atoms  |
| у        | COMPONENTS        | the y-component of the vector connecting the two atoms  |
| Z        | COMPONENTS        | the z-component of the vector connecting the two atoms  |
| а        | SCALED_COMPONENTS | the normalized projection on the first lattice vector of the vector connecting the two atoms  |
| b        | SCALED_COMPONENTS | the normalized projection on the second lattice vector of the vector connecting the two atoms |
| С        | SCALED_COMPONENTS | the normalized projection on the third lattice vector of the vector connecting the two atoms  |

The atoms involved can be specified using

| ATOMS | the pair of atom that we are calculating the distance between. For more information on how to specify | 1 |
|-------|---|---|
|       | lists of atoms see Groups and Virtual Atoms   |   |

## **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-  |
|                       | tances   |
| COMPONENTS            | ( $default=off$ ) calculate the x, y and z components of the distance separately and store them as label.x, label.y and label.z      |
| SCALED_COMPONENTS     | ( default=off ) calculate the a, b and c scaled components of the distance separately and store them as label.a, label.b and label.c |

# **Examples**

The following input tells plumed to print the distance between atoms 3 and 5, the distance between atoms 2 and 4 and the x component of the distance between atoms 2 and 4.

```
d1: DISTANCE ATOMS=3,5
d2: DISTANCE ATOMS=2,4
d2c: DISTANCE ATOMS=2,4 COMPONENTS
PRINT ARG=d1,d2,d2c.x
```

(See also PRINT).

The following input computes the end-to-end distance for a polymer of 100 atoms and keeps it at a value around 5.

```
WHOLEMOLECULES ENTITY0=1-100
e2e: DISTANCE ATOMS=1,100 NOPBC
RESTRAINT ARG=e2e KAPPA=1 AT=5
```

(See also WHOLEMOLECULES and RESTRAINT).

Notice that NOPBC is used to be sure that if the end-to-end distance is larger than half the simulation box the distance is compute properly. Also notice that, since many MD codes break molecules across cell boundary, it might be necessary to use the WHOLEMOLECULES keyword (also notice that it should be *before* distance). The list of atoms provided to WHOLEMOLECULES here contains all the atoms between 1 and 100. Strictly speaking, this is not necessary. If you know for sure that atoms with difference in the index say equal to 10 are *not* going to be farther than half cell you can e.g. use

```
WHOLEMOLECULES ENTITY0=1,10,20,30,40,50,60,70,80,90,100 e2e: DISTANCE ATOMS=1,100 NOPBC RESTRAINT ARG=e2e KAPPA=1 AT=5
```

Just be sure that the ordered list provide to WHOLEMOLECULES has the following properties:

- · Consecutive atoms should be closer than half-cell throughout the entire simulation.
- · Atoms required later for the distance (e.g. 1 and 100) should be included in the list

The following example shows how to take into account periodicity e.g. in z-component of a distance

```
# this is a center of mass of a large group
c: COM ATOMS=1-100
# this is the distance between atom 101 and the group
d: DISTANCE ATOMS=c,101 COMPONENTS
# this makes a new variable, dd, equal to d and periodic, with domain -10,10
# this is the right choise if e.g. the cell is orthorombic and its size in
# z direction is 20.
dz: COMBINE ARG=d.z PERIODIC=-10,10
# metadynamics on dd
METAD ARG=dz SIGMA=0.1 HEIGHT=0.1 PACE=200
```

(see also COM, COMBINE, and METAD)

Using SCALED\_COMPONENTS this problem should not arise because they are always periodic with domain (-0. ← 5,+0.5).

#### **5.2.15 ENERGY**

This is part of the colvar module

Calculate the total energy of the simulation box.

Total energy can be biased with umbrella sampling? or with well tempered metadynamics?.

Notice that this CV could be unavailable with some MD code. When it is available, and when also replica exchange is available, metadynamics applied to ENERGY can be used to decrease the number of required replicas.

**Bug** Acceptance for replica exchange when **ENERGY** is biased is computed correctly only of all the replicas has the same potential energy function. This is for instance not true when using GROMACS with lambda replica exchange of with plumed-hrex branch.

#### **Examples**

The following input instructs plumed to print the energy of the system

```
ENERGY LABEL=ene
PRINT ARG=ene
```

(See also PRINT).

#### 5.2.16 ERMSD

This is part of the colvar module

Calculate eRMSD with respect to a reference structure.

eRMSD is a metric developed for measuring distances between three-dimensional RNA structures. The standard RMSD measure is highly inaccurate when measuring distances among three-dimensional structures of nucleic acids. It is not unusual, for example, that two RNA structures with low RMSD (i.e. less than 0.4nm) display a completely different network of base-base interactions.

eRMSD measures the distance between structures by considering only the relative positions and orientations of nucleobases. The eRMSD can be considered as a vectorial version of contact maps and it is calculated as follows:

- 1. Set up a local reference system in the center of the six-membered ring of each nucleobase in a molecule. The xy plane lies on the plane of the nucleobase, and it is oriented such that the Watson-Crick interaction is always at  $\theta \approx 60^{\circ}$ .
- 2. Calculate all pairwise distance vectors  $\vec{r}_{i,j}$  among base centers.
- 3. Rescale distance vectors as  $\vec{r}_{i,j} = (r_x/a, r_y/a, r_z/b)$ , where a = b = 5, c = 3. This rescaling has the effect of weighting more deviations on the z-axis with respect to the x/y directions.
- 4. Calculate the G vectors

$$\vec{G}(\tilde{\vec{r}}) = (\sin(\gamma \tilde{r}) \tilde{r}_x / \tilde{r}, \sin(\gamma \tilde{r}) \tilde{r}_y / \tilde{r}, \sin(\gamma \tilde{r}) \tilde{r}_z / \tilde{r}, 1 + \cos(\gamma \tilde{r})) \times \Theta(\tilde{r}_{cutoff} - \tilde{r})$$

Here,  $\gamma = \pi/\tilde{r}_{cutoff}$  and  $\Theta$  is the Heaviside step function. The default cutoff is set to 2.4.

1. The eRMSD between two structures  $\alpha$  and  $\beta$  reads

$$eRMSD = \sqrt{\frac{1}{N} \sum_{j,k} |\vec{G}(\tilde{\vec{r}}_{jk}^{\alpha}) - \vec{G}(\tilde{\vec{r}}_{jk}^{\beta})|^2}$$

Using the default cutoff, two structures with eRMSD of 0.7 or lower can be considered as significantly similar. A full description of the eRMSD can be found in ?

### Warning

Notice that the ERMSD implemented here is not integrated with the other metrics in plumed. As a consequence, it is not (yet) possible to e.g. build path collective variables using ERMSD

Notice that ERMSD expect a single molecule and makes coordinate whole before anything else. As such, results might be unexpected for a multi molecular system.

The atoms involved can be specified using

| ATOMS | the list of atoms (use lcs). For more information on how to specify lists of atoms see Groups and |
|-------|---|
|       | Virtual Atoms   |

## Compulsory keywords

| REFERENCE | a file in pdb format containing the reference structure and the atoms involved in the CV. |
|-----------|---|
| CUTOFF    | ( default=2.4 ) only pairs of atoms closer than CUTOFF are considered in the calculation. |

## **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically         |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances |
| PAIRS                 | List of pairs considered. All pairs are considered if this value is not specified. |

## **Examples**

Calculate the eRMSD from reference structure reference.pdb using the default cutoff (2.4). The list of residues involved in the calculation has to be specified. In this example, the eRMSD is calculated considering residues 1,2,3,4,5,6.

eRMSD1: ERMSD REFERENCE=reference.pdb ATOMS=@lcs-1,@lcs-2,@lcs-3,@lcs-4,@lcs-5,@lcs-6

### 5.2.17 FAKE

This is part of the colvar module

This is a fake colvar container used by cltools or various other actions and just support input and period definition

The atoms involved can be specified using

| ATOMS | the fake atom index, a number is enough. For more information on how to specify lists of atoms see | 1 |
|-------|--|---|
|       | Groups and Virtual Atoms   |   |

## Compulsory keywords

| PERIODIC | if the output of your function is periodic then you should specify the periodicity of the func- |
|----------|---|
|          | tion. If the output is not periodic you must state this using PERIODIC=NO,NO (one for the       |
|          | lower and the other for the upper boundary). For multicomponents then it is PERIOD←             |
|          | IC=mincomp1,maxcomp1,mincomp2,maxcomp2 etc  |

# **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically                             |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances                     |
| COMPONENTS            | additional componnets that this variable is supposed to have. Periodicity is ruled by PERIODIC keyword |

# **Examples**

```
FAKE ATOMS=1 PERIODIC=-3.14,3.14 LABEL=d2
```

(See also PRINT).

# 5.2.18 FRET

This is part of the colvar module

Calculate the FRET efficiency between a pair of atoms. The efficiency is calculated using the Forster relation:

$$E = \frac{1}{1 + (R/R_0)^6}$$

where  $\ensuremath{\ensuremath{R}}$  is the distance and  $\ensuremath{\ensuremath{R}}_0$  is the Forster radius.

By default the distance is computed taking into account periodic boundary conditions. This behavior can be changed with the NOPBC flag.

The atoms involved can be specified using

| ATOMS | the pair of atom that we are calculating the distance between. For more information on how to specify |
|-------|---|
|       | lists of atoms see Groups and Virtual Atoms   |

Compulsory keywords

**R0** The value of the Forster radius.

**Options** 

| NUMERICAL_DERIVATIVES (default=off) calculate the derivatives for these quantities numerically |  |
|--|--|
| NOPBC  | ( default=off ) ignore the periodic boundary conditions when calculating distances |

### **Examples**

The following input tells plumed to print the FRET efficiencies calculated as a function of the distance between atoms 3 and 5 and the distance between atoms 2 and 4.

```
fel: FRET ATOMS=3,5 R0=5.5
fe2: FRET ATOMS=2,4 R0=5.5
PRINT ARG=fe1,fe2
```

#### (See also PRINT).

The following input computes the FRET efficiency calculated on the terminal atoms of a polymer of 100 atoms and keeps it at a value around 0.5.

```
WHOLEMOLECULES ENTITY0=1-100
fe: FRET ATOMS=1,100 R0=5.5 NOPBC
RESTRAINT ARG=fe KAPPA=100 AT=0.5
```

## (See also WHOLEMOLECULES and RESTRAINT).

Notice that NOPBC is used to be sure that if the distance is larger than half the simulation box the distance is compute properly. Also notice that, since many MD codes break molecules across cell boundary, it might be necessary to use the WHOLEMOLECULES keyword (also notice that it should be *before* FRET). Just be sure that the ordered list provide to WHOLEMOLECULES has the following properties:

- Consecutive atoms should be closer than half-cell throughout the entire simulation.
- · Atoms required later for the distance (e.g. 1 and 100) should be included in the list

# 5.2.19 GPROPERTYMAP

This is part of the mapping module

Property maps but with a more flexible framework for the distance metric being used.

This colvar calculates a property map using the formalism developed by Spiwork  $\mathbf{?}$ . In essence if you have the value of some property,  $X_i$ , that it takes at a set of high-dimensional positions then you calculate the value of the property at some arbitrary point in the high-dimensional space using:

$$X = \frac{\sum_{i} X_{i} * \exp(-\lambda D_{i}(x))}{\sum_{i} \exp(-\lambda D_{i}(x))}$$

Within PLUMED there are multiple ways to define the distance from a high-dimensional configuration,  $D_i$ . You could calculate the RMSD distance or you could calculate the ammount by which a set of collective variables change. As such this implementation of the propertymap allows one to use all the different distance metric that are discussed in Distances from reference configurations. This is as opposed to the alternative implementation PROPERTYMAP which is a bit faster but which only allows one to use the RMSD distance.

### Compulsory keywords

| REFERENCE | a pdb file containing the set of reference configurations  |  |
|-----------|--|--|
| PROPERTY  | the property to be used in the index. This should be in the REMARK of the reference  |  |
| TYPE      | ( default=OPTIMAL-FAST ) the manner in which distances are calculated. More information on<br>the different metrics that are available in PLUMED can be found in the section of the manual on<br>Distances from reference configurations |  |
| LAMBDA    | ( default=0 ) the value of the lambda parameter for paths  |  |

#### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically                |  |
|-----------------------|---|--|
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize                          |  |
| LOWMEM                | ( default=off ) lower the memory requirements   |  |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation |  |
| DISABLE_CHECKS        | ( default=off ) disable checks on reference input structures.                             |  |
| NOZPATH               | ( default=off ) do not calculate the zpath position                                       |  |
| NOMAPPING             | ( default=off ) do not calculate the position on the manifold                             |  |

# **Examples**

### 5.2.20 GYRATION

This is part of the colvar module

Calculate the radius of gyration, or other properties related to it.

The different properties can be calculated and selected by the TYPE keyword: the Radius of Gyration (RADIUS); the Trace of the Gyration Tensor (TRACE); the Largest Principal Moment of the Gyration Tensor (GTPC\_1); the middle Principal Moment of the Gyration Tensor (GTPC\_2); the Smallest Principal Moment of the Gyration Tensor (GTPC\_3); the Asphericiry (ASPHERICITY); the Acylindricity (ACYLINDRICITY); the Relative Shape Anisotropy (KAPPA2); the Smallest Principal Radius Of Gyration (GYRATION\_3); the Middle Principal Radius of Gyration (G← YRATION\_2); the Largest Principal Radius of Gyration (GYRATION\_1). A derivation of all these different variants can be found in ?

The radius of gyration is calculated using:

$$s_{\text{Gyr}} = \left(\frac{\sum_{i=1}^{n} m_i |r_i - r_{\text{COM}}|^2}{\sum_{i=1}^{n} m_i}\right)^{1/2}$$

with the position of the center of mass  $r_{\rm COM}$  given by:

$$r_{\text{COM}} = \frac{\sum_{i=1}^{n} r_i \ m_i}{\sum_{i=1}^{n} m_i}$$

The radius of gyration usually makes sense when atoms used for the calculation are all part of the same molecule. When running with periodic boundary conditions, the atoms should be in the proper periodic image. This is done automatically since PLUMED 2.2, by considering the ordered list of atoms and rebuilding PBCs with a procedure that is equivalent to that done in WHOLEMOLECULES. Notice that rebuilding is local to this action. This is different from WHOLEMOLECULES which actually modifies the coordinates stored in PLUMED.

In case you want to recover the old behavior you should use the NOPBC flag. In that case you need to take care that atoms are in the correct periodic image.

The atoms involved can be specified using

| ATOMS | the group of atoms that you are calculating the Gyration Tensor for. For more information on how to |
|-------|---|
|       | specify lists of atoms see Groups and Virtual Atoms   |

Compulsory keywords

| TYPE | ( default=RADIUS ) The type of calculation relative to the Gyration Tensor you want to perform |
|------|--|
|------|--|

**Options** 

| NUMERICAL_DERIVATIVES (default=off) calculate the derivatives for these quantities numerically |  |
|--|--|
| NOPBC ( default=off ) ignore the periodic boundary conditions when calculating distant         |  |
| MASS_WEIGHTED  | ( default=off ) set the masses of all the atoms equal to one |

**Examples** 

The following input tells plumed to print the radius of gyration of the chain containing atoms 10 to 20.

```
WHOLEMOLECULES ENTITY0=10-20
GYRATION TYPE=RADIUS ATOMS=10-20 LABEL=rg
PRINT ARG=rg STRIDE=1 FILE=colvar
```

(See also PRINT)

### **5.2.21 IMPLICIT**

This is part of the colvar module

Calculate EEF1-SB solvation free energy for a group of atoms.

EEF1-SB is a solvent-accessible surface area based model, where the free energy of solvation is computed using a pairwise interaction term for non-hydrogen atoms:

$$\Delta G_i^{\rm solv} = \Delta G_i^{\rm ref} - \sum_{j \neq i} f_i(r_{ij}) V_j$$

where  $\Delta G_i^{
m solv}$  is the free energy of solvation,  $\Delta G_i^{
m ref}$  is the reference solvation free energy,  $V_j$  is the volume of atom j and

$$f_i(r)4\pi r^2 = \frac{2}{\sqrt{\pi}} \frac{\Delta G_i^{\text{free}}}{\lambda_i} \exp\left\{-\frac{(r-R_i)^2}{\lambda_i^2}\right\}$$

where  $\Delta G_i^{\text{free}}$  is the solvation free energy of the isolated group,  $\lambda_i$  is the correlation length equal to the width of the first solvation shell and  $R_i$  is the van der Waals radius of atom i.

The output from this collective variable, the free energy of solvation, can be used with the BIASVALUE keyword to provide implicit solvation to a system. All parameters are designed to be used with a modified CHARMM36 force field. It takes only non-hydrogen atoms as input, these can be conveniently specified using the GROUP action with the NDX\_GROUP parameter. To speed up the calculation, IMPLICIT internally uses a neighbourlist with a cutoff dependent on the type of atom (maximum of 1.95 nm). This cutoff can be extended further by using the NL BUFFER keyword.

#### **Examples**

```
MOLINFO MOLTYPE=protein STRUCTURE=peptide.pdb
WHOLEMOLECULES ENTITY0=1-111

# This allows us to select only non-hydrogen atoms
protein-h: GROUP NDX_FILE=index.ndx NDX_GROUP=Protein-H

# We extend the cutoff by 0.2 nm and update the neighbourlist every 10 steps
solv: IMPLICIT ATOMS=protein-h NL_STRIDE=10 NL_BUFFER=0.2

# Here we actually add our calculated energy back to the potential
bias: BIASVALUE ARG=solv

PRINT ARG=solv FILE=SOLV

(see also PRINT, GROUP, MOLINFO, WHOLEMOLECULES)
```

## 5.2.22 JCOUPLING

This is part of the colvar module

Calculates  $^3J$  coupling constants for a dihedral angle.

The J-coupling between two atoms is given by the Karplus relation:

$$^{3}J(\theta) = A\cos^{2}(\theta + \Delta\theta) + B\cos(\theta + \Delta\theta) + C$$

where A,B and C are the Karplus parameters and  $\Delta\theta$  is an additional constant added on to the dihedral angle  $\theta$ . The Karplus parameters are determined empirically and are dependent on the type of J-coupling.

This collective variable computes the J-couplings for a set of atoms defining a dihedral angle. You can specify the atoms involved using the MOLINFO notation. You can also specify the experimental couplings using the ADD ← COUPLINGS flag and COUPLING keywords. These will be included in the output. You must choose the type of coupling using the type keyword, you can also supply custom Karplus parameters using TYPE=CUSTOM and the A, B, C and SHIFT keywords. You will need to make sure you are using the correct dihedral angle:

- Ha-N:  $\psi$
- Ha-HN: φ
- N-C  $\gamma$ :  $\chi_1$
- CO-C  $\gamma$ :  $\chi_1$

**Description of components** 

The names of the components in this action can be customized by the user in the actions input file. However, in addition to these customizable components the following quantities will always be output

| Quantity | Description               |  |
|----------|---------------------------|--|
| j        | the calculated J-coupling |  |

In addition the following quantities can be calculated by employing the keywords listed below

| Quantity | Keyword      | Description                 |
|----------|--------------|-----------------------------|
| ехр      | ADDCOUPLINGS | the experimental J-coupling |

The atoms involved can be specified using

| ATOMS | the 4 atoms involved in each of the bonds for which you wish to calculate the J-coupling. Keywords |
|-------|--|
|       | like ATOMS1, ATOMS2, ATOMS3, should be listed and one J-coupling will be calculated for each       |
|       | ATOMS keyword you specify. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2,     |
|       | ATOMS3   |

Compulsory keywords

| TYPE | Type of J-coupling to compute (HAN,HAHN,CCG,NCG,CUSTOM) |
|------|---|
|      | 'Jp' '' ' '' '' '' '' '' '' '' '' '' '' ''              |

### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically         |  |
|-----------------------|--|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-      |  |
|                       | tances   |  |
| ADDCOUPLINGS          | ( default=off ) Set this flag if you want to have fixed components with the exper- |  |
|                       | imental values.  |  |
|                       |  |  |
| A                     | Karplus parameter A  |  |
| В                     | Karplus parameter B  |  |
| С                     | Karplus parameter C  |  |
| SHIFT                 | Angle shift in radians   |  |
| COUPLING              | Add an experimental value for each coupling You can use multiple instances of      |  |
|                       | this keyword i.e. COUPLING1, COUPLING2, COUPLING3                                  |  |
|                       |  |  |

#### **Examples**

In the following example we calculate the Ha-N J-coupling from a set of atoms involved in dihedral  $\psi$  angles in the peptide backbone. We also add the experimental datapoints and compute the correlation and other measures and finally print the results.

```
MOLINFO MOLTYPE=protein STRUCTURE=peptide.pdb
WHOLEMOLECULES ENTITY0=1-111

JCOUPLING ...
ADDCOUPLINGS
TYPE=HAN
ATOMS1=@psi-2 COUPLING1=-0.49
ATOMS2=@psi-4 COUPLING2=-0.54
ATOMS3=@psi-5 COUPLING3=-0.53
ATOMS4=@psi-7 COUPLING4=-0.39
ATOMS5=@psi-8 COUPLING5=-0.39
LABEL=jhan
... JCOUPLING
jhanst: STATS ARG=(jhan\.j_.*) PARARG=(jhan\.exp_.*)

PRINT ARG=jhanst.*, jhan.* FILE=COLVAR STRIDE=100

ENDPLUMED
```

5.2.23 NOE

(See also PRINT, STATS)

This is part of the colvar module

Calculates NOE intensities as sums of  $1/r^{6}$ , also averaging over multiple equivalent atoms or ambiguous NOE.

Each NOE is defined by two groups containing the same number of atoms, distances are calculated in pairs, transformed in  $1/r^6$ , summed and saved as components.

$$NOE() = (\frac{1}{N_{eq}} \sum_{j}^{N_{eq}} (\frac{1}{r_j^6}))^{\frac{-1}{6}}$$

Intensities can then in principle ensemble averaged using ENSEMBLE and used to calculate a scoring function for example with METAINFERENCE.

**Description of components** 

The names of the components in this action can be customized by the user in the actions input file. However, in addition to these customizable components the following quantities will always be output

| Quantity | Description |
|----------|-------------|
| noe      | the # NOE   |

In addition the following quantities can be calculated by employing the keywords listed below

| Quantity | Keyword | Description                     |
|----------|---------|---------------------------------|
| ехр      | ADDEXP  | the # NOE experimental distance |

The atoms involved can be specified using

| GROUPA | the atoms involved in each of the contacts you wish to calculate. Keywords like GROUPA1, GR← OUPA2, GROUPA3, should be listed and one contact will be calculated for each ATOM keyword you specify. You can use multiple instances of this keyword i.e. GROUPA1, GROUPA2, GROUP← A3 |
|--------|---|
| GROUPB | the atoms involved in each of the contacts you wish to calculate. Keywords like GROUPB1, GR← OUPB2, GROUPB3, should be listed and one contact will be calculated for each ATOM keyword you specify. You can use multiple instances of this keyword i.e. GROUPB1, GROUPB2, GROUP← B3 |

### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-  |
|                       | tances   |
| ADDEXP                | ( default=off ) Set to TRUE if you want to have fixed components with the experimental reference values.                 |
| NOEDIST               | Add an experimental value for each NOE. You can use multiple instances of this keyword i.e. NOEDIST1, NOEDIST2, NOEDIST3 |

### **Examples**

In the following examples three noes are defined, the first is calculated based on the distances of atom 1-2 and 3-2; the second is defined by the distance 5-7 and the third by the distances 4-15,4-16,8-15,8-16.

```
NOE ...
GROUPA1=1,3 GROUPB1=2,2
GROUPA2=5 GROUPB2=7
```

```
GROUPA3=4,4,8,8 GROUPB3=15,16,15,16
LABEL=noes
... NOE

PRINT ARG=noes.* FILE=colvar
```

(See also PRINT)

### 5.2.24 PARABETARMSD

This is part of the secondarystructure module

Probe the parallel beta sheet content of your protein structure.

Two protein segments containing three continguous residues can form a parallel beta sheet. Although if the two segments are part of the same protein chain they must be separated by a minimum of 3 residues to make room for the turn. This colvar thus generates the set of all possible six residue sections that could conceivably form a parallel beta sheet and calculates the RMSD distance between the configuration in which the residues find themselves and an idealized parallel beta sheet structure. These distances can be calculated by either aligning the instantaneous structure with the reference structure and measuring each atomic displacement or by calculating differences between the set of interatomic distances in the reference and instantaneous structures.

This colvar is based on the following reference ?. The authors of this paper use the set of distances from the parallel beta sheet configurations to measure the number of segments whose configuration resembles a parallel beta sheet. This is done by calculating the following sum of functions of the rmsd distances:

$$s = \sum_{i} \frac{1 - \left(\frac{r_i - d_0}{r_0}\right)^n}{1 - \left(\frac{r_i - d_0}{r_0}\right)^m}$$

where the sum runs over all possible segments of parallel beta sheet. By default the NN, MM and D\_0 parameters are set equal to those used in ?. The R 0 parameter must be set by the user - the value used in ? was 0.08 nm.

If you change the function in the above sum you can calculate quantities such as the average distance from a structure composed of only parallel beta sheets or the distance between the set of residues that is closest to a parallel beta sheet and the reference configuration. To do these sorts of calculations you can use the AVERAGE and MIN keywords. In addition you can use the LESS\_THAN keyword if you would like to change the form of the switching function. If you use any of these options you no longer need to specify NN, R\_0, MM and D\_0.

Please be aware that for codes like gromacs you must ensure that plumed reconstructs the chains involved in your CV when you calculate this CV using anthing other than TYPE=DRMSD. For more details as to how to do this see WHOLEMOLECULES.

**Description of components** 

By default this Action calculates the number of structural units that are within a certain distance of a idealised secondary structure element. This quantity can then be referenced elsewhere in the input by using the label of the action. However, thes Action can also be used to calculate the following quantities by using the keywords as described below. The quantities then calculated can be referened using the label of the action followed by a dot and then the name from the table below. Please note that you can use the LESS\_THAN keyword more than once. The resulting components will be labelled *label*.lessthan-1, *label*.lessthan-2 and so on unless you exploit the fact that these labels are customizable. In particular, by using the LABEL keyword in the description of you LESS\_THAN function you can set name of the component that you are calculating

| Quantity | Keyword   | Description  |
|----------|-----------|--|
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description   |
|          |           | of the keyword so as to make it continuous.  |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action   |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the   |
|          |           | formula described in the description of the keyword so as to make it continuous.   |
|          |           | You can calculate this quantity multiple times using different parameters.   |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous. |

The atoms involved can be specified using

| RESIDUES | this command is used to specify the set of residues that could conceivably form part of the sec-       |
|----------|--|
|          | ondary structure. It is possible to use residues numbers as the various chains and residues            |
|          | should have been identified else using an instance of the MOLINFO action. If you wish to use all       |
|          | the residues from all the chains in your system you can do so by specifying all. Alternatively, if you |
|          | wish to use a subset of the residues you can specify the particular residues you are interested in     |
|          | as a list of numbers. Please be aware that to form secondary structure elements your chain must        |
|          | contain at least N residues, where N is dependent on the particular secondary structure you are        |
|          | interested in. As such if you define portions of the chain with fewer than N residues the code will    |
|          | crash.   |

# Compulsory keywords

| TYPE  | ( default=DRMSD ) the manner in which RMSD alignment is performed. Should be OPTIMAL, S↔  |
|-------|---|
|       | IMPLE or DRMSD. For more details on the OPTIMAL and SIMPLE methods see RMSD. For more   |
|       | details on the DRMSD method see DRMSD.  |
| R_0   | The r_0 parameter of the switching function.  |
| D_0   | ( default=0.0 ) The d_0 parameter of the switching function   |
| NN    | ( default=8 ) The n parameter of the switching function   |
| ММ    | ( default=12 ) The m parameter of the switching function  |
| STYLE | ( default=all ) Parallel beta sheets can either form in a single chain or from a pair of chains. If $S \leftarrow TYLE=all$ all chain configuration with the appropriate geometry are counted. If $STYLE=inter$ only sheet-like configurations involving two chains are counted, while if $STYLE=inter$ only sheet-like configurations involving a single chain are counted |

# Options

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically                |
|-----------------------|---|
| VERBOSE               | ( default=off ) write a more detailed output  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize                          |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation |

| LESS_THAN      | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.lessthan</code> . You can use multiple instances of this keyword i.e. <code>LESS_THAN1</code> , <code>LESS_THAN2</code> , <code>LESS_THAN3</code> The corresponding values are then referenced using <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-3</code> |
|----------------|---|
| MIN            | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label.</i> min-1, <i>label.</i> min-2, <i>label.</i> min-3                                |
| ALT_MIN        | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3  |
| LOWEST         | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest   |
| HIGHEST        | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest   |
| STRANDS_CUTOFF | If in a segment of protein the two strands are further apart then the calculation of the actual RMSD is skipped as the structure is very far from being beta-sheet like. This keyword speeds up the calculation enormously when you are using the LESS_THAN option. However, if you are using some other option, then this cannot be used   |

## **Examples**

The following input calculates the number of six residue segments of protein that are in an parallel beta sheet configuration.

```
MOLINFO STRUCTURE=helix.pdb PARABETARMSD RESIDUES=all TYPE=DRMSD LESS_THAN={RATIONAL R_0=0.08 NN=8 MM=12} LABEL=a
```

(see also MOLINFO)

## 5.2.25 PATHMSD

This is part of the colvar module

This Colvar calculates path collective variables.

This is the Path Collective Variables implementation (see?). This variable computes the progress along a given set of frames that is provided in input ("sss" component) and the distance from them ("zzz" component). (see below).

**Description of components** 

By default this Action calculates the following quantities. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Description                |
|----------|----------------------------|
| sss      | the position on the path   |
| ZZZ      | the distance from the path |

#### Compulsory keywords

| LAMBDA    | the lambda parameter is needed for smoothing, is in the units of plumed |  |
|-----------|---|--|
| REFERENCE | ENCE the pdb is needed to provide the various milestones                |  |

### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically |
|-----------------------|--|
| NEIGH_SIZE            | size of the neighbor list  |
| NEIGH_STRIDE          | how often the neighbor list needs to be calculated in time units           |

#### **Examples**

Here below is a case where you have defined three frames and you want to calculate the progress along the path and the distance from it in p1

```
p1: PATHMSD REFERENCE=file.pdb LAMBDA=500.0 NEIGH_STRIDE=4 NEIGH_SIZE=8 PRINT ARG=p1.sss,p1.zzz STRIDE=1 FILE=colvar FMT=%8.4f
```

note that NEIGH\_STRIDE=4 NEIGH\_SIZE=8 control the neighborlist parameter (optional but recommended for performance) and states that the neighbor list will be calculated every 4 timesteps and consider only the closest 8 member to the actual md snapshots.

In the REFERENCE PDB file the frames must be separated either using END or ENDMDL.

Note

The implementation of this collective variable and of PROPERTYMAP is shared, as well as most input options.

## 5.2.26 PATH

Path collective variables with a more flexible framework for the distance metric being used.

The Path Collective Variables developed by Branduardi and co-workers ? allow one to compute the progress along a high-dimensional path and the distance from the high-dimensional path. The progress along the path (s) is computed using:

$$s = \frac{\sum_{i=1}^{N} i \exp(-\lambda R[X - X_i])}{\sum_{i=1}^{N} \exp(-\lambda R[X - X_i])}$$

while the distance from the path (z) is measured using:

$$z = -\frac{1}{\lambda} \ln \left[ \sum_{i=1}^{N} \exp(-\lambda R[X - X_i]) \right]$$

In these expressions N high-dimensional frames ( $X_i$ ) are used to describe the path in the high-dimensional space. The two expressions above are then functions of the distances from each of the high-dimensional frames  $R[X-X_i]$ . Within PLUMED there are multiple ways to define the distance from a high-dimensional configuration. You could calculate the RMSD distance or you could calculate the ammount by which a set of collective variables change. As such this implementation of the path cv allows one to use all the difference distance metrics that are discussed in Distances from reference configurations. This is as opposed to the alternative implementation of path (PATHMSD) which is a bit faster but which only allows one to use the RMSD distance.

The s and z variables are calculated using the above formulas by default. However, there is an alternative method of calculating these collective variables, which is detailed in ?. This alternative method uses the tools of geometry (as opposed to algebra, which is used in the equations above). In this alternative formula the progress along the path s is calculated using:

$$s = i_2 + \operatorname{sign}(i_2 - i_1) \frac{\sqrt{(\mathbf{v}_1 \cdot \mathbf{v}_2)^2 - |\mathbf{v}_3|^2(|\mathbf{v}_1|^2 - |\mathbf{v}_2|^2)}}{2|\mathbf{v}_3|^2} - \frac{\mathbf{v}_1 \cdot \mathbf{v}_3 - |\mathbf{v}_3|^2}{2|\mathbf{v}_3|^2}$$

where  $\mathbf{v}_1$  and  $\mathbf{v}_3$  are the vectors connecting the current position to the closest and second closest node of the path, respectfully and  $i_1$  and  $i_2$  are the projections of the closest and second closest frames of the path.  $\mathbf{v}_2$ , meanwhile, is the vector connecting the closest frame to the second closest frame. The distance from the path, z is calculated using:

$$z = \sqrt{\left[ |\mathbf{v}_1|^2 - |\mathbf{v}_2| \left( \frac{\sqrt{(\mathbf{v}_1 \cdot \mathbf{v}_2)^2 - |\mathbf{v}_3|^2(|\mathbf{v}_1|^2 - |\mathbf{v}_2|^2)}}{2|\mathbf{v}_3|^2} - \frac{\mathbf{v}_1 \cdot \mathbf{v}_3 - |\mathbf{v}_3|^2}{2|\mathbf{v}_3|^2} \right) \right]^2}$$

The symbols here are as they were for s. If you would like to use these equations to calculate s and z then you should use the GPATH flag. The values of s and z can then be referenced using the gspath and gzpath labels.

**Description of components** 

By default the value of the calculated quantity can be referenced elsewhere in the input file by using the label of the action. Alternatively this Action can be used to be used to calculate the following quantities by employing the keywords listed below. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Keyword | Description  |                    |
|----------|---------|--|--------------------|
| gspath   | GPATH   | the position on the path calculated using trigonometry Ger | nerated by Doxygen |
| gzpath   | GPATH   | the distance from the path calculated using trigonometry   |                    |

#### Compulsory keywords

| REFERENCE | a pdb file containing the set of reference configurations  |
|-----------|--|
| TYPE      | ( default=OPTIMAL-FAST ) the manner in which distances are calculated. More information on the different metrics that are available in PLUMED can be found in the section of the manual on Distances from reference configurations |
| LAMBDA    | ( default=0 ) the value of the lambda parameter for paths  |

### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation  |
| DISABLE_CHECKS        | ( default=off ) disable checks on reference input structures.  |
| NOZPATH               | ( default=off ) do not calculate the zpath position  |
| NOSPATH               | ( default=off ) do not calculate the spath position  |
| GPATH                 | calculate the position on the path using trigonometry The final value can be referenced using <i>label</i> .gpath. You can use multiple instances of this keyword i.e. GPATH1, GPATH2, GPATH3 The corresponding values are then referenced using <i>label</i> .gpath-1, <i>label</i> .gpath-2, <i>label</i> .gpath-3 |

## **Examples**

In the example below the path is defined using RMSD distance from frames. The reference frames in the path are defined in the pdb file. In this frame each configuration in the path is separated by a line containing just the word END.

```
p1: PATH REFERENCE=file.pdb TYPE=OPTIMAL LAMBDA=500.0 PRINT ARG=p1.sss,p1.zzz STRIDE=1 FILE=colvar FMT=%8.4f
```

In the example below the path is defined using the values of two torsional angles (t1 and t2). In addition, the s and z are calculated using the geometric expressions described above rather than the alegebraic expressions that are used by default.

```
t1: TORSION ATOMS=5,7,9,15
t2: TORSION ATOMS=7,9,15,17
pp: PATH TYPE=EUCLIDEAN REFERENCE=epath.pdb GPATH NOSPATH NOZPATH
PRINT ARG=pp.* FILE=colvar
```

Notice that the LAMBDA parameter is not required here as we are not calculating s and s using the algebraic formulae defined earlier. The positions of the frames in the path are defined in the file epath.pdb. An extract from this file looks as shown below.

```
REMARK ARG=t1,t2 t1=-4.25053 t2=3.88053 END

REMARK ARG=t1,t2 t1=-4.11 t2=3.75 END

REMARK ARG=t1,t2 t1=-3.96947 t2=3.61947 END
```

The remarks in this pdb file tell PLUMED the labels that are being used to define the position in the high dimensional space and the values that these arguments have at each point on the path.

## **5.2.27 PCAVARS**

This is part of the mapping module

Projection on principal component eigenvectors or other high dimensional linear subspace

The collective variables described in Distances from reference configurations allow one to calculate the distance between the instaneous structure adopted by the system and some high-dimensional, reference configuration. The problem with doing this is that, as one gets further and further from the reference configuration, the distance from it becomes a progressively poorer and poorer collective variable. This happens because the "number" of structures at a distance d from a reference configuration is proportional to  $d^N$  in an N dimensional space. Consequently, when d is small the distance from the reference configuration may well be a good collective variable. However, when d is large it is unlikely that the distance from the reference structure is a good CV. When the distance is large there will almost certainly be markedly different configuration that have the same CV value and hence barriers in transverse degrees of freedom.

For these reasons dimensionality reduction is often employed so a projection s of a high-dimensional configuration X in a lower dimensionality space using a function:

$$\mathbf{s} = F(\mathbf{X} - \mathbf{X}^{ref})$$

where here we have introduced some high-dimensional reference configuration  $\mathbf{X}^{ref}$ . By far the simplest way to do this is to use some linear operator for F. That is to say we find a low-dimensional projection by rotating the basis vectors using some linear algebra:

$$\mathbf{s}_i = \sum_k A_{ik} (X_k - X_k^{ref})$$

Here A is a d by D matrix where D is the dimensionality of the high dimensional space and d is the dimensionality of the lower dimensional subspace. In plumed when this kind of projection you can use the majority of the metrics detailed on Distances from reference configurations to calculate the displacement,  $\mathbf{X} - \mathbf{X}^{ref}$ , from the reference configuration. The matrix A can be found by various means including principal component analysis and normal mode analysis. In both these methods the rows of A would be the principle eigenvectors of a square matrix. For PCA the covariance while for normal modes the Hessian.

Bug It is not possible to use the DRMSD metric with this variable. You can get around this by listing the set of distances you wish to calculate for your DRMSD in the plumed file explicitally and using the EUCLIDEAN metric. MAHALONOBIS and NORM-EUCLIDEAN also do not work with this variable but using these options makes little sense when projecting on a linear subspace.

**Description of components** 

By default this Action calculates the following quantities. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Description   |
|----------|---|
| eig      | the projections on each eigenvalue are stored on values labeled eig-1, eig-2,   |
| residual | the distance of the configuration from the linear subspace defined by the vectors, $e_i$ , that are contained in the rows of $A$ . In other words this is $\sqrt{(r^2 - \sum_i [\mathbf{r}.\mathbf{e_i}]^2)}$ where $r$ is the distance between |
|          | the instantaneous position and the reference point.   |

#### Compulsory keywords

| REFERENCE | a pdb file containing the reference configuration and configurations that define the directions for each eigenvector |
|-----------|--|
| TYPE      | ( default=OPTIMAL ) The method we are using for alignment to the reference structure                                 |

#### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| NORMALIZE             | ( default=off ) calculate the length of the eigenvector input and divide the components by it so as to have a normalised vector |
|                       |   |

#### **Examples**

The following input calculates a projection on a linear subspace where the displacements from the reference configuration are calculated using the OPTIMAL metric. Consequently, both translation of the center of mass of the atoms and rotation of the reference frame are removed from these displacements. The matrix A and the reference configuration  $R^{ref}$  are specified in the pdb input file reference.pdb and the value of all projections (and the residual) are output to a file called colvar2.

```
PCAVARS REFERENCE=reference.pdb TYPE=OPTIMAL LABEL=pca2 PRINT ARG=pca2.* FILE=colvar2
```

The reference configurations can be specified using a pdb file. The first configuration that you provide is the reference configuration, which is referred to in the above as  $X^{ref}$  subsequent configurations give the directions of row vectors that are contained in the matrix A above. These directions can be specified by specifying a second configuration - in this case a vector will be constructed by calculating the displacement of this second configuration from the reference configuration. A pdb input prepared in this way would look as follows:

| 2  | СНЗ   | ACE  | 1   | 12.932  | -14.718  | -6.016   | 1.00  | 1.00  |
|----|---|--|---|---|--|--|---|---|
| 5  | С   | ACE  | 1   | 21.312  | -9.928   | -5.946   | 1.00  | 1.00  |
| 9  | CA  | ALA  | 2   | 19.462  | -11.088  | -8.986   | 1.00  | 1.00  |
| 13 | HB2   | ALA  | 2   | 21.112  | -10.688  | -12.476  | 1.00  | 1.00  |
| 15 | С   | ALA  | 2   | 19.422  | 7.978  | -14.536  | 1.00  | 1.00  |
| 20 | нн31  | NME  | 3   | 20.122  | -9.928   | -17.746  | 1.00  | 1.00  |
| 21 | HH32  | NME  | 3   | 18.572  | -13.148  | -16.346  | 1.00  | 1.00  |
|    |   |  |   |   |  |  |   |   |
| 2  | СНЗ   | ACE  | 1   | 13.932  | -14.718  | -6.016   | 1.00  | 1.00  |
| 5  | С   | ACE  | 1   | 20.312  | -9.928   | -5.946   | 1.00  | 1.00  |
| 9  | CA  | ALA  | 2   | 18.462  | -11.088  | -8.986   | 1.00  | 1.00  |
| 13 | HB2   | ALA  | 2   | 20.112  | -11.688  | -12.476  | 1.00  | 1.00  |
| 15 | С   | ALA  | 2   | 19.422  | 7.978  | -12.536  | 1.00  | 1.00  |
| 20 | HH31  | NME  | 3   | 20.122  | -9.928   | -17.746  | 1.00  | 1.00  |
| 21 | HH32  | NME  | 3   | 18.572  | -13.148  | -16.346  | 1.00  | 1.00  |
|    |   |  |   |   |  |  |   |   |
|    | 5<br>9<br>13<br>15<br>20<br>21<br>2<br>5<br>9<br>13<br>15<br>20 | 5 C<br>9 CA<br>13 HB2<br>15 C<br>20 HH31<br>21 HH32<br>2 CH3<br>5 C<br>9 CA<br>13 HB2<br>15 C<br>20 HH31 | 5 C ACE 9 CA ALA 13 HB2 ALA 15 C ALA 20 HH31 NME 21 HH32 NME 2 CH3 ACE 5 C ACE 9 CA ALA 13 HB2 ALA 15 C ALA 20 HH31 NME | 5 C ACE 1 9 CA ALA 2 13 HB2 ALA 2 15 C ALA 2 20 HH31 NME 3 21 HH32 NME 3 2 CH3 ACE 1 5 C ACE 1 9 CA ALA 2 13 HB2 ALA 2 13 HB2 ALA 2 20 HH31 NME 3 | 5 C ACE 1 21.312<br>9 CA ALA 2 19.462<br>13 HB2 ALA 2 21.112<br>15 C ALA 2 19.422<br>20 HH31 NME 3 20.122<br>21 HH32 NME 3 18.572<br>2 CH3 ACE 1 13.932<br>5 C ACE 1 20.312<br>9 CA ALA 2 18.462<br>13 HB2 ALA 2 20.112<br>15 C ALA 2 19.422<br>20 HH31 NME 3 20.122 | 5 C ACE 1 21.312 -9.928 9 CA ALA 2 19.462 -11.088 13 HB2 ALA 2 21.112 -10.688 15 C ALA 2 19.422 7.978 20 HH31 NME 3 20.122 -9.928 21 HH32 NME 3 18.572 -13.148  2 CH3 ACE 1 13.932 -14.718 5 C ACE 1 20.312 -9.928 9 CA ALA 2 18.462 -11.088 13 HB2 ALA 2 20.112 -11.688 15 C ALA 2 19.422 7.978 20 HH31 NME 3 20.122 -9.928 | 5 C ACE 1 21.312 -9.928 -5.946 9 CA ALA 2 19.462 -11.088 -8.986 13 HB2 ALA 2 21.112 -10.688 -12.476 15 C ALA 2 19.422 7.978 -14.536 20 HH31 NME 3 20.122 -9.928 -17.746 21 HH32 NME 3 18.572 -13.148 -16.346  2 CH3 ACE 1 13.932 -14.718 -6.016 5 C ACE 1 20.312 -9.928 -5.946 9 CA ALA 2 18.462 -11.088 -8.986 13 HB2 ALA 2 20.112 -11.688 -12.476 15 C ALA 2 19.422 7.978 -12.536 20 HH31 NME 3 20.122 -9.928 -17.746 | 5         C         ACE         1         21.312         -9.928         -5.946         1.00           9         CA         ALA         2         19.462         -11.088         -8.986         1.00           13         HB2         ALA         2         21.112         -10.688         -12.476         1.00           15         C         ALA         2         19.422         7.978         -14.536         1.00           20         HH31         NME         3         20.122         -9.928         -17.746         1.00           21         HH32         NME         3         18.572         -13.148         -16.346         1.00           2         CH3         ACE         1         13.932         -14.718         -6.016         1.00           5         C         ACE         1         20.312         -9.928         -5.946         1.00           9         CA         ALA         2         18.462         -11.088         -8.986         1.00           13         HB2         ALA         2         20.112         -11.688         -12.476         1.00           15         C         ALA         2         19.42 |

Alternatively, the second configuration can specify the components of A explicitally. In this case you need to include the keyword TYPE=DIRECTION in the remarks to the pdb as shown below.

| ATOM   | 2     | СНЗ   | ACE   | 1 | 12.932  | -14.718 | -6.016  | 1.00 | 1.00 |
|--------|-------|-------|-------|---|---------|---------|---------|------|------|
| ATOM   | 5     | С     | ACE   | 1 | 21.312  | -9.928  | -5.946  | 1.00 | 1.00 |
| ATOM   | 9     | CA    | ALA   | 2 | 19.462  | -11.088 | -8.986  | 1.00 | 1.00 |
| ATOM   | 13    | HB2   | ALA   | 2 | 21.112  | -10.688 | -12.476 | 1.00 | 1.00 |
| ATOM   | 15    | С     | ALA   | 2 | 19.422  | 7.978   | -14.536 | 1.00 | 1.00 |
| ATOM   | 20    | НН31  | NME   | 3 | 20.122  | -9.928  | -17.746 | 1.00 | 1.00 |
| ATOM   | 21    | НН32  | NME   | 3 | 18.572  | -13.148 | -16.346 | 1.00 | 1.00 |
| END    |       |       |       |   |         |         |         |      |      |
| REMARK | TYPE= | =DIRE | CTION |   |         |         |         |      |      |
| ATOM   | 2     | СНЗ   | ACE   | 1 | 0.1414  | 0.3334  | -0.0302 | 1.00 | 0.00 |
| ATOM   | 5     | С     | ACE   | 1 | 0.0893  | -0.1095 | -0.1434 | 1.00 | 0.00 |
| ATOM   | 9     | CA    | ALA   | 2 | 0.0207  | -0.321  | 0.0321  | 1.00 | 0.00 |
| ATOM   | 13    | HB2   | ALA   | 2 | 0.0317  | -0.6085 | 0.0783  | 1.00 | 0.00 |
| ATOM   | 15    | С     | ALA   | 2 | 0.1282  | -0.4792 | 0.0797  | 1.00 | 0.00 |
| ATOM   | 20    | НН31  | NME   | 3 | 0.0053  | -0.465  | 0.0309  | 1.00 | 0.00 |
| ATOM   | 21    | НН32  | NME   | 3 | -0.1019 | -0.4261 | -0.0082 | 1.00 | 0.00 |
| END    |       |       |       |   |         |         |         |      |      |

If your metric involves arguments the labels of these arguments in your plumed input file should be specified in the REMARKS for each of the frames of your path. An input file in this case might look like this:

```
DESCRIPTION: a pca eigenvector specified using the start point and direction in the HD space. REMARK WEIGHT=1.0 REMARK ARG=d1,d2 REMARK d1=1.0 d2=1.0 END REMARK TYPE=DIRECTION REMARK ARG=d1,d2 REMARK d1=0.1 d2=0.25 REMARK d1=0.1 d2=0.25
```

Here we are working with the EUCLIDEAN metric and notice that we have specified the components of A using D $\leftarrow$  IRECTION. Consequently, the values of d1 and d2 in the second frame above do not specify a particular coordinate in the high-dimensional space as in they do in the first frame. Instead these values are the coefficients that can be used to construct a linear combination of d1 and d2. If we wanted to specify the direction in this metric using the start and end point of the vector we would write:

```
DESCRIPTION: a pca eigenvector specified using the start and end point of a vector in the HD space. REMARK WEIGHT=1.0 REMARK ARG=d1,d2 REMARK d1=1.0 d2=1.0 END REMARK ARG=d1,d2 REMARK d1=1.1 d2=1.25 END
```

### 5.2.28 POSITION

This is part of the colvar module

Calculate the components of the position of an atom.

Notice that single components will not have the proper periodicity! If you need the values to be consistent through PBC you should use SCALED\_COMPONENTS, which defines values that by construction are in the -0.5,0.  $\leftarrow$  5 domain. This is similar to the equivalent flag for DISTANCE. Also notice that by default the minimal image distance from the origin is considered (can be changed with NOPBC).

### Attention

This variable should be used with extreme care since it allows to easily go into troubles. See comments below.

This variable can be safely used only if Hamiltonian is not invariant for translation (i.e. there are other absolute positions which are biased, e.g. by position restraints) and cell size and shapes are fixed through the simulation.

If you are not in this situation and still want to use the absolute position of an atom you should first fix the reference frame. This can be done e.g. using FIT\_TO\_TEMPLATE.

**Description of components** 

By default this Action calculates the following quantities. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity Description |                                      |
|----------------------|--------------------------------------|
| X                    | the x-component of the atom position |
| у                    | the y-component of the atom position |
| z                    | the z-component of the atom position |

In addition the following quantities can be calculated by employing the keywords listed below

| Quantity | Keyword           | Description   |
|----------|-------------------|---|
| а        | SCALED_COMPONENTS | the normalized projection on the first lattice vector of the atom position  |
| b        | SCALED_COMPONENTS | the normalized projection on the second lattice vector of the atom position |
| С        | SCALED_COMPONENTS | the normalized projection on the third lattice vector of the atom posi-     |
|          |                   | tion  |

The atoms involved can be specified using

# **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-  |
|                       | tances   |
| SCALED_COMPONENTS     | ( default=off ) calculate the a, b and c scaled components of the position separately and store them as label.a, label.b and label.c |

## **Examples**

# align to a template

```
FIT_TO_TEMPLATE REFERENCE=ref.pdb
p: POSITION ATOM=3
PRINT ARG=p.x,p.y,p.z
```

(see also FIT\_TO\_TEMPLATE)

## 5.2.29 PRE

| This is | part | of the | colvar | module |
|---------|------|--------|--------|--------|
|---------|------|--------|--------|--------|

Calculates the Paramegnetic Resonance Enhancement intensity ratio between two atoms. The reference atom for the spin label is added with SPINLABEL, the affected atom(s) are give as numbered GROUPA1, GROUPA2, ... The additional parameters needed for the calculation are given as INEPT, the inept time, TAUC the correlation time, OMEGA, the larmor frequency and RTWO for the relaxation time.

**Description of components** 

The names of the components in this action can be customized by the user in the actions input file. However, in addition to these customizable components the following quantities will always be output

| Quantity | Description |
|----------|-------------|
| pre      | the # PRE   |

In addition the following quantities can be calculated by employing the keywords listed below

| Quantity | Keyword | Description                      |
|----------|---------|----------------------------------|
| ехр      | ADDEXP  | the # PRE experimental intensity |

The atoms involved can be specified using

| SPINLABEL | The atom to be used as the paramagnetic center For more information on how to specify lists of atoms see Groups and Virtual Atoms   |  |
|-----------|---|--|
| GROUPA    | the atoms involved in each of the contacts you wish to calculate. Keywords like GROUPA1, GROUPA2, GROUPA3, should be listed and one contact will be calculated for each ATOM keyword you specify. You can use multiple instances of this keyword i.e. GROUPA1, GROUPA2, GROUPA3 |  |

## Compulsory keywords

| INEPT | is the INEPT time (in ms).   |
|-------|--|
| TAUC  | is the correlation time (in ns) for this electron-nuclear interaction. |
| OMEGA | is the Larmor frequency of the nuclear spin (in MHz).                  |

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# **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances  |
| ADDEXP                | ( default=off ) Set to TRUE if you want to have fixed components with the experimetnal values.  |
| RTWO                  | The relaxation of the atom/atoms in the corresponding GROUPA of atoms. Keywords like RTWO1, RTWO2, RTWO3, should be listed. You can use multiple instances of this keyword i.e. RTWO1, RTWO2, RTWO3 |
| PREINT                | Add an experimental value for each PRE. You can use multiple instances of this keyword i.e. PREINT1, PREINT2, PREINT3   |

#### **Examples**

In the following example five PRE intensities are calculated using the distance between the oxigen of the spin label and the backbone hydrogens. Omega is the NMR frequency, RTWO the R2 for the hydrogens, INEPT of 8 ms for the experiment and a TAUC of 1.21 ns

```
PRE ...
LABEL=HN_pre
INEPT=8
TAUC=1.21
OMEGA=900
SPINLABEL=1818
GROUPA1=86 RTW01=0.0120272827
GROUPA2=177 RTWO2=0.0263953158
GROUPA3=285 RTWO3=0.0058899829
GROUPA4=335 RTWO4=0.0102072646
GROUPA5=451 RTWO5=0.0086341843
PRINT ARG=HN_pre.* FILE=PRE.dat STRIDE=1
```

## 5.2.30 PROPERTYMAP

This is part of the colvar module

Calculate generic property maps.

This Colvar calculates the property maps according to the work of Spiwok ?.

Basically it calculates

$$X = \frac{\sum_{i} X_{i} * \exp(-\lambda D_{i}(x))}{\sum_{i} \exp(-\lambda D_{i}(x))}$$

$$Y = \frac{\sum_{i} Y_{i} * \exp(-\lambda D_{i}(x))}{\sum_{i} \exp(-\lambda D_{i}(x))}$$
(5.2)

$$Y = \frac{\sum_{i} Y_i * \exp(-\lambda D_i(x))}{\sum_{i} \exp(-\lambda D_i(x))}$$
(5.2)

$$zzz = -\frac{1}{\lambda}\log(\sum_{i}\exp(-\lambda D_{i}(x)))$$
(5.4)

where the parameters  $X_i$  and  $Y_i$  are provided in the input pdb (allv.pdb in this case) and  $D_i(x)$  is the MSD after optimal alignment calculated on the pdb frames you input (see Kearsley).

#### **Description of components**

The names of the components in this action can be customized by the user in the actions input file. However, in addition to these customizable components the following quantities will always be output

| Quantity | Description                                    |  |
|----------|--|--|
| ZZZ      | the minimum distance from the reference points |  |

#### Compulsory keywords

| LAMBDA    | the lambda parameter is needed for smoothing, is in the units of plumed                 |  |
|-----------|---|--|
| REFERENCE | the pdb is needed to provide the various milestones                                     |  |
| PROPERTY  | the property to be used in the indexing: this goes in the REMARK field of the reference |  |

#### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically |  |
|-----------------------|--|--|
| NEIGH_SIZE            | size of the neighbor list  |  |
| NEIGH_STRIDE          | how often the neighbor list needs to be calculated in time units           |  |

## **Examples**

```
p3: PROPERTYMAP REFERENCE=../../trajectories/path_msd/allv.pdb PROPERTY=X,Y LAMBDA=69087 NEIGH_SIZE=8 NEIGPRINT ARG=p3.X,p3.Y,p3.Zzz STRIDE=1 FILE=colvar FMT=%8.4f
```

note that NEIGH\_STRIDE=4 NEIGH\_SIZE=8 control the neighborlist parameter (optional but recommended for performance) and states that the neighbor list will be calculated every 4 timesteps and consider only the closest 8 member to the actual md snapshots.

In this case the input line instructs plumed to look for two properties X and Y with attached values in the REMARK line of the reference pdb (Note: No spaces from X and = and 1 !!!!). e.g.

```
REMARK X=1 Y=2
     1 CL ALA
        1 CL ALA 1
5 CLP ALA 1
MOTA
                           -3.171
                                 0.295
                                         2.045 1.00 1.00
                           -1.819 -0.143
                                        1.679 1.00 1.00
ATOM
REMARK X=2 Y=3
ATOM 1 CL ALA 1
                           -3.175 0.365
                                        2.024 1.00 1.00
ATOM
       5 CLP ALA
                           -1.814 -0.106
                                         1.685 1.00 1.00
END
```

#### Note

The implementation of this collective variable and of PATHMSD is shared, as well as most input options.

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# 5.2.31 PUCKERING

This is part of the colvar module

Calculate sugar pseudorotation coordinates.

This command can be used to calculate ring's pseudorotations in sugars (puckers). It works for both 5-membered and 6-membered rings. Notice that there are two different implementations depending if one passes 5 or 6 atoms in the ATOMS keyword.

For 5-membered rings the implementation is the one discussed in ? . This implementation is simple and can be used in RNA to distinguish C2'-endo and C3'-endo conformations. Both the polar coordinates (phs and amp) and the cartesian coordinates (Zx and Zy) are provided. C2'-endo conformations have negative Zx, whereas C3'-endo conformations have positive Zy. Notation is consistent with ? . The five atoms should be provided as C4',O4',C1',C2',C3'. Notice that this is the same order that can be obtained using the MOLINFO syntax (see example below).

For 6-membered rings the implementation is the general Cremer-Pople one ? as also discussed in ? . This implementation provides both a triplet with Cartesian components (qx, qy, and qz) and a triplet of polar components (amplitude, phi, and theta). Applications of this particular implentation are to be published (paper in preparation).

Components of this action are:

**Description of components** 

By default the value of the calculated quantity can be referenced elsewhere in the input file by using the label of the action. Alternatively this Action can be used to be used to calculate the following quantities by employing the keywords listed below. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity  | Description   |
|-----------|---|
| phs       | Pseudorotation phase (5 membered rings)                 |
| amp       | Pseudorotation amplitude (5 membered rings)             |
| Zx        | Pseudorotation x cartesian component (5 membered rings) |
| Zy        | Pseudorotation y cartesian component (5 membered rings) |
| phi       | Pseudorotation phase (6 membered rings)                 |
| theta     | Theta angle (6 membered rings)                          |
| amplitude | Pseudorotation amplitude (6 membered rings)             |
| qx        | Cartesian component x (6 membered rings)                |
| qy        | Cartesian component y (6 membered rings)                |
| qz        | Cartesian component z (6 membered rings)                |

The atoms involved can be specified using

**ATOMS** 

the five or six atoms of the sugar ring in the proper order. For more information on how to specify lists of atoms see Groups and Virtual Atoms

**Options** 

NUMERICAL\_DERIVATIVES ( default=off ) calculate the derivatives for these quantities numerically

**Examples** 

This input tells plumed to print the puckering phase angle of the 3rd nucleotide of a RNA molecule on file COLVAR.

MOLINFO STRUCTURE=rna.pdb MOLTYPE=rna PUCKERING ATOMS=@sugar-3 LABEL=puck PRINT ARG=puck.phs FILE=COLVAR

5.2.32 RDC

This is part of the colvar module

Calculates the (Residual) Dipolar Coupling between two atoms.

The RDC between two atomic nuclei depends on the  $\theta$  angle between the inter-nuclear vector and the external magnetic field. In isotropic media RDCs average to zero because of the orientational averaging, but when the rotational symmetry is broken, either through the introduction of an alignment medium or for molecules with highly anisotropic paramagnetic susceptibility, RDCs become measurable.

$$D = D_{max}0.5(3\cos^2(\theta) - 1)$$

where

$$D_{max} = -\mu_0 \gamma_1 \gamma_2 h / (8\pi^3 r^3)$$

that is the maximal value of the dipolar coupling for the two nuclear spins with gyromagnetic ratio  $\gamma$ .  $\mu$  is the magnetic constant and h is the Planck constant.

Common Gyromagnetic Ratios (C.G.S)

- H(1) 26.7513
- · C(13) 6.7261
- N(15) -2.7116
- NH -72.5388
- · CH 179.9319
- CN -18.2385
- · CC 45.2404

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This collective variable calculates the Residual Dipolar Coupling for a set of couple of atoms using the above definition. From the calculated RDCs and a set of experimental values it calculates either their correlation or the squared quality factor

$$Q^{2} = \frac{\sum_{i} (D_{i} - D_{i}^{exp})^{2}}{\sum_{i} (D_{i}^{exp})^{2}}$$

RDCs report only on the fraction of molecules that is aligned, this means that comparing the RDCs from a single structure in a MD simulation to the experimental values is not particularly meaningfull, from this point of view it is better to compare their correlation. The fraction of aligned molecules can be obtained by maximising the correlation between the calculated and the experimental RDCs. This fraction can be used as a scaling factor in the calculation of the RDCs in order to compare their values. The averaging of the RDCs calculated with the above definition from a standard MD should result to 0 because of the rotational diffusion, but this variable can be used to break the rotational symmetry.

RDCs can also be calculated using a Single Value Decomposition approach, in this case the code rely on the a set of function from the GNU Scientific Library (GSL). (With SVD forces are not currently implemented).

Replica-Averaged restrained simulations can be performed with this CV and the function ENSEMBLE.

Additional material and examples can be also found in the tutorial Belfast tutorial: NMR restraints

**Description of components** 

The names of the components in this action can be customized by the user in the actions input file. However, in addition to these customizable components the following quantities will always be output

| Quantity | Description          |  |
|----------|----------------------|--|
| rdc      | the calculated # RDC |  |

In addition the following quantities can be calculated by employing the keywords listed below

| Quantity | Keyword          | Description            |
|----------|------------------|------------------------|
| ехр      | SVD/ADDCOUPLINGS | the experimental # RDC |

The atoms involved can be specified using

# **ATOMS**

the couple of atoms involved in each of the bonds for which you wish to calculate the RDC. Keywords like ATOMS1, ATOMS2, ATOMS3,... should be listed and one dipolar coupling will be calculated for each ATOMS keyword you specify. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3...

Compulsory keywords

| GYROM   | Add the product of the gyromagnetic constants for the bond. |  |
|---|---|--|
| SCALE Add the scaling factor to take into account concentration and other effects |   |  |

# **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-   |
|                       | tances  |
| SVD                   | ( default=off ) Set to TRUE if you want to backcalculate using Single Value Decomposition (need GSL at compilation time).   |
| ADDCOUPLINGS          | ( default=off ) Set to TRUE if you want to have fixed components with the experimetnal values.  |
| COUPLING              | Add an experimental value for each coupling (needed by SVD and usefull for ef STATS). You can use multiple instances of this keyword i.e. COUPLING1, COUPLING2, COUPLING3 |

# **Examples**

In the following example five N-H RDCs are defined and their correlation with respect to a set of experimental data is calculated and restrained. In addition, and only for analysis purposes, the same RDCs are calculated using a Single Value Decomposition algorithm.

```
RDC ...
GYROM = -72.5388
SCALE=1.0
ATOMS1=20,21
ATOMS2=37,38
ATOMS3=56,57
ATOMS4=76,77
ATOMS5=92,93
LABEL=nh
... RDC
STATS ARG=nh.* PARAMETERS=8.17,-8.271,-10.489,-9.871,-9.152
rdce: RESTRAINT ARG=nh.corr KAPPA=0. SLOPE=-25000.0 AT=1.
GYROM=-72.5388
SCALE=1.0
SVD
ATOMS1=20,21 COUPLING1=8.17
ATOMS2=37,38 COUPLING2=-8.271
ATOMS3=56,57 COUPLING3=-10.489
ATOMS4=76,77 COUPLING4=-9.871
ATOMS5=92,93 COUPLING5=-9.152
LABEL=svd
... RDC
PRINT ARG=nh.corr, rdce.bias FILE=colvar
PRINT ARG=svd.* FILE=svd
```

(See also PRINT, RESTRAINT)

# **5.2.33 TEMPLATE**

This is part of the colvar module

This file provides a template for if you want to introduce a new CV.

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The atoms involved can be specified using

| ATOMS | the keyword with which you specify what atoms to use should be added like this. For more information |  |
|-------|--|--|
|       | on how to specify lists of atoms see Groups and Virtual Atoms  |  |

Compulsory keywords

| like this with a description here |
|-----------------------------------|
|-----------------------------------|

**Options** 

| NUMERICAL_DERIVATIVES     | ( default=off ) calculate the derivatives for these quantities numerically       |
|---------------------------|--|
| NOPBC                     | ( default=off ) ignore the periodic boundary conditions when calculating         |
|                           | distances  |
| TEMPLATE_DEFAULT_OFF_FLAG | ( default=off ) flags that are by default not performed should be specified      |
|                           | like this  |
| TEMPLATE_DEFAULT_ON_FLAG  | ( default=on ) flags that are by default performed should be specified like this |
| TEMPLATE_OPTIONAL         | all optional keywords that have input should be added like a description here    |

Examples

# **5.2.34 TORSION**

This is part of the colvar module

Calculate a torsional angle.

This command can be used to compute the torsion between four atoms or alternatively to calculate the angle between two vectors projected on the plane orthogonal to an axis.

The atoms involved can be specified using

| TOMS the four atoms involved in the torsional angle |
|---|
|---|

Or alternatively by using

| AXIS    | two atoms that define an axis. You can use this to find the angle in the plane perpendicular to the axis between the vectors specified using the VECTOR1 and VECTOR2 keywords. |
|---------|--|
| VECTOR1 | two atoms that define a vector. You can use this in combination with VECTOR2 and AXIS  |
| VECTOR2 | two atoms that define a vector. You can use this in combination with VECTOR1 and AXIS  |

#### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically         |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances |
| COSINE                | ( default=off ) calculate cosine instead of dihedral                               |

#### **Examples**

This input tells plumed to print the torsional angle between atoms 1, 2, 3 and 4 on file COLVAR.

```
t: TORSION ATOMS=1,2,3,4
# this is an alternative, equivalent, definition:
# t: TORSION VECTOR1=2,1 AXIS=2,3 VECTOR2=3,4
PRINT ARG=t FILE=COLVAR
```

If you are working with a protein you can specify the special named torsion angles  $\phi$ ,  $\psi$ ,  $\omega$  and  $\chi_1$  by using TOR $\leftarrow$  SION in combination with the MOLINFO command. This can be done by using the following syntax.

```
MOLINFO MOLTYPE=protein STRUCTURE=myprotein.pdb
t1: TORSION ATOMS=@phi-3
t2: TORSION ATOMS=@psi-4
PRINT ARG=t1,t2 FILE=colvar STRIDE=10
```

Here, @phi-3 tells plumed that you would like to calculate the  $\phi$  angle in the third residue of the protein. Similarly @psi-4 tells plumed that you want to calculate the  $\psi$  angle of the 4th residue of the protein.

#### 5.2.35 **VOLUME**

This is part of the colvar module

Calculate the volume of the simulation box.

#### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically |
|-----------------------|--|

#### **Examples**

The following input tells plumed to print the volume of the system

```
PRINT ARG=vol

(See also PRINT).
```

# 5.3 Distances from reference configurations

One colvar that has been shown to be very sucessful in studying protein folding is the distance between the instantaneous configuration and a reference configuration - often the structure of the folded state. When the free energy of a protein is shown as a function of this collective variable there is a minima for low values of the CV, which is due to the folded state of the protein. There is then a second minima at higher values of the CV, which is the minima corresponding to the unfolded state.

A slight problem with this sort of collective variable is that there are many different ways of calculating the distance from a particular reference structure. The simplest - adding together the distances by which each of the atoms has been translated in going from the reference configuration to the instantanous configuration - is not particularly sensible. A distance calculated in this way does not neglect translation of the center of mass of the molecule and rotation of the frame of reference. A common practise is thus to remove these components by calculating the RMSD distance between the reference and instantaneous configurations. This is not the only way to calculate the distance, however. One could also calculate the total ammount by which a large number of collective variables change in moving from the reference to the instaneous configurations. One could even combine RMSD distances with the ammount the collective variables change. A full list of the ways distances can be measured in PLUMED is given below:

| DRMSD      | Calculate the distance RMSD with respect to a reference structure.   |
|------------|--|
| MULTI-RMSD | Calculate the RMSD distance moved by a number of separated domains from their positions in   |
|            | a reference structure.   |
| PCARMSD    | Calculate the PCA components ( see ? and ? ) for a number of provided eigenvectors and an average structure. Performs optimal alignment at every step and reports the rmsd so you know if you are far or close from the average structure. It takes the average structure and eigenvectors in form of a pdb. Note that beta and occupancy values in the pdb are neglected and all the weights are placed to 1 (differently from the RMSD colvar for example) |
| RMSD       | Calculate the RMSD with respect to a reference structure.  |
| TARGET     | This function measures the pythagorean distance from a particular structure measured in the space defined by some set of collective variables.   |

These options for calculating distances are re-used in a number of places in the code. For instance they are used in some of the analysis algorithms that are implemented in PLUMED and in PATH collective variables.

# 5.3.1 DRMSD

This is part of the colvar module

Calculate the distance RMSD with respect to a reference structure.

To calculate the root-mean-square deviation between the atoms in two configurations you must first superimpose the two structures in some ways. Obviously, it is the internal vibrational motions of the structure - i.e. not the translations and rotations - that are interesting. However, aligning two structures by removing the translational and

rotational motions is not easy. Furthermore, in some cases there can be alignment issues caused by so-called frame-fitting problems. It is thus often cheaper and easier to calculate the distances between all the pairs of atoms. The distance between the two structures,  $\mathbf{X}^a$  and  $\mathbf{X}^b$  can then be measured as:

$$d(\mathbf{X}^A, \mathbf{X}^B) = \frac{1}{N(N-1)} \sum_{i \neq j} [d(\mathbf{x}_i^a, \mathbf{x}_j^a) - d(\mathbf{x}_i^b, \mathbf{x}_j^b)]^2$$

where N is the number of atoms and  $d(\mathbf{x}_i, \mathbf{x}_j)$  represents the distance between atoms i and j. Clearly, this representation of the configuration is invariant to translation and rotation. However, it can become expensive to calculate when the number of atoms is large. This can be resolved within the DRMSD colvar by setting LOWER $\leftarrow$ \_CUTOFF and UPPER\_CUTOFF. These keywords ensure that only pairs of atoms that are within a certain range are incorporated into the above sum.

In PDB files the atomic coordinates and box lengths should be in Angstroms unless you are working with natural units. If you are working with natural units then the coordinates should be in your natural length unit. For more details on the PDB file format visit <a href="http://www.wwpdb.org/docs.html">http://www.wwpdb.org/docs.html</a>

#### Compulsory keywords

| REFERENCE    | a file in pdb format containing the reference structure and the atoms involved in the CV.  |
|--------------|--|
| LOWER_CUTOFF | only pairs of atoms further than LOWER_CUTOFF are considered in the calculation.   |
| UPPER_CUTOFF | only pairs of atoms closer than UPPER_CUTOFF are considered in the calculation.  |
| ТҮРЕ         | ( default=DRMSD ) what kind of DRMSD would you like to calculate. You can use either the normal DRMSD involving all the distances between the atoms in your molecule. Alternatively, if you have multiple molecules you can use the type INTER-DRMSD to compute DRMSD values involving only those distances between the atoms at least two molecules or the type INTRA-DRMSD to compute DRMSD values involving only those distances between atoms in the same molecule |

#### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically         |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances |

#### **Examples**

The following tells plumed to calculate the distance RMSD between the positions of the atoms in the reference file and their instantaneous position. Only pairs of atoms whose distance in the reference structure is within 0.1 and 0.8 nm are considered.

DRMSD REFERENCE=file.pdb LOWER\_CUTOFF=0.1 UPPER\_CUTOFF=0.8

The following tells plumed to calculate a DRMSD value for a pair of molecules.

DRMSD REFERENCE=file.pdb LOWER\_CUTOFF=0.1 UPPER\_CUTOFF=0.8 TYPE=INTER-DRMSD

In the input reference file (file.pdb) the atoms in each of the two molecules are separated by a TER command as shown below.

| ATOM | 8  | нтз | ALA | 2 | -1.480 | -1.560 | 1.212  | 1.00 | 1.00 | D | ΙA | Н |
|------|----|-----|-----|---|--------|--------|--------|------|------|---|----|---|
| ATOM | 9  | CAY | ALA | 2 | -0.096 | 2.144  | -0.669 | 1.00 | 1.00 | D | ΙA | С |
| ATOM | 10 | HY1 | ALA | 2 | 0.871  | 2.385  | -0.588 | 1.00 | 1.00 | D | ΙA | Н |
| TER  |    |     |     |   |        |        |        |      |      |   |    |   |
| ATOM | 12 | нүз | ALA | 2 | -0.520 | 2.679  | -1.400 | 1.00 | 1.00 | D | ΙA | Н |
| ATOM | 14 | OY  | ALA | 2 | -1.139 | 0.931  | -0.973 | 1.00 | 1.00 | D | ΙA | 0 |
| END  |    |     |     |   |        |        |        |      |      |   |    |   |

In this example the INTER-DRMSD type ensures that the set of distances from which the final quantity is computed involve one atom from each of the two molecules. If this is replaced by INTRA-DRMSD then only those distances involving pairs of atoms that are both in the same molecule are computed.

#### 5.3.2 MULTI-RMSD

This is part of the colvar module

Calculate the RMSD distance moved by a number of separated domains from their positions in a reference structure.

When you have large proteins the calculation of the root mean squared deviation between all the atoms in a reference structure and the instantaneous configuration becomes prohibitively expensive. You may thus instead want to calculate the RMSD between the atoms in a set of domains of your protein and your reference structure. That is to say:

$$d(X, X_r) = \sqrt{\sum_{i} w_i |X_i - X_i'|^2}$$

where here the sum is over the domains of the protein,  $X_i$  represents the positions of the atoms in domain i in the instantaneous configuration and  $X_i'$  is the positions of the atoms in domain i in the reference configuration.  $w_i$  is an optional weight.

The distances for each of the domains in the above sum can be calculated using the DRMSD or RMSD measures or using a combination of these distance. The reference configuration is specified in a pdb file like the one below:

| ATOM | 2  | 0   | ALA | 2 | -0.926 | -2.447 | -0.497 | 1.00 | 1.00 | DIA | 0 |
|------|----|-----|-----|---|--------|--------|--------|------|------|-----|---|
| ATOM | 4  | HNT | ALA | 2 | 0.533  | -0.396 | 1.184  | 1.00 | 1.00 | DIA | Н |
| ATOM | 6  | HT1 | ALA | 2 | -0.216 | -2.590 | 1.371  | 1.00 | 1.00 | DIA | Н |
| MOTA | 7  | HT2 | ALA | 2 | -0.309 | -1.255 | 2.315  | 1.00 | 1.00 | DIA | Н |
| MOTA | 8  | нтз | ALA | 2 | -1.480 | -1.560 | 1.212  | 1.00 | 1.00 | DIA | Н |
| MOTA | 9  | CAY | ALA | 2 | -0.096 | 2.144  | -0.669 | 1.00 | 1.00 | DIA | С |
| ATOM | 10 | HY1 | ALA | 2 | 0.871  | 2.385  | -0.588 | 1.00 | 1.00 | DIA | Н |
| TER  |    |     |     |   |        |        |        |      |      |     |   |
| MOTA | 12 | нүз | ALA | 2 | -0.520 | 2.679  | -1.400 | 1.00 | 1.00 | DIA | Н |
| ATOM | 14 | OY  | ALA | 2 | -1.139 | 0.931  | -0.973 | 1.00 | 1.00 | DIA | 0 |
| MOTA | 16 | HN  | ALA | 2 | 1.713  | 1.021  | -0.873 | 1.00 | 1.00 | DIA | Н |
| MOTA | 18 | HA  | ALA | 2 | 0.099  | -0.774 | -2.218 | 1.00 | 1.00 | DIA | Н |
| ATOM | 19 | CB  | ALA | 2 | 2.063  | -1.223 | -1.276 | 1.00 | 1.00 | DIA | С |
| ATOM | 20 | HB1 | ALA | 2 | 2.670  | -0.716 | -2.057 | 1.00 | 1.00 | DIA | Н |
| MOTA | 21 | HB2 | ALA | 2 | 2.556  | -1.051 | -0.295 | 1.00 | 1.00 | DIA | Н |
| ATOM | 22 | нвз | ALA | 2 | 2.070  | -2.314 | -1.490 | 1.00 | 1.00 | DIA | Н |
| F.ND |    |     |     |   |        |        |        |      |      |     |   |

with the TER keyword being used to separate the various domains in you protein.

Compulsory keywords

| REFERENCE | a file in pdb format containing the reference structure and the atoms involved in the CV. |
|-----------|---|
| TYPE      | ( default=MULTI-SIMPLE ) the manner in which RMSD alignment is performed. Should be       |
|           | MULTI-OPTIMAL, MULTI-OPTIMAL-FAST, MULTI-SIMPLE or MULTI-DRMSD.                           |

#### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically |
|-----------------------|--|
| SQUARED               | ( default=off ) This should be setted if you want MSD instead of RMSD      |

#### **Examples**

The following tells plumed to calculate the RMSD distance between the positions of the atoms in the reference file and their instantaneous position. The Kearseley algorithm for each of the domains.

```
MULTI-RMSD REFERENCE=file.pdb TYPE=MULTI-OPTIMAL
```

The following tells plumed to calculate the RMSD distance btween the positions of the atoms in the domains of reference the reference structure and their instantaneous positions. Here distances are calculated using the DR← MSD measure.

```
MULTI-RMSD REFERENCE=file.pdb TYPE=MULTI-DRMSD
```

in this case it is possible to use the following DRMSD options in the pdb file using the REMARK syntax:

```
NOPBC to calculate distances without PBC LOWER_CUTOFF=# only pairs of atoms further than LOWER_CUTOFF are considered in the calculation UPPER_CUTOFF=# only pairs of atoms further than UPPER_CUTOFF are considered in the calculation
```

### as shown in the following example

```
REMARK NOPBC
REMARK LOWER_CUTOFF=0.1
REMARK UPPER_CUTOFF=0.8
                               -0.926 -2.447 -0.497 1.00 1.00
                                                                      DTA O
ATOM
        2 O ALA 2
         4 HNT ALA 2
6 HT1 ALA 2
ATOM
                                0.533 -0.396
                                               1.184
                                                      1.00
                                                                       DIA
                                               1.371 1.00 1.00
                               -0.216 -2.590
                                                                      DIA H
ATOM
        7 HT2 ALA 2
8 HT3 ALA 2
9 CAY ALA 2
                                               2.315 1.00 1.00
1.212 1.00 1.00
ATOM
                               -0.309 -1.255
                                                                      DIA H
                               -1.480 -1.560
ATOM
                                                                      DIA
                                                                           Η
                               -0.096 2.144 -0.669 1.00 1.00
ATOM
                                                                      DTA C
ATOM
        10 HY1 ALA 2
                               0.871 2.385 -0.588 1.00 1.00
                                                                      DIA H
TER
        12 HY3 ALA
                       2.
                               -0.520 2.679 -1.400 1.00 1.00
                                                                      DTA H
ATOM
        14 OY ALA 2
                             -1.139 0.931 -0.973 1.00 1.00
ATOM
                                                                      DIA O
                      2
                               1.713 1.021 -0.873 1.00 1.00 0.099 -0.774 -2.218 1.00 1.00
        16 HN ALA
                                                                      DIA H
ATOM
ATOM
        18 HA ALA
                                                                      DTA
                                                                           Н
        19 CB ALA
                               2.063 -1.223 -1.276 1.00 1.00
                                                                      DIA C
        20 HB1 ALA 2
21 HB2 ALA 2
22 HB3 ALA 2
                              2.670 -0.716 -2.057 1.00 1.00
2.556 -1.051 -0.295 1.00 1.00
                                                                      DIA H
ATOM
MOTA
                                                                       DIA
                                                                           Н
MOTA
        22 HB3 ALA
                               2.070 -2.314 -1.490 1.00 1.00
                                                                      DIA H
END
```

#### 5.3.3 PCARMSD

This is part of the colvar module

Calculate the PCA components ( see ? and ? ) for a number of provided eigenvectors and an average structure. Performs optimal alignment at every step and reports the rmsd so you know if you are far or close from the average structure. It takes the average structure and eigenvectors in form of a pdb. Note that beta and occupancy values in the pdb are neglected and all the weights are placed to 1 (differently from the RMSD colvar for example)

**Description of components** 

By default the value of the calculated quantity can be referenced elsewhere in the input file by using the label of the action. Alternatively this Action can be used to be used to calculate the following quantities by employing the keywords listed below. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Description  |
|----------|--|
| eig      | the projections on each eigenvalue are stored on values labeled eig-1, eig-2,  |
| residual | the distance of the present configuration from the configuration supplied as AVERAGE in terms of MSD after optimal alignment |

#### Compulsory keywords

| AVERAGE             | a file in pdb format containing the reference structure and the atoms involved in the CV. |
|---------------------|---|
| <b>EIGENVECTORS</b> | a file in pdb format containing the reference structure and the atoms involved in the CV. |

#### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically         |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances |
| SQUARED-ROOT          | ( default=off ) This should be setted if you want RMSD instead of MSD              |

#### **Examples**

PCARMSD AVERAGE=file.pdb EIGENVECTORS=eigenvectors.pdb

The input is taken so to be compatible with the output you get from g\_covar utility of gromacs (suitably adapted to have a pdb input format).

# 5.3.4 RMSD

This is part of the colvar module

Calculate the RMSD with respect to a reference structure.

The aim with this colvar it to calculate something like:

$$d(X, X') = |X - X'|$$

where X is the instantaneous position of all the atoms in the system and X' is the positions of the atoms in some reference structure provided as input. d(X,X') thus measures the distance all the atoms have moved away from this reference configuration. Oftentimes, it is only the internal motions of the structure - i.e. not the translations of the center of mass or the rotations of the reference frame - that are interesting. Hence, when calculating the the root-mean-square deviation between the atoms in two configurations you must first superimpose the two structures in some way. At present PLUMED provides two distinct ways of performing this superposition. The first method is applied when you use TYPE=SIMPLE in the input line. This instruction tells PLUMED that the root mean square deviation is to be calculated after the positions of the geometric centers in the reference and instantaneous configurations are aligned. In other words d(X,x') is to be calculated using:

$$d(X, X') = \sqrt{\sum_{i} \sum_{\alpha}^{x,y,z} \frac{w_i}{\sum_{j} w_j} (X_{i,\alpha} - com_{\alpha}(X) - X'_{i,\alpha} + com_{\alpha}(X'))^2}$$

with

$$com_{\alpha}(X) = \sum_{i} \frac{w'_{i}}{\sum_{j} w'_{j}} X_{i,\alpha}$$

and

$$com_{\alpha}(X') = \sum_{i} \frac{w'_{i}}{\sum_{j} w'_{j}} X'_{i,\alpha}$$

Obviously,  $com_{\alpha}(X)$  and  $com_{\alpha}(X')$  represent the positions of the center of mass in the reference and instantaneous configurations if the weights \$w'\$ are set equal to the atomic masses. If the weights are all set equal to one, however,  $com_{\alpha}(X)$  and  $com_{\alpha}(X')$  are the positions of the geometric centers. Notice that there are sets of weights: w' and w. The first is used to calculate the position of the center of mass (so it determines how the atoms are aligned). Meanwhile, the second is used when calculating how far the atoms have actually been displaced. These weights are assigned in the reference configuration that you provide as input (i.e. the appear in the input file to this action that you set using REFERENCE=whatever.pdb). This input reference configuration consists of a simple pdb file containing the set of atoms for which you want to calculate the RMSD displacement and their positions in the reference configuration. It is important to note that the indices in this pdb need to be set correctly. The indices in this file determine the indices of the instantaneous atomic positions that are used by PLUMED when calculating this colvar. As such if you want to calculate the RMSD distance moved by the 1st, 4th, 6th and 28th atoms in the MD codes input file then the indices of the corresponding reference positions in this pdb file should be set equal to 1, 4, 6 and 28.

The pdb input file should also contain the values of w and w'. In particular, the OCCUPANCY column (the first column after the coordinates) is used provides the values of w' that are used to calculate the position of the centre of mass. The BETA column (the second column after the Cartesian coordinates) is used to provide the w values which are used in the the calculation of the displacement. Please note that it is possible to use fractional values for beta and for the occupancy. However, we recommend you only do this when you really know what you are doing however as the results can be rather strange.

In PDB files the atomic coordinates and box lengths should be in Angstroms unless you are working with natural units. If you are working with natural units then the coordinates should be in your natural length unit. For more details on the PDB file format visit http://www.wwpdb.org/docs.html.

A different method is used to calculate the RMSD distance when you use TYPE=OPTIMAL on the input line. In this case the root mean square deviation is calculated after the positions of geometric centers in the reference and instantaneous configurations are aligned AND after an optimal alignment of the two frames is performed so that motion due to rotation of the reference frame between the two structures is removed. The equation for d(X,X') in this case reads:

$$d(X, X') = \sqrt{\sum_{i} \sum_{\alpha}^{x,y,z} \frac{w_i}{\sum_{j} w_j} [X_{i,\alpha} - com_{\alpha}(X) - \sum_{\beta} M(X, X', w')_{\alpha,\beta} (X'_{i,\beta} - com_{\beta}(X'))]^2}$$

where M(X,X',w') is the optimal alignment matrix which is calculated using the Kearsley ? algorithm. Again different sets of weights are used for the alignment (w') and for the displacement calcuations (w). This gives a great deal of flexibility as it allows you to use a different sets of atoms (which may or may not overlap) for the alignment and displacement parts of the calculation. This may be very useful when you want to calculate how a ligand moves about in a protein cavity as you can use the protein as a reference system and do no alignment of the ligand.

(Note: when this form of RMSD is used to calculate the secondary structure variables (ALPHARMSD, ANTIBE TARMSD and PARABETARMSD all the atoms in the segment are assumed to be part of both the alignment and displacement sets and all weights are set equal to one)

Please note that there are a number of other methods for calculating the distance between the instantaneous configuration and a reference configuration that are available in plumed. More information on these various methods can be found in the section of the manual on Distances from reference configurations.

#### Compulsory keywords

| REFERENCE | a file in pdb format containing the reference structure and the atoms involved in the CV.        |  |
|-----------|--|--|
| TYPE      | ( default=SIMPLE ) the manner in which RMSD alignment is performed. Should be OPTIMAL or SIMPLE. |  |

# **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically |
|-----------------------|--|
| SQUARED               | ( default=off ) This should be setted if you want MSD instead of RMSD      |

#### **Examples**

The following tells plumed to calculate the RMSD distance between the positions of the atoms in the reference file and their instantaneous position. The Kearseley algorithm is used so this is done optimally.

RMSD REFERENCE=file.pdb TYPE=OPTIMAL

**5.3.5 TARGET** 

This is part of the function module

This function measures the pythagorean distance from a particular structure measured in the space defined by some set of collective variables.

Compulsory keywords

| TYPE      | ( default=EUCLIDEAN ) the manner in which the distance should be calculated  |
|-----------|--|
| REFERENCE | a file in pdb format containing the reference structure. In the PDB file the atomic coordinates and box lengths should be in Angstroms unless you are working with natural units. If you are working with natural units then the coordinates should be in your natural length unit. The charges and masses of the atoms (if required) should be inserted in the beta and occupancy columns respectively. For more details on the PDB file format visit http://www.wwpdb.corg/docs.html |

**Options** 

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically |
|-----------------------|--|
| I I                   |  |

**Examples** 

# 5.4 Functions

When performing biased dynamics or analysing a trajectory you may wish to analyse/bias the value of some function of a set of collective variables rather than the values of the collective variables directly. You can do this with PLUMED by using any one of the following list of functions:

| COMBINE       | Calculate a polynomial combination of a set of other variables.                                  |
|---------------|--|
| ENSEMBLE      | Calculates the replica averaging of a collective variable over multiple replicas.                |
| FUNCPATHMSD   | This function calculates path collective variables.  |
| FUNCSUMHILLS  | This function is intended to be called by the command line tool sum_hillsand it is meant         |
|               | to integrate a HILLS file or an HILLS file interpreted as a histogram i a variety of ways.       |
|               | Therefore it is not expected that you use this during your dynamics (it will crash!)             |
| LOCALENSEMBLE | Calculates the average over multiple arguments.  |
| MATHEVAL      | Calculate a combination of variables using a matheval expression.                                |
| PIECEWISE     | Compute a piecewise straight line through its arguments that passes througha set of              |
|               | ordered control points.  |
| SORT          | This function can be used to sort colvars according to their magnitudes.                         |
| STATS         | Calculates statistical properties of a set of collective variables with respect to a set of ref- |
|               | erence values. In particular it calculates and store as components the sum of the squared        |
|               | deviations, the correlation, the slope and the intercept of a linear fit.                        |
|               |  |

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# 5.4.1 COMBINE

This is part of the function module

Calculate a polynomial combination of a set of other variables.

The functional form of this function is

$$C = \sum_{i=1}^{N_{arg}} c_i (x_i - a_i)^{p_i}$$

The coefficients c, the parameters a and the powers p are provided as vectors.

Notice that COMBINE is not able to predict which will be periodic domain of the computed value automatically. The user is thus forced to specify it explicitly. Use PERIODIC=NO if the resulting variable is not periodic, and PERIODIC=A,B where A and B are the two boundaries if the resulting variable is periodic.

Compulsory keywords

| PERIODIC     | if the output of your function is periodic then you should specify the periodicity of the function. If the output is not periodic you must state this using PERIODIC=NO |
|--------------|---|
| COEFFICIENTS | ( default=1.0 ) the coefficients of the arguments in your function  |
| PARAMETERS   | ( default=0.0 ) the parameters of the arguments in your function  |
| POWERS       | ( default=1.0 ) the powers to which you are raising each of the arguments in your function  |

**Options** 

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| NORMALIZE             | ( default=off ) normalize all the coefficents so that in total they are equal to one  |
| ARG                   | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |

# **Examples**

The following input tells plumed to print the distance between atoms 3 and 5 its square (as computed from the x,y,z components) and the distance again as computed from the square root of the square.

```
DISTANCE LABEL=dist ATOMS=3,5 COMPONENTS

COMBINE LABEL=distance2 ARG=dist.x,dist.y,dist.z POWERS=2,2,2 PERIODIC=NO

COMBINE LABEL=distance ARG=distance2 POWERS=0.5 PERIODIC=NO

PRINT ARG=distance,distance2
```

(See also PRINT and DISTANCE).

The following input tells plumed to add a restraint on the cube of a dihedral angle. Notice that since the angle has a periodic domain -pi,pi its cube has a domain -pi\*\*3,pi\*\*3.

```
t: TORSION ATOMS=1,3,5,7
c: COMBINE ARG=t POWERS=3 PERIODIC=-31.0062766802998,31.0062766802998
RESTRAINT ARG=c KAPPA=10 AT=0
```

#### 5.4.2 ENSEMBLE

This is part of the function module

Calculates the replica averaging of a collective variable over multiple replicas.

Each collective variable is averaged separately and stored in a component labelled label.cvlabel.

# **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| REWEIGHT              | ( default=off ) simple REWEIGHT using the latest ARG as energy  |
| CENTRAL               | ( default=off ) calculate a central moment instead of a standard moment   |
| ARG                   | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |
| TEMP                  | the system temperature - this is only needed if you are reweighting   |
| MOMENT                | the moment you want to calculate in alternative to the mean or the variance   |
| POWER                 | the power of the mean (and moment)  |

# **Examples**

The following input tells plumed to calculate the distance between atoms 3 and 5 and the average it over the available replicas.

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dist: DISTANCE ATOMS=3,5
ens: ENSEMBLE ARG=dist
PRINT ARG=dist,ens.dist

(See also PRINT and DISTANCE).

#### 5.4.3 FUNCPATHMSD

This is part of the function module

This function calculates path collective variables.

This is the Path Collective Variables implementation (see ?). This variable computes the progress along a given set of frames that is provided in input ("s" component) and the distance from them ("z" component). It is a function of MSD that are obtained by the joint use of MSD variable and SQUARED flag (see below).

**Description of components** 

By default this Action calculates the following quantities. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Description                |
|----------|----------------------------|
| s        | the position on the path   |
| Z        | the distance from the path |

Compulsory keywords

### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |  |  |  |
|-----------------------|--|--|--|--|
| ARG                   | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, |  |  |  |
| Generated by Doxygen  | ARG2, ARG3   |  |  |  |

| NEIGH_SIZE   | size of the neighbor list  |
|--------------|--|
| NEIGH_STRIDE | how often the neighbor list needs to be calculated in time units |

#### **Examples**

Here below is a case where you have defined three frames and you want to calculate the progress alng the path and the distance from it in p1

```
t1: RMSD REFERENCE=frame_1.dat TYPE=OPTIMAL SQUARED
t2: RMSD REFERENCE=frame_21.dat TYPE=OPTIMAL SQUARED
t3: RMSD REFERENCE=frame_42.dat TYPE=OPTIMAL SQUARED
p1: FUNCPATHMSD ARG=t1,t2,t3 LAMBDA=500.0
PRINT ARG=t1,t2,t3,p1.s,p1.z STRIDE=1 FILE=colvar FMT=%8.4f
```

In this second example is shown how to define a PATH in the CONTACTMAP space:

```
CONTACTMAP ...
ATOMS1=1,2 REFERENCE1=0.1
ATOMS2=3,4 REFERENCE2=0.5
ATOMS3=4,5 REFERENCE3=0.25
ATOMS4=5,6 REFERENCE4=0.0
SWITCH=(RATIONAL R_0=1.5)
LABEL=c1
CMDIST
... CONTACTMAP
CONTACTMAP ...
ATOMS1=1,2 REFERENCE1=0.3
ATOMS2=3,4 REFERENCE2=0.9
ATOMS3=4,5 REFERENCE3=0.45
ATOMS4=5,6 REFERENCE4=0.1
SWITCH=(RATIONAL R_0=1.5)
LABEL=c2
CMDIST
... CONTACTMAP
CONTACTMAP ...
ATOMS1=1,2 REFERENCE1=1.0
ATOMS2=3,4 REFERENCE2=1.0
ATOMS3=4,5 REFERENCE3=1.0
ATOMS4=5,6 REFERENCE4=1.0
SWITCH=(RATIONAL R_0=1.5)
LABEL=c3
CMDIST
... CONTACTMAP
p1: FUNCPATHMSD ARG=c1,c2,c3 LAMBDA=500.0
PRINT ARG=c1,c2,c3,p1.s,p1.z STRIDE=1 FILE=colvar FMT=%8.4f
```

#### 5.4.4 FUNCSUMHILLS

This is part of the function module

This function is intended to be called by the command line tool sum\_hills and it is meant to integrate a HILLS file or an HILLS file interpreted as a histogram i a variety of ways. Therefore it is not expected that you use this during your dynamics (it will crash!)

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In the future one could implement periodic integration during the metadynamics or straightforward MD as a tool to check convergence

# **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |  |  |  |
|-----------------------|--|--|--|--|
| ISCLTOOL              | ( default=on ) use via plumed commandline: calculate at read phase and then  |  |  |  |
|                       | go   |  |  |  |
| PARALLELREAD          | ( default=off ) read parallel HILLS file   |  |  |  |
| NEGBIAS               | ( default=off ) dump negative bias ( -bias ) instead of the free energy: needed  |  |  |  |
|                       | in welltempered with flexible hills  |  |  |  |
| NOHISTORY             | ( default=off ) to be used with INITSTRIDE: it splits the bias/histogram in pieces   |  |  |  |
|                       | without previous history   |  |  |  |
| MINTOZERO             | ( default=off ) translate the resulting bias/histogram to have the minimum to zero   |  |  |  |
|                       | 2010   |  |  |  |
| ARG                   | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new  |  |  |  |
|                       | action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three components x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |  |  |  |
| HILLSFILES            | source file for hills creation(may be the same as HILLS)   |  |  |  |
| HISTOFILES            | source file for histogram creation(may be the same as HILLS)   |  |  |  |
| HISTOSIGMA            | sigmas for binning when the histogram correction is needed   |  |  |  |
| PROJ                  | only with sumhills: the projection on the cvs  |  |  |  |
| КТ                    | only with sumhills: the kt factor when projection on cvs   |  |  |  |
| GRID_MIN              | the lower bounds for the grid  |  |  |  |
| GRID_MAX              | the upper bounds for the grid  |  |  |  |
| GRID_BIN              | the number of bins for the grid  |  |  |  |
| GRID_SPACING          | the approximate grid spacing (to be used as an alternative or together with GRID_BIN)  |  |  |  |
| INTERVAL              | set monodimensional INTERVAL   |  |  |  |
| OUTHILLS              | output file for hills  |  |  |  |
| OUTHISTO              | output file for histogram  |  |  |  |
| INITSTRIDE            | stride if you want an initial dump   |  |  |  |
| STRIDE                | stride when you do it on the fly   |  |  |  |
| FMT                   | the format that should be used to output real numbers  |  |  |  |

Examples

There are currently no examples for this keyword.

# 5.4.5 LOCALENSEMBLE

This is part of the function module

Calculates the average over multiple arguments.

If more than one collective variable is given for each argument then they are averaged separately. The average is stored in a component labelled *label*.cvlabel.

Compulsory keywords

**NUM** the number of local replicas

#### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| ARG                   | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |

# **Examples**

The following input tells plumed to calculate the chemical shifts for four different proteins in the same simulation box then average them, calculated the sum of the squared deviation with respect to the experiemntal values and applies a linear restraint.

```
MOLINFO STRUCTURE=data/template.pdb

chaina: GROUP ATOMS=1-1640
chainb: GROUP ATOMS=1641-3280
chainc: GROUP ATOMS=3281-4920
chaind: GROUP ATOMS=4921-6560

WHOLEMOLECULES ENTITYO=chaina ENTITY1=chainb ENTITY2=chainc ENTITY3=chaind

csa: CS2BACKBONE ATOMS=chaina NRES=100 DATA=data/ TEMPLATE=chaina.pdb NOPBC
```

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```
csb: CS2BACKBONE ATOMS=chainb NRES=100 DATA=data/ TEMPLATE=chainb.pdb NOPBC
csc: CS2BACKBONE ATOMS=chainc NRES=100 DATA=data/ TEMPLATE=chainc.pdb NOPBC
csd: CS2BACKBONE ATOMS=chaind NRES=100 DATA=data/ TEMPLATE=chaind.pdb NOPBC

ensca: LOCALENSEMBLE NUM=4 ARG1=(csa\.ca_.*) ARG2=(csb\.ca_.*) ARG3=(csc\.ca_.*) ARG4=(csd\.ca_.*)
enscb: LOCALENSEMBLE NUM=4 ARG1=(csa\.cb_.*) ARG2=(csb\.cb_.*) ARG3=(csc\.cb_.*) ARG4=(csd\.cb_.*)
ensco: LOCALENSEMBLE NUM=4 ARG1=(csa\.co_.*) ARG2=(csb\.co_.*) ARG3=(csc\.co_.*) ARG4=(csd\.co_.*)
enshn: LOCALENSEMBLE NUM=4 ARG1=(csa\.hn_.*) ARG2=(csb\.hn_.*) ARG3=(csc\.hn_.*) ARG4=(csd\.hn_.*)
ensh: LOCALENSEMBLE NUM=4 ARG1=(csa\.hn_.*) ARG2=(csb\.hn_.*) ARG3=(csc\.hn_.*) ARG4=(csd\.hn_.*)
ensh: LOCALENSEMBLE NUM=4 ARG1=(csa\.hn_.*) ARG2=(csb\.hn_.*) ARG3=(csc\.hn_.*) ARG4=(csd\.hn_.*)
ensh: LOCALENSEMBLE NUM=4 ARG1=(csa\.hn_.*) ARG2=(csb\.nh_.*) ARG3=(csc\.hn_.*) ARG4=(csd\.hn_.*)
ensh: LOCALENSEMBLE NUM=4 ARG1=(csa\.hn_.*) ARG2=(csb\.nh_.*) ARG3=(csc\.hn_.*) ARG4=(csd\.hn_.*)
ensh: LOCALENSEMBLE NUM=4 ARG1=(csa\.hn_.*) ARG2=(csb\.nh_.*) ARG3=(csc\.hn_.*) ARG4=(csd\.hn_.*)
ensh: LOCALENSEMBLE NUM=4 ARG1=(csa\.hn_.*) ARG2=(csb\.hn_.*) ARG3=(csc\.hn_.*) ARG4=(csd\.hn_.*)
ensh: LOCALENSEMBLE NUM=4 ARG1=(csa\.hn_.*) ARG2=(csb\.hn_.*) ARG3=(csc\.hn_.*) ARG4=(csd\.hn_.*)
ensh: LOCALENSEMBLE NUM=4 ARG1=(csa\.hn_.*) ARG2=(csb\.hn_.*) ARG3=(csc\.hn_.*) ARG4=(csd\.hn_.*)
ensh: LOCALENSEMBLE NUM=4 ARG1=(csa\.hn_.*) PARARG=(csa\.expco_.*) SQDEVSUM
ensh: LOCALENSEMBLE NUM=4 ARG1=(csa\.hn_.*) PARARG=(csa\.expco_.*) SQDEVSUM
ensh: LOCALENSEMBLE NUM=4 ARG1=(csa\.hn_.*) PARARG=(csa\.exphn_.*) SQDEVSUM
ensh: LOCALENSEMBLE NUM=4 ARG
```

#### 5.4.6 MATHEVAL

This is part of the function module

Calculate a combination of variables using a matheval expression.

This action computes an arbitrary function of one or more precomputed collective variables. Arguments are chosen with the ARG keyword, and the function is provided with the FUNC string. Notice that this string should contain no space. Within FUNC, one can refer to the arguments as x,y,z, and t (up to four variables provided as ARG). This names can be customized using the VAR keyword (see examples below).

If you want a function that depends not only on collective variables but also on time you can use the TIME action.

#### Attention

The MATHEVAL object only works if libmatheval is installed on the system and PLUMED has been linked to it

#### Compulsory keywords

| PERIODIC | if the output of your function is periodic then you should specify the periodicity of the function. If the output is not periodic you must state this using PERIODIC=NO |
|----------|---|
| FUNC     | the function you wish to evaluate   |

#### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically |
|-----------------------|--|
|                       |  |

| ARG | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |
|-----|---|
| VAR | the names to give each of the arguments in the function. If you have up to three arguments in your function you can use x, y and z to refer to them. Otherwise you must use this flag to give your variables names.   |

#### **Examples**

The following input tells plumed to perform a metadynamics using as a CV the difference between two distances.

```
daB: DISTANCE ARG=10,12
daC: DISTANCE ARG=10,15
diff: MATHEVAL ARG=dAB,dAC FUNC=y-x PERIODIC=NO
# notice: the previous line could be replaced with the following
# diff: COMBINE ARG=dAB,dAC COEFFICIENTS=-1,1
METAD ARG=diff WIDTH=0.1 HEIGHT=0.5 BIASFACTOR=10 PACE=100
```

(see also DISTANCE, COMBINE, and METAD). Notice that forces applied to diff will be correctly propagated to atoms 10, 12, and 15. Also notice that since MATHEVAL is used without the VAR option the two arguments should be referred to as x and y in the expression FUNC. For simple functions such as this one it is possible to use COMBINE, which does not require libmatheval to be installed on your system.

The following input tells plumed to print the angle between vectors identified by atoms 1,2 and atoms 2,3 its square (as computed from the x,y,z components) and the distance again as computed from the square root of the square.

```
DISTANCE LABEL=d1 ATOMS=1,2 COMPONENTS
DISTANCE LABEL=d2 ATOMS=2,3 COMPONENTS
MATHEVAL ...

LABEL=theta
ARG=d1.x,d1.y,d1.z,d2.x,d2.y,d2.z
VAR=ax,ay,az,bx,by,bz
FUNC=acos((ax*bx+ay*by+az*bz)/sqrt((ax*ax+ay*ay+az*az)*(bx*bx+by*by+bz*bz))
PERIODIC=NO
... MATHEVAL
PRINT ARG=theta
```

#### (See also PRINT and DISTANCE).

Notice that the matheval library implements a large number of functions (trigonometric, exp, log, etc). Among the useful functions, have a look at the step function (that is the Heaviside function). step(x) is defined as 1 when x is positive and 0 when x is negative. This allows for a straightforward implementation of if clauses.

For example, imagine that you want to implement a restraint that only acts when a distance is larger than 0.5. You can do it with

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```
d: DISTANCE ATOMS=10,15
m: MATHEVAL ARG=d FUNC=0.5*step(0.5-x)+x*step(x-0.5) PERIODIC=NO
# check the function you are applying:
PRINT ARG=d,n FILE=checkme
RESTRAINT ARG=d AT=0.5 KAPPA=10.0
```

(see also DISTANCE, PRINT, and RESTRAINT)

The meaning of the function 0.5\*step(0.5-x)+x\*step(x-0.5) is:

- If x<0.5 (step(0.5-x)!=0) use 0.5
- If x>0.5 (step(x-0.5)!=0) use x Notice that the same could have been obtained using an UPPER\_WALLS However, with MATHEVAL you can create way more complex definitions.

#### Warning

If you apply forces on the variable (as in the previous example) you should make sure that the variable is continuous! Conversely, if you are just analyzing a trajectory you can safely use discontinuous variables.

A possible continuity check with gnuplot is

```
# this allow to step function to be used in gnuplot: gnuplot> step(x)=0.5*(erf(x*10000000)+1) # here you can test your function gnuplot> p 0.5*step(0.5-x)+x*step(x-0.5)
```

Also notice that you can easily make logical operations on the conditions that you create. The equivalent of the AND operator is the product: step(1.0-x)\*step(x-0.5) is only equal to 1 when x is between 0.5 and 1.0. By combining negation and AND you can obtain an OR. That is, 1-step(1.0-x)\*step(x-0.5) is only equal to 1 when x is outside the 0.5-1.0 interval.

MATHEVAL can be used in combination with DISTANCE to implement variants of the DISTANCE keyword that were present in PLUMED 1.3 and that allowed to compute the distance of a point from a line defined by two other points, or the progression along that line.

```
# take center of atoms 1 to 10 as reference point 1
p1: CENTER ATOMS=1-10
 # take center of atoms 11 to 20 as reference point 2
p2: CENTER ATOMS=11-20
 # take center of atoms 21 to 30 as reference point 3
p3: CENTER ATOMS=21-30
 # compute distances
 d12: DISTANCE ATOMS=p1,p2
d13: DISTANCE ATOMS=p1,p3
d23: DISTANCE ATOMS=p2,p3
 # compute progress variable of the projection of point p3
 # along the vector joining p1 and p2
 # notice that progress is measured from the middle point
onaxis: MATHEVAL ARG=d13,d23,d12 FUNC=(0.5*(y^2-x^2)/z) PERIODIC=NO
 # compute between point p3 and the vector joining p1 and p2
  from axis: MATHEVAL \ ARG=d13, d23, d12, on axis \ VAR=x, y, z, o \ FUNC=(0.5*(y^2+x^2)-o^2-0.25*z^2) \ PERIODIC=NO(0.5*(y^2+x^2)-0.25*z^2) \ P
PRINT ARG=onaxis.fromaxis
```

Notice that these equations have been used to combine RMSD from different snapshots of a protein so as to define progression (S) and distance (Z) variables ?.

5.4.6.1 TIME

This is part of the generic module

retrieve the time of the simulation to be used elsewere

**Options** 

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically |
|-----------------------|--|
|                       |  |

#### **Examples**

TIME LABEL=t1 PRINT ARG=t1

(See also PRINT).

#### 5.4.7 PIECEWISE

This is part of the function module

Compute a piecewise straight line through its arguments that passes through a set of ordered control points.

For variables less than the first (greater than the last) point, the value of the first (last) point is used.

$$\begin{aligned} \frac{y_{i+1} - y_i}{x_{i+1} - x_i}(s - x_i) + y_i; & if x_i < s < x_{i+1} \\ y_N; & if x > x_{N-1} \\ y_1; & if x < x_0 \end{aligned}$$

Control points are passed using the POINT0=... POINT1=... syntax as in the example below

If one argument is supplied, it results in a scalar quantity. If multiple arguments are supplied, it results in a vector of values. Each value will be named as the name of the original argument with suffix \_pfunc.

**Description of components** 

By default this Action calculates the following quantities. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Description  |
|----------|--|
| _pfunc   | one or multiple instances of this quantity will be referenceable elsewhere in the input file. These  |
|          | quantities will be named with the arguments of the function followed by the character string _pfunc.  These quantities tell the user the values of the piecewise functions of each of the arguments. |

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Compulsory keywords

**POINT** 

This keyword is used to specify the various points in the function above. You can use multiple instances of this keyword i.e. POINT1, POINT2, POINT3...

**Options** 

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| ARG                   | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |

# **Examples**

```
dist1: DISTANCE ATOMS=1,10
dist2: DISTANCE ATOMS=2,11

pw: PIECEWISE POINT0=1,10 POINT1=1,PI POINT2=3,10 ARG=dist1
ppww: PIECEWISE POINT0=1,10 POINT1=1,PI POINT2=3,10 ARG=dist1,dist2
PRINT ARG=pw,ppww.dist1_pfunc,ppww.dist2_pfunc
(See also PRINT and DISTANCE).
```

## 5.4.8 SORT

This is part of the function module

This function can be used to sort colvars according to their magnitudes.

**Description of components** 

This function sorts its arguments according to their magnitudes. The lowest argument will be labelled *label.*1, the second lowest will be labelled *label.*2 and so on.

**Options** 

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| ARG                   | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |

# **Examples**

The following input tells plumed to print the distance of the closest and of the farthest atoms to atom 1, chosen among atoms from 2 to 5

```
d12: DISTANCE ATOMS=1,2
d13: DISTANCE ATOMS=1,3
d14: DISTANCE ATOMS=1,4
d15: DISTANCE ATOMS=1,5
sort: SORT ARG=d12,d13,d14,d15
PRINT ARG=sort.1,sort.4
```

(See also PRINT and DISTANCE).

# 5.4.9 STATS

This is part of the function module

Calculates statistical properties of a set of collective variables with respect to a set of reference values. In particular it calculates and store as components the sum of the squared deviations, the correlation, the slope and the intercept of a linear fit.

The reference values can be either provided as values using PARAMETERS or using value without derivatives from other actions using PARARG (for example using experimental values from collective variables such as CS2BAC← KBONE, RDC, NOE, PRE).

**Description of components** 

The names of the components in this action can be customized by the user in the actions input file. However, in addition to these customizable components the following quantities will always be output

| Quantity  | Description  |                 |
|-----------|--|-----------------|
| sqdevsum  | the sum of the squared deviations between arguments and parameters   |                 |
| corr      | the correlation between arguments and parameters                     |                 |
| slope     | the slope of a linear fit between arguments and parameters           |                 |
| intercept | the intercept of a linear fit between arguments and parameters Gener | ated by Doxygen |

5.5 MultiColvar

In addition the following quantities can be calculated by employing the keywords listed below

| Quantity | Keyword | Description   |  |
|----------|---------|---|--|
| sqd      | SQDEV   | the squared deviations between arguments and parameters |  |

#### **Options**

| NUMERICAL DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
|                       | ,   |
| SQDEVSUM              | ( default=off ) calculates only SQDEVSUM  |
| SQDEV                 | ( default=off ) calculates and store the SQDEV as components  |
| UPPERDISTS            | ( default=off ) calculates and store the SQDEV as components  |
| ARG                   | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |
| PARARG                | the input for this action is the scalar output from one or more other actions without derivatives.  |
| PARAMETERS            | the parameters of the arguments in your function  |

# **Examples**

The following input tells plumed to print the distance between three couple of atoms and compare them with three reference distances.

```
d1: DISTANCE ATOMS=10,50
d2: DISTANCE ATOMS=1,100
d3: DISTANCE ATOMS=45,75
st: STATS ARG=d1,d2,d3 PARAMETERS=1.5,4.0,2.0
PRINT ARG=d1,d2,d3,st.*
```

# 5.5 MultiColvar

Oftentimes, when you do not need one of the collective variables described elsewhere in the manual, what you want instead is a function of a distribution of collective variables of a particular type. In other words, you would like to calculate a function something like this:

$$s = \sum_{i} g[f(\{X\}_i)]$$

In this expression g is a function that takes in one argument and f is a function that takes a set of atomic positions as argument. The symbol  $\{X\}_i$  is used to indicate the fact that the function f is evaluated for a number of different

sets of atoms. If you would just like to output the values of all the various f functions you should use the command <code>DUMPMULTICOLVAR</code>

This functionality is useful if you need to calculate a minimum distance or the number of coordination numbers greater than a 3.0. To avoid dupilcating the code to calculate an angle or distance many times and to make it easier to implement very complex collective variables PLUMED provides these sort of collective variables using so-called MultiColvars. MultiColvars are named in this way because a single PLUMED action can be used to calculate a number of different collective variables. For instance the DISTANCES action can be used to calculate the minimum distance, the number of distances less than a certain value, the number of distances within a certain range... A more detailed introduction to multicolvars is provided in this 10-minute video. Descriptions of the various multicolvars that are implemented in PLUMED 2 are given below:

| ANGLES             | Calculate functions of the distribution of angles .  |
|--------------------|--|
| BRIDGE             | Calculate the number of atoms that bridge two parts of a structure   |
| COORDINATIONNUMBER | Calculate the coordination numbers of atoms so that you can then calculate functions of the distribution of coordination numbers such as the minimum, the number less than a certain quantity and so on.               |
| DENSITY            | Calculate functions of the density of atoms as a function of the box. This allows one to calculate the number of atoms in half the box.  |
| DISTANCES          | Calculate the distances between one or many pairs of atoms. You can then calculate functions of the distribution of distances such as the minimum, the number less than a certain quantity and so on.                  |
| FCCUBIC            | Measure how similar the environment around atoms is to that found in a FCC structure.  |
| INPLANEDISTANCES   | Calculate distances in the plane perpendicular to an axis  |
| MOLECULES          | Calculate the vectors connecting a pair of atoms in order to represent the orientation of a molecule.  |
| PLANES             | Calculate the plane perpendicular to two vectors in order to represent the orientation of a planar molecule.   |
| Q3                 | Calculate 3rd order Steinhardt parameters.   |
| Q4                 | Calculate 4th order Steinhardt parameters.   |
| Q6                 | Calculate 6th order Steinhardt parameters.   |
| SIMPLECUBIC        | Calculate whether or not the coordination spheres of atoms are arranged as they would be in a simplecubic structure.   |
| TETRAHEDRAL        | Calculate the degree to which the environment about ions has a tetrahedral order.  |
| TORSIONS           | Calculate whether or not a set of torsional angles are within a particular range.  |
| XANGLES            | Calculate the angles between the vector connecting two atoms and the x axis.   |
| XDISTANCES         | Calculate the x components of the vectors connecting one or many pairs of atoms. You can then calculate functions of the distribution ofvalues such as the minimum, the number less than a certain quantity and so on. |
| XYDISTANCES        | Calculate distance between a pair of atoms neglecting the z-component. You can then calculate functions of the distribution of values such as the minimum, the number less than a certain quantity and so on.          |
| XYTORSIONS         | Calculate the torsional angle around the x axis from the positive y direction.   |
| XZDISTANCES        | Calculate distance between a pair of atoms neglecting the y-component. You can then calculate functions of the distribution ofvalues such as the minimum, the number less than a certain quantity and so on.           |
| XZTORSIONS         | Calculate the torsional angle around the x axis from the positive z direction.   |
| YANGLES            | Calculate the angles between the vector connecting two atoms and the y axis.   |
| YDISTANCES         | Calculate the y components of the vectors connecting one or many pairs of atoms. You can then calculate functions of the distribution ofvalues such as the minimum, the number less than a certain quantity and so on. |
| YXTORSIONS         | Calculate the torsional angle around the y axis from the positive x direction.   |
|                    | 1  |

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| YZDISTANCES | Calculate distance between a pair of atoms neglecting the x-component. You can then calculate functions of the distribution ofvalues such as the minimum, the number less than a certain quantity and so on.           |
|-------------|--|
| YZTORSIONS  | Calculate the torsional angle around the y axis from the positive z direction.   |
| ZANGLES     | Calculate the angles between the vector connecting two atoms and the z axis.   |
| ZDISTANCES  | Calculate the z components of the vectors connecting one or many pairs of atoms. You can then calculate functions of the distribution ofvalues such as the minimum, the number less than a certain quantity and so on. |
| ZXTORSIONS  | Calculate the torsional angle around the z axis from the positive x direction.   |
| ZYTORSIONS  | Calculate the torsional angle around the z axis from the positive y direction.   |

To instruct PLUMED to calculate a multicolvar you give an instruction that looks something like this:

```
NAME <atoms involved> <parameters> <what am I calculating> TOL=0.001 LABEL=label
```

Oftentimes the simplest way to specify the atoms involved is to use multiple instances of the ATOMS keyword i.e. ATOMS1, ATOMS2, ATOMS3,... Separate instances of the quantity specified by NAME are then calculated for each of the sets of atoms. For example if the command issued contains the following:

```
DISTANCES ATOMS1=1,2 ATOMS2=3,4 ATOMS3=5,6
```

The distances between atoms 1 and 2, atoms 3 and 4, and atoms 5 and 6 are calculated. Obviously, generating this sort of input is rather tedious so short cuts are also available many of the collective variables. These are described on the manual pages for the actions.

After specifying the atoms involved you sometimes need to specify some parameters that required in the calculation. For instance, for COORDINATIONNUMBER - the number of atoms in the first coordination sphere of each of the atoms in the system - you need to specify the parameters for a switchingfunction that will tell us whether or not an atom is in the first coordination sphere. Details as to how to do this are provided on the manual pages.

One of the most important keywords for multicolvars is the TOL keyword. This specifies that terms in sums that contribute less than a certain value can be ignored. In addition, it is assumed that the derivative with respect to these terms are essentially zero. By increasing the TOL parameter you can increase the speed of the calculation. Be aware, however, that this increase in speed is only possible because you are lowering the accuracy with which you are computing the quantity of interest.

Once you have specified the base quanties that are to be calculated from the atoms involved and any parameters you need to specify what function of these base quanties is to be calculated. For most multicolvars you can calculate the minimum, the number less than a target value, the number within a certain range, the number more than a target value and the average value directly.

# 5.5.1 MultiColvar functions

It is possible to use multicolvars to calculate complicated collective variables by exploiting the fact that the output from one multicolvar can be used as input to a second multicolvar. One simple way of exploiting this functionality is to filter the atoms based on the value they have for a symmetry function. For example you might want to consider only those atoms that with a COORDINATIONNUMBER higher that a certain threshold when calculating some particularly expensive symmetry function such as Q6. The following methods can thus all be used to filter the values of multicolvars in this way:

| MFILTER_BETWEEN        | This action can be used to filter the colvar values calculated by a multicolvar so that one can compute the mean and so on for only those multicolvars within a certain range.     |
|------------------------|--|
| Celubrated phyborhasis | This action can be used to filter the distribution of colvar values in a multicolvar so that one can compute the mean and so on for only those multicolvars less than a tolerance. |
| MFILTER_MORE           | This action can be used to filter the distribution of colvar values in a multicolvar so that one can compute the mean and so on for only those multicolvars more than a tolerance. |

An alternative way of filtering atoms is to consider only those atoms in a particular part of the simulation box. This can be done by exploiting the following methods

| AROUND          | This quantity can be used to calculate functions of the distribution of collective variables for the atoms that lie in a particular, user-specified part of of the cell.                                |
|-----------------|---|
| CAVITY          | This quantity can be used to calculate functions of the distribution of collective variables for the atoms that lie in a box defined by the positions of four atoms.                                    |
| INCYLINDER      | This quantity can be used to calculate functions of the distribution of collective variables for the atoms that lie in a particular, user-specified part of of the cell.                                |
| INSPHERE        | This quantity can be used to calculate functions of the distribution of collective variables for the atoms that lie in a particular, user-specified part of of the cell.                                |
| TETRAHEDRALPORE | This quantity can be used to calculate functions of the distribution of collective variablesfor the atoms lie that lie in a box defined by the positions of four atoms at the corners of a tetrahedron. |

The idea with these methods is that function of the form:

$$s = \sum_{i} w(\{X\}_i) g[f(\{X\}_i)]$$

can be evaluated where once again g is a function with one argumet and g is a function of a set of atomic positions. The difference from the more general function described earlier is that we now have a weight w which is again a function of the atomic positions. This weight varies between zero and one and it is this weight that is calculated in the list of filtering methods and volume methods described in the lists above.

In addition to these volume and filtering methods it is also possible to calculate the local average of a quantities in the manner described in **?** using the LOCAL\_AVERAGE method. Furthermore, in many cases Q6, MOLECULES and PLANES the symmetry function being evaluated is a vector. You can thus construct a variety of novel collective variables by taking dot products of vectors on adjacent atoms as described below:

| GRADIENT               | Calculate the gradient of the average value of a multicolvar value  |
|------------------------|---|
| INTERMOLECULARTORSIONS | Calculate torsions between vectors on adjacent molecules  |
| LOCAL_AVERAGE          | Calculate averages over spherical regions centered on atoms   |
| LOCAL_Q3               | Calculate the local degree of order around an atoms by taking the average dot product between the $q_3$ vector on the central atom and the $q_3$ vectoron the atoms in the first coordination sphere. |
| LOCAL_Q4               | Calculate the local degree of order around an atoms by taking the average dot product between the $q_4$ vector on the central atom and the $q_4$ vectoron the atoms in the first coordination sphere. |
| LOCAL_Q6               | Calculate the local degree of order around an atoms by taking the average dot product between the $q_6$ vector on the central atom and the $q_6$ vectoron the atoms in the first coordination sphere. |
| NLINKS                 | Calculate number of pairs of atoms/molecules that are "linked"  |
| SMAC                   | Calculate a variant on the SMAC collective variable discussed in ?  |

The final set of functions that you can apply on multicolvars are functions that transform all the colvars calculated using a multicolvar using a function. This can be useful if you are calculating some complicated derived quantity of some simpler quantity. It is also useful if you are calculating a Willard Chandler surface or a histogram. The actions that you can use to perform these transforms are:

| MTRANSFORM_BETWEEN | This action can be useed to transform the colvar values calculated by a multi-<br>colvar using a histogrambead     |
|--------------------|--|
| MTRANSFORM_LESS    | This action can be useed to transform the colvar values calculated by a multi-<br>colvar using a switchingfunction |

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| <br>ITR | A N | $\sim$ 1 | ~ A ~ | 1 N | $\sim$ | $\neg$ |
|---------|-----|----------|-------|-----|--------|--------|
|         |     |          |       |     |        |        |
|         |     |          |       |     |        |        |

This action can be useed to transform the colvar values calculated by a multicolvar using one minus a switchingfunction

# 5.5.2 MultiColvar bias

There may be occasitions when you want add restraints on many collective variables. For instance if you are studying a cluster you might want to add a wall on the distances between each of the atoms and the center of mass of the cluster in order to prevent the cluster subliming. Alternatively, you may wish to insist that a particular set of atoms in your system all have a coordination number greater than 2. You can add these sorts of restraints by employing the following biases, which all act on the set of collective variable values calculated by a multicolvar. So for example the following set of commands:

```
COM ATOMS=1-20 LABEL=c1
DISTANCES GROUPA=c1 GROUPB=1-20 LABEL=d1
UWALLS DATA=d1 AT=2.5 KAPPA=0.2 LABEL=sr
```

creates the aforementioned set of restraints on the distances between the 20 atoms in a cluster and the center of mass of the cluster.

The list of biases of this type are as follows:

| LWALLS | Add LOWER_WALLS restraints on all the multicolvar values |
|--------|--|
| UWALLS | Add UPPER_WALLS restraints on all the multicolvar values |

Notice that (in theory) you could also use this functionality to add additional terms to your forcefield or to implement your forcefield.

#### **5.5.3 ANGLES**

This is part of the multicolvar module

Calculate functions of the distribution of angles .

You can use this command to calculate functions such as:

$$f(x) = \sum_{ijk} g(\theta_{ijk})$$

Alternatively you can use this command to calculate functions such as:

$$f(x) = \sum_{ijk} s(r_{ij})s(r_{jk})g(\theta_{ijk})$$

where s(r) is a switchingfunction. This second form means that you can use this to calculate functions of the angles in the first coordination sphere of an atom / molecule ?.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

| ATOMS | the atoms involved in each of the collective variables you wish to calculate. Keywords like ATOM←       |
|-------|---|
|       | S1, ATOMS2, ATOMS3, should be listed and one CV will be calculated for each ATOM keyword                |
|       | you specify (all ATOM keywords should define the same number of atoms). The eventual number             |
|       | of quantities calculated by this action will depend on what functions of the distribution you choose to |
|       | calculate. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3                   |

Or alternatively by using

| GROUP | Calculate angles for each distinct set of three atoms in the group |
|-------|--|
|-------|--|

Or alternatively by using

| GROUPA | A group of central atoms about which angles should be calculated   |  |
|--------|--|--|
| GROUPB | When used in conjuction with GROUPA this keyword instructs plumed to calculate all distinct angles involving one atom from GROUPA and two atoms from GROUPB. The atom from GROUPA is the central atom. |  |

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Or alternatively by using

| GROUPC | This must be used in conjuction with GROUPA and GROUPB. All angles involving one atom from |  |
|--------|--|--|
|        | GROUPA, one atom from GROUPB and one atom from GROUPC are calculated. The GROUPA           |  |
|        | atoms are assumed to be the central atoms  |  |

# Options

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances   |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize   |
| LOWMEM                | ( default=off ) lower the memory requirements  |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation  |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA $\leftarrow$ N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3  |
| LESS_THAN             | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_THAN2, LESS_THAN3 The corresponding values are then referenced using <i>label</i> .lessthan-1, <i>label</i> .lessthan-2, <i>label</i> .lessthan-3                                      |
| BETWEEN               | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE∈ EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3  |
| HISTOGRAM             | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |
| MORE_THAN             | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.morethan</code> . You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THA $\sim$ N3 The corresponding values are then referenced using <code>label.morethan-1</code> , <code>label.morethan-2</code> , <code>label.morethan-3</code> |
| SWITCH                | A switching function that ensures that only angles between atoms that are within a certain fixed cutoff are calculated. The following provides information on the switchingfunction that are available.  |
| SWITCHA               | A switching function on the distance between the atoms in group A and the atoms in group B   |
| SWITCHB               | A switching function on the distance between the atoms in group A and the atoms in group B   |

### **Examples**

The following example instructs plumed to find the average of two angles and to print it to a file

```
ANGLES ATOMS1=1,2,3 ATOMS2=4,5,6 MEAN LABEL=a1 PRINT ARG=a1.mean FILE=colvar
```

The following example tells plumed to calculate all angles involving at least one atom from GROUPA and two atoms from GROUPB in which the distances are less than 1.0. The number of angles between  $\frac{\pi}{4}$  and  $\frac{3\pi}{4}$  is then output

```
ANGLES GROUPA=1-10 GROUPB=11-100 BETWEEN={GAUSSIAN LOWER=0.25pi UPPER=0.75pi} SWITCH={GAUSSIAN R_0=1.0} LABEL=PRINT ARG=a1.between FILE=colvar
```

This final example instructs plumed to calculate all the angles in the first coordination spheres of the atoms. A discretized-normalized histogram of the distribution is then output

```
ANGLES GROUP=1-38 HISTOGRAM={GAUSSIAN LOWER=0.0 UPPER=pi NBINS=20} SWITCH={GAUSSIAN R_0=1.0} LABEL=a1 PRINT ARG=a1.* FILE=colvar
```

# **5.5.4 BRIDGE**

This is part of the multicolvar module

Calculate the number of atoms that bridge two parts of a structure

This quantity calculates:

$$f(x) = \sum_{ijk} s_A(r_{ij}) s_B(r_{ik})$$

where the sum over i is over all the "bridging atoms" and  $s_A$  and  $s_B$  are switchingfunction.

The atoms involved can be specified using

# **ATOMS**

the atoms involved in each of the collective variables you wish to calculate. Keywords like ATOM ← S1, ATOMS2, ATOMS3,... should be listed and one CV will be calculated for each ATOM keyword you specify (all ATOM keywords should define the same number of atoms). The eventual number of quantities calculated by this action will depend on what functions of the distribution you choose to calculate. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3...

Or alternatively by using

| BRIDGING_ATOMS | The list of atoms that can form the bridge between the two interesting parts of the struc- |
|----------------|--|
|                | ture.  |
| GROUPA         | The list of atoms that are in the first interesting part of the structure                  |
| GROUPB         | The list of atoms that are in the second interesting part of the structure                 |

### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically                |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-             |
|                       | tances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize                          |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation |
| SWITCH                | The parameters of the two switchingfunction in the above formula                          |
| SWITCHA               | The switchingfunction on the distance between bridging atoms and the atoms in group A     |
| SWITCHB               | The switchingfunction on the distance between the bridging atoms and the atoms in group B |

#### **Examples**

The following example instructs plumed to calculate the number of water molecules that are bridging between atoms 1-10 and atoms 11-20 and to print the value to a file

BRIDGE BRIDGING\_ATOMS=100-200 GROUPA=1-10 GROUPB=11-20 LABEL=w1 PRINT ARG=a1.mean FILE=colvar

## 5.5.5 COORDINATIONNUMBER

This is part of the multicolvar module

Calculate the coordination numbers of atoms so that you can then calculate functions of the distribution of coordination numbers such as the minimum, the number less than a certain quantity and so on.

To make the calculation of coordination numbers differentiable the following function is used:

$$s = \frac{1 - \left(\frac{r - d_0}{r_0}\right)^n}{1 - \left(\frac{r - d_0}{r_0}\right)^m}$$

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

#### **SPECIES**

this keyword is used for colvars such as coordination number. In that context it specifies that plumed should calculate one coordination number for each of the atoms specified. Each of these coordination numbers specifies how many of the other specified atoms are within a certain cutoff of the central atom. You can specify the atoms here as another multicolvar action or using a MultiColvar Filter or ActionVolume action. When you do so the quantity is calculated for those atoms specified in the previous multicolvar. This is useful if you would like to calculate the Steinhardt parameter for those atoms that have a coordination number more than four for example

Or alternatively by using

| SPECIESA | this keyword is used for colvars such as the coordination number. In that context it species that plumed should calculate one coordination number for each of the atoms specified in SPECIESA. Each of these cooordination numbers specifies how many of the atoms specifies using SPEC—IESB is within the specified cutoff. As with the species keyword the input can also be specified using the label of another multicolvar |
|----------|---|
| SPECIESB | this keyword is used for colvars such as the coordination number. It must appear with SPECIESA. For a full explanation see the documentation for that keyword   |

# Compulsory keywords

| NN | ( default=6 ) The n parameter of the switching function                 |
|----|---|
| MM | ( default=0 ) The m parameter of the switching function; 0 implies 2*NN |
| D← | ( default=0.0 ) The d_0 parameter of the switching function             |
| _0 |   |
| R↔ | The r_0 parameter of the switching function                             |
| _0 |   |

| NUMERICAL DERIVATIVES |   |
|-----------------------|---|
| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize  |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation   |
| SWITCH                | This keyword is used if you want to employ an alternative to the continuous swiching function defined above. The following provides information on the switchingfunction that are available. When this keyword is present you no longer need the NN, MM, D_0 and R_0 keywords.  |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA $\leftarrow$ N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3   |
| MORE_THAN             | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.morethan</code> . You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THA $\sim$ N3 The corresponding values are then referenced using <code>label.morethan-1</code> , <code>label.morethan-2</code> , <code>label.morethan-3</code>                            |
| LESS_THAN             | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.lessthan</code> . You can use multiple instances of this keyword i.e. <code>LESS_THAN1</code> , <code>LESS_THAN2</code> , <code>LESS_THAN3</code> The corresponding values are then referenced using <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-3</code> |

| MAX       | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3        |
|-----------|--|
| MIN       | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label.</i> min-1, <i>label.</i> min-2, <i>label.</i> min-3 |
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3   |
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .   |
| ALT_MIN   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3               |
| LOWEST    | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST   | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |

#### **Examples**

The following input tells plumed to calculate the coordination numbers of atoms 1-100 with themselves. The minimum coordination number is then calculated.

```
COORDINATIONNUMBER SPECIES=1-100 R_0=1.0 MIN={BETA=0.1}
```

The following input tells plumed to calculate how many atoms from 1-100 are within 3.0 of each of the atoms from 101-110. In the first 101 is the central atom, in the second 102 is the central atom and so on. The number of coordination numbers more than 6 is then computed.

COORDINATIONNUMBER SPECIESA=101-110 SPECIESB=1-100 R\_0=3.0 MORE\_THAN={RATIONAL R\_0=6.0 NN=6 MM=12 D\_0=0}

### 5.5.6 DENSITY

This is part of the multicolvar module

Calculate functions of the density of atoms as a function of the box. This allows one to calculate the number of atoms in half the box.

The atoms involved can be specified using

#### **SPECIES**

this keyword is used for colvars such as coordination number. In that context it specifies that plumed should calculate one coordination number for each of the atoms specified. Each of these coordination numbers specifies how many of the other specified atoms are within a certain cutoff of the central atom. You can specify the atoms here as another multicolvar action or using a MultiColvar Filter or ActionVolume action. When you do so the quantity is calculated for those atoms specified in the previous multicolvar. This is useful if you would like to calculate the Steinhardt parameter for those atoms that have a coordination number more than four for example

#### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically                |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-             |
|                       | tances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize                          |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation |

### **Examples**

The following example calculates the number of atoms in one half of the simulation box.

DENSITY SPECIES=1-100 LABEL=d

AROUND ARG=d XLOWER=0.0 XUPPER=0.5 LABEL=d1

PRINT ARG=d1.\* FILE=colvar1 FMT=%8.4f

#### 5.5.7 DISTANCES

This is part of the multicolvar module

Calculate the distances between one or many pairs of atoms. You can then calculate functions of the distribution of distances such as the minimum, the number less than a certain quantity and so on.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

#### **ATOMS**

the atoms involved in each of the collective variables you wish to calculate. Keywords like ATOM ← S1, ATOMS2, ATOMS3,... should be listed and one CV will be calculated for each ATOM keyword you specify (all ATOM keywords should define the same number of atoms). The eventual number of quantities calculated by this action will depend on what functions of the distribution you choose to calculate. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3...

Or alternatively by using

# Or alternatively by using

| GROUPA | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPB. |
|--------|---|
| GROUPB | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPA. |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize  |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation   |
| ALT_MIN               | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3  |
| LOWEST                | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest   |
| HIGHEST               | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest   |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA $\leftarrow$ N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3   |
| MIN                   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3                                |
| MAX                   | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3                                       |
| LESS_THAN             | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.lessthan</code> . You can use multiple instances of this keyword i.e. <code>LESS_THAN1</code> , <code>LESS_THAN2</code> , <code>LESS_THAN3</code> The corresponding values are then referenced using <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-3</code> |

| MORE_THAN | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.morethan</code> . You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THANN3 The corresponding values are then referenced using <code>label.morethan-1</code> , <code>label.morethan-2</code> , <code>label.morethan-3</code> |
|-----------|---|
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE← EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3   |
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3   |
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .  |

#### **Examples**

The following input tells plumed to calculate the distances between atoms 3 and 5 and between atoms 1 and 2 and to print the minimum for these two distances.

```
DISTANCES ATOMS1=3,5 ATOMS2=1,2 MIN={BETA=0.1} LABEL=d1 PRINT ARG=d1.min
```

### (See also PRINT).

The following input tells plumed to calculate the distances between atoms 3 and 5 and between atoms 1 and 2 and then to calculate the number of these distances that are less than 0.1 nm. The number of distances less than 0.1 nm is then printed to a file.

```
DISTANCES ATOMS1=3,5 ATOMS2=1,2 LABEL=d1 LESS_THAN={RATIONAL R_0=0.1} PRINT ARG=d1.lt0.1
```

## (See also PRINT switchingfunction).

The following input tells plumed to calculate all the distances between atoms 1, 2 and 3 (i.e. the distances between atoms 1 and 2, atoms 1 and 3 and atoms 2 and 3). The average of these distances is then calculated.

```
DISTANCES GROUP=1-3 MEAN LABEL=d1 PRINT ARG=d1.mean
```

### (See also PRINT)

The following input tells plumed to calculate all the distances between the atoms in GROUPA and the atoms in GROUPB. In other words the distances between atoms 1 and 2 and the distance between atoms 1 and 3. The number of distances more than 0.1 is then printed to a file.

```
DISTANCES GROUPA=1 GROUPB=2,3 MORE_THAN={RATIONAL R_0=0.1} PRINT ARG=d1.gt0.1
```

(See also PRINT switchingfunction)

Calculating minimum distances

To calculate and print the minimum distance between two groups of atoms you use the following commands

```
d1: DISTANCES GROUPA=1-10 GROUPB=11-20 MIN={BETA=500.} PRINT ARG=d1.min FILE=colvar STRIDE=10
```

(see DISTANCES and PRINT)

In order to ensure differentiability the minimum is calculated using the following function:

$$s = \frac{\beta}{\log \sum_{i} \exp\left(\frac{\beta}{s_{i}}\right)}$$

where  $\beta$  is a user specified parameter.

This input is used rather than a separate MINDIST colvar so that the same routine and the same input style can be used to calculate minimum coordinatetion numbers (see COORDINATIONNUMBER), minimum angles (see ANGLES) and many other variables.

This new way of calculating mindist is part of plumed 2's multicolvar functionality. These special actions allow you to calculate multiple functions of a distribution of simple collective variables. As an example you can calculate the number of distances less than 1.0, the minimum distance, the number of distances more than 2.0 and the number of distances between 1.0 and 2.0 by using the following command:

```
DISTANCES ...

GROUPA=1-10 GROUPB=11-20

LESS_THAN={RATIONAL R_0=1.0}

MORE_THAN={RATIONAL R_0=2.0}

BETWEEN={GAUSSIAN LOWER=1.0 UPPER=2.0}

MIN={BETA=500.}

... DISTANCES

PRINT ARG=d1.lessthan,d1.morethan,d1.between,d1.min FILE=colvar STRIDE=10
```

### (see DISTANCES and PRINT)

A calculation performed this way is fast because the expensive part of the calculation - the calculation of all the distances - is only done once per step. Furthermore, it can be made faster by using the TOL keyword to discard those distance that make only a small contributions to the final values together with the NL\_STRIDE keyword, which ensures that the distances that make only a small contribution to the final values aren't calculated at every step.

#### 5.5.8 FCCUBIC

This is part of the crystallization module

It is only available if you configure PLUMED with ./configure –enable-modules=crystallization . FurtherGener 計的 地,Denay Teature is still being developed so take care when using it and report any problems on the mailing list.

Measure how similar the environment around atoms is to that found in a FCC structure.

This CV was introduced in this article ? and again in this article ? This CV essentially determines whether the environment around any given atom is similar to that found in the FCC structure or not. The function that is used to make this determination is as follows:

$$s_{i} = \frac{\sum_{i \neq j} \sigma(r_{ij}) \left\{ a \left[ \frac{(x_{ij}y_{ij})^{4} + (x_{ij}z_{ij})^{4} + (y_{ij}z_{ij})^{4}}{r_{ij}^{8}} - \frac{\alpha(x_{ij}y_{ij}z_{ij})^{4}}{r_{ij}^{12}} \right] + b \right\}}{\sum_{i \neq j} \sigma(r_{ij})}$$

In this expression  $x_{ij}$ ,  $y_{ij}$  and  $z_{ij}$  are the x, y and z components of the vector connecting atom i to atom j and  $r_{ij}$  is the magnitude of this vector.  $\sigma(r_{ij})$  is a switchingfunction that acts on the distance between atom i and atom j and its inclusion in the numerator and the denominator of the above expression as well as the fact that we are summing over all of the other atoms in the system ensures that we are calculating an average of the function of  $x_{ij}$ ,  $y_{ij}$  and  $z_{ij}$  for the atoms in the first coordination sphere around atom i. Lastly,  $\alpha$  is a parameter that can be set by the user, which by default is equal to three. The values of a and b are calculated from  $\alpha$  using:

$$a = \frac{80080}{2717 + 16\alpha}$$
 and  $b = \frac{16(\alpha - 143)}{2717 + 16\alpha}$ 

This quantity is once again a multicolvar so you can compute it for multiple atoms using a single PLUMED action and then compute the average value for the atoms in your system, the number of atoms that have an  $s_i$  value that is more that some target and so on. Notice also that you can rotate the reference frame if you are using a non-standard unit cell.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. <code>label.lessthan-1</code>, <code>label.lessthan-2</code> etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |

| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.   |
|----------|-----------|--|
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean  |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.   |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.   |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |

The atoms involved can be specified using

| SPECIES | this keyword is used for colvars such as coordination number. In that context it specifies that plumed  |
|---------|---|
|         | should calculate one coordination number for each of the atoms specified. Each of these coordi-         |
|         | nation numbers specifies how many of the other specified atoms are within a certain cutoff of the       |
|         | central atom. You can specify the atoms here as another multicolvar action or using a MultiColvar←      |
|         | Filter or ActionVolume action. When you do so the quantity is calculated for those atoms specified      |
|         | in the previous multicolvar. This is useful if you would like to calculate the Steinhardt parameter for |
|         | those atoms that have a coordination number more than four for example                                  |

Or alternatively by using

| SPECIESA | this keyword is used for colvars such as the coordination number. In that context it species that plumed should calculate one coordination number for each of the atoms specified in SPECIESA. Each of these cooordination numbers specifies how many of the atoms specifies using SPEC IESB is within the specified cutoff. As with the species keyword the input can also be specified using the label of another multicolvar |
|----------|---|
| SPECIESB | this keyword is used for colvars such as the coordination number. It must appear with SPECIESA. For a full explanation see the documentation for that keyword   |

# Compulsory keywords

| NN    | ( default=6 ) The n parameter of the switching function                 |
|-------|---|
| ММ    | ( default=0 ) The m parameter of the switching function; 0 implies 2*NN |
| D_0   | ( default=0.0 ) The d_0 parameter of the switching function             |
| R_0   | The r_0 parameter of the switching function                             |
| PHI   | ( default=0.0 ) The Euler rotational angle phi                          |
| THETA | ( default=0.0 ) The Euler rotational angle theta                        |
| PSI   | ( default=0.0 ) The Euler rotational angle psi                          |
| ALPHA | ( default=3.0 ) The alpha parameter of the angular function             |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances   |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize   |
| LOWMEM                | ( default=off ) lower the memory requirements  |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation  |
| SWITCH                | This keyword is used if you want to employ an alternative to the continuous swiching function defined above. The following provides information on the switchingfunction that are available. When this keyword is present you no longer need the NN, MM, D_0 and R_0 keywords.   |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label.</i> mean. You can use multiple instances of this keyword i.e. MEAN1, MEA $\leftarrow$ N2, MEAN3 The corresponding values are then referenced using <i>label.</i> mean-1, <i>label.</i> mean-2, <i>label.</i> mean-3  |
| MORE_THAN             | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .morethan. You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THA N3 The corresponding values are then referenced using <i>label</i> .morethan-1, <i>label</i> .morethan-2, <i>label</i> .morethan-3                           |
| LESS_THAN             | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_THAN2, LESS_THAN3 The corresponding values are then referenced using <i>label</i> .lessthan-1, <i>label</i> .lessthan-2, <i>label</i> .lessthan-3                                  |
| MAX                   | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3        |
| MIN                   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3 |
| BETWEEN               | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE—EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3   |
| HISTOGRAM             | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |

| MOMENTS | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^N(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .   |
|---------|--|
| ALT_MIN | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3 |
| LOWEST  | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |

#### **Examples**

The following input calculates the FCCUBIC parameter for the 64 atoms in the system and then calculates and prints the average value for this quantity.

FCCUBIC SPECIES=1-64 SWITCH={RATIONAL D\_0=3.0 R\_0=1.5} MEAN LABEL=d PRINT ARG=d.\* FILE=colv

### 5.5.9 INPLANEDISTANCES

This is part of the multicolvar module

Calculate distances in the plane perpendicular to an axis

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

| VECTORSTART  | The first atom position that is used to define the normal to the plane of interest. For more information on how to specify lists of atoms see Groups and Virtual Atoms |
|--|--|
| <b>VECTOREND</b> The second atom position that is used to defin the normal to the plane of interest. For information on how to specify lists of atoms see Groups and Virtual Atoms |  |

Or alternatively by using

| <b>GROUP</b> The set of atoms for which you wish to calculate the in plane dista | nce |
|--|-----|
|--|-----|

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically                |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-             |
|                       | tances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize                          |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation |

| ALT_MIN   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using <code>label.altmin</code> . You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using <code>label.altmin-1</code> , <code>label.altmin-2</code> , <code>label.altmin-3</code> |
|-----------|---|
| LOWEST    | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest   |
| HIGHEST   | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest   |
| MEAN      | take the mean of these variables. The final value can be referenced using label.mean. You can use multiple instances of this keyword i.e. MEAN1, MEA—N2, MEAN3 The corresponding values are then referenced using label.mean-1, label.mean-2, label.mean-3  |
| MIN       | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3  |
| MAX       | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3   |
| LESS_THAN | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_THAN2, LESS_THAN3 The corresponding values are then referenced using <i>label</i> .lessthan-1, <i>label</i> .lessthan-2, <i>label</i> .lessthan-3   |
| MORE_THAN | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.morethan</code> . You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THA $\leftarrow$ N3 The corresponding values are then referenced using <code>label.morethan-1</code> , <code>label.morethan-2</code> , <code>label.morethan-3</code>                                |
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE← EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3   |
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3   |
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^N(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .  |

**Examples** 

#### 5.5.10 MOLECULES

This is part of the crystallization module

It is only available if you configure PLUMED with ./configure –enable-modules=crystallization . Further-more, this feature is still being developed so take care when using it and report any problems on the mailing list.

Calculate the vectors connecting a pair of atoms in order to represent the orientation of a molecule.

At its simplest this command can be used to calculate the average length of an internal vector in a collection of different molecules. When used in conjunction with MutiColvarFunctions in can be used to do a variety of more complex tasks.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. <code>label.lessthan-1</code>, <code>label.lessthan-2</code> etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword | Description   |
|----------|---------|---|
| vmean    | VMEAN   | the norm of the mean vector. The output component can be refererred to elsewhere in |
|          |         | the input file by using the label.vmean   |

The atoms involved can be specified using

MOL The numerical indices of the atoms in the molecule. The orientation of the molecule is equal to the vector connecting the first two atoms specified. If a third atom is specified its position is used to specify where the molecule is. If a third atom is not present the molecule is assumed to be at the center of the vector connecting the first two atoms. You can use multiple instances of this keyword i.e. MOL1, MOL2, MOL3...

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize  |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation   |
| VMEAN                 | calculate the norm of the mean vector. The final value can be referenced using label.vmean. You can use multiple instances of this keyword i.e. VMEAN1, VMEAN2, VMEAN3 The corresponding values are then referenced using label.vmean-1, label.vmean-2, label.vmean-3 |

#### **Examples**

The following input tells plumed to calculate the distances between two of the atoms in a molecule. This is done for the same set of atoms four different molecules and the average separation is then calculated.

MOLECULES MOL1=1,2 MOL2=3,4 MOL3=5,6 MOL4=7,8 MEAN LABEL=mm PRINT ARG=mm.mean FILE=colvar

#### 5.5.11 PLANES

This is part of the crystallization module

It is only available if you configure PLUMED with ./configure -enable-modules=crystallization . Furthermore, this feature is still being developed so take care when using it and report any problems on the mailing list.

Calculate the plane perpendicular to two vectors in order to represent the orientation of a planar molecule.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity             | Keyword | Description   |
|----------------------|---------|---|
| vmean                | VMEAN   | the norm of the mean vector. The output component can be refererred to elsewhere in |
| Generated by Doxygen |         | the input file by using the label.vmean   |

The atoms involved can be specified using

MOL

The numerical indices of the atoms in the molecule. If three atoms are specified the orientation of the molecule is taken as the normal to the plane containing the vector connecting the first and second atoms and the vector connecting the second and third atoms. If four atoms are specified the orientation of the molecule is taken as the normal to the plane containing the vector connecting the first and second atoms and the vector connecting the third and fourth atoms. The molecule is always assumed to lie at the geometric centre for the three/four atoms. You can use multiple instances of this keyword i.e. MOL1, MOL2, MOL3...

#### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-   |
|                       | tances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize  |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation   |
| VMEAN                 | calculate the norm of the mean vector. The final value can be referenced using label.vmean. You can use multiple instances of this keyword i.e. VMEAN1, VMEAN2, VMEAN3 The corresponding values are then referenced using label.vmean-1, label.vmean-2, label.vmean-3 |

**Examples** 

#### 5.5.12 Q3

This is part of the crystallization module

It is only available if you configure PLUMED with ./configure -enable-modules=crystallization . Furthermore, this feature is still being developed so take care when using it and report any problems on the mailing list.

Calculate 3rd order Steinhardt parameters.

The 3rd order Steinhardt parameters allow us to measure the degree to which the first coordination shell around an atom is ordered. The Steinhardt parameter for atom, i is complex vector whose components are calculated using the following formula:

$$q_{3m}(i) = \frac{\sum_{j} \sigma(r_{ij}) Y_{3m}(\mathbf{r}_{ij})}{\sum_{j} \sigma(r_{ij})}$$

where  $Y_{3m}$  is one of the 3rd order spherical harmonics so m is a number that runs from -3 to +3. The function  $\sigma(r_{ij})$  is a switchingfunction that acts on the distance between atoms i and j. The parameters of this function

should be set so that it the function is equal to one when atom j is in the first coordination sphere of atom i and is zero otherwise.

The Steinhardt parameters can be used to measure the degree of order in the system in a variety of different ways. The simplest way of measuring whether or not the coordination sphere is ordered is to simply take the norm of the above vector i.e.

$$Q_3(i) = \sqrt{\sum_{m=-3}^{3} q_{3m}(i)^* q_{3m}(i)}$$

This norm is small when the coordination shell is disordered and larger when the coordination shell is ordered. Furthermore, when the keywords LESS\_THAN, MIN, MAX, HISTOGRAM, MEAN and so on are used with this colvar it is the distribution of these normed quantities that is investigated.

Other measures of order can be taken by averaging the components of the individual  $q_3$  vectors individually or by taking dot products of the  $q_3$  vectors on adjacent atoms. More information on these variables can be found in the documentation for LOCAL Q3, LOCAL AVERAGE and NLINKS.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. <code>label.lessthan-1</code>, <code>label.lessthan-2</code> etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity             | Keyword   | Description   |
|----------------------|-----------|---|
| vmean                | VMEAN     | the norm of the mean vector. The output component can be refererred to elsewhere in the input file by using the label.vmean   |
| altmin               | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between              | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest              | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan             | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest               | LOWEST    | the lowest of the quantitities calculated by this action  |
| mean                 | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min                  | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment               | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as   |
| Generated by Doxygen |           | label.moment-3, etc.  |
| morethan             | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

| SPECIES | this keyword is used for colvars such as coordination number. In that context it specifies that plumed  |
|---------|---|
|         | should calculate one coordination number for each of the atoms specified. Each of these coordi-         |
|         | nation numbers specifies how many of the other specified atoms are within a certain cutoff of the       |
|         | central atom. You can specify the atoms here as another multicolvar action or using a MultiColvar ←     |
|         | Filter or ActionVolume action. When you do so the quantity is calculated for those atoms specified      |
|         | in the previous multicolvar. This is useful if you would like to calculate the Steinhardt parameter for |

those atoms that have a coordination number more than four for example

Or alternatively by using

| SPECIESA | this keyword is used for colvars such as the coordination number. In that context it species that plumed should calculate one coordination number for each of the atoms specified in SPECIESA. Each of these cooordination numbers specifies how many of the atoms specifies using SPEC—IESB is within the specified cutoff. As with the species keyword the input can also be specified using the label of another multicolvar |
|----------|---|
| SPECIESB | this keyword is used for colvars such as the coordination number. It must appear with SPECIESA. For a full explanation see the documentation for that keyword   |

# Compulsory keywords

| NN | ( default=12 ) The n parameter of the switching function                |
|----|---|
| MM | ( default=0 ) The m parameter of the switching function; 0 implies 2*NN |
| D↔ | ( default=0.0 ) The d_0 parameter of the switching function             |
| _0 |   |
| R↔ | The r_0 parameter of the switching function                             |
| _0 |   |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-   |
|                       | tances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize  |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation   |
| SWITCH                | This keyword is used if you want to employ an alternative to the continuous swiching function defined above. The following provides information on the switchingfunction that are available. When this keyword is present you no longer need the NN, MM, D_0 and R_0 keywords.                          |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA $\leftarrow$ N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3 |

| LESS_THAN | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_THAN2, LESS_THAN3 The corresponding values are then referenced using <i>label</i> .lessthan-1, <i>label</i> .lessthan-2, <i>label</i> .lessthan-3                                  |
|-----------|--|
| MORE_THAN | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .morethan. You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THAN2 N3 The corresponding values are then referenced using <i>label</i> .morethan-1, <i>label</i> .morethan-2, <i>label</i> .morethan-3                         |
| VMEAN     | calculate the norm of the mean vector. The final value can be referenced using label.vmean. You can use multiple instances of this keyword i.e. VMEAN1, VMEAN2, VMEAN3 The corresponding values are then referenced using label.vmean-1, label.vmean-2, label.vmean-3  |
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using label.between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE← EN3 The corresponding values are then referenced using label.between-1, label.between-2, label.between-3  |
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .   |
| MIN       | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3 |
| ALT_MIN   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3               |
| LOWEST    | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST   | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |

## **Examples**

The following command calculates the average Q3 parameter for the 64 atoms in a box of Lennard Jones and prints this quantity to a file called colvar:

```
Q3 SPECIES=1-64 D_0=1.3 R_0=0.2 MEAN LABEL=q3 PRINT ARG=q3.mean FILE=colvar
```

The following command calculates the histogram of Q3 parameters for the 64 atoms in a box of Lennard Jones and prints these quantities to a file called colvar:

```
Q3 SPECIES=1-64 D_0=1.3 R_0=0.2 HISTOGRAM={GAUSSIAN LOWER=0.0 UPPER=1.0 NBINS=20 SMEAR=0.1} LABEL=q3 PRINT ARG=q3.* FILE=colvar
```

The following command could be used to measure the Q3 paramters that describe the arrangement of chlorine ions around the sodium atoms in NaCl. The imagined system here is composed of 64 NaCl formula units and the atoms are arranged in the input with the 64 Na $^+$  ions followed by the 64 Cl $^-$  ions. Once again the average Q3 paramter is calculated and output to a file called colvar

```
Q3 SPECIESA=1-64 SPECIESB=65-128 D_0=1.3 R_0=0.2 MEAN LABEL=q3 PRINT ARG=q3.mean FILE=colvar
```

#### 5.5.13 Q4

#### This is part of the crystallization module

It is only available if you configure PLUMED with ./configure -enable-modules=crystallization . Furthermore, this feature is still being developed so take care when using it and report any problems on the mailing list.

Calculate 4th order Steinhardt parameters.

The 4th order Steinhardt parameters allow us to measure the degree to which the first coordination shell around an atom is ordered. The Steinhardt parameter for atom, i is complex vector whose components are calculated using the following formula:

$$q_{4m}(i) = \frac{\sum_{j} \sigma(r_{ij}) Y_{4m}(\mathbf{r}_{ij})}{\sum_{j} \sigma(r_{ij})}$$

where  $Y_{4m}$  is one of the 4th order spherical harmonics so m is a number that runs from -4 to +4. The function  $\sigma(r_{ij})$  is a switchingfunction that acts on the distance between atoms i and j. The parameters of this function should be set so that it the function is equal to one when atom j is in the first coordination sphere of atom i and is zero otherwise.

The Steinhardt parameters can be used to measure the degree of order in the system in a variety of different ways. The simplest way of measuring whether or not the coordination sphere is ordered is to simply take the norm of the above vector i.e.

$$Q_4(i) = \sqrt{\sum_{m=-4}^{4} q_{4m}(i)^* q_{4m}(i)}$$

This norm is small when the coordination shell is disordered and larger when the coordination shell is ordered. Furthermore, when the keywords LESS\_THAN, MIN, MAX, HISTOGRAM, MEAN and so on are used with this colvar it is the distribution of these normed quantities that is investigated.

Other measures of order can be taken by averaging the components of the individual  $q_4$  vectors individually or by taking dot products of the  $q_4$  vectors on adjacent atoms. More information on these variables can be found in the documentation for LOCAL\_Q4, LOCAL\_AVERAGE and NLINKS.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| vmean    | VMEAN     | the norm of the mean vector. The output component can be refererred to elsewhere in the input file by using the label.vmean   |
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

| S | PE | C | ΙE | S |
|---|----|---|----|---|
|   |    |   |    |   |

this keyword is used for colvars such as coordination number. In that context it specifies that plumed should calculate one coordination number for each of the atoms specified. Each of these coordination numbers specifies how many of the other specified atoms are within a certain cutoff of the central atom. You can specify the atoms here as another multicolvar action or using a MultiColvar Filter or ActionVolume action. When you do so the quantity is calculated for those atoms specified in the previous multicolvar. This is useful if you would like to calculate the Steinhardt parameter for those atoms that have a coordination number more than four for example

# Or alternatively by using

| SPECIESA | this keyword is used for colvars such as the coordination number. In that context it species that plumed should calculate one coordination number for each of the atoms specified in SPECIESA. Each of these cooordination numbers specifies how many of the atoms specifies using SPEC← IESB is within the specified cutoff. As with the species keyword the input can also be specified using the label of another multicolvar |
|----------|--|
| SPECIESB | this keyword is used for colvars such as the coordination number. It must appear with SPECIESA. For a full explanation see the documentation for that keyword  |

# Compulsory keywords

| NN | ( default=12 ) The n parameter of the switching function                |
|----|---|
| MM | ( default=0 ) The m parameter of the switching function; 0 implies 2*NN |
| D↔ | ( default=0.0 ) The d_0 parameter of the switching function             |
| _0 |   |
| R← | The r_0 parameter of the switching function                             |
| _0 |   |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances   |
| SERIAL                |  |
|                       | ( default=off ) do the calculation in serial. Do not parallelize   |
| LOWMEM                | ( default=off ) lower the memory requirements  |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation  |
| SWITCH                | This keyword is used if you want to employ an alternative to the continuous swiching function defined above. The following provides information on the switchingfunction that are available. When this keyword is present you no longer need the NN, MM, D_0 and R_0 keywords.   |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA $\leftarrow$ N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3  |
| LESS_THAN             | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using label.lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_THAN2, LESS_THAN3 The corresponding values are then referenced using label.lessthan-1, label.lessthan-2, label.lessthan-3  |
| MORE_THAN             | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.morethan</code> . You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THA $\sim$ N3 The corresponding values are then referenced using <code>label.morethan-1</code> , <code>label.morethan-2</code> , <code>label.morethan-3</code> |

| VMEAN     | calculate the norm of the mean vector. The final value can be referenced using label.vmean. You can use multiple instances of this keyword i.e. VMEAN1, VMEAN2, VMEAN3 The corresponding values are then referenced using label.vmean-1, label.vmean-2, label.vmean-3  |
|-----------|--|
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWEEN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3  |
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^N(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .   |
| MIN       | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3 |
| ALT_MIN   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3               |
| LOWEST    | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST   | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |

### **Examples**

The following command calculates the average Q4 parameter for the 64 atoms in a box of Lennard Jones and prints this quantity to a file called colvar:

```
Q4 SPECIES=1-64 D_0=1.3 R_0=0.2 MEAN LABEL=q4 PRINT ARG=q4.mean FILE=colvar
```

The following command calculates the histogram of Q4 parameters for the 64 atoms in a box of Lennard Jones and prints these quantities to a file called colvar:

Q4 SPECIES=1-64 D\_0=1.3 R\_0=0.2 HISTOGRAM={GAUSSIAN LOWER=0.0 UPPER=1.0 NBINS=20 SMEAR=0.1} LABEL=q4 PRINT ARG=q4.\* FILE=colvar

The following command could be used to measure the Q4 paramters that describe the arrangement of chlorine ions around the sodium atoms in NaCl. The imagined system here is composed of 64 NaCl formula units and the atoms are arranged in the input with the 64 Na $^+$  ions followed by the 64 Cl $^-$  ions. Once again the average Q4 paramter is calculated and output to a file called colvar

Q4 SPECIESA=1-64 SPECIESB=65-128 D\_0=1.3 R\_0=0.2 MEAN LABEL=q4 PRINT ARG=q4.mean FILE=colvar

#### 5.5.14 Q6

This is part of the crystallization module

It is only available if you configure PLUMED with ./configure -enable-modules=crystallization . Furthermore, this feature is still being developed so take care when using it and report any problems on the mailing list.

Calculate 6th order Steinhardt parameters.

The 6th order Steinhardt parameters allow us to measure the degree to which the first coordination shell around an atom is ordered. The Steinhardt parameter for atom, i is complex vector whose components are calculated using the following formula:

$$q_{6m}(i) = \frac{\sum_{j} \sigma(r_{ij}) Y_{6m}(\mathbf{r}_{ij})}{\sum_{j} \sigma(r_{ij})}$$

where  $Y_{6m}$  is one of the 6th order spherical harmonics so m is a number that runs from -6 to +6. The function  $\sigma(r_{ij})$  is a switchingfunction that acts on the distance between atoms i and j. The parameters of this function should be set so that it the function is equal to one when atom j is in the first coordination sphere of atom i and is zero otherwise.

The Steinhardt parameters can be used to measure the degree of order in the system in a variety of different ways. The simplest way of measuring whether or not the coordination sphere is ordered is to simply take the norm of the above vector i.e.

$$Q_6(i) = \sqrt{\sum_{m=-6}^{6} q_{6m}(i)^* q_{6m}(i)}$$

This norm is small when the coordination shell is disordered and larger when the coordination shell is ordered. Furthermore, when the keywords LESS\_THAN, MIN, MAX, HISTOGRAM, MEAN and so on are used with this colvar it is the distribution of these normed quantities that is investigated.

Other measures of order can be taken by averaging the components of the individual  $q_6$  vectors individually or by taking dot products of the  $q_6$  vectors on adjacent atoms. More information on these variables can be found in the documentation for LOCAL Q6, LOCAL AVERAGE and NLINKS.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| vmean    | VMEAN     | the norm of the mean vector. The output component can be refererred to elsewhere in the input file by using the label.vmean   |
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

#### **SPECIES**

this keyword is used for colvars such as coordination number. In that context it specifies that plumed should calculate one coordination number for each of the atoms specified. Each of these coordination numbers specifies how many of the other specified atoms are within a certain cutoff of the central atom. You can specify the atoms here as another multicolvar action or using a MultiColvar Filter or ActionVolume action. When you do so the quantity is calculated for those atoms specified in the previous multicolvar. This is useful if you would like to calculate the Steinhardt parameter for those atoms that have a coordination number more than four for example

Or alternatively by using

| SPECIESA | this keyword is used for colvars such as the coordination number. In that context it species that plumed should calculate one coordination number for each of the atoms specified in SPECIESA. Each of these cooordination numbers specifies how many of the atoms specifies using SPEC—IESB is within the specified cutoff. As with the species keyword the input can also be specified using the label of another multicolvar |
|----------|---|
| SPECIESB | this keyword is used for colvars such as the coordination number. It must appear with SPECIESA. For a full explanation see the documentation for that keyword   |

# Compulsory keywords

| NN | ( default=12 ) The n parameter of the switching function                |
|----|---|
| MM | ( default=0 ) The m parameter of the switching function; 0 implies 2*NN |
| D← | ( default=0.0 ) The d_0 parameter of the switching function             |
| _0 |   |
| R← | The r_0 parameter of the switching function                             |
| _0 |   |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |  |
|-----------------------|--|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-  |  |
|                       | tances   |  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize   |  |
| LOWMEM                | ( default=off ) lower the memory requirements  |  |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation  |  |
| SWITCH                | This keyword is used if you want to employ an alternative to the continuous swiching function defined above. The following provides information on the switchingfunction that are available. When this keyword is present you no longer need the NN, MM, D_0 and R_0 keywords.   |  |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA $\leftarrow$ N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3  |  |
| LESS_THAN             | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_THAN2, LESS_THAN3 The corresponding values are then referenced using <i>label</i> .lessthan-1, <i>label</i> .lessthan-2, <i>label</i> .lessthan-3                                  |  |
| MORE_THAN             | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.morethan</code> . You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THAN0. N3 The corresponding values are then referenced using <code>label.morethan-1</code> , <code>label.morethan-2</code> , <code>label.morethan-3</code> |  |
| VMEAN                 | calculate the norm of the mean vector. The final value can be referenced using label.vmean. You can use multiple instances of this keyword i.e. VMEAN1, VMEAN2, VMEAN3 The corresponding values are then referenced using label.vmean-1, label.vmean-2, label.vmean-3  |  |

| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogram-   |
|-----------|--|
|           | bead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE← EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3   |
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^N(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .   |
| MIN       | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label.</i> min-1, <i>label.</i> min-2, <i>label.</i> min-3 |
| ALT_MIN   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta} \log \sum_i \exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3            |
| LOWEST    | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST   | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |

### **Examples**

The following command calculates the average Q6 parameter for the 64 atoms in a box of Lennard Jones and prints this quantity to a file called colvar:

```
Q6 SPECIES=1-64 D_0=1.3 R_0=0.2 MEAN LABEL=q6 PRINT ARG=q6.mean FILE=colvar
```

The following command calculates the histogram of Q6 parameters for the 64 atoms in a box of Lennard Jones and prints these quantities to a file called colvar:

```
Q6 SPECIES=1-64 D_0=1.3 R_0=0.2 HISTOGRAM={GAUSSIAN LOWER=0.0 UPPER=1.0 NBINS=20 SMEAR=0.1} LABEL=q6 PRINT ARG=q6.* FILE=colvar
```

The following command could be used to measure the Q6 paramters that describe the arrangement of chlorine ions around the sodium atoms in NaCl. The imagined system here is composed of 64 NaCl formula units and the atoms are arranged in the input with the 64 Na $^+$  ions followed by the 64 Cl $^-$  ions. Once again the average Q6 paramter is calculated and output to a file called colvar

```
Q6 SPECIESA=1-64 SPECIESB=65-128 D_0=1.3 R_0=0.2 MEAN LABEL=q6 PRINT ARG=q6.mean FILE=colvar
```

### 5.5.15 SIMPLECUBIC

This is part of the crystallization module

It is only available if you configure PLUMED with ./configure -enable-modules=crystallization . Furthermore, this feature is still being developed so take care when using it and report any problems on the mailing list.

Calculate whether or not the coordination spheres of atoms are arranged as they would be in a simple cubic structure.

We can measure how similar the environment around atom i is to a simple cubic structure is by evaluating the following quantity:

$$s_{i} = \frac{\sum_{i \neq j} \sigma(r_{ij}) \left[ \frac{x_{ij}^{4} + y_{ij}^{4} + z_{ij}^{4}}{r_{ij}^{4}} \right]}{\sum_{i \neq j} \sigma(r_{ij})}$$

In this expression  $x_{ij}$ ,  $y_{ij}$  and  $z_{ij}$  are the x, y and z components of the vector connecting atom i to atom j and  $r_{ij}$  is the magnitude of this vector.  $\sigma(r_{ij})$  is a switchingfunction that acts on the distance between atom i and atom j and its inclusion in the numerator and the denominator of the above expression as well as the fact that we are summing over all of the other atoms in the system ensures that we are calculating an average of the function of  $x_{ij}$ ,  $y_{ij}$  and  $z_{ij}$  for the atoms in the first coordination sphere around atom i. This quantity is once again a multicolvar so you can compute it for multiple atoms using a single PLUMED action and then compute the average value for the atoms in your system, the number of atoms that have an  $s_i$  value that is more that some target and so on. Notice also that you can rotate the reference frame if you are using a non-standard unit cell.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |  |
|----------|-----------|---|--|
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |  |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |  |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |  |

| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.   |
|----------|-----------|--|
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean  |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.   |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.   |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |

The atoms involved can be specified using

| SPECIES | this keyword is used for colvars such as coordination number. In that context it specifies that plumed should calculate one coordination number for each of the atoms specified. Each of these coordination numbers specifies how many of the other specified atoms are within a certain cutoff of the central atom. You can specify the atoms here as another multicolvar action or using a MultiColvar Filter or ActionVolume action. When you do so the quantity is calculated for those atoms specified in the previous multicolvar. This is useful if you would like to calculate the Steinbardt parameter for |
|---------|---|
|         | in the previous multicolvar. This is useful if you would like to calculate the Steinhardt parameter for those atoms that have a coordination number more than four for example  |

Or alternatively by using

| SPECIESA | this keyword is used for colvars such as the coordination number. In that context it species that plumed should calculate one coordination number for each of the atoms specified in SPECIESA. Each of these cooordination numbers specifies how many of the atoms specifies using SPEC—IESB is within the specified cutoff. As with the species keyword the input can also be specified using the label of another multicolvar |  |
|----------|---|--|
| SPECIESB | SB this keyword is used for colvars such as the coordination number. It must appear with SPECIESA. For a full explanation see the documentation for that keyword  |  |

# Compulsory keywords

| NN    | ( default=6 ) The n parameter of the switching function                 |  |
|-------|---|--|
| ММ    | ( default=0 ) The m parameter of the switching function; 0 implies 2*NN |  |
| D_0   | ( default=0.0 ) The d_0 parameter of the switching function             |  |
| R_0   | The r_0 parameter of the switching function                             |  |
| PHI   | ( default=0.0 ) The Euler rotational angle phi                          |  |
| THETA | ( default=0.0 ) The Euler rotational angle theta                        |  |
| PSI   | ( default=0.0 ) The Euler rotational angle psi                          |  |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances   |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize   |
| LOWMEM                | ( default=off ) lower the memory requirements  |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation  |
| SWITCH                | This keyword is used if you want to employ an alternative to the continuous swiching function defined above. The following provides information on the switchingfunction that are available. When this keyword is present you no longer need the NN, MM, D_0 and R_0 keywords.   |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA $\leftarrow$ N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3  |
| MORE_THAN             | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .morethan. You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THA $\leftarrow$ N3 The corresponding values are then referenced using <i>label</i> .morethan-1, <i>label</i> .morethan-2, <i>label</i> .morethan-3              |
| LESS_THAN             | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_THAN2, LESS_THAN3 The corresponding values are then referenced using <i>label</i> .lessthan-1, <i>label</i> .lessthan-2, <i>label</i> .lessthan-3                                  |
| MAX                   | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3        |
| MIN                   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3 |
| BETWEEN               | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE← EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3  |
| HISTOGRAM             | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |

| MOMENTS | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^N(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .  |
|---------|---|
| ALT_MIN | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta} \log \sum_i \exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3 |
| LOWEST  | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest   |
| HIGHEST | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest   |

#### **Examples**

The following input tells plumed to calculate the simple cubic parameter for the atoms 1-100 with themselves. The mean value is then calculated.

SIMPLECUBIC SPECIES=1-100 R\_0=1.0 MEAN

The following input tells plumed to look at the ways atoms 1-100 are within 3.0 are arranged about atoms from 101-110. The number of simple cubic parameters that are greater than 0.8 is then output

 ${\tt SIMPLECUBIC SPECIESA=101-110 SPECIESB=1-100 R\_0=3.0 MORE\_THAN=\{RATIONAL R\_0=0.8 NN=6 MM=12 D\_0=0\}}$ 

#### 5.5.16 TETRAHEDRAL

This is part of the crystallization module

It is only available if you configure PLUMED with ./configure -enable-modules=crystallization . Furthermore, this feature is still being developed so take care when using it and report any problems on the mailing list.

Calculate the degree to which the environment about ions has a tetrahedral order.

We can measure the degree to which the first coordination shell around any atom, i is tetrahedrally ordered using the following function.

$$s(i) = \frac{1}{\sum_{j} \sigma(r_{ij})} \sum_{j} \sigma(r_{ij}) \left[ \frac{(x_{ij} + y_{ij} + z_{ij})^{3}}{r_{ij}^{3}} + \frac{(x_{ij} - y_{ij} - z_{ij})^{3}}{r_{ij}^{3}} + \frac{(-x_{ij} + y_{ij} - z_{ij})^{3}}{r_{ij}^{3}} + \frac{(-x_{ij} + y_{ij} - z_{ij})^{3}}{r_{ij}^{3}} \right]$$

Here  $r_{ij}$  is the magnitude fo the vector connecting atom i to atom j and  $x_{ij}$ ,  $y_{ij}$  and  $z_{ij}$  are its three components. The function  $\sigma(r_{ij})$  is a switchingfunction that acts on the distance between atoms i and j. The parameters of this function should be set so that the function is equal to one when atom j is in the first coordination sphere of atom i and is zero otherwise.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

### **SPECIES**

this keyword is used for colvars such as coordination number. In that context it specifies that plumed should calculate one coordination number for each of the atoms specified. Each of these coordination numbers specifies how many of the other specified atoms are within a certain cutoff of the central atom. You can specify the atoms here as another multicolvar action or using a MultiColvar Filter or ActionVolume action. When you do so the quantity is calculated for those atoms specified in the previous multicolvar. This is useful if you would like to calculate the Steinhardt parameter for those atoms that have a coordination number more than four for example

# Or alternatively by using

| SPECIESA | this keyword is used for colvars such as the coordination number. In that context it species that plumed should calculate one coordination number for each of the atoms specified in SPECIESA. Each of these cooordination numbers specifies how many of the atoms specifies using SPEC IESB is within the specified cutoff. As with the species keyword the input can also be specified using the label of another multicolvar |
|----------|---|
| SPECIESB | this keyword is used for colvars such as the coordination number. It must appear with SPECIESA. For a full explanation see the documentation for that keyword   |

## Compulsory keywords

| NN    | ( default=6 ) The n parameter of the switching function                 |  |
|-------|---|--|
| ММ    | ( default=0 ) The m parameter of the switching function; 0 implies 2*NN |  |
| D_0   | ( default=0.0 ) The d_0 parameter of the switching function             |  |
| R_0   | The r_0 parameter of the switching function                             |  |
| PHI   | ( default=0.0 ) The Euler rotational angle phi                          |  |
| THETA | ( default=0.0 ) The Euler rotational angle theta                        |  |
| PSI   | ( default=0.0 ) The Euler rotational angle psi                          |  |
|       |   |  |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize  |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation   |
| SWITCH                | This keyword is used if you want to employ an alternative to the continuous switching function defined above. The following provides information on the switchingfunction that are available. When this keyword is present you no longer need the NN, MM, D_0 and R_0 keywords.   |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA $\leftarrow$ N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3   |
| MORE_THAN             | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.morethan</code> . You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THA $\leftrightarrow$ N3 The corresponding values are then referenced using <code>label.morethan-1</code> , <code>label.morethan-2</code> , <code>label.morethan-3</code> |
| LESS_THAN             | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_THAN2, LESS_THAN3 The corresponding values are then referenced using <i>label</i> .lessthan-1, <i>label</i> .lessthan-2,  |
| Generated by Doxygen  | label.lessthan-3  |

| MAX       | calculate the maximum value. To make this quantity continuous the maximum   |
|-----------|---|
| WIPAC     | is calculated using $\max = \beta \log \sum_{i} \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is   |
|           | specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .max.   |
|           | You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3  |
|           | The corresponding values are then referenced using <i>label</i> .max-1, <i>label</i> .max-2,  |
|           | label.max-3   |
| MIN       | calculate the minimum value. To make this quantity continuous the minimum is  |
|           | calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is spec-                                 |
|           | ified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You   |
|           | can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corre-   |
|           | sponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-  |
| DETWEEN   | 3   |
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogram-            |
|           | bead. The final value can be referenced using <i>label</i> between. You can use   |
|           | multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE   |
|           | EN3 The corresponding values are then referenced using <i>label</i> .between-1,   |
|           | label.between-2, label.between-3  |
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut  |
|           | allows you to calculates NBIN quantites like BETWEEN. The final value can   |
|           | be referenced using label.histogram. You can use multiple instances of this   |
|           | keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corre-  |
|           | sponding values are then referenced using label.histogram-1, label.histogram-   |
|           | 2, label.histogram-3  |
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th mo-   |
|           | ment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the  |
|           | average for the distribution. The moments keyword takes a lists of integers as  |
|           | input or a range. Each integer is a value of $m$ . The final calculated values can  |
|           | be referenced using moment- $m$ .   |
| ALT_MIN   | calculate the minimum value. To make this quantity continuous the minimum   |
|           | is calculated using $\min = -\frac{1}{\beta} \log \sum_{i} \exp(-\beta s_i)$ The value of $\beta$ in this function is expected using                                  |
|           | tion is specified using (BETA= $\beta$ ). The final value can be referenced using <i>label</i> .altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, |
|           | ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using   |
|           | label.altmin-1, label.altmin-2, label.altmin-3  |
| LOWEST    | this flag allows you to recover the lowest of these variables. The final value can  |
|           | be referenced using <i>label</i> .lowest  |
| HIGHEST   | this flag allows you to recover the highest of these variables. The final value   |
|           | can be referenced using <i>label</i> .highest   |
|           |   |

### **Examples**

The following command calculates the average value of the tetrahedrality parameter for a set of 64 atoms all of the same type and outputs this quantity to a file called colvar.

```
tt: TETRAHEDRAL SPECIES=1-64 SWITCH={RATIONAL D_0=1.3 R_0=0.2} MEAN PRINT ARG=tt.mean FILE=colvar
```

The following command calculates the number of tetrahedrality parameters that are greater than 0.8 in a set of 10 atoms. In this calculation it is assumed that there are two atom types A and B and that the first coordination sphere of the 10 atoms of type A contains atoms of type B. The formula above is thus calculated for ten different A atoms and within it the sum over j runs over 40 atoms of type B that could be in the first coordination sphere.

tt: TETRAHEDRAL SPECIESA=1-10 SPECIESB=11-40 SWITCH={RATIONAL D\_0=1.3 R\_0=0.2} MORE\_THAN={RATIONAL R\_0=0.8} PRINT ARG=tt.\* FILE=colvar

### 5.5.17 TORSIONS

This is part of the multicolvar module

Calculate whether or not a set of torsional angles are within a particular range.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword | Description   |  |
|----------|---------|---|--|
| between  | BETWEEN | the number/fraction of values within a certain range. This is calculated using one of |  |
|          |         | the formula described in the description of the keyword so as to make it continuous.  |  |
|          |         | You can calculate this quantity multiple times using different parameters.            |  |

The atoms involved can be specified using

the atoms involved in each of the collective variables you wish to calculate. Keywords like ATOM← S1, ATOMS2, ATOMS3,... should be listed and one CV will be calculated for each ATOM keyword you specify (all ATOM keywords should define the same number of atoms). The eventual number of quantities calculated by this action will depend on what functions of the distribution you choose to calculate. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3...

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically                |  |
|-----------------------|---|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-             |  |
|                       | tances  |  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize                          |  |
| LOWMEM                | ( default=off ) lower the memory requirements   |  |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation |  |

| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE← EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3 |
|-----------|---|
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3               |

### **Examples**

The following provides an example of the input for the torsions command

```
TORSIONS ...
ATOMS1=168,170,172,188
ATOMS2=170,172,188,190
ATOMS3=188,190,192,230
LABEL=ab
... TORSIONS
PRINT ARG=ab.* FILE=colvar STRIDE=10
```

Writing out the atoms involved in all the torsions in this way can be rather tedious. Thankfully if you are working with protein you can avoid this by using the MOLINFO command. PLUMED uses the pdb file that you provide to this command to learn about the topology of the protein molecule. This means that you can specify torsion angles using the following syntax:

```
MOLINFO MOLTYPE=protein STRUCTURE=myprotein.pdb
TORSIONS ...
ATOMS1=@phi-3
ATOMS2=@psi-3
ATOMS3=@phi-4
LABEL=ab
... TORSIONS
PRINT ARG=ab FILE=colvar STRIDE=10
```

Here, @phi-3 tells plumed that you would like to calculate the  $\phi$  angle in the third residue of the protein. Similarly @psi-4 tells plumed that you want to calculate the  $\psi$  angle of the 4th residue of the protein.

## **5.5.18 XANGLES**

This is part of the multicolvar module

Calculate the angles between the vector connecting two atoms and the x axis.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

### **ATOMS**

the atoms involved in each of the collective variables you wish to calculate. Keywords like ATOM ← S1, ATOMS2, ATOMS3,... should be listed and one CV will be calculated for each ATOM keyword you specify (all ATOM keywords should define the same number of atoms). The eventual number of quantities calculated by this action will depend on what functions of the distribution you choose to calculate. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3...

Or alternatively by using

# Or alternatively by using

| GROUPA | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPB. |
|--------|---|
| GROUPB | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPA. |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |  |
|-----------------------|---|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances  |  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize  |  |
| LOWMEM                | ( default=off ) lower the memory requirements   |  |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation   |  |
| MAX                   | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is   |  |
|                       | specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3   |  |
| ALT_MIN               | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3  |  |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA $\leftarrow$ N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3   |  |
| MIN                   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label.</i> min-1, <i>label.</i> min-2, <i>label.</i> min-3                                |  |
| LESS_THAN             | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.lessthan</code> . You can use multiple instances of this keyword i.e. <code>LESS_THAN1</code> , <code>LESS_THAN2</code> , <code>LESS_THAN3</code> The corresponding values are then referenced using <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-3</code> |  |
| LOWEST                | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest   |  |
| HIGHEST               | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest   |  |

| MORE_THAN | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.morethan</code> . You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THA $\sim$ N3 The corresponding values are then referenced using <code>label.morethan-1</code> , <code>label.morethan-2</code> , <code>label.morethan-3</code> |
|-----------|--|
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE← EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3  |
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^N(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .   |
| SWITCH    | A switching function that ensures that only angles are only computed when atoms are within are within a certain fixed cutoff. The following provides information on the switchingfunction that are available.  |

## **Examples**

The following input tells plumed to calculate the angles between the x-axis and the vector connecting atom 3 to atom 5 and between the x-axis and the vector connecting atom 1 to atom 2. The minimum of these two quantities is then

```
XANLGES ATOMS1=3,5 ATOMS2=1,2 MIN={BETA=0.1} LABEL=d1
PRINT ARG=d1.min
```

(See also PRINT).

## 5.5.19 XDISTANCES

This is part of the multicolvar module

Calculate the x components of the vectors connecting one or many pairs of atoms. You can then calculate functions of the distribution of values such as the minimum, the number less than a certain quantity and so on.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

### **ATOMS**

the atoms involved in each of the collective variables you wish to calculate. Keywords like ATOM ← S1, ATOMS2, ATOMS3,... should be listed and one CV will be calculated for each ATOM keyword you specify (all ATOM keywords should define the same number of atoms). The eventual number of quantities calculated by this action will depend on what functions of the distribution you choose to calculate. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3...

Or alternatively by using

| distinct pair of atoms in the group | GROUP Calculate the distance between each |
|-------------------------------------|---|
|-------------------------------------|---|

# Or alternatively by using

| GROUPA | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPB. |
|--------|---|
| GROUPB | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPA. |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize  |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation   |
| MAX                   | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3   |
| ALT_MIN               | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using <code>label.altmin</code> . You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using <code>label.altmin-1</code> , <code>label.altmin-2</code> , <code>label.altmin-3</code> |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA← N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3   |
| MIN                   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label.</i> min-1, <i>label.</i> min-2, <i>label.</i> min-3  |
| LESS_THAN             | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_THAN2, LESS_THAN3 The corresponding values are then referenced using <i>label</i> .lessthan-1, <i>label</i> .lessthan-2, <i>label</i> .lessthan-3   |
| LOWEST                | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest   |
| HIGHEST               | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest   |

| MORE_THAN | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.morethan</code> . You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THANN3 The corresponding values are then referenced using <code>label.morethan-1</code> , <code>label.morethan-2</code> , <code>label.morethan-3</code> |
|-----------|---|
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE← EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3   |
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3   |
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .  |

### **Examples**

The following input tells plumed to calculate the x-component of the vector connecting atom 3 to atom 5 and the x-component of the vector connecting atom 1 to atom 2. The minimum of these two quantities is then printed

```
XDISTANCES ATOMS1=3,5 ATOMS2=1,2 MIN={BETA=0.1} LABEL=d1 PRINT ARG=d1.min
```

### (See also PRINT).

The following input tells plumed to calculate the x-component of the vector connecting atom 3 to atom 5 and the x-component of the vector connecting atom 1 to atom 2. The number of values that are less than 0.1nm is then printed to a file.

```
XDISTANCES ATOMS1=3,5 ATOMS2=1,2 LABEL=d1 LESS_THAN={RATIONAL R_0=0.1} PRINT ARG=d1.lt0.1
```

### (See also PRINT switchingfunction).

The following input tells plumed to calculate the x-components of all the distinct vectors that can be created between atoms 1, 2 and 3 (i.e. the vectors between atoms 1 and 2, atoms 1 and 3 and atoms 2 and 3). The average of these quantities is then calculated.

```
XDISTANCES GROUP=1-3 AVERAGE LABEL=d1 PRINT ARG=d1.average
```

## (See also PRINT)

The following input tells plumed to calculate all the vectors connecting the the atoms in GROUPA to the atoms in GROUPB. In other words the vector between atoms 1 and 2 and the vector between atoms 1 and 3. The number of values more than 0.1 is then printed to a file.

```
XDISTANCES GROUPA=1 GROUPB=2,3 MORE_THAN={RATIONAL R_0=0.1}
PRINT ARG=d1.gt0.1
```

## (See also PRINT switchingfunction)

## 5.5.20 XYDISTANCES

This is part of the multicolvar module

Calculate distance between a pair of atoms neglecting the z-component. You can then calculate functions of the distribution of values such as the minimum, the number less than a certain quantity and so on.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

|--|

the atoms involved in each of the collective variables you wish to calculate. Keywords like ATOM← S1, ATOMS2, ATOMS3,... should be listed and one CV will be calculated for each ATOM keyword you specify (all ATOM keywords should define the same number of atoms). The eventual number of quantities calculated by this action will depend on what functions of the distribution you choose to calculate. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3...

Or alternatively by using

Or alternatively by using

| GROUPA | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPB. |
|--------|---|
| GROUPB | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPA. |

| NUMERICAL DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize  |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation   |
| MAX                   | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3 |
| ALT_MIN               | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3        |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA $\leftarrow$ N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3   |

| MIN  LESS_THAN | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <code>label.min</code> . You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <code>label.min-1</code> , <code>label.min-2</code> , <code>label.min-3</code> calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.lessthan</code> . You can use multiple instances of this keyword i.e. <code>LESS_THAN1</code> , <code>LESS_THAN2</code> , <code>LESS_THAN3</code> The corresponding values are then referenced using <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-1</code> , <code>label.lessthan-1</code> , <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-1</code> , <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-2</code> , <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-2</code> , <code>label.lessthan-3</code> , <code>label.lessthan-3</code> , <code>label.lessthan-3</code> , <code>label.lessthan-3</code> , <code>label.lessthan-3</code> , <code>label.lessthan-3</code> , <code>label.lessthan-3, <code>label.lesst</code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code> |
|----------------|--|
| LOWEST         | label.lessthan-3 this flag allows you to recover the lowest of these variables. The final value can be referenced using label.lowest   |
| HIGHEST        | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |
| MORE_THAN      | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .morethan. You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THA $\sim$ N3 The corresponding values are then referenced using <i>label</i> .morethan-1, <i>label</i> .morethan-2, <i>label</i> .morethan-3  |
| BETWEEN        | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using label.between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE← EN3 The corresponding values are then referenced using label.between-1, label.between-2, label.between-3  |
| HISTOGRAM      | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |
| MOMENTS        | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .   |

## **Examples**

The following input tells plumed to calculate the projection of the length of the vector connecting atom 3 to atom 5 and that is projected in the xy-plane and the projection of the length of the vector the vector connecting atom 1 to atom 2 in the xy-plane. The minimum of these two quantities is then printed

(See also PRINT).

# 5.5.21 XYTORSIONS

This is part of the multicolvar module

Calculate the torsional angle around the x axis from the positive y direction.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword | Description   |
|----------|---------|---|
| altmin   | ALT_MIN | the minimum value. This is calculated using the formula described in the description  |
|          |         | of the keyword so as to make it continuous.   |
| between  | BETWEEN | the number/fraction of values within a certain range. This is calculated using one of |
|          |         | the formula described in the description of the keyword so as to make it continuous.  |
|          |         | You can calculate this quantity multiple times using different parameters.            |
| highest  | HIGHEST | the lowest of the quantitities calculated by this action                              |
| lowest   | LOWEST  | the lowest of the quantitities calculated by this action                              |
| max      | MAX     | the maximum value. This is calculated using the formula described in the description  |
|          |         | of the keyword so as to make it continuous.   |
| mean     | MEAN    | the mean value. The output component can be refererred to elsewhere in the input      |
|          |         | file by using the label.mean  |
| min      | MIN     | the minimum value. This is calculated using the formula described in the description  |
|          |         | of the keyword so as to make it continuous.   |
| moment   | MOMENTS | the central moments of the distribution of values. The second moment would be refer-  |
|          |         | enced elsewhere in the input file using label.moment-2, the third as label.moment-3,  |
|          |         | etc.  |

The atoms involved can be specified using

| <b>ATOMS</b> | the atoms involved in each of the collective variables you wish to calculate. Keywords like ATOM        |  |
|--------------|---|--|
|              | S1, ATOMS2, ATOMS3, should be listed and one CV will be calculated for each ATOM keyword                |  |
|              | you specify (all ATOM keywords should define the same number of atoms). The eventual number             |  |
|              | of quantities calculated by this action will depend on what functions of the distribution you choose to |  |
|              | calculate. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3                   |  |

Or alternatively by using

# Or alternatively by using

| GROUPA | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPB. |
|--------|---|
| GROUPB | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPA. |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances   |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize   |
| LOWMEM                | ( default=off ) lower the memory requirements  |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation  |
| MAX                   | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3        |
| ALT_MIN               | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3               |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA← N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3  |
| MIN                   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3 |
| LOWEST                | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST               | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |
| BETWEEN               | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE EN3 The corresponding values are then referenced using <i>label</i> .between-1,  |
| Generated by Doxygen  | label.between-2, label.between-3   |

| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <code>label.histogram</code> . You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <code>label.histogram-1</code> , <code>label.histogram-3</code> |
|-----------|---|
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .          |
| SWITCH    | A switching function that ensures that only angles are only computed when atoms are within are within a certain fixed cutoff. The following provides information on the switchingfunction that are available.   |

### **Examples**

The following input tells plumed to calculate the angle around the x direction between the positive y-axis and the vector connecting atom 3 to atom 5 and the angle around the x direction between the positive y axis and the vector connecting atom 1 to atom 2. The minimum of these two quantities is then output

XYTORSIONS ATOMS1=3,5 ATOMS2=1,2 MIN={BETA=0.1} LABEL=d1 PRINT ARG=d1.min

(See also PRINT).

# 5.5.22 XZDISTANCES

This is part of the multicolvar module

Calculate distance between a pair of atoms neglecting the y-component. You can then calculate functions of the distribution of values such as the minimum, the number less than a certain quantity and so on.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

| ATOMS | the atoms involved in each of the collective variables you wish to calculate. Keywords like ATOM←       |
|-------|---|
|       | S1, ATOMS2, ATOMS3, should be listed and one CV will be calculated for each ATOM keyword                |
|       | you specify (all ATOM keywords should define the same number of atoms). The eventual number             |
|       | of quantities calculated by this action will depend on what functions of the distribution you choose to |
|       | calculate. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3                   |

Or alternatively by using

Or alternatively by using

| GROUPA | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPB. |
|--------|---|
| GROUPB | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPA. |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances   |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize   |
| LOWMEM                | ( default=off ) lower the memory requirements  |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation  |
| MAX                   | calculate the maximum value. To make this quantity continuous the maximum  |
|                       | is calculated using $\max=\beta\log\sum_i\exp\left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is  |
|                       | specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label</i> .max-1, <i>label</i> .max-2, <i>label</i> .max-3  |
| ALT_MIN               | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3               |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA $\leftarrow$ N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3  |
| MIN                   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3 |
| LESS_THAN             | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_THAN2, LESS_THAN3 The corresponding values are then referenced using <i>label</i> .lessthan-1, <i>label</i> .lessthan-2, <i>label</i> .lessthan-3                                  |
| LOWEST                | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST               | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |
| MORE_THAN             | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .morethan. You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THA $\sim$ N3 The corresponding values are then referenced using <i>label</i> .morethan-1, <i>label</i> .morethan-2, <i>label</i> .morethan-3                    |
| BETWEEN               | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE← EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3  |

| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3 |
|-----------|---|
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .                    |

#### **Examples**

See documentation for XYDISTANCES for examples of how to use this command. You just need to substitute XZDISTANCES for XYDISTANCES to investigate the xz component rather than the xy component.

### 5.5.23 XZTORSIONS

This is part of the multicolvar module

Calculate the torsional angle around the x axis from the positive z direction.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. <code>label.lessthan-1</code>, <code>label.lessthan-2</code> etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword | Description   |
|----------|---------|---|
| altmin   | ALT_MIN | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST | the lowest of the quantitities calculated by this action  |
| lowest   | LOWEST  | the lowest of the quantitities calculated by this action  |

| max    | MAX     | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.   |
|--------|---------|--|
| mean   | MEAN    | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean  |
| min    | MIN     | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.   |
| moment | MOMENTS | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc. |

The atoms involved can be specified using

| ATOMS | the atoms involved in each of the collective variables you wish to calculate. Keywords like ATOM↔       |
|-------|---|
|       | S1, ATOMS2, ATOMS3, should be listed and one CV will be calculated for each ATOM keyword                |
|       | you specify (all ATOM keywords should define the same number of atoms). The eventual number             |
|       | of quantities calculated by this action will depend on what functions of the distribution you choose to |
|       | calculate. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3                   |

Or alternatively by using

| <b>GROUP</b> Calculate the distance between each distinct pair of atoms in the group |
|--|
|--|

Or alternatively by using

| GROUPA | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPB. |
|--------|---|
| GROUPB | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPA. |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-   |
|                       | tances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize  |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation   |
| MAX                   | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3 |

| ALT_MIN   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta} \log \sum_i \exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3            |
|-----------|--|
| MEAN      | take the mean of these variables. The final value can be referenced using label.mean. You can use multiple instances of this keyword i.e. MEAN1, MEA—N2, MEAN3 The corresponding values are then referenced using label.mean-1, label.mean-2, label.mean-3   |
| MIN       | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3 |
| LOWEST    | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST   | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE← EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3  |
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .   |
| SWITCH    | A switching function that ensures that only angles are only computed when atoms are within are within a certain fixed cutoff. The following provides information on the switchingfunction that are available.  |

## **Examples**

The following input tells plumed to calculate the angle around the x direction between the positive z-axis and the vector connecting atom 3 to atom 5 and the angle around the x direction between the positive z direction and the vector connecting atom 1 to atom 2. The minimum of these two quantities is then output

```
XZTORSIONS ATOMS1=3,5 ATOMS2=1,2 MIN={BETA=0.1} LABEL=d1 PRINT ARG=d1.min
```

(See also PRINT).

# **5.5.24 YANGLES**

This is part of the multicolvar module

Calculate the angles between the vector connecting two atoms and the y axis.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

| ATOMS |
|-------|
|-------|

the atoms involved in each of the collective variables you wish to calculate. Keywords like ATOM← S1, ATOMS2, ATOMS3,... should be listed and one CV will be calculated for each ATOM keyword you specify (all ATOM keywords should define the same number of atoms). The eventual number of quantities calculated by this action will depend on what functions of the distribution you choose to calculate. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3...

Or alternatively by using

Or alternatively by using

| GROUPA | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPB. |
|--------|---|
| GROUPB | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPA. |

| NUMERICAL DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically                                    |
|-----------------------|---|
|                       |   |
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-                                 |
|                       | tances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize  |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the cal-                            |
|                       | culation  |
|                       |   |
| MAX                   | calculate the maximum value. To make this quantity continuous the maximum                                     |
|                       | is calculated using $\max=eta\log\sum_i\exp\left(rac{s_i}{eta} ight)$ The value of $eta$ in this function is |
|                       | specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .max.                   |
|                       | You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3  |
|                       | The corresponding values are then referenced using label.max-1, label.max-2,                                  |
|                       | label.max-3   |
| ALT_MIN               | calculate the minimum value. To make this quantity continuous the minimum                                     |
|                       | is calculated using $\min = -rac{1}{eta}\log\sum_i\exp\left(-eta s_i ight)$ The value of $eta$ in this func- |
|                       | tion is specified using (BETA= $\beta$ ). The final value can be referenced using                             |
|                       | label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1,                                   |
|                       | ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using   |
|                       | label.altmin-1, label.altmin-2, label.altmin-3  |
| MEAN                  | take the mean of these variables. The final value can be referenced using                                     |
|                       | label.mean. You can use multiple instances of this keyword i.e. MEAN1, MEA                                    |
|                       | N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-                              |
|                       | , ,   |
|                       | 1, label.mean-2, label.mean-3   |

| MIN       | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3     |
|-----------|--|
| LESS_THAN | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_THAN2, LESS_THAN3 The corresponding values are then referenced using <i>label</i> .lessthan-1, <i>label</i> .lessthan-2, <i>label</i> .lessthan-3                                      |
| LOWEST    | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST   | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |
| MORE_THAN | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.morethan</code> . You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THA $\sim$ N3 The corresponding values are then referenced using <code>label.morethan-1</code> , <code>label.morethan-2</code> , <code>label.morethan-3</code> |
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE∈ EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3  |
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^N (s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .  |
| SWITCH    | A switching function that ensures that only angles are only computed when atoms are within are within a certain fixed cutoff. The following provides information on the switchingfunction that are available.  |

# Examples

The following input tells plumed to calculate the angles between the y-axis and the vector connecting atom 3 to atom 5 and between the y-axis and the vector connecting atom 1 to atom 2. The minimum of these two quantities is then

YANLGES ATOMS1=3,5 ATOMS2=1,2 MIN={BETA=0.1} LABEL=d1 PRINT ARG=d1.min

(See also PRINT).

# 5.5.25 YDISTANCES

This is part of the multicolvar module

Calculate the y components of the vectors connecting one or many pairs of atoms. You can then calculate functions of the distribution of values such as the minimum, the number less than a certain quantity and so on.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

## **ATOMS**

the atoms involved in each of the collective variables you wish to calculate. Keywords like ATOM← S1, ATOMS2, ATOMS3,... should be listed and one CV will be calculated for each ATOM keyword you specify (all ATOM keywords should define the same number of atoms). The eventual number of quantities calculated by this action will depend on what functions of the distribution you choose to calculate. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3...

Or alternatively by using

Or alternatively by using

| GROUPA | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPB. |
|--------|---|
| GROUPB | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPA. |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize  |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation   |
| MAX                   | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3 |
| ALT_MIN               | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3        |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA $\leftarrow$ N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3   |

| MIN  LESS_THAN | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <code>label.min</code> . You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <code>label.min-1</code> , <code>label.min-2</code> , <code>label.min-3</code> calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.lessthan</code> . You can use multiple instances of this keyword i.e. <code>LESS_THAN1</code> , <code>LESS_THAN2</code> , <code>LESS_THAN3</code> The corresponding values are then referenced using <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-1</code> , <code>label.lessthan-1</code> , <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-1</code> , <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-2</code> , <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-2</code> , <code>label.lessthan-3</code> , <code>label.lessthan-3</code> , <code>label.lessthan-3</code> , <code>label.lessthan-3</code> , <code>label.lessthan-3</code> , <code>label.lessthan-3</code> , <code>label.lessthan-3, <code>label.lesst</code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code> |
|----------------|--|
| LOWEST         | label.lessthan-3 this flag allows you to recover the lowest of these variables. The final value can be referenced using label.lowest   |
| HIGHEST        | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |
| MORE_THAN      | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .morethan. You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THA $\sim$ N3 The corresponding values are then referenced using <i>label</i> .morethan-1, <i>label</i> .morethan-2, <i>label</i> .morethan-3  |
| BETWEEN        | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using label.between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE← EN3 The corresponding values are then referenced using label.between-1, label.between-2, label.between-3  |
| HISTOGRAM      | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |
| MOMENTS        | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .   |

## **Examples**

See documentation for XDISTANCES for examples of how to use this command. You just need to substitute YDI $\leftarrow$  STANCES for XDISTANCES to investigate the y component rather than the x component.

# 5.5.26 YXTORSIONS

This is part of the multicolvar module

Calculate the torsional angle around the y axis from the positive x direction.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword | Description   |  |
|----------|---------|---|--|
| altmin   | ALT_MIN | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |  |
| between  | BETWEEN | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |  |
| highest  | HIGHEST | HIGHEST the lowest of the quantitities calculated by this action  |  |
| lowest   | LOWEST  | the lowest of the quantitities calculated by this action  |  |
| max      | MAX     | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |  |
| mean     | MEAN    | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |  |
| min      | MIN     | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |  |
| moment   | MOMENTS | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |  |

The atoms involved can be specified using

## **ATOMS**

the atoms involved in each of the collective variables you wish to calculate. Keywords like ATOM ← S1, ATOMS2, ATOMS3,... should be listed and one CV will be calculated for each ATOM keyword you specify (all ATOM keywords should define the same number of atoms). The eventual number of quantities calculated by this action will depend on what functions of the distribution you choose to calculate. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3...

Or alternatively by using

Or alternatively by using

| GROUPA | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. must be used in conjuction with GROUPB.      |  |
|--------|---|--|
| GROUPB | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPA. |  |

| SERIAL ( LOWMEM ( TIMINGS ( COMMAX COMMAX ( SERIAL ( COMMEM ( COMMAX ( SERIAL ( COMMEM ( SERIAL ( SERI | default=off) calculate the derivatives for these quantities numerically  |
|--|--|
| LOWMEM  TIMINGS  (CI MAX  CI SI SI YO T ILE ALT_MIN  CI SI   | default=off) ignore the periodic boundary conditions when calculating disances   |
| TIMINGS  ( cc  MAX  is  sp  You  That  ALT_MIN  cc  is  tit  | default=off ) do the calculation in serial. Do not parallelize   |
| MAX  C: is S  Y( T) Iz  ALT_MIN  C: is tit   | default=off ) lower the memory requirements  |
| ALT_MIN calls to the state of t | default=off) output information on the timings of the various parts of the cal-<br>culation  |
| is<br>tie  | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ . The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using $label.max$ . You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3   |
| A  | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using abel.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using abel.altmin-1, label.altmin-2, label.altmin-3                 |
| la<br>N  | ake the mean of these variables. The final value can be referenced using abel.mean. You can use multiple instances of this keyword i.e. MEAN1, MEA 2, MEAN3 The corresponding values are then referenced using label.mean, label.mean-2, label.mean-3  |
| ca<br>ifi<br>ca<br>sp  | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3 |
| <b>LOWEST</b> th   | his flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest   |
|  | his flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest   |
| tion by the state of the state  | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogramical. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWEEN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-3   |
| HISTOGRAM C: a b k s s 2   | alculate a discretized histogram of the distribution of values. This shortcut  |

| MOMENTS | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ . |
|---------|--|
| SWITCH  | A switching function that ensures that only angles are only computed when atoms are within are within a certain fixed cutoff. The following provides information on the switchingfunction that are available.  |

### **Examples**

The following input tells plumed to calculate the angle around the y direction between the positive x-direction and the vector connecting atom 3 to atom 5 and the angle around the y direction between the positive x axis and the vector connecting atom 1 to atom 2. The minimum of these two quantities is then output

```
YXTORSIONS ATOMS1=3,5 ATOMS2=1,2 MIN={BETA=0.1} LABEL=d1 PRINT ARG=d1.min
```

(See also PRINT).

## 5.5.27 YZDISTANCES

This is part of the multicolvar module

Calculate distance between a pair of atoms neglecting the x-component. You can then calculate functions of the distribution of values such as the minimum, the number less than a certain quantity and so on.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword | Description   |  |
|----------|---------|---|--|
| altmin   | ALT_MIN | the minimum value. This is calculated using the formula described in the descrip- |  |
|          |         | tion of the keyword so as to make it continuous.                                  |  |

| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
|----------|-----------|---|
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

|--|

the atoms involved in each of the collective variables you wish to calculate. Keywords like ATOM ← S1, ATOMS2, ATOMS3,... should be listed and one CV will be calculated for each ATOM keyword you specify (all ATOM keywords should define the same number of atoms). The eventual number of quantities calculated by this action will depend on what functions of the distribution you choose to calculate. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3...

Or alternatively by using

| <b>GROUP</b> Calculate the distance between e | each distinct pair of atoms in the group |
|---|--|
|---|--|

Or alternatively by using

| GROUPA | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPB. |  |
|--------|---|--|
| GROUPB | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPA. |  |

| NOPBC     | ( default=off ) ignore the periodic boundary conditions when calculating distances  |
|-----------|---|
| SERIAL    | ( default=off ) do the calculation in serial. Do not parallelize  |
| LOWMEM    | ( default=off ) lower the memory requirements   |
| TIMINGS   | ( default=off ) output information on the timings of the various parts of the calculation   |
| MAX       | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3                                       |
| ALT_MIN   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3  |
| MEAN      | take the mean of these variables. The final value can be referenced using label.mean. You can use multiple instances of this keyword i.e. MEAN1, MEA—N2, MEAN3 The corresponding values are then referenced using label.mean-1, label.mean-2, label.mean-3  |
| MIN       | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3                                |
| LESS_THAN | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.lessthan</code> . You can use multiple instances of this keyword i.e. <code>LESS_THAN1</code> , <code>LESS_THAN2</code> , <code>LESS_THAN3</code> The corresponding values are then referenced using <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-3</code> |
| LOWEST    | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest   |
| HIGHEST   | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest   |
| MORE_THAN | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.morethan</code> . You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THA $\leftrightarrow$ N3 The corresponding values are then referenced using <code>label.morethan-1</code> , <code>label.morethan-2</code> , <code>label.morethan-3</code>                 |
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE← EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3   |

| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3 |
|-----------|---|
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .                    |

### **Examples**

See documentation for XYDISTANCES for examples of how to use this command. You just need to substitute YZDISTANCES for XYDISTANCES to investigate the yz component rather than the xy component.

### 5.5.28 YZTORSIONS

This is part of the multicolvar module

Calculate the torsional angle around the y axis from the positive z direction.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. <code>label.lessthan-1</code>, <code>label.lessthan-2</code> etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword | Description   |
|----------|---------|---|
| altmin   | ALT_MIN | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST | the lowest of the quantitities calculated by this action  |
| lowest   | LOWEST  | the lowest of the quantitities calculated by this action  |

| max    | MAX     | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.   |
|--------|---------|--|
| mean   | MEAN    | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean  |
| min    | MIN     | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.   |
| moment | MOMENTS | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc. |

The atoms involved can be specified using

| ATOMS | the atoms involved in each of the collective variables you wish to calculate. Keywords like ATOM↔       |
|-------|---|
|       | S1, ATOMS2, ATOMS3, should be listed and one CV will be calculated for each ATOM keyword                |
|       | you specify (all ATOM keywords should define the same number of atoms). The eventual number             |
|       | of quantities calculated by this action will depend on what functions of the distribution you choose to |
|       | calculate. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3                   |

Or alternatively by using

| GROUP | Calculate the distance between each distinct pair of atoms in the group |
|-------|---|
|-------|---|

Or alternatively by using

| GROUPA | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPB. |
|--------|---|
| GROUPB | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPA. |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-   |
|                       | tances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize  |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation   |
| MAX                   | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3 |

| ALT_MIN   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using  |
|-----------|--|
| MEAN      | label.altmin-1, label.altmin-2, label.altmin-3  take the mean of these variables. The final value can be referenced using label.mean. You can use multiple instances of this keyword i.e. MEAN1, MEA← N2, MEAN3 The corresponding values are then referenced using label.mean-1, label.mean-2, label.mean-3  |
| MIN       | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3 |
| LOWEST    | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST   | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWEEN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3  |
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^N(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .   |
| SWITCH    | A switching function that ensures that only angles are only computed when atoms are within are within a certain fixed cutoff. The following provides information on the switchingfunction that are available.  |

# **Examples**

The following input tells plumed to calculate the angle around the y direction between the positive z-direction and the vector connecting atom 3 to atom 5 and the angle around the y direction between the positive z direction and the vector connecting atom 1 to atom 2. The minimum of these two quantities is then output

YZTORSIONS ATOMS1=3,5 ATOMS2=1,2 MIN={BETA=0.1} LABEL=d1 PRINT ARG=d1.min

(See also PRINT).

# **5.5.29 ZANGLES**

This is part of the multicolvar module

Calculate the angles between the vector connecting two atoms and the z axis.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

the atoms involved in each of the collective variables you wish to calculate. Keywords like ATOM ← S1, ATOMS2, ATOMS3,... should be listed and one CV will be calculated for each ATOM keyword you specify (all ATOM keywords should define the same number of atoms). The eventual number of quantities calculated by this action will depend on what functions of the distribution you choose to calculate. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3...

Or alternatively by using

Or alternatively by using

| GROUPA | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPB. |
|--------|---|
| GROUPB | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPA. |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize  |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation   |
| MAX                   | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3 |
| ALT_MIN               | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3        |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA $\leftarrow$ N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3   |

| MIN       | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3           |
|-----------|--|
| LESS_THAN | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_THAN2, LESS_THAN3 The corresponding values are then referenced using <i>label</i> .lessthan-1, <i>label</i> .lessthan-2, <i>label</i> .lessthan-3  |
| LOWEST    | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST   | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |
| MORE_THAN | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.morethan</code> . You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THA $\leftarrow$ N3 The corresponding values are then referenced using <code>label.morethan-1</code> , <code>label.morethan-2</code> , <code>label.morethan-3</code> |
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE← EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3  |
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .   |
| SWITCH    | A switching function that ensures that only angles are only computed when atoms are within are within a certain fixed cutoff. The following provides information on the switchingfunction that are available.  |

### Examples

The following input tells plumed to calculate the angles between the z-axis and the vector connecting atom 3 to atom 5 and between the z-axis and the vector connecting atom 1 to atom 2. The minimum of these two quantities is then

```
ZANLGES ATOMS1=3,5 ATOMS2=1,2 MIN={BETA=0.1} LABEL=d1 PRINT ARG=d1.min
```

(See also PRINT).

## 5.5.30 ZDISTANCES

This is part of the multicolvar module

Calculate the z components of the vectors connecting one or many pairs of atoms. You can then calculate functions of the distribution of values such as the minimum, the number less than a certain quantity and so on.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

the atoms involved in each of the collective variables you wish to calculate. Keywords like ATOM ← S1, ATOMS2, ATOMS3,... should be listed and one CV will be calculated for each ATOM keyword you specify (all ATOM keywords should define the same number of atoms). The eventual number of quantities calculated by this action will depend on what functions of the distribution you choose to calculate. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3...

Or alternatively by using

Or alternatively by using

| GROUPA | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPB. |
|--------|---|
| GROUPB | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPA. |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize  |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation   |
| MAX                   | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label</i> .max-1, <i>label</i> .max-2, <i>label</i> .max-3 |
| ALT_MIN               | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3        |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA $\leftarrow$ N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3   |

| MIN  LESS_THAN | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <code>label.min</code> . You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <code>label.min-1</code> , <code>label.min-2</code> , <code>label.min-3</code> calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.lessthan</code> . You can use multiple instances of this keyword i.e. <code>LESS_THAN1</code> , <code>LESS_THAN2</code> , <code>LESS_THAN3</code> The corresponding values are then referenced using <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-1</code> , <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-1</code> , <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-1</code> , <code>label.lessthan-1</code> , <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-1</code> , <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-1</code> , <code>label.lessthan-1</code> , <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-1</code> , <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-1</code> , <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-2</code> , <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-2</code> , <code>label.lessthan-3</code> , <code>label.lessthan-3</code> , <code>label.lessthan-3</code> , <code>label.lessthan-3</code> , <code>label.lessthan-3</code> , <code>label.lessthan-3</code> , <code>label.lessthan-3, <code>label.lesst</code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code></code> |
|----------------|--|
| LOWEST         | label.lessthan-3 this flag allows you to recover the lowest of these variables. The final value can be referenced using label.lowest   |
| HIGHEST        | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |
| MORE_THAN      | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .morethan. You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THA $\sim$ N3 The corresponding values are then referenced using <i>label</i> .morethan-1, <i>label</i> .morethan-2, <i>label</i> .morethan-3  |
| BETWEEN        | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using label.between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE← EN3 The corresponding values are then referenced using label.between-1, label.between-2, label.between-3  |
| HISTOGRAM      | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |
| MOMENTS        | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .   |

#### **Examples**

See documentation for XDISTANCES for examples of how to use this command. You just need to substitute ZDI $\leftarrow$  STANCES for XDISTANCES to investigate the z component rather than the x component.

## 5.5.31 ZXTORSIONS

This is part of the multicolvar module

Calculate the torsional angle around the z axis from the positive x direction.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword | Description   |
|----------|---------|---|
| altmin   | ALT_MIN | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST | the lowest of the quantitities calculated by this action  |
| lowest   | LOWEST  | the lowest of the quantitities calculated by this action  |
| max      | MAX     | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| mean     | MEAN    | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN     | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |

The atoms involved can be specified using

#### **ATOMS**

the atoms involved in each of the collective variables you wish to calculate. Keywords like ATOM ← S1, ATOMS2, ATOMS3,... should be listed and one CV will be calculated for each ATOM keyword you specify (all ATOM keywords should define the same number of atoms). The eventual number of quantities calculated by this action will depend on what functions of the distribution you choose to calculate. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3...

Or alternatively by using

Or alternatively by using

| GROUPA | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPB. |
|--------|---|
| GROUPB | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPA. |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances   |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize   |
| LOWMEM                | ( default=off ) lower the memory requirements  |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation  |
| MAX                   | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max=\beta\log\sum_i\exp\left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3              |
| ALT_MIN               | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3               |
| MEAN                  | take the mean of these variables. The final value can be referenced using label.mean. You can use multiple instances of this keyword i.e. MEAN1, MEA—N2, MEAN3 The corresponding values are then referenced using label.mean-1, label.mean-2, label.mean-3   |
| MIN                   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3 |
| LOWEST                | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST               | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |
| BETWEEN               | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE—EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3   |
| HISTOGRAM             | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |

| MOMENTS | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^N(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ . |
|---------|--|
| SWITCH  | A switching function that ensures that only angles are only computed when atoms are within are within a certain fixed cutoff. The following provides information on the switchingfunction that are available.  |

#### **Examples**

The following input tells plumed to calculate the angle around the z direction between the positive x-direction and the vector connecting atom 3 to atom 5 and the angle around the z direction between the positive x-direction and the vector connecting atom 1 to atom 2. The minimum of these two quantities is then output

```
ZXTORSIONS ATOMS1=3,5 ATOMS2=1,2 MIN={BETA=0.1} LABEL=d1
PRINT ARG=d1.min
```

(See also PRINT).

#### 5.5.32 ZYTORSIONS

This is part of the multicolvar module

Calculate the torsional angle around the z axis from the positive y direction.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword | Description   |
|----------|---------|---|
| altmin   | ALT_MIN | the minimum value. This is calculated using the formula described in the description  |
|          |         | of the keyword so as to make it continuous.   |
| between  | BETWEEN | the number/fraction of values within a certain range. This is calculated using one of |
|          |         | the formula described in the description of the keyword so as to make it continuous.  |
|          |         | You can calculate this quantity multiple times using different parameters.            |

| highest | HIGHEST | the lowest of the quantitities calculated by this action   |
|---------|---------|--|
| lowest  | LOWEST  | the lowest of the quantitities calculated by this action   |
| max     | MAX     | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.   |
| mean    | MEAN    | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean  |
| min     | MIN     | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.   |
| moment  | MOMENTS | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc. |

The atoms involved can be specified using

| ATOMS | the atoms involved in each of the collective variables you wish to calculate. Keywords like ATOM←       |
|-------|---|
|       | S1, ATOMS2, ATOMS3, should be listed and one CV will be calculated for each ATOM keyword                |
|       | you specify (all ATOM keywords should define the same number of atoms). The eventual number             |
|       | of quantities calculated by this action will depend on what functions of the distribution you choose to |
|       | calculate. You can use multiple instances of this keyword i.e. ATOMS1, ATOMS2, ATOMS3                   |

Or alternatively by using

| GROUP Calculate the distance between each distinct pair of atoms in the g | roup |
|---|------|
|---|------|

Or alternatively by using

| GROUPA | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPB. |
|--------|---|
| GROUPB | Calculate the distances between all the atoms in GROUPA and all the atoms in GROUPB. This must be used in conjuction with GROUPA. |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically                |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-             |
|                       | tances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize                          |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation |

| MAX       | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3        |
|-----------|--|
| ALT_MIN   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3               |
| MEAN      | take the mean of these variables. The final value can be referenced using label.mean. You can use multiple instances of this keyword i.e. MEAN1, MEA—N2, MEAN3 The corresponding values are then referenced using label.mean-1, label.mean-2, label.mean-3   |
| MIN       | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3 |
| LOWEST    | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST   | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE← EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3  |
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .   |
| SWITCH    | A switching function that ensures that only angles are only computed when atoms are within are within a certain fixed cutoff. The following provides information on the switchingfunction that are available.  |

Examples

The following input tells plumed to calculate the angle around the z direction between the positive y-axis and the vector connecting atom 3 to atom 5 and the angle around the z direction between the positive y axis and the vector connecting atom 1 to atom 2. The minimum of these two quantities is then output

ZYTORSIONS ATOMS1=3,5 ATOMS2=1,2 MIN={BETA=0.1} LABEL=d1 PRINT ARG=d1.min

(See also PRINT).

## 5.5.33 MFILTER\_BETWEEN

This is part of the multicolvar module

This action can be used to filter the colvar values calculated by a multicolvar so that one can compute the mean and so on for only those multicolvars within a certain range.

This action can be used to create a dynamic group of atom based on the value of a multicolvar. In this action a multicolvar is within the dynamic group if its value lies in a particular range. In practise a weight,  $w_i$  is ascribed to each colvar,  $s_i$  calculated by a multicolvar and this weight measures the degree to which a colvar is a member of the group. This weight is calculated using a histogrambead so it is given by:

$$w_i = \int_a^b K\left(\frac{s - s_i}{w}\right)$$

where a,b and w are parameters. If one calculates a function of the set of multicolvars these weights are included in the calculation. As such if one calculates the MEAN,  $\mu$  of a filtered multicolvar what is computed is the following:

$$\mu = \frac{\sum_{i} w_{i} s_{i}}{\sum_{i} w_{i}}$$

One is thus calculating the mean for those colvars that are within the range of interest.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword | Description  |
|----------|---------|--|
| vmean    | VMEAN   | the norm of the mean vector. The output component can be refererred to elsewhere                     |
|          |         | in the input file by using the label.vmean   |
| altmin   | ALT_MIN | the minimum value. This is calculated using the formula described in the description                 |
|          |         | of the keyword so as to make it continuous.  |
| highest  | HIGHEST | the lowest of the quantitities calculated by this action   |
| lowest   | LOWEST  | the lowest of the quantitities calculated by this action   |
| max      | MAX     | the maximum value. This is calculated using the formula described in the description                 |
|          |         | of the keyword so as to make it continuous.  |
| mean     | MEAN    | the mean value. The output component can be refererred to elsewhere in the input                     |
|          |         | file by using the label.mean   |
| min      | MIN     | the minimum value. This is calculated using the formula described in the description                 |
|          |         | of the keyword so as to make it continuous.  |
| moment   | MOMENTS | the central moments of the distribution of values. The second moment would be refer-                 |
|          |         | enced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, |
|          |         | etc.   |

# Compulsory keywords

| DATA  | The multicolvar that calculates the set of base quantities that we are interested in  |
|-------|---|
| LOWER | the lower boundary for the range of interest  |
| UPPER | the upper boundary for the range of interest  |
| SMEAR | ( default=0.5 ) the ammount by which to smear the value for kernel density estimation |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances   |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize   |
| LOWMEM                | ( default=off ) lower the memory requirements  |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation  |
| VMEAN                 | calculate the norm of the mean vector. The final value can be referenced using label.vmean. You can use multiple instances of this keyword i.e. VMEAN1, VMEAN2, VMEAN3 The corresponding values are then referenced using label.vmean-1, label.vmean-2, label.vmean-3  |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA← N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2. <i>label</i> .mean-3  |
| MOMENTS               | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ . |

| MIN     | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3 |
|---------|--|
| MAX     | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3        |
| ALT_MIN | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3               |
| LOWEST  | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |
| BEAD    | This keywords is used if you want to employ an alternative to the function defeind above. The following provides information on the histogrambead that are available. When this keyword is present you no longer need the LOWER, U← PPER and SMEAR keywords.   |

#### **Examples**

The example shown below calculates the mean for those distances that are between 0 and 3 nm in length

```
DISTANCES GROUPA=1 GROUPB=2-50 MEAN LABEL=d1
MFILTER_BETWEEN DATA=d1 LOWER=0 UPPER=3.0 SMEAR=0.0001 MEAN LABEL=d4
```

More complicated things can be done by using the label of a filter as input to a new multicolvar as shown in the example below. Here the coordination numbers of all atoms are computed. The atoms with a coordination number between 4 and 6 are then identified using the filter. This reduced list of atoms is then used as input to a second coordination number calculation. This second coordination number thus measures the number of atoms 4-6 coordinated atoms each of the 4-6 coordination atoms is bound to.

```
c1: COORDINATIONNUMBER SPECIES=1-150 SWITCH={EXP D_0=4.0 R_0=0.5 D_MAX=6.0}
cf: MFILTER_BETWEEN DATA=c1 LOWER=4 UPPER=6 SMEAR=0.5 LOWMEM
c2: COORDINATIONNUMBER SPECIES=cf SWITCH={EXP D_0=4.0 R_0=0.5 D_MAX=6.0} MORE_THAN={RATIONAL D_0=2.0 R_0=0.1}
```

### 5.5.34 MFILTER\_LESS

This is part of the multicolvar module

This action can be used to filter the distribution of colvar values in a multicolvar so that one can compute the mean and so on for only those multicolvars less than a tolerance.

This action can be used to create a dynamic group of atom based on the value of a multicolvar. In this action a multicolvar is within the dynamic group if its value is less than a target. In practise a weight,  $w_i$  is ascribed to each colvar,  $s_i$  calculated by a multicolvar and this weight measures the degree to which a colvar is a member of the group. This weight is a number between 0 and 1 that is calculated using a switchingfunction ,  $\sigma$ . If one calculates a function of the set of multicolvars these weights are included in the calculation. As such if one calculates the MEAN,  $\mu$  of a filtered multicolvar what is computed is the following:

$$\mu = \frac{\sum_{i} w_{i} s_{i}}{\sum_{i} w_{i}}$$

One is thus calculating the mean for those colvars that are less than the target.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword | Description  |
|----------|---------|--|
| vmean    | VMEAN   | the norm of the mean vector. The output component can be refererred to elsewhere in the input file by using the label.vmean  |
| altmin   | ALT_MIN | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.   |
| highest  | HIGHEST | the lowest of the quantitities calculated by this action   |
| lowest   | LOWEST  | the lowest of the quantitities calculated by this action   |
| max      | MAX     | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.   |
| mean     | MEAN    | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean  |
| min      | MIN     | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.   |
| moment   | MOMENTS | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc. |

Compulsory keywords

| DATA | The multicolvar that calculates the set of base quantities that we are interested in |
|------|--|
| NN   | ( default=6 ) The n parameter of the switching function                              |
| ММ   | ( default=0 ) The m parameter of the switching function                              |
| D_0  | ( default=0.0 ) The d_0 parameter of the switching function                          |
| R_0  | The r_0 parameter of the switching function  |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-  |
|                       | tances   |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize   |
| LOWMEM                | ( default=off ) lower the memory requirements  |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation  |
| VMEAN                 | calculate the norm of the mean vector. The final value can be referenced using label.vmean. You can use multiple instances of this keyword i.e. VMEAN1, VMEAN2, VMEAN3 The corresponding values are then referenced using label.vmean-1, label.vmean-2, label.vmean-3  |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA $\leftarrow$ N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3  |
| MOMENTS               | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .   |
| MIN                   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3 |
| MAX                   | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3        |
| ALT_MIN               | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3               |
| LOWEST                | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST               | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |

| SWITCH  This keyword is used if you want to employ an alternative to the continuous switching function defined above. The following provides information on the switchingfunction that are available. When this keyword is present you relonger need the NN, MM, D_0 and R_0 keywords. | SWITCH |
|--|--------|
|--|--------|

**Examples** 

The example shown below calculates the mean for those distances that less than 1.5 nm in length

```
DISTANCES GROUPA=1 GROUPB=2-50 MEAN LABEL=d1 MFILTER_LESS DATA=d1 SWITCH={GAUSSIAN D_0=1.5 R_0=0.00001} MEAN LABEL=d4
```

## 5.5.35 MFILTER\_MORE

This is part of the multicolvar module

This action can be used to filter the distribution of colvar values in a multicolvar so that one can compute the mean and so on for only those multicolvars more than a tolerance.

This action can be used to create a dynamic group of atom based on the value of a multicolvar. In this action a multicolvar is within the dynamic group if its value is greater than a target. In practise a weight,  $w_i$  is ascribed to each colvar,  $s_i$  calculated by a multicolvar and this weight measures the degree to which a colvar is a member of the group. This weight is calculated using a switchingfunction,  $\sigma$  so it is given by:

$$w_i = 1 - \sigma(s_i)$$

If one calculates a function of the set of multicolvars these weights are included in the calculation. As such if one calculates the MEAN,  $\mu$  of a filtered multicolvar what is computed is the following:

$$\mu = \frac{\sum_{i} w_i s_i}{\sum_{i} w_i}$$

One is thus calculating the mean for those colvars that are greater than the target.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword | Description  |
|----------|---------|--|
| vmean    | VMEAN   | the norm of the mean vector. The output component can be refererred to elsewhere     |
|          |         | in the input file by using the label.vmean   |
| altmin   | ALT_MIN | the minimum value. This is calculated using the formula described in the description |
|          |         | of the keyword so as to make it continuous.  |
| highest  | HIGHEST | the lowest of the quantitities calculated by this action                             |
| lowest   | LOWEST  | the lowest of the quantitities calculated by this action                             |
| max      | MAX     | the maximum value. This is calculated using the formula described in the description |
|          |         | of the keyword so as to make it continuous.  |
| mean     | MEAN    | the mean value. The output component can be refererred to elsewhere in the input     |
|          |         | file by using the label.mean   |
| min      | MIN     | the minimum value. This is calculated using the formula described in the description |
|          |         | of the keyword so as to make it continuous.  |
| moment   | MOMENTS | the central moments of the distribution of values. The second moment would be refer- |
|          |         | enced elsewhere in the input file using label.moment-2, the third as label.moment-3, |
|          |         | etc.   |

# Compulsory keywords

| DATA | The multicolvar that calculates the set of base quantities that we are interested in |
|------|--|
| NN   | ( default=6 ) The n parameter of the switching function                              |
| MM   | ( default=0 ) The m parameter of the switching function; 0 implies 2*NN              |
| D_0  | ( default=0.0 ) The d_0 parameter of the switching function                          |
| R_0  | The r_0 parameter of the switching function  |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances   |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize   |
|                       |  |
| LOWMEM                | ( default=off ) lower the memory requirements  |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the cal-<br>culation   |
| VMEAN                 | calculate the norm of the mean vector. The final value can be referenced using label.vmean. You can use multiple instances of this keyword i.e. VMEAN1, VMEAN2, VMEAN3 The corresponding values are then referenced using label.vmean-1, label.vmean-2, label.vmean-3  |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA← N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3  |
| MOMENTS               | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^N(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ . |

| MIN     | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3 |
|---------|--|
| MAX     | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3        |
| ALT_MIN | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta} \log \sum_i \exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3            |
| LOWEST  | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |
| SWITCH  | This keyword is used if you want to employ an alternative to the continuous switching function defined above. The following provides information on the switchingfunction that are available. When this keyword is present you no longer need the NN, MM, D_0 and R_0 keywords.  |

#### **Examples**

The example shown below calculates the mean for those distances that greater than 1.5 nm in length

```
DISTANCES GROUPA=1 GROUPB=2-50 MEAN LABEL=d1
MFILTER_MORE DATA=d1 SWITCH={GAUSSIAN D_0=1.5 R_0=0.00001} MEAN LABEL=d4
```

More complicated things can be done by using the label of a filter as input to a new multicolvar as shown in the example below. Here the coordination numbers of all atoms are computed. The atoms with a coordination number greater than 2 are then identified using the filter. This reduced list of atoms is then used as input to a second coordination number calculation. This second coordination number thus measures the number of two-coordinated atoms that each of the two-coordinated atoms is bound to.

```
1: COORDINATIONNUMBER SPECIES=1-150 SWITCH={EXP D_0=4.0 R_0=0.5 D_MAX=6.0}
cf: MFILTER_MORE DATA=c1 SWITCH={RATIONAL D_0=2.0 R_0=0.1} LOWMEM
c2: COORDINATIONNUMBER SPECIES=cf SWITCH={EXP D_0=4.0 R_0=0.5 D_MAX=6.0} MORE_THAN={RATIONAL D_0=2.0 R_0=0.1}
```

#### 5.5.36 AROUND

This is part of the multicolvar module

This quantity can be used to calculate functions of the distribution of collective variables for the atoms that lie in a particular, user-specified part of the cell.

Each of the base quantities calculated by a multicolvar can can be assigned to a particular point in three dimensional space. For example, if we have the coordination numbers for all the atoms in the system each coordination number can be assumed to lie on the position of the central atom. Because each base quantity can be assigned to a particular point in space we can calculate functions of the distribution of base quantities in a particular part of the box by using:

$$\overline{s}_{\tau} = \frac{\sum_{i} f(s_i) w(x_i, y_i, z_i)}{\sum_{i} w(x_i, y_i, z_i)}$$

where the sum is over the collective variables,  $s_i$ , each of which can be thought to be at  $(x_i, y_i, z_i)$ . The function  $w(x_i, y_i, z_i)$  measures whether or not the system is in the subregion of interest. It is equal to:

$$w(x_i, y_i, z_i) = \int_{x_l}^{x_u} \int_{y_l}^{y_u} \int_{z_l}^{z_u} dx dy dz K\left(\frac{x - x_i}{\sigma}\right) K\left(\frac{y - y_i}{\sigma}\right) K\left(\frac{z - z_i}{\sigma}\right)$$

where K is one of the kernel functions described on histogrambead and  $\sigma$  is a bandwidth parameter. The function  $(s_i)$  can be any of the usual LESS\_THAN, MORE\_THAN, WITHIN etc that are used in all other multicolvars.

When AROUND is used with the DENSITY action the number of atoms in the specified region is calculated

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity             | Keyword   | Description   |
|----------------------|-----------|---|
| vmean                | VMEAN     | the norm of the mean vector. The output component can be refererred to elsewhere in the input file by using the label.vmean   |
| between              | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| lessthan             | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| mean                 | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| morethan             | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
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The atoms involved can be specified using

| ATOM | the atom whose vicinity we are interested in examining. For more information on how to specify lists of |
|------|---|
|      | atoms see Groups and Virtual Atoms  |

# Compulsory keywords

| DATA   | The multicolvar that calculates the set of base quantities that we are interested in                                   |
|--------|--|
| SIGMA  | the width of the function to be used for kernel density estimation   |
| KERNEL | ( default=gaussian ) the type of kernel function to be used  |
| XLOWER | ( default=0.0 ) the lower boundary in x relative to the x coordinate of the atom (0 indicates use full extent of box). |
| XUPPER | ( default=0.0 ) the upper boundary in x relative to the x coordinate of the atom (0 indicates use full extent of box). |
| YLOWER | ( default=0.0 ) the lower boundary in y relative to the y coordinate of the atom (0 indicates use full extent of box). |
| YUPPER | ( default=0.0 ) the upper boundary in y relative to the y coordinate of the atom (0 indicates use full extent of box). |
| ZLOWER | ( default=0.0 ) the lower boundary in z relative to the z coordinate of the atom (0 indicates use full extent of box). |
| ZUPPER | ( default=0.0 ) the upper boundary in z relative to the z coordinate of the atom (0 indicates use full extent of box). |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize  |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation   |
| OUTSIDE               | ( default=off ) calculate quantities for colvars that are on atoms outside the region of interest   |
| VMEAN                 | calculate the norm of the mean vector. The final value can be referenced using label.vmean. You can use multiple instances of this keyword i.e. VMEAN1, VMEAN2, VMEAN3 The corresponding values are then referenced using label.vmean-1, label.vmean-2, label.vmean-3   |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA $\leftarrow$ N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3   |
| LESS_THAN             | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.lessthan</code> . You can use multiple instances of this keyword i.e. <code>LESS_THAN1</code> , <code>LESS_THAN2</code> , <code>LESS_THAN3</code> The corresponding values are then referenced using <code>label.lessthan-1</code> , <code>label.lessthan-2</code> , <code>label.lessthan-3</code> |

| MORE_THAN | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.morethan</code> . You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THAN0. N3 The corresponding values are then referenced using <code>label.morethan-1</code> , <code>label.morethan-2</code> , <code>label.morethan-3</code> |
|-----------|--|
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE← EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3  |
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |

#### **Examples**

The following commands tell plumed to calculate the average coordination number for the atoms that have x (in fractional coordinates) within 2.0 nm of the com of mass c1. The final value will be labeled s.mean.

```
COM ATOMS=1-100 LABEL=c1
COORDINATIONNUMBER SPECIES=1-100 R_0=1.0 LABEL=c
AROUND DATA=c ORIGIN=c1 XLOWER=-2.0 XUPPER=2.0 SIGMA=0.1 MEAN LABEL=s
```

#### 5.5.37 **CAVITY**

This is part of the multicolvar module

This quantity can be used to calculate functions of the distribution of collective variables for the atoms that lie in a box defined by the positions of four atoms.

Each of the base quantities calculated by a multicolvar can can be assigned to a particular point in three dimensional space. For example, if we have the coordination numbers for all the atoms in the system each coordination number can be assumed to lie on the position of the central atom. Because each base quantity can be assigned to a particular point in space we can calculate functions of the distribution of base quantities in a particular part of the box by using:

$$\overline{s}_{\tau} = \frac{\sum_{i} f(s_i) w(u_i, v_i, w_i)}{\sum_{i} w(u_i, v_i, w_i)}$$

where the sum is over the collective variables,  $s_i$ , each of which can be thought to be at  $(u_i, v_i, z_i)$ . The function  $(s_i)$  can be any of the usual LESS\_THAN, MORE\_THAN, WITHIN etc that are used in all other multicolvars. Notice that here (at variance with what is done in AROUND) we have transformed from the usual  $(x_i, y_i, z_i)$  position to a position in  $(u_i, v_i, z_i)$ . This is done using a rotation matrix as follows:

$$(u_i v_i w_i) = \mathbf{R} (x_i - x_o y_i - y_o z_i - z_o)$$

where  ${\bf R}$  is a rotation matrix that is calculated by constructing a set of three orthonormal vectors from the reference positions specified by the user. The first of these unit vectors points from the first reference atom to the second. The second is then the normal to the plane containing atoms 1,2 and 3 and the the third is the unit vector orthogonal to these first two vectors.  $(x_0, y_0, z_0)$ , meanwhile, specifies the position of the first reference atom.

In the previous function  $w(u_i, v_i, w_i)$  measures whether or not the system is in the subregion of interest. It is equal to:

$$w(u_i, v_i, w_i) = \int_0^{u'} \int_0^{v'} \int_0^{w'} du dv dw K\left(\frac{u - u_i}{\sigma}\right) K\left(\frac{v - v_i}{\sigma}\right) K\left(\frac{w - w_i}{\sigma}\right)$$

where K is one of the kernel functions described on histogrambead and  $\sigma$  is a bandwidth parameter. The vector connecting atom 1 to atom 4 is used to define the extent of the box in each of the u, v and w directions. Essentially the vector connecting atom 1 to atom 4 is projected onto the three unit vectors described above and the resulting projections determine the u', v' and w' parameters in the above expression.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| vmean    | VMEAN     | the norm of the mean vector. The output component can be refererred to elsewhere in the input file by using the label.vmean   |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

| ATOMS | the positions of four atoms that define spatial extent of the cavity. For more information on how to |  |
|-------|--|--|
|       | specify lists of atoms see Groups and Virtual Atoms  |  |

# Compulsory keywords

| DATA   | The multicolvar that calculates the set of base quantities that we are interested in |
|--------|--|
| SIGMA  | the width of the function to be used for kernel density estimation                   |
| KERNEL | ( default=gaussian ) the type of kernel function to be used                          |

## Options

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances   |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize   |
| LOWMEM                | ( default=off ) lower the memory requirements  |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation  |
| OUTSIDE               | ( default=off ) calculate quantities for colvars that are on atoms outside the region of interest  |
| PRINT_BOX             | ( default=off ) write out the positions of the corners of the box to an xyz file   |
| VMEAN                 | calculate the norm of the mean vector. The final value can be referenced using <i>label.</i> vmean. You can use multiple instances of this keyword i.e. VMEAN1, VMEAN2, VMEAN3 The corresponding values are then referenced using <i>label.</i> vmean-1, <i>label.</i> vmean-2, <i>label.</i> vmean-3  |
| MEAN                  | take the mean of these variables. The final value can be referenced using label.mean. You can use multiple instances of this keyword i.e. MEAN1, MEA N2, MEAN3 The corresponding values are then referenced using label.mean-1, label.mean-2, label.mean-3   |
| LESS_THAN             | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_THAN2, LESS_THAN3 The corresponding values are then referenced using <i>label</i> .lessthan-1, <i>label</i> .lessthan-2, <i>label</i> .lessthan-3                                      |
| MORE_THAN             | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.morethan</code> . You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THA $\sim$ N3 The corresponding values are then referenced using <code>label.morethan-1</code> , <code>label.morethan-2</code> , <code>label.morethan-3</code> |
| BETWEEN               | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE← EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3  |

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| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3 |
|-----------|---|
| FILE      | the file on which to write out the box coordinates  |
| UNITS     | ( default=nm ) the units in which to write out the corners of the box   |

#### **Examples**

The following commands tell plumed to calculate the number of atoms in an ion channel in a protein. The extent of the channel is calculated from the positions of atoms 1, 4, 5 and 11. The final value will be labeled cav.

```
d1: DENSITY SPECIES=20-500
CAVITY DATA=d1 ATOMS=1,4,5,11 SIGMA=0.1 LABEL=cav
```

The following command tells plumed to calculate the coordination numbers (with other water molecules) for the water molecules in the protein channel described above. The average coordination number and the number of coordination numbers more than 4 is then calculated. The values of these two quantities are given the labels cav.mean and cav.morethan

```
d1: COORDINATIONNUMBER SPECIES=20-500 CAVITY DATA=d1 ATOMS=1,4,5,11 SIGMA=0.1 MEAN MORE_THAN={RATIONAL R_0=4} LABEL=cav
```

#### 5.5.38 INCYLINDER

This is part of the multicolvar module

This quantity can be used to calculate functions of the distribution of collective variables for the atoms that lie in a particular, user-specified part of of the cell.

Each of the base quantities calculated by a multicolvar can can be assigned to a particular point in three dimensional space. For example, if we have the coordination numbers for all the atoms in the system each coordination number can be assumed to lie on the position of the central atom. Because each base quantity can be assigned to a particular point in space we can calculate functions of the distribution of base quantities in a particular part of the box by using:

$$\bar{s}_{\tau} = \frac{\sum_{i} f(s_{i}) \sigma(r_{xy})}{\sum_{i} \sigma(r_{xy})}$$

where the sum is over the collective variables,  $s_i$ , each of which can be thought to be at  $(x_i, y_i, z_i)$ . The function  $\sigma$  is a switchingfunction that acts on the distance between the point at which the collective is located  $(x_i, y_i, z_i)$  and the position of the atom that was specified using the ORIGIN keyword projected in the xy plane if DIRECTION=z is used. In other words:

$$r_{xy} = sqrt(x_i - x_0)^2 + (y_i - y_0)^2$$

In short this function,  $\sigma(r_{xy})$ , measures whether or not the CV is within a cylinder that runs along the axis specified using the DIRECTION keyword and that is centered on the position of the atom specified using ORIGIN.

The function  $(s_i)$  can be any of the usual LESS\_THAN, MORE\_THAN, WITHIN etc that are used in all other multicolvars.

When INCYLINDER is used with the DENSITY action the number of atoms in the specified region is calculated

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. <code>label.lessthan-1</code>, <code>label.lessthan-2</code> etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| vmean    | VMEAN     | the norm of the mean vector. The output component can be refererred to elsewhere in the input file by using the label.vmean   |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

| ATOM | the atom whose vicinity we are interested in examining. For more information on how to specify lists of |
|------|---|
|      | atoms see Groups and Virtual Atoms  |

#### Compulsory keywords

| DATA   | The multicolvar that calculates the set of base quantities that we are interested in |
|--------|--|
| KERNEL | ( default=gaussian ) the type of kernel function to be used                          |

| DIRECTION | the direction of the long axis of the cylinder. Must be x, y or z                                       |  |
|-----------|---|--|
| RADIUS    | a switching function that gives the extent of the cyclinder in the plane perpendicular to the direction |  |
| LOWER     | ( default=0.0 ) the lower boundary on the direction parallel to the long axis of the cylinder           |  |
| UPPER     | ( default=0.0 ) the upper boundary on the direction parallel to the long axis of the cylinder           |  |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-  |
|                       | tances   |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize   |
| LOWMEM                | ( default=off ) lower the memory requirements  |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the cal-   |
|                       | culation   |
| OUTSIDE               | ( default=off ) calculate quantities for colvars that are on atoms outside the   |
|                       | region of interest   |
| VMEAN                 | calculate the norm of the mean vector. The final value can be referenced using   |
|                       | label.vmean. You can use multiple instances of this keyword i.e. VMEAN1,   |
|                       | VMEAN2, VMEAN3 The corresponding values are then referenced using  |
|                       | label.vmean-1, label.vmean-2, label.vmean-3  |
| MEAN                  | take the mean of these variables. The final value can be referenced using  |
|                       | label.mean. You can use multiple instances of this keyword i.e. MEAN1, MEA↔  |
|                       | N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-   |
|                       | 1, label.mean-2, label.mean-3  |
| LESS_THAN             | calculate the number of variables less than a certain target value. This quan-   |
|                       | tity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final  |
|                       | value can be referenced using <i>label</i> .lessthan. You can use multiple instances   |
|                       | of this keyword i.e. LESS_THAN1, LESS_THAN2, LESS_THAN3 The corresponding values are then referenced using <i>label</i> .lessthan-1, <i>label</i> .lessthan-2, |
|                       | label.lessthan-3   |
| MORE_THAN             | calculate the number of variables more than a certain target value. This quan-   |
|                       | tity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The  |
|                       | final value can be referenced using <i>label</i> .morethan. You can use multiple in-   |
|                       | stances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THA↔   |
|                       | N3 The corresponding values are then referenced using <i>label</i> .morethan-1,  |
|                       | label.morethan-2, label.morethan-3   |
| BETWEEN               | calculate the number of values that are within a certain range. These quanti-  |
|                       | ties are calculated using kernel density estimation as described on histogram-   |
|                       | bead. The final value can be referenced using <i>label</i> .between. You can use   |
|                       | multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE  |
|                       | EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3                               |
| HISTOGRAM             | calculate a discretized histogram of the distribution of values. This shortcut   |
|                       | allows you to calculates NBIN quantites like BETWEEN. The final value can  |
|                       | be referenced using <i>label</i> .histogram. You can use multiple instances of this  |
|                       | keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corre-   |
|                       | sponding values are then referenced using label.histogram-1, label.histogram-  |
|                       | 2, label.histogram-3   |
| SIGMA                 | the width of the function to be used for kernel density estimation   |
|                       |  |

**Examples** 

#### **5.5.39 INSPHERE**

This is part of the multicolvar module

This quantity can be used to calculate functions of the distribution of collective variables for the atoms that lie in a particular, user-specified part of the cell.

Each of the base quantities calculated by a multicolvar can can be assigned to a particular point in three dimensional space. For example, if we have the coordination numbers for all the atoms in the system each coordination number can be assumed to lie on the position of the central atom. Because each base quantity can be assigned to a particular point in space we can calculate functions of the distribution of base quantities in a particular part of the box by using:

$$\bar{s}_{\tau} = \frac{\sum_{i} f(s_{i})\sigma(r)}{\sum_{i} \sigma(r)}$$

where the sum is over the collective variables,  $s_i$ , each of which can be thought to be at  $(x_i, y_i, z_i)$ . The function  $\sigma$  is a switchingfunction that acts on the distance between the point at which the collective is located  $(x_i, y_i, z_i)$  and the position of the atom that was specified using the ORIGIN keyword. In other words:

$$r = sqrt(x_i - x_0)^2 + (y_i - y_0)^2 + (z_i - z_0)^2$$

In short this function,  $\sigma(r_{xy})$ , measures whether or not the CV is within a sphere that is centered on the position of the atom specified using the keyword ORIGIN.

The function  $(s_i)$  can be any of the usual LESS\_THAN, MORE\_THAN, WITHIN etc that are used in all other multicolvars.

When INCYLINDER is used with the DENSITY action the number of atoms in the specified region is calculated

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| vmean    | VMEAN     | the norm of the mean vector. The output component can be refererred to elsewhere in the input file by using the label.vmean   |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

| ATOM | the atom whose vicinity we are interested in examining. For more information on how to specify lists of |
|------|---|
|      | atoms see Groups and Virtual Atoms  |

## Compulsory keywords

| DATA   | The multicolvar that calculates the set of base quantities that we are interested in |
|--------|--|
| KERNEL | ( default=gaussian ) the type of kernel function to be used                          |
| RADIUS | the switching function that tells us the extent of the sphereical region of interest |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize  |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation   |
| OUTSIDE               | ( default=off ) calculate quantities for colvars that are on atoms outside the region of interest   |
| VMEAN                 | calculate the norm of the mean vector. The final value can be referenced using label.vmean. You can use multiple instances of this keyword i.e. VMEAN1, VMEAN2, VMEAN3 The corresponding values are then referenced using label.vmean-1, label.vmean-2, label.vmean-3                                   |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA $\leftarrow$ N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3 |

| LESS_THAN | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using label.lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_THAN2, LESS_THAN3 The corresponding values are then referenced using label.lessthan-1, label.lessthan-2, label.lessthan-3  |
|-----------|--|
| MORE_THAN | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.morethan</code> . You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THA $\leftarrow$ N3 The corresponding values are then referenced using <code>label.morethan-1</code> , <code>label.morethan-2</code> , <code>label.morethan-3</code> |
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE← EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3  |
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |

**Examples** 

#### 5.5.40 TETRAHEDRALPORE

This is part of the multicolvar module

This quantity can be used to calculate functions of the distribution of collective variables for the atoms lie that lie in a box defined by the positions of four atoms at the corners of a tetrahedron.

Each of the base quantities calculated by a multicolvar can can be assigned to a particular point in three dimensional space. For example, if we have the coordination numbers for all the atoms in the system each coordination number can be assumed to lie on the position of the central atom. Because each base quantity can be assigned to a particular point in space we can calculate functions of the distribution of base quantities in a particular part of the box by using:

$$\overline{s}_{\tau} = \frac{\sum_{i} f(s_i) w(u_i, v_i, w_i)}{\sum_{i} w(u_i, v_i, w_i)}$$

where the sum is over the collective variables,  $s_i$ , each of which can be thought to be at  $(u_i, v_i, z_i)$ . The function  $(s_i)$  can be any of the usual LESS\_THAN, MORE\_THAN, WITHIN etc that are used in all other multicolvars. Notice that here (at variance with what is done in AROUND) we have transformed from the usual  $(x_i, y_i, z_i)$  position to a position in  $(u_i, v_i, z_i)$ . This is done using a rotation matrix as follows:

$$(u_i v_i w_i) = \mathbf{R} (x_i - x_o y_i - y_o z_i - z_o)$$

where  ${\bf R}$  is a rotation matrix that is calculated by constructing a set of three orthonormal vectors from the reference positions specified by the user. Initially unit vectors are found by calculating the bisector,  ${\bf b}$ , and cross product,  ${\bf c}$ , of the vectors connecting atoms 1 and 2. A third unit vector,  ${\bf p}$  is then found by taking the cross product between the cross product calculated during the first step,  ${\bf c}$  and the bisector,  ${\bf b}$ . From this second cross product  ${\bf p}$  and the bisector  ${\bf b}$  two new vectors are calculated using:

$$v_1 = \cos\left(\frac{\pi}{4}\right)\mathbf{b} + \sin\left(\frac{\pi}{4}\right)\mathbf{p}$$
 and  $v_2 = \cos\left(\frac{\pi}{4}\right)\mathbf{b} - \sin\left(\frac{\pi}{4}\right)\mathbf{p}$ 

In the previous function  $w(u_i,v_i,w_i)$  measures whether or not the system is in the subregion of interest. It is equal to:

$$w(u_i, v_i, w_i) = \int_0^{u'} \int_0^{v'} \int_0^{w'} du dv dw K\left(\frac{u - u_i}{\sigma}\right) K\left(\frac{v - v_i}{\sigma}\right) K\left(\frac{w - w_i}{\sigma}\right)$$

where K is one of the kernel functions described on histogrambead and  $\sigma$  is a bandwidth parameter. The values of u' and v' are found by finding the projections of the vectors connecting atoms 1 and 2 and 1 and 3  $v_1$  and  $v_2$ . This gives four projections: the largest two projections are used in the remainder of the calculations. w' is calculated by taking the projection of the vector connecting atoms 1 and 4 on the vector  $\mathbf{c}$ . Notice that the manner by which this box is constructed differs from the way this is done in CAVITY. This is in fact the only point of difference between these two actions.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| vmean    | VMEAN     | the norm of the mean vector. The output component can be refererred to elsewhere in the input file by using the label.vmean   |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

| ATOMS | the positions of four atoms that define spatial extent of the cavity. For more information on how to |
|-------|--|
|       | specify lists of atoms see Groups and Virtual Atoms  |

# Compulsory keywords

| DATA   | The multicolvar that calculates the set of base quantities that we are interested in |
|--------|--|
| SIGMA  | the width of the function to be used for kernel density estimation                   |
| KERNEL | ( default=gaussian ) the type of kernel function to be used                          |

## Options

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize  |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation   |
| OUTSIDE               | ( default=off ) calculate quantities for colvars that are on atoms outside the region of interest   |
| PRINT_BOX             | ( default=off ) write out the positions of the corners of the box to an xyz file  |
| VMEAN                 | calculate the norm of the mean vector. The final value can be referenced using label.vmean. You can use multiple instances of this keyword i.e. VMEAN1, VMEAN2, VMEAN3 The corresponding values are then referenced using label.vmean-1, label.vmean-2, label.vmean-3   |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA⇔ N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3   |
| LESS_THAN             | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using label.lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_THAN2, LESS_THAN3 The corresponding values are then referenced using label.lessthan-1, label.lessthan-2, label.lessthan-3   |
| MORE_THAN             | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.morethan</code> . You can use multiple instances of this keyword i.e. <code>MORE_THAN1</code> , <code>MORE_THAN2</code> , <code>MORE_THA</code> N3… The corresponding values are then referenced using <code>label.morethan-1</code> , <code>label.morethan-2</code> , <code>label.morethan-3</code> … |
| BETWEEN               | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE← EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3   |

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| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <code>label.histogram</code> . You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <code>label.histogram-1</code> , <code>label.histogram-2</code> , <code>label.histogram-3</code> |
|-----------|--|
| FILE      | the file on which to write out the box coordinates   |
| UNITS     | ( default=nm ) the units in which to write out the corners of the box  |

#### **Examples**

The following commands tell plumed to calculate the number of atom inside a tetrahedral cavity. The extent of the tetrahedral cavity is calculated from the positions of atoms 1, 4, 5, and 11, The final value will be labeled cav.

```
d1: DENSITY SPECIES=20-500
TETRAHEDRALPORE DATA=d1 ATOMS=1,4,5,11 SIGMA=0.1 LABEL=cav
```

The following command tells plumed to calculate the coordination numbers (with other water molecules) for the water molecules in the tetrahedral cavity described above. The average coordination number and the number of coordination numbers more than 4 is then calculated. The values of these two quantities are given the labels cav.mean and cav.morethan

```
d1: COORDINATIONNUMBER SPECIES=20-500 CAVITY DATA=d1 ATOMS=1,4,5,11 SIGMA=0.1 MEAN MORE_THAN={RATIONAL R_0=4} LABEL=cav
```

#### 5.5.41 GRADIENT

This is part of the crystallization module

It is only available if you configure PLUMED with ./configure –enable-modules=crystallization . Furthermore, this feature is still being developed so take care when using it and report any problems on the mailing list.

Calculate the gradient of the average value of a multicolvar value

The atoms involved can be specified using

**ORIGIN** we will use the position of this atom as the origin in our calculation. For more information on how to specify lists of atoms see Groups and Virtual Atoms

Compulsory keywords

| DATA   | The multicolvar that calculates the set of base quantities that we are interested in                      |  |
|--------|---|--|
| DIR    | ( default=xyz ) the directions in which we are calculating the graident. Should be x, y, z, xy, xz, yz or |  |
|        | хуz   |  |
| NBINS  | number of bins to use in each direction for the calculation of the gradient                               |  |
| SIGMA  | ( default=1.0 ) the width of the function to be used for kernel density estimation                        |  |
| KERNEL | ( default=gaussian ) the type of kernel function to be used   |  |

#### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically                |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-             |
|                       | tances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize                          |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation |

**Examples** 

#### 5.5.42 LOCAL\_AVERAGE

This is part of the multicolvar module

Calculate averages over spherical regions centered on atoms

As is explained in this video certain multicolvars calculate one scalar quantity or one vector for each of the atoms in the system. For example COORDINATIONNUMBER measures the coordination number of each of the atoms in the system and Q4 measures the 4th order Steinhardt parameter for each of the atoms in the system. These quantities provide tell us something about the disposition of the atoms in the first coordination sphere of each of the atoms of interest. Lechner and Dellago? have suggested that one can probe local order in a system by taking the average value of such symmetry functions over the atoms within a spherical cutoff of each of these atoms in the systems. When this is done with Steinhardt parameters they claim this gives a coordinate that is better able to distinguish solid and liquid configurations of Lennard-Jones atoms.

You can calculate such locally averaged quantities within plumed by using the LOCAL\_AVERAGE command. This command calculates the following atom-centered quantities:

$$s_i = \frac{c_i + \sum_j \sigma(r_{ij})c_j}{1 + \sum_j \sigma(r_{ij})}$$

where the  $c_i$  and  $c_j$  values can be for any one of the symmetry functions that can be calculated using plumed multicolvars. The function  $\sigma(r_{ij})$  is a switchingfunction that acts on the distance between atoms i and j. Lechner and Dellago suggest that the parameters of this function should be set so that it the function is equal to one when atom j is in the first coordination sphere of atom i and is zero otherwise.

The  $s_i$  quantities calculated using the above command can be again thought of as atom-centred symmetry functions. They thus operate much like multicolvars. You can thus calculate properties of the distribution of  $s_i$  values using MEAN, LESS\_THAN, HISTOGRAM and so on. You can also probe the value of these averaged variables in regions of the box by using the command in tandem with the AROUND command.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| vmean    | VMEAN     | the norm of the mean vector. The output component can be refererred to elsewhere in the input file by using the label.vmean   |
| vsum     | VSUM      | the norm of sum of vectors. The output component can be refererred to elsewhere in the input file by using the label.vsum   |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

# this keyword is used for colvars such as coordination number. In that context it specifies that plumed should calculate one coordination number for each of the atoms specified. Each of these coordination numbers specifies how many of the other specified atoms are within a certain cutoff of the central atom. You can specify the atoms here as another multicolvar action or using a MultiColvar Filter or ActionVolume action. When you do so the quantity is calculated for those atoms specified in the previous multicolvar. This is useful if you would like to calculate the Steinhardt parameter for

those atoms that have a coordination number more than four for example

Or alternatively by using

| SPECIESA | this keyword is used for colvars such as the coordination number. In that context it species that plumed should calculate one coordination number for each of the atoms specified in SPECIESA. Each of these cooordination numbers specifies how many of the atoms specifies using SPEC—IESB is within the specified cutoff. As with the species keyword the input can also be specified using the label of another multicolvar |
|----------|---|
| SPECIESB | this keyword is used for colvars such as the coordination number. It must appear with SPECIESA.  For a full explanation see the documentation for that keyword  |

# Compulsory keywords

| NN | ( default=6 ) The n parameter of the switching function                   |
|----|---|
| MM | ( default=0 ) The m parameter of the switching function; 0 implies $2*NN$ |
| D← | ( default=0.0 ) The d_0 parameter of the switching function               |
| _0 |   |
| R↔ | The r_0 parameter of the switching function                               |
| _0 |   |

| NOPBC     | ( default=off ) ignore the periodic boundary conditions when calculating distances  |
|-----------|---|
| SERIAL    | ( default=off ) do the calculation in serial. Do not parallelize  |
| TIMINGS   | ( default=off ) output information on the timings of the various parts of the calculation   |
| LOWMEM    | ( default=off ) lower the memory requirements   |
| SWITCH    | This keyword is used if you want to employ an alternative to the continuous swiching function defined above. The following provides information on the switchingfunction that are available. When this keyword is present you no longer need the NN, MM, D_0 and R_0 keywords.  |
| MEAN      | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEAN2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3   |
| MORE_THAN | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using label.morethan. You can use multiple instances of this keyword i.e. MORE_THA $\leftarrow$ N1, MORE_THAN2, MORE_THAN3 The corresponding values are then referenced using label.morethan-1, label.morethan-2, label.morethan-3 |
| LESS_THAN | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using label.lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_T HAN2, LESS_THAN3 The corresponding values are then referenced using label.lessthan-1, label.lessthan-2, label.lessthan-3                    |
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BET WEEN1, BETWEEN2, BETWEEN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3      |
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGR← AM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3                 |

| MOMENTS | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ . |
|---------|--|
| VMEAN   | calculate the norm of the mean vector. The final value can be referenced using <i>label.</i> vmean. You can use multiple instances of this keyword i.e. VMEAN1, VMEAN2, VMEAN3 The corresponding values are then referenced using <i>label.</i> vmean-1, <i>label.</i> vmean-2, <i>label.</i> vmean-3  |
| VSUM    | calculate the norm of the sum of vectors. The final value can be referenced using <i>label.</i> vsum. You can use multiple instances of this keyword i.e. VSUM1, VSUM2, VSUM3 The corresponding values are then referenced using <i>label.</i> vsum-1, <i>label.</i> vsum-2, <i>label.</i> vsum-3  |

#### **Examples**

This example input calculates the coordination numbers for all the atoms in the system. These coordination numbers are then averaged over spherical regions. The number of averaged coordination numbers that are greater than 4 is then output to a file.

```
COORDINATIONNUMBER SPECIES=1-64 D_0=1.3 R_0=0.2 LABEL=d1 LOCAL_AVERAGE ARG=d1 SWITCH={RATIONAL D_0=1.3 R_0=0.2} MORE_THAN={RATIONAL R_0=4} LABEL=la PRINT ARG=la.* FILE=colvar
```

This example input calculates the  $q_4$  (see Q4) vectors for each of the atoms in the system. These vectors are then averaged component by component over a spherical region. The average value for this quantity is then outputeed to a file. This calculates the quantities that were used in the paper by Lechner and Dellago ?

```
Q4 SPECIES=1-64 SWITCH={RATIONAL D_0=1.3 R_0=0.2} LABEL=q4 LOCAL_AVERAGE ARG=q4 SWITCH={RATIONAL D_0=1.3 R_0=0.2} MEAN LABEL=la PRINT ARG=la.* FILE=colvar
```

#### 5.5.43 LOCAL\_Q3

#### This is part of the crystallization module

It is only available if you configure PLUMED with ./configure -enable-modules=crystallization . Furthermore, this feature is still being developed so take care when using it and report any problems on the mailing list.

Calculate the local degree of order around an atoms by taking the average dot product between the  $q_3$  vector on the central atom and the  $q_3$  vector on the atoms in the first coordination sphere.

The Q3 command allows one to calculate one complex vectors for each of the atoms in your system that describe the degree of order in the coordination sphere around a particular atom. The difficulty with these vectors comes when combining the order parameters from all of the individual atoms/molecules so as to get a measure of the global degree of order for the system. The simplest way of doing this - calculating the average Steinhardt parameter - can be problematic. If one is examining nucleation say only the order parameters for those atoms in the nucleus will change significantly when the nucleus forms. The order parameters for the atoms in the surrounding liquid will remain pretty much the same. As such if one models a small nucleus embedded in a very large amount of solution/melt any change in the average order parameter will be negligible. Substantial changes in the value of this average can be observed in simulations of nucleation but only because the number of atoms is relatively small.

When the average Q3 parameter is used to bias the dynamics a problems can occur. These averaged coordinates cannot distinguish between the correct, single-nucleus pathway and a concerted pathway in which all the atoms rearrange themselves into their solid-like configuration simultaneously. This second type of pathway would be impossible in reality because there is a large entropic barrier that prevents concerted processes like this from happening. However, in the finite sized systems that are commonly simulated this barrier is reduced substantially. As a result in simulations where average Steinhardt parameters are biased there are often quite dramatic system size effects

If one wants to simulate nucleation using some form on biased dynamics what is really required is an order parameter that measures:

- · Whether or not the coordination spheres around atoms are ordered
- · Whether or not the atoms that are ordered are clustered together in a crystalline nucleus

LOCAL\_AVERAGE and NLINKS are variables that can be combined with the Steinhardt parameteters allow to calculate variables that satisfy these requirements. LOCAL\_Q3 is another variable that can be used in these sorts of calculations. The LOCAL\_Q3 parameter for a particular atom is a number that measures the extent to which the orientation of the atoms in the first coordination sphere of an atom match the orientation of the central atom. It does this by calculating the following quantity for each of the atoms in the system:

$$s_i = \frac{\sum_{j} \sigma(r_{ij}) \sum_{m=-3}^{3} q_{3m}^*(i) q_{3m}(j)}{\sum_{j} \sigma(r_{ij})}$$

where  $q_{3m}(i)$  and  $q_{3m}(j)$  are the 3rd order Steinhardt vectors calculated for atom i and atom j respectively and the asterix denotes complex conjugation. The function  $\sigma(r_{ij})$  is a switchingfunction that acts on the distance between atoms i and j. The parameters of this function should be set so that it the function is equal to one when atom j is in the first coordination sphere of atom i and is zero otherwise. The sum in the numerator of this expression is the dot product of the Steinhardt parameters for atoms i and j and thus measures the degree to which the orientations of these adjacent atoms is correlated.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. <code>label.lessthan-1</code>, <code>label.lessthan-2</code> etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

| SPECIES | this keyword is used for colvars such as coordination number. In that context it specifies that plumed  |
|---------|---|
|         | should calculate one coordination number for each of the atoms specified. Each of these coordi-         |
|         | nation numbers specifies how many of the other specified atoms are within a certain cutoff of the       |
|         | central atom. You can specify the atoms here as another multicolvar action or using a MultiColvar ↔     |
|         | Filter or ActionVolume action. When you do so the quantity is calculated for those atoms specified      |
|         | in the previous multicolvar. This is useful if you would like to calculate the Steinhardt parameter for |
|         | those atoms that have a coordination number more than four for example                                  |

Or alternatively by using

| SPECIESA | this keyword is used for colvars such as the coordination number. In that context it species that plumed should calculate one coordination number for each of the atoms specified in SPECIESA. Each of these cooordination numbers specifies how many of the atoms specifies using SPEC—IESB is within the specified cutoff. As with the species keyword the input can also be specified using the label of another multicolvar |
|----------|---|
| SPECIESB | this keyword is used for colvars such as the coordination number. It must appear with SPECIESA. For a full explanation see the documentation for that keyword   |

# Compulsory keywords

| NN | ( default=6 ) The n parameter of the switching function                 |
|----|---|
| MM | ( default=0 ) The m parameter of the switching function; 0 implies 2*NN |
| D↔ | ( default=0.0 ) The d_0 parameter of the switching function             |
| _0 |   |

| R⊷ | The r_0 parameter of the switching function |
|----|---|
| 0  |   |

# Options

| NOPBC     | ( default=off ) ignore the periodic boundary conditions when calculating distances   |  |
|-----------|--|--|
| SERIAL    | ( default=off ) do the calculation in serial. Do not parallelize   |  |
| LOWMEM    | ( default=off ) lower the memory requirements  |  |
| TIMINGS   | ( default=off ) output information on the timings of the various parts of the calculation  |  |
| SWITCH    | This keyword is used if you want to employ an alternative to the continuous swiching function defined above. The following provides information on the switchingfunction that are available. When this keyword is present you no longer need the NN, MM, D_0 and R_0 keywords.   |  |
| MEAN      | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEAN2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3  |  |
| MORE_THAN | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using label.morethan. You can use multiple instances of this keyword i.e. MORE_THA $\hookrightarrow$ N1, MORE_THAN2, MORE_THAN3 The corresponding values are then referenced using label.morethan-1, label.morethan-2, label.morethan-3   |  |
| LESS_THAN | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using label.lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_T HAN2, LESS_THAN3 The corresponding values are then referenced using label.lessthan-1, label.lessthan-2, label.lessthan-3   |  |
| MIN       | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3 |  |
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using label.between. You can use multiple instances of this keyword i.e. BET WEEN1, BETWEEN2, BETWEEN3 The corresponding values are then referenced using label.between-1, label.between-2, label.between-3   |  |
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |  |
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .   |  |
| LOWEST    | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |  |
| HIGHEST   | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |  |
|           |  |  |

Examples

The following command calculates the average value of the LOCAL\_Q3 parameter for the 64 Lennard Jones atoms in the system under study and prints this quantity to a file called colvar.

```
Q3 SPECIES=1-64 D_0=1.3 R_0=0.2 LABEL=q3 LOCAL_Q3 ARG=q3 SWITCH={RATIONAL D_0=1.3 R_0=0.2} MEAN LABEL=1q3 PRINT ARG=1q3.mean FILE=colvar
```

The following input calculates the distribution of LOCAL\_Q3 parameters at any given time and outputs this information to a file.

```
Q3 SPECIES=1-64 D_0=1.3 R_0=0.2 LABEL=q3 LOCAL_Q3 ARG=q3 SWITCH={RATIONAL D_0=1.3 R_0=0.2} HISTOGRAM={GAUSSIAN LOWER=0.0 UPPER=1.0 NBINS=20 SMEAR=0.1} PRINT ARG=lq3.* FILE=colvar
```

The following calculates the LOCAL\_Q3 parameters for atoms 1-5 only. For each of these atoms comparisons of the geometry of the coordination sphere are done with those of all the other atoms in the system. The final quantity is the average and is outputted to a file

```
Q3 SPECIESA=1-5 SPECIESB=1-64 D_0=1.3 R_0=0.2 LABEL=q3a
Q3 SPECIESA=6-64 SPECIESB=1-64 D_0=1.3 R_0=0.2 LABEL=q3b

LOCAL_Q3 ARG=q3a,q3b SWITCH={RATIONAL D_0=1.3 R_0=0.2} MEAN LOWMEM LABEL=w3
PRINT ARG=w3.* FILE=colvar
```

### 5.5.44 LOCAL\_Q4

#### This is part of the crystallization module

It is only available if you configure PLUMED with ./configure -enable-modules=crystallization . Furthermore, this feature is still being developed so take care when using it and report any problems on the mailing list.

Calculate the local degree of order around an atoms by taking the average dot product between the  $q_4$  vector on the central atom and the  $q_4$  vector on the atoms in the first coordination sphere.

The Q4 command allows one to calculate one complex vectors for each of the atoms in your system that describe the degree of order in the coordination sphere around a particular atom. The difficulty with these vectors comes when combining the order parameters from all of the individual atoms/molecules so as to get a measure of the global degree of order for the system. The simplest way of doing this - calculating the average Steinhardt parameter - can be problematic. If one is examining nucleation say only the order parameters for those atoms in the nucleus will change significantly when the nucleus forms. The order parameters for the atoms in the surrounding liquid will remain pretty much the same. As such if one models a small nucleus embedded in a very large amount of solution/melt any change in the average order parameter will be negligible. Substantial changes in the value of this average can be observed in simulations of nucleation but only because the number of atoms is relatively small.

When the average Q4 parameter is used to bias the dynamics a problems can occur. These averaged coordinates cannot distinguish between the correct, single-nucleus pathway and a concerted pathway in which all the atoms rearrange themselves into their solid-like configuration simultaneously. This second type of pathway would be impossible in reality because there is a large entropic barrier that prevents concerted processes like this from happening. However, in the finite sized systems that are commonly simulated this barrier is reduced substantially. As a result in simulations where average Steinhardt parameters are biased there are often quite dramatic system size effects

If one wants to simulate nucleation using some form on biased dynamics what is really required is an order parameter that measures:

- Whether or not the coordination spheres around atoms are ordered
- · Whether or not the atoms that are ordered are clustered together in a crystalline nucleus

LOCAL\_AVERAGE and NLINKS are variables that can be combined with the Steinhardt parameteters allow to calculate variables that satisfy these requirements. LOCAL\_Q4 is another variable that can be used in these sorts of calculations. The LOCAL\_Q4 parameter for a particular atom is a number that measures the extent to which the orientation of the atoms in the first coordination sphere of an atom match the orientation of the central atom. It does this by calculating the following quantity for each of the atoms in the system:

$$s_i = \frac{\sum_j \sigma(r_{ij}) \sum_{m=-4}^4 q_{4m}^*(i) q_{4m}(j)}{\sum_j \sigma(r_{ij})}$$

where  $q_{4m}(i)$  and  $q_{4m}(j)$  are the 4th order Steinhardt vectors calculated for atom i and atom j respectively and the asterix denotes complex conjugation. The function  $\sigma(r_{ij})$  is a switchingfunction that acts on the distance between atoms i and j. The parameters of this function should be set so that it the function is equal to one when atom j is in the first coordination sphere of atom i and is zero otherwise. The sum in the numerator of this expression is the dot product of the Steinhardt parameters for atoms i and j and thus measures the degree to which the orientations of these adjacent atoms is correlated.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. <code>label.lessthan-1</code>, <code>label.lessthan-2</code> etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity         | Keyword   | Description   |
|------------------|-----------|---|
| between          | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest          | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan         | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest           | LOWEST    | the lowest of the quantitities calculated by this action  |
| mean             | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min              | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment           | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan         | MORE_THAN | the number of values more than a target value. This is calculated using one of the  |
| Generated by Dox | ygen      | formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.   |

The atoms involved can be specified using

| SPECIES | this keyword is used for colvars such as coordination number. In that context it specifies that plumed  |
|---------|---|
|         | should calculate one coordination number for each of the atoms specified. Each of these coordi-         |
|         | nation numbers specifies how many of the other specified atoms are within a certain cutoff of the       |
|         | central atom. You can specify the atoms here as another multicolvar action or using a MultiColvar ↔     |
|         | Filter or ActionVolume action. When you do so the quantity is calculated for those atoms specified      |
|         | in the previous multicolvar. This is useful if you would like to calculate the Steinhardt parameter for |
|         | those atoms that have a coordination number more than four for example                                  |

Or alternatively by using

| SPECIESA | this keyword is used for colvars such as the coordination number. In that context it species that plumed should calculate one coordination number for each of the atoms specified in SPECIESA. Each of these cooordination numbers specifies how many of the atoms specifies using SPEC—IESB is within the specified cutoff. As with the species keyword the input can also be specified using the label of another multicolvar |
|----------|---|
| SPECIESB | this keyword is used for colvars such as the coordination number. It must appear with SPECIESA. For a full explanation see the documentation for that keyword   |

# Compulsory keywords

| NN | ( default=6 ) The n parameter of the switching function                 |
|----|---|
| MM | ( default=0 ) The m parameter of the switching function; 0 implies 2*NN |
| D← | ( default=0.0 ) The d_0 parameter of the switching function             |
| _0 |   |
| R↔ | The r_0 parameter of the switching function                             |
| _0 |   |

# Options

| ( default=off ) ignore the periodic boundary conditions when calculating distances   |
|--|
| ( default=off ) do the calculation in serial. Do not parallelize   |
| ( default=off ) lower the memory requirements  |
| ( default=off ) output information on the timings of the various parts of the calculation  |
| This keyword is used if you want to employ an alternative to the continuous swiching function defined above. The following provides information on the switchingfunction that are available. When this keyword is present you no longer need the NN, MM, D_0 and R_0 keywords.   |
| take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEAN2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3  |
| calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using label.morethan. You can use multiple instances of this keyword i.e. MORE_THA $\hookrightarrow$ N1, MORE_THAN2, MORE_THAN3 The corresponding values are then referenced using label.morethan-1, label.morethan-2, label.morethan-3 |
|  |

Generated by Doxygen

| LESS_THAN | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using label.lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_T HAN2, LESS_THAN3 The corresponding values are then referenced using label.lessthan-1, label.lessthan-2, label.lessthan-3   |
|-----------|--|
| MIN       | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3 |
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BET—WEEN1, BETWEEN2, BETWEEN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3   |
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGR← AM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .   |
| LOWEST    | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST   | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |

### **Examples**

The following command calculates the average value of the LOCAL\_Q4 parameter for the 64 Lennard Jones atoms in the system under study and prints this quantity to a file called colvar.

```
Q4 SPECIES=1-64 D_0=1.3 R_0=0.2 LABEL=q4 LOCAL_Q4 ARG=q4 SWITCH={RATIONAL D_0=1.3 R_0=0.2} MEAN LABEL=1q4 PRINT ARG=1q4.mean FILE=colvar
```

The following input calculates the distribution of LOCAL\_Q4 parameters at any given time and outputs this information to a file.

```
Q4 SPECIES=1-64 D_0=1.3 R_0=0.2 LABEL=q4 LOCAL_Q4 ARG=q4 SWITCH={RATIONAL D_0=1.3 R_0=0.2} HISTOGRAM={GAUSSIAN LOWER=0.0 UPPER=1.0 NBINS=20 SMEAR=0.1} PRINT ARG=lq4.* FILE=colvar
```

The following calculates the LOCAL\_Q4 parameters for atoms 1-5 only. For each of these atoms comparisons of the geometry of the coordination sphere are done with those of all the other atoms in the system. The final quantity is the average and is outputted to a file

```
Q4 SPECIESA=1-5 SPECIESB=1-64 D_0=1.3 R_0=0.2 LABEL=q4a
Q4 SPECIESA=6-64 SPECIESB=1-64 D_0=1.3 R_0=0.2 LABEL=q4b

LOCAL_Q4 ARG=q4a,q4b SWITCH={RATIONAL D_0=1.3 R_0=0.2} MEAN LOWMEM LABEL=w4
PRINT ARG=w4.* FILE=colvar
```

5.5.45 LOCAL\_Q6

This is part of the crystallization module

It is only available if you configure PLUMED with ./configure –enable-modules=crystallization . Further-more, this feature is still being developed so take care when using it and report any problems on the mailing list.

Calculate the local degree of order around an atoms by taking the average dot product between the  $q_6$  vector on the central atom and the  $q_6$  vector on the atoms in the first coordination sphere.

The Q6 command allows one to calculate one complex vectors for each of the atoms in your system that describe the degree of order in the coordination sphere around a particular atom. The difficulty with these vectors comes when combining the order parameters from all of the individual atoms/molecules so as to get a measure of the global degree of order for the system. The simplest way of doing this - calculating the average Steinhardt parameter - can be problematic. If one is examining nucleation say only the order parameters for those atoms in the nucleus will change significantly when the nucleus forms. The order parameters for the atoms in the surrounding liquid will remain pretty much the same. As such if one models a small nucleus embedded in a very large amount of solution/melt any change in the average order parameter will be negligible. Substantial changes in the value of this average can be observed in simulations of nucleation but only because the number of atoms is relatively small.

When the average Q6 parameter is used to bias the dynamics a problems can occur. These averaged coordinates cannot distinguish between the correct, single-nucleus pathway and a concerted pathway in which all the atoms rearrange themselves into their solid-like configuration simultaneously. This second type of pathway would be impossible in reality because there is a large entropic barrier that prevents concerted processes like this from happening. However, in the finite sized systems that are commonly simulated this barrier is reduced substantially. As a result in simulations where average Steinhardt parameters are biased there are often quite dramatic system size effects

If one wants to simulate nucleation using some form on biased dynamics what is really required is an order parameter that measures:

- · Whether or not the coordination spheres around atoms are ordered
- · Whether or not the atoms that are ordered are clustered together in a crystalline nucleus

LOCAL\_AVERAGE and NLINKS are variables that can be combined with the Steinhardt parameteters allow to calculate variables that satisfy these requirements. LOCAL\_Q6 is another variable that can be used in these sorts of calculations. The LOCAL\_Q6 parameter for a particular atom is a number that measures the extent to which the orientation of the atoms in the first coordination sphere of an atom match the orientation of the central atom. It does this by calculating the following quantity for each of the atoms in the system:

$$s_i = \frac{\sum_j \sigma(r_{ij}) \sum_{m=-6}^6 q_{6m}^*(i) q_{6m}(j)}{\sum_j \sigma(r_{ij})}$$

where  $q_{6m}(i)$  and  $q_{6m}(j)$  are the 6th order Steinhardt vectors calculated for atom i and atom j respectively and the asterix denotes complex conjugation. The function  $\sigma(r_{ij})$  is a switchingfunction that acts on the distance between atoms i and j. The parameters of this function should be set so that it the function is equal to one when atom j is in the first coordination sphere of atom i and is zero otherwise. The sum in the numerator of this expression is the dot product of the Steinhardt parameters for atoms i and j and thus measures the degree to which the orientations of these adjacent atoms is correlated.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

# SPECIES

this keyword is used for colvars such as coordination number. In that context it specifies that plumed should calculate one coordination number for each of the atoms specified. Each of these coordination numbers specifies how many of the other specified atoms are within a certain cutoff of the central atom. You can specify the atoms here as another multicolvar action or using a MultiColvar Filter or ActionVolume action. When you do so the quantity is calculated for those atoms specified in the previous multicolvar. This is useful if you would like to calculate the Steinhardt parameter for those atoms that have a coordination number more than four for example

Or alternatively by using

#### **SPECIESA**

this keyword is used for colvars such as the coordination number. In that context it species that plumed should calculate one coordination number for each of the atoms specified in SPECIESA. Each of these cooordination numbers specifies how many of the atoms specifies using SPEC IESB is within the specified cutoff. As with the species keyword the input can also be specified using the label of another multicolvar

| CDECIEC |  |
|---------|--|
| SPECIES |  |
|         |  |

this keyword is used for colvars such as the coordination number. It must appear with SPECIESA. For a full explanation see the documentation for that keyword

# Compulsory keywords

| NN | ( default=6 ) The n parameter of the switching function                 |
|----|---|
| ММ | ( default=0 ) The m parameter of the switching function; 0 implies 2*NN |
| D← | ( default=0.0 ) The d_0 parameter of the switching function             |
| _0 |   |
| R← | The r_0 parameter of the switching function                             |
| _0 |   |

# Options

| NOPBC     | ( default=off ) ignore the periodic boundary conditions when calculating distances   |
|-----------|--|
| SERIAL    | ( default=off ) do the calculation in serial. Do not parallelize   |
| LOWMEM    | ( default=off ) lower the memory requirements  |
| TIMINGS   | ( default=off ) output information on the timings of the various parts of the calculation  |
| SWITCH    | This keyword is used if you want to employ an alternative to the continuous swiching function defined above. The following provides information on the switchingfunction that are available. When this keyword is present you no longer need the NN, MM, D_0 and R_0 keywords.   |
| MEAN      | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEAN2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3  |
| MORE_THAN | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using label.morethan. You can use multiple instances of this keyword i.e. MORE_THA $\leftarrow$ N1, MORE_THAN2, MORE_THAN3 The corresponding values are then referenced using label.morethan-1, label.morethan-2, label.morethan-3  |
| LESS_THAN | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using label.lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_T $\leftarrow$ HAN2, LESS_THAN3 The corresponding values are then referenced using label.lessthan-1, label.lessthan-2, label.lessthan-3  |
| MIN       | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3 |
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BET—WEEN1, BETWEEN2, BETWEEN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3   |
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGR← AM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |

| MOMENTS | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ . |
|---------|--|
| LOWEST  | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |

#### **Examples**

The following command calculates the average value of the LOCAL\_Q6 parameter for the 64 Lennard Jones atoms in the system under study and prints this quantity to a file called colvar.

```
Q6 SPECIES=1-64 D_0=1.3 R_0=0.2 LABEL=q6 LOCAL_Q6 ARG=q6 SWITCH={RATIONAL D_0=1.3 R_0=0.2} MEAN LABEL=1q6 PRINT ARG=1q6.mean FILE=colvar
```

The following input calculates the distribution of LOCAL\_Q6 parameters at any given time and outputs this information to a file.

```
Q6 SPECIES=1-64 D_0=1.3 R_0=0.2 LABEL=q6 LOCAL_Q6 ARG=q6 SWITCH={RATIONAL D_0=1.3 R_0=0.2} HISTOGRAM={GAUSSIAN LOWER=0.0 UPPER=1.0 NBINS=20 SMEAR=0.1} PRINT ARG=1q6.* FILE=colvar
```

The following calculates the LOCAL\_Q6 parameters for atoms 1-5 only. For each of these atoms comparisons of the geometry of the coordination sphere are done with those of all the other atoms in the system. The final quantity is the average and is outputted to a file

```
Q6 SPECIESA=1-5 SPECIESB=1-64 D_0=1.3 R_0=0.2 LABEL=q6a
Q6 SPECIESA=6-64 SPECIESB=1-64 D_0=1.3 R_0=0.2 LABEL=q6b

LOCAL_Q6 ARG=q4a,q4b SWITCH={RATIONAL D_0=1.3 R_0=0.2} MEAN LOWMEM LABEL=w4
PRINT ARG=w6.* FILE=colvar
```

### 5.5.46 NLINKS

This is part of the multicolvar module

Calculate number of pairs of atoms/molecules that are "linked"

In its simplest guise this coordinate calculates a coordination number. Each pair of atoms is assumed "linked" if they are within some cutoff of each other. In more complex applications each entity is a vector and this quantity measures whether pairs of vectors are (a) within a certain cutoff and (b) if the two vectors have similar orientations. The vectors on individual atoms could be Steinhardt parameters (see Q3, Q4 and Q6) or they could describe some internal vector in a molecule.

The atoms involved can be specified using

| GROUP | . For more information on how to specify lists of atoms see Groups and Virtual Atoms |  |
|-------|--|--|
|-------|--|--|

Or alternatively by using

| GROUPA |  |
|--------|--|
| GROUPB |  |

#### Compulsory keywords

| NN | ( default=6 ) The n parameter of the switching function                 |
|----|---|
| ММ | ( default=0 ) The m parameter of the switching function; 0 implies 2*NN |
| D↔ | ( default=0.0 ) The d_0 parameter of the switching function             |
| _0 |   |
| R⇔ | The r_0 parameter of the switching function                             |
| _0 |   |

#### **Options**

| NOPBC   | ( default=off ) ignore the periodic boundary conditions when calculating distances   |
|---------|--|
| SERIAL  | ( default=off ) do the calculation in serial. Do not parallelize   |
| TIMINGS | ( default=off ) output information on the timings of the various parts of the calculation  |
| LOWMEM  | ( default=off ) lower the memory requirements  |
| SWITCH  | This keyword is used if you want to employ an alternative to the continuous swiching function defined above. The following provides information on the switchingfunction that are available. When this keyword is present you no longer need the NN, MM, D_0 and R_0 keywords. |

# Examples

The following calculates how many bonds there are in a system containing 64 atoms and outputs this quantity to a file.

```
DENSITY SPECIES=1-64 LABEL=d1
NLINKS ARG=d1 SWITCH={RATIONAL D_0=1.3 R_0=0.2} LABEL=dd
PRINT ARG=dd FILE=colvar
```

The following calculates how many pairs of neighbouring atoms in a system containg 64 atoms have similar dispositions for the atoms in their coordination sphere. This calculation uses the dot product of the Q6 vectors on adjacent atoms to measure whether or not two atoms have the same "orientation"

```
Q6 SPECIES=1-64 SWITCH={RATIONAL D_0=1.3 R_0=0.2} LABEL=q6 NLINKS ARG=q6 SWITCH={RATIONAL D_0=1.3 R_0=0.2} LABEL=dd PRINT ARG=dd FILE=colvar
```

### 5.5.47 SMAC

This is part of the crystallization module

It is only available if you configure PLUMED with ./configure –enable-modules=crystallization. Further-more, this feature is still being developed so take care when using it and report any problems on the mailing list.

Calculate a variant on the SMAC collective variable discussed in ?

The SMAC collective variable can be used to study the formation of molecular solids from either the melt or from solution. The idea behind this variable is that what differentiates a molecular solid from a molecular liquid is an alignment of internal vectors in neighboring molecules. In other words, the relative orientation of neighboring molecules is no longer random as it is in a liquid. In a solid particular torsional angles between molecules are preferred. As such this CV calculates the following average:

$$s_i = \frac{\left\{1 - \psi\left[\sum_{j \neq i} \sigma(r_{ij})\right]\right\} \sum_{j \neq i} \sigma(r_{ij}) \sum_n K_n(\theta_{ij})}{\sum_{j \neq i} \sigma(r_{ij})}$$

In this expression  $r_{ij}$  is the distance between molecule i and molecule j and  $\sigma(r_{ij})$  is a switchingfunction that acts on this distance. By including this switching function in the second summation in the numerator and in the denominator we are thus ensuring that we calculate an average over the molecules in the first coordination sphere of molecule i. All molecules in higher coordination sphere will essentially contribute zero to the sums in the above expression because their  $\sigma(r_{ij})$  will be very small.  $\psi$  is also a switching function. The term including  $\psi$  in the numerator is there to ensure that only those molecules that are attached to a reasonably large number of molecules. It is important to include this "more than" switching function when you are simulating nucleation from solution with this CV. Lastly, the \$K\_n functions are kernelfunctions that take the torsion angle,  $\theta_{ij}$ , between the internal orientation vectors for molecules i and j as input. These kernel functions should be set so that they are equal to one when the relative orientation of the molecules are as they are in the solid and equal to zero otherwise. The final  $s_i$  quantity thus measures whether (on average) the molecules in the first coordination sphere around molecule i are oriented as they would be in the solid. Furthermore, this Action is a multicolvar so you can calculate the  $s_i$  values for all the molecules in your system simultaneously and then determine the average, the number less than and so on.

Description of components

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. <code>label.lessthan-1</code>, <code>label.lessthan-2</code> etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

The atoms involved can be specified using

| SPECIES | this keyword is used for colvars such as coordination number. In that context it specifies that plumed  |
|---------|---|
|         | should calculate one coordination number for each of the atoms specified. Each of these coordi-         |
|         | nation numbers specifies how many of the other specified atoms are within a certain cutoff of the       |
|         | central atom. You can specify the atoms here as another multicolvar action or using a MultiColvar←      |
|         | Filter or ActionVolume action. When you do so the quantity is calculated for those atoms specified      |
|         | in the previous multicolvar. This is useful if you would like to calculate the Steinhardt parameter for |
|         | those atoms that have a coordination number more than four for example                                  |

Or alternatively by using

| SPECIESA | this keyword is used for colvars such as the coordination number. In that context it species that plumed should calculate one coordination number for each of the atoms specified in SPECIESA. Each of these cooordination numbers specifies how many of the atoms specifies using SPEC—IESB is within the specified cutoff. As with the species keyword the input can also be specified using the label of another multicolvar |
|----------|---|
| SPECIESB | this keyword is used for colvars such as the coordination number. It must appear with SPECIESA. For a full explanation see the documentation for that keyword   |

# Compulsory keywords

| NN  | ( default=6 ) The n parameter of the switching function                 |
|-----|---|
| ММ  | ( default=0 ) The m parameter of the switching function; 0 implies 2*NN |
| D_0 | ( default=0.0 ) The d_0 parameter of the switching function             |
| R_0 | The r_0 parameter of the switching function                             |

| KERNEL       | The kernels used in the function of the angle You can use multiple instances of this keyword i.e. KERNEL1, KERNEL2, KERNEL3 |
|--------------|---|
| SWITCH_COORD | This keyword is used to define the coordination switching function.   |

# **Options**

| NOPBC     | ( default=off ) ignore the periodic boundary conditions when calculating distances   |
|-----------|--|
| SERIAL    | ( default=off ) do the calculation in serial. Do not parallelize   |
| LOWMEM    | ( default=off ) lower the memory requirements  |
| TIMINGS   | ( default=off ) output information on the timings of the various parts of the calculation  |
| SWITCH    | This keyword is used if you want to employ an alternative to the continuous swiching function defined above. The following provides information on the switchingfunction that are available. When this keyword is present you no longer need the NN, MM, D_0 and R_0 keywords.   |
| MEAN      | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEAN2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3  |
| MORE_THAN | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using label.morethan. You can use multiple instances of this keyword i.e. MORE_THA $\hookrightarrow$ N1, MORE_THAN2, MORE_THAN3 The corresponding values are then referenced using label.morethan-1, label.morethan-2, label.morethan-3   |
| LESS_THAN | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using label.lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_T HAN2, LESS_THAN3 The corresponding values are then referenced using label.lessthan-1, label.lessthan-2, label.lessthan-3   |
| MIN       | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3 |
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using label.between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWEEN3 The corresponding values are then referenced using label.between-1, label.between-2, label.between-3  |
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGR← AM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .   |
| LOWEST    | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST   | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |
|           |  |

#### **Examples**

In the example below the orientation of the molecules in the system is determined by calculating the vector that connects a pair of atoms. SMAC is then used to determine whether the molecules are sitting in a solid or liquid like environment. We can determine whether the environment is solid or liquid like because in the solid the torsional angle between the bond vectors on adjacent molecules is close to 0 or  $\pi$ . The final quantity that is output to the colvar file measures the number of molecules that have a SMAC parameter that is greater than 0.7. N.B. By using the indices of three atoms for each of the MOL keywords below we are telling PLUMED to use the first two numbers to determine the orientation of the molecule that will ultimately be used when calculating the  $\theta_{ij}$  terms in the formula above. The atom with the third index meanwhile is used when we calculate  $r_{ij}$ .

```
MOLECULES ...
MOL1=9, 10, 9
MOL2=89,90,89
MOL3=473,474,473
MOL4=1161,1162,1161
MOL5=1521, 1522, 1521
MOL6=1593,1594,1593
MOL7=1601,1602,1601
MOL8=2201,2202,2201
LABEL=m3
... MOLECULES
   SPECIES=m3 LOWMEM
   KERNEL1={GAUSSIAN CENTER=0 SIGMA=0.480} KERNEL2={GAUSSIAN CENTER=pi SIGMA=0.480}
   SWITCH={RATIONAL R_0=0.6} MORE_THAN={RATIONAL R_0=0.7} SWITCH_COORD={EXP R_0=4}
   LABEL=s2
... SMAC
PRINT ARG=s2.* FILE=colvar
```

This second example works in a way that is very similar to the previous command. Now, however, the orientation of the molecules is determined by finding the plane that contains the positions of three atoms.

```
PLANES ..
MOL1=9, 10, 11
MOL2=89,90,91
MOL3=473,474,475
MOL4=1161,1162,1163
MOL5=1521,1522,1523
MOL6=1593,1594,1595
MOL7=1601,1602,1603
MOL8=2201,2202,2203
VMEAN
LABEL=m3
... PLANES
   SPECIES=m3 LOWMEM
   KERNEL1={GAUSSIAN CENTER=0 SIGMA=0.480} KERNEL2={GAUSSIAN CENTER=pi SIGMA=0.480}
   SWITCH={RATIONAL R_0=0.6} MORE_THAN={RATIONAL R_0=0.7} SWITCH_COORD={EXP R_0=3.0}
   LABEL-s2
... SMAC
PRINT ARG=s2.* FILE=colvar
```

### 5.5.48 MTRANSFORM\_BETWEEN

This is part of the multicolvar module

This action can be useed to transform the colvar values calculated by a multicolvar using a histogrambead

In this action each colvar,  $s_i$ , calculated by multicolvar is transformed by a histogrambead function that is equal to one if the colvar is within a certain range and which is equal to zero otherwise. In other words, we compute:

$$f_i = \int_a^b K\left(\frac{s - s_i}{w}\right)$$

where a, b and w are parameters.

It is important to understand the distinction between what is done here and what is done by MFILTER\_BETWEEN. In MFILTER\_BETWEEN a weight,  $w_i$  for the colvar is calculated using the histogrambead. If one calculates the MEAN for MFILTER\_BETWEEN one is thus calculating:

$$\mu = \frac{\sum_{i} f_i s_i}{\sum_{i} f_i}$$

In this action by contrast the colvar is being transformed by the histogrambead. If one thus calculates a MEAN for thia action one computes:

$$\mu = \frac{\sum_{i=1}^{N} f_i}{N}$$

In other words, you are calculating the mean for the transformed colvar.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. <code>label.lessthan-1</code>, <code>label.lessthan-2</code> etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword | Description  |
|----------|---------|--|
| vmean    | VMEAN   | the norm of the mean vector. The output component can be refererred to elsewhere in the input file by using the label.vmean      |
| altmin   | ALT_MIN | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous. |
| highest  | HIGHEST | the lowest of the quantitities calculated by this action   |
| lowest   | LOWEST  | the lowest of the quantitities calculated by this action   |
| max      | MAX     | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous. |
| mean     | MEAN    | the mean value. The output component can be refererred to elsewhere in the input   |
|          |         | file by using the label.mean Generated by Doxygen  |
| min      | MIN     | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous. |
| moment   | MOMENTS | the central moments of the distribution of values. The second moment would be refer-   |

# Compulsory keywords

| DATA  | The multicolvar that calculates the set of base quantities that we are interested in  |
|-------|---|
| LOWER | the lower boundary for the range of interest  |
| UPPER | the upper boundary for the range of interest  |
| SMEAR | ( default=0.5 ) the ammount by which to smear the value for kernel density estimation |

# **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances   |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize   |
| LOWMEM                | ( default=off ) lower the memory requirements  |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation  |
| VMEAN                 | calculate the norm of the mean vector. The final value can be referenced using label.vmean. You can use multiple instances of this keyword i.e. VMEAN1, VMEAN2, VMEAN3 The corresponding values are then referenced using label.vmean-1, label.vmean-2, label.vmean-3  |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA $\leftarrow$ N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3  |
| MOMENTS               | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^N(s_i-\bar{s})^m$ , where $\bar{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .   |
| MIN                   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3 |
| MAX                   | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3        |
| ALT_MIN               | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3               |
| LOWEST                | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |

| HIGHEST | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest   |
|---------|---|
| BEAD    | This keywords is used if you want to employ an alternative to the function defeind above. The following provides information on the histogrambead that are available. When this keyword is present you no longer need the LOWER, U PPER and SMEAR keywords. |

#### **Examples**

The following input gives an example of how a MTRANSFORM\_BETWEEN action can be used to duplicate functionality that is elsehwere in PLUMED.

```
DISTANCES ...

GROUPA=1-10 GROUPB=11-20

LABEL=d1

... DISTANCES

MTRANSFORM_BETWEEN DATA=d1 LOWER=1.0 UPPER=2.0 SMEAR=0.5
```

In this case you can achieve the same result by using:

```
DISTANCES ...

GROUPA=1-10 GROUPB=11-20

BETWEEN={GAUSSIAN LOWER=1.0 UPPER=2.0}
... DISTANCES
```

### (see DISTANCES)

The advantage of MTRANSFORM\_BETWEEN comes, however, if you want to use transformed colvars as input for MULTICOLVARDENS

### 5.5.49 MTRANSFORM LESS

This is part of the multicolvar module

This action can be useed to transform the colvar values calculated by a multicolvar using a switchingfunction

In this action each colvar,  $s_i$ , calculated by multicolvar is transformed by a switchingfunction function that is equal to one if the colvar is less than a certain target value and which is equal to zero otherwise. It is important to understand the distinction between what is done here and what is done by MFILTER\_LESS. In MFILTER\_LESS a weight,  $w_i$  for the colvar is calculated using the switchingfunction. If one calculates the MEAN for MFILTER\_LESS one is thus calculating:

$$\mu = \frac{\sum_{i} \sigma(s_i) s_i}{\sum_{i} (s_i)}$$

where  $\sigma$  is the switchingfunction. In this action by contrast the colvar is being transformed by the switchingfunction. If one thus calculates a MEAN for thia action one computes:

$$\mu = \frac{\sum_{i=1}^{N} (s_i)}{N}$$

In other words, you are calculating the mean for the transformed colvar.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword | Description  |
|----------|---------|--|
| vmean    | VMEAN   | the norm of the mean vector. The output component can be refererred to elsewhere in the input file by using the label.vmean  |
| altmin   | ALT_MIN | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.   |
| highest  | HIGHEST | the lowest of the quantitities calculated by this action   |
| lowest   | LOWEST  | the lowest of the quantitities calculated by this action   |
| max      | MAX     | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.   |
| mean     | MEAN    | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean  |
| min      | MIN     | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.   |
| moment   | MOMENTS | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc. |

# Compulsory keywords

| DATA | The multicolvar that calculates the set of base quantities that we are interested in |
|------|--|
| NN   | ( default=6 ) The n parameter of the switching function                              |
| MM   | ( default=0 ) The m parameter of the switching function                              |
| D_0  | ( default=0.0 ) The d_0 parameter of the switching function                          |
| R_0  | The r_0 parameter of the switching function  |

**Options** 

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances   |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize   |
| LOWMEM                | ( default=off ) lower the memory requirements  |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation  |
| VMEAN                 | calculate the norm of the mean vector. The final value can be referenced using <i>label.</i> vmean. You can use multiple instances of this keyword i.e. VMEAN1, VMEAN2, VMEAN3 The corresponding values are then referenced using <i>label.</i> vmean-1, <i>label.</i> vmean-2, <i>label.</i> vmean-3  |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA← N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3  |
| MOMENTS               | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^N(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .   |
| MIN                   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3 |
| MAX                   | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3        |
| ALT_MIN               | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3               |
| LOWEST                | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST               | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |
| SWITCH                | This keyword is used if you want to employ an alternative to the continuous swiching function defined above. The following provides information on the switchingfunction that are available. When this keyword is present you no longer need the NN, MM, D_0 and R_0 keywords.   |

## **Examples**

The following input gives an example of how a MTRANSFORM\_LESS action can be used to duplicate functionality that is elsehwere in PLUMED.

```
DISTANCES ...

GROUPA=1-10 GROUPB=11-20

LABEL=d1
... DISTANCES

MTRANSFORM_LESS DATA=d1 SWITCH={GAUSSIAN D_0=1.5 R_0=0.00001}
```

In this case you can achieve the same result by using:

```
DISTANCES ...

GROUPA=1-10 GROUPB=11-20

LESS_THAN={GAUSSIAN D_0=1.5 R_0=0.00001}
... DISTANCES
```

#### (see **DISTANCES**)

The advantage of MTRANSFORM\_LESS comes, however, if you want to use transformed colvars as input for MULTICOLVARDENS

### 5.5.50 MTRANSFORM\_MORE

This is part of the multicolvar module

This action can be useed to transform the colvar values calculated by a multicolvar using one minus a switchingfunction

In this action each colvar,  $s_i$ , calculated by multicolvar is transformed by a switchingfunction function that is equal to one if the colvar is greater than a certain target value and which is equal to zero otherwise. It is important to understand the distinction between what is done here and what is done by MFILTER\_MORE. In MFILTER\_MORE a weight,  $w_i$  for the colvar is calculated using the histogrambead. If one calculates the MEAN for MFILTER\_MORE one is thus calculating:

$$\mu = \frac{\sum_{i} [1 - \sigma(s_i)] s_i}{\sum_{i} [1 - \sigma(s_i)]}$$

where  $\sigma$  is the switchingfunction. In this action by contrast the colvar is being transformed by the switchingfunction. If one thus calculates a MEAN for this action one computes:

$$\mu = \frac{\sum_{i=1}^{N} 1 - \sigma(s_i)}{N}$$

In other words, you are calculating the mean for the transformed colvar.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. <code>label.lessthan-1</code>, <code>label.lessthan-2</code> etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword | Description  |
|----------|---------|--|
| vmean    | VMEAN   | the norm of the mean vector. The output component can be refererred to elsewhere     |
|          |         | in the input file by using the label.vmean   |
| altmin   | ALT_MIN | the minimum value. This is calculated using the formula described in the description |
|          |         | of the keyword so as to make it continuous.  |
| highest  | HIGHEST | the lowest of the quantitities calculated by this action                             |
| lowest   | LOWEST  | the lowest of the quantitities calculated by this action                             |
| max      | MAX     | the maximum value. This is calculated using the formula described in the description |
|          |         | of the keyword so as to make it continuous.  |
| mean     | MEAN    | the mean value. The output component can be refererred to elsewhere in the input     |
|          |         | file by using the label.mean   |
| min      | MIN     | the minimum value. This is calculated using the formula described in the description |
|          |         | of the keyword so as to make it continuous.  |
| moment   | MOMENTS | the central moments of the distribution of values. The second moment would be refer- |
|          |         | enced elsewhere in the input file using label.moment-2, the third as label.moment-3, |
|          |         | etc.   |

# Compulsory keywords

| DATA | The multicolvar that calculates the set of base quantities that we are interested in |
|------|--|
| NN   | ( default=6 ) The n parameter of the switching function                              |
| MM   | ( default=0 ) The m parameter of the switching function; 0 implies 2*NN              |
| D_0  | ( default=0.0 ) The d_0 parameter of the switching function                          |
| R_0  | The r_0 parameter of the switching function  |

# Options

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances   |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize   |
| LOWMEM                | ( default=off ) lower the memory requirements  |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation  |
| VMEAN                 | calculate the norm of the mean vector. The final value can be referenced using label.vmean. You can use multiple instances of this keyword i.e. VMEAN1, VMEAN2, VMEAN3 The corresponding values are then referenced using label.vmean-1, label.vmean-2, label.vmean-3  |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA← N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3  |
| MOMENTS               | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^N(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ . |

| MIN     | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3 |
|---------|--|
| MAX     | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3        |
| ALT_MIN | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta} \log \sum_i \exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3            |
| LOWEST  | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |
| SWITCH  | This keyword is used if you want to employ an alternative to the continuous switching function defined above. The following provides information on the switchingfunction that are available. When this keyword is present you no longer need the NN, MM, D_0 and R_0 keywords.  |

### **Examples**

The following input gives an example of how a MTRANSFORM\_MORE action can be used to duplicate functionality that is elsehwere in PLUMED.

```
DISTANCES ...

GROUPA=1-10 GROUPB=11-20

LABEL=d1

... DISTANCES

MTRANSFORM_MORE DATA=d1 SWITCH={GAUSSIAN D_0=1.5 R_0=0.00001}
```

In this case you can achieve the same result by using:

```
DISTANCES ...

GROUPA=1-10 GROUPB=11-20

MORE_THAN={GAUSSIAN D_0=1.5 R_0=0.00001}
... DISTANCES
```

## (see DISTANCES)

The advantage of MTRANSFORM\_MORE comes, however, if you want to use transformed colvars as input for MULTICOLVARDENS

### 5.5.51 LWALLS

This is part of the manyrestraints module

It is only available if you configure PLUMED with ./configure –enable-modules=manyrestraints. Furthermore, this feature is still being developed so take care when using it and report any problems on the mailing list.

Add LOWER\_WALLS restraints on all the multicolvar values

This action takes the set of values calculated by the colvar specified by label in the DATA keyword and places a restraint on each quantity, x, with the following functional form:

$$k((x-a+o)/s)^e$$

k (KAPPA) is an energy constant in internal unit of the code, s (EPS) a rescaling factor and e (EXP) the exponent determining the power law. By default: EXP = 2, EPS = 1.0, OFF = 0.

**Description of components** 

By default the value of the calculated quantity can be referenced elsewhere in the input file by using the label of the action. Alternatively this Action can be used to be used to calculate the following quantities by employing the keywords listed below. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Description                                    |
|----------|--|
| bias     | the instantaneous value of the bias potentials |

In addition the following quantities can be calculated by employing the keywords listed below

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| gradient | GRADIENT  | the gradient  |
| vmean    | VMEAN     | the norm of the mean vector. The output component can be refererred to elsewhere in the input file by using the label.vmean   |
| vsum     | VSUM      | the norm of sum of vectors. The output component can be refererred to elsewhere in the input file by using the label.vsum   |
| spath    | SPATH     | the position on the path  |
| gspath   | GPATH     | the position on the path calculated using trigonometry  |
| gzpath   | GPATH     | the distance from the path calculated using trigonometry  |
| zpath    | ZPATH     | the distance from the path  |
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |

| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean  |
|----------|-----------|--|
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.   |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.   |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| sum      | SUM       | the sum of values  |

#### Compulsory keywords

| DATA   | certain actions in plumed work by calculating a list of variables and summing over them. This particular action can be used to calculate functions of these base variables or prints them to a file. This keyword thus takes the label of one of those such variables as input. |  |
|--------|---|--|
| AT     | the radius of the sphere  |  |
| KAPPA  | the force constant for the wall. The k_i in the expression for a wall.  |  |
| OFFSET | ( default=0.0 ) the offset for the start of the wall. The o_i in the expression for a wall.   |  |
| EXP    | ( default=2.0 ) the powers for the walls. The e_i in the expression for a wall.   |  |
| EPS    | ( default=1.0 ) the values for s_i in the expression for a wall   |  |

## **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically                |
|-----------------------|---|
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize                          |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation |

## Examples

The following set of commands can be used to stop any of the 800 atoms in group A from moving more than 2.46425 nm in the z direction from atom 34137. This is done by adding a lower wall on the z-distance between all the atoms in group A and the position of 34137.

1: ZDISTANCES GROUPA=1-800 GROUPB=34137 NOPBC LWALLS DATA=1 AT=2.46465 KAPPA=150.0 EXP=2 EPS=1 OFFSET=0 LABEL=lwall

## 5.5.52 UWALLS

### This is part of the manyrestraints module

It is only available if you configure PLUMED with ./configure —enable-modules=manyrestraints . Furthermore, this feature is still being developed so take care when using it and report any problem somethe mailing list.

Add UPPER\_WALLS restraints on all the multicolvar values

This action takes the set of values calculated by the colvar specified by label in the DATA keyword and places a restraint on each quantity, x, with the following functional form:

$$k((x-a+o)/s)^e$$

k (KAPPA) is an energy constant in internal unit of the code, s (EPS) a rescaling factor and e (EXP) the exponent determining the power law. By default: EXP = 2, EPS = 1.0, OFF = 0.

**Description of components** 

By default the value of the calculated quantity can be referenced elsewhere in the input file by using the label of the action. Alternatively this Action can be used to be used to calculate the following quantities by employing the keywords listed below. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Description                                    |
|----------|--|
| bias     | the instantaneous value of the bias potentials |

In addition the following quantities can be calculated by employing the keywords listed below

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| gradient | GRADIENT  | the gradient  |
| vmean    | VMEAN     | the norm of the mean vector. The output component can be refererred to elsewhere in the input file by using the label.vmean   |
| vsum     | VSUM      | the norm of sum of vectors. The output component can be refererred to elsewhere in the input file by using the label.vsum   |
| spath    | SPATH     | the position on the path  |
| gspath   | GPATH     | the position on the path calculated using trigonometry  |
| gzpath   | GPATH     | the distance from the path calculated using trigonometry  |
| zpath    | ZPATH     | the distance from the path  |
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |

| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the |
|----------|-----------|--|
|          |           | formula described in the description of the keyword so as to make it continuous.   |
|          |           | You can calculate this quantity multiple times using different parameters.         |
| sum      | SUM       | the sum of values  |

#### Compulsory keywords

| DATA   | certain actions in plumed work by calculating a list of variables and summing over them. This particular action can be used to calculate functions of these base variables or prints them to a file. This keyword thus takes the label of one of those such variables as input. |  |
|--------|---|--|
| AT     | the radius of the sphere  |  |
| KAPPA  | the force constant for the wall. The k_i in the expression for a wall.  |  |
| OFFSET | ( default=0.0 ) the offset for the start of the wall. The o_i in the expression for a wall.   |  |
| EXP    | ( default=2.0 ) the powers for the walls. The e_i in the expression for a wall.   |  |
| EPS    | ( default=1.0 ) the values for s_i in the expression for a wall   |  |

#### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically                |
|-----------------------|---|
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize                          |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation |

### **Examples**

The following set of commands can be used to stop a cluster composed of 20 atoms subliming. The position of the centre of mass of the cluster is calculated by the COM command labelled c1. The DISTANCES command labelled d1 is then used to calculate the distance between each of the 20 atoms in the cluster and the center of mass of the cluster. These distances are then passed to the UWALLS command, which adds a UPPER\_WALLS restraint on each of them and thereby prevents each of them from moving very far from the centre of mass of the cluster.

COM ATOMS=1-20 LABEL=c1
DISTANCES GROUPA=c1 GROUPB=1-20 LABEL=d1
UWALLS DATA=d1 AT=2.5 KAPPA=0.2 LABEL=sr

# 5.6 Exploiting contact matrices

A contact matrix is an  $N \times N$  matrix in which the ith, jth element tells you whether or not the ith and jth atoms/molecules from a set of N atoms/molecules are adjacent or not. There are various ways of definining whether a pair of atoms/molecules are adjacent or not. For example we can say two atoms are adjacent if the distance between them is less than some cutoff. Alternatively, if we have a have a pair of molecules, we might state they are adjacent if their centre's of mass are within a certain cutoff and if the two molecules have the same orientation. Two electronegative atoms might be said to be adjacent if there is a hydrogen bond between them. For these reasons then PLUMED contains all of the following methods for calculating an adjacency matrix

| ALIGNED_MATRIX       | Adjacency matrix in which two molecule are adjacent if they are within a certain cutoff and if they have the same orientation.                   |
|----------------------|--|
| CONTACT_MATRIX       | Adjacency matrix in which two atoms are adjacent if they are within a certain cutoff.  |
| HBOND_MATRIX         | Adjacency matrix in which two atoms are adjacent if there is a hydrogen bond between them.   |
| SMAC_MATRIX          | Adjacency matrix in which two molecules are adjacent if they are within a certain cutoff and if the angle between them is within certain ranges. |
| TOPOLOGY_MAT↔<br>RIX | Adjacency matrix in which two atoms are adjacent if they are connected topologically   |

Once you have calculated an adjacency matrix you can then perform any one of the following operations on this object in order to reduce it to a scalar number or a set of connected components.

| CLUSTER_WITHSURFACE | Find the various connected components in an adjacency matrix and then output averageproperties of the atoms in those connected components. |
|---------------------|--|
| COLUMNSUMS          | Sum the columns of a contact matrix  |
| DFSCLUSTERING       | Find the connected components of the matrix using the DFS clustering algorithm.  |
| ROWSUMS             | Sum the rows of a contact matrix   |
| SPRINT              | Calculate SPRINT topological variables from an adjacency matrix.   |

If the function you have chosen reduces your contact matrix to a set of connected components you then need a method to convert these connected components into a scalar number or to output this information to a file. The various things that you can do with a set of connected components are listed below:

| CLUSTER_DIAMETER     | Print out the diameter of one of the connected components                           |
|----------------------|---|
| CLUSTER_DISTRIBUTION | Calculate functions of the distribution of properties in your connected compo-      |
|                      | nents.  |
| CLUSTER_NATOMS       | Gives the number of atoms in the connected component                                |
| CLUSTER_PROPERTIES   | Calculate properties of the distribution of some quantities that are part of a con- |
|                      | nected component  |
| DUMPGRAPH            | Write out the connnectivity of the nodes in the graph in dot format.                |
| OUTPUT_CLUSTER       | Output the indices of the atoms in one of the clusters identified by a clustering   |
|                      | object  |

### 5.6.1 ALIGNED MATRIX

This is part of the adjmat module

It is only available if you configure PLUMED with ./configure –enable-modules=adjmat . Furthermore, this feature is still being developed so take care when using it and report any problems on the mailing list.

Adjacency matrix in which two molecule are adjacent if they are within a certain cutoff and if they have the same orientation.

The atoms involved can be specified using

### **ATOMS**

The list of molecules for which you would like to calculate the contact matrix. The molecules involved must have an orientation so your list will be a list of the labels of MultiColvar or MultiColvar functions as PLUMED calculates the orientations of molecules within these operations. Please note also that the majority of MultiColvar and MultiColvar functions do not calculate a molecular orientation.. For more information on how to specify lists of atoms see Groups and Virtual Atoms

Or alternatively by using

| ATOMSA | MSA The list of molecules that you would like to use for the rows of the contact matrix. The molecule     |  |  |
|--------|---|--|--|
|        | involved must have an orientation so your list will be a list of the labels of MultiColvar or MultiColvar |  |  |
|        | functions as PLUMED calculates the orientations of molecules within these operations. Please              |  |  |
|        | note also that the majority of MultiColvar and MultiColvar functions do not calculate a molecular         |  |  |
|        | orientation.  |  |  |
| ATOMSB | The list of molecules that you would like to use for the columns of the contact matrix. The molecules     |  |  |
|        | involved must have an orientation so your list will be a list of the labels of MultiColvar or MultiColvar |  |  |
|        | functions as PLUMED calculates the orientations of molecules within these operations. Please              |  |  |
|        | note also that the majority of MultiColvar and MultiColvar functions do not calculate a molecular         |  |  |
|        | orientation.  |  |  |

**Options** 

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |  |  |
|-----------------------|--|--|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-  |  |  |
|                       | tances   |  |  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize   |  |  |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the cal-<br>culation   |  |  |
| HIGHMEM               | ( default=off ) use a more memory intensive version of this collective variable  |  |  |
| SWITCH                | This keyword is used if you want to employ an alternative to the continuous swiching function defined above. The following provides information on the switchingfunction that are available. When this keyword is present you no longer need the NN, MM, D_0 and R_0 keywords. You can use multiple instances of this keyword i.e. SWITCH1, SWITCH2, SWITCH3 |  |  |
| ORIENTATION_SWITCH    | A switching function that transforms the dot product of the input vectors. You can use multiple instances of this keyword i.e. ORIENTATION_SWITCH1, OHRIENTATION_SWITCH2, ORIENTATION_SWITCH3  |  |  |

**Examples** 

# 5.6.2 CONTACT\_MATRIX

| This is | part of | of the | adjmat | module |
|---------|---------|--------|--------|--------|
|---------|---------|--------|--------|--------|

It is only available if you configure PLUMED with ./configure –enable-modules=adjmat . Furthermore, this feature is still being developed so take care when using it and report any problems on the mailing list.

Adjacency matrix in which two atoms are adjacent if they are within a certain cutoff.

The atoms involved can be specified using

### **ATOMS**

The list of atoms for which you would like to calculate the contact matrix. The atoms involved must be specified as a list of labels of MultiColvar or labels of a MultiColvar functions actions. If you would just like to use the atomic positions you can use a DENSITY command to specify a group of atoms. Specifying your atomic positions using labels of other MultiColvar or MultiColvar functions commands is useful, however, as you can then exploit a much wider variety of functions of the contact matrix as described in Exploiting contact matrices. For more information on how to specify lists of atoms see Groups and Virtual Atoms

#### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-  |
|                       | tances   |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the cal-   |
|                       | culation   |
| HIGHMEM               | ( default=off ) use a more memory intensive version of this collective variable  |
| SWITCH                | This keyword is used if you want to employ an alternative to the continuous swiching function defined above. The following provides information on the switchingfunction that are available. When this keyword is present you no longer need the NN, MM, D_0 and R_0 keywords. You can use multiple instances of this keyword i.e. SWITCH1, SWITCH2, SWITCH3 |

**Examples** 

#### 5.6.3 HBOND\_MATRIX

| This is part of the adjmat module   |
|---|
| It is only available if you configure PLUMED with ./configure –enable-modules=adjmat . Furthermore, this feature is still being developed so take care when using it and report any problems on the mailing list. |

Adjacency matrix in which two atoms are adjacent if there is a hydrogen bond between them.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This

is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. <code>label.lessthan-1</code>, <code>label.lessthan-2</code> etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword | Description       |
|----------|---------|-------------------|
| sum      | SUM     | the sum of values |

The atoms involved can be specified using

| ATOMS     | The list of atoms which can be part of a hydrogen bond. When this command is used the set of atoms that can donate a hydrogen bond is assumed to be the same as the set of atoms that can form hydrogen bonds. The atoms involved must be specified as a list of labels of MultiColvar or labels of a MultiColvar functions actions. If you would just like to use the atomic positions you can use a DENSITY command to specify a group of atoms. Specifying your atomic positions using labels of other MultiColvar or MultiColvar functions commands is useful, however, as you can then exploit a much wider variety of functions of the contact matrix as described in Exploiting contact matrices. For more information on how to specify lists of atoms see Groups and Virtual Atoms |
|-----------|---|
| HYDROGENS | The list of hydrogen atoms that can form part of a hydrogen bond. The atoms must be specified using a comma separated list, an index range or by using a GROUP. A list of hydrogen atoms is always required even if you specify the other atoms using DONORS and ACCEPTORS as described below. For more information on how to specify lists of atoms see Groups and Virtual Atoms   |

Or alternatively by using

| DONORS    | The list of atoms which can donate a hydrogen bond. The atoms involved must be specified as a list of labels of MultiColvar or labels of a MultiColvar functions actions. If you would just like to use the atomic positions you can use a DENSITY command to specify a group of atoms. Specifying your atomic positions using labels of other MultiColvar or MultiColvar functions commands is useful, however, as you can then exploit a much wider variety of functions of the contact matrix as described in Exploiting contact matrices |
|-----------|--|
| ACCEPTORS | The list of atoms which can accept a hydrogen bond. The atoms involved must be specified as a list of labels of MultiColvar or labels of a MultiColvar functions actions. If you would just like to use the atomic positions you can use a DENSITY command to specify a group of atoms. Specifying your atomic positions using labels of other MultiColvar or MultiColvar functions commands is useful, however, as you can then exploit a much wider variety of functions of the contact matrix as described in Exploiting contact matrices |

**Options** 

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances   |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation  |
| HIGHMEM               | ( default=off ) use a more memory intensive version of this collective variable  |
| SWITCH                | The switchingfunction that specifies how close a pair of atoms must be together for there to be a hydrogen bond between them You can use multiple instances of this keyword i.e. SWITCH1, SWITCH2, SWITCH3   |
| HSWITCH               | The switchingfunction that specifies how close the hydrogen must be to the donor atom of the hydrogen bond for it to be considered a hydrogen bond You can use multiple instances of this keyword i.e. HSWITCH1, HSWITCH2, HS↔ WITCH3  |
| ASWITCH               | A switchingfunction that is used to specify what the angle between the vector connecting the donor atom to the acceptor atom and the vector connecting the donor atom to the hydrogen must be in order for it considered to be a hydrogen bond You can use multiple instances of this keyword i.e. ASWITCH1, ASWICH2, ASWITCH3 |
| SUM                   | calculate the sum of all the quantities. The final value can be referenced using <i>label.</i> sum. You can use multiple instances of this keyword i.e. SUM1, SU← M2, SUM3 The corresponding values are then referenced using <i>label.</i> sum-1, <i>label.</i> sum-2, <i>label.</i> sum-3                                    |

**Examples** 

# 5.6.4 SMAC\_MATRIX

| This is part of the adjmat |
|----------------------------|
|----------------------------|

It is only available if you configure PLUMED with ./configure –enable-modules=adjmat . Furthermore, this feature is still being developed so take care when using it and report any problems on the mailing list.

Adjacency matrix in which two molecules are adjacent if they are within a certain cutoff and if the angle between them is within certain ranges.

In this case the elements of the adjacency matrix are calculated using:

$$A_{ij} = \sigma(r_{ij}) \sum_{n} K_n(\theta_{ij})$$

In this expression  $r_{ij}$  is the distance between molecule i and molecule j and  $\sigma(r_{ij})$  is a switchingfunction that acts on this distance. The \$K\_n functions are kernelfunctions that take the torsion angle,  $\theta_{ij}$ , between the internal orientation vectors for molecules i and j as input. These kernel functions should be set so that they are equal to one when the relative orientation of the molecules are as they are in the solid and equal to zero otherwise. As the above matrix element is a product of functions it is only equal to one when the centers of mass of molecules i and j are with a certain distance of each other and when the molecules are aligned in some desirable way.

The atoms involved can be specified using

|  | Α | Т | 0 | N | 19 |
|--|---|---|---|---|----|
|--|---|---|---|---|----|

The list of molecules for which you would like to calculate the contact matrix. The molecules involved must have an orientation so your list will be a list of the labels of MultiColvar or MultiColvar functions as PLUMED calculates the orientations of molecules within these operations. Please note also that the majority of MultiColvar and MultiColvar functions do not calculate a molecular orientation.. For more information on how to specify lists of atoms see Groups and Virtual Atoms

Or alternatively by using

| ATOMSA | The list of molecules that you would like to use for the rows of the contact matrix. The molecules involved must have an orientation so your list will be a list of the labels of MultiColvar or MultiColvar functions as PLUMED calculates the orientations of molecules within these operations. Please note also that the majority of MultiColvar and MultiColvar functions do not calculate a molecular orientation.    |
|--------|---|
| ATOMSB | The list of molecules that you would like to use for the columns of the contact matrix. The molecules involved must have an orientation so your list will be a list of the labels of MultiColvar or MultiColvar functions as PLUMED calculates the orientations of molecules within these operations. Please note also that the majority of MultiColvar and MultiColvar functions do not calculate a molecular orientation. |

### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-  |
|                       | tances   |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation  |
| HIGHMEM               | ( default=off ) use a more memory intensive version of this collective variable  |
| SWITCH                | This keyword is used if you want to employ an alternative to the continuous swiching function defined above. The following provides information on the switchingfunction that are available. When this keyword is present you no longer need the NN, MM, D_0 and R_0 keywords. You can use multiple instances of this keyword i.e. SWITCH1, SWITCH2, SWITCH3 |
| KERNEL                | The various kernels that are used to determine whether or not the molecules are aligned You can use multiple instances of this keyword i.e. KERNEL1, K← ERNEL2, KERNEL3  |

### **Examples**

In the following example an adjacency matrix is constructed in which the (i,j) element is equal to one if molecules i and j are within 6 angstroms of each other and if the torsional angle between the orientations of these molecules is close to 0 or  $\pi$ . The various connected components of this matrix are determined using the DFSCLUSTERING algorithm and then the size of the largest cluster of connectes molecules is output to a colvar file

UNITS LENGTH=A

```
MOLECULES ...
MOL1=1, 2, 1
MOL2=5, 6, 5
MOL3=9,10,9
MOL4=13,14,13
MOL5=17,18,17
LABEL=m1
... MOLECULES
SMAC_MATRIX ...
  ATOMS=m1 SWITCH={RATIONAL D_0=5.99 R_0=0.1 D_MAX=6.0}
  KERNEL1={TRIANGULAR CENTER=0 SIGMA=1.0} KERNEL2={TRIANGULAR CENTER=pi SIGMA=0.6}
  LABEL=smacm
... SMAC_MATRIX
dfs1: DFSCLUSTERING MATRIX=smacm
cc2: CLUSTER_NATOMS CLUSTERS=dfs1 CLUSTER=1
PRINT ARG=smac.*,cc1.*,cc2 FILE=colvar
```

# 5.6.5 TOPOLOGY\_MATRIX

#### This is part of the adjmat module

It is only available if you configure PLUMED with ./configure –enable-modules=adjmat . Furthermore, this feature is still being developed so take care when using it and report any problems on the mailing list.

Adjacency matrix in which two atoms are adjacent if they are connected topologically

The atoms involved can be specified using

| NODES | The list of atoms for which you would like to calculate the contact matrix. The atoms involved must be specified as a list of labels of MultiColvar or labels of a MultiColvar functions actions. If you would just like to use the atomic positions you can use a DENSITY command to specify a group of atoms. Specifying your atomic positions using labels of other MultiColvar or MultiColvar functions commands is useful, however, as you can then exploit a much wider variety of functions of the contact matrix as described in Exploiting contact matrices. For more information on how to specify lists of atoms see Groups and Virtual Atoms |
|-------|--|
| ATOMS | . For more information on how to specify lists of atoms see Groups and Virtual Atoms   |

Compulsory keywords

| DENSITY_THRESHOLD |  |
|-------------------|--|
| SIGMA             | the width of the function to be used for kernel density estimation |
| KERNEL            | ( default=gaussian ) the type of kernel function to be used        |

|--|

| NOPBC   | ( default=off ) ignore the periodic boundary conditions when calculating distances   |  |  |  |
|---|--|--|--|--|
| SERIAL  | ( default=off ) do the calculation in serial. Do not parallelize   |  |  |  |
| TIMINGS   | ( default=off ) output information on the timings of the various parts of the calculation  |  |  |  |
| HIGHMEM ( default=off ) use a more memory intensive version of this collective va |  |  |  |  |
| SWITCH  | This keyword is used if you want to employ an alternative to the continuous swiching function defined above. The following provides information on the switchingfunction that are available. When this keyword is present you no longer need the NN, MM, D_0 and R_0 keywords. You can use multiple instances of this keyword i.e. SWITCH1, SWITCH2, SWITCH3 |  |  |  |
| RADIUS  | You can use multiple instances of this keyword i.e. RADIUS1, RADIUS2, RA⇔ DIUS3  |  |  |  |
| CYLINDER_SWITCH   | a switching function on ( <code>r_ij</code> . <code>r_ik</code> - 1 )/ <code>r_ij</code> You can use multiple instances of this keyword i.e. CYLINDER_SWITCH1, CYLINDER_SWITCH2, CYLINDE $\leftarrow$ R_SWITCH3  |  |  |  |
| BIN_SIZE  | the size to use for the bins You can use multiple instances of this keyword i.e. BIN_SIZE1, BIN_SIZE2, BIN_SIZE3   |  |  |  |

**Examples** 

# 5.6.6 CLUSTER\_WITHSURFACE

| This is | part of | the ad | jmat mod | ule |
|---------|---------|--------|----------|-----|
|---------|---------|--------|----------|-----|

It is only available if you configure PLUMED with ./configure –enable-modules=adjmat . Furthermore, this feature is still being developed so take care when using it and report any problems on the mailing list.

Find the various connected components in an adjacency matrix and then output average properties of the atoms in those connected components.

Compulsory keywords

| CLUS | STERS  | the label of the action that does the clustering   |
|------|--------|--|
| RCU' | T_SURF | you also have the option to find the atoms on the surface of the cluster. An atom must be within |
|      |        | this distance of one of the atoms of the cluster in order to be considered a surface atom        |

| NOPBC   | ( default=off ) ignore the periodic boundary conditions when calculating distances        |  |  |  |  |
|---------|---|--|--|--|--|
| SERIAL  | ( default=off ) do the calculation in serial. Do not parallelize                          |  |  |  |  |
| LOWMEM  | ( default=off ) lower the memory requirements   |  |  |  |  |
| TIMINGS | ( default=off ) output information on the timings of the various parts of the calculation |  |  |  |  |
|         |   |  |  |  |  |

**Examples** 

#### 5.6.7 COLUMNSUMS

This is part of the adjmat module

It is only available if you configure PLUMED with ./configure –enable-modules=adjmat . Furthermore, this feature is still being developed so take care when using it and report any problems on the mailing list.

Sum the columns of a contact matrix

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |  |  |  |
|----------|-----------|---|--|--|--|
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |  |  |  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |  |  |  |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |  |  |  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |  |  |  |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |  |  |  |
| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |  |  |  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |  |  |  |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |  |  |  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |  |  |  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |  |  |  |

# Compulsory keywords

| MAT← | the action that calcualtes the adjacency matrix vessel we would like to analyse |
|------|---|
| RIX  |   |

| NOPBC     | ( default=off ) ignore the periodic boundary conditions when calculating distances  |  |  |  |  |
|-----------|---|--|--|--|--|
| SERIAL    | ( default=off ) do the calculation in serial. Do not parallelize  |  |  |  |  |
| LOWMEM    | ( default=off ) lower the memory requirements   |  |  |  |  |
| TIMINGS   |   |  |  |  |  |
| TIMINGS   | ( default=off ) output information on the timings of the various parts of the calculation   |  |  |  |  |
| ALT_MIN   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta} \log \sum_i \exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BE $\leftarrow$ TA= $\beta$ ). The final value can be referenced using <i>label</i> .altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using <i>label</i> .altmin-1, <i>label</i> .altmin-2, <i>label</i> .altmin-3 |  |  |  |  |
| LOWEST    | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest   |  |  |  |  |
| HIGHEST   | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest   |  |  |  |  |
| MEAN      | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEAN2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3   |  |  |  |  |
| MEAN      | take the mean of these variables. The final value can be referenced using <i>label.</i> mean. You can use multiple instances of this keyword i.e. MEAN1, MEAN2, MEAN3 The corresponding values are then referenced using <i>label.</i> mean-1, <i>label.</i> mean-2, <i>label.</i> mean-3   |  |  |  |  |
| MIN       | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3                                    |  |  |  |  |
| MAX       | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3   |  |  |  |  |
| LESS_THAN | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using label.lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_T $\leftarrow$ HAN2, LESS_THAN3 The corresponding values are then referenced using label.lessthan-1, label.lessthan-2, label.lessthan-3   |  |  |  |  |
| MORE_THAN | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using label.morethan. You can use multiple instances of this keyword i.e. MORE_THA $\leftrightarrow$ N1, MORE_THAN2, MORE_THAN3 The corresponding values are then referenced using label.morethan-1, label.morethan-2, label.morethan-3  |  |  |  |  |
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using label.between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWEEN3 The corresponding values are then referenced using label.between-1, label.between-2, label.between-3   |  |  |  |  |

| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGR← AM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3 |
|-----------|---|
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .                      |

**Examples** 

# 5.6.8 DFSCLUSTERING

| This is pa | rt of the | adimat | module |
|------------|-----------|--------|--------|
|------------|-----------|--------|--------|

It is only available if you configure PLUMED with ./configure –enable-modules=adjmat . Furthermore, this feature is still being developed so take care when using it and report any problems on the mailing list.

Find the connected components of the matrix using the DFS clustering algorithm.

Compulsory keywords

| MATRIX     | the action that calcualtes the adjacency matrix vessel we would like to analyse  |  |
|------------|--|--|
| MAXCONNECT | ( default=0 ) maximum number of connections that can be formed by any given node in the graph. By default this is set equal to zero and the number of connections is set equal to the number of nodes. You only really need to set this if you are working with a very large system and memory is at a premium |  |

**Options** 

| NOPBC   | ( default=off ) ignore the periodic boundary conditions when calculating distances        |  |
|---------|---|--|
| SERIAL  | ( default=off ) do the calculation in serial. Do not parallelize                          |  |
| LOWMEM  | ( default=off ) lower the memory requirements   |  |
| TIMINGS | ( default=off ) output information on the timings of the various parts of the calculation |  |

**Examples** 

# 5.6.9 ROWSUMS

This is part of the adjmat module

It is only available if you configure PLUMED with ./configure –enable-modules=adjmat . Furthermore, this feature is still being developed so take care when using it and report any problems on the mailing list.

Sum the rows of a contact matrix

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

Compulsory keywords

| MAT← | the action that calcualtes the adjacency matrix vessel we would like to analyse |
|------|---|
| RIX  |   |

| Nonno     |  |  |
|-----------|--|--|
| NOPBC     | ( default=off ) ignore the periodic boundary conditions when calculating distances   |  |
| SERIAL    | ( default=off ) do the calculation in serial. Do not parallelize   |  |
| LOWMEM    | ( default=off ) lower the memory requirements  |  |
| TIMINGS   | ( default=off ) output information on the timings of the various parts of the calculation  |  |
| ALT_MIN   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BE $\leftarrow$ TA= $\beta$ ). The final value can be referenced using <i>label</i> .altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using <i>label</i> .altmin-1, <i>label</i> .altmin-2, <i>label</i> .altmin-3 |  |
| LOWEST    | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |  |
| HIGHEST   | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |  |
| MEAN      | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEAN2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3  |  |
| MEAN      | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEAN2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3  |  |
| MIN       | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3                                 |  |
| MAX       | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3  |  |
| LESS_THAN | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using label.lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_T $\leftarrow$ HAN2, LESS_THAN3 The corresponding values are then referenced using label.lessthan-1, label.lessthan-2, label.lessthan-3  |  |
| MORE_THAN | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using label.morethan. You can use multiple instances of this keyword i.e. MORE_THA $\leftrightarrow$ N1, MORE_THAN2, MORE_THAN3 The corresponding values are then referenced using label.morethan-1, label.morethan-2, label.morethan-3   |  |
| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using label.between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWEEN3 The corresponding values are then referenced using label.between-1, label.between-2, label.between-3  |  |

| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGR← AM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3 |
|-----------|---|
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .                      |

**Examples** 

#### 5.6.10 **SPRINT**

|   | This is part of the adjmat module   |
|---|---|
| _ | It is only available if you configure PLUMED with ./configure -enable-modules=adjmat . Furthermore,     |
|   | this feature is still being developed so take care when using it and report any problems on the mailing |

Calculate SPRINT topological variables from an adjacency matrix.

The SPRINT topological variables are calculated from the largest eigenvalue,  $\lambda$  of an  $n \times n$  adjacency matrix and its corresponding eigenvector,  $\mathbf{V}$ , using:

$$s_i = \sqrt{n}\lambda v_i$$

You can use different quantities to measure whether or not two given atoms/molecules are adjacent or not in the adjacency matrix. The simplest measure of adjacency is is whether two atoms/molecules are within some cutoff of each other. Further complexity can be added by insisting that two molecules are adjacent if they are within a certain distance of each other and if they have similar orientations.

**Description of components** 

By default this Action calculates the following quantities. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Description   |
|----------|---|
| coord    | all $n$ sprint coordinates are calculated and then stored in increasing order. the smallest sprint coordinate will be labelled <i>label</i> .coord-1, the second smallest will be labelled <i>label</i> .coord-1 and so |
|          | on  |

In addition the following quantities can be calculated by employing the keywords listed below

| Quantity | Keyword  | Description  |
|----------|----------|--------------|
| gradient | GRADIENT | the gradient |

| vmean    | VMEAN     | the norm of the mean vector. The output component can be refererred to else-  |
|----------|-----------|---|
|          |           | where in the input file by using the label.vmean  |
| vsum     | VSUM      | the norm of sum of vectors. The output component can be refererred to elsewhere   |
|          |           | in the input file by using the label.vsum   |
| spath    | SPATH     | the position on the path  |
| gspath   | GPATH     | the position on the path calculated using trigonometry  |
| gzpath   | GPATH     | the distance from the path calculated using trigonometry  |
| zpath    | ZPATH     | the distance from the path  |
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| sum      | SUM       | the sum of values   |
|          |           |   |

# Compulsory keywords

| MAT← | the action that calcualtes the adjacency matrix vessel we would like to analyse |   |
|------|---|---|
| RIX  |   | ١ |

# Options

| NOPBC   | ( default=off ) ignore the periodic boundary conditions when calculating distances        |
|---------|---|
| SERIAL  | ( default=off ) do the calculation in serial. Do not parallelize                          |
| LOWMEM  | ( default=off ) lower the memory requirements   |
| TIMINGS | ( default=off ) output information on the timings of the various parts of the calculation |
|         |   |

# Examples

This example input calculates the 7 SPRINT coordinates for a 7 atom cluster of Lennard-Jones atoms and prints their values to a file. In this input the SPRINT coordinates are calculated in the manner described in ?? so two atoms are adjacent if they are within a cutoff:

```
DENSITY SPECIES=1-7 LABEL=d1
CONTACT_MATRIX ATOMS=d1 SWITCH={RATIONAL R_0=0.1} LABEL=mat
SPRINT MATRIX=mat LABEL=ss
PRINT ARG=ss.* FILE=colvar
```

This example input calculates the 14 SPRINT coordinates foa a molecule composed of 7 hydrogen and 7 carbon atoms. Once again two atoms are adjacent if they are within a cutoff:

```
DENSITY SPECIES=1-7 LABEL=c
DENSITY SPECIES=8-14 LABEL=h

CONTACT_MATRIX ...
ATOMS=c,h
SWITCH11={RATIONAL R_0=2.6 NN=6 MM=12}
SWITCH12={RATIONAL R_0=2.2 NN=6 MM=12}
SWITCH2={RATIONAL R_0=2.2 NN=6 MM=12}
LABEL=mat
... CONTACT_MATRIX

SPRINT MATRIX=mat LABEL=ss

PRINT ARG=ss.* FILE=colvar
```

#### 5.6.11 CLUSTER\_DIAMETER

#### This is part of the adjmat module

It is only available if you configure PLUMED with ./configure –enable-modules=adjmat . Furthermore, this feature is still being developed so take care when using it and report any problems on the mailing list.

Print out the diameter of one of the connected components

Compulsory keywords

| CLUSTERS | the label of the action that does the clustering   |
|----------|--|
| CLUSTER  | ( default=1 ) which cluster would you like to look at 1 is the largest cluster, 2 is the second largest, |
|          | 3 is the the third largest and so on.  |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically    |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis- |
|                       | tances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize              |
| LOWMEM                | ( default=off ) lower the memory requirements                                 |

| TIMINGS | ( default=off ) output information on the timings of the various parts of the cal- |  |
|---------|--|--|
|         | culation   |  |

**Examples** 

#### 5.6.12 CLUSTER DISTRIBUTION

| This is part of the adjmat module   |
|---|
| It is only available if you configure PLUMED with ./configure –enable-modules=adjmat . Furthermore, this feature is still being developed so take care when using it and report any problems on the mailing |
| list.   |

Calculate functions of the distribution of properties in your connected components.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |

# Compulsory keywords

| CLUSTERS             | the label of the action that does the clustering  |
|----------------------|---|
| TRANSFORM            | ( default=none ) the switching function to use to convert the crystallinity parameter to a number |
| between zero and one |   |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically   |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances   |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize   |
| LOWMEM                | ( default=off ) lower the memory requirements  |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation  |
| INVERSE_TRANSFORM     | ( default=off ) when TRANSFORM appears alone the input symmetry functions, $x$ are transformed used $1-s(x)$ where $s(x)$ is a switching function. When this option is used you instead transform using $s(x)$ only.   |
| MORE_THAN             | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <code>label.morethan</code> . You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THA $\sim$ N3 The corresponding values are then referenced using <code>label.morethan-1</code> , <code>label.morethan-2</code> , <code>label.morethan-3</code> |
| LESS_THAN             | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_THAN2, LESS_THAN3 The corresponding values are then referenced using <i>label</i> .lessthan-1, <i>label</i> .lessthan-2, <i>label</i> .lessthan-3                                      |
| BETWEEN               | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using <i>label</i> .between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE∈ EN3 The corresponding values are then referenced using <i>label</i> .between-1, <i>label</i> .between-2, <i>label</i> .between-3  |
| HISTOGRAM             | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |
| ALT_MIN               | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta}\log\sum_i\exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3                   |

| MIN | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label.</i> min-1, <i>label.</i> min-2, <i>label.</i> min-3 |
|-----|--|
| MAX | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3        |

Examples

# 5.6.13 CLUSTER\_NATOMS

| This is part of the adjmat module   |
|---|
| It is only available if you configure PLUMED with ./configure -enable-modules=adjmat . Furthermore,     |
| this feature is still being developed so take care when using it and report any problems on the mailing |
| liet  |

Gives the number of atoms in the connected component

Compulsory keywords

| CLUSTERS | the label of the action that does the clustering   |
|----------|--|
| CLUSTER  | ( default=1 ) which cluster would you like to look at 1 is the largest cluster, 2 is the second largest, 3 is the the third largest and so on. |

**Options** 

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically                |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-             |
|                       | tances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize                          |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation |

Examples

# 5.6.14 CLUSTER\_PROPERTIES

This is part of the adjmat module

It is only available if you configure PLUMED with ./configure –enable-modules=adjmat . Furthermore, this feature is still being developed so take care when using it and report any problems on the mailing list.

Calculate properties of the distribution of some quantities that are part of a connected component

This collective variable was developed for looking at nucleation phenomena, where you are interested in using studying the behavior of atoms in small aggregates or nuclei. In these sorts of problems you might be interested in the degree the atoms in a nucleus have adopted their crystalline structure or (in the case of heterogenous nucleation of a solute from a solvent) you might be interested in how many atoms are present in the largest cluster.

**Description of components** 

When the label of this action is used as the input for a second you are not referring to a scalar quantity as you are in regular collective variables. The label is used to reference the full set of quantities calculated by the action. This is usual when using MultiColvar functions. Generally when doing this the previously calculated multicolvar will be referenced using the DATA keyword rather than ARG.

This Action can be used to calculate the following scalar quantities directly. These quantities are calculated by employing the keywords listed below. These quantities can then be referenced elsewhere in the input file by using this Action's label followed by a dot and the name of the quantity. Some amongst them can be calculated multiple times with different parameters. In this case the quantities calculated can be referenced elsewhere in the input by using the name of the quantity followed by a numerical identifier e.g. *label*.lessthan-1, *label*.lessthan-2 etc. When doing this and, for clarity we have made the label of the components customizable. As such by using the LABEL keyword in the description of the keyword input you can customize the component name

| Quantity | Keyword   | Description   |
|----------|-----------|---|
| vmean    | VMEAN     | the norm of the mean vector. The output component can be refererred to elsewhere in the input file by using the label.vmean   |
| vsum     | VSUM      | the norm of sum of vectors. The output component can be refererred to elsewhere in the input file by using the label.vsum   |
| altmin   | ALT_MIN   | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| between  | BETWEEN   | the number/fraction of values within a certain range. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| highest  | HIGHEST   | the lowest of the quantitities calculated by this action  |
| lessthan | LESS_THAN | the number of values less than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters.        |
| lowest   | LOWEST    | the lowest of the quantitities calculated by this action  |
| max      | MAX       | the maximum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |
| mean     | MEAN      | the mean value. The output component can be refererred to elsewhere in the input file by using the label.mean   |
| min      | MIN       | the minimum value. This is calculated using the formula described in the description of the keyword so as to make it continuous.  |

| moment   | MOMENTS   | the central moments of the distribution of values. The second moment would be referenced elsewhere in the input file using <i>label</i> .moment-2, the third as <i>label</i> .moment-3, etc.   |
|----------|-----------|--|
| morethan | MORE_THAN | the number of values more than a target value. This is calculated using one of the formula described in the description of the keyword so as to make it continuous. You can calculate this quantity multiple times using different parameters. |
| sum      | SUM       | the sum of values  |

# Compulsory keywords

| CLUSTERS | the label of the action that does the clustering   |
|----------|--|
| CLUSTER  | ( default=1 ) which cluster would you like to look at 1 is the largest cluster, 2 is the second largest, |
|          | 3 is the the third largest and so on.  |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating dis-   |
|                       | tances  |
| SERIAL                | ( default=off ) do the calculation in serial. Do not parallelize  |
| LOWMEM                | ( default=off ) lower the memory requirements   |
| TIMINGS               | ( default=off ) output information on the timings of the various parts of the calculation   |
| MEAN                  | take the mean of these variables. The final value can be referenced using <i>label</i> .mean. You can use multiple instances of this keyword i.e. MEAN1, MEA $\leftarrow$ N2, MEAN3 The corresponding values are then referenced using <i>label</i> .mean-1, <i>label</i> .mean-2, <i>label</i> .mean-3   |
| MORE_THAN             | calculate the number of variables more than a certain target value. This quantity is calculated using $\sum_i 1.0 - \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .morethan. You can use multiple instances of this keyword i.e. MORE_THAN1, MORE_THAN2, MORE_THA $\leftarrow$ N3 The corresponding values are then referenced using <i>label</i> .morethan-1, <i>label</i> .morethan-2, <i>label</i> .morethan-3 |
| LESS_THAN             | calculate the number of variables less than a certain target value. This quantity is calculated using $\sum_i \sigma(s_i)$ , where $\sigma(s)$ is a switchingfunction. The final value can be referenced using <i>label</i> .lessthan. You can use multiple instances of this keyword i.e. LESS_THAN1, LESS_THAN2, LESS_THAN3 The corresponding values are then referenced using <i>label</i> .lessthan-1, <i>label</i> .lessthan-2, <i>label</i> .lessthan-3                     |
| VMEAN                 | calculate the norm of the mean vector. The final value can be referenced using label.vmean. You can use multiple instances of this keyword i.e. VMEAN1, VMEAN2, VMEAN3 The corresponding values are then referenced using label.vmean-1, label.vmean-2, label.vmean-3   |
| VSUM                  | calculate the norm of the sum of vectors. The final value can be referenced using <i>label.</i> vsum. You can use multiple instances of this keyword i.e. VSU← M1, VSUM2, VSUM3 The corresponding values are then referenced using <i>label.</i> vsum-1, <i>label.</i> vsum-2, <i>label.</i> vsum-3   |

| BETWEEN   | calculate the number of values that are within a certain range. These quantities are calculated using kernel density estimation as described on histogrambead. The final value can be referenced using label.between. You can use multiple instances of this keyword i.e. BETWEEN1, BETWEEN2, BETWE← EN3 The corresponding values are then referenced using label.between-1, label.between-2, label.between-3  |
|-----------|--|
| HISTOGRAM | calculate a discretized histogram of the distribution of values. This shortcut allows you to calculates NBIN quantites like BETWEEN. The final value can be referenced using <i>label</i> .histogram. You can use multiple instances of this keyword i.e. HISTOGRAM1, HISTOGRAM2, HISTOGRAM3 The corresponding values are then referenced using <i>label</i> .histogram-1, <i>label</i> .histogram-2, <i>label</i> .histogram-3  |
| MOMENTS   | calculate the moments of the distribution of collective variables. The $m$ th moment of a distribution is calculated using $\frac{1}{N}\sum_{i=1}^{N}(s_i-\overline{s})^m$ , where $\overline{s}$ is the average for the distribution. The moments keyword takes a lists of integers as input or a range. Each integer is a value of $m$ . The final calculated values can be referenced using moment- $m$ .   |
| ALT_MIN   | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = -\frac{1}{\beta} \log \sum_i \exp\left(-\beta s_i\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ). The final value can be referenced using label.altmin. You can use multiple instances of this keyword i.e. ALT_MIN1, ALT_MIN2, ALT_MIN3 The corresponding values are then referenced using label.altmin-1, label.altmin-2, label.altmin-3            |
| MIN       | calculate the minimum value. To make this quantity continuous the minimum is calculated using $\min = \frac{\beta}{\log \sum_i \exp\left(\frac{\beta}{s_i}\right)}$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label</i> .min. You can use multiple instances of this keyword i.e. MIN1, MIN2, MIN3 The corresponding values are then referenced using <i>label</i> .min-1, <i>label</i> .min-2, <i>label</i> .min-3 |
| MAX       | calculate the maximum value. To make this quantity continuous the maximum is calculated using $\max = \beta \log \sum_i \exp \left(\frac{s_i}{\beta}\right)$ The value of $\beta$ in this function is specified using (BETA= $\beta$ ) The final value can be referenced using <i>label.</i> max. You can use multiple instances of this keyword i.e. MAX1, MAX2, MAX3 The corresponding values are then referenced using <i>label.</i> max-1, <i>label.</i> max-2, <i>label.</i> max-3        |
| SUM       | calculate the sum of all the quantities. The final value can be referenced using label.sum. You can use multiple instances of this keyword i.e. SUM1, SU← M2, SUM3 The corresponding values are then referenced using label.sum-1, label.sum-2, label.sum-3  |
| LOWEST    | this flag allows you to recover the lowest of these variables. The final value can be referenced using <i>label</i> .lowest  |
| HIGHEST   | this flag allows you to recover the highest of these variables. The final value can be referenced using <i>label</i> .highest  |

Examples

# 5.6.15 DUMPGRAPH

| This is part of the adjmat module   |
|---|
| It is only available if you configure PLUMED with ./configure –enable-modules=adjmat . Furthermore,           |
| this feature is still being developed so take care when using it and report any problems on the mailing list. |

Write out the connnectivity of the nodes in the graph in dot format.

#### Compulsory keywords

| MATRIX     | the action that calcualtes the adjacency matrix vessel we would like to analyse  |
|------------|--|
| STRIDE     | ( default=1 ) the frequency with which you would like to output the graph  |
| FILE       | the name of the file on which to output the data   |
| MAXCONNECT | ( default=0 ) maximum number of connections that can be formed by any given node in the graph. By default this is set equal to zero and the number of connections is set equal to the number of nodes. You only really need to set this if you are working with a very large system and memory is at a premium |

**Examples** 

# 5.6.16 OUTPUT CLUSTER

| This is part of the adjmat module   |
|---|
| It is only available if you configure PLUMED with ./configure -enable-modules=adjmat . Furthermore      |
| this feature is still being developed so take care when using it and report any problems on the mailing |
| list.   |

Output the indices of the atoms in one of the clusters identified by a clustering object

This action provides one way of getting output from a DFSCLUSTERING calculation. The output in question here is either

- a file that contains a list of the atom indices that form part of one of the clusters that was identified using DFSCLUSTERING
- an xyz file containing the positions of the atoms in one of the the clusters that was identified using DFSCL
   USTERING

Notice also that if you choose to output an xyz file you can ask PLUMED to try to reconstruct the cluster taking the periodic boundary conditions into account by using the MAKE\_WHOLE flag.

#### Compulsory keywords

| CLUSTERS | the action that performed the clustering  |
|----------|---|
| CLUSTER  | ( default=1 ) which cluster would you like to look at 1 is the largest cluster, 2 is the second largest, 3 is the the third largest and so on |
| STRIDE   | ( default=1 ) the frequency with which you would like to output the atoms in the cluster  |
| FILE     | the name of the file on which to output the details of the cluster  |
| MAXDEPTH | ( default=6 ) maximum depth for searches over paths to reconstruct clusters for PBC   |
| MAXGOES  | ( default=200 ) number of times to run searches to reconstuct clusters  |

**Options** 

| MAKE_WHOLE | ( default=off ) reconstruct the clusters and remove all periodic boundary conditions. |
|------------|---|
|            |   |

#### **Examples**

The input shown below identifies those atoms with a coordination number less than 13 and then constructs a contact matrix that describes the connectivity between the atoms that satisfy this criteria. The DFS algorithm is then used to find the connected components in this matrix and the indices of the atoms in the largest connected component are then output to a file.

```
c1: COORDINATIONNUMBER SPECIES=1-1996 SWITCH={CUBIC D_0=0.34 D_MAX=0.38}
cf: MFILTER_LESS DATA=c1 SWITCH={CUBIC D_0=13 D_MAX=13.5}
mat: CONTACT_MATRIX ATOMS=cf SWITCH={CUBIC D_0=0.34 D_MAX=0.38}
dfs: DFSCLUSTERING MATRIX=mat
OUTPUT_CLUSTER CLUSTERS=dfs CLUSTER=1 FILE=dfs.dat
```

# **Chapter 6**

# **Analysis**

PLUMED can be used to analyse trajectories either on the fly during an MD run or via postprocessing a trajectory using driver. About the simplest form of analysis that PLUMED can perform involves printing information to a file. PLUMED can output various different kinds of information to files as described below:

| COMMITTOR       | Does a committor analysis.  |
|-----------------|---|
| DUMPATOMS       | Dump selected atoms on a file.  |
| DUMPDERIVATIVES | Dump the derivatives with respect to the input parameters for one or more objects (generally CVs, functions or biases). |
| DUMPFORCES      | Dump the force acting on one of a values in a file.   |
| DUMPMASSCHARGE  | Dump masses and charges on a selected file.   |
| DUMPMULTICOLVAR | Dump atom positions and multicolvar on a file.  |
| DUMPPROJECTIONS | Dump the derivatives with respect to the input parameters for one or more objects (generally CVs, functions or biases). |
| PRINT           | Print quantities to a file.   |
| UPDATE_IF       | Conditional update of other actions.  |

The UPDATE\_IF action allows you to do more complex things using the above print commands. As detailed in the documentation for UPDATE\_IF when you put any of the above actions within an UPDATE\_IF block then data will only be output to the file if colvars are within particular ranges. In other words, the above printing commands, in tandem with UPDATE\_IF, allow you to identify the frames in your trajectory that satisfy some particular criteria and output information on those frames only.

Another useful command is the COMMITTOR command. This command can only be used when running an molecular dynamics trajectory - it cannot be used when analysing a trajectory using driver. As detailed in the documentation for COMMITTOR this command tells PLUMED (and the underlying MD code) to stop the calculation one some criteria is satisified.

A number of more complicated forms of analysis can be performed that take a number of frames from the trajectory as input. In all these commands the STRIDE keyword is used to tell PLUMED how frequently to collect data from the trajectory. In all these methods the output from the analysis is a form of enseble average. If you are running with a bias it is thus likely that you may want to reweight the trajectory frames in order to remove the effect the bias has on the static behavoir of the system. The following methods can thus be used to calculate weights for the various trajectory frames so that the final ensemble average is an average for the cannonical ensemble at the appropriate temperature.

| REWEIGHT_BIAS | Calculate weights for ensemble averages that negate the effect the bias has on the |
|---------------|--|
|               | region of phase space explored   |

| REWEIGHT_METAD | Calculate the weights configurations should contribute to the histogram in a simulation in which a metadynamics bias acts upon the system.                    |
|----------------|---|
| REWEIGHT_TEMP  | Calculate weights for ensemble averages allow for the computing of ensemble averages at temperatures lower/higher than that used in your original simulation. |

You can then calculate ensemble averages using the following actions.

| AVERAGE         | Calculate the ensemble average of a collective variable                       |
|-----------------|---|
| HISTOGRAM       | Accumulate the average probability density along a few CVs from a trajectory. |
| MULTICOLVARDENS | Evaluate the average value of a multicolvar on a grid.                        |

For many of the above commands data is accumulated on the grids. These grids can be further analysed using one of the actions detailed below at some time.

| 00111/EDT TO EEO       |  |
|------------------------|--|
| CONVERT_TO_FES         | Convert a histogram, $H(x)$ , to a free energy surface using $F(x) = 0$        |
|                        | $-k_BT\ln H(x)$ .  |
| DUMPOURE               |  |
| DUMPCUBE               | Output a three dimensional grid using the Gaussian cube file format.           |
| DUMPGRID               | Output the function on the grid to a file with the PLUMED grid format.         |
| FIND_CONTOUR_SURFACE   | Find an isocontour by searching along either the x, y or direction.            |
| FIND_CONTOUR           | Find an isocontour in a smooth function.                                       |
| FIND_SPHERICAL_CONTOUR | Find an isocontour in a three dimensional grid by searching over a Fibonacci   |
|                        | sphere.  |
| FOURIER_TRANSFORM      | Compute the Discrete Fourier Transform (DFT) by means of FFTW of data          |
|                        | stored on a 2D grid.   |
| GRID_TO_XYZ            | Output the function on the grid to an xyz file                                 |
| INTEGRATE_GRID         | Calculate the total integral of the function on the input grid                 |
| INTERPOLATE GRID       | Interpolate a smooth function stored on a grid onto a grid with a smaller grid |
| _                      | spacing.   |
| 1                      |  |

As an example the following set of commands instructs PLUMED to calculate the distance between atoms 1 and 2 for every 5th frame in the trajectory and to accumulate a histogram from this data which will be output every 100 steps (i.e. when 20 distances have been added to the histogram).

```
x: DISTANCE ATOMS=1,2
h: HISTOGRAM ARG=x GRID_MIN=0.0 GRID_MAX=3.0 GRID_BIN=100 BANDWIDTH=0.1 STRIDE=5
DUMPGRID GRID=h FILE=histo STRIDE=100
```

It is important to note when using commands such as the above the first frame in the trajectory is assumed to be the initial configuration that was input to the MD code. It is thus ignored. Furthermore, if you are running with driver and you would like to analyse the whole trajectory (without specifying its length) and then print the result you simply call DUMPGRID (or any of the commands above) without a STRIDE keyword as shown in the example below.

```
x: DISTANCE ATOMS=1,2
h: HISTOGRAM ARG=x GRID_MIN=0.0 GRID_MAX=3.0 GRID_BIN=100 BANDWIDTH=0.1 STRIDE=5
DUMPGRID GRID=h FILE=histo
```

Please note that even with this calculation the first frame in the trajectory is ignored when computing the histogram.

Notice that all the commands for calculating smooth functions described above calculate some sort of average. There are two ways that you may wish to average the data in your trajectory:

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• You might want to calculate block averages in which the first NN frames in your trajectory are averaged separately to the second block of N frames. If this is the case you should use the keyword CLEAR in the input to the action that calculates the smooth function. This keyword is used to specify how frequently you are clearing the stored data.

• You might want to calculate an accumulate an average over the whole trajectory and output the average accumulated at step N, step  $2N\ldots$  This is what PLUMED does by default so you do not need to use CLEAR in this case.

# 6.1 Dimensionality Reduction

The remainder of the analysis tools within PLUMED allow one to do some form of dimensionality reduction as detailed below.

| CLASSICAL_MDS | Create a low-dimensional projection of a trajectory using the classical multidimensional scaling algorithm.                         |
|---------------|---|
| PCA           | Perform principal component analysis (PCA) using either the positions of the atoms a large number of collective variables as input. |

As with the grids described previously the STRIDE keyword tells PLUMED how frequently to collect data from the trajectory. The RUN keyword then tells PLUMED how frequently to do the dimensionality reduction. As described above if RUN is not present and you are analysing trajectories using driver all the data in the traejctory (with the expection of the first frame) will be analysed.

#### 6.2 COMMITTOR

This is part of the analysis module

Does a committor analysis.

Compulsory keywords

| BASIN_LL | List of lower limits for basin # You can use multiple instances of this keyword i.e. BASIN_LL1, BASIN_LL2, BASIN_LL3 |
|----------|--|
| BASIN_UL | List of upper limits for basin # You can use multiple instances of this keyword i.e. BASIN_UL1, BASIN_UL2, BASIN_UL3 |
| STRIDE   | ( default=1 ) the frequency with which the CVs are analysed  |

| AR  | the input for this action is the scalar output from one or more other actions. The particular scalars        |
|-----|--|
|     | that you will use are referenced using the label of the action. If the label appears on its own then it is   |
|     | assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the       |
|     | input to this new action. If $*$ or $*.*$ appears the scalars calculated by all the proceding actions in the |
|     | input file are taken. Some actions have multi-component outputs and each component of the output has         |
|     | a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z.           |
|     | To take just the x component you should use dist.x, if you wish to take all three components then use        |
|     | dist.*.More information on the referencing of Actions can be found in the section of the manual on the       |
|     | PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as              |
|     | detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with         |
|     | the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3                   |
| FIL | the name of the file on which to output the reached basin  |
| FM  | the format that should be used to output real numbers  |
|     |  |

#### **Examples**

The following input monitors two torsional angles during a simulation, defines two basins (A and B) as a function of the two torsions and stops the simulation when it falls in one of the two. In the log file will be shown the latest values for the CVs and the basin reached.

```
TORSION ATOMS=1,2,3,4 LABEL=r1
TORSION ATOMS=2,3,4,5 LABEL=r2
COMMITTOR ...

ARG=r1,r2
STRIDE=10
BASIN_LL1=0.15,0.20
BASIN_UL1=0.25,0.40
BASIN_LL2=-0.15,-0.20
BASIN_UL2=-0.25,-0.40
... COMMITTOR
```

# 6.3 DUMPATOMS

This is part of the generic module

Dump selected atoms on a file.

This command can be used to output the positions of a particular set of atoms. The atoms required are ouput in a xyz or gro formatted file. If PLUMED has been compiled with xdrfile support, then also xtc and trr files can be written. To this aim one should install xdrfile library (http://www.gromacs.org/Developer\_Zone/ $\leftarrow$  Programming\_Guide/XTC\_Library). If the xdrfile library is installed properly the PLUMED configure script should be able to detect it and enable it. The type of file is automatically detected from the file extension, but can be also enforced with TYPE. Importantly, if your input file contains actions that edit the atoms position (e.g. WH $\leftarrow$  OLEMOLECULES) and the DUMPATOMS command appears after this instruction, then the edited atom positions are output. You can control the buffering of output using the FLUSH keyword on a separate line.

Units of the printed file can be controlled with the UNITS keyword. By default PLUMED units as controlled in the UNITS command are used, but one can override it e.g. with UNITS=A. Notice that gro/xtc/trr files can only contain coordinates in nm.

The atoms involved can be specified using

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| ATOMS | the atom indices whose positions you would like to print out. For more information on how to specify |
|-------|--|
|       | lists of atoms see Groups and Virtual Atoms  |

#### Compulsory keywords

| STRIDE | ( default=1 ) the frequency with which the atoms should be output        |  |
|--------|--|--|
| FILE   | file on which to output coordinates; extension is automatically detected |  |
| UNITS  | ( , , ,  |  |
|        | MED units  |  |

#### **Options**

| PRECISION   | The number of digits in trajectory file  |  |
|---|--|--|
| TYPE  | file type, either xyz, gro, xtc, or trr, can override an automatically detected file extension |  |
| RESTART   | allows per-action setting of restart (YES/NO/AUTO)   |  |
| UPDATE_FROM   | Only update this action from this time   |  |
| UPDATE_UN ← Only update this action until this time |  |  |
| TIL   |  |  |

#### **Examples**

The following input instructs plumed to print out the positions of atoms 1-10 together with the position of the center of mass of atoms 11-20 every 10 steps to a file called file.xyz.

```
COM ATOMS=11-20 LABEL=c1
DUMPATOMS STRIDE=10 FILE=file.xyz ATOMS=1-10,c1
```

#### (see also COM)

The following input is very similar but dumps a .gro (gromacs) file, which also contains atom and residue names.

```
# this is required to have proper atom names:
MOLINFO STRUCTURE=reference.pdb
# if omitted, atoms will have "X" name...

COM ATOMS=11-20 LABEL=c1
DUMPATOMS STRIDE=10 FILE=file.gro ATOMS=1-10,c1
# notice that last atom is a virtual one and will not have
# a correct name in the resulting gro file
```

(see also COM and MOLINFO)

# 6.4 DUMPDERIVATIVES

This is part of the generic module

Dump the derivatives with respect to the input parameters for one or more objects (generally CVs, functions or biases).

For a CV this line in input instructs plumed to print the derivative of the CV with respect to the atom positions and the cell vectors (virial-like form). In contrast, for a function or bias the derivative with respect to the input "CVs" will be output. This command is most often used to test whether or not analytic derivatives have been implemented correctly. This can be done by outputting the derivatives calculated analytically and numerically. You can control the buffering of output using the FLUSH keyword.

#### Compulsory keywords

| STRIDE | ( default=1 ) the frequency with which the derivatives should be output    |
|--------|--|
| FILE   | the name of the file on which to output the derivatives                    |
| FMT    | ( default=%15.10f ) the format with which the derivatives should be output |

#### **Options**

| ARG               | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. Ac RG1, ARG2, ARG3 |
|-------------------|---|
| RESTART           | allows per-action setting of restart (YES/NO/AUTO)  |
| UPDATE_FROM       | Only update this action from this time  |
| UPDATE_UN←<br>TIL | Only update this action until this time   |

#### **Examples**

The following input instructs plumed to write a file called deriv that contains both the analytical and numerical derivatives of the distance between atoms 1 and 2.

```
DISTANCE ATOM=1,2 LABEL=distance
DISTANCE ATOM=1,2 LABEL=distanceN NUMERICAL_DERIVATIVES
DUMPDERIVATIVES ARG=distance, distanceN STRIDE=1 FILE=deriv
```

# (See also **DISTANCE**)

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# 6.5 DUMPFORCES

This is part of the generic module

Dump the force acting on one of a values in a file.

For a CV this command will dump the force on the CV itself. Be aware that in order to have the forces on the atoms you should multiply the output from this argument by the output from DUMPDERIVATIVES. Furthermore, also note that you can output the forces on multiple quantities simultaneously by specifying more than one argument. You can control the buffering of output using the FLUSH keyword.

#### Compulsory keywords

| STRIDE | ( default=1 ) the frequency with which the forces should be output         |
|--------|--|
| FILE   | the name of the file on which to output the forces                         |
| FMT    | ( default=%15.10f ) the format with which the derivatives should be output |

#### **Options**

| ARG               | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. Active RG1, ARG2, ARG3 |
|-------------------|---|
| RESTART           | allows per-action setting of restart (YES/NO/AUTO)  |
| UPDATE_FROM       | Only update this action from this time  |
| UPDATE_UN←<br>TIL | Only update this action until this time   |

#### **Examples**

The following input instructs plumed to write a file called forces that contains the force acting on the distance between atoms 1 and 2.

DISTANCE ATOM=1,2 LABEL=distance
DUMPFORCES ARG=distance STRIDE=1 FILE=forces

(See also **DISTANCE**)

# 6.6 DUMPMASSCHARGE

6.6 DUMPMASSCHARGE 311

This is part of the generic module

Dump masses and charges on a selected file.

This command dumps a file containing charges and masses. It does so only once in the simulation (at first step). File can be recycled in the driver tool.

Notice that masses and charges are only written once at the beginning of the simulation. In case no atom list is provided, charges and masses for all atoms are written.

The atoms involved can be specified using

| ATOM | the atom indices whose positions you would like to print out. For more information on how to specify |  |
|------|--|--|
|      | lists of atoms see Groups and Virtual Atoms  |  |

Compulsory keywords

| STRIDE | ( default=1 ) the frequency with which the atoms should be output          |  |
|--------|--|--|
| FILE   | file on which to output coordinatesgro extension is automatically detected |  |

#### **Examples**

You can add the DUMPMASSCHARGE action at the end of the plumed.dat file that you use during an MD simulations:

```
c1: COM ATOMS=1-10
c2: COM ATOMS=11-20
PRINT ARG=c1,c2 FILE=colvar STRIDE=100
DUMPMASSCHARGE FILE=mcfile
```

#### (see also COM and PRINT)

In this way, you will be able to use the same masses while processing a trajectory from the driver . To do so, you need to add the -mc flag on the driver command line, e.g.

```
plumed driver --mc mcfile --plumed plumed.dat --ixyz traj.xyz
```

With the following input you can dump only the charges for a specific group.

```
solute_ions: GROUP ATOMS=1-121,200-2012
DUMPATOMS FILE=traj.gro ATOMS=solute_ions STRIDE=100
DUMPMASSCHARGE FILE=mcfile ATOMS=solute_ions
```

Notice however that if you want to process the charges with the driver (e.g. reading traj.gro) you have to fix atom numbers first, e.g. with the script

```
awk 'BEGIN{c=0}{
  if(match($0,"#")) print; else {print c,$2,$3; c++}
}' < mc > newmc
}'
then
plumed driver --mc newmc --plumed plumed.dat --ixyz traj.gro
```

# 6.7 DUMPMULTICOLVAR

This is part of the multicolvar module

Dump atom positions and multicolvar on a file.

The atoms involved can be specified using

| ORIGIN | You can use this keyword to specify the position of an atom as an origin. The positions output will  |
|--------|--|
|        | then be displayed relative to that origin. For more information on how to specify lists of atoms see |
|        | Groups and Virtual Atoms   |

#### Compulsory keywords

| DATA   | certain actions in plumed work by calculating a list of variables and summing over them. This particular action can be used to calculate functions of these base variables or prints them to a file. This keyword thus takes the label of one of those such variables as input. |  |
|--------|---|--|
| STRIDE | ( default=1 ) the frequency with which the atoms should be output   |  |
| FILE   | file on which to output coordinates   |  |
| UNITS  | ( default=PLUMED ) the units in which to print out the coordinates. PLUMED means internal PLU←  |  |
|        | MED units   |  |

#### **Options**

| PRECISION | The number of digits in trajectory file |
|-----------|---|
|           |   |

# **Examples**

In this examples we calculate the distances between the atoms of the first and the second group and we write them in the file MULTICOLVAR.xyz. For each couple it writes the coordinates of their geometric center and their distance.

```
pos: GROUP ATOMS=220,221,235,236,247,248,438,439,450,451,534,535
neg: GROUP ATOMS=65,68,138,182,185,267,270,291,313,316,489,583,621,711
DISTANCES GROUPA=pos GROUPB=neg LABEL=slt
DUMPMULTICOLVAR DATA=slt FILE=MULTICOLVAR.xyz
```

(see also DISTANCES)

# 6.8 DUMPPROJECTIONS

6.9 PRINT 313

This is part of the generic module

Dump the derivatives with respect to the input parameters for one or more objects (generally CVs, functions or biases).

# Compulsory keywords

| STRIDE ( default=1 ) the frequency with which the derivatives should be output |  |
|--|--|
| FILE the name of the file on which to output the derivatives                   |  |
| FMT ( default=%15.10f ) the format with which the derivatives should be out    |  |

# **Options**

| ARG               | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. Ac RG1, ARG2, ARG3 |
|-------------------|---|
| RESTART           | allows per-action setting of restart (YES/NO/AUTO)  |
| UPDATE_FROM       | Only update this action from this time  |
| UPDATE_UN↔<br>TIL | Only update this action until this time   |

#### **Examples**

Compute the distance between two groups and write on a file the derivatives of this distance with respect to all the atoms of the two groups

```
x1: CENTER ATOMS=1-10
x2: CENTER ATOMS=11-20
d: DISTANCE ATOMS=x1,x2
DUMPPROJECTIONS ARG=d FILE=proj STRIDE=20
```

# 6.9 PRINT

This is part of the generic module

Print quantities to a file.

This directive can be used multiple times in the input so you can print files with different strides or print different quantities to different files. You can control the buffering of output using the FLUSH keyword.

Compulsory keywords

| STRIDE (default=1) the frequency with which the quantities of interest should be output |
|---|
|---|

**Options** 

| the input for this action is the scalar output from one or more other actions. The scalars that you will use are referenced using the label of the action. If the label its own then it is assumed that the Action calculates a single scalar value. The scalar is thus used as the input to this new action. If * or *.* appears the scalar by all the proceding actions in the input file are taken. Some actions have multiputs and each component of the output has a specific label. For example action labelled dist may have three components x, y and z. To take just the x conshould use dist.x, if you wish to take all three components then use dist.*.More on the referencing of Actions can be found in the section of the manual on the Getting started. Scalar values can also be referenced using POSIX regular examples action to the section on Regular Expressions. To use this feature you you will be proposed to the appropriate flag. You can use multiple instances of this key. |  |
|---|--|
| FILE  | RG1, ARG2, ARG3 the name of the file on which to output these quantities |
| FMT   | the format that should be used to output real numbers                    |
| RESTART   | allows per-action setting of restart (YES/NO/AUTO)                       |
| UPDATE_FROM   | Only update this action from this time                                   |
| UPDATE_UN↔<br>TIL   | Only update this action until this time                                  |

#### **Examples**

The following input instructs plumed to print the distance between atoms 3 and 5 on a file called COLVAR every 10 steps, and the distance and total energy on a file called COLVAR\_ALL every 1000 steps.

```
DISTANCE ATOMS=2,5 LABEL=distance
ENERGY LABEL=energy
PRINT ARG=distance STRIDE=10 FILE=COLVAR
PRINT ARG=distance, energy STRIDE=1000 FILE=COLVAR_ALL
```

(See also DISTANCE and ENERGY).

#### 6.9.1 FLUSH

This is part of the generic module

This command instructs plumed to flush all the open files with a user specified frequency. Notice that all files are flushed anyway every 10000 steps.

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This is useful for preventing data loss that would otherwise arrise as a consequence of the code storing data for printing in the buffers. Notice that wherever it is written in the plumed input file, it will flush all the open files.

Compulsory keywords

STRIDE the frequency with which all the open files should be flushed

#### **Examples**

6.10

A command like this in the input will instruct plumed to flush all the output files every 100 steps

```
d1: DISTANCE ATOMS=1,10
PRINT ARG=d1 STRIDE=5 FILE=colvar1
FLUSH STRIDE=100
d2: DISTANCE ATOMS=2,11
# also this print is flushed every 100 steps:
PRINT ARG=d2 STRIDE=10 FILE=colvar2
```

# 0 UPDATE IF

(see also DISTANCE and PRINT).

This is part of the generic module

Conditional update of other actions.

This action can be used to enable and disable the update step for the following actions depending on the value of its arguments. This allows for example to extract snapshots with value of some CVs in a given range.

When called with MORE\_THAN and/or LESS\_THAN keywords, this action starts an if block. The block is executed if all the arguments are less than all the respective values in the LESS\_THAN keyword (if present) and all the arguments are more than all the respective values in the MORE\_THAN keyword (if present).

When called with the END flag, this action ends the corresponding IF block. Notice that in this case one should also provide the ARG keyword. It is recommended to use the same ARG keyword that was used to begin the block, so as to make the input more readable.

Of course, blocks can be nested at will.

There are many potential usages for this keyword. One might e.g. decide to analyze some variable only when another variable is within a given range.

#### Warning

Notice that not all the possible usage make particular sense. For example, conditionally updating a METAD keyword (that is: adding hills only if a variable is within a given range) can lead to unexpected results.

Compulsory keywords

**STRIDE** (default=1) the frequency with which the quantities of interest should be output

#### **Options**

| END       | ( default=off ) end  |  |
|-----------|--|--|
| ARG       | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three components x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |  |
| LESS_THAN | upper bound  |  |
| MORE_THAN | lower bound  |  |

#### **Examples**

The following input instructs plumed dump all the snapshots where an atom is in touch with the solute.

```
solute: GROUP ATOMS=1-124
coord: COORDINATION GROUPA=solute GROUPB=500 R_0=0.5

UPDATE_IF ARG=coord LESS_THAN=0.5

DUMPATOMS ATOMS=solute,500 FILE=output.xyz

UPDATE_IF ARG=coord END
```

(See also GROUP, COORDINATION, and DUMPATOMS)

# 6.11 REWEIGHT\_BIAS

This is part of the bias module

Calculate weights for ensemble averages that negate the effect the bias has on the region of phase space explored

If a static or pseudo-static bias V(x,t') is acting on the system we can remove the bias and get the unbiased probability distribution using:

$$\langle P(s',t) \rangle = \frac{\sum_{t'}^{t} \delta(s(x) - s') \exp\left(+\frac{V(x,t')}{k_B T}\right)}{\sum_{t'}^{t} \exp\left(+\frac{V(x,t')}{k_B T}\right)}$$

The weights calculated by this action are equal to  $\exp\left(+\frac{V(x,t')}{k_BT}\right)$  these weights can then be used in any action that computes ensemble averages. For example this action can be used in tandem with HISTOGRAM or AVERAGE.

Compulsory keywords

**ARG** (default=\*.bias) the biases that must be taken into account when reweighting

**Options** 

**TEMP** the system temperature. This is not required if your MD code passes this quantity to PLUMED

#### **Examples**

In the following example there is a fixed restraint on the distance between atoms 1 and 2. Clearly, this restraint will have an effect on the region of phase space that will be sampled when an MD simulation is run using this variable. Consequently, when the histogram as a function of the distance, x, is accumulated, we use reweighting into order to discount the effect of the bias from our final histogram.

```
x: DISTANCE ATOMS=1,2
RESTRAINT ARG=x SLOPE=1.0 AT=0.0
as: REWEIGHT_BIAS TEMP=300

HISTOGRAM ...
ARG=x
GRID_MIN=0.0
GRID_MAX=3.0
GRID_BIN=100
BANDWIDTH=0.1
LOGWEIGHTS=bias
LABEL=hB
... HISTOGRAM

DUMPGRID GRID=hB FILE=histoB STRIDE=1 FMT=%8.4f
```

# 6.12 REWEIGHT\_METAD

This is part of the bias module

Calculate the weights configurations should contribute to the histogram in a simulation in which a metadynamics bias acts upon the system.

This command allows you to use the reweighting algorithm discussed in ? when constructing a histogram of the configurations visited during a metadynamics simulation.

Compulsory keywords

**ARG** (default=\*.rbias) the biases that must be taken into account when reweighting

**Options** 

**TEMP** the system temperature. This is not required if your MD code passes this quantity to PLUMED

**Examples** 

In the following example there is a metadynamics bias acting on the distance between atoms 1 and 2. Clearly, this bias will have an effect on the region of phase space that will be sampled when an MD simulation is run using this variable. Consequently, when the histogram as a function of the angle, a, is accumulated, we use reweighting into order to discount the effect of the bias from our final histogram. We do not use REWEIGHT\_BIAS here, however, as the bias changes with time. We thus use the reweighting algorithm for metadynamics instead. Notice also that we have to specify how often we would like to calculate the c(t) reweighting factor and the grid over which we calculate c(t) in the input to the METAD command.

```
a: ANGLE ATOMS=1,2,3
x: DISTANCE ATOMS=1,2
METAD ARG=x PACE=100 SIGMA=0.1 HEIGHT=1.5 BIASFACTOR=5 GRID_MIN=0 GRID_MAX=10 GRID_BIN=100 REWEIGHTING_NGRID=1
as: REWEIGHT_METAD TEMP=300

HISTOGRAM ...
ARG=a
GRID_MIN=0.0
GRID_MAX=pi
GRID_BIN=100
BANDWIDTH=0.1
LOGWEIGHTS=bias
LABEL=hB
... HISTOGRAM

DUMPGRID GRID=hB FILE=histoB STRIDE=1 FMT=%8.4f
```

# 6.13 REWEIGHT\_TEMP

This is part of the bias module

Calculate weights for ensemble averages allow for the computing of ensemble averages at temperatures lower/higher than that used in your original simulation.

We can use our knowledge of the Boltzmann distribution in the cannonical ensemble to reweight the data contained in trajectories. Using this procedure we can take trajectory at temperature  $T_1$  and use it to extract probabilities at a different temperature,  $T_2$ , using:

$$P(s',t) = \frac{\sum_{t'}^{t} \delta(s(x) - s') \exp\left(+\left(\left[\frac{1}{T_{1}} - \frac{1}{T_{2}}\right] \frac{U(x,t')}{k_{B}}\right)\right)}{\sum_{t'}^{t} \exp\left(+\left[\frac{1}{T_{1}} - \frac{1}{T_{2}}\right] \frac{U(x,t')}{k_{B}}\right)}$$

The weights calculated by this action are equal to  $\exp\left(+\left(\left[\frac{1}{T_1}-\frac{1}{T_2}\right]\frac{U(x,t')}{k_B}\right)$  and take the effect the bias has on the system into account. These weights can be used in any action that computes ensemble averages. For example this action can be used in tandem with HISTOGRAM or AVERAGE.

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Compulsory keywords

| REWEIGHT_TEMP | reweight data from a trajectory at one temperature and output the probability distribution |
|---------------|--|
|               | at a second temperature. This is not possible during postprocessing.                       |

**Options** 

| TEMP | the system temperature. | This is not required if your MD code passes this quantity to PLUMED |
|------|-------------------------|---|
| 1    |                         |   |

**Examples** 

#### 6.14 AVERAGE

This is part of the analysis module

Calculate the ensemble average of a collective variable

The ensemble average for a non-periodic, collective variable, s is given by the following expression:

$$\langle s \rangle = \frac{\sum_{t'=0}^{t} w(t')s(t')}{\sum_{t'=0}^{t} w(t')}$$

Here the sum runs over a the trajectory and s(t') is used to denote the value of the collective variable at time t'. The final quantity evalulated is a weighted average as the weights, w(t'), allow us to negate the effect any bias might have on the region of phase space sampled by the system. This is discussed in the section of the manual on Analysis.

When the variable is periodic (e.g. TORSION) and has a value, s, in  $a \le s \le b$  the ensemble average is evaluated using:

$$\langle s \rangle = a + \frac{b-a}{2\pi} \arctan \left[ \frac{\sum_{t'=0}^{t} w(t') \sin\left(\frac{2\pi [s(t')-a]}{b-a}\right)}{\sum_{t'=0}^{t} w(t') \cos\left(\frac{2\pi [s(t')-a]}{b-a}\right)} \right]$$

Compulsory keywords

| STRIDE | ( default=1 ) the frequency with which the data should be collected and added to the quantity being averaged  |
|--------|---|
| CLEAR  | ( default=0 ) the frequency with which to clear all the accumulated data. The default value of 0 implies that all the data will be used and that the grid will never be cleared |

#### **Options**

| TIMINGS     | ( default=off ) output information on the timings of the various parts of the calculation   |
|-------------|---|
| TIMINGS     | ( default=off ) output information off the tillings of the various parts of the calculation   |
| UNORMALIZED | ( default=off ) output the unaveraged quantity/quantities.  |
| LOGWEIGHTS  | list of actions that calculates log weights that should be used to weight configurations when calculating averages  |
| ARG         | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile P LUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |

#### **Examples**

The following example calculates the ensemble average for the distance between atoms 1 and 2 and output this to a file called COLVAR. In this example it is assumed that no bias is acting on the system and that the weights, w(t') in the formulae above can thus all be set equal to one.

```
d1: DISTANCE ATOMS=1,2
d1a: AVERAGE ARG=d1
PRINT ARG=d1a FILE=colvar STRIDE=100
```

The following example calculates the ensemble average for the torsional angle involving atoms 1, 2, 3 and 4. At variance with the previous example this quantity is periodic so the second formula in the above introduction is used to calculate the average. Furthermore, by using the CLEAR keyword we have specified that block averages are to be calculated. Consequently, after 100 steps all the information aquired thus far in the simulation is forgotten and the process of averaging is begun again. The quantities output in the colvar file are thus the block averages taken over the first 100 frames of the trajectory, the block average over the second 100 frames of trajectory and so on.

```
t1: TORSION ATOMS=1,2,3,4
t1a: AVERAGE ARG=t1 CLEAR=100
PRINT ARG=t1a FILE=colvar STRIDE=100
```

This third example incorporates a bias. Notice that the effect the bias has on the ensemble average is removed by taking advantage of the REWEIGHT\_BIAS method. The final ensemble averages output to the file are thus block ensemble averages for the unbiased canononical ensemble at a temperature of 300 K.

```
t1: TORSION ATOMS=1,2,3,4
RESTRAINT ARG=t1 AT=pi KAPPA=100.
ww: REWEIGHT_BIAS TEMP=300
t1a: AVERAGE ARG=t1 LOGWEIGHTS=ww CLEAR=100
PRINT ARG=t1a FILE=colvar STRIDE=100
```

#### 6.15 HISTOGRAM

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This is part of the analysis module

Accumulate the average probability density along a few CVs from a trajectory.

When using this method it is supposed that you have some collective variable  $\zeta$  that gives a reasonable description of some physical or chemical phenomenon. As an example of what we mean by this suppose you wish to examine the following SN2 reaction:

$$OH^- + CH_3Cl \rightarrow CH_3OH + Cl^-$$

The distance between the chlorine atom and the carbon is an excellent collective variable,  $\zeta$ , in this case because this distance is short for the reactant,  ${\rm CH_3}Cl$ , because the carbon and chlorine are chemically bonded, and because it is long for the product state when these two atoms are not chemically bonded. We thus might want to accumulate the probability density,  $P(\zeta)$ , as a function of this distance as this will provide us with information about the overall likelihood of the reaction. Furthermore, the free energy,  $F(\zeta)$ , is related to this probability density via:

$$F(\zeta) = -k_B T \ln P(\zeta)$$

Accumulating these probability densities is precisely what this Action can be used to do. Furthermore, the conversion of the histogram to the free energy can be achieved by using the method CONVERT TO FES.

We calculate histograms within PLUMED using a method known as kernel density estimation, which you can read more about here:

https://en.wikipedia.org/wiki/Kernel\_density\_estimation

In PLUMED the value of  $\zeta$  at each discrete instant in time in the trajectory is accumulated. A kernel,  $K(\zeta-\zeta(t'),\sigma)$ , centered at the current value,  $\zeta(t)$ , of this quantity is generated with a bandwith  $\sigma$ , which is set by the user. These kernels are then used to accumulate the ensemble average for the probability density:

$$\langle P(\zeta) \rangle = \frac{\sum_{t'=0}^{t} w(t') K(\zeta - \zeta(t'), \sigma)}{\sum_{t'=0}^{t} w(t')}$$

Here the sums run over a portion of the trajectory specified by the user. The final quantity evalulated is a weighted average as the weights, w(t'), allow us to negate the effect any bias might have on the region of phase space sampled by the system. This is discussed in the section of the manual on Analysis.

A discrete analogue of kernel density estimation can also be used. In this analogue the kernels in the above formula are replaced by dirac delta functions. When this method is used the final function calculated is no longer a probability density - it is instead a probability mass function as each element of the function tells you the value of an integral between two points on your grid rather than the value of a (continuous) function on a grid.

Additional material and examples can be also found in the tutorial Belfast tutorial: Analyzing CVs.

Compulsory keywords

| STRIDE                         | ( default=1 ) the frequency with which the data should be collected and added to the quantity being averaged  |
|--------------------------------|---|
| Ge <b>©etrEroN</b> ETy Doxygen | ( default=0 ) the frequency with which to clear all the accumulated data. The default value of 0 implies that all the data will be used and that the grid will never be cleared |
| BANDWIDTH                      | the bandwidths for kernel density esimtation  |
| KERNEL                         | ( default=gaussian ) the kernel function you are using. More details on the kernels available in  |

### **Options**

| SERIAL        | ( default=off ) do the calculation in serial. Do not parallelize   |
|---------------|--|
| LOWMEM        | ( default=off ) lower the memory requirements  |
| TIMINGS       | ( default=off ) output information on the timings of the various parts of the calculation  |
| UNORMALIZED   | ( default=off ) output the unaveraged quantity/quantities.   |
| LOGWEIGHTS    | list of actions that calculates log weights that should be used to weight configurations when calculating averages   |
| CONCENTRATION | the concentration parameter for Von Mises-Fisher distributions   |
| ARG           | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three components x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |
| DATA          | input data from action with vessel and compute histogram   |
| GRID_BIN      | the number of bins for the grid  |
| GRID_SPACING  | the approximate grid spacing (to be used as an alternative or together with GRID_BIN)  |
| UPDATE_FROM   | Only update this action from this time   |
| UPDATE_UNTIL  | Only update this action until this time  |

## **Examples**

The following input monitors two torsional angles during a simulation and outputs a continuos histogram as a function of them at the end of the simulation.

```
TORSION ATOMS=1,2,3,4 LABEL=r1
TORSION ATOMS=2,3,4,5 LABEL=r2
HISTOGRAM ...
ARG=r1,r2
GRID_MIN=-3.14,-3.14
GRID_BIN=200,200
BANDWIDTH=0.05,0.05
LABEL=hh
... HISTOGRAM

DUMPGRID GRID=hh FILE=histo
```

The following input monitors two torsional angles during a simulation and outputs a discrete histogram as a function of them at the end of the simulation.

```
TORSION ATOMS=1,2,3,4 LABEL=r1
TORSION ATOMS=2,3,4,5 LABEL=r2
HISTOGRAM ...
```

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```
ARG=r1,r2
USE_ALL_DATA
KERNEL=DISCRETE
GRID_MIN=-3.14,-3.14
GRID_MAX=3.14,3.14
GRID_BIN=200,200
LABEL=hh
... HISTOGRAM

DUMPGRID GRID=hh FILE=histo
```

The following input monitors two torsional angles during a simulation and outputs the histogram accumulated thus far every 100000 steps.

```
TORSION ATOMS=1,2,3,4 LABEL=r1
TORSION ATOMS=2,3,4,5 LABEL=r2
HISTOGRAM ...
ARG=r1,r2
GRID_MIN=-3.14,-3.14
GRID_MAX=3.14,3.14
GRID_BIN=200,200
BANDWIDTH=0.05,0.05
LABEL=hh
... HISTOGRAM

DUMPGRID GRID=hh FILE=histo STRIDE=100000
```

The following input monitors two torsional angles during a simulation and outputs a separate histogram for each 100000 steps worth of trajectory. Notice how the CLEAR keyword is used here and how it is not used in the previous example.

```
TORSION ATOMS=1,2,3,4 LABEL=r1
TORSION ATOMS=2,3,4,5 LABEL=r2
HISTOGRAM ...

ARG=r1,r2 CLEAR=100000
GRID_MIN=-3.14,-3.14
GRID_MAX=3.14,3.14
GRID_BIN=200,200
BANDWIDTH=0.05,0.05
GRID_WFILE=histo
LABEL=hh
... HISTOGRAM

DUMPGRID GRID=hh FILE=histo STRIDE=100000
```

# 6.16 MULTICOLVARDENS

This is part of the multicolvar module

Evaluate the average value of a multicolvar on a grid.

This keyword allows one to construct a phase field representation for a symmetry function from an atomistic description. If each atom has an associated order parameter,  $\phi_i$  then a smooth phase field function  $\phi(r)$  can be computed using:

$$\phi(\mathbf{r}) = \frac{\sum_{i} K(\mathbf{r} - \mathbf{r}_{i})\phi_{i}}{\sum_{i} K(\mathbf{r} - \mathbf{r}_{i})}$$

where  $\mathbf{r}_i$  is the position of atom i, the sums run over all the atoms input and  $K(\mathbf{r}-\mathbf{r}_i)$  is one of the kernelfunctions implemented in plumed. This action calculates the above function on a grid, which can then be used in the input to further actions.

The atoms involved can be specified using

| ORIGIN | we will use the position of this atom as the origin. For | r more information on how to specify lists of |
|--------|--|---|
|        | atoms see Groups and Virtual Atoms                       |   |

### Compulsory keywords

| STRIDE    | ( default=1 ) the frequency with which the data should be collected and added to the quantity being averaged  |
|-----------|---|
| CLEAR     | ( default=0 ) the frequency with which to clear all the accumulated data. The default value of 0 implies that all the data will be used and that the grid will never be cleared |
| BANDWIDTH | the bandwidths for kernel density esimtation  |
| KERNEL    | ( default=gaussian ) the kernel function you are using. More details on the kernels available in plumed plumed can be found in kernelfunctions.                                 |
| DATA      | the multicolvar which you would like to calculate the density profile for   |
| DIR       | the direction in which to calculate the density profile   |

| SERIAL        | ( default=off ) do the calculation in serial. Do not parallelize  |
|---------------|---|
| LOWMEM        | ( default=off ) lower the memory requirements   |
| TIMINGS       | ( default=off ) output information on the timings of the various parts of the calculation   |
| UNORMALIZED   | ( default=off ) output the unaveraged quantity/quantities.  |
| FRACTIONAL    | ( default=off ) use fractional coordinates for the various axes   |
| XREDUCED      | ( default=off ) limit the calculation of the density/average to a portion of the z-axis only  |
| YREDUCED      | ( default=off ) limit the calculation of the density/average to a portion of the y-axis only  |
| ZREDUCED      | ( default=off ) limit the calculation of the density/average to a portion of the z-axis only  |
| LOGWEIGHTS    | list of actions that calculates log weights that should be used to weight configurations when calculating averages  |
| CONCENTRATION | the concentration parameter for Von Mises-Fisher distributions  |
| NBINS         | the number of bins to use to represent the density profile  |
| SPACING       | the approximate grid spacing (to be used as an alternative or together with NBINS)  |
| XLOWER        | this is required if you are using XREDUCED. It specifes the lower bound for the region of the x-axis that for which you are calculating the density/average |
| XUPPER        | this is required if you are using XREDUCED. It specifes the upper bound for the region of the x-axis that for which you are calculating the density/average |
| YLOWER        | this is required if you are using YREDUCED. It specifes the lower bound for the region of the y-axis that for which you are calculating the density/average |
| YUPPER        | this is required if you are using YREDUCED. It specifes the upper bound for the region of the y-axis that for which you are calculating the density/average |

| ZLOWER | this is required if you are using ZREDUCED. It specifes the lower bound for the region of the z-axis that for which you are calculating the density/average |
|--------|---|
| ZUPPER | this is required if you are using ZREDUCED. It specifes the upper bound for the region of the z-axis that for which you are calculating the density/average |

### **Examples**

The following example shows perhaps the simplest way in which this action can be used. The following input computes the density of atoms at each point on the grid and ouptuts this quantity to a file. In other words this input instructs plumed to calculate  $\rho(\mathbf{r}) = \sum_i K(\mathbf{r} - \mathbf{r}_i)$ 

```
dens: DENSITY SPECIES=1-100
grid: MULTICOLVARDENS DATA=dens ORIGIN=1 DIR=xyz NBINS=100,100,100 BANDWIDTH=0.05,0.05,0.05 STRIDE=1
DUMPGRID GRID=grid STRIDE=500 FILE=density
```

In the above example density is added to the grid on every step. The PRINT\_GRID instruction thus tells PLUMED to output the average density at each point on the grid every 500 steps of simulation. Notice that the that grid output on step 1000 is an average over all 1000 frames of the trajectory. If you would like to analyse these two blocks of data separately you must use the CLEAR flag.

This second example computes an order parameter (in this case FCCUBIC) and constructs a phase field model for this order parameter using the equation above.

```
fcc: FCCUBIC SPECIES=1-5184 SWITCH={CUBIC D_0=1.2 D_MAX=1.5} ALPHA=27 dens: MULTICOLVARDENS DATA=fcc ORIGIN=1 DIR=xyz NBINS=14,14,28 BANDWIDTH=1.0,1.0,1.0 STRIDE=1 CLEAR=1 DUMPCUBE GRID=dens STRIDE=1 FILE=dens.cube
```

In this example the phase field model is computed and output to a file on every step of the simulation. Furthermore, because the CLEAR=1 keyword is set on the MULTICOLVARDENS line each Gaussian cube file output is a phase field model for a particular trajectory frame. The average value accumulated thus far is cleared at the start of every single timestep and there is no averaging over trajectory frames in this case.

### 6.17 CONVERT TO FES

Convert a histogram, H(x), to a free energy surface using  $F(x) = -k_BT \ln H(x)$ .

Compulsory keywords

| GRID the action that creates the input grid you would like to use |
|---|
|---|

| SERIAL        | ( default=off ) do the calculation in serial. Do not parallelize  |
|---------------|---|
| LOWMEM        | ( default=off ) lower the memory requirements   |
| TIMINGS       | ( default=off ) output information on the timings of the various parts of the calculation                             |
| CONCENTRATION | the concentration parameter for Von Mises-Fisher distributions  |
| COMPONENT     | if your input is a vector field use this to specify the component of the input vector field for which you wish to use |
| TEMP          | the temperature at which you are operating  |

Examples

# 6.18 DUMPCUBE

Output a three dimensional grid using the Gaussian cube file format.

Compulsory keywords

| GRID   | the action that creates the grid you would like to output  |
|--------|--|
| STRIDE | ( default=0 ) the frequency with which the grid should be output to the file. The default value of 0 |
|        | ensures that the grid is only output at the end of the trajectory                                    |
| FILE   | ( default=density ) the file on which to write the grid.   |

**Options** 

| FMT       | the format that should be used to output real numbers   |
|-----------|---|
| COMPONENT | if your input is a vector field use this to specifiy the component of the input vector field for which you wish to output |

Examples

# 6.19 DUMPGRID

Output the function on the grid to a file with the PLUMED grid format.

Compulsory keywords

| GRID   | the action that creates the grid you would like to output  |
|--------|--|
| STRIDE | ( default=0 ) the frequency with which the grid should be output to the file. The default value of 0 ensures that the grid is only output at the end of the trajectory |
| FILE   | ( default=density ) the file on which to write the grid.   |

# **Options**

| FMT | the format that should be used to output real numbers |
|-----|---|
|     |   |

Examples

# 6.20 FIND\_CONTOUR\_SURFACE

Find an isocontour by searching along either the x, y or direction.

# Compulsory keywords

| STRIDE    | ( default=1 ) the frequency with which the data should be collected and added to the quantity being averaged  |
|-----------|---|
| CLEAR     | ( default=0 ) the frequency with which to clear all the accumulated data. The default value of 0 implies that all the data will be used and that the grid will never be cleared |
| GRID      | the action that creates the input grid you would like to use  |
| CONTOUR   | the value we would like to draw the contour at in the space   |
| SEARCHDIR | In which directions do you wish to search for the contour.  |
| BUFFER    | ( default=0 ) number of buffer grid points around location where grid was found on last step. If this is zero the full grid is calculated on each step                          |

| SERIAL        | ( default=off ) do the calculation in serial. Do not parallelize   |
|---------------|--|
| LOWMEM        | ( default=off ) lower the memory requirements  |
| TIMINGS       | ( default=off ) output information on the timings of the various parts of the calculation                              |
| UNORMALIZED   | ( default=off ) output the unaveraged quantity/quantities.   |
| LOGWEIGHTS    | list of actions that calculates log weights that should be used to weight configurations when calculating averages     |
| CONCENTRATION | the concentration parameter for Von Mises-Fisher distributions   |
| COMPONENT     | if your input is a vector field use this to specifiy the component of the input vector field for which you wish to use |

Examples

# 6.21 FIND\_CONTOUR

Find an isocontour in a smooth function.

Compulsory keywords

| STRIDE  | ( default=1 ) the frequency with which the data should be collected and added to the quantity being averaged  |
|---------|---|
| CLEAR   | ( default=0 ) the frequency with which to clear all the accumulated data. The default value of 0 implies that all the data will be used and that the grid will never be cleared |
| GRID    | the action that creates the input grid you would like to use  |
| CONTOUR | the value we would like to draw the contour at in the space   |
| BUFFER  | ( default=0 ) number of buffer grid points around location where grid was found on last step. If this is zero the full grid is calculated on each step                          |
| FILE    | file on which to output coordinates   |
| UNITS   | ( default=PLUMED ) the units in which to print out the coordinates. PLUMED means internal PLUMED units  |

# Options

| SERIAL        | ( default=off ) do the calculation in serial. Do not parallelize   |
|---------------|--|
| LOWMEM        | ( default=off ) lower the memory requirements  |
| TIMINGS       | ( default=off ) output information on the timings of the various parts of the calculation                              |
| UNORMALIZED   | ( default=off ) output the unaveraged quantity/quantities.   |
| LOGWEIGHTS    | list of actions that calculates log weights that should be used to weight configurations when calculating averages     |
| CONCENTRATION | the concentration parameter for Von Mises-Fisher distributions   |
| COMPONENT     | if your input is a vector field use this to specifyy the component of the input vector field for which you wish to use |
| PRECISION     | The number of digits in trajectory file  |

Examples

# 6.22 FIND\_SPHERICAL\_CONTOUR

Find an isocontour in a three dimensional grid by searching over a Fibonacci sphere.

Compulsory keywords

| STRIDE       | ( default=1 ) the frequency with which the data should be collected and added to the quantity being averaged  |
|--------------|---|
| CLEAR        | ( default=0 ) the frequency with which to clear all the accumulated data. The default value of 0 implies that all the data will be used and that the grid will never be cleared |
| GRID         | the action that creates the input grid you would like to use  |
| CONTOUR      | the value we would like to draw the contour at in the space   |
| NPOINTS      | the number of points for which we are looking for the contour   |
| INNER_RADIUS | the minimum radius on which to look for the contour   |
| OUTER_RADIUS | the outer radius on which to look for the contour   |
| NBINS        | ( default=1 ) the number of discrete sections in which to divide the distance between the inner and outer radius when searching for a contour                                   |

### **Options**

| SERIAL        | ( default=off ) do the calculation in serial. Do not parallelize   |
|---------------|--|
| LOWMEM        | ( default=off ) lower the memory requirements  |
| TIMINGS       | ( default=off ) output information on the timings of the various parts of the calculation                              |
| UNORMALIZED   | ( default=off ) output the unaveraged quantity/quantities.   |
| LOGWEIGHTS    | list of actions that calculates log weights that should be used to weight configurations when calculating averages     |
| CONCENTRATION | the concentration parameter for Von Mises-Fisher distributions   |
| COMPONENT     | if your input is a vector field use this to specifiy the component of the input vector field for which you wish to use |

### **Examples**

# 6.23 FOURIER\_TRANSFORM

Compute the Discrete Fourier Transform (DFT) by means of FFTW of data stored on a 2D grid.

This action can operate on any other action that outputs scalar data on a two-dimensional grid.

Up to now, even if the input data are purely real the action uses a complex DFT.

Just as a quick reference, given a 1D array  ${\bf X}$  of size n, this action computes the vector  ${\bf Y}$  given by

$$Y_k = \sum_{j=0}^{n-1} X_j e^{2\pi jk\sqrt{-1}/n}.$$

This can be easily extended to more than one dimension. All the other details can be found at  $http://www. \leftarrow fftw.org/doc/What-FFTW-Really-Computes.html#What-FFTW-Really-Computes.$ 

The keyword "FOURIER\_PARAMETERS" deserves just a note on the usage. This keyword specifies how the Fourier transform will be normalized. The keyword takes two numerical parameters (  $a,\ b$ ) that define the normalization according to the following expression

$$\frac{1}{n^{(1-a)/2}} \sum_{j=0}^{n-1} X_j e^{2\pi b \, jk\sqrt{-1}/n}$$

The default values of these parameters are: a=1 and b=1.

### Compulsory keywords

| STRIDE             | ( default=1 ) the frequency with which the data should be collected and added to the quantity being averaged   |
|--------------------|--|
| CLEAR              | ( default=0 ) the frequency with which to clear all the accumulated data. The default value of 0 implies that all the data will be used and that the grid will never be cleared  |
| GRID               | the action that creates the input grid you would like to use   |
| FOURIER_PARAMETERS | ( default=default ) what kind of normalization is applied to the output and if the Fourier transform in FORWARD or BACKWARD. This keyword takes the form FOURIER_PARAMETERS=A,B, where A and B can be 0, 1 or -1. The default values are A=1 (no normalization at all) and B=1 (forward FFT). Other possible choices for A are: A=-1: normalize by the number of data, A=0: normalize by the square root of the number of data (one forward and followed by backward FFT recover the original data). |

### **Options**

| SERIAL        | ( default=off ) do the calculation in serial. Do not parallelize  |
|---------------|---|
| LOWMEM        | ( default=off ) lower the memory requirements   |
| TIMINGS       | ( default=off ) output information on the timings of the various parts of the calculation   |
| UNORMALIZED   | ( default=off ) output the unaveraged quantity/quantities.  |
| LOGWEIGHTS    | list of actions that calculates log weights that should be used to weight configurations when calculating averages  |
| CONCENTRATION | the concentration parameter for Von Mises-Fisher distributions  |
| COMPONENT     | if your input is a vector field use this to specifyy the component of the input vector field for which you wish to use  |
| FT_TYPE       | choose what kind of data you want as output on the grid. Possible values are: ABS = compute the complex modulus of Fourier coefficients (DEFAULT); NORM = compute the norm (i.e. ABS^2) of Fourier coefficients; COMPLEX = store the FFTW complex output on the grid (as a vector). |

## **Examples**

The following example tells Plumed to compute the complex 2D 'backward' Discrete Fourier Transform by taking the data saved on a grid called 'density', and normalizing the output by  $\frac{1}{\sqrt{N_x\,N_y}}$ , where  $N_x$  and  $N_y$  are the number of data on the grid (it can be the case that  $N_x \neq N_y$ ):

FOURIER\_TRANSFORM STRIDE=1 GRID=density FT\_TYPE=complex FOURIER\_PARAMETERS=0,-1 FILE=fourier.dat

# 6.24 GRID\_TO\_XYZ

Output the function on the grid to an xyz file

Compulsory keywords

| GRID   | the action that creates the grid you would like to output  |
|--------|--|
| STRIDE | ( default=0 ) the frequency with which the grid should be output to the file. The default value of 0 ensures that the grid is only output at the end of the trajectory |
| FILE   | ( default=density ) the file on which to write the grid.   |
| UNITS  | ( default=PLUMED ) the units in which to print out the coordinates. PLUMED means internal PLU← MED units   |

### **Options**

| COMPONENT | if your input is a vector field use this to specifiy the component of the input vector field for which you wish to output |
|-----------|---|
| PRECISION | The number of digits in trajectory file   |

### Examples

# 6.25 INTEGRATE\_GRID

Calculate the total integral of the function on the input grid

Compulsory keywords

| STRIDE | ( default=1 ) the frequency with which the data should be collected and added to the quantity being averaged |  |
|--------|--|--|
| GRID   | GRID the action that creates the input grid you would like to use  |  |
| CLEAR  | ( default=1 ) the frequency with which to clear all the accumulated data.                                    |  |

| SERIAL  | ( default=off ) do the calculation in serial. Do not parallelize                          |
|---------|---|
| LOWMEM  | ( default=off ) lower the memory requirements   |
| TIMINGS | ( default=off ) output information on the timings of the various parts of the calculation |

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| UNORMALIZED   | ( default=off ) output the unaveraged quantity/quantities.   |
|---------------|--|
| LOGWEIGHTS    | list of actions that calculates log weights that should be used to weight configurations when calculating averages     |
| CONCENTRATION | the concentration parameter for Von Mises-Fisher distributions   |
| COMPONENT     | if your input is a vector field use this to specifiy the component of the input vector field for which you wish to use |

Examples

# 6.26 INTERPOLATE\_GRID

Interpolate a smooth function stored on a grid onto a grid with a smaller grid spacing.

Compulsory keywords

| STRIDE | ( default=1 ) the frequency with which the data should be collected and added to the quantity being averaged  |
|--------|---|
| CLEAR  | ( default=0 ) the frequency with which to clear all the accumulated data. The default value of 0 implies that all the data will be used and that the grid will never be cleared |
| GRID   | the action that creates the input grid you would like to use  |

### **Options**

| SERIAL        | ( default=off ) do the calculation in serial. Do not parallelize  |
|---------------|---|
| LOWMEM        | ( default=off ) lower the memory requirements   |
| TIMINGS       | ( default=off ) output information on the timings of the various parts of the calculation                             |
| UNORMALIZED   | ( default=off ) output the unaveraged quantity/quantities.  |
| LOGWEIGHTS    | list of actions that calculates log weights that should be used to weight configurations when calculating averages    |
| CONCENTRATION | the concentration parameter for Von Mises-Fisher distributions  |
| COMPONENT     | if your input is a vector field use this to specify the component of the input vector field for which you wish to use |
| GRID_BIN      | the number of bins for the grid   |
| GRID_SPACING  | the approximate grid spacing (to be used as an alternative or together with GRID_BIN)                                 |

Examples

# 6.27 CLASSICAL\_MDS

This is part of the analysis module

Create a low-dimensional projection of a trajectory using the classical multidimensional scaling algorithm.

Multidimensional scaling (MDS) is similar to what is done when you make a map. You start with distances between London, Belfast, Paris and Dublin and then you try to arrange points on a piece of paper so that the (suitably scaled) distances between the points in your map representing each of those cities are related to the true distances between the cities. Stating this more mathematically MDS endeavors to find an <code>isometry</code> between points distributed in a high-dimensional space and a set of points distributed in a low-dimensional plane. In other words, if we have M D-dimensional points,  $\mathbf{X}$ , and we can calculate dissimilarities between pairs them,  $D_{ij}$ , we can, with an MDS calculation, try to create M projections,  $\mathbf{x}$ , of the high dimensionality points in a d-dimensional linear space by trying to arrange the projections so that the Euclidean distances between pairs of them,  $d_{ij}$ , resemble the dissimilarities between the high dimensional points. In short we minimize:

$$\chi^2 = \sum_{i \neq j} \left( D_{ij} - d_{ij} \right)^2$$

where  $D_{ij}$  is the distance between point  $X^i$  and point  $X^j$  and  $d_{ij}$  is the distance between the projection of  $X^i$ ,  $x^i$ , and the projection of  $X^j$ ,  $x^j$ . A tutorial on this approach can be used to analyse simulations can be found in the tutorial Belfast tutorial: Adaptive variables II and in the following short video.

The atoms involved can be specified using

| ATOMS | the atoms whose positions we are tracking for the purpose of analysing the data. For more information |  |
|-------|---|--|
|       | on how to specify lists of atoms see Groups and Virtual Atoms   |  |

Compulsory keywords

| STRIDE          | ( default=1 ) the frequency with which the data should be collected and added to the quantity being averaged  |
|-----------------|---|
| CLEAR           | ( default=0 ) the frequency with which to clear all the accumulated data. The default value of 0 implies that all the data will be used and that the grid will never be cleared |
| METRIC          | ( default=EUCLIDEAN ) how are we measuring the distances between configurations   |
| RUN             | ( default=0 ) the frequency with which to run the analysis algorithm. The default value of zero assumes you want to analyse the whole trajectory                                |
| LANDMARKS       | ( default=ALL ) only use a subset of the data that was collected. For more information on the landmark selection algorithms that are available in plumed see landmarkselection. |
| NLOW_DIM        | number of low-dimensional coordinates required  |
| OUTPUT_FILE     | file on which to output the final embedding coordinates   |
| EMBEDDING_OFILE | ( default=dont output ) file on which to output the embedding in plumed input format  |

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| SERIAL           | ( default=off ) do the calculation in serial. Do not parallelize  |
|------------------|---|
| LOWMEM           | ( default=off ) lower the memory requirements   |
| TIMINGS          | ( default=off ) output information on the timings of the various parts of the calculation   |
| UNORMALIZED      | ( default=off ) output the unaveraged quantity/quantities.  |
| WRITE_CHECKPOINT | ( default=off ) write out a checkpoint so that the analysis can be restarted in a later   |
|                  | run   |
| LOGWEIGHTS       | list of actions that calculates log weights that should be used to weight configurations  |
|                  | when calculating averages   |
| ARG              | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three components x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PL UMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |
| FMT              | the format that should be used in analysis output files   |
| RESTART          | allows per-action setting of restart (YES/NO/AUTO)  |
| UPDATE_FROM      | Only update this action from this time  |
| UPDATE_UNTIL     | Only update this action until this time   |

### **Examples**

The following command instructs plumed to construct a classical multidimensional scaling projection of a trajectory. The RMSD distance between atoms 1-256 have moved is used to measure the distances in the high-dimensional space.

```
CLASSICAL_MDS ...
ATOMS=1-256
METRIC=OPTIMAL-FAST
USE_ALL_DATA
NLOW_DIM=2
OUTPUT_FILE=rmsd-embed
... CLASSICAL_MDS
```

The following section is for people who are interested in how this method works in detail. A solid understanding of this material is not necessary to use MDS.

## 6.27.1 Method of optimisation

The stress function can be minimized using a standard optimization algorithm such as conjugate gradients or steepest descent. However, it is more common to do this minimization using a technique known as classical scaling. Classical scaling works by recognizing that each of the distances \$D\_{ij}\$ in the above sum can be written as:

$$D_{ij}^{2} = \sum_{\alpha} (X_{\alpha}^{i} - X_{\alpha}^{j})^{2} = \sum_{\alpha} (X_{\alpha}^{i})^{2} + (X_{\alpha}^{j})^{2} - 2X_{\alpha}^{i}X_{\alpha}^{j}$$

We can use this expression and matrix algebra to calculate multiple distances at once. For instance if we have three points, X, we can write distances between them as:

$$D^{2}(\mathbf{X}) = \begin{bmatrix} 0 & d_{12}^{2} & d_{13}^{2} \\ d_{12}^{2} & 0 & d_{23}^{2} \\ d_{13}^{2} & d_{23}^{2} & 0 \end{bmatrix}$$

$$= \sum_{\alpha} \begin{bmatrix} (X_{\alpha}^{1})^{2} & (X_{\alpha}^{1})^{2} & (X_{\alpha}^{1})^{2} \\ (X_{\alpha}^{2})^{2} & (X_{\alpha}^{2})^{2} & (X_{\alpha}^{2})^{2} \\ (X_{\alpha}^{2})^{2} & (X_{\alpha}^{2})^{2} & (X_{\alpha}^{2})^{2} \end{bmatrix} + \sum_{\alpha} \begin{bmatrix} (X_{\alpha}^{1})^{2} & (X_{\alpha}^{2})^{2} & (X_{\alpha}^{3})^{2} \\ (X_{\alpha}^{1})^{2} & (X_{\alpha}^{2})^{2} & (X_{\alpha}^{3})^{2} \end{bmatrix} - 2 \sum_{\alpha} \begin{bmatrix} X_{\alpha}^{1} X_{\alpha}^{1} & X_{\alpha}^{1} X_{\alpha}^{2} & X_{\alpha}^{1} X_{\alpha}^{3} \\ X_{\alpha}^{2} X_{\alpha}^{1} & X_{\alpha}^{2} X_{\alpha}^{2} & X_{\alpha}^{2} X_{\alpha}^{3} \\ X_{\alpha}^{1} X_{\alpha}^{1} & X_{\alpha}^{2} X_{\alpha}^{2} & X_{\alpha}^{2} X_{\alpha}^{3} \end{bmatrix}$$

$$= \mathbf{c} \mathbf{1}^{\mathbf{T}} + \mathbf{1} \mathbf{c}^{\mathbf{T}} - 2 \sum_{\alpha} \mathbf{x}_{\alpha} \mathbf{x}_{\alpha}^{T} = \mathbf{c} \mathbf{1}^{\mathbf{T}} + \mathbf{1} \mathbf{c}^{\mathbf{T}} - 2 \mathbf{X} \mathbf{X}^{\mathbf{T}}$$

This last equation can be extended to situations when we have more than three points. In it  $\mathbf{X}$  is a matrix that has one high-dimensional point on each of its rows and  $\mathbf{X}^T$  is its transpose. 1 is an  $M \times 1$  vector of ones and  $\mathbf{c}$  is a vector with components given by:

$$c_i = \sum_{\alpha} (x_{\alpha}^i)^2$$

These quantities are the diagonal elements of  $XX^T$ , which is a dot product or Gram Matrix that contains the dot product of the vector  $X_i$  with the vector  $X_j$  in element i, j.

In classical scaling we introduce a centering matrix J that is given by:

$$\mathbf{J} = \mathbf{I} - \frac{1}{M} \mathbf{1} \mathbf{1}^{\mathbf{T}}$$

where I is the identity. Multiplying the equations above from the front and back by this matrix and a factor of a  $-\frac{1}{2}$  gives:

$$\begin{aligned} -\frac{1}{2}\mathbf{J}\mathbf{D}^{2}(\mathbf{X})\mathbf{J} &= -\frac{1}{2}\mathbf{J}(\mathbf{c}\mathbf{1}^{\mathbf{T}} + \mathbf{1}\mathbf{c}^{\mathbf{T}} - 2\mathbf{X}\mathbf{X}^{\mathbf{T}})\mathbf{J} \\ &= -\frac{1}{2}\mathbf{J}\mathbf{c}\mathbf{1}^{\mathbf{T}}\mathbf{J} - \frac{1}{2}\mathbf{J}\mathbf{1}\mathbf{c}^{\mathbf{T}}\mathbf{J} + \frac{1}{2}\mathbf{J}(2\mathbf{X}\mathbf{X}^{\mathbf{T}})\mathbf{J} \\ &= \mathbf{J}\mathbf{X}\mathbf{X}^{\mathbf{T}}\mathbf{J} = \mathbf{X}\mathbf{X}^{\mathbf{T}} \end{aligned}$$

The fist two terms in this expression disappear because  $\mathbf{1}^T\mathbf{J} = \mathbf{J}\mathbf{1} = \mathbf{0}$ , where  $\mathbf{0}$  is a matrix containing all zeros. In the final step meanwhile we use the fact that the matrix of squared distances will not change when we translate all the points. We can thus assume that the mean value,  $\mu$ , for each of the components,  $\alpha$ :

$$\mu_{\alpha} = \frac{1}{M} \sum_{i=1}^{N} \mathbf{X}_{\alpha}^{i}$$

is equal to 0 so the columns of X add up to 0. This in turn means that each of the columns of  $XX^T$  adds up to zero, which is what allows us to write  $JXX^TJ = XX^T$ .

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The matrix of squared distances is symmetric and positive-definite we can thus use the spectral decomposition to decompose it as:

$$\Phi = \mathbf{V}\Lambda\mathbf{V}^T$$

Furthermore, because the matrix we are diagonalizing,  $\mathbf{X}\mathbf{X}^{\mathbf{T}}$ , is the product of a matrix and its transpose we can use this decomposition to write:

$$\mathbf{X} = \mathbf{V} \Lambda^{\frac{1}{2}}$$

Much as in PCA there are generally a small number of large eigenvalues in  $\Lambda$  and many small eigenvalues. We can safely use only the large eigenvalues and their corresponding eigenvectors to express the relationship between the coordinates X. This gives us our set of low-dimensional projections.

This derivation makes a number of assumptions about the how the low dimensional points should best be arranged to minimise the stress. If you use an interative optimization algorithm such as SMACOF you may thus be able to find a better (lower-stress) projection of the points. For more details on the assumptions made see this website.

### 6.28 PCA

This is part of the analysis module

Perform principal component analysis (PCA) using either the positions of the atoms a large number of collective variables as input.

Principal component analysis is a statistical technique that uses an orthogonal transformation to convert a set of observations of poorly correlated variables into a set of linearly uncorrelated variables. You can read more about the specifics of this technique here: https://en.wikipedia.org/wiki/Principal\_component\_canalysis

When used with molecular dynamics simulations a set of frames taken from the trajectory,  $\{X_i\}$ , or the values of a number of collective variables which are calculated from the trajectory frames are used as input. In this second instance your input to the PCA analysis algorithm is thus a set of high-dimensional vectors of collective variables. However, if collective variables are calculated from the positions of the atoms or if the positions are used directly the assumption is that this input trajectory is a set of poorly correlated (high-dimensional) vectors. After principal component analysis has been performed the output is a set of orthogonal vectors that describe the directions in which the largest motions have been seen. In other words, principal component analysis provides a method for lowering the dimensionality of the data contained in a trajectory. These output directions are some linear combination of the x, y and z positions if the positions were used as input or some linear combination of the input collective variables if a high-dimensional vector of collective variables was used as input.

As explained on the Wikipedia page you must calculate the average and covariance for each of the input coordinates. In other words, you must calculate the average structure and the amount the system fluctuates around this average structure. The problem in doing so when the  $x,\,y$  and z coordinates of a molecule are used as input is that the majority of the changes in the positions of the atoms comes from the translational and rotational degrees of freedom of the molecule. The first six principal components will thus, most likely, be uninteresting. Consequently, to remedy this problem PLUMED provides the functionality to perform an RMSD alignment of the all the structures to be analysed to the first frame in the trajectory. This can be used to effectively remove translational and/or rotational motions from consideration. The resulting principal components thus describe vibrational motions of the molecule.

If you wish to calculate the projection of a trajectory on a set of principal components calculated from this PCA action then the output can be used as input for the PCAVARS action.

The atoms involved can be specified using

| ATOMS | the atoms whose positions we are tracking for the purpose of analysing the data. For more information |
|-------|---|
|       | on how to specify lists of atoms see Groups and Virtual Atoms   |

# Compulsory keywords

| STRIDE   | ( default=1 ) the frequency with which the data should be collected and added to the quantity being averaged  |  |
|----------|---|--|
| CLEAR    | ( default=0 ) the frequency with which to clear all the accumulated data. The default value of 0 implies that all the data will be used and that the grid will never be cleared |  |
| METRIC   | ( default=EUCLIDEAN ) how are we measuring the distances between configurations   |  |
| RUN      | ( default=0 ) the frequency with which to run the analysis algorithm. The default value of zero assumes you want to analyse the whole trajectory                                |  |
| NLOW_DIM | number of PCA coordinates required  |  |
| OFILE    | the file on which to output the eigenvectors  |  |

| SERIAL           | ( default=off ) do the calculation in serial. Do not parallelize   |
|------------------|--|
| LOWMEM           | ( default=off ) lower the memory requirements  |
| TIMINGS          | ( default=off ) output information on the timings of the various parts of the calculation  |
| UNORMALIZED      | ( default=off ) output the unaveraged quantity/quantities.   |
| WRITE_CHECKPOINT | ( default=off ) write out a checkpoint so that the analysis can be restarted in a later run  |
| LOGWEIGHTS       | list of actions that calculates log weights that should be used to weight configurations when calculating averages   |
| ARG              | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PL UMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |
| FMT              | the format that should be used in analysis output files  |
| RESTART          | allows per-action setting of restart (YES/NO/AUTO)   |
| UPDATE_FROM      | Only update this action from this time   |
| UPDATE_UNTIL     | Only update this action until this time  |

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### **Examples**

The following input instructs PLUMED to perform a principal component analysis in which the covariance matrix is calculated from changes in the positions of the first 22 atoms. The TYPE=OPTIMAL instruction ensures that translational and rotational degrees of freedom are removed from consideration. The first two principal components will be output to a file called pca-comp.pdb. Trajectory frames will be collected on every step and the PCA calculation will be performed at the end of the simulation.

```
PCA METRIC=OPTIMAL ATOMS=1-22 STRIDE=1 USE_ALL_DATA NLOW_DIM=2 OFILE=pca-comp.pdb
```

The following input instructs PLUMED to perform a principal component analysis in which the covariance matrix is calculated from chnages in the six distances seen in the previous lines. Notice that here the TYPE=EUCLID ← EAN keyword is used to indicate that no alighment has to be done when calculating the various elements of the covariance matrix from the input vectors. In this calculation the first two principal components will be output to a file called pca-comp.pdb. Trajectory frames will be collected every five steps and the PCA calculation is performed every 1000 steps. Consequently, if you run a 2000 step simulation the PCA analysis will be performed twice. The REWE ← IGHT\_BIAS keyword in this input tells PLUMED that rather that ascribing a weight of one to each of the frames when calculating averages and covariances a reweighting should be performed based and each frames' weight in these calculations should be determined based on the current value of the instantaneous bias (see REWEIGHT\_BIAS).

```
d1: DISTANCE ATOMS=1,2
d2: DISTANCE ATOMS=1,3
d3: DISTANCE ATOMS=1,4
d4: DISTANCE ATOMS=2,3
d5: DISTANCE ATOMS=2,4
d6: DISTANCE ATOMS=3,4

PCA ARG=d1,d2,d3,d4,d5,d6 METRIC=EUCLIDEAN STRIDE=5 RUN=1000 NLOW_DIM=2 REWEIGHT_BIAS OFILE=pca-comp.pdb
```

# **Chapter 7**

# **Bias**

PLUMED allows you to run a number of enhanced sampling algorithms. The list of enhanced sampling algorithms contained in PLUMED is as follows:

| ABMD                | Adds a ratchet-and-pawl like restraint on one or more variables.   |
|---------------------|--|
| BIASVALUE           | Takes the value of one variable and use it as a bias   |
| EXTENDED_LAGRANGIAN | Add extended Lagrangian.   |
| EXTERNAL            | Calculate a restraint that is defined on a grid that is read during start up   |
| LOWER_WALLS         | Defines a wall for the value of one or more collective variables, which limits the region of the phase space accessible during the simulation. |
| METAD               | Used to performed MetaDynamics on one or more collective variables.  |
| METAINFERENCE       | Calculate the Metainference Score for a set of back calculated experimental data.  |
| MOVINGRESTRAINT     | Add a time-dependent, harmonic restraint on one or more variables.   |
| PBMETAD             | Used to performed Parallel Bias MetaDynamics.  |
| RESTRAINT           | Adds harmonic and/or linear restraints on one or more variables.   |
| UPPER_WALLS         | Defines a wall for the value of one or more collective variables, which limits the region of the phase space accessible during the simulation. |

Methods, such as METAD or PBMETAD, that work by introducing a history dependent bias can be restarted using the RESTART keyword

## **7.1 ABMD**

This is part of the bias module

Adds a ratchet-and-pawl like restraint on one or more variables.

This action can be used to evolve a system towards a target value in CV space using an harmonic potential moving with the thermal fluctuations of the CV ? ??. The biasing potential in this method is as follows:

$$V(\rho(t)) = \begin{cases} \frac{K}{2} \left( \rho(t) - \rho_m(t) \right)^2, & \rho(t) > \rho_m(t) \\ 0, & \rho(t) \le \rho_m(t), \end{cases}$$

where

$$\rho(t) = \left(CV(t) - TO\right)^2$$

and

$$\rho_m(t) = \min_{0 < \tau < t} \rho(\tau) + \eta(t).$$

The method is based on the introduction of a biasing potential which is zero when the system is moving towards the desired arrival point and which damps the fluctuations when the system attempts to move in the opposite direction. As in the case of the ratchet and pawl system, propelled by thermal motion of the solvent molecules, the biasing potential does not exert work on the system.  $\eta(t)$  is an additional white noise acting on the minimum position of the bias.

**Description of components** 

By default this Action calculates the following quantities. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Description   |
|----------|---|
| bias     | the instantaneous value of the bias potential   |
| force2   | the instantaneous value of the squared force due to this bias potential   |
| _min     | one or multiple instances of this quantity will be refereceable elsewhere in the input file. These quantities will be named with the arguments of the bias followed by the character string _min. These quantities tell the user the minimum value assumed by rho_m(t). |

### Compulsory keywords

| то    | The array of target values    |
|-------|-------------------------------|
| KAPPA | The array of force constants. |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| ARG                   | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |

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| MIN   | Array of starting values for the bias (set rho_m(t), otherwise it is set using the current value of ARG) |
|-------|--|
| NOISE | Array of white noise intensities (add a temperature to the ABMD)   |
| SEED  | Array of seeds for the white noise (add a temperature to the ABMD)                                       |

### **Examples**

The following input sets up two biases, one on the distance between atoms 3 and 5 and another on the distance between atoms 2 and 4. The two target values are defined using TO and the two strength using KAPPA. The total energy of the bias is printed.

```
DISTANCE ATOMS=3,5 LABEL=d1
DISTANCE ATOMS=2,4 LABEL=d2
ABMD ARG=d1,d2 TO=1.0,1.5 KAPPA=5.0,5.0 LABEL=abmd
PRINT ARG=abmd.bias,abmd.d1_min,abmd.d2_min
```

(See also DISTANCE and PRINT).

### 7.2 BIASVALUE

Takes the value of one variable and use it as a bias

This is the simplest possible bias: the bias potential is equal to a collective variable. It is useful to create custom biasing potential, e.g. applying a function (see Functions) to some collective variable then using the value of this function directly as a bias.

**Description of components** 

By default this Action calculates the following quantities. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Description   |
|----------|---|
| bias     | the instantaneous value of the bias potential   |
| _bias    | one or multiple instances of this quantity will be refereceable elsewhere in the input file. these quantities will named with the arguments of the bias followed by the character string _bias. These quantities tell the user how much the bias is due to each of the colvars. |

| NUMERICAL DERIVATIVES | ( default, off ) calculate the derivatives for those quantities numerically |
|-----------------------|---|
| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|                       |   |

#### **ARG**

the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If \* or \*.\* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.\*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3...

### **Examples**

The following input tells plumed to use the value of the distance between atoms 3 and 5 and the value of the distance between atoms 2 and 4 as biases. It then tells plumed to print the energy of the restraint

```
DISTANCE ATOMS=3,5 LABEL=d1
DISTANCE ATOMS=3,6 LABEL=d2
BIASVALUE ARG=d1,d2 LABEL=b
PRINT ARG=d1,d2,b.d1,b.d2
```

(See also DISTANCE and PRINT).

Another thing one can do is asking one system to follow a circle in sin/cos according a time dependence

```
t: TIME
# this just print cos and sin of time
cos: MATHEVAL ARG=t VAR=t FUNC=cos(t) PERIODIC=NO
sin: MATHEVAL ARG=t VAR=t FUNC=sin(t) PERIODIC=NO
c1: COM ATOMS=1.2
c2: COM ATOMS=3,4
d: DISTANCE COMPONENTS ATOMS=c1.c2
PRINT ARG=t,cos,sin,d.x,d.y,d.z STRIDE=1 FILE=colvar FMT=%8.4f
# this calculates sine and cosine of a projected component of distance
# this creates a moving spring so that the system follows a circle-like dynamics
# but it is not a bias, it is a simple value now
vv1: MATHEVAL ARG=mycos, mysin, cos, sin VAR=mc, ms, c, s FUNC=100*((mc-c)^2+(ms-s)^2) PERIODIC=NO
# this takes the value calculated with matheval and uses as a bias
cc: BIASVALUE ARG=vv1
# some printout
PRINT ARG=t,cos,sin,d.x,d.y,d.z,mycos,mysin,cc.bias.vv1 STRIDE=1 FILE=colvar FMT=%8.4f
```

(see also TIME, MATHEVAL, COM, DISTANCE, and PRINT).

## 7.3 EXTENDED\_LAGRANGIAN

Add extended Lagrangian.

This action can be used to create fictitious collective variables coupled to the real ones. Given  $x_i$  the i-th argument of this bias potential, potential and kinetic contributions are added to the energy of the system as

$$V = \sum_{i} \frac{k_i}{2} (x_i - s_i)^2 + \sum_{i} \frac{\dot{s}_i^2}{2m_i}$$

.

The resulting potential is thus similar to a RESTRAINT, but the restraint center moved with time following Hamiltonian dynamics with mass  $m_i$ .

This bias potential accepts thus vectorial keywords (one element per argument) to define the coupling constant (KAPPA) and a relaxation time tau (TAU). The mass is them computed as  $m=k(\frac{\tau}{2\pi})^2$ .

Notice that this action creates several components. The ones named XX\_fict are the fictitious coordinates. It is possible to add further forces on them by means of other bias potential, e.g. to obtain an indirect METAD as in ? . Also notice that the velocities of the fictitious coordinates are reported (XX\_vfict). However, printed velocities are the ones at the previous step.

It is also possible to provide a non-zero friction (one value per component). This is then used to implement a Langevin thermostat, so as to implement TAMD/dAFED method ? ? . Notice that here a massive Langevin thermostat is used, whereas usually TAMD employs an overamped Langevin dynamics and dAFED a Gaussian thermostat.

### Warning

The bias potential is reported in the component bias. Notice that this bias potential, although formally compatible with replica exchange framework, probably does not work as expected in that case. Indeed, since fictitious coordinates are not swapped upon exchange, acceptace can be expected to be extremely low unless (by chance) two neighboring replicas have the fictitious variables located properly in space.

RESTART is not properly supported by this action. Indeed, at every start the postion of the fictitious variable is reset to the value of the real variable, and its velocity is set to zero. This is not expected to introduce big errors, but certainly is introducing a small inconsistency between a single long run and many shorter runs.

**Description of components** 

By default this Action calculates the following quantities. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Description  |
|----------|--|
| bias     | the instantaneous value of the bias potential  |
| _fict    | one or multiple instances of this quantity will be refereceable elsewhere in the input file. These quantities will named with the arguments of the bias followed by the character string _tilde. It is possible to add forces on these variable.     |
| _vfict   | one or multiple instances of this quantity will be refereceable elsewhere in the input file. These quantities will named with the arguments of the bias followed by the character string _tilde. It is NOT possible to add forces on these variable. |

### Compulsory keywords

| KAPPA    | specifies that the restraint is harmonic and what the values of the force constants on each of the |
|----------|--|
|          | variables are  |
| TAU      | specifies that the restraint is harmonic and what the values of the force constants on each of the |
|          | variables are  |
| FRICTION | ( default=0.0 ) add a friction to the variable   |

### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| ARG                   | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |
| TEMP                  | the system temperature - needed when FRICTION is present. If not provided will be taken from MD code (if available)   |

#### **Examples**

The following input tells plumed to perform a metadynamics with an extended Lagrangian on two torsional angles.

```
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
ex: EXTENDED_LAGRANGIAN ARG=phi,psi KAPPA=20,20.0 TAU=0.1,0.1
METAD ARG=ex.phi_fict,ex.psi_fict PACE=100 SIGMA=0.35,0.35 HEIGHT=0.1
# monitor the two variables
PRINT STRIDE=10 ARG=phi,psi,ex.phi_fict,ex.psi_fict FILE=COLVAR
```

### (See also TORSION, METAD, and PRINT).

The following input tells plumed to perform a TAMD (or dAFED) calculation on two torsional angles, keeping the two variables at a fictitious temperature of 3000K with a Langevin thermostat with friction 10

```
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
ex: EXTENDED_LAGRANGIAN ARG=phi,psi KAPPA=20,20.0 TAU=0.1,0.1 FRICTION=10,10 TEMP=3000
# monitor the two variables
PRINT STRIDE=10 ARG=phi,psi,ex.phi_fict,ex.psi_fict FILE=COLVAR
```

## (See also TORSION and PRINT)

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# 7.4 EXTERNAL

This is part of the bias module

Calculate a restraint that is defined on a grid that is read during start up

**Description of components** 

By default this Action calculates the following quantities. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Description                                   |  |
|----------|---|--|
| bias     | the instantaneous value of the bias potential |  |

### Compulsory keywords

| FILE | the name of the file containing the external potential. |
|------|---|
|------|---|

## **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| NOSPLINE              | ( default=off ) specifies that no spline interpolation is to be used when calculating the energy and forces due to the external potential   |
| SPARSE                | ( default=off ) specifies that the external potential uses a sparse grid  |
| ARG                   | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |

# **Examples**

The following is an input for a calculation with an external potential that is defined in the file bias.dat and that acts on the distance between atoms 3 and 5.

```
DISTANCE ATOMS=3,5 LABEL=d1
EXTERNAL ARG=d1 FILE=bias.dat LABEL=external
(See also DISTANCE PRINT).
```

The header in the file bias.dat should read:

```
#! FIELDS d1 external.bias der_d1
#! SET min_d1 0.0
#! SET max_d1 1.0
#! SET nbins_d1 100
#! SET periodic_d1 false
```

This should then be followed by the value of the potential and its derivative at 100 equally spaced points along the distance between 0 and 1. If you run with NOSPLINE you do not need to provide derivative information.

You can also include grids that are a function of more than one collective variable. For instance the following would be the input for an external potential acting on two torsional angles:

```
TORSION ATOMS=4,5,6,7 LABEL=t1
TORSION ATOMS=6,7,8,9 LABEL=t2
EXTERNAL ARG=t1,t2 FILE=bias.dat LABEL=ext
```

The header in the file bias.dat for this calculation would read:

```
#! FIELDS t1 t2 ext.bias der_t1 der_t2
#! SET min_t1 -pi
#! SET max_t1 +pi
#! SET nbins_t1 100
#! SET periodic_t1 true
#! SET min_t2 -pi
#! SET max_t2 +pi
#! SET nbins_t2 100
#! SET periodic_t2 true
```

This would be then followed by 100 blocks of data. In the first block of data the value of t1 (the value in the first column) is kept fixed and the value of the function is given at 100 equally spaced values for t2 between -pi and +pi. In the second block of data t1 is fixed at  $-pi+\frac{2pi}{100}$  and the value of the function is given at 100 equally spaced values for t2 between -pi and +pi. In the third block of data the same is done but t1 is fixed at  $-pi+\frac{4pi}{100}$  and so on untill you get to the 100th block of data where t1 is fixed at +pi.

Please note the order that the order of arguments in the plumed.dat file must be the same as the order of arguments in the header of the grid file.

### 7.5 LOWER WALLS

This is part of the bias module

Defines a wall for the value of one or more collective variables, which limits the region of the phase space accessible during the simulation.

The restraining potential starts acting on the system when the value of the CV is greater (in the case of UPPER—WALLS) or lower (in the case of LOWER\_WALLS) than a certain limit  $a_i$  (AT) minus an offset  $o_i$  (OFFSET). The expression for the bias due to the wall is given by:

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$$\sum_{i} k_i ((x_i - a_i + o_i)/s_i)_i^e$$

 $k_i$  (KAPPA) is an energy constant in internal unit of the code,  $s_i$  (EPS) a rescaling factor and  $e_i$  (EXP) the exponent determining the power law. By default: EXP = 2, EPS = 1.0, OFFSET = 0.

**Description of components** 

By default this Action calculates the following quantities. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Description  |  |
|----------|--|--|
| bias     | the instantaneous value of the bias potential                                  |  |
| force2   | force2 the instantaneous value of the squared force due to this bias potential |  |

### Compulsory keywords

| AT     | the positions of the wall. The a_i in the expression for a wall.                            |  |
|--------|---|--|
| KAPPA  | the force constant for the wall. The k_i in the expression for a wall.                      |  |
| OFFSET | ( default=0.0 ) the offset for the start of the wall. The o_i in the expression for a wall. |  |
| EXP    | P (default=2.0) the powers for the walls. The e_i in the expression for a wall.             |  |
| EPS    | ( default=1.0 ) the values for s_i in the expression for a wall                             |  |

### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| ARG                   | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |

### **Examples**

The following input tells plumed to add both a lower and an upper walls on the distance between atoms 3 and 5 and the distance between atoms 2 and 4. The lower and upper limits are defined at different values. The strength of the walls is the same for the four cases. It also tells plumed to print the energy of the walls.

```
DISTANCE ATOMS=3,5 LABEL=d1
DISTANCE ATOMS=2,4 LABEL=d2
UPPER_WALLS ARG=d1,d2 AT=1.0,1.5 KAPPA=150.0,150.0 EXP=2,2 EPS=1,1 OFFSET=0,0 LABEL=uwall
LOWER_WALLS ARG=d1,d2 AT=0.0,1.0 KAPPA=150.0,150.0 EXP=2,2 EPS=1,1 OFFSET=0,0 LABEL=lwall
PRINT ARG=uwall.bias,lwall.bias
```

(See also DISTANCE and PRINT).

### 7.6 METAD

This is part of the bias module

Used to performed MetaDynamics on one or more collective variables.

In a metadynamics simulations a history dependent bias composed of intermittently added Gaussian functions is added to the potential ?.

$$V(\vec{s}, t) = \sum_{k\tau < t} W(k\tau) \exp\left(-\sum_{i=1}^{d} \frac{(s_i - s_i^{(0)}(k\tau))^2}{2\sigma_i^2}\right).$$

This potential forces the system away from the kinetic traps in the potential energy surface and out into the unexplored parts of the energy landscape. Information on the Gaussian functions from which this potential is composed is output to a file called HILLS, which is used both the restart the calculation and to reconstruct the free energy as a function of the CVs. The free energy can be reconstructed from a metadynamics calculation because the final bias is given by:

$$V(\vec{s}) = -F(\vec{(s)})$$

During post processing the free energy can be calculated in this way using the sum\_hills utility.

In the simplest possible implementation of a metadynamics calculation the expense of a metadynamics calculation increases with the length of the simulation as one has to, at every step, evaluate the values of a larger and larger number of Gaussians. To avoid this issue you can store the bias on a grid. This approach is similar to that proposed in ? but has the advantage that the grid spacing is independent on the Gaussian width. Notice that you should provide either the number of bins for every collective variable (GRID\_BIN) or the desired grid spacing (GRID\_SP ACING). In case you provide both PLUMED will use the most conservative choice (highest number of bins) for each dimension. In case you do not provide any information about bin size (neither GRID\_BIN nor GRID\_SPACING) and if Gaussian width is fixed PLUMED will use 1/5 of the Gaussian width as grid spacing. This default choice should be reasonable for most applications.

Metadynamics can be restarted either from a HILLS file as well as from a GRID, in this second case one can first save a GRID using GRID\_WFILE (and GRID\_WSTRIDE) and at a later stage read it using GRID\_RFILE.

Another option that is available in plumed is well-tempered metadynamics?. In this varient of metadynamics the heights of the Gaussian hills are rescaled at each step so the bias is now given by:

$$V(s,t) = \sum_{t'=0,\tau_G,2\tau_G,...}^{t' < t} W e^{-V(s(q(t'),t')/\Delta T)} \exp\left(-\sum_{i=1}^{d} \frac{(s_i(q) - s_i(q(t'))^2}{2\sigma_i^2}\right),$$

This method ensures that the bias converges more smoothly. It should be noted that, in the case of well-tempered metadynamics, in the output printed the Gaussian height is re-scaled using the bias factor. Also notice that with

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well-tempered metadynamics the HILLS file does not contain the bias, but the negative of the free-energy estimate. This choice has the advantage that one can restart a simulation using a different value for the  $\Delta T$ . The applied bias will be scaled accordingly.

Note that you can use here also the flexible gaussian approach? in which you can adapt the gaussian to the extent of Cartesian space covered by a variable or to the space in collective variable covered in a given time. In this case the width of the deposited gaussian potential is denoted by one value only that is a Cartesian space (ADAPT  $\leftarrow$  IVE=GEOM) or a time (ADAPTIVE=DIFF). Note that a specific integration technique for the deposited gaussians should be used in this case. Check the documentation for utility sum\_hills.

With the keyword INTERVAL one changes the metadynamics algorithm setting the bias force equal to zero outside boundary ?. If, for example, metadynamics is performed on a CV s and one is interested only to the free energy for s > sw, the history dependent potential is still updated according to the above equations but the metadynamics force is set to zero for s < sw. Notice that Gaussians are added also if s < sw, as the tails of these Gaussians influence VG in the relevant region s > sw. In this way, the force on the system in the region s > sw comes from both metadynamics and the force field, in the region s < sw only from the latter. This approach allows obtaining a history-dependent bias potential VG that fluctuates around a stable estimator, equal to the negative of the free energy far enough from the boundaries. Note that:

- · It works only for one-dimensional biases;
- · It works both with and without GRID;
- The interval limit sw in a region where the free energy derivative is not large;
- If in the region outside the limit sw the system has a free energy minimum, the INTERVAL keyword should be used together with a UPPER\_WALLS or LOWER\_WALLS at sw.

As a final note, since version 2.0.2 when the system is outside of the selected interval the force is set to zero and the bias value to the value at the corresponding boundary. This allows acceptances for replica exchange methods to be computed correctly.

Multiple walkers ? can also be used. See below the examples.

The c(t) reweighting factor can also be calculated on the fly using the equations presented in ?. The expression used to calculate c(t) follows directly from using Eq. 12 in Eq. 3 in ? and gives smoother results than equivalent Eqs. 13 and Eqs. 14 in that paper. The c(t) is given by the rct component while the bias normalized by c(t) is given by the rbias component (rbias=bias-ct) which can be used to obtain a reweighted histogram. The calculation of c(t) is enabled by using the keyword REWEIGHTING\_NGRID where the grid used for the calculation is specified. This grid should have a size that is equal or larger than the grid given in GRID\_BIN./ By default c(t) is updated every 50 Gaussian hills but this can be changed by using the REWEIGHTING\_NHILLS keyword. This option can only be employed together with Well-Tempered Metadynamics and requires that a grid is used.

Additional material and examples can be also found in the tutorials:

- · Belfast tutorial: Metadynamics
- · Belfast tutorial: Replica exchange I
- Belfast tutorial: Replica exchange II and Multiple walkers

Notice that at variance with PLUMED 1.3 it is now straightforward to apply concurrent metadynamics as done e.g. in Ref. ? . This indeed can be obtained by using the METAD action multiple times in the same input file.

**Description of components** 

By default this Action calculates the following quantities. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Description                                   |
|----------|---|
| bias     | the instantaneous value of the bias potential |
| work     | accumulator for work                          |

In addition the following quantities can be calculated by employing the keywords listed below

| Quantity | Keyword           | Description  |
|----------|-------------------|--|
| rbias    | REWEIGHTING_NGRID | the instantaneous value of the bias normalized using the $c(t)$ reweighting factor [rbias=bias-c(t)]. This component can be used to obtain a reweighted histogram. |
| rct      | REWEIGHTING_NGRID | the reweighting factor $c(t)$ .  |
| acc      | ACCELERATION      | the metadynamics acceleration factor   |

# Compulsory keywords

| SIGMA | SIGMA the widths of the Gaussian hills                              |  |
|-------|---|--|
| PACE  | the frequency for hill addition                                     |  |
| FILE  | ( default=HILLS ) a file in which the list of added hills is stored |  |

| NUMERICAL DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically          |
|-----------------------|---|
|                       | , , ,   |
| GRID_SPARSE           | ( default=off ) use a sparse grid to store hills                                    |
| GRID_NOSPLINE         | ( default=off ) don't use spline interpolation with grids                           |
| STORE_GRIDS           | ( default=off ) store all the grid files the calculation generates. They will be    |
|                       | deleted if this keyword is not present  |
| WALKERS_MPI           | ( default=off ) Switch on MPI version of multiple walkers - not compatible with     |
|                       | other WALKERS_* options   |
| ACCELERATION          | ( default=off ) Set to TRUE if you want to compute the metadynamics acceler-        |
|                       | ation factor.   |
|                       |   |
| ARG                   | the input for this action is the scalar output from one or more other actions. The  |
|                       | particular scalars that you will use are referenced using the label of the action.  |
|                       | If the label appears on its own then it is assumed that the Action calculates a     |
|                       | single scalar value. The value of this scalar is thus used as the input to this new |
|                       | action. If * or *.* appears the scalars calculated by all the proceding actions     |
|                       | in the input file are taken. Some actions have multi-component outputs and          |
|                       | each component of the output has a specific label. For example a DISTANCE           |
|                       | action labelled dist may have three componets x, y and z. To take just the x        |
|                       | component you should use dist.x, if you wish to take all three components then      |
|                       | use dist.*.More information on the referencing of Actions can be found in the       |
|                       | section of the manual on the PLUMED Getting started. Scalar values can also         |
|                       | be referenced using POSIX regular expressions as detailed in the section on         |
|                       | Regular Expressions. To use this feature you you must compile PLUMED with           |
|                       | the appropriate flag. You can use multiple instances of this keyword i.e. ARG1,     |
|                       | ARG2, ARG3  |
| HEIGHT                | the heights of the Gaussian hills. Compulsory unless TAU and either BIASF↔          |
|                       | ACTOR or DAMPFACTOR are given   |

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| FMT                | specify format for HILLS files (useful for decrease the number of digits in regtests)  |
|--------------------|--|
| BIASFACTOR         | use well tempered metadynamics and use this biasfactor. Please note you must also specify temp   |
| DAMPFACTOR         | damp hills with exp(-max(V)/(kbT*DAMPFACTOR)   |
| TARGET             | target to a predefined distribution  |
| ТЕМР               | the system temperature - this is only needed if you are doing well-tempered metadynamics   |
| TAU                | in well tempered metadynamics, sets height to (kb*DeltaT*pace*timestep)/tau  |
| GRID_MIN           | the lower bounds for the grid  |
| GRID_MAX           | the upper bounds for the grid  |
| GRID_BIN           | the number of bins for the grid  |
| GRID_SPACING       | the approximate grid spacing (to be used as an alternative or together with GRID_BIN)  |
| REWEIGHTING_NGRID  | calculate the c(t) reweighting factor and use that to obtain the normalized bias [rbias=bias-c(t)]. Here you should specify the number of grid points required in each dimension. The number of grid points should be equal or larger to the number of grid points given in GRID_BIN. This method is not compatible with metadynamics not on a grid. |
| REWEIGHTING_NHILLS | how many Gaussian hills should be deposited between calculating the c(t) reweighting factor. The default is to do this every 50 hills.   |
| GRID_WSTRIDE       | write the grid to a file every N steps   |
| GRID_WFILE         | the file on which to write the grid  |
| GRID_RFILE         | a grid file from which the bias should be read at the initial step of the simulation   |
| ADAPTIVE           | use a geometric (=GEOM) or diffusion (=DIFF) based hills width scheme. Sigma is one number that has distance units or timestep dimensions  |
| WALKERS_ID         | walker id  |
| WALKERS_N          | number of walkers  |
| WALKERS_DIR        | shared directory with the hills files from all the walkers   |
| WALKERS_RSTRIDE    | stride for reading hills files   |
| INTERVAL           | monodimensional lower and upper limits, outside the limits the system will not feel the biasing force.   |
| SIGMA_MAX          | the upper bounds for the sigmas (in CV units) when using adaptive hills. Negative number means no bounds   |
| SIGMA_MIN          | the lower bounds for the sigmas (in CV units) when using adaptive hills. Negative number means no bounds   |
| RESTART            | allows per-action setting of restart (YES/NO/AUTO)   |
| UPDATE_FROM        | Only update this action from this time   |
| UPDATE_UNTIL       | Only update this action until this time  |

### **Examples**

The following input is for a standard metadynamics calculation using as collective variables the distance between atoms 3 and 5 and the distance between atoms 2 and 4. The value of the CVs and the metadynamics bias potential are written to the COLVAR file every 100 steps.

```
DISTANCE ATOMS=3,5 LABEL=d1
DISTANCE ATOMS=2,4 LABEL=d2
METAD ARG=d1,d2 SIGMA=0.2,0.2 HEIGHT=0.3 PACE=500 LABEL=restraint
PRINT ARG=d1,d2,restraint.bias STRIDE=100 FILE=COLVAR
```

(See also DISTANCE PRINT).

If you use adaptive Gaussians, with diffusion scheme where you use a Gaussian that should cover the space of 20 timesteps in collective variables. Note that in this case the histogram correction is needed when summing up hills.

```
DISTANCE ATOMS=3,5 LABEL=d1
DISTANCE ATOMS=2,4 LABEL=d2
METAD ARG=d1,d2 SIGMA=20 HEIGHT=0.3 PACE=500 LABEL=restraint ADAPTIVE=DIFF
PRINT ARG=d1,d2,restraint.bias STRIDE=100 FILE=COLVAR
```

If you use adaptive Gaussians, with geometrical scheme where you use a Gaussian that should cover the space of 0.05 nm in Cartesian space. Note that in this case the histogram correction is needed when summing up hills.

```
DISTANCE ATOMS=3,5 LABEL=d1
DISTANCE ATOMS=2,4 LABEL=d2
METAD ARG=d1,d2 SIGMA=0.05 HEIGHT=0.3 PACE=500 LABEL=restraint ADAPTIVE=GEOM
PRINT ARG=d1,d2,restraint.bias STRIDE=100 FILE=COLVAR
```

When using adaptive Gaussians you might want to limit how the hills width can change. You can use SIG← MA\_MIN and SIGMA\_MAX keywords. The sigmas should specified in terms of CV so you should use the CV units. Note that if you use a negative number, this means that the limit is not set. Note also that in this case the histogram correction is needed when summing up hills.

```
DISTANCE ATOMS=3,5 LABEL=d1
DISTANCE ATOMS=2,4 LABEL=d2
METAD ...
ARG=d1,d2 SIGMA=0.05 HEIGHT=0.3 PACE=500 LABEL=restraint ADAPTIVE=GEOM SIGMA_MIN=0.2,0.1 SIGMA_MAX=0.5,1.0
... METAD
PRINT ARG=d1,d2,restraint.bias STRIDE=100 FILE=COLVAR
```

Multiple walkers can be also use as in ? These are enabled by setting the number of walker used, the id of the current walker which interprets the input file, the directory where the hills containing files resides, and the frequency to read the other walkers. Here is an example

```
DISTANCE ATOMS=3,5 LABEL=d1
METAD ...

ARG=d1 SIGMA=0.05 HEIGHT=0.3 PACE=500 LABEL=restraint
WALKERS_N=10
WALKERS_ID=3
WALKERS_DIR=../
WALKERS_RSTRIDE=100
... METAD
```

where WALKERS\_N is the total number of walkers, WALKERS\_ID is the id of the present walker (starting from 0 ) and the WALKERS\_DIR is the directory where all the walkers are located. WALKERS\_RSTRIDE is the number of step between one update and the other.

The c(t) reweighting factor can be calculated on the fly using the equations presented in ? as described above. This is enabled by using the keyword REWEIGHTING\_NGRID where the grid used for the calculation is set. The number of grid points given in REWEIGHTING\_NGRID should be equal or larger than the number of grid points given in GRID\_BIN.

```
METAD ...

LABEL=metad

ARG=phi,psi SIGMA=0.20,0.20 HEIGHT=1.20 BIASFACTOR=5 TEMP=300.0 PACE=500

GRID_MIN=-pi,-pi GRID_MAX=pi,pi GRID_BIN=150,150

REWEIGHTING_NGRID=150,150

REWEIGHTING_NHILLS=20
... METAD
```

Here we have asked that the calculation is performed every 20 hills by using REWEIGHTING\_NHILLS keyword. If this keyword is not given the calculation will by default be performed every 50 hills. The c(t) reweighting factor will be given in the rct component while the instantaneous value of the bias potential normalized using the c(t) reweighting factor is given in the rbias component [rbias=bias-c(t)] which can be used to obtain a reweighted histogram or free energy surface using the HISTOGRAM analysis.

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The kinetics of the transitions between basins can also be analysed on the fly as in ?. The flag ACCEL← ERATION turn on accumulation of the acceleration factor that can then be used to determine the rate. This method can be used together with COMMITTOR analysis to stop the simulation when the system get to the target basin. It must be used together with Well-Tempered Metadynamics.

You can also provide a target distribution using the keyword TARGET ? ? The TARGET should be a grid containing a free-energy (i.e. the -kbT\*log of the desired target distribution). Gaussians will then be scaled by a factor

$$e^{\beta(\tilde{F}(s)-\tilde{F}_{max})}$$

Here  $\tilde{F}(s)$  is the free energy defined on the grid and  $\tilde{F}_{max}$  its maximum value. Notice that we here used the maximum value as in ref ? This choice allows to avoid exceedingly large Gaussians to be added. However, it could make the Gaussian too small. You should always choose carefully the HEIGHT parameter in this case. The grid file should be similar to other PLUMED grid files in that it should contain both the target free-energy and its derivatives.

Notice that if you wish your simulation to converge to the target free energy you should use the DAMPFACTOR command to provide a global tempering ? Alternatively, if you use a BIASFACTOR yout simulation will converge to a free energy that is a linear combination of the target free energy and of the intrinsic free energy determined by the original force field.

```
DISTANCE ATOMS=3,5 LABEL=d1
METAD ...
LABEL=t1
ARG=d1 SIGMA=0.05 TAU=200 DAMPFACTOR=100 PACE=250
GRID_MIN=0 GRID_MAX=2 GRID_BIN=200
TARGET=dist.dat
... METAD
PRINT ARG=d1,t1.bias STRIDE=100 FILE=COLVAR
```

The header in the file dist.dat for this calculation would read:

```
#! FIELDS d1 t1.target der_d1
#! SET min_d1 0
#! SET max_d1 2
#! SET nbins_d1 200
#! SET periodic_d1 false
```

### 7.7 METAINFERENCE

This is part of the bias module

Calculate the Metainference Score for a set of back calculated experimental data.

The back calculated data, that are expected to be averages over replicas (NR=1,2,..,N) The functional form of this bias can be chosen between three variants selected with NOISE=GAUSS,MGAUSS,OUTLIERS which correspond to modelling the noise for the arguments as a single gaussian common to all the data points, a gaussian per data point or a single long-tailed gaussian common to all the data points.

As from Metainference theory there are two sigma values: SIGMA\_MEAN represent the error of calculating an average quanity using a finite set of replica and should be set as small as possible following the guidelines for

replica-averaged simulations in the framework of the Maximum Entropy Principle. SIGMA\_BIAS is an uncertainty parameter, sampled by a MC algorithm in the bounded interval defined by SIGMA\_MIN and SIGMA\_MAX. The initial value is set at SIGMA0. The MC move is a random displacement of maximum value equal to DSIGMA.

**Description of components** 

The names of the components in this action can be customized by the user in the actions input file. However, in addition to these customizable components the following quantities will always be output

| Quantity | Description                                   |
|----------|---|
| bias     | the instantaneous value of the bias potential |
| sigma    | uncertainty parameter                         |
| scale    | scale parameter                               |
| accept   | MC acceptance                                 |

### Compulsory keywords

| NOISETYPE  | functional form of the noise (GAUSS,MGAUSS,OUTLIERS)    |
|------------|---|
| SCALE0     | initial value of the uncertainty parameter              |
| SCALE_MIN  | minimum value of the uncertainty parameter              |
| SCALE_MAX  | maximum value of the uncertainty parameter              |
| DSCALE     | maximum MC move of the uncertainty parameter            |
| SIGMA0     | initial value of the uncertainty parameter              |
| SIGMA_MIN  | minimum value of the uncertainty parameter              |
| SIGMA_MAX  | maximum value of the uncertainty parameter              |
| DSIGMA     | maximum MC move of the uncertainty parameter            |
| SIGMA_MEAN | starting value for the uncertainty in the mean estimate |

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically                           |
|-----------------------|--|
| SCALEDATA             | ( default=off ) Set to TRUE if you want to sample a scaling factor common to all values and replicas |

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| ARG        | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |
|------------|---|
| PARARG     | reference values for the experimental data, these can be provided as arguments without derivatives  |
| PARAMETERS | reference values for the experimental data  |
| TEMP       | the system temperature - this is only needed if code doesnt' pass the temperature to plumed   |
| MC_STEPS   | number of MC steps  |
| MC_STRIDE  | MC stride   |

### **Examples**

In the following example we calculate a set of RDC, take the replica-average of them and comparing them with a set of experimental values. RDCs are compared with the experimental data but for a multiplication factor SCALE that is also sampled by MC on-the-fly

```
RDC ...
LABEL=rdc
SCALE=0.0001
GYROM = -72.5388
ATOMS1=22,23
ATOMS2=25,27
ATOMS3=29,31
ATOMS4=33,34
... RDC
ardc: ENSEMBLE ARG=rdc.*
METAINFERENCE ...
ARG=ardc.*
NOISETYPE=MGAUSS
PARAMETERS=1.9190, 2.9190, 3.9190, 4.9190
SCALEDATA SCALE0=1 SCALE_MIN=0.00001 SCALE_MAX=3 DSCALE=0.00
SIGMA0=0.01 SIGMA_MIN=0.00001 SIGMA_MAX=3 DSIGMA=0.00
SIGMA_MEAN=0.001
TEMP=300
LABEL=spe
... METAINFERENCE
PRINT ARG=spe.bias FILE=BIAS STRIDE=1
```

in the following example instead of using one uncertainty parameter per data point we use a single uncertainty value in a long-tailed gaussian to take into account for outliers.

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```
METAINFERENCE ...

ARG=ardc.*
NOISETYPE=OUTLIERS
PARAMETERS=1.9190,2.9190,3.9190,4.9190
SCALEDATA SCALEO=1 SCALE_MIN=0.00001 SCALE_MAX=3 DSCALE=0.00
SIGMA0=0.01 SIGMA_MIN=0.00001 SIGMA_MAX=3 DSIGMA=0.00
SIGMA_MEAN=0.001
TEMP=300
LABEL=spe
... METAINFERENCE
```

(See also RDC and ENSEMBLE).

# 7.8 MOVINGRESTRAINT

This is part of the bias module

Add a time-dependent, harmonic restraint on one or more variables.

This form of bias can be used to performed steered MD? and Jarzynski sampling?.

The harmonic restraint on your system is given by:

$$V(\vec{s},t) = \frac{1}{2}\kappa(t)(\vec{s} - \vec{s}_0(t))^2$$

The time dependence of  $\kappa$  and  $\vec{s}_0$  are specified by a list of STEP, KAPPA and AT keywords. These keywords tell plumed what values  $\kappa$  and  $\vec{s}_0$  should have at the time specified by the corresponding STEP keyword. Inbetween these times the values of  $\kappa$  and  $\vec{s}_0$  are linearly interpolated.

Additional material and examples can be also found in the tutorial Belfast tutorial: Out of equilibrium dynamics

**Description of components** 

By default this Action calculates the following quantities. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Description   |
|----------|---|
| bias     | the instantaneous value of the bias potential   |
| work     | the total work performed changing this restraint  |
| force2   | the instantaneous value of the squared force due to this bias potential   |
| _cntr    | one or multiple instances of this quantity will be refereceable elsewhere in the input file. these quantities will named with the arguments of the bias followed by the character string _cntr. These quantities give the instantaneous position of the center of the harmonic potential.   |
| _work    | one or multiple instances of this quantity will be refereceable elsewhere in the input file. These quantities will named with the arguments of the bias followed by the character string _work. These quantities tell the user how much work has been done by the potential in dragging the system along the various colvar axis. |
| _kappa   | one or multiple instances of this quantity will be refereceable elsewhere in the input file. These quantities will named with the arguments of the bias followed by the character string _kappa. These quantities tell the user the time dependent value of kappa.  |

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# Compulsory keywords

| VERSE | ( default=B ) Tells plumed whether the restraint is only acting for CV larger (U) or smaller (L) than the restraint or whether it is acting on both sides (B)  |
|-------|--|
| STEP  | This keyword appears multiple times as STEPx with $x=0,1,2,,n$ . Each value given represents the MD step at which the restraint parameters take the values KAPPAx and ATx. You can use multiple instances of this keyword i.e. STEP1, STEP2, STEP3   |
| AT    | ATx is equal to the position of the restraint at time STEPx. For intermediate times this parameter is linearly interpolated. If no ATx is specified for STEPx then the values of AT are kept constant during the interval of time between STEPx-1 and STEPx. You can use multiple instances of this keyword i.e. AT1, AT2, AT3                       |
| KAPPA | KAPPAx is equal to the value of the force constants at time STEPx. For intermediate times this parameter is linearly interpolated. If no KAPPAx is specified for STEPx then the values of KAPPAx are kept constant during the interval of time between STEPx-1 and STEPx. You can use multiple instances of this keyword i.e. KAPPA1, KAPPA2, KAPPA3 |

# **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| ARG                   | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |

### **Examples**

The following input is dragging the distance between atoms 2 and 4 from 1 to 2 in the first 1000 steps, then back in the next 1000 steps. In the following 500 steps the restraint is progressively switched off.

```
DISTANCE ATOMS=2,4 LABEL=d

MOVINGRESTRAINT ...

ARG=d

STEP0=0 AT0=1.0 KAPPA0=100.0

STEP1=1000 AT1=2.0

STEP2=2000 AT2=1.0

STEP3=2500 KAPPA3=0.0

... MOVINGRESTRAINT
```

The following input is progressively building restraints distances between atoms 1 and 5 and between atoms 2 and 4 in the first 1000 steps. Afterwards, the restraint is kept static.

```
DISTANCE ATOMS=1,5 LABEL=d1
DISTANCE ATOMS=2,4 LABEL=d2
MOVINGRESTRAINT ...
```

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```
ARG=d1,d2

STEP0=0 AT0=1.0,1.5 KAPPA0=0.0,0.0

STEP1=1000 AT1=1.0,1.5 KAPPA1=1.0,1.0

... MOVINGRESTRAINT
```

The following input is progressively bringing atoms 1 and 2 close to each other with an upper wall

```
DISTANCE ATOMS=1,2 LABEL=d1

MOVINGRESTRAINT ...

ARG=d1

VERSE=U

STEP0=0 AT0=1.0 KAPPA0=10.0

STEP1=1000 AT1=0.0

... MOVINGRESTRAINT
```

By default the Action is issuing some values which are the work on each degree of freedom, the center of the harmonic potential, the total bias deposited

(See also DISTANCE).

Attention

Work is not computed properly when KAPPA is time dependent.

### 7.9 PBMETAD

This is part of the bias module

Used to performed Parallel Bias MetaDynamics.

This action activate Parallel Bias MetaDynamics (PBMetaD) ?, a version of MetaDynamics ? in which multiple low-dimensional bias potentials are applied in parallel. In the current implementation, these have the form of monodimensional MetaDynamics bias potentials:

$$V(s_1, t), ..., V(s_N, t)$$

where:

$$V(s_i, t) = \sum_{k\tau < t} W_i(k\tau) \exp\left(-\frac{(s_i - s_i^{(0)}(k\tau))^2}{2\sigma_i^2}\right).$$

To ensure the convergence of each mono-dimensional bias potential to the corresponding free energy, at each deposition step the Gaussian heights are multiplied by the so-called conditional term:

$$W_i(k\tau) = W_0 \frac{\exp\left(-\frac{V(s_i, k\tau)}{k_B T}\right)}{\sum_{i=1}^{N} \exp\left(-\frac{V(s_i, k\tau)}{k_B T}\right)}$$

where  $W_0$  is the initial Gaussian height.

The PBMetaD bias potential is defined by:

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$$V_{PB}(\vec{s},t) = -k_B T \log \sum_{i=1}^{N} \exp\left(-\frac{V(s_i,t)}{k_B T}\right).$$

Information on the Gaussian functions that build each bias potential are printed to multiple HILLS files, which are used both to restart the calculation and to reconstruct the mono-dimensional free energies as a function of the corresponding CVs. These can be reconstructed using the sum hills utility because the final bias is given by:

$$V(s_i) = -F(s_i)$$

Currently, only a subset of the METAD options are available in PBMetaD.

The bias potentials can be stored on a grid to increase performances of long PBMetaD simulations. You should provide either the number of bins for every collective variable (GRID\_BIN) or the desired grid spacing (GRID\_SP← ACING). In case you provide both PLUMED will use the most conservative choice (highest number of bins) for each dimension. In case you do not provide any information about bin size (neither GRID\_BIN nor GRID\_SPACING) and if Gaussian width is fixed PLUMED will use 1/5 of the Gaussian width as grid spacing. This default choice should be reasonable for most applications.

Another option that is available is well-tempered metadynamics ?. In this variant of PBMetaD the heights of the Gaussian hills are rescaled at each step by the additional well-tempered metadynamics term. This ensures that each bias converges more smoothly. It should be noted that, in the case of well-tempered metadynamics, in the output printed the Gaussian height is re-scaled using the bias factor. Also notice that with well-tempered metadynamics the HILLS files do not contain the bias, but the negative of the free-energy estimate. This choice has the advantage that one can restart a simulation using a different value for the  $\Delta T$ . The applied bias will be scaled accordingly.

Note that you can use here also the flexible gaussian approach? in which you can adapt the gaussian to the extent of Cartesian space covered by a variable or to the space in collective variable covered in a given time. In this case the width of the deposited gaussian potential is denoted by one value only that is a Cartesian space (ADAPT  $\leftarrow$  IVE=GEOM) or a time (ADAPTIVE=DIFF). Note that a specific integration technique for the deposited gaussians should be used in this case. Check the documentation for utility sum\_hills.

With the keyword INTERVAL one changes the metadynamics algorithm setting the bias force equal to zero outside boundary ?. If, for example, metadynamics is performed on a CV s and one is interested only to the free energy for s > sw, the history dependent potential is still updated according to the above equations but the metadynamics force is set to zero for s < sw. Notice that Gaussians are added also if s < sw, as the tails of these Gaussians influence VG in the relevant region s > sw. In this way, the force on the system in the region s > sw comes from both metadynamics and the force field, in the region s < sw only from the latter. This approach allows obtaining a history-dependent bias potential VG that fluctuates around a stable estimator, equal to the negative of the free energy far enough from the boundaries. Note that:

- · It works only for one-dimensional biases;
- · It works both with and without GRID;
- · The interval limit sw in a region where the free energy derivative is not large;
- If in the region outside the limit sw the system has a free energy minimum, the INTERVAL keyword should be used together with a UPPER\_WALLS or LOWER\_WALLS at sw.

Multiple walkers? can also be used. See below the examples.

**Description of components** 

By default this Action calculates the following quantities. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

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| Quantity | Description                                   |
|----------|---|
| bias     | the instantaneous value of the bias potential |

# Compulsory keywords

| SIGMA | the widths of the Gaussian hills                    |
|-------|---|
| PACE  | the frequency for hill addition, one for all biases |

# **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| GRID_SPARSE           | ( default=off ) use a sparse grid to store hills  |
| GRID_NOSPLINE         | ( default=off ) don't use spline interpolation with grids   |
| WALKERS_MPI           | ( default=off ) Switch on MPI version of multiple walkers - not compatible with other WALKERS_* options   |
| ARG                   | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |
| FILE                  | files in which the lists of added hills are stored, default names are assigned using arguments if FILE is not found   |
| HEIGHT                | the height of the Gaussian hills, one for all biases. Compulsory unless TAU, TEMP and BIASFACTOR are given  |
| FMT                   | specify format for HILLS files (useful for decrease the number of digits in regtests)   |
| BIASFACTOR            | use well tempered metadynamics with this biasfactor, one for all biases. Please note you must also specify temp   |
| TEMP                  | the system temperature - this is only needed if you are doing well-tempered metadynamics  |
| TAU                   | in well tempered metadynamics, sets height to (kb*DeltaT*pace*timestep)/tau   |
| GRID_RFILES           | read grid for the bias  |
| GRID_WSTRIDE          | frequency for dumping the grid  |
| GRID_WFILES           | dump grid for the bias, default names are used if GRID_WSTRIDE is used without GRID_WFILES.   |
| GRID_MIN              | the lower bounds for the grid   |
| GRID_MAX              | the upper bounds for the grid   |
| GRID_BIN              | the number of bins for the grid   |

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| GRID_SPACING    | the approximate grid spacing (to be used as an alternative or together with GRID_BIN)   |
|-----------------|---|
| WALKERS_ID      | walker id   |
| WALKERS_N       | number of walkers   |
| WALKERS_DIR     | shared directory with the hills files from all the walkers  |
| WALKERS_RSTRIDE | stride for reading hills files  |
| INTERVAL_MIN    | monodimensional lower limits, outside the limits the system will not feel the biasing force.  |
| INTERVAL_MAX    | monodimensional upper limits, outside the limits the system will not feel the biasing force.  |
| ADAPTIVE        | use a geometric (=GEOM) or diffusion (=DIFF) based hills width scheme. Sigma is one number that has distance units or timestep dimensions |
| SIGMA_MAX       | the upper bounds for the sigmas (in CV units) when using adaptive hills. Negative number means no bounds                                  |
| SIGMA_MIN       | the lower bounds for the sigmas (in CV units) when using adaptive hills. Negative number means no bounds                                  |
| RESTART         | allows per-action setting of restart (YES/NO/AUTO)  |
| UPDATE_FROM     | Only update this action from this time  |
| UPDATE_UNTIL    | Only update this action until this time   |

#### **Examples**

The following input is for PBMetaD calculation using as collective variables the distance between atoms 3 and 5 and the distance between atoms 2 and 4. The value of the CVs and the PBMetaD bias potential are written to the COLVAR file every 100 steps.

```
DISTANCE ATOMS=3,5 LABEL=d1
DISTANCE ATOMS=2,4 LABEL=d2
PBMETAD ARG=d1,d2 SIGMA=0.2,0.2 HEIGHT=0.3 PACE=500 LABEL=pb FILE=HILLS_d1,HILLS_d2
PRINT ARG=d1,d2,pb.bias STRIDE=100 FILE=COLVAR
```

(See also DISTANCE and PRINT).

If you use well-tempered metadynamics, you should specify a single biasfactor and initial Gaussian height.

```
DISTANCE ATOMS=3,5 LABEL=d1
DISTANCE ATOMS=2,4 LABEL=d2
PBMETAD ...
ARG=d1,d2 SIGMA=0.2,0.2 HEIGHT=0.3
PACE=500 BIASFACTOR=8 LABEL=pb
FILE=HILLS_d1,HILLS_d2
... PBMETAD
PRINT ARG=d1,d2,pb.bias STRIDE=100 FILE=COLVAR
```

The following input enables the MPI version of multiple-walkers.

```
DISTANCE ATOMS=3,5 LABEL=d1
DISTANCE ATOMS=2,4 LABEL=d2
PBMETAD ...
ARG=d1,d2 SIGMA=0.2,0.2 HEIGHT=0.3
PACE=500 BIASFACTOR=8 LABEL=pb
FILE=HILLS_d1,HILLS_d2
WALKERS_MPI
... PBMETAD
PRINT ARG=d1,d2,pb.bias STRIDE=100 FILE=COLVAR
```

The disk version of multiple-walkers can be enabled by setting the number of walker used, the id of the current walker which interprets the input file, the directory where the hills containing files resides, and the frequency to read the other walkers. Here is an example

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```
DISTANCE ATOMS=3,5 LABEL=d1
DISTANCE ATOMS=2,4 LABEL=d2
PBMETAD ...
ARG=d1,d2 SIGMA=0.2,0.2 HEIGHT=0.3
PACE=500 BIASFACTOR=8 LABEL=pb
FILE=HILLS_d1,HILLS_d2
WALKERS_N=10
WALKERS_ID=3
WALKERS_DIR=../
WALKERS_RSTRIDE=100
... PBMETAD
PRINT ARG=d1,d2,pb.bias STRIDE=100 FILE=COLVAR
```

where WALKERS\_N is the total number of walkers, WALKERS\_ID is the id of the present walker (starting from 0 ) and the WALKERS\_DIR is the directory where all the walkers are located. WALKERS\_RSTRIDE is the number of step between one update and the other.

# 7.10 RESTRAINT

This is part of the bias module

Adds harmonic and/or linear restraints on one or more variables.

Either or both of SLOPE and KAPPA must be present to specify the linear and harmonic force constants respectively. The resulting potential is given by:

$$\sum_{i} \frac{k_i}{2} (x_i - a_i)^2 + m_i * (x_i - a_i)$$

The number of components for any vector of force constants must be equal to the number of arguments to the action.

Additional material and examples can be also found in the tutorial Belfast tutorial: Umbrella sampling

**Description of components** 

By default this Action calculates the following quantities. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Description   |
|----------|---|
| bias     | the instantaneous value of the bias potential                           |
| force2   | the instantaneous value of the squared force due to this bias potential |

# Compulsory keywords

| SLOPE | ( default=0.0 ) specifies that the restraint is linear and what the values of the force constants on each of the variables are |
|-------|--|
| KAPPA | ( default=0.0 ) specifies that the restraint is harmonic and what the values of the force constants on                         |
|       | each of the variables are  |
| AT    | the position of the restraint  |

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**Options** 

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| ARG                   | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |

# **Examples**

The following input tells plumed to restrain the distance between atoms 3 and 5 and the distance between atoms 2 and 4, at different equilibrium values, and to print the energy of the restraint

```
DISTANCE ATOMS=3,5 LABEL=d1
DISTANCE ATOMS=2,4 LABEL=d2
RESTRAINT ARG=d1,d2 AT=1.0,1.5 KAPPA=150.0,150.0 LABEL=restraint
PRINT ARG=restraint.bias
```

(See also DISTANCE and PRINT).

# 7.11 UPPER WALLS

This is part of the bias module

Defines a wall for the value of one or more collective variables, which limits the region of the phase space accessible during the simulation.

The restraining potential starts acting on the system when the value of the CV is greater (in the case of UPPER $\leftarrow$  \_WALLS) or lower (in the case of LOWER\_WALLS) than a certain limit  $a_i$  (AT) minus an offset  $o_i$  (OFFSET). The expression for the bias due to the wall is given by:

$$\sum_{i} k_i ((x_i - a_i + o_i)/s_i)_i^e$$

 $k_i$  (KAPPA) is an energy constant in internal unit of the code,  $s_i$  (EPS) a rescaling factor and  $e_i$  (EXP) the exponent determining the power law. By default: EXP = 2, EPS = 1.0, OFFSET = 0.

**Description of components** 

By default this Action calculates the following quantities. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

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| Quantity | Description   |
|----------|---|
| bias     | the instantaneous value of the bias potential                           |
| force2   | the instantaneous value of the squared force due to this bias potential |

# Compulsory keywords

| AT     | the positions of the wall. The a_i in the expression for a wall.                            |  |  |
|--------|---|--|--|
| KAPPA  | the force constant for the wall. The k_i in the expression for a wall.                      |  |  |
| OFFSET | ( default=0.0 ) the offset for the start of the wall. The o_i in the expression for a wall. |  |  |
| EXP    | ( default=2.0 ) the powers for the walls. The e_i in the expression for a wall.             |  |  |
| EPS    | ( default=1.0 ) the values for s_i in the expression for a wall                             |  |  |

### **Options**

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically  |
|-----------------------|---|
| ARG                   | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |

# **Examples**

The following input tells plumed to add both a lower and an upper walls on the distance between atoms 3 and 5 and the distance between atoms 2 and 4. The lower and upper limits are defined at different values. The strength of the walls is the same for the four cases. It also tells plumed to print the energy of the walls.

```
DISTANCE ATOMS=3,5 LABEL=d1
DISTANCE ATOMS=2,4 LABEL=d2
UPPER_WALLS ARG=d1,d2 AT=1.0,1.5 KAPPA=150.0,150.0 EXP=2,2 EPS=1,1 OFFSET=0,0 LABEL=uwall
LOWER_WALLS ARG=d1,d2 AT=0.0,1.0 KAPPA=150.0,150.0 EXP=2,2 EPS=1,1 OFFSET=0,0 LABEL=lwall
PRINT ARG=uwall.bias,lwall.bias
```

(See also DISTANCE and PRINT).

# 7.12 RESTART

This is part of the setup module

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Activate restart.

This is a Setup directive and, as such, should appear at the beginning of the input file. It influences the way PLUMED treat files open for writing (see also Files).

Notice that it is also possible to enable or disable restart on a per-action basis using the RESTART keyword on a single action. In this case, the keyword should be assigned a value. RESTART=AUTO means that global settings are used, RESTART=YES or RESTART=NO respectively enable and disable restart for that single action.

### Attention

This directive can have also other side effects, e.g. on METAD and PBMETAD and on some analysis action.

# **Options**

NO (default=off) switch off restart - can be used to override the behavior of the MD engine

#### **Examples**

### Using the following input:

```
d: DISTANCE ATOMS=1,2
PRINT ARG=d FILE=out
```

(See also DISTANCE and PRINT). a new 'out' file will be created. If an old one is on the way, it will be automatically backed up.

On the other hand, using the following input:

```
RESTART
d: DISTANCE ATOMS=1,2
PRINT ARG=d FILE=out
```

the file 'out' will be appended. (See also DISTANCE and PRINT).

In the following case, file out1 will be backed up and file out2 will be concatenated

```
RESTART
d1: DISTANCE ATOMS=1,2
d2: DISTANCE ATOMS=1,2
PRINT ARG=d1 FILE=out1 RESTART=NO
PRINT ARG=d2 FILE=out2
```

(See also DISTANCE and PRINT).

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# **Chapter 8**

# **Variationally Enhanced Sampling**

The VES code is a module for PLUMED that implements enhanced sampling methods based on *Variationally Enhanced Sampling* (VES) ?. The VES code is developed independently from the PLUMED code, see the homepage of the VES code for further information.

The VES code is an optional module, to enable it you need to configure PLUMED using ./configure -enable-modules.

This manual is currently under construction. All keywords should be listed for the available actions while more detailed descriptions of the actions can be missing. The manual will be updated frequently. Furthermore, some of the keywords and options might be changed without warning.

- MARVEL-VES School February 2017
- Tutorials
- Bias
- · Basis functions
- · Target Distributions
- · Optimizers
- · Collective Variables
- Utilities
- · Command Line Tools
- · VES Index of Actions

# 8.1 MARVEL-VES School February 2017

Tutorials for the MARVEL School on Variationally Enhanced Sampling in Lugano, February 14-17, 2017.

Tuesday February 14

Tutorial 1: Introduction to PLUMED and analyzing molecular simulations - Gareth Tribello

Wednesday February 15

Tutorial 2: Biasing with metadynamics - Pablo Piaggi

Tutorial 3: Biasing with variationally enhanced sampling - Pablo Piaggi, Omar Valsson, and Michele Invernizzi

**Thursday February 16** 

Tutorial 4: Further on variationally enhanced sampling - Pablo Piaggi, Omar Valsson, and Michele Invernizzi

Tutorial 5: Advanced collective variables - Gareth Tribello

- Path CVs
- Multicolvar
- · Dimensionality reduction

Friday February 17

Tutorial 6: Obtaining kinetics from molecular simulations - James McCarty and Ferruccio Palazzesi

# 8.2 Tutorials

The following tutorials are available for the VES code

| MARVEL-VES tutorial (Lugano 2017): Kinetics     | How to obtain kinetics from biased molecular simula-      |
|---|---|
|   | tions using VES.  |
| MARVEL-VES tutorial (Lugano 2017): Metadynamics | Brief introduction to metadynamics.                       |
| MARVEL-VES tutorial (Lugano 2017): VES 1        | Introduction to VES, using different target distributions |
|   | and basis sets.   |
| MARVEL-VES tutorial (Lugano 2017): VES 2        | VES, well-tempered target distribution and 2 dimen-       |
|   | sional biases.  |

# 8.2.1 MARVEL-VES tutorial (Lugano 2017): Kinetics

#### 8.2.1.1 Aims

The aim of this tutorial is to introduce the use of VES for obtaining kinetic information of activated processes. We will learn how to set up a biased simulation using a fixed flooding potential acting on a relevant slow degree of freedom. We can then rescale the accelerated MD time in a post-processing procedure.

### 8.2.1.2 Learning Outcomes

Once this tutorial is completed students will:

· Optimize a bias using VES with an energy cutoff to selectively fill low regions of the free energy surface.

- · Use the optimized bias to observe several rare event transitions
- · Post-process the accelerated trajectory to obtain an unbiased estimate of the transition rate
- · Compute the empirical cumulative distribution of first passage times and compare to a theoretical model.

#### 8.2.1.3 Resources

The tarball for this project contains the following files:

- · CH.airebo: Force field parameters for LAMMPS
- · input: LAMMPS input script
- · data.start : Starting configuration in LAMMPS format
- plumed.dat : Example PLUMED file
- · time-reweighting.py: Python script for post-processing trajectory
- TRAJECTORIES-1700K: A directory containing many trajectories for post processing
- get-all-fpt.py : A python script to extract transition times from the trajectories
- cdf.analysis.py: A python script to compute the cumulative probability distribution and perform KS test

# 8.2.1.4 Requirements

- · python with numpy, scipy, and statsmodels
- · LAMMPS compiled with MANYBODY package
- · VMD for visualization

# 8.2.1.5 Instructions

# 8.2.1.5.1 Exercise 1A. Preliminary investigation using VES

As an example of an activated process in materials science, we will work with the Stone-Wales transformation in a carbon nanotube. The tarball for this project contains the inputs neccessary to run a simulation in LAMMPS for a 480 atom carbon nanotube. We use the AIREBO (Adaptive Intermolecular Reactive Empirical Bond Order) force field parameters which can approximately describe C-C bond breakage and formation at reasonable computational cost. For CVs we can use the coordination number in PLUMED to measure the number of covalent bonds among different groups of atoms. The transformation involves breaking two C-C bonds and forming two alternative C-C bonds. A definition of these CVs as well as the relevant C-C bonds are depicted in Figure stone-wales. We prepare a PLUMED input file as follows.

```
# set distance units to angstrom, time to ps, and energy to eV
UNITS LENGTH=A TIME=ps ENERGY=eV

# define two variables
COORDINATION GROUPA=229,219 GROUPB=238,207 R_0=1.8 NN=8 MM=16 PAIR LABEL=CV1
COORDINATION GROUPA=229,219 GROUPB=207,238 R_0=1.8 NN=9 MM=16 PAIR LABEL=CV2

# the difference between variables
COMBINE ARG=CV1,CV2 COEFFICIENTS=1,-1 POWERS=1,1 LABEL=d1 PERIODIC=NO
```

In the above, the first line sets the energy units. The second and third line define the two CVs for the C-C covalent bonds. (We have chosen atoms 238,207,229 and 219; however this choice is arbitrary and other atoms could equally well have been chosen.) Lastly, we define a simple approximate reaction coordinate given by the difference between CV1 and CV2 that we can use to monitor the transition.

Next we will use VES to drive the transformation at 1700 K. We bias the formation of bonds DB and AC shown in Figure stone-wales using CV2 which changes from 0 to 2 during the transformation. (Although a more rigorous treatment would bias both CVs, for this tutorial we will simplify things and work in only one dimension). We choose a Chebyshev polynomial basis set up to order 36

```
# The basis set to use
bf1: BF_CHEBYSHEV ORDER=36 INTERVAL_MIN=0.0 INTERVAL_MAX=2.0
```

and we tell PLUMED to use VES acting on CV2 with a free energy cutoff

```
VES_LINEAR_EXPANSION ...

ARG=CV2

BASIS_FUNCTIONS=bf1

LABEL=variational

TEMP=1700

BIAS_CUTOFF=15.0

BIAS_CUTOFF_FERMI_LAMBDA=10.0
... VES_LINEAR_EXPANSION
```

Here we are biasing CV2 with the basis set defined above. The final two lines impose the cutoff at 15 eV. The cutoff is of the form

$$\frac{1}{1 + e^{\lambda[F(s) - F_c]}}$$

where  $\lambda$  (inverse energy units) controls how sharply the function goes to zero. Above we have set  $\lambda=10.0$  to ensure the cutoff goes sharply enough to zero.

The following input updates the VES bias every 200 steps, writing out the bias every 10 iterations. To enforce the energy cutoff we also need to update the target distribution which we do every 40 iterations with the TARGETDI ← ST\_STRIDE flag.

```
AVERAGED_SGD ...
BIAS=variational
STRIDE=200
LABEL=var-S
STEPSIZE=0.1
COEFFS_FILE=coeffs.dat
BIAS_OUTPUT=10
TARGETDIST_STRIDE=40
TARGETDIST_OUTPUT=40
COEFFS_OUTPUT=1
... AVERAGED_SGD
```

Finally, we will stop the simulation when the transition occurs using the COMMITTOR in PLUMED

```
COMMITTOR ARG=d1 BASIN_LL1=-2.0 BASIN_UL1=-1.0 STRIDE=600
```

Run the simulation using LAMMPS

```
lmp_mpi < input</pre>
```

and plot the last few bias output files (bias.variational.iter-n.data) using gnuplot. What is the difference between the maximum and minimum values of the bias obtained during the simulation? Is the cutoff value sufficient to cross the barrier? Is the cutoff value too large?

Figure Figure1A shows an example bias potential after 90 iterations. Note that a cutoff of 15 eV is too large as the system transitions before the bias reaches the prescribed cutoff. From Figure Figure1A we see a barrier height of approximately 7.3 eV.

The output also produces an movie.xyz file which can be viewed in vmd. For better visualization, first change atom id from 1 to C by typing

```
sed "s/^1 /C /" movie.xyz > newmovie.xyz
```

Then load the newmovie.xyz into vmd and choose Graphics -> Representations and set Drawing Method to DynamicBonds. Create a second representation by clicking Create Rep and set the Drawing Method to VDW. Change the sphere scale to 0.3 and play the movie. You should observe the Stone-Wales transformation right before the end of the trajectory.

8.2.1.5.2 Exercise 1B. Set up and run a VES bias imposing a cutoff

In this exercise we will run a VES simulation to fill the FES only up to a certain cutoff. This will be the first step in order to obtain kinetic information from biased simulations. In the previous section, we observed that a cutoff of 15 eV is too strong for our purpose. Change the cutoff energy from 15.0 to 6.0 eV by setting

```
BIAS_CUTOFF=6.0
```

and rerun the simulation from Exercise 1A. [Note: In practice one can use multiple walkers during the optimization by adding the flag MULTIPLE WALKERS]

Plot some of the bias files (bias.variational.iter-n.data) that are printed during the simulation using gnuplot. At the end of the simulation, you should be able to reproduce something like Figure Figure 1B. Is the bias converging? If so, how many iterations does it require to converge?

Figure Figure 1B shows the bias potential after 70,80, and 90 iteration steps. Note that the bias has reached the cutoff and goes to zero at around 1 Angstrom.

#### 8.2.1.5.3 Exercise 2. Using a fixed bias as a flooding potential to obtain rates

In this exercise we will use the bias obtained above as a static umbrella potential. We will set up and run a new trajectory to measure the first passage time of escape from the well.

We can extract the coefficients that we need from the final iteration in Exercise-1B above.

```
tail -n 47 coeffs.dat > fixed-coeffs.dat
```

Now create a new directory from which you will run a new simulation and copy the necessary input files (including the fixed-coeffs.dat) into this directory. Modify the PLUMED file so that the optimized coefficients are read by the VES\_LINEAR\_EXPANSION

```
VES_LINEAR_EXPANSION ...

ARG=CV2

BASIS_FUNCTIONS=bf1

LABEL=variational

TEMP=1700

BIAS_CUTOFF=6.0

BIAS_CUTOFF_FERMI_LAMBDA=10.0

COEFFS=fixed-coeffs.dat
... VES_LINEAR_EXPANSION
```

The final line specifies the coefficients to be read from a file.

Make sure to remove the lines for the stochastic optimization (AVERAGED\_SGD) as we no longer wish to update the bias.

We will also perform metadynamics with an infrequent deposition stride to ensure that the trajectory does not get stuck in any regions where the bias potential is not fully converged The following implements metadynamics on both CV1 and CV2 with a deposition stride of 4000 steps and a hill height of 0.15 eV.

```
METAD ...

ARG=CV1,CV2

SIGMA=0.2,0.2

HEIGHT=0.15,0.15

PACE=4000

LABEL=metad
... METAD
```

Again we will use the COMMITTOR to stop the trajectory after the transition.

```
COMMITTOR ARG=d1 BASIN_LL1=-2.0 BASIN_UL1=-1.0
```

Now run a trajectory with the fixed bias. What is the time (biased) to escape? Plot the trajectory of the approximate reaction coordinate (column 4 in the COLVAR) in gnuplot. An example is shown in Figure Figure 2.

Also look at the metadynamics bias in the column labeled metad.bias. How does the magnitude compare to the bias from VES in column variational.bias?

The crossing time for a single event doesn't tell us much because we don't have any statistics on the transition events. To obtain the mean first passage time, we have to repeat the calculation many times. To generate statistically independent samples, we have to change the seed for the random velocities that are generated in the LAMMPS input file. In a new directory, copy the necessary files and edit the following line in the input file

```
velocity all create 1700. 495920
```

Choose a different 6 digit random number and repeat Exercise 2. How does the escape time compare to what you obtained before? Repeat the procedure several times with different velocity seeds to get a distribution of first passage times. Make sure you launch each simulation from a separate directory and keep all COLVAR files as you will need them in the next section where we will analyze the transition times.

# 8.2.1.5.4 Exercise 3. Post processing to obtain unbiased estimate for the transition rate

In the previous section you generated several trajectories with different first passage times. However, these times need to be re-weighted to correct for the bias potential. We can rescale the time according to the hyperdynamics formula

$$t^* = \Delta t_{MD} \sum_{i}^{n} e^{\beta V(s)}$$

Note that we need to add the total bias at each step, coming from both the VES bias and metadynamics. The python script time-reweighting.py will read the COLVAR from Exercise 2 and print the final reweighted time (in seconds). Open the script to make sure you understand how it works.

Run the script using

```
python time-reweighting.py
```

Note that the output first passage time is converted to seconds. What is the acceleration factor of our biased simulation? (i.e. the ratio of biased to unbiased transition times) The script also produces a time-reweighted trajectory COLVAR-RW for a specified CV (here we choose the approximate reaction coordinate, d1). Plot the reweighted COLVAR-RW in gnuplot and compare the original vs. time-reweighted trajectories. In particular, what effect does rescaling have on the time step?

Rerun the script for each of the trajectories you have run with the fixed bias and compute the mean first passage time from your data. The Stone-Wales transformation at 1700 K is estimated in fullerene to be  $\sim$ 10 days. How does your average time compare to this value?

The distribution of first passage times for an activated processes typically follows an exponential distribution. Instead of directly making a histogram of the first passage times, we can look at the cumulative distribution function which maps a value x to the fraction of values less than or equal to x. Since we are computing the cumulative distribution from a data set, this is called the empirical cumulative distribution (ECDF). On the other hand, the theoretical cumulative distribution (CDF) of an exponentially distributed random process is

$$P(t) = 1 - e^{-t/\tau}$$

where  $\boldsymbol{\tau}$  is the mean first passage time.

In order to calculate the ECDF we need many trajectories. Several COLVAR files are included in the TRAJECT ← ORIES-1700K directory. The script get-all-fpt.py is a modified version of time-reweighting.py and will calculate the first passage time (fpt) from all the simulation data and will output the times to a file fpt.dat. Run the script from the TRAJECTORIES-1700K directory

```
python get-all-fpt.py
```

You should obtain the output file fpt.dat which has a list of all the times. You can append your own values you obtained from Exercise 2 to the end of the list to increase the number of data points.

The script cdf-analysis.py will compute the ECDF and fit the distribution to the theoretical CDF. The script uses the statsmodels Python module. Run the script with

```
python cdf-analyysis.py
```

from the same directory where the fpt.dat file is located. The script prints both the mean first passage time of the data as well as the fit parameter  $\tau$ . How do these two values compare?

Figure Figure3 shows an example fit of the ECDF to the theoretical CDF for a Poisson process. To test the reliability of the fit, we can generate some data set according the theoretical CDF and perform a two-sample Kolmogorov- $\hookrightarrow$  Smirnov (KS) test. The KS test provides the probability that the two sets of data are drawn from the same underlying distribution expressed in the so-called p-value. The null hypothesis is typically rejected for p-value < 0.05. The script cdf-analysis.py also performs the KS test and prints the p-value. What is the p-value we obtain from your dataset of transition times?

# 8.2.2 MARVEL-VES tutorial (Lugano 2017): Metadynamics

### 8.2.2.1 Learning Outcomes

Once this tutorial is completed students will learn to:

- · Perform metadynamics simulations using PLUMED 2 and LAMMPS
- Construct a bias potential on 1 and 2 collective variables (CVs)
- · Assess the convergence of the free energy surface
- · Distinguish between good and bad CVs
- · Reweight with more than one bias potential

#### 8.2.2.2 Resources

The tarball for this project contains the following folders:

- Example1: Contains the input file for the unbiased simulation.
- Example2: Contains the input files for one of the biased simulations. The rest of the biased simulations inputs should be created by modifying this one.

# 8.2.2.3 Instructions

# 8.2.2.3.1 The system

We consider the association/dissociation of NaCl in acqueous solution. The dissociation barrier is expected to be around 2.5  $k_{\rm B}T$ . One interesting aspect of the ion dissociation problem is that collective solvent motions play an important role in the transition. This problem has been considered in the original metadynamics paper ? and also in reference ? . We will use the potential developed in ref. ? for NaCl and TIP3P water with parameters corrected to be used with long-range Coulomb solvers ?. The system contains 1 Na, 1 Cl, and 106 water molecules (total 320 atoms).

# 8.2.2.3.2 Perform an unbiased simulation and control the distance Na-Cl

We first perform a standard MD simulation and control the distance Na-Cl. All the files needed for this example are contained in the folder Example1 . The distance Na-Cl can be calculated in Plumed 2 using:

```
d1: DISTANCE ATOMS=319,320
```

The coordination number of Na with respect to O in water will also be calculated for later use. This variable will represent the collective motion of the solvent.

```
COORDINATION ...

GROUPA=319

GROUPB=1-318:3

SWITCH={RATIONAL R_0=0.315 D_MAX=0.5 NN=12 MM=24} NLIST

NL_CUTOFF=0.55

NL_STRIDE=10

LABEL=coord
... COORDINATION
```

To run LAMMPS you can use the run.sh script:

This command runs LAMMPS using 2 MPI threads. The use of partitions will be discussed when using multiple walkers

Once the simulation is launched, the so called COLVAR file is written. In this case it contains the following:

```
#! FIELDS time d1 coord
0.200000 0.568067 5.506808
0.400000 0.500148 4.994588
0.600000 0.449778 4.931140
0.800000 0.528272 5.105816
1.000000 0.474371 5.089863
1.200000 0.430620 5.091551
1.400000 0.470374 4.993886
1.600000 0.458768 4.940097
1.800000 0.471886 4.952868
2.000000 0.489058 4.897593
```

If you plot the time (column 1) vs the distance (column 2), for instance in gnuplot:

```
pl "./COLVAR" u 1:2 w lp,
```

you will see that the ion pair is stuck in the dissociated state during the 1 ns simulation. It is unable to cross the  $\sim 5k_{\rm B}T$  barrier located at a distance of approximately 0.4 nm. You can also observe this behavior in the trajectory using VMD:

```
vmd out.dcd -psf nacl.psf
```

The trajectory has been saved in unwrapped format in order to avoid bonds stretching from one side to the box to the other due to periodic bounday conditions. In VMD we can wrap the atoms without breaking the bonds and show the box using the commands:

```
pbc wrap -compound res -all
pbc box
```

You can play with different visualization styles and options that VMD has. Therefore, if we want the system to go back and forth between the associated and dissociated state, we will need enhanced sampling.

# 8.2.2.3.3 Construct a bias potential on the distance Na-Cl

We now construct a bias potential  $V(\mathbf{s})$  on the distance Na-Cl using well-tempered metadynamics. The files for this example are contained in the directory Example2. As argument for the construction of the potential we will use the distance Na-Cl (label d1). We choose a gaussian height of 1 kJ/mol which is slightly less than 0.5  $k_{\rm B}T$ . The gaussian width is 0.02 nm, in the same order of the features in the FES. A rule of thumb for choosing the gaussian width is to use the standard deviation of the unbiased fluctuations of the CV. The bias factor is set to 5 since the largest barrier in the FES is expected to be roughly 5  $k_{\rm B}T$ . Once the metadynamics simulation is converged, the bias will be (up to an arbitrary constant):

$$V(\mathbf{s}) = -\left(1 - \frac{1}{\gamma}\right)F(\mathbf{s})$$

and therefore the system will evolve under an effective free energy:

$$\tilde{F}(\mathbf{s}) = F(\mathbf{s}) + V(\mathbf{s}) = \frac{F(\mathbf{s})}{\gamma},$$

that is to say, the largest barrier will be of around 1  $k_{\rm B}T$ . The input is:

```
METAD ...

LABEL=metad

ARG=d1

SIGMA=0.02

HEIGHT=1.

BIASFACTOR=5

TEMP=300.0

PACE=500

GRID_MIN=0.2

GRID_MAX=1.0

GRID_BIN=300

REWEIGHTING_NGRID=300

.. METAD
```

Here the REWEIGHTING\_NGRID keyword turns on the calculation of the time dependent constant c(t) that we will use below when reweighting the simulations.

We will also limit the exploration of the CV space by introducing an upper wall bias  $V_{wall}(\mathbf{s})$ :

$$V_{wall}(s) = \kappa(s - s_0)^2$$
 if  $s > s_0$  and 0 otherwise.

The wall will focus the sampling in the most interesting region of the free energy surface. The effect of this bias potential will have to be corrected later in order to calculate ensemble averages. The syntax in Plumed 2 is:

```
UPPER_WALLS ...
ARG=d1
AT=0.6
KAPPA=2000.0
EXP=2
EPS=1
OFFSET=0.
LABEL=uwall
... UPPER_WALLS
```

You can run the simulation with the run.sh script as done in the previous example.

It is possible to try different bias factors to check the effect that it has on the trajectory and the effective FES.

In principle the cost of a metadynamics simulation should increase as the simulation progresses due to the need of adding an increasing number of gaussians to calculate the bias. However, since a grid is used to build up the bias this effect is not observed. You can check what happens if you do not use the GRID\_\* keywords. Remember that the bins in the grid should be small enough to describe the changes in the bias created by the gaussians. Normally a bin of size  $\sigma/5$  (with  $\sigma$  the gaussian width) is small enough.

#### 8.2.2.3.4 Assess convergence

One way to identify if a WT-MetaD simulation has converged is observing the estimated free energy surface at different times. The FES is estimated by using the relation (again up to an arbitrary constant):

$$F(\mathbf{s}) = -\left(\frac{\gamma}{\gamma - 1}\right)V(\mathbf{s}, t)$$

and the bias potential is calculated as a sum of gaussians. This can be done with Plumed 2 using for instance:

```
plumed sum_hills --hills ../HILLS --min 0.1 --max 0.8 --bin 300 --stride 100
```

Most of the flags are self explanatory. The flag –stride 100 will result in the FES been written every 100 gaussians, i.e. 100 ps. Inside the folder FES\_calculation you will find a script run.sh that executes the sum\_hills command and a gnuplot script plot.gpi that can be used typing:

```
gnuplot plot.gpi
```

After roughly 3 ns the free energy surface does not change significantly with time except for an immaterial constant c(t) that grows in time. This is in line with well-tempered metadynamics asymptotic behaviour:

$$V(\mathbf{s},t) = -\left(1 - \frac{1}{\gamma}\right)F(\mathbf{s}) + c(t).$$

The behavior of c(t) will be studied with greater detail later. It should be stressed that we are actually not calculating the free energy  $F(\mathbf{s})$  but rather  $F(\mathbf{s}) + V_{wall}(\mathbf{s})$ . For this reason for distances higher than 0.6 nm the free energy increases sharply.

An alternative way to observe the evolution of the bias is plotting the final free energy plus the instantaneous bias. The scripts for this example can be found in the folder Bias\_calculation. In this case we observe only the first 200 ps of the simulation. The (negative) bias can be calculated using:

```
plumed sum_hills --hills ../HILLS --min 0.1 --max 0.8 --bin 300 --stride 100 --negbias
```

This plot illustrates clearly how the bias is constructed to progressively "fill" the FES.

It is also possible to track convergence by controlling the evolution of some quantity connected to the free energy surface. In this case we will calculate the dissociation barrier, e.g. the height of the barrier that separates the associated state from the dissociated one. The scripts for this example are found in the folder Barrier\_calculation. Using the python script calculate\_barrier.py we can compute the barrier, for instance:

The script can be executed using:

```
python barrier_calculation.py > barrier.txt
```

and the results can be plotted using the gnuplot script plot.gpi. After roughly 4 ns the barrier stabilizes around 3 and 3.5  $k_{\rm B}T$ . It is important to stress that it is only possible to calculate the free energy difference between two points if the system has gone back and forth between these points several times. This applies both for the calculation of a barrier and the difference in free energy between two basins. It is also important to understand that none of the free energy methods described in this series of tutorials will be able to calculate free energies of regions that have not been sampled, i.e. visited.

Reweighting the simulation on the same CV that was used for biasing can also be used as a test of convergence. We will show that in the next section.

#### 8.2.2.3.5 Reweight the simulation

We first reweight the simulation on the distance Na-Cl, the same CV used for biasing. This reweighting is useful to check convergence and to have an estimate of the free energy that does not rely on using kernels. For instance if some features of the FES could not be captured by the kernels, the reweighting procedure will show them. This will become clearer in the VES tutorial. The scripts to perform this calculation are found in the folder ReweightDistance. In metadynamics quasistationary limit the weight assigned to a given configuration is ?:

$$w(\mathbf{R}) \propto e^{\beta(V(\mathbf{s},t)-c(t))}$$
.

By plotting time (column 1) versus c(t) (column 6) using the COLVAR file, the importance of taking c(t) into account becomes clear. c(t) keeps growing even after long times, reflecting the approximately rigid shift of the bias with time. Normally the first part of the trajectory is not used for reweighting since during this period the simulation has not reached the quasistationary limit. In this case we can discard the first 2 or 3 ns of simulation. To disregard the first 3 ns of simulation we can use sed to delete the first 15000 lines from the COLVAR file:

```
sed '2,15000d' ../COLVAR > COLVAR
```

We then use Plumed to calculate two histograms, one taking into account the wall bias and the other one neglecting it. The weights for the reweighting involving only the metadynamics bias have already been discussed while the weights considering both biases are:

$$w(\mathbf{R}) \propto e^{\beta(V(\mathbf{s},t)-c(t)+V_{wall}(\mathbf{s}))}$$
.

The input script for Plumed is:

```
# Read COLVAR file
distance:
              READ FILE=COLVAR IGNORE_TIME VALUES=d1
metad:
             READ FILE=COLVAR IGNORE_TIME VALUES=metad.rbias
            READ FILE=COLVAR IGNORE_TIME VALUES=uwall.bias
uwall:
# Define weights
weights1: REWEIGHT_METAD TEMP=300
weights2: REWEIGHT_BIAS TEMP=300 ARG=metad.rbias,uwall.bias
# Calculate histograms
HISTOGRAM ...
  ARG=distance
  GRID_MIN=0.2
  GRID MAX=0.8
  GRID BIN=100
  BANDWIDTH=0.002
 LOGWEIGHTS=weights1
 LABEL=hh1
... HISTOGRAM
HISTOGRAM ...
  ARG=distance
  GRID_MIN=0.2
  GRID_MAX=0.8
  GRID_BIN=100
  BANDWIDTH=0.002
  LOGWEIGHTS=weights2
  LABEL-hh2
... HISTOGRAM
# Print histograms to file
DUMPGRID GRID=hh1 FILE=histo FMT=%24.16e
DUMPGRID GRID=hh2 FILE=histo_wall FMT=%24.16e
```

### This example can be run with:

```
plumed --no-mpi driver --plumed plumed.dat --noatoms > plumed.out
```

and will generate the files histo and histo\_wall. The histograms represent the probability p(s) of observing a given value of the CV s. From the histograms the FES can be calculated using:

$$\beta F(\mathbf{s}) = -\log p(\mathbf{s})$$

and therefore we plot the FES in gnuplot using for instance:

```
pl "./histo" u 1:(-log($2)) w lp
```

The next plot compares the estimations of the FES from sum\_hills, reweighting with metadynamics bias, and reweighting using both the metadynamics bias and the upper wall bias You will find a gnuplot script plot.gpi to make this plot inside the ReweightDistance folder.

We can obtain important information of the system by reweighting on 2 CVs: The distance Na-Cl and the coordination of Na with O. This reweighting is similar to the one already done and the files that you will need are located in the ReweightBoth folder. The plot of the FES as a function of these 2 CVs provides important information of the association/dissociation mechanism. In the dissociated state, Na can have a coordination of 5 or 6, though it is more likely to find a coordination number of 6. However, in order to associate Na must have a coordination with O of 5. In the associated state Na can have a coordination of 3, 4 or 5. The transition state is characterized by a coordination number of  $\sim$ 5.

#### 8.2.2.3.6 Construct a bias potential on the coordination Na-O

As an exercise, you can write the input files for a simulation in which a bias potential is constructed on the coordination Na-0, i.e. the solvent degree of freedom. You can use the same gaussian height as before and  $\sigma = 0.1$ .

You will find that the exploration of the CV space is not efficient. The reason is that there is a slow degree of freedom that it is not being biased: the distance Na-Cl. Furthermore you can see in the 2 CV reweighting that the coordination Na-O shows significant overlap between the associated and dissociated states.

Bear in mind that this is a rather trivial example since the existing barriers are relatively low. Real problems in materials science usually involve large barriers and are not as forgiving as this example; a bad CV may lead to huge hysteresis and problems in convergence.

### 8.2.2.3.7 Construct a bias potential on both CVs

We will now construct a bias potential on both CVs. We have already calculated the FES as a function of both CVs through reweighting. In this example the FES will be calculated using the metadynamics bias potential. You can use the input files from Example2.tar and changed the plumed.dat file. To construct a 2 dimensional bias with metadynamics use the following input:

```
METAD ...

LABEL=metad

ARG=d1,coord

SIGMA=0.02,0.1

HEIGHT=1.

BIASFACTOR=5

TEMP=300.0

PACE=500

GRID_MIN=0.15,2.

GRID_MAX=0.9,9.

GRID_BIN=400,400

REWEIGHTING_NGRID=400,400

... METAD
```

Once that the simulation is completed you can run plumed sum hills to calculate the FES:

```
plumed sum hills --hills HILLS --mintozero
```

and plot the results using the following lines in gnuplot:

```
set pm3d map
set zr [0:15]
pl "fes.dat" u 1:2:3
```

#### 8.2.2.4 Final remarks

Some valuable tools for metadynamics simulations will be discussed in the VES tutorial. These include:

- · Restarting a simulation.
- Using Plumed driver to calculate a CV that was not calculated during the simulation. A reweighting can then be performed on this CV.
- Constructing biased histograms, i.e. histograms without weights to calculate the effective FES  $\tilde{F}(\mathbf{s}) = F(\mathbf{s}) + V(\mathbf{s})$ .
- Use multiple walkers to improve the exploration of CV space.

# 8.2.3 MARVEL-VES tutorial (Lugano 2017): VES 1

### 8.2.3.1 Learning Outcomes

Once this tutorial is completed students will learn to:

- Use different target distributions and choose the most appropriate for their problem.
- Use different basis sets and order of the expansions. Select the appropriate order for their problem.
- Use the optimization algorithm and choose the parameters.
- · Construct biases in 1 dimension.
- Assess the convergence of the simulation.
- · Obtain biased and unbiased histograms.

#### 8.2.3.2 Resources

The tarball for this project contains the following folders:

- Example1 : Contains the input file for the first example.
- Example2 : Contains the input file for the second example.

# 8.2.3.3 Summary of theory

Variationally enhanced sampling? is based on the the following functional of the bias potential:

$$\Omega[V] = \frac{1}{\beta} \log \frac{\int d\mathbf{s} \, e^{-\beta[F(\mathbf{s}) + V(\mathbf{s})]}}{\int d\mathbf{s} \, e^{-\beta F(\mathbf{s})}} + \int d\mathbf{s} \, p(\mathbf{s}) V(\mathbf{s}),$$

where  ${\bf s}$  are the CVs to be biased,  $p({\bf s})$  is a predefined probability distribution that we will refer to as the target distribution, and  $F({\bf s})$  is the free energy surface. This functional can be shown to be convex and to have a minimum at:

$$V(\mathbf{s}) = -F(\mathbf{s}) - \frac{1}{\beta} \log p(\mathbf{s}).$$

The last equation states that once that the functional  $\Omega[V]$  is minimized, the bias and the target distribution allow calculating the free energy. The target distribution  $p(\mathbf{s})$  can be chosen at will and it is the distribution of the CVs once that  $\Omega[V]$  has been minimized.

The variational principle is put to practice by expanding  $V(\mathbf{s})$  in some basis set:

$$V(\mathbf{s}) = \sum_{i} \alpha_i f_i(\mathbf{s}),$$

where  $f_i(\mathbf{s})$  are the basis functions and the  $\alpha$  are the coefficients in the expansion. We then need to find the  $\alpha$  that minimize  $\Omega[V]$ . In principle one could use any optimization algorithm. In practice the algorithm that has become the default choice for VES is the so-called averaged stochastic gradient descent algorithm ?. In this algorithm the  $\alpha$  are evolved iteratively according to:

$$\alpha^{(n+1)} = \alpha^{(n)} - \mu \left[ \nabla \Omega(\bar{\alpha}^{(n)}) + H(\bar{\alpha}^{(n)}) [\alpha^{(n)} - \bar{\alpha}^{(n)}] \right]$$

where  $\mu$  is the step size,  $\bar{\alpha}^{(n)}$  is the running average of  $\alpha^{(n)}$  at iteration n, and  $\nabla\Omega(\bar{\alpha}^{(n)})$  and  $H(\bar{\alpha}^{(n)})$  are the gradient and Hessian of  $\Omega[V]$  evaluated at the running average at iteration n, respectively. The behavior of the coefficients will become clear in the examples below.

8.2.3.4 Instructions

8.2.3.4.1 The system

We will consider the same system employed for the metadynamics tutorial.

### 8.2.3.4.2 Example 1: First VES simulation

For the first VES simulation we will revisit the problem of the ion pair dissociation but replacing the metadynamics bias with a VES bias. The bias potential will be constructed on the distance Na-Cl as done before. We will still use the upper wall used in the metadynamics tutorial to make the actual example as similar as possible to the previous one. We will then see that VES has a more natural way to deal with barriers. All files needed for this example can be found in the Example1 folder.

Every VES simulation has three key ingredients:

- · Basis set
- Target distribution
- Optimization algorithm

For the basis set we will choose Legendre polynomials defined in the interval [0.23,0.7] nm. Legendre polynomials are a good choice for non-periodic CVs. A rule of thumb for choosing the order of the expansion is that an expansion of order N can capture features of the FES of approximately L/N where L is the length of the interval. In this case, an order of 10 is able to capture features of the order of around 0.05 nm. We will see afterwards that the order of the expansion is not critical as long as we obtain good sampling at convergence. If this is the case, it is possible to obtain finer features of the FES through reweighting. The syntax for this basis set in Plumed is:

```
BF_LEGENDRE ...
ORDER=10
INTERVAL_MIN=0.23
INTERVAL_MAX=0.8
LABEL=bf1
... BF_LEGENDRE
```

We will use a uniform target distribution:

$$p(\mathbf{s}) = 1/C$$

with C a normalization constant. Once that  $\Omega[V]$  is minimized, the bias potential satisfies (up to an arbitrary constant):

$$V(\mathbf{s}) = -F(\mathbf{s})$$

This is the same relation that holds for non-tempered metadynamics.

The syntax for the bias potential in Plumed is:

```
VES_LINEAR_EXPANSION ...

ARG=d1

BASIS_FUNCTIONS=bf1

GRID_BINS=300

TARGET_DISTRIBUTION={UNIFORM}

LABEL=b1
... VES_LINEAR_EXPANSION
```

Finally we have to choose the optimization algorithm. The standard is the averaged stochastic gradient descent. One has to define two parameters: the stride and the step size. The stride is the number of steps in which samples are collected to calculate the gradient and hessian of  $\Omega[V]$  and the step size is the step by which the coefficients are evolved at every optimization steps. Both of this parameters are connected. Increasing the stride will have an effect similar to reducing the step size. It has become traditional to choose a stride of around 500-2000 steps. It must be noted that we are not looking for an accurate estimation of the gradient, since for this we would need to sample all the CV space. The step size in the optimization has a strong connection with the height of typical barriers in the system. The larger the barriers, the larger the step size needed such that the bias can grow fast enough to overcome them. For this example we have chosen a stride of 500 steps and a step size of 0.5 kJ/mol. The syntax in Plumed is:

```
AVERAGED_SGD ...
BIAS=b1
STRIDE=500
LABEL=o1
STEPSIZE=0.5
FES_OUTPUT=100
BIAS_OUTPUT=500
COEFFS_OUTPUT=10
```

Now that we have set the scene, we can run our simulation using the run.sh script in the Example1 folder. The simulation will produce several files:

- · COLVAR: Just as in the metadynamics example.
- coeffs.data : Values of the coefficients  $\alpha$  and  $\bar{\alpha}$  .
- bias.<bission-number>.iter-<iteration-number>: Bias potential as a function of s at iteration <iteration-number>.

- fes.<br/>bias-name>.iter-<iteration-number> : FES at iteration <iteration-number>.
- targetdistribution.<br/>
  <br/>bias-name>.data : Target distribution.

4.4467081175713474e-03

-1.1504176822089783e-01

You can first observe how the system moves in the CV space in a fashion similar to metadynamics. Then we can see the evolution of  $\alpha$  and  $\bar{\alpha}$ . The first lines of the file coeffs.data are:

```
#! FIELDS idx_dl bl.coeffs bl.aux_coeffs index
#! SET time 0.000000
#! SET iteration 0
#! SET type LinearBasisSet
#! SET ndimensions 1
#! SET ncoeffs total 11
#! SET shape_d1 11
                0.00000000000000000e+00
                                               0.00000000000000000e+00
      0
                                                                             0
                0.00000000000000000e+00
                                               0.00000000000000000e+00
      1
                                                                             1
      2
                0.00000000000000000e+00
                                               0.0000000000000000e+00
                                                                             2
      3
                0.00000000000000000e+00
                                               0.00000000000000000e+00
                                                                             3
                0.00000000000000000e+00
                                               0.0000000000000000e+00
                                                                             4
      4
      5
                0.00000000000000000e+00
                                               0.00000000000000000e+00
                                                                             5
                0.0000000000000000e+00
                                               0.0000000000000000e+00
                                                                             6
       6
      7
                0.00000000000000000e+00
                                               0.0000000000000000e+00
                                                                             7
                                               0.00000000000000000e+00
                                                                             8
      8
                0.0000000000000000e+00
      9
                0.00000000000000000e+00
                                               0.0000000000000000e+00
                                                                             9
     10
                0.0000000000000000e+00
                                               0.0000000000000000e+00
                                                                            10
#! FIELDS idx_d1 b1.coeffs b1.aux_coeffs index
#! SET time 10.000000
#! SET iteration 10
#! SET type LinearBasisSet
#! SET ndimensions 1
#! SET ncoeffs_total
#! SET shape_d1 11
                                              0.00000000000000000e+00
                0
      Ω
      1
                5.1165453234702052e-01
                                               1.1482045941475065e+00
               -1.0356798763597277e+00
                                              -1.7365051185667855e+00
      2.
      3
               -5.1830527698835660e-01
                                              -1.1651638070736938e+00
                                                                             3
                4.1754103138162207e-01
                                               4.8203393927719917e-01
                                                                             4
      5
                3.2087945211009694e-01
                                               6.6606116920677805e-01
                                                                             5
               -1.5499943980403830e-01
                                              -4.7946750842365812e-03
                                                                             6
       6
                -1.1433825688016251e-01
                                              -1.5099503286093419e-01
                                                                             7
                                                                             8
      8
                9.8787914656136719e-02
                                               1.3156529595420300e-02
```

The first column are the coefficient indices, the second are the  $\bar{\alpha}$ , and the third are the  $\alpha$ . Each block in the file corresponds to a different iteration, in this case iteration 0 and 10. We can plot the evolution of the coefficients using the gnuplot script plotCoeffs.gpi . The output should be similar to the next figure.

-8.7160339645570323e-02

-1.5789737594248379e-01

9

10

The  $\alpha$  change fast and oscillate around some mean value. The  $\bar{\alpha}$  evolve smoothly until they stabilize around some equilibrium value. It is important to remember that the bias is a function of  $\bar{\alpha}$  and since these evolve smoothly, so will the bias. Once that the  $\bar{\alpha}$  have stabilized, the simulation can be considered converged.

It is also interesting to observe how the estimation of the FES evolves in time. For this we will plot the FES using the files fes.b1.iter-<iteration-number>. There is a gnuplot script plotFes.gpi that you can use for this purpose. At variance with metadynamics, in this case there is no growing offset in the bias and therefore we will have to shift the FES ourselves to distinguish several FES at different times in the same plot.

We can also calculate the height of the barrier as we did in the metadynamics tutorial. The files for carrying out this task can be found in the Barrier\_calculation folder. Remember that the accuracy of this calculation is limited by the fact that we have chosen a small order in the basis set expansion. We will discuss this aspect in greater detail in the next example.

9

10

#### 8.2.3.4.3 Example 2: Target distributions and basis sets

In this example we will consider other choices of target distributions and we will understand the influence of the order of the basis set expansion. The files needed for this example are contained in the directory Example2. Instead of introducing a barrier as done in the example above, in this case we will use a uniform target distribution in the interval [0.23:0.6] nm and decaying to zero in the interval [0.6:0.8] nm. The expression is:

$$p(s) = \{ 1C \text{ if } s < s_0 \frac{1}{C} e^{-\frac{(s-s_0)^2}{2\sigma^2}} \text{ if } s > s_0 \}$$

where  $s_0 = 0.6$  nm and  $\sigma = 0.05$ . To define this p(s) in Plumed the input is:

```
VES_LINEAR_EXPANSION ...

ARG=d1

BASIS_FUNCTIONS=bf1

LABEL=b1

TEMP=300.0

GRID_BINS=300

TARGET_DISTRIBUTION={UNIFORM MINIMA=0.23 MAXIMA=0.6 SIGMA_MAXIMA=0.05}}
... VES_LINEAR_EXPANSION
```

We will choose a basis set of order 20 to be able to capture the features of the FES with detail. If you are doing this example in a group, each member of the group can choose a different order in the expansion, for instance 5, 10, 20, and 40. The syntax in Plumed is:

```
BF_LEGENDRE ...
ORDER=20
INTERVAL_MIN=0.23
INTERVAL_MAX=0.8
LABEL=bf1
... BF_LEGENDRE
```

Once that you start running the simulation, a file named targetdist.b1.data will be created. This file contains the chosen target distribution. We can plot it to confirm that it is what we are looking for. There is a gnuplot script plotTargetDistrib.gpi that creates the following plot.

As the simulation runs, it is useful to control the evolution of the coefficients using the gnuplot script plotCoeffs.gpi.

The FES is calculated from the expression:

$$F(\mathbf{s}) = -V(\mathbf{s}) - \frac{1}{\beta} \log p(\mathbf{s}) = \{ -V(s) \text{ if } s < s_0 - V(s) + \frac{(s - s_0)^2}{2\beta\sigma^2} \text{ if } s > s_0 \}$$

In other words the bias potential is forced to create the upper barrier that we were explicitly introducing in the first example. When the FES is calculated the effect of the barrier is "subtracted" through p(s) and therefore the FES that we calculate does not include the barrier. This can be seen by plotting the fes.b1.iter-<iteration-number> files with gnuplot, for instance:

```
pl "./fes.bl.iter-10000.data" u 1:2 w l
```

This plot should be similar to the next figure.

Only the interval [0.23:0.7] is plotted since there is little sampling in the region [0.7:0.8] due to the small value of p(s) in this region. As discussed before, if there is no sampling, it is not possible to obtain free energies.

When the simulation ends, it is interesting to check if in fact the sampled biased distribution is equal to the chosen target distribution. The scripts to calculate the sampled biased distribution are located in the directory Biased Distribution. As usual, we will disregard the initial part of the simulation since in this period the bias is changing a lot. As done before, we get rid of the first 2 ns of simulation using sed:

```
sed '2,10000d' ../COLVAR > COLVAR
```

Once that the coefficients in the expansion have stabilized it is possible to calculate the biased distribution of CVs by constructing a histogram with equal weights for all points. This distribution should be equal to the target distribution p(s). The histogram can be calculated in plumed using the following input in the plumed dat file:

```
distance: READ FILE=COLVAR IGNORE_TIME VALUES=d1

HISTOGRAM ...

ARG=distance
GRID_MIN=0.2
GRID_MAX=0.8
GRID_BIN=100
BANDWIDTH=0.004
LABEL=hh1
... HISTOGRAM

DUMPGRID GRID=hh1 FILE=histo FMT=%24.16e

and running (or using the run.sh script):

plumed --no-mpi driver --plumed plumed.dat --noatoms > plumed.out
```

The next plot shows that in fact the sampled distribution agrees with the target distribution.

Once that the coefficients are stabilized it is possible to reweight using the standard umbrella sampling formula ? . In this case the weight assigned to each configuration is:

$$w(\mathbf{R}) \propto e^{\beta V(\mathbf{s})}$$
.

The files needed for this reweighting are contained in the folder ReweightDistance. The procedure to the the reweighting and plot the results is similar to the ones in the cases above and therefore it is not described in detail. The reweighted FES is plotted in the next figure and compared to the FES calculated from the formula  $V(\mathbf{s}) = -F(\mathbf{s}) - \frac{1}{\beta} \log p(\mathbf{s})$ 

The two curves do not differ much since the order of the expansion was relatively large. What happens if you chose a lower or higher order in the expansion?

# 8.2.3.4.4 Restarting a simulation

In this section we will restart the simulation that we have performed in our second example. In directory Example2, cd to the folder Restart. To restart the simulation we will need:

- LAMMPS restart file, since it stores the last configuration
- · COLVAR file, since new lines will be appended
- · coeff.data file, containing the iteration number and the values of the coefficients.

Therefore we execute in the command line the following commands:

```
cp ../restart .
cp ../COLVAR .
cp ../coeffs.data .
```

In order to restart, the RESTART keyword must be added at the beginning of Plumed's input named plumed. ← restart.dat:

```
RESTART
dl: DISTANCE ATOMS=319,320
.
.
```

Then the simulation can be restarted using the script runRestart.sh. Check that the output of the new simulation is appended to the COLVAR file, that the starting time of the new simulation is the ending time of the old simulation, that CV values are coherent, and that coefficients evolve continuously.

#### 8.2.3.4.5 Gaussian target distribution

As an exercise, you can use a target distribution consisting in a gaussian centered at the dissociation barrier. The syntax in Plumed is:

```
VES_LINEAR_EXPANSION ...

ARG=d1

BASIS_FUNCTIONS=bf1

LABEL=b1

TEMP=300.0

GRID_BINS=300

TARGET_DISTRIBUTION={GAUSSIAN CENTER=0.325 SIGMA=0.03}
... VES_LINEAR_EXPANSION
```

Gaussian target distributions are useful to focus the sampling on a particular region of CV space. This has been used in protein folding problems to focus the sampling on the small but relevant folded state ?.

# 8.2.3.4.6 Optimization algorithm

We suggest an exercise to gain experience in choosing the parameters of the optimization algorithm. The averaged stochastic gradient descent algorithm has two parameters: the stride and the step size. Normally a stride of around 500-2000 steps is used. However it is not always easy to choose the step size. Luckily, the algorithm is quite robust and will work for different step sizes.

Run different simulation using step sizes  $\mu=0.001$  and  $\mu=10$  and try to rationalize the behavior. Normally, when the step size is too large, the system gets stuck in CV space and coefficients oscillate wildly. When the step size is too small, the algorithm runs out of "steam" too fast and the simulation converges slowly. These two extreme cases should be avoided.

#### 8.2.3.5 Final remarks

The purpose of this first tutorial was to introduce the student to VES. At this point one can see that VES is a powerful and versatile enhanced sampling method. We suggest to explore different possibilities of basis sets and target distributions. It is also interesting to experiment with different optimization algorithms and parameters of these.

The next tutorial will deal with the use of the well-tempered target distribution and the construction of biases on 2 CVs.

# 8.2.4 MARVEL-VES tutorial (Lugano 2017): VES 2

### 8.2.4.1 Learning Outcomes

Once this tutorial is completed students will learn to:

- · Use the well-tempered target distribution and understand its usefulness
- · Construct biases in 1 and 2 dimensions.

#### 8.2.4.2 Resources

The tarball for this project contains the following folders:

- Example1 : Contains the input file for the the first example.
- Example2: Contains the input file for the the second example.

### 8.2.4.3 Summary of theory

One of the most useful target distribution is the well-tempered one. The well-tempered target distribution is ?:

$$p(\mathbf{s}) = \frac{e^{-(\beta/\gamma)F(\mathbf{s})}}{\int d\mathbf{s} \, e^{-(\beta/\gamma)F(\mathbf{s})}}$$

where  $\gamma$  is the so-called bias factor. It is possible to show that:

$$p(\mathbf{s}) = \frac{[P(\mathbf{s})]^{1/\gamma}}{\int d\mathbf{s} [P(\mathbf{s})]^{1/\gamma}}$$

where  $P(\mathbf{s})$  is the unbiased distribution of CVs. Therefore the target distribution is the unbiased distribution with enhanced fluctuations and lowered barriers. This is the same distribution as sampled in well-tempered metadynamics. The advantages of this distribution are that the features of the FES (metastable states) are preserved and that the system is not forced to sample regions of high free energy as it would if we had chosen the uniform target distribution. This is specially important when biasing 2 CVs and there are large regions of very high free energy and therefore they represent unphysical configurations.

There is a caveat though, p(s) depends on F(s) that is the function that we are trying to calculate. One way to approach this problem is to calculate p(s) self-consistently ?, for instance at iteration k:

$$p^{(k+1)}(\mathbf{s}) = \frac{e^{-(\beta/\gamma)F^{(k+1)}(\mathbf{s})}}{\int d\mathbf{s} \, e^{-(\beta/\gamma)F^{(k+1)}(\mathbf{s})}}$$

where:

$$F^{(k+1)}(\mathbf{s}) = -V^{(k)}(\mathbf{s}) - \frac{1}{\beta} \log p^{(k)}(\mathbf{s})$$

Normally  $p^{(0)}(\mathbf{s})$  is taken to be uniform. Therefore the target distribution evolves in time until it becomes stationary when the simulation has converged. It has been shown that in some cases the convergence is faster using the well-tempered target distribution than using the uniform  $p(\mathbf{s})$ ?

8.2.4.4 Instructions

#### 8.2.4.4.1 The system

We will consider the same system employed in previous tutorials.

#### 8.2.4.4.2 Example 1: Enhancing fluctuations

We consider Example 2 of the VES 1 tutorial. In that case we used a uniform target distribution that at some value decayed to zero. In this case we will use a product of two distributions:

$$p(s) = \frac{p_{\text{WT}}(s) \, p_{\text{barrier}}(s)}{\int ds \, p_{\text{WT}}(s) \, p_{\text{barrier}}(s)}$$

where  $p_{WT}(s)$  is the well-tempered target distribution and:

$$p_{\text{barrier}}(s) = \{ 1C \text{ if } s < s_0 \frac{1}{C} e^{-\frac{(s-s_0)^2}{2\sigma^2}} \text{ if } s > s_0 \}$$

with  ${\cal C}$  a normalization factor. The files needed for this exercise are in the directory Example 1. This target distribution can be specified in plumed using:

As usual, we run the example using the run.sh script. As the simulation progresses we can track the evolution of the target distribution. At variance with previous simulations where p(s) was stationary, in this case it evolves in time. The p(s) is dumped every 500 steps in a file named targetdist.b1.iter-<iteration-number>.data. You can plot these files manually or using the script plotTargetDistrib.gpi. The result should be similar to the following plot where the distribution at different times has been shifted to see more clearly the difference.

To shed some light on the nature of the well-tempered target distribution, we will compare the unbiased and biased distribution of CVs. The unbiased distribution of CVs P(s) is calculated by constructing a histogram of the CVs with weights given by:

$$w(\mathbf{R}) \propto e^{\beta V(\mathbf{s})}$$
.

The biased distribution of CVs p'(s) is calculated also by constructing a histogram of the CVs but in this case each point is assigned equal weights. The prime is added in p'(s) to distinguish the biased distribution from the target distribution p(s). If the simulation has converged then p'(s) = p(s). The files needed for this calculation are located in the Reweight directory. Since this simulation converges fast as compared to previous ones, we only disregard the first 1 ns of simulation:

```
sed '2,5000d' ../COLVAR > COLVAR
```

To calculate the biased and unbiased distribution of CVs we use the following Plumed's input:

```
distance: READ FILE=COLVAR IGNORE_TIME VALUES=d1 ves: READ FILE=COLVAR IGNORE_TIME VALUES=b1.bias weights: REWEIGHT_BIAS TEMP=300 ARG=ves.bias

HISTOGRAM ...
ARG=distance
GRID_MIN=0.23
GRID_MAX=0.8
GRID_BIN=301
BANDWIDTH=0.006
LABEL=hh1
```

```
... HISTOGRAM

HISTOGRAM ...

ARG=distance

GRID_MIN=0.23

GRID_MAX=0.8

GRID_BIN=301

BANDWIDTH=0.006

LOGWEIGHTS=weights

LABEL=hh2

... HISTOGRAM

DUMPGRID GRID=hh1 FILE=histo_biased FMT=%24.16e

DUMPGRID GRID=hh2 FILE=histo_unbiased FMT=%24.16e
```

If you do not understand what this input does, you might want to read once again the previous tutorials. The histograms histo\_biased and histo\_unbiased correspond to p'(s) and P(s), respectively. We are interested in comparing the unbiased distribution of CVs P(s) and the well-tempered distribution  $p_{\mathrm{WT}}(s)$ . We know from the equations above that:

$$p_{\rm WT}(s) \propto [P(\mathbf{s})]^{1/\gamma},$$

and also,

$$p_{\rm WT}(s) \propto p(s)/p_{\rm barrier}(s) \propto p'(s)/p_{\rm barrier}(s)$$
.

Therefore we have two ways to calculate the well-tempered target distribution. We can compare P(s) and the well-tempered target distribution calculated in two ways with the following gnuplot lines:

```
biasFactor=5.
invBiasFactor=1./biasFactor
pl "./histo_unbiased" u 1:(-log($2)) w l title "P(s)"
repl "./histo_unbiased" u 1:(-log($2**invBiasFactor)) w l title "[P(s)]^(1/gamma)"
repl "< paste ./histo_biased ../targetdist.bl.iter-0.data" u 1:(-log($2/$5)) w l title "Sampled p(s)"</pre>
```

There is also a gnuplot script plot.gpi that should do everything for you. The output should be similar to the next plot where we plot the negative logarithm of the distributions.

Notice that as expected both equations to calculate  $p_{WT}(s)$  agree. Also the association barrier of  $5~k_BT$  becomes of  $1~k_BT$  when the well-tempered target distribution is sampled.

The take home message of this tutorial is that when the well-tempered target distribution is employed, the biased distribution of CVs preserves all the features of the unbiased distribution, but barriers are lowered. Equivalently one may say that fluctuations are enhanced.

# 8.2.4.4.3 Example 2: Constructing a 2 dimensional bias

In this example we will construct a 2 dimensional bias on the distance Na-Cl and the coodrination number of Na with respect to O. The files to run this example are included in the Example2 folder. Two dimensional biases in VES can be written:

$$V(s_1, s_2; \alpha) = \sum_{i_1, i_2} \alpha_{i_1, i_2} f_{i_1}(s_1) f_{i_2}(s_2),$$

where  $f_{i_1}(s_1)$  and  $f_{i_2}(s_2)$  are the basis functions. We will choose to expand the bias potential in Legendre polynomials up to order 20 in both dimensions.

```
# CV1
BF_LEGENDRE ...
ORDER=20
INTERVAL_MIN=0.23
INTERVAL_MAX=0.8
LABEL=bf1
... BF_LEGENDRE
# CV2
BF_LEGENDRE ...
ORDER=20
INTERVAL_MIN=2.5
INTERVAL_MAX=7.5
LABEL=bf2
... BF_LEGENDRE
```

We have chosen the interval [0.23,0.8] nm for the distance and [2.5,7.5] for the coordination number. The total number of non-zero coefficients will be 400. In the coefficients file the indices  $i_1$  and  $i_2$  are given by the first two columns. We use the well-tempered target distribution together with a barrier at 0.6 nm on the distance Na-Cl.

```
VES_LINEAR_EXPANSION ...

ARG=d1,coord

BASIS_FUNCTIONS=bf1,bf2

LABEL=b1

TEMP=300.0

GRID_BINS=300,300

TARGET_DISTRIBUTION={PRODUCT_COMBINATION}

DISTRIBUTION1={UNIFORM}

MINIMA=0.2,2.5

MAXIMA=0.6,7.5

SIGMA_MAXIMA=0.05,0.}

DISTRIBUTION2={WELL_TEMPERED}

BIASFACTOR=5}}

... VES LINEAR EXPANSION
```

We can now run the simulation and control its progress. Since there are 400 coefficients we choose the largest (in absolute value) to control the convergence of the simulation. In this case we have chosen coefficients with indices  $(i_1,i_2)$  as (1,0), (0,1), (1,1), (2,1), and (0,2). You can plot the evolution of the coefficients using the gnuplot script plotCoeffs.gpi. This plot should look similar to the following one. The bias therefore converges smoothly as in one dimensional problems.

The estimated FES can also be plotted to control the progress of the simulation. For instance in gnuplot,

```
set xr [0.23:0.7]
set yr [3:7]
set zr [0:6]
set cbr [0:6]
set pm3d map
temp=2.494
spl "./fes.bl.iter-1000.data" u 1:2:($3/temp) w pm3d notitle
```

There is a gnuplot script plotFes.gpi that generates the following plot for the FES after 10 ns of simulation:

This FES agrees with that calculated through reweighting in the metadynamics tutorial.

As an exercise, you can repeat this simulation using the uniform target distribution instead of the well-tempered p(s). Compare the convergence time of both simulations. Discuss the reasons why the algorithm converges faster to the well-tempered target distribution than to the uniform one. Does it make sense to sample all the CV space uniformly?

# 8.2.4.5 Final remarks

At this point the student has acquired experience with several characteristics of the VES method. There is one tool that has proven to be instrumental for many problems and that has not yet been discussed in this series of tutorials: the use of multiple walkers. This tool will be the subject of another tutorial.

# 8.3 Bias

The following list contains the biases available in the VES code.

VES LINEAR EXPANSION | Linear basis set expansion bias.

8.3 Bias 393

### 8.3.1 VES\_LINEAR\_EXPANSION

Linear basis set expansion bias.

This bias action takes the bias potential to be a linear expansion in some basis set that is written as a product of one-dimensional basis functions. For example, for one CV the bias would be written as

$$V(s_1; \alpha) = \sum_{i_1} \alpha_{i_1} f_{i_1}(s_1),$$

while for two CVs it is written as

$$V(s_1, s_2; \alpha) = \sum_{i_1, i_2} \alpha_{i_1, i_2} f_{i_1}(s_1) f_{i_2}(s_2)$$

where  $\alpha$  is the set of expansion coefficients that are optimized within VES. With an appropriate choice of the basis functions it is possible to represent any generic free energy surface. The relationship between the bias and the free energy surface is given by

$$V(\mathbf{s}) = -F(\mathbf{s}) - \frac{1}{\beta} \log p(\mathbf{s}).$$

where  $p(\mathbf{s})$  is the target distribution that is employed in the VES simulation.

**Basis Functions** 

Various one-dimensional basis functions are available in the VES code, see the complete list here. At the current moment we recommend to use legendre polynomicals for non-periodic CVs and Fourier basis functions for periodic CV (e.g. dihedral angles).

To use these basis functions within VES\_LINEAR\_EXPANSION do you first need to define them in the input file before the VES\_LINEAR\_EXPANSION action and then give their labels using the BASIS\_FUNCTIONS keyword.

**Target Distributions** 

The default option is to employ a uniform target distribution. Various other target distributions  $p(\mathbf{s})$  are available in the VES code, see the complete list here. To use any of these target distribution you need to use the TARGET\_ $\leftarrow$  DISTRIBUTION keyword where the keyword relevant to the target distribution are enclosed within curly brackets.

**Description of components** 

By default this Action calculates the following quantities. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Description  |
|----------|--|
| bias     | the instantaneous value of the bias potential                            |
| force2   | the instantaneous value of the squared force due to this bias potential. |

Compulsory keywords

| BASIS_FUNCTIONS | the label of the basis sets that you want to use |
|-----------------|--|
|-----------------|--|

# **Options**

| NUMERICAL_DERIVATIVES    | ( default=off ) calculate the derivatives for these quantities numerically  |
|--------------------------|---|
| TEMP                     | the system temperature - this is needed if the MD code does not pass the temperature to PLUMED.   |
| BIAS_FILE                | filename of the file on which the bias should be written out. By default it is bias.LABEL.data. Note that suffixes indicating the iteration number (iter-#) are added to the filename when optimizing coefficients.   |
| FES_FILE                 | filename of the file on which the FES should be written out. By default it is fes.LABEL.data. Note that suffixes indicating the iteration number (iter-#) are added to the filename when optimizing coefficients.   |
| TARGETDIST_FILE          | filename of the file on which the target distribution should be written out. By default it is targetdist.LABEL.data. Note that suffixes indicating the iteration number (iter-#) are added to the filename when optimizing coefficients.  |
| COEFFS                   | read-in the coefficents from files.   |
| TARGET_DISTRIBUTION      | the target distribution to be used. See the list in Target Distributions  |
| BIAS_CUTOFF              | cutoff the bias such that it only fills the free energy surface up to certain level F_cutoff, here you should give the value of the F_cutoff.   |
| BIAS_CUTOFF_FERMI_LAMBDA | the lambda value used in the Fermi switching function for the bias cutoff (BIAS_CUTOFF). Lambda is by default 1.0.  |
| GRID_BINS                | the number of bins used for the grid. The default value is 100 bins per dimension.  |
| PROJ_ARG                 | arguments for doing projections of the FES or the target distribution. You can use multiple instances of this keyword i.e. PROJ_ARG1, PROJ_A← RG2, PROJ_ARG3  |
| ARG                      | the input for this action is the scalar output from one or more other actions. The particular scalars that you will use are referenced using the label of the action. If the label appears on its own then it is assumed that the Action calculates a single scalar value. The value of this scalar is thus used as the input to this new action. If * or *.* appears the scalars calculated by all the proceding actions in the input file are taken. Some actions have multi-component outputs and each component of the output has a specific label. For example a DISTANCE action labelled dist may have three componets x, y and z. To take just the x component you should use dist.x, if you wish to take all three components then use dist.*.More information on the referencing of Actions can be found in the section of the manual on the PLUMED Getting started. Scalar values can also be referenced using POSIX regular expressions as detailed in the section on Regular Expressions. To use this feature you you must compile PLUMED with the appropriate flag. You can use multiple instances of this keyword i.e. ARG1, ARG2, ARG3 |

# Examples

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### 8.4 Basis functions

The following list contains the one-dimensional basis functions available in the VES code.

| BF_CHEBYSHEV | Chebyshev polynomial basis functions. |
|--------------|---------------------------------------|
| BF_COMBINED  | Combining other basis functions types |
| BF_COSINE    | Fourier cosine basis functions.       |
| BF_FOURIER   | Fourier basis functions.              |
| BF_LEGENDRE  | Legendre polynomials basis functions. |
| BF_POWERS    | Polynomial power basis functions.     |
| BF_SINE      | Fourier sine basis functions.         |

### 8.4.1 BF\_CHEBYSHEV

Chebyshev polynomial basis functions.

Use as basis functions Chebyshev polynomials of the first kind  $T_n(x)$  defined on a bounded interval. You need to provide the interval [a,b] on which the basis functions are to be used, and the order of the expansion N (i.e. the highest order polynomial used). The total number of basis functions is N+1 as the constant  $T_0(x)=1$  is also included. These basis functions should not be used for periodic CVs.

Intrinsically the Chebyshev polynomials are defined on the interval [-1,1]. A variable t in the interval [a,b] is transformed to a variable x in the intrinsic interval [-1,1] by using

$$x(t) = \frac{t - (a+b)/2}{(b-a)/2}$$

The Chebyshev polynomials are given by the recurrence relation  $T_0(x) = 1$ 

$$T_1(x) = x$$
  
 $T_{n+1}(x) = 2 x T_n(x) - T_{n-1}(x)$ 

The first 6 polynomials are shown below

The Chebyshev polynomial are orthogonal over the interval [-1,1] with respect to the weight  $\frac{1}{\sqrt{1-x^2}}$ 

$$\int_{-1}^{1} dx \, T_n(x) \, T_m(x) \, \frac{1}{\sqrt{1-x^2}} = \{ \, 0 \, \, n \neq m\pi n = m = 0\pi/2n = m \neq 0 \, \}$$

For further mathematical properties of the Chebyshev polynomials see for example the Wikipedia page.

Compulsory keywords

| ORDER        | The order of the basis function expansion.                            |
|--------------|---|
| INTERVAL_MIN | The minimum of the interval on which the basis functions are defined. |
| INTERVAL_MAX | The maximum of the interval on which the basis functions are defined. |

| DEBUG_INFO          | ( default=off ) Print out more detailed information about the basis set. Useful for debugging.                    |
|---------------------|---|
| NUMERICAL_INTEGRALS | ( default=off ) Calculate basis function integral for the uniform distribution numerically. Useful for debugging. |

Here we employ a Chebyshev expansion of order 20 over the interval 0.0 to 10.0. This results in a total number of 21 basis functions. The label used to identify the basis function action can then be referenced later on in the input file

bfC: BF\_CHEBYSHEV INTERVAL\_MIN=0.0 INTERVAL\_MAX=10.0 ORDER=20

## 8.4.2 BF\_COMBINED

Combining other basis functions types

Compulsory keywords

| BASIS_FUNCTIONS | Labels of the basis functions that should be combined. Note that the order used matters |
|-----------------|---|
|                 | for the ordering of the basis functions. This needs to be kept in mind when restarting  |
|                 | from previous coefficients.   |

## **Options**

| DEBUG_INFO | ( default=off ) Print out more detailed information about the basis set. Useful for debugging.                 |
|------------|--|
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#### **Examples**

Here we define both Fourier cosine and sine expansions of order 10, each with 11 basis functions, which are combined. This results in a total number of 21 basis functions as only the constant from is bf\_cos is used.

```
bf_cos: BF_COSINE INTERVAL_MIN=-pi INTERVAL_MAX=+pi ORDER=10 bf_sin: BF_SINE INTERVAL_MIN=-pi INTERVAL_MAX=+pi ORDER=10 bf_comb: BF_COMBINED BASIS_FUNCTIONS=bf_cos,bf_sin
```

In principle this is the same as using BF\_FOURIER with ORDER=10 but with different ordering of the basis functions. Note that the order used in BASIS\_FUNCTIONS matters for the ordering of the basis functions, using BAS IS\_FUNCTIONS=bf\_sin,bf\_cos would results in a different order of the basis functions. This should be kept in mind when restarting from previous coefficients.

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## 8.4.3 BF\_COSINE

Fourier cosine basis functions.

Use as basis functions Fourier cosine series defined on a periodic interval. You need to provide the periodic interval [a,b] on which the basis functions are to be used, and the order of the expansion N (i.e. the highest Fourier cosine mode used). The total number of basis functions is N+1 as the constant  $f_0(x)=1$  is also included. These basis functions should only be used for periodic CVs. They can be useful if the periodic function being expanded is an even function, i.e. F(-x)=F(x).

```
The Fourier cosine basis functions are given by f_0(x)=1 f_1(x)=cos(\frac{2\pi}{P}x) f_2(x)=cos(2\cdot\frac{2\pi}{P}x) f_3(x)=cos(3\cdot\frac{2\pi}{P}x) \vdots f_n(x)=cos(n\cdot\frac{2\pi}{P}x) \vdots f_N(x)=cos(N\cdot\frac{2\pi}{P}x) where P=(b-a) is the periodicity of the interval.
```

#### Compulsory keywords

| ORDER        | The order of the basis function expansion.                            |
|--------------|---|
| INTERVAL_MIN | The minimum of the interval on which the basis functions are defined. |
| INTERVAL_MAX | The maximum of the interval on which the basis functions are defined. |

#### **Options**

| DEBUG_INFO          | ( default=off ) Print out more detailed information about the basis set. Useful for debugging.                    |
|---------------------|---|
| NUMERICAL_INTEGRALS | ( default=off ) Calculate basis function integral for the uniform distribution numerically. Useful for debugging. |

# Examples

Here we employ a Fourier cosine expansion of order 10 over the periodic interval  $-\pi$  to  $+\pi$ . This results in a total number of 11 basis functions. The label used to identify the basis function action can then be referenced later on in the input file.

```
BF_COSINE INTERVAL_MIN=-pi INTERVAL_MAX=+pi ORDER=10 LABEL=bf1
```

## 8.4.4 BF\_FOURIER

Fourier basis functions.

Use as basis functions Fourier series defined on a periodic interval. You need to provide the periodic interval [a,b] on which the basis functions are to be used, and the order of the expansion N (i.e. the highest Fourier mode used). The total number of basis functions is 2N+1 as for each Fourier mode there is both the cosine and sine term, and the constant  $f_0(x)=1$  is also included. These basis functions should only be used for periodic CVs.

```
The Fourier series basis functions are given by f_0(x)=1 f_1(x)=cos(\frac{2\pi}{P}x) f_2(x)=sin(\frac{2\pi}{P}x) f_3(x)=cos(2\cdot\frac{2\pi}{P}x) f_4(x)=sin(2\cdot\frac{2\pi}{P}x) \vdots \vdots f_{2n-1}(x)=cos(n\cdot\frac{2\pi}{P}x) \vdots \vdots f_{2n-1}(x)=sin(n\cdot\frac{2\pi}{P}x) \vdots \vdots f_{2N-1}(x)=cos(N\cdot\frac{2\pi}{P}x) \vdots f_{2N-1}(x)=cos(N\cdot\frac{2\pi}{P}x) where P=(b-a) is the periodicity of the interval.
```

#### Compulsory keywords

| ORDER        | The order of the basis function expansion.                            |
|--------------|---|
| INTERVAL_MIN | The minimum of the interval on which the basis functions are defined. |
| INTERVAL_MAX | The maximum of the interval on which the basis functions are defined. |

#### **Options**

| DEBUG_INFO          | ( default=off ) Print out more detailed information about the basis set. Useful for debugging.                    |
|---------------------|---|
| NUMERICAL_INTEGRALS | ( default=off ) Calculate basis function integral for the uniform distribution numerically. Useful for debugging. |

## **Examples**

Here we employ a Fourier expansion of order 10 over the periodic interval  $-\pi$  to  $+\pi$ . This results in a total number of 21 basis functions. The label used to identify the basis function action can then be referenced later on in the input file.

```
BF_FOURIER INTERVAL_MIN=-pi INTERVAL_MAX=+pi ORDER=10 LABEL=bf_fourier
```

### 8.4.5 BF\_LEGENDRE

Legendre polynomials basis functions.

Use as basis functions Legendre polynomials  $P_n(x)$  defined on a bounded interval. You need to provide the interval [a,b] on which the basis functions are to be used, and the order of the expansion N (i.e. the highest

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order polynomial used). The total number of basis functions is N+1 as the constant  $P_0(x)=1$  is also included. These basis functions should not be used for periodic CVs.

Intrinsically the Legendre polynomials are defined on the interval [-1,1]. A variable t in the interval [a,b] is transformed to a variable x in the intrinsic interval [-1,1] by using

$$x(t) = \frac{t - (a+b)/2}{(b-a)/2}$$

The Legendre polynomials are given by the recurrence relation  $P_0(x)=1$ 

$$P_1(x) = x$$

$$P_{n+1}(x) = \frac{2n+1}{n+1} x P_n(x) - \frac{n}{n+1} P_{n-1}(x)$$

The first 6 polynomials are shown below

The Legendre polynomial are orthogonal over the interval [-1, 1]

$$\int_{-1}^{1} dx \, P_n(x) \, P_m(x) = \frac{2}{2n+1} \delta_{n,m}$$

By using the SCALED keyword the polynomials are scaled by a factor of  $\sqrt{\frac{2n+1}{2}}$  such that they are orthonormal to 1.

From the above equation it follows that integral of the basis functions over the uniform target distribution  $p_{\rm u}(x)$  are given by

$$\int_{-1}^{1} dx P_n(x) p_{\mathbf{u}}(x) = \delta_{n,0},$$

and thus always zero except for the constant  $P_0(x) = 1$ .

For further mathematical properties of the Legendre polynomials see for example the Wikipedia page.

Compulsory keywords

| ORDER        | The order of the basis function expansion.                            |
|--------------|---|
| INTERVAL_MIN | The minimum of the interval on which the basis functions are defined. |
| INTERVAL_MAX | The maximum of the interval on which the basis functions are defined. |

**Options** 

| DEBUG_INFO          | ( default=off ) Print out more detailed information about the basis set. Useful for   |
|---------------------|---|
|                     | debugging.  |
| NUMERICAL_INTEGRALS | ( default=off ) Calculate basis function integral for the uniform distribution numer- |
|                     | ically. Useful for debugging.   |
| SCALED              | ( default=off ) Scale the polynomials such that they are orthonormal to 1.            |
|                     |   |

**Examples** 

Here we employ a Legendre expansion of order 20 over the interval -4.0 to 8.0. This results in a total number of 21 basis functions. The label used to identify the basis function action can then be referenced later on in the input file.

```
bf_leg: BF_LEGENDRE INTERVAL_MIN=-4.0 INTERVAL_MAX=8.0 ORDER=20
```

**Examples** 

#### 8.4.6 BF POWERS

Polynomial power basis functions.

#### Attention

These basis functions should not be used in conventional biasing simulations. Instead you should use orthogonal basis functions like Legendre or Chebyshev polynomials. They are only included for usage in md linear expansion and some special cases.

Basis functions given by polynomial powers defined on a bounded interval. You need to provide the interval [a,b] on which the basis functions are to be used, and the order of the expansion N (i.e. the highest power used). The total number of basis functions is N+1 as the constant  $f_0(x)=1$  is also included. These basis functions should not be used for periodic CVs.

```
The basis functions are given by f_0(x)=1 f_1(x)=x f_2(x)=x^2 \vdots f_n(x)=x^n \vdots f_N(x)=x^N
```

Note that these basis functions are **not** orthogonal. In fact the integral over the uniform target distribution blows up as the interval is increased. Therefore they should not be used in conventional biasing simulations. However, they can be useful for usage with md\_linearexpansion.

#### Compulsory keywords

| ORDER        | The order of the basis function expansion.                            |
|--------------|---|
| INTERVAL_MIN | The minimum of the interval on which the basis functions are defined. |
| INTERVAL_MAX | The maximum of the interval on which the basis functions are defined. |

| DEBUG_INFO    | ( default=off ) Print out more detailed information about the basis set. Useful for debugging. |
|---------------|--|
| NORMALIZATION | The normalization factor that is used to normalize the basis functions. By default it is 1.0.  |
|               |  |

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### **Examples**

Here we employ a polynomial power expansion of order 5 over the interval -2.0 to 2.0. This results in a total number of 6 basis functions. The label used to identify the basis function action can then be referenced later on in the input file

```
BF_POWERS INTERVAL_MIN=-2.0 INTERVAL_MAX=2.0 ORDER=5 LABEL=bf_pow
```

## 8.4.7 BF\_SINE

Fourier sine basis functions.

Use as basis functions Fourier sine series defined on a periodic interval. You need to provide the periodic interval [a,b] on which the basis functions are to be used, and the order of the expansion N (i.e. the highest Fourier sine mode used). The total number of basis functions is N+1 as the constant  $f_0(x)=1$  is also included. These basis functions should only be used for periodic CVs. They can be useful if the periodic function being expanded is an odd function, i.e. F(-x)=-F(x).

```
The Fourier sine basis functions are given by f_0(x) = 1
```

```
\begin{split} f_1(x) &= sin(\frac{2\pi}{P}x) \\ f_2(x) &= sin(2 \cdot \frac{2\pi}{P}x) \\ f_3(x) &= sin(3 \cdot \frac{2\pi}{P}x) \\ \vdots \\ f_n(x) &= sin(n \cdot \frac{2\pi}{P}x) \\ \vdots \\ f_N(x) &= sin(N \cdot \frac{2\pi}{P}x) \\ where & P = (b-a) \text{ is the periodicity of the interval.} \end{split}
```

#### Compulsory keywords

| ORDER        | The order of the basis function expansion.                            |
|--------------|---|
| INTERVAL_MIN | The minimum of the interval on which the basis functions are defined. |
| INTERVAL_MAX | The maximum of the interval on which the basis functions are defined. |

#### **Options**

| DEBUG_INFO          | ( default=off ) Print out more detailed information about the basis set. Useful for debugging.                    |
|---------------------|---|
| NUMERICAL_INTEGRALS | ( default=off ) Calculate basis function integral for the uniform distribution numerically. Useful for debugging. |

# **Examples**

Here we employ a Fourier sine expansion of order 10 over the periodic interval  $-\pi$  to  $+\pi$ . This results in a total number of 11 basis functions. The label used to identify the basis function action can then be referenced later on in the input file.

BF\_SINE INTERVAL\_MIN=-pi INTERVAL\_MAX=+pi ORDER=10 LABEL=bfS

**Examples** 

# 8.5 Target Distributions

The following list contains the target distributions available in the VES code.

| GAUSSIAN             | Target distribution given by a sum of Gaussians (static).   |
|----------------------|---|
| GRID_DIST            | Target distribution from an external grid file (static).  |
| LINEAR_COMBINATION   | Target distribution given by linear combination of distributions (static or dynamic).                 |
| MATHEVAL_DIST        | Target distribution given by a matheval parsed function (static or dynamic).                          |
| PRODUCT_COMBINATION  | Target distribution given by product combination of distributions (static or dynamic).                |
| PRODUCT_DISTRIBUTION | Target distribution given by a separable productof one-dimensional distributions (static or dynamic). |
| UNIFORM              | Uniform target distribution (static).   |
| VON_MISES            | Target distribution given by a sum of Von Mises distributions (static).                               |
| WELL_TEMPERED        | Well-tempered target distribution (dynamic).  |

## 8.5.1 GAUSSIAN

Target distribution given by a sum of Gaussians (static).

Employ a target distribution that is given by a sum of multivariate Gaussian (or normal) distributions, defined as

$$p(\mathbf{s}) = \sum_{i} w_{i} N(\mathbf{s}; \mu_{i}, \Sigma_{i})$$

where  $\mu_i = (\mu_{1,i}, \mu_{2,i}, \dots, \mu_{d,i})$  and  $\Sigma_i$  are the center and covariance matrix for the i-th Gaussian. The weights  $w_i$  are normalized to 1,  $\sum_i w_i = 1$ .

By default the Gaussian distributions are considered as separable into independent one-dimensional Gaussian distributions. In other words, the covariance matrix is taken as diagonal  $\Sigma_i = (\sigma_{1,i}^2, \sigma_{2,i}^2, \dots, \sigma_{d,i}^2)$ . The Gaussian distribution is then written as

$$N(\mathbf{s}; \mu_i, \sigma_i) = \prod_{k=1}^{d} \frac{1}{\sqrt{2\pi\sigma_{d,i}^2}} \exp\left(-\frac{(s_d - \mu_{d,i})^2}{2\sigma_{d,i}^2}\right)$$

where  $\sigma_i = (\sigma_{1,i}, \sigma_{2,i}, \dots, \sigma_{d,i})$  is the standard deviation. In this case you need to specify the centers  $\mu_i$  using the numbered CENTER keywords and the standard deviations  $\sigma_i$  using the numbered SIGMA keywords.

For two arguments it is possible to employ bivariate Gaussians with correlation between arguments, defined as

$$N(\mathbf{s}; \mu_i, \sigma_i, \rho_i) = \frac{1}{2\pi\sigma_{1,i}\sigma_{2,i}\sqrt{1-\rho_i^2}} \exp\left(-\frac{1}{2(1-\rho_i^2)} \left[ \frac{(s_1 - \mu_{1,i})^2}{\sigma_{1,i}^2} + \frac{(s_2 - \mu_{2,i})^2}{\sigma_{2,i}^2} + \frac{2\rho_i(s_1 - \mu_{1,i})(s_2 - \mu_{2,i})}{\sigma_{1,i}\sigma_{2,i}} \right] \right)$$

where  $\rho_i$  is the correlation between  $s_1$  and  $s_2$  that goes from -1 to 1. A value of 0 means that the arguments are considered as un-correlated, which is the default behavior. In this case the covariance matrix is given as

$$\Sigma = \left[ \begin{array}{cc} \sigma_{1,i}^2 & \rho_i \sigma_{1,i} \sigma_{2,i} \\ \rho_i \sigma_{1,i} \sigma_{2,i} & \sigma_{2,i}^2 \end{array} \right]$$

For the bivariate Gaussians the correlation  $\rho$  is given using the numbered CORRELATION keywords.

The Gaussian distributions are always defined with the conventional normalization factor such that they are normalized to 1 over an unbounded region. However, in calculation within VES we normally consider bounded region on which the target distribution is defined. Thus, if the center of a Gaussian is close to the boundary of the region it can happen that the tails go outside the region. In that case it might be needed to use the NORMALIZE keyword to make sure that the target distribution is properly normalized to 1 over the bounded region. The code will issue a warning if that is needed.

For periodic CVs it is generally better to use Von Mises distributions instead of Gaussians as these distributions properly account for the periodicity of the CVs.

#### **Options**

| SHIFT_TO_ZERO       | ( default=off ) Shift the minimum value of the target distribution to zero. This can for example be used to avoid negative values in the target distribution. If this option is active the distribution will be automatically normalized.   |
|---------------------|---|
| NORMALIZE           | ( default=off ) Renormalized the target distribution over the intervals on which it is defined to make sure that it is properly normalized to 1. In most cases this should not be needed as the target distributions should be normalized. The code will issue a warning (but still run) if this is needed for some reason.   |
| CENTER              | The centers of the Gaussian distributions. For one Gaussians you can use either CENTER or CENTER1. For more Gaussians you need to use the numbered CENTER keywords, one for each Gaussian. You can use multiple instances of this keyword i.e. CENTER1, CENTER2, CENTER3  |
| SIGMA               | The standard deviations of the Gaussian distributions. For one Gaussians you can use either SIGMA or SIGMA1. For more Gaussians you need to use the numbered SIGMA keywords, one for each Gaussian. You can use multiple instances of this keyword i.e. SIGMA1, SIGMA2, SIGMA3  |
| CORRELATION         | The correlation for two-dimensional bivariate Gaussian distributions. Only works for two arguments. The value should be between -1 and 1. If no value is given the Gaussians is considered as un-correlated (i.e. value of 0.0). For one Gaussians you can use either CORRELATION or CORRELATION1. For more Gaussians you need to use the numbered CORRELATION keywords, one for each Gaussian. You can use multiple instances of this keyword i.e. CORRE ← LATION1, CORRELATION2, CORRELATION3 |
| WEIGHTS             | The weights of the Gaussian distributions. Have to be as many as the number of centers given with the numbered CENTER keywords. If no weights are given the distributions are weighted equally. The weights are automatically normalized to 1.  |
| WELLTEMPERED_FACTOR | Broaden the target distribution such that it is taken as $[p(s)]^{\wedge}(1/g)$ where g is the well tempered factor given here. If this option is active the distribution will be automatically normalized.   |

**Examples** 

One single Gaussians in one-dimension.

```
TARGET_DISTRIBUTION={GAUSSIAN CENTER=-1.5 SIGMA=0.8}
```

Sum of three Gaussians in two-dimensions with equal weights as no weights are given.

Sum of three Gaussians in two-dimensions which are weighted unequally. Note that weights are automatically normalized to 1 so that WEIGHTS=1.0,2.0,1.0 is equal to specifying WEIGHTS=0.25,0.50,0.25.

Sum of two bivariate Gaussians where there is correlation of  $\rho_2=0.75$  between the two arguments for the second Gaussian.

## 8.5.2 GRID\_DIST

Target distribution from an external grid file (static).

Using this keyword you can use a target distribution that is read from an external grid file that is in the proper PLU ← MED file format. You do not to give any information about the external grid file as all relevant information should be automatically detected. It is assumed that the distribution read-in from the grid is a proper probability distribution, i.e. always non-negative and can be normalized.

By default the target distribution from the external grid is always normalized inside the code. You can disable this normalization by using DO\_NOT\_NORMALIZE keyword. However, be warned that this will generally lead to the wrong behavior if the distribution from the external grid is not properly normalized to 1.

If the distribution from the external grid file has for some reason negative values can you use the SHIFT keyword to shift the distribution by a given value. Another option is to use the SHIFT\_TO\_ZERO keyword to shift the minimum of the distribution to zero.

Note that the number of grid bins used in the external grid file do not have to be the same as used in the bias or action where the target distribution is employed as the code will employ a spline interpolation to calculate values.

It can happen that the intervals on which the target distribution is defined is larger than the intervals covered by the external grid file. In this case the default option is to consider the target distribution as continuous such that values outside the boundary of the external grid file are the same as at the boundary. This can be changed by using the ZERO OUTSIDE keyword which will make values outside to be taken as zero.

Compulsory keywords

| FILE | The name of the external grid file to be used as a target distribution. |
|------|---|
|      |   |

**Options** 

| ZERO_OUTSIDE        | ( default=off ) By default the target distribution is continuous such that values outside the boundary of the external grid file are the same as at the boundary. This can be changed by using this flag which will make values outside to be taken as zero.  |
|---------------------|---|
| DO_NOT_NORMALIZE    | ( default=off ) By default the target distribution from the external grid is always normalized inside the code. You can use this flag to disable this normalization. However, be warned that this will generally lead to the wrong behavior if the distribution from the external grid is not properly normalized to 1. |
| SHIFT_TO_ZERO       | ( default=off ) Shift the minimum value of the target distribution to zero. This can for example be used to avoid negative values in the target distribution. If this option is active the distribution will be automatically normalized.   |
| SHIFT               | Shift the grid read-in by some constant value. Due to normalization the final shift in the target distribution will generally not be the same as the value given here   |
| WELLTEMPERED_FACTOR | Broaden the target distribution such that it is taken as $[p(s)]^{-}(1/g)$ where g is the well tempered factor given here. If this option is active the distribution will be automatically normalized.  |

#### **Examples**

Generally you only need to provide the the filename of the external grid file. The target distribution is then automatically normalized to 1 inside the code.

```
TARGET_DISTRIBUTION={GRID_DIST FILE=input-grid.data}
```

## 8.5.3 LINEAR\_COMBINATION

Target distribution given by linear combination of distributions (static or dynamic).

Employ a target distribution that is a linear combination of the other distributions, defined as

$$p(\mathbf{s}) = \sum_{i} w_i \, p_i(\mathbf{s})$$

where the weights  $w_i$  are normalized to 1,  $\sum_i w_i = 1$ .

The distributions  $p_i(\mathbf{s})$  are given by using a separate numbered DISTRIBUTION keyword for each distribution. The keywords for each distribution should be enclosed within curly brackets.

The weights  $w_i$  can be given using the WEIGHTS keyword. The distributions are weighted equally if no weights are given.

It is assumed that all the distributions  $p_i(\mathbf{s})$  given with the numbered DISTRIBUTION keywords are normalized. If that is not the case you should normalize each distribution separately by using the NORMALIZE keyword within the curly brackets of each separate DISTRIBUTION keyword. Note that normalizing the overall linear combination will generally lead to different results than normalizing each distribution separately.

The linear combination will be a dynamic target distribution if one or more of the distributions used is a dynamic distribution. Otherwise it will be a static distribution.

**Options** 

| NORMALIZE           | ( default=off ) Renormalized the target distribution over the intervals on which it is defined to make sure that it is properly normalized to 1. In most cases this should not be needed as the target distributions should be normalized. The code will issue a warning (but still run) if this is needed for some reason. |
|---------------------|---|
| DISTRIBUTION        | The target distributions to be used in the linear combination, each given within a separate numbered DISTRIBUTION keyword and enclosed in curly brackets {}. You can use multiple instances of this keyword i.e. DISTRIBUTION1, DIS← TRIBUTION2, DISTRIBUTION3  |
| WEIGHTS             | The weights of target distributions. Have to be as many as the number of target distributions given with the numbered DISTRIBUTION keywords. If no weights are given the distributions are weighted equally. The weights are automatically normalized to 1.   |
| WELLTEMPERED_FACTOR | Broaden the target distribution such that it is taken as $[p(s)]^{\land}(1/g)$ where g is the well tempered factor given here. If this option is active the distribution will be automatically normalized.  |

#### **Examples**

Here we employ a linear combination of a uniform and a Gaussian distribution. No weights are given so the two distributions will be weighted equally.

Here we employ a linear combination of a uniform and two Gaussian distribution. The weights are automatically normalized to 1 such that giving WEIGHTS=1.0,1.0,2.0 as we do here is equal to giving WEIGHTS=0.25,0.25,0.50.

In the above example the two Gaussians are given using two separate DISTRIBUTION keywords. As the GAU← SSIAN target distribution allows multiple centers is it also possible to use just one DISTRIBUTION keyword for the two Gaussians. This is shown in the following example which will give the exact same result as the one above as the weights have been appropriately adjusted

### 8.5.4 MATHEVAL\_DIST

Target distribution given by a matheval parsed function (static or dynamic).

Use as a target distribution the distribution defined by

$$p(\mathbf{s}) = \frac{f(\mathbf{s})}{\int d\mathbf{s} f(\mathbf{s})}$$

where f(s) is some arbitrary mathematical function that is parsed by the matheval library.

The function f(s) is given by the FUNCTION keywords by using  $s1, s2, ..., s_d$ , as variables for the arguments  $s = (s_1, s_2, ..., s_d)$ . If one variable is not given the target distribution will be taken as uniform in that argument.

It is also possible to include the free energy surface  $F(\mathbf{s})$  in the target distribution by using the FE variable. In this case the target distribution is dynamic and needs to be updated with current best estimate of  $F(\mathbf{s})$ , similarly as for the well-tempered target distribution. Furthermore, the inverse temperature  $\beta=(k_{\rm B}T)^{-1}$  and the thermal energy  $k_{\rm B}T$  can be included by using the *beta* and *kBT* variables.

The target distribution will be automatically normalized over the region on which it is defined on. Therefore, the function given in FUNCTION needs to be non-negative and normalizable. The code will perform checks to make sure that this is indeed the case.

#### Attention

The MATHEVAL\_DIST only works if libmatheval is installed on the system and PLUMED has been linked to it.

Compulsory keywords

| FUNCTION | The function you wish to use for the target distribution where you should use the variables \$1,52, |
|----------|---|
|          | for the arguments. You can also use the current estimate of the FES by using the variable FE and    |
|          | the temperature by using the <i>kBT</i> and <i>beta</i> variables.                                  |

**Options** 

| SHIFT_TO_ZERO       | ( default=off ) Shift the minimum value of the target distribution to zero. This can for example be used to avoid negative values in the target distribution. If this option is active the distribution will be automatically normalized. |  |
|---------------------|---|--|
| WELLTEMPERED_FACTOR | Broaden the target distribution such that it is taken as $[p(s)]^{-}(1/g)$ where g is the well tempered factor given here. If this option is active the distribution will be automatically normalized.                                    |  |

#### **Examples**

Here we use as shifted Maxwell-Boltzmann distribution as a target distribution in one-dimension. Note that it is not need to include the normalization factor as the distribution will be automatically normalized.

```
 \begin{tabular}{ll} TARGET\_DISTRIBUTION= & \{MATHEVAL\_DIST \\ FUNCTION= & (s1+20)^2 * exp(-(s1+20)^2/(2*10.0^2)) \} \end{tabular}
```

Here we have a two dimensional target distribution where we use a generalized normal distribution for argument  $s_2$  while the distribution for  $s_1$  is taken as uniform as the variable  $s_1$  is not included in the function.

```
TARGET_DISTRIBUTION={MATHEVAL_DIST
    FUNCTION=exp(-(abs(s2-20.0)/5.0)^4.0)}
```

By using the FE variable the target distribution can depend on the free energy surface  $F(\mathbf{s})$ . For example, the following input is identical to using WELL\_TEMPERED with BIASFACTOR=10.

```
\label{thm:target_distribution=} \begin{split} & \texttt{TARGET\_DISTRIBUTION=} \{ \texttt{MATHEVAL\_DIST} \\ & & \texttt{FUNCTION=} \exp\left(-\left(\text{beta/10.0}\right) \star \texttt{FE}\right) \right\} \end{split}
```

Here the inverse temperature is automatically obtained by using the *beta* variable. It is also possible to use the *kBT* variable. The following syntax will give the exact same results as the syntax above

#### 8.5.5 PRODUCT COMBINATION

Target distribution given by product combination of distributions (static or dynamic).

Employ a target distribution that is a product combination of the other distributions, defined as

$$p(\mathbf{s}) = \frac{\prod_{i} p_i(\mathbf{s})}{\int d\mathbf{s} \prod_{i} p_i(\mathbf{s})}$$

where the distributions  $p_i(\mathbf{s})$  are in full dimensional space of the arguments used.

Note the difference between this target distribution and the one defined in PRODUCT\_DISTRIBUTION. Here we have a non-separable distribution given as a product of distribution  $p_i(\mathbf{s})$  which are in full dimensional space of the arguments used.

The distributions  $p_i(\mathbf{s})$  are given by using a separate numbered DISTRIBUTION keyword for each distribution. The keywords for each distribution should be enclosed within curly brackets.

The target distribution resulting from the product combination will be automatically normalized. Therefore, the product combination needs to be a proper distribution that is non-negative and normalizable. The code will perform checks to make sure that this is indeed the case.

The product combination will be a dynamic target distribution if one or more of the distributions used is a dynamic distribution. Otherwise it will be a static distribution.

| SHIFT_TO_ZERO       | ( default=off ) Shift the minimum value of the target distribution to zero. This can for example be used to avoid negative values in the target distribution. If this option is active the distribution will be automatically normalized. |
|---------------------|---|
| DISTRIBUTION        | The target distributions to be used in the product combination, each given within   |
|                     | a separate numbered DISTRIBUTION keyword and enclosed in First haskets {}. You can use multiple instances of this keyword i.e. DISTRIBUTION1, DIS← TRIBUTION2, DISTRIBUTION3  |
| WELLTEMPERED_FACTOR | Broaden the target distribution such that it is taken as $[p(s)]^{\wedge}(1/g)$ where g is  |

In the following example the overall interval on which the target distribution is defined is from -4 to 4. We employ a product of a Gaussian distribution with two centers and distribution that is uniform on the interval -3 to 3 and then smoothly decays to zero outside that interval. The overall effect will then be to cut off the tails of the Gaussian distribution

#### 8.5.6 PRODUCT\_DISTRIBUTION

Target distribution given by a separable product of one-dimensional distributions (static or dynamic).

Employ a target distribution that is a separable product of one-dimensional distributions, defined as

$$p(\mathbf{s}) = \prod_{k}^{d} p_k(s_k)$$

where d is the number of arguments used and  $p_k(s_k)$  is the one-dimensional distribution corresponding to the k-th argument.

Note the difference between this target distribution and the one defined in PRODUCT\_COMBINATION. Here we have a separable distribution given as a product of one-dimensional distribution  $p_k(s_k)$ .

The distributions  $p_k(s_k)$  are given by using a separate numbered DIST\_ARG keyword for each argument. The keywords for each distribution should be enclosed within curly brackets.

It is assumed that all the distributions given with the DIST\_ARG keywords are normalized. If that is not the case you need to normalize the distributions by using the NORMALIZE keyword. Here it does not matter if you normalize each distribution separately or the overall product, it will give the same results.

The product distribution will be a dynamic target distribution if one or more of the distributions used is a dynamic distribution. Otherwise it will be a static distribution.

| SHIFT_TO_ZERO                  | ( default=off ) Shift the minimum value of the target distribution to zero. This can for example be used to avoid negative values in the target distribution. If this option is active the distribution will be automatically normalized.   |
|--------------------------------|---|
| NORMALIZE                      | ( default=off ) Renormalized the target distribution over the intervals on which it is defined to make sure that it is properly normalized to 1. In most cases this should not be needed as the target distributions should be normalized. The code will issue a warning (but still run) if this is needed for some reason. |
| DIST_ARG  Generated by Doxygen | The one-dimensional target distributions for each argument to be used in the product distribution, each given within a separate numbered DIST_ARG keyword and enclosed in curly brackets {}. You can use multiple instances of this keyword i.e. DIST_ARG1, DIST_ARG2, DIST_ARG3  |
| WELLTEMPERED_FACTOR            | Broaden the target distribution such that it is taken as $[p(s)]^{\wedge}(1/g)$ where g is the well tempered factor given here. If this option is active the distribution will be automatically normalized.   |

In the following example we employ a uniform distribution for argument 1 and a Gaussian distribution for argument 2.

```
TARGET_DISTRIBUTION={PRODUCT_DISTRIBUTION DIST_ARG1={UNIFORM} DIST_ARG2={GAUSSIAN CENTER=-2.0 SIGMA=0.5}}
```

### 8.5.7 UNIFORM

Uniform target distribution (static).

Using this keyword you can define a uniform target distribution which is a product of one-dimensional distributions  $p_k(s_k)$  that are uniform over a given interval  $[a_k, b_k]$ 

$$p_k(s_k) = \{ 1(b_k - a_k) \text{ if } a_k \le s_k \le b_k \text{ 0otherwise } \}$$

The overall distribution is then given as

$$p(\mathbf{s}) = \prod_{k=1}^{d} p_k(s_k) = \left\{ \prod_{k=1}^{d} \frac{1}{(b_k - a_k)} \text{ if } a_k \leq s_k \leq b_k \text{ for all } k \text{ 0 otherwise} \right\}$$

The distribution is thus uniform inside a rectangular for two arguments and a cube for a three arguments.

The limits of the intervals  $a_k$  and  $b_k$  are given with the MINIMA and MAXIMA keywords, respectively. If one or both of these keywords are missing the code should automatically detect the limits.

It is also possible to use one-dimensional distributions that go smoothly to zero at the boundaries. This is done by employing a function with Gaussian switching functions at the boundaries  $a_k$  and  $b_k$ 

$$f_k(s_k) = \left\{ \exp\left( -\frac{(s_k - a_k)^2}{2\sigma_{a,k}^2} \right) \text{ if } s_k < a_k 1 \text{ if } a_k \le s_k \le b_k \exp\left( -\frac{(s_k - b_k)^2}{2\sigma_{b,k}^2} \right) \text{ if } s_k > b_k \right\}$$

where the standard deviation parameters  $\sigma_{a,k}$  and  $\sigma_{b,k}$  determine how quickly the switching functions goes to zero. The overall distribution is then normalized

$$p(\mathbf{s}) = \prod_{k}^{d} p_k(s_k) = \prod_{k}^{d} \frac{f(s_k)}{\int ds_k f(s_k)}$$

To use this option you need to provide the standard deviation parameters  $\sigma_{a,k}$  and  $\sigma_{b,k}$  by using the SIGMA\_MI $\leftarrow$  NIMA and SIGMA\_MAXIMA keywords, respectively. Giving a value of 0.0 means that the boundary is sharp, which is the default behavior.

| MINIMA       | The minima of the intervals where the target distribution is taken as uniform. You should give one value for each argument.   |  |
|--------------|---|--|
| MAXIMA       | The maxima of the intervals where the target distribution is taken as uniform. You should give one value for each argument.   |  |
| SIGMA_MINIMA | The standard deviation parameters of the Gaussian switching functions for the intervals. You should give one value for each argument. Value of 0.0 means that switch is done without a smooth switching function, this is the default behavior. |  |
| SIGMA_MAXIMA | The standard deviation parameters of the Gaussian switching functions for the maxima of   |  |

If one or both of the MINIMA or MAXIMA keywords are missing the code should automatically detect the limits not given. Therefore, if we consider a target distribution that is defined over an interval from 0.0 to 10.0 for the first argument and from 0.2 to 1.0 for the second argument are all of the following examples equivalent

```
TARGET_DISTRIBUTION={UNIFORM

MINIMA=0.0,0,2

MAXIMA=10.0,1.0}

TARGET_DISTRIBUTION={UNIFORM

MAXIMA=10.0,1.0}

TARGET_DISTRIBUTION={UNIFORM

MINIMA=0.0,0,2}
```

We can also define a target distribution that goes smoothly to zero at the boundaries of the uniform distribution. In the following we consider an interval of 0 to 10 for the target distribution. The following input would result in a target distribution that would be uniform from 2 to 7 and then smoothly go to zero.

It is also possible to employ a smooth switching function for just one of the boundaries as shown here where the target distribution would be uniform from 0 to 7.

Furthermore, it is possible to employ a sharp boundary by using

or

## 8.5.8 VON\_MISES

Target distribution given by a sum of Von Mises distributions (static).

Employ a target distribution that is given by a sum where each term is a product of one-dimensional Von Mises distributions,

$$p(\mathbf{s}) = \sum_{i} w_{i} \prod_{k}^{d} \frac{\exp\left(\kappa_{k,i} \cos(s_{k} - \mu_{k,i})\right)}{2\pi I_{0}(\kappa_{k,i})}$$

where  $\mu_i=(\mu_{1,i},\mu_{2,i},\dots,\mu_{d,i})$  are the centers of the distributions,  $\kappa_i=(\kappa_{1,i},\kappa_{2,i},\dots,\kappa_{d,i})$  are parameters that determine the extend of each distribution, and  $I_0(x)$  is the modified Bessel function of order 0. The weights  $w_i$  are normalized to 1,  $\sum_i w_i=1$ .

The Von Mises distribution is defined for periodic variables with a periodicity of  $2\pi$  and is analogous to the Gaussian distribution. The parameter  $\sqrt{1/\kappa}$  is comparable to the standard deviation  $\sigma$  for the Gaussian distribution.

To use this target distribution you need to give the centers  $\mu_i = (\mu_{1,i}, \mu_{2,i}, \dots, \mu_{d,i})$  by using the numbered CEN $\leftarrow$  TER keywords and the "standard deviations"  $\sigma_i = (\sqrt{1/\kappa_{1,i}}, \sqrt{1/\kappa_{2,i}}, \dots, \sqrt{1/\kappa_{d,i}})$  using the numbered SIGMA keywords.

| SHIFT_TO_ZERO       | ( default=off ) Shift the minimum value of the target distribution to zero. This can for example be used to avoid negative values in the target distribution. If this option is active the distribution will be automatically normalized.   |
|---------------------|---|
| CENTER              | The centers of the Von Mises distributions. For one distribution you can use either CENTER or CENTER1. For more distributions you need to use the numbered CENTER keywords, one for each distribution. You can use multiple instances of this keyword i.e. CENTER1, CENTER2, CENTER3          |
| SIGMA               | The standard deviations of the Von Mises distributions. For one distribution you can use either CENTER or CENTER1. For more distributions you need to use the numbered CENTER keywords, one for each distribution. You can use multiple instances of this keyword i.e. SIGMA1, SIGMA2, SIGMA3 |
| WEIGHTS             | The weights of the Von Mises distributions. Have to be as many as the number of centers given with the numbered CENTER keywords. If no weights are given the distributions are weighted equally. The weights are automatically normalized to 1.   |
| WELLTEMPERED_FACTOR | Broaden the target distribution such that it is taken as $[p(s)]^{-1/2}$ where g is the well tempered factor given here. If this option is active the distribution will be automatically normalized.  |

Sum of two Von Mises distribution in one dimension that have equal weights as no weights are given.

```
TARGET_DISTRIBUTION={VON_MISES}
CENTER1=+2.0 SIGMA1=0.6
CENTER2=-2.0 SIGMA2=0.7}
```

Sum of two Von Mises distribution in two dimensions that have different weights. Note that the weights are automatically normalized to 1 such that specifying WEIGHTS=1.0,2.0 is equal to specifying WEIGHTS=0.33333,0.66667.

## 8.5.9 WELL\_TEMPERED

Well-tempered target distribution (dynamic).

Use as a target distribution the well-tempered distribution ? given by

$$p(\mathbf{s}) = \frac{e^{-(\beta/\gamma)F(\mathbf{s})}}{\int d\mathbf{s} \, e^{-(\beta/\gamma)F(\mathbf{s})}} = \frac{[P_0(\mathbf{s})]^{1/\gamma}}{\int d\mathbf{s} \, [P_0(\mathbf{s})]^{1/\gamma}}$$

where  $\gamma$  is a so-called bias factor and  $P_0(\mathbf{s})$  is the unbiased canonical distribution of the CVs. This target distribution thus correponds to a biased ensemble where, as compared to the unbiased one, the probability peaks have been broaden and the fluctations of the CVs are enhanced. The value of the bias factor  $\gamma$  determines by how much the fluctations are enhanced.

The well-tempered distribution can be view as sampling on an effective free energy surface  $\tilde{F}(\mathbf{s})=(1/\gamma)F(\mathbf{s})$  which has largely the same metastable states as the original  $F(\mathbf{s})$  but with barriers that have been reduced by a

factor of  $\gamma$ . Generally one should use a value of  $\gamma$  that results in effective barriers on the order of few  $k_{\rm B}T$  such that thermal fluctuations can easily induce transitions between different metastable states.

At convergence the relationship between the bias potential and the free energy surface is given by

$$F(\mathbf{s}) = -\left(\frac{1}{1 - \gamma^{-1}}\right) V(\mathbf{s})$$

This target distribution depends directly on the free energy surface  $F(\mathbf{s})$  which is quantity that we do not know a-priori and want to obtain. Therefore, this target distribution is iteratively updated? according to

$$p^{(m+1)}(\mathbf{s}) = \frac{e^{-(\beta/\gamma)F^{(m+1)}(\mathbf{s})}}{\int d\mathbf{s} \, e^{-(\beta/\gamma)F^{(m+1)}(\mathbf{s})}}$$

where  $F^{(m+1)}(s)$  is the current best estimate of the free energy surface obtained according to

$$F^{(m+1)}(\mathbf{s}) = -V^{(m+1)}(\mathbf{s}) - \frac{1}{\beta} \log p^{(m)}(\mathbf{s}) = -V^{(m+1)}(\mathbf{s}) + \frac{1}{\gamma} F^{(m)}(\mathbf{s})$$

The frequency of performing this update needs to be set in the optimizer used in the calculation. Normally it is sufficient to do it every 100-1000 bias update iterations.

Compulsory keywords

| BIASFACTOR | The bias factor used for the well-tempered distribution. |
|------------|--|
|            |  |

#### **Examples**

Employ a well-tempered target distribution with a bias factor of 10

TARGET\_DISTRIBUTION={WELL\_TEMPERED BIASFACTOR=10}

# 8.6 Optimizers

The following list contains the optimizers available in the VES code.

| AVERAGED_SGD      | Averaged stochastic gradient decent with fixed step size. |
|-------------------|---|
| FAKE_OPTIMIZER    | Dummy optimizer for debugging.                            |
| ROBBINS_MONRO_SGD | Robbins-Monro stochastic gradient decent.                 |

# 8.6.1 AVERAGED\_SGD

Averaged stochastic gradient decent with fixed step size.

**Algorithim** 

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This optimizer updates the coefficients according to the averaged stochastic gradient decent algorithm described in ref?. This algorithm considers two sets of coefficients, the so-called instantaneous coefficients that are updated according to the recursion formula given by

$$\alpha^{(n+1)} = \alpha^{(n)} - \mu \left[ \nabla \Omega(\bar{\alpha}^{(n)}) + \mathbf{H}(\bar{\alpha}^{(n)}) [\alpha^{(n)} - \bar{\alpha}^{(n)}] \right],$$

where  $\mu$  is a fixed step size and the gradient  $\nabla\Omega(\bar{\alpha}^{(n)})$  and the Hessian  $\mathbf{H}(\bar{\alpha}^{(n)})$  depend on the averaged coefficients defined as

$$\bar{\alpha}^{(n)} = \frac{1}{n+1} \sum_{k=0}^{n} \alpha^{(k)}.$$

This means that the bias acting on the system depends on the averaged coefficients  $\bar{\alpha}^{(n)}$  which leads to a smooth convergence of the bias and the estimated free energy surface. Furthermore, this allows for a rather short sampling time for each iteration, for classical MD simulations typical sampling times are on the order of few ps (around 1000-4000 MD steps).

Currently it is only supported to employ the diagonal part of the Hessian which is generally sufficient. Support for employing the full Hessian will be added later on.

The VES bias that is to be optimized should be specified using the BIAS keyword. The fixed step size  $\mu$  is given using the STEPSIZE keyword. The frequency of updating the coefficients is given using the STRIDE keyword where the value is given in the number of MD steps. For example, if the MD time step is 0.02 ps and STRIDE=2000 will the coefficients be updated every 4 ps. The coefficients will be outputted to the file given by the COEFFS\_FILE keyword. How often the coefficients are written to this file is controlled by the COEFFS\_OUTPUT keyword.

#### Multiple walkers

This optimizer supports the usage of multiple walkers where different copies of the system share the same bias potential (i.e. coefficients) and cooperatively sample the averages needed for the gradient and Hessian. This can significantly help with convergence in difficult cases. It is of course best to start the different copies from different positions in CV space. To activate this option you just need to add the MULTIPLE\_WALKERS flag. Note that this is only supported if the MD code support running multiple replicas connected via MPI.

#### **Description of components**

The names of the components in this action can be customized by the user in the actions input file. However, in addition to these customizable components the following quantities will always be output

| Quantity | Description   |
|----------|---|
| gradrms  | the root mean square value of the coefficent gradient. For multiple biases this component is labeled using the number of the bias as gradrms-#. |
| gradmax  | the largest absolute value of the coefficent gradient. For multiple biases this component is labeled using the number of the bias as gradmax-#. |

#### Compulsory keywords

| BIAS   | the label of the VES bias to be optimized                                   |
|--------|---|
| STRIDE | the frequency of updating the coefficients given in the number of MD steps. |

| COEFFS_FILE   | ( default=coeffs.data ) the name of output file for the coefficients                          |  |
|---------------|---|--|
| COEFFS_OUTPUT | ( default=100 ) how often the coefficients should be written to file. This parameter is given |  |
|               | as the number of iterations.  |  |
| STEPSIZE      | the step size used for the optimization   |  |

| MULTIPLE_WALKERS           | ( default=off ) if optimization is to be performed using multiple walkers connected via MPI  |
|----------------------------|--|
| START_OPTIMIZATION_AFRESH  | ( default=off ) if the iterations should be started afresh when a restart has been triggered by the RESTART keyword or the MD code.  |
| COEFFS_FMT                 | specify format for coefficient file(s) (useful for decrease the number of digits in regtests)  |
| COEFFS_SET_ID_PREFIX       | suffix to add to the filename given in FILE to identify the bias, should only be given if a single filename is given in FILE when optimizing multiple biases.  |
| INITIAL_COEFFS             | the name(s) of file(s) with the initial coefficents  |
| TARGETDIST_AVERAGES_FILE   | the name of output file for the target distribution averages. By default it is targetdist-averages.data.   |
| TARGETDIST_AVERAGES_OUTPUT | how often the target distribution averages should be written out to file. Note that the value is given in terms of coefficent iterations. If no value is given are the averages only written at the begining of the optimization                               |
| BIAS_OUTPUT                | how often the bias(es) should be written out to file. Note that the value is given in terms of coefficent iterations.  |
| FES_OUTPUT                 | how often the FES(s) should be written out to file. Note that the value is given in terms of coefficent iterations.  |
| FES_PROJ_OUTPUT            | how often the projections of the FES(s) should be written out to file. Note that the value is given in terms of coefficent iterations.   |
| RESTART                    | allows per-action setting of restart (YES/NO/AUTO)   |
| UPDATE_FROM                | Only update this action from this time   |
| UPDATE_UNTIL               | Only update this action until this time  |
| MASK_FILE                  | read in a mask file which allows one to employ different step sizes for different coefficents and/or deactive the optimization of certain coefficients (by putting values of 0.0). One can write out the resulting mask by using the OUTPUT_MASK_FILE keyword. |
| OUTPUT_MASK_FILE           | Name of the file to write out the mask resulting from using the M← ASK_FILE keyword. Can also be used to generate a template mask file.  |
| TARGETDIST_STRIDE          | stride for updating a target distribution that is iteratively updated during the optimization. Note that the value is given in terms of coefficent iterations.   |
| TARGETDIST_OUTPUT          | how often the dynamic target distribution(s) should be written out to file. Note that the value is given in terms of coefficent iterations.  |
| TARGETDIST_PROJ_OUTPUT     | how often the projections of the dynamic target distribution(s) should<br>be written out to file. Note that the value is given in terms of coefficent<br>iterations.   |
| EXP_DECAYING_AVER          | calculate the averaged coefficients using exponentially decaying averaging using the decaying constant given here in the number of iterations  |

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Examples

# 8.6.2 FAKE\_OPTIMIZER

Dummy optimizer for debugging.

**Description of components** 

The names of the components in this action can be customized by the user in the actions input file. However, in addition to these customizable components the following quantities will always be output

| Quantity | Description   |
|----------|---|
| gradrms  | the root mean square value of the coefficent gradient. For multiple biases this component is labeled using the number of the bias as gradrms-#. |
| gradmax  | the largest absolute value of the coefficent gradient. For multiple biases this component is labeled using the number of the bias as gradmax-#. |

## Compulsory keywords

| BIAS          | the label of the VES bias to be optimized   |
|---------------|---|
| STRIDE        | the frequency of updating the coefficients given in the number of MD steps.                   |
| COEFFS_FILE   | ( default=coeffs.data ) the name of output file for the coefficients                          |
| COEFFS_OUTPUT | ( default=100 ) how often the coefficients should be written to file. This parameter is given |
|               | as the number of iterations.  |

| MULTIPLE_WALKERS           | ( default=off ) if optimization is to be performed using multiple walkers connected via MPI  |
|----------------------------|--|
| MONITOR_HESSIAN            | ( default=off ) also monitor the Hessian   |
| COEFFS_FMT                 | specify format for coefficient file(s) (useful for decrease the number of digits in regtests)  |
| COEFFS_SET_ID_PREFIX       | suffix to add to the filename given in FILE to identify the bias, should only be given if a single filename is given in FILE when optimizing multiple biases.  |
| INITIAL_COEFFS             | the name(s) of file(s) with the initial coefficents  |
| TARGETDIST_AVERAGES_FILE   | the name of output file for the target distribution averages. By default it is targetdist-averages.data.   |
| TARGETDIST_AVERAGES_OUTPUT | how often the target distribution averages should be written out to file. Note that the value is given in terms of coefficent iterations. If no value is given are the averages only written at the begining of the optimization |

| BIAS_OUTPUT     | how often the bias(es) should be written out to file. Note that the value is given in terms of coefficent iterations.                  |
|-----------------|--|
| FES_OUTPUT      | how often the FES(s) should be written out to file. Note that the value is given in terms of coefficent iterations.                    |
| FES_PROJ_OUTPUT | how often the projections of the FES(s) should be written out to file. Note that the value is given in terms of coefficent iterations. |
| RESTART         | allows per-action setting of restart (YES/NO/AUTO)   |
| UPDATE_FROM     | Only update this action from this time   |
| UPDATE_UNTIL    | Only update this action until this time  |

# 8.6.3 ROBBINS\_MONRO\_SGD

Robbins-Monro stochastic gradient decent.

**Description of components** 

The names of the components in this action can be customized by the user in the actions input file. However, in addition to these customizable components the following quantities will always be output

| Quantity | Description   |
|----------|---|
| gradrms  | the root mean square value of the coefficent gradient. For multiple biases this component is labeled using the number of the bias as gradrms-#.           |
| gradmax  | the largest absolute value of the coefficent gradient. For multiple biases this component is labeled using the number of the bias as gradmax-#.           |
| stepsize | the current value of step size used to update the coefficients. For multiple biases this component is labeled using the number of the bias as stepsize-#. |

# Compulsory keywords

| BIAS             | the label of the VES bias to be optimized  |
|------------------|--|
| STRIDE           | the frequency of updating the coefficients given in the number of MD steps.  |
| COEFFS_FILE      | ( default=coeffs.data ) the name of output file for the coefficients   |
| COEFFS_OUTPUT    | ( default=100 ) how often the coefficients should be written to file. This parameter is given as the number of iterations. |
| INITIAL_STEPSIZE | the initial step size used for the optimization  |

| MULTIPLE_WALKERS | ( default=off ) if optimization is to be performed using multiple walkers |
|------------------|---|
|                  | connected via MPI   |

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| START_OPTIMIZATION_AFRESH  | ( default=off ) if the iterations should be started afresh when a restart has been triggered by the RESTART keyword or the MD code.  |
|----------------------------|--|
| COEFFS_FMT                 | specify format for coefficient file(s) (useful for decrease the number of digits in regtests)  |
| COEFFS_SET_ID_PREFIX       | suffix to add to the filename given in FILE to identify the bias, should only be given if a single filename is given in FILE when optimizing multiple biases.  |
| INITIAL_COEFFS             | the name(s) of file(s) with the initial coefficents  |
| TARGETDIST_AVERAGES_FILE   | the name of output file for the target distribution averages. By default it is targetdist-averages.data.   |
| TARGETDIST_AVERAGES_OUTPUT | how often the target distribution averages should be written out to file. Note that the value is given in terms of coefficent iterations. If no value is given are the averages only written at the begining of the optimization                               |
| BIAS_OUTPUT                | how often the bias(es) should be written out to file. Note that the value is given in terms of coefficent iterations.  |
| FES_OUTPUT                 | how often the FES(s) should be written out to file. Note that the value is given in terms of coefficent iterations.  |
| FES_PROJ_OUTPUT            | how often the projections of the FES(s) should be written out to file. Note that the value is given in terms of coefficent iterations.   |
| RESTART                    | allows per-action setting of restart (YES/NO/AUTO)   |
| UPDATE_FROM                | Only update this action from this time   |
| UPDATE_UNTIL               | Only update this action until this time  |
| MASK_FILE                  | read in a mask file which allows one to employ different step sizes for different coefficents and/or deactive the optimization of certain coefficients (by putting values of 0.0). One can write out the resulting mask by using the OUTPUT_MASK_FILE keyword. |
| OUTPUT_MASK_FILE           | Name of the file to write out the mask resulting from using the M $\leftarrow$ ASK_FILE keyword. Can also be used to generate a template mask file.  |
| TARGETDIST_STRIDE          | stride for updating a target distribution that is iteratively updated during the optimization. Note that the value is given in terms of coefficent iterations.   |
| TARGETDIST_OUTPUT          | how often the dynamic target distribution(s) should be written out to file. Note that the value is given in terms of coefficent iterations.  |
| TARGETDIST_PROJ_OUTPUT     | how often the projections of the dynamic target distribution(s) should be written out to file. Note that the value is given in terms of coefficent iterations.   |
| DECAY_CONSTANT             | the decay constant used for the step size.   |

Examples

# 8.7 Collective Variables

The following list contains the CV available in the VES code.

| MDRUNNER_POSITION | Use as CVs the postions from dynamics of md_linearexpansion |
|-------------------|---|
|-------------------|---|

## 8.7.1 MDRUNNER\_POSITION

Use as CVs the postions from dynamics of md\_linearexpansion

**Description of components** 

By default the value of the calculated quantity can be referenced elsewhere in the input file by using the label of the action. Alternatively this Action can be used to be used to calculate the following quantities by employing the keywords listed below. These quanties can be referenced elsewhere in the input by using this Action's label followed by a dot and the name of the quantity required from the list below.

| Quantity | Description             |
|----------|-------------------------|
| X        | x-postion of the walker |
| у        | y-postion of the walker |
| Z        | z-postion of the walker |

**Options** 

| NUMERICAL_DERIVATIVES | ( default=off ) calculate the derivatives for these quantities numerically         |
|-----------------------|--|
| NOPBC                 | ( default=off ) ignore the periodic boundary conditions when calculating distances |

**Examples** 

## 8.8 Utilities

The following list contains various utilities available in the VES code.

| DUMP_BASISFUNCTIONS      | Dump basis functions to file.     |
|--------------------------|-----------------------------------|
| DUMP_TARGET_DISTRIBUTION | Dump target distribution to file. |

## 8.8.1 DUMP\_BASISFUNCTIONS

Dump basis functions to file.

Compulsory keywords

| BASIS SET | the label of the basis set that you want to use |
|-----------|---|

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# Options

| IGNORE_PERIODICITY         | ( default=off ) if the periodicity of the basis functions should be ignored.  |
|----------------------------|---|
| NUMERICAL_DERIVATIES       | ( default=off ) if the derivatives of the basis functions should be calculated numerically.   |
| GRID_BINS                  | the number of bins used for the grid for writing the basis function values and derivatives. The default value is 1000.  |
| GRID_MIN                   | the minimum of the grid for writing the basis function values and derivatives. By default it is the minimum of the interval on which the basis functions are defined. |
| GRID_MAX                   | the maximum of the grid for writing the basis function values and derivatives. By default it is the maximum of the interval on which the basis functions are defined. |
| FILE_VALUES                | filename of the file on which the basis function values are written. By default it is BASIS_SET.values.data.  |
| FILE_DERIVS                | filename of the file on which the basis function derivatives are written.<br>By default it is BASIS_SET.derivs.data.  |
| FORMAT_VALUES_DERIVS       | the numerical format of the basis function values and derivatives written to file. By default it is %15.8f.   |
| FILE_TARGETDIST_AVERAGES   | filename of the file on which the averages over the target distributions are written. By default it is BASIS_SET.targetdist-averages.data.                            |
| FORMAT_TARGETDIST_AVERAGES | the numerical format of the target distribution averages written to file. By default it is %15.8f.  |
| FILE_TARGETDIST            | filename of the files on which the target distributions are written. By default it is BASIS_SET.targetdist-#.data.  |
| TARGET_DISTRIBUTION        | the target distribution to be used. You can use multiple instances of this keyword i.e. TARGET_DISTRIBUTION1, TARGET_DISTRIBU ← TION2, TARGET_DISTRIBUTION3           |

Examples

# 8.8.2 DUMP\_TARGET\_DISTRIBUTION

Dump target distribution to file.

Compulsory keywords

| GRID_MIN            | the lower bounds for the grid                            |
|---------------------|--|
| GRID_MAX            | the upper bounds for the grid                            |
| GRID_BINS           | the number of bins used for the grid.                    |
| TARGETDIST_FILE     | filename of the file for writing the target distribution |
| TARGET_DISTRIBUTION | the target distribution to be used.                      |

**Options** 

| DO_1D_PROJECTIONS   | ( default=off ) Also output the one-dimensional marginal distributions for multi-dimensional target distribution.                  |
|---------------------|--|
| GRID_PERIODICITY    | specfiy if the individual arguments should be made periodic (YES) or not (NO). By default all arguments are taken as not periodic. |
| LOG_TARGETDIST_FILE | filename of the file for writing the log of the target distribution  |
| FMT_GRIDS           | the numerical format of the target distribution grids written to file. By default it is %14.9f                                     |

**Examples** 

# 8.9 Command Line Tools

The following list contains the command line tools available in the VES code.

| manual_ves         | manual_ves is a command line tool for constructing the manual page fora particular target |
|--------------------|---|
|                    | distribution included in the VES code.  |
| md_linearexpansion | Simple MD code for dynamics on a energy landscape given by a linear basis set expan-      |
|                    | sion.   |

# 8.9.1 manual\_ves

manual\_ves is a command line tool for constructing the manual page for a particular target distribution included in the VES code.

The manual constructed by this action is in html. In all probability you will never need to use this tool. However, it is used within the scripts that generate plumed's html manual. If you need to use this tool outside those scripts the input is specified using the following command line arguments.

Compulsory keywords

| help/-h | ( default=off ) print this help                  |  |
|---------|--|--|
| vim     | ( default=off ) print the keywords in vim syntax |  |

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# Examples

The following generates the html manual for the target distribution VON\_MISES

plumed manual\_ves --targetdist VON\_MISES

# 8.9.2 md\_linearexpansion

Simple MD code for dynamics on a energy landscape given by a linear basis set expansion.

# Compulsory keywords

| nstep                 | ( default=10 ) The number of steps of dynamics you want to run.   |
|-----------------------|---|
| tstep                 | ( default=0.005 ) The integration timestep.   |
| temperature           | ( default=1.0 ) The temperature to perform the simulation at.   |
| friction              | ( default=10. ) The friction of the langevin thermostat.  |
| random_seed           | ( default=5293818 ) Value of random number seed.  |
| plumed_input          | ( default=plumed.dat ) The name of the plumed input file(s). Either give one file or separate files for each partition. |
| dimension             | ( default=1 ) Number of dimensions, supports 1 to 3.  |
| initial_position      | Initial position for each partition.  |
| partitions            | ( default=1 ) Number of partitions.   |
| basis_functions_1     | Basis functions for dimension 1.  |
| input_coeffs          | ( default=potential-coeffs.in.data ) Filename of the input coefficent file for the potential.                           |
| output_coeffs         | ( default=potential-coeffs.out.data ) Filename of the output coefficent file for the potential.                         |
| output_coeffs_fmt     | ( default=%30.16e ) Format of the output coefficent file for the potential. Useful for regtests.                        |
| output_potential_grid | ( default=100 ) The number of grid points used for the potential and histogram output files.                            |
| output_potential      | ( default=potential.data ) Filename of the potential output file.   |
| output_histogram      | ( default=histogram.data ) Filename of the histogram output file.   |

## **Options**

| help/-h              | ( default=off ) print this help  |  |
|----------------------|--|--|
|                      |  |  |
| basis_functions_2    | Basis functions for dimension 2 if needed.                                 |  |
| basis_functions_3    | Basis functions for dimension 3 if needed.                                 |  |
| coeffs_prefactor     | prefactor for multiplying the coefficents with.                            |  |
| template_coeffs_file | only generate a template coefficent file with the filename given and exit. |  |
|                      |  |  |

# Examples

plumed md\_linearexpansion input

# 8.10 VES Index of Actions

The following list contains all actions available in the VES code

| AVERAGED_SGD             | VES_OPTIMIZER  | Averaged stochastic gradient decent with fixed step size.  |
|--------------------------|----------------|--|
| BF_CHEBYSHEV             | VES_BASISF     | Chebyshev polynomial basis functions.  |
| BF_COMBINED              | VES_BASISF     | Combining other basis functions types  |
| BF_COSINE                | VES_BASISF     | Fourier cosine basis functions.  |
| BF_FOURIER               | VES_BASISF     | Fourier basis functions.   |
| BF_LEGENDRE              | VES_BASISF     | Legendre polynomials basis functions.  |
| BF_POWERS                | VES_BASISF     | Polynomial power basis functions.  |
| BF_SINE                  | VES_BASISF     | Fourier sine basis functions.  |
| DUMP_BASISFUNCTIONS      | VES_UTILS      | Dump basis functions to file.  |
| DUMP_TARGET_DISTRIBUTION | VES_UTILS      | Dump target distribution to file.  |
| FAKE_OPTIMIZER           | VES_OPTIMIZER  | Dummy optimizer for debugging.   |
| GAUSSIAN                 | VES_TARGETDIST | Target distribution given by a sum of Gaussians (static).  |
| GRID_DIST                | VES_TARGETDIST | Target distribution from an external grid file (static).   |
| LINEAR_COMBINATION       | VES_TARGETDIST | Target distribution given by linear combination of distributions (static or dynamic).  |
| manual_ves               | VES_CLTOOLS    | manual_ves is a command line tool for constructing the manual page fora particular target distribution included in the VES code. |
| MATHEVAL_DIST            | VES_TARGETDIST | Target distribution given by a matheval parsed function (static or dynamic).   |
| md_linearexpansion       | VES_CLTOOLS    | Simple MD code for dynamics on a energy land-<br>scape given by a linear basis set expansion.                                    |
| MDRUNNER_POSITION        | VES_COLVAR     | Use as CVs the postions from dynamics of md_← linearexpansion  |
| PRODUCT_COMBINATION      | VES_TARGETDIST | Target distribution given by product combination of distributions (static or dynamic).   |
| PRODUCT_DISTRIBUTION     | VES_TARGETDIST | Target distribution given by a separable productof one-dimensional distributions (static or dynamic).                            |
| ROBBINS_MONRO_SGD        | VES_OPTIMIZER  | Robbins-Monro stochastic gradient decent.  |
| UNIFORM                  | VES_TARGETDIST | Uniform target distribution (static).  |
| VES_LINEAR_EXPANSION     | VES_BIASES     | Linear basis set expansion bias.   |
| VON_MISES                | VES_TARGETDIST | Target distribution given by a sum of Von Mises distributions (static).  |
| WELL_TEMPERED            | VES_TARGETDIST | Well-tempered target distribution (dynamic).   |

# **Chapter 9**

# **Command Line Tools**

PLUMED contains a number of simple command line tools. To use one of these tools you issue a command something like:

plumed <toolname> <list of input flags for that tool>

The following is a list of the various standalone tools that PLUMED contains.

| driver-float | Equivalent to driver, but using single precision reals.  |
|--------------|--|
| driver       | driver is a tool that allows one to to use plumed to post-process an existing trajectory.          |
| gentemplate  | gentemplate is a tool that you can use to construct template inputs for the variousactions         |
| info         | This tool allows you to obtain information about your plumed version                               |
| kt           | Print out the value of $k_BT$ at a particular temperature  |
| manual       | manual is a tool that you can use to construct the manual page for a particular action             |
| pathtools    | pathtools can be used to construct paths from pdb data   |
| simplemd     | simplemd allows one to do molecular dynamics on systems of Lennard-Jones atoms.                    |
| sum_hills    | sum_hills is a tool that allows one to to use plumed to post-process an existing hills/colvar file |

For all these tools and to use PLUMED as a plugin in an MD calculation you will need an input file.

# 9.1 driver-float

This is part of the cltools module

Equivalent to driver, but using single precision reals.

The purpose of this tool is just to test what PLUMED does when linked from a single precision code.

The input trajectory is specified using one of the following

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| іхуг      | the trajectory in xyz format                          |
|-----------|---|
| igro      | the trajectory in gro format                          |
| ixtc      | the trajectory in xtc format (xdrfile implementation) |
| itrr      | the trajectory in trr format (xdrfile implementation) |
| mf_dcd    | molfile: the trajectory in dcd format                 |
| mf_crd    | molfile: the trajectory in crd format                 |
| mf_crdbox | molfile: the trajectory in crdbox format              |
| mf_gro    | molfile: the trajectory in gro format                 |
| mf_g96    | molfile: the trajectory in g96 format                 |
| mf_trr    | molfile: the trajectory in trr format                 |
| mf_trj    | molfile: the trajectory in trj format                 |
| mf_xtc    | molfile: the trajectory in xtc format                 |
| mf_pdb    | molfile: the trajectory in pdb format                 |

The following must be present

| plumed            | ( default=plumed.dat ) specify the name of the plumed input file   |
|-------------------|--|
| timestep          | ( default=1.0 ) the timestep that was used in the calculation that produced this trajectory in picoseconds   |
| trajectory-stride | ( default=1 ) the frequency with which frames were output to this trajectory during the simulation (0 means that the number of the step is read from the trajectory file, currently working only for xtc/trr files read with –ixtc/–trr) |
| multi             | ( default=0 ) set number of replicas for multi environment (needs mpi)   |

The following options are available

| help/-h          | ( default=off ) print this help  |
|------------------|--|
| help-debug       | ( default=off ) print special options that can be used to create regtests  |
| noatoms          | ( default=off ) don't read in a trajectory. Just use colvar files as specified in plumed.dat   |
| dump-full-virial | ( default=off ) with -dump-forces, it dumps the 9 components of the virial   |
| length-units     | units for length, either as a string or a number   |
| mass-units       | units for mass in pdb and mc file, either as a string or a number  |
| charge-units     | units for charge in pdb and mc file, either as a string or a number  |
| dump-forces      | dump the forces on a file  |
| dump-forces-fmt  | ( default=%f ) the format to use to dump the forces  |
| pdb              | provides a pdb with masses and charges   |
| mc               | provides a file with masses and charges as produced with DUMPMASSCHARGE  |
| box              | comma-separated box dimensions (3 for orthorombic, 9 for generic)  |
| natoms           | provides number of atoms - only used if file format does not contain number of atoms   |
| debug-forces     | output a file containing the forces due to the bias evaluated using numerical derivatives and using the analytical derivatives implemented in plumed |

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### **Examples**

```
plumed driver-float --plumed plumed.dat --ixyz trajectory.xyz
```

See also examples in driver

## 9.2 driver

This is part of the citools module

driver is a tool that allows one to to use plumed to post-process an existing trajectory.

The input to driver is specified using the command line arguments described below.

In addition, you can use the special READ command inside your plumed input to read in colvar files that were generated during your MD simulation. The values read in can then be treated like calculated colvars.

### Warning

Notice that by default the driver has no knowledge about the masses and charges of your atoms! Thus, if you want to compute quantities depending charges (e.g. DHENERGY) or masses (e.g. COM) you should pass the proper information to the driver. You can do it either with the –pdb option or with the –mc option. The latter will read a file produced by DUMPMASSCHARGE.

The input trajectory is specified using one of the following

| ixyz      | the trajectory in xyz format                          |
|-----------|---|
| igro      | the trajectory in gro format                          |
| ixtc      | the trajectory in xtc format (xdrfile implementation) |
| itrr      | the trajectory in trr format (xdrfile implementation) |
| mf_dcd    | molfile: the trajectory in dcd format                 |
| mf_crd    | molfile: the trajectory in crd format                 |
| mf_crdbox | molfile: the trajectory in crdbox format              |
| mf_gro    | molfile: the trajectory in gro format                 |
| mf_g96    | molfile: the trajectory in g96 format                 |
| mf_trr    | molfile: the trajectory in trr format                 |
| mf_trj    | molfile: the trajectory in trj format                 |
| mf_xtc    | molfile: the trajectory in xtc format                 |
| mf_pdb    | molfile: the trajectory in pdb format                 |

The following must be present

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| plumed            | ( default=plumed.dat ) specify the name of the plumed input file   |
|-------------------|--|
| timestep          | ( default=1.0 ) the timestep that was used in the calculation that produced this trajectory in picoseconds   |
| trajectory-stride | ( default=1 ) the frequency with which frames were output to this trajectory during the simulation (0 means that the number of the step is read from the trajectory file, currently working only for xtc/trr files read with –ixtc/–trr) |
| multi             | ( default=0 ) set number of replicas for multi environment (needs mpi)   |

The following options are available

| help/-h          | ( default=off ) print this help  |
|------------------|--|
| help-debug       | ( default=off ) print special options that can be used to create regtests  |
| noatoms          | ( default=off ) don't read in a trajectory. Just use colvar files as specified in plumed.dat   |
| dump-full-virial | ( default=off ) with -dump-forces, it dumps the 9 components of the virial   |
| length-units     | units for length, either as a string or a number   |
| mass-units       | units for mass in pdb and mc file, either as a string or a number  |
| charge-units     | units for charge in pdb and mc file, either as a string or a number  |
| dump-forces      | dump the forces on a file  |
| dump-forces-fmt  | ( default=%f ) the format to use to dump the forces  |
| pdb              | provides a pdb with masses and charges   |
| mc               | provides a file with masses and charges as produced with DUMPMASSCHARGE  |
| box              | comma-separated box dimensions (3 for orthorombic, 9 for generic)  |
| natoms           | provides number of atoms - only used if file format does not contain number of atoms   |
| debug-forces     | output a file containing the forces due to the bias evaluated using numerical derivatives and using the analytical derivatives implemented in plumed |

## **Examples**

The following command tells plumed to postprocess the trajectory contained in trajectory.xyz by performing the actions described in the input file plumed.dat. If an action that takes the stride keyword is given a stride equal to n then it will be performed only on every nth frame in the trajectory file.

```
plumed driver --plumed plumed.dat --ixyz trajectory.xyz
```

The following command tells plumed to postprocess the trajectory contained in trajectory.xyz. by performing the actions described in the input file plumed.dat. Here though –trajectory-stride is set equal to the frequency with which frames were output during the trajectory and the –timestep is equal to the simulation timestep. As such the STRIDE parameters in the plumed.dat files are no longer ignored and any files output resemble those that would have been generated had we run the calculation we are running with driver when the MD simulation was running.

```
\verb|plumed driver --plumed plumed.dat --ixyz trajectory.xyz --trajectory-stride 100 --timestep 0.001|\\
```

By default you have access to a subset of the trajectory file formats supported by VMD, e.g. xtc and dcd:

```
plumed driver --plumed plumed.dat --pdb diala.pdb --mf_xtc traj.xtc --trajectory-stride 100 --timestep 0.001
```

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where -mf\_ prefixes the extension of one of the accepted molfile plugin format.

To have support of all of VMD's plugins you need to recompile PLUMED. You need to download the SOURCE of VMD, which contains a plugins directory. Adapt build.sh and compile it. At the end, you should get the molfile plugins compiled as a static library libmolfile\_plugin.a. Locate said file and libmolfile\_plugin.h, and customize the configure command with something along the lines of:

```
configure [...] LDFLAGS="-ltcl8.5 -L/mypathtomolfilelibrary/ -L/mypathtotcl" CPPFLAGS="-I/mypathtolibmolfile_p
```

and rebuild.

Molfile plugin require periodic cell to be triangular (i.e. first vector oriented along x and second vector in xy plane). This is true for many MD codes. However, it could be false if you rotate the coordinates in your trajectory before reading them in the driver. Also notice that some formats (e.g. amber crd) do not specify atom number. In this case you can use the --natoms option:

```
plumed driver --plumed plumed.dat --imf_crd trajectory.crd --natoms 128
```

Check the available molfile plugins and limitations at http://www.ks.uiuc.edu/Research/vmd/plugins/molfile/.

Additionally, you can use the xdrfile implementation of xtc and trr. To this aim, just download and install properly the xdrfile library (see here: http://www.gromacs.org/Developer\_Zone/Programming\_Guide/XT C\_Library). If the xdrfile library is installed properly the PLUMED configure script should be able to detect it and enable it. Notice that the xdrfile implementation of xtc and trr is more robust than the molfile one, since it provides support for generic cell shapes.

## 9.2.1 READ

This is part of the generic module

Read quantities from a colvar file.

This Action can be used with driver to read in a colvar file that was generated during an MD simulation

**Description of components** 

The READ command will read those fields that are labelled with the text string given to the VALUE keyword. It will also read in any fields that are labelleded with the text string given to the VALUE keyword followed by a dot and a further string. If a single Value is read in this value can be referenced using the label of the Action. Alternatively, if multiple quanties are read in, they can be referenced elsewhere in the input by using the label for the Action followed by a dot and the character string that appeared after the dot in the title of the field.

#### Compulsory keywords

| STRIDE                    | ( default=1 ) the frequency with which the file should be read.  |  |
|---------------------------|--|--|
| EVERY                     | ( default=1 ) only read every ith line of the colvar file. This should be used if the colvar was written |  |
|                           | more frequently than the trajectory.   |  |
| VALUES<br>Generated by Do | the values to read from the file   |  |
| FILE                      | the values to read from the file xygen the name of the file from which to read these quantities          |  |

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# **Options**

| IGNORE_TIME   | ( default=off ) ignore the time in the colvar file. When this flag is not present read will be quite strict about the start time of the simulation and the stride between frames                        |  |
|---------------|---|--|
| IGNORE_FORCES | ( default=off ) use this flag if the forces added by any bias can be safely ignored. As an example forces can be safely ignored if you are doing postprocessing that does not involve outputting forces |  |
| UPDATE_FROM   | Only update this action from this time  |  |
| UPDATE_UNTIL  | Only update this action until this time   |  |

#### **Examples**

This input reads in data from a file called input\_colvar.data that was generated in a calculation that involved PLU ← MED. The first command reads in the data from the column headed phi1 while the second reads in the data from the column headed phi2.

```
rphi1:     READ FILE=input_colvar.data     VALUES=phi1
rphi2:     READ FILE=input_colvar.data     VALUES=phi2
PRINT ARG=rphi1,rphi2 STRIDE=500 FILE=output_colvar.data
```

# 9.3 gentemplate

This is part of the cltools module

gentemplate is a tool that you can use to construct template inputs for the various actions

The templates generated by this tool are primarily for use with Toni Giorgino's vmd gui. It may be useful however to use this tool as a quick aid memoir.

#### **Options**

| help/-h          | ( default=off ) print this help                       |
|------------------|---|
| list             | ( default=off ) print a list of the available actions |
| include-optional | ( default=off ) also print optional modifiers         |
| action           | print the template for this particular action         |

## **Examples**

The following generates template input for the action DISTANCE.

```
\verb"plumed gentemplate -- action DISTANCE"
```

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# 9.4 info

This is part of the citools module

This tool allows you to obtain information about your plumed version

You can specify the information you require using the following command line arguments

## **Options**

| help/-h       | ( default=off ) print this help  |
|---------------|--|
| configuration | ( default=off ) prints the configuration file                                  |
| root          | ( default=off ) print the location of the root directory for the plumed source |
| user-doc      | ( default=off ) print the location of user manual (html)                       |
| developer-doc | ( default=off ) print the location of user manual (html)                       |
| version       | ( default=off ) print the version number                                       |
| long-version  | ( default=off ) print the version number (long version)                        |
| git-version   | ( default=off ) print the version number (git version, if available)           |
|               |  |

## **Examples**

The following command returns the root directory for your plumed distribution.

plumed info --root

# 9.5 kt

This is part of the cltools module

Print out the value of  $k_BT$  at a particular temperature

# Compulsory keywords

| temp  | print the manual for this particular action   |  |
|-------|---|--|
| units | ( default=kj/mol ) the units of energy can be kj/mol, kcal/mol, j/mol, eV or the conversion factor from |  |
|       | kj/mol  |  |

## **Options**

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| help/-h | ( default=off ) print this help |
|---------|---------------------------------|
|         |                                 |

**Examples** 

The following command will tell you the value of  $k_BT$  when T is equal to 300 K in eV

```
plumed kt --temp 300 --units eV
```

## 9.6 manual

This is part of the cltools module

manual is a tool that you can use to construct the manual page for a particular action

The manual constructed by this action is in html. In all probability you will never need to use this tool. However, it is used within the scripts that generate plumed's html manual. If you need to use this tool outside those scripts the input is specified using the following command line arguments.

Compulsory keywords

| action | print the manual for this particular action |  |
|--------|---|--|
|--------|---|--|

**Options** 

| help/-h | ( default=off ) print this help                  |
|---------|--|
| vim     | ( default=off ) print the keywords in vim syntax |

**Examples** 

The following generates the html manual for the action DISTANCE.

```
plumed manual --action DISTANCE
```

# 9.7 pathtools

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This is part of the mapping module

pathtools can be used to construct paths from pdb data

The path CVs in PLUMED are curvilinear coordinates through a high dimensional vector space. Enhanced sampling calculations are ofen run using the progress along the paths and the distance from the path as CVs as this provides a convenient way of defining a reaction coordinate for a complicated process. This method is explained in the documentation for PATH.

The path itself is an ordered set of equally-spaced, high-dimensional frames the way in which these frames should be constructed will depend on the problem in hand. In other words, you will need to understand the reaction you wish to study in order to select a sensible set of frames to use in your path CV. This tool provides two methods that may be useful when it comes to constructing paths; namely:

- A tool that takes in an initial guess path in which the frames are not equally spaced. This tool adjusts the
  positions of the frames in order to make them equally spaced so that they can be used as the basis for a path
  CV.
- A tool that takes two frames as input and that allows you to return a linear path connecting these two frames.
   The output from this method may be useful as an initial guess path. It is arguable that a linear path rather defeats the purpose of the path CV method, however, as the whole purpose is to be able to define non-linear paths.

Notice that you can use these two methods and take advantage of all the ways of measuring Distances from reference configurations that are available within PLUMED. The way you do this with each of these tools described above is explained in the example below.

The atoms involved can be specified using

| start | a pdb file that contains the structure for the initial frame of your path. For more information on how to specify lists of atoms see Groups and Virtual Atoms |
|-------|---|
| end   | a pdb file that contains the structure for the final frame of your path. For more information on how to specify lists of atoms see Groups and Virtual Atoms   |

Or alternatively by using

| path a pdb file that contains an initial path in which the frames are not equally space | ed |
|---|----|
|---|----|

#### Compulsory keywords

| fixed   | ( default=0 ) the frames to fix when constructing the path using -path |
|---------|--|
| metric  | the measure to use to calculate the distance between frames            |
| out     | the name of the file on which to output your path                      |
| arg-fmt | ( default=f ) the format to use for argument values in your frames     |

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| tolerance            | ( default=1E-4 ) the tolerance to use for the path reparameterization algorithm  |
|----------------------|--|
| nframes-before-start | ( default=1 ) the number of frames to include in the path before the first       |
|                      | frame  |
| nframes              | ( default=1 ) the number of frames between the start and end frames in your path |
| nframes-after-end    | ( default=1 ) the number of frames to put after the last frame of your path      |

#### **Options**

| help/-h | ( default=off ) print this help |
|---------|---------------------------------|
|         |                                 |

## **Examples**

The example below shows how you can take a set of unequally spaced frames from a pdb file named inpath.pdb and use pathtools to make them equally spaced so that they can be used as the basis for a path CV. The file containing this final path is named outpath.pdb.

```
plumed pathtools --path inpath.pdb --metric EUCLIDEAN --out outpath.pdb
```

The example below shows how can create an initial linear path connecting the two pdb frames in start.pdb and end.pdb. In this case the path output to path.pdb will consist of 6 frames: the initial and final frames that were contained in start.pdb and end.pdb as well as four equally spaced frames along the vector connecting start.pdb to end.pdb.

```
plumed pathtools --start start.pdb --end end.pdb --nframes 4 --metric OPTIMAL --out path.pdb
```

Often the idea with path cvs is to create a path connecting some initial state A to some final state B. You would in this case have representative configurations from your A and B states defined in the input files to pathtools that we have called start.pdb and end.pdb in the example above. Furthermore, it may be useful to have a few frames before your start frame and after your end frame. You can use path tools to create these extended paths as shown below. In this case the final path would now consist of 8 frames. Four of these frames would lie on the vector connecting state A to state B, there would be one frame each at start.pdb and end.pdb as well as one frame just before start.pdb and one frame just after end.pdb. All these frames would be equally spaced.

```
plumed pathtools --start start.pdb --end end.pdb --nframes 4 --metric OPTIMAL --out path.pdb --nframes-before-
```

Notice also that when you reparameterise paths you must choose two frames to fix. Generally you chose to fix the states that are representative of your states A and B. By default pathtools will fix the first and last frames. You can, however, change the states to fix by taking advantage of the fixed flag as shown below.

```
plumed pathtools --path inpath.pdb --metric EUCLIDEAN --out outpath.pdb --fixed 2,12
```

# 9.8 simplemd

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This is part of the cltools module

simplemd allows one to do molecular dynamics on systems of Lennard-Jones atoms.

The input to simplemd is spcified in an input file. Configurations are input and output in xyz format. The input file should contain one directive per line. The directives available are as follows:

#### Compulsory keywords

| nstep         | The number of steps of dynamics you want to run  |  |
|---------------|--|--|
| temperature   | ( default=NVE ) the temperature at which you wish to run the simulation in LJ units  |  |
| friction      | ( default=off ) The friction (in LJ units) for the langevin thermostat that is used to keep the                                    |  |
|               | temperature constant   |  |
| tstep         | ( default=0.005 ) the integration timestep in LJ units   |  |
| inputfile     | An xyz file containing the initial configuration of the system   |  |
| forcecutoff   | ( default=2.5 )  |  |
| listcutoff    | ( default=3.0 )  |  |
| outputfile    | An output xyz file containing the final configuration of the system  |  |
| nconfig       | ( default=10 ) The frequency with which to write configurations to the trajectory file followed by the name of the trajectory file |  |
| nstat         | ( default=1 ) The frequency with which to write the statistics to the statistics file followed by the name of the statistics file  |  |
| maxneighbours | ( default=10000 ) The maximum number of neighbours an atom can have  |  |
| idum          | ( default=0 ) The random number seed   |  |
| ndim          | ( default=3 ) The dimensionality of the system (some interesting LJ clusters are two dimen-  |  |
|               | sional)  |  |
| wrapatoms     | ( default=false ) If true, atomic coordinates are written wrapped in minimal cell  |  |

## **Examples**

You run an MD simulation using simplemd with the following command:

```
plumed simplemd < in
```

The following is an example of an input file for a simplemd calculation. This file instructs simplemd to do 50 steps of MD at a temperature of 0.722

```
nputfile input.xyz
outputfile output.xyz
temperature 0.722
tstep 0.005
friction 1
forcecutoff 2.5
listcutoff 3.0
nstep 50
nconfig 10 trajectory.xyz
nstat 10 energies.dat
```

If you run the following a description of all the directives that can be used in the input file will be output.

```
\verb"plumed simplemd --help"
```

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# 9.9 sum\_hills

This is part of the cltools module

sum\_hills is a tool that allows one to to use plumed to post-process an existing hills/colvar file

## **Options**

| help/-h    | ( default=off ) print this help  |
|------------|--|
| help-debug | ( default=off ) print special options that can be used to create regtests  |
| negbias    | ( default=off ) print the negative bias instead of the free energy (only needed with welltempered runs and flexible hills)   |
| nohistory  | ( default=off ) to be used with -stride: it splits the bias/histogram in pieces without previous history   |
| mintozero  | ( default=off ) it translate all the minimum value in bias/histogram to zero (usefull to compare results)  |
| hills      | specify the name of the hills file   |
| histo      | specify the name of the file for histogram a colvar/hills file is good   |
| stride     | specify the stride for integrating hills file (default 0=never)  |
| min        | the lower bounds for the grid  |
| max        | the upper bounds for the grid  |
| bin        | the number of bins for the grid  |
| spacing    | grid spacing, alternative to the number of bins  |
| idw        | specify the variables to be used for the free-energy/histogram (default is all). With –hills the other variables will be integrated out, with –histo the other variables won't be considered |
| outfile    | specify the outputfile for sumhills  |
| outhisto   | specify the outputfile for the histogram   |
| kt         | specify temperature in energy units for integrating out variables  |
| sigma      | a vector that specify the sigma for binning (only needed when doing histogram  |
| fmt        | specify the output format  |

## **Examples**

a typical case is about the integration of a hills file:

```
plumed sum_hills --hills PATHTOMYHILLSFILE
```

The default name for the output file will be fes.dat Note that starting from this version plumed will automatically detect the number of the variables you have and their periodicity. Additionally, if you use flexible hills (multivariate gaussians), plumed will understand it from the HILLS file.

now sum\_hills tool accepts als multiple files that will be integrated one after the other

plumed sum\_hills --hills PATHTOMYHILLSFILE1,PATHTOMYHILLSFILE2,PATHTOMYHILLSFILE3

9.9 sum\_hills 437

if you want to integrate out some variable you do

```
plumed sum_hills --hills PATHTOMYHILLSFILE --idw t1 --kt 0.6
```

where with –idw you define the variables that you want all the others will be integrated out. –kt defines the temperature of the system in energy units. (be consistent with the units you have in your hills: plumed will not check this for you) If you need more variables then you may use a comma separated syntax

```
plumed sum_hills --hills PATHTOMYHILLSFILE --idw t1,t2 --kt 0.6
```

You can define the output grid only with the number of bins you want while min/max will be detected for you

```
plumed sum_hills --bin 99,99 --hills PATHTOMYHILLSFILE
```

or full grid specification

```
plumed sum_hills --bin 99,99 --min -pi,-pi --max pi,pi --hills PATHTOMYHILLSFILE
```

You can of course use numbers instead of -pi/pi.

You can use a -stride keyword to have a dump each bunch of hills you read

```
plumed sum_hills --stride 300 --hills PATHTOMYHILLSFILE
```

You can also have, in case of welltempered metadynamics, only the negative bias instead of the free energy through the keyword –negbias

```
plumed sum_hills --negbias --hills PATHTOMYHILLSFILE
```

Here the default name will be negativebias.dat

From time to time you might need to use HILLS or a COLVAR file as it was just a simple set of points from which you want to build a free energy by using -(1/beta)log(P) then you use -histo

```
plumed sum_hills --histo PATHTOMYCOLVARORHILLSFILE --sigma 0.2,0.2 --kt 0.6
```

in this case you need a –kt to do the reweighting and then you need also some width (with the –sigma keyword) for the histogram calculation (actually will be done with gaussians, so it will be a continuous histogram) Here the default output will be histo.dat. Note that also here you can have multiple input files separated by a comma.

Additionally, if you want to do histogram and hills from the same file you can do as this

```
plumed sum_hills --hills --histo PATHTOMYCOLVARORHILLSFILE --sigma 0.2,0.2 --kt 0.6
```

The two files can be eventually the same

Another interesting thing one can do is monitor the difference in blocks as a metadynamics goes on. When the bias deposited is constant over the whole domain one can consider to be at convergence. This can be done with the –nohistory keyword

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```
plumed sum_hills --stride 300 --hills PATHTOMYHILLSFILE --nohistory
```

and similarly one can do the same for an histogram file

```
plumed sum_hills --histo PATHTOMYCOLVARORHILLSFILE --sigma 0.2,0.2 --kt 0.6 --nohistory
```

just to check the hypothetical free energy calculated in single blocks of time during a simulation and not in a cumulative way

Output format can be controlled via the -fmt field

```
plumed sum_hills --hills PATHTOMYHILLSFILE --fmt %8.3f
```

where here we chose a float with length of 8 and 3 digits

The output can be named in a arbitrary way:

```
plumed sum_hills --hills PATHTOMYHILLSFILE --outfile myfes.dat
```

will produce a file myfes.dat which contains the free energy.

If you use stride, this keyword is the suffix

```
plumed sum_hills --hills PATHTOMYHILLSFILE --outfile myfes_ --stride 100
```

will produce myfes\_0.dat, myfes\_1.dat, myfes\_2.dat etc.

The same is true for the output coming from histogram

```
plumed sum_hills --histo HILLS --kt 2.5 --sigma 0.01 --outhisto myhisto.dat
```

is producing a file myhisto.dat while, when using stride, this is the suffix

```
plumed sum_hills --histo HILLS --kt 2.5 --sigma 0.01 --outhisto myhisto_ --stride 100
```

that gives myhisto 0.dat, myhisto 1.dat, myhisto 3.dat etc..

# **Chapter 10**

# **Miscelaneous**

- Comments
- · Continuation lines
- · Using VIM syntax file
- · Including other files
- · Loading shared libraries
- · Debugging the code
- · Changing exchange patterns in replica exchange
- · List of modules
- · Frequently used tools

## 10.1 Comments

If you are an organised sort of person who likes to remember what the hell you were trying to do when you ran a particular simulation you might find it useful to put comments in your input file. In PLUMED you can do this as comments can be added using a # sign. On any given line everything after the # sign is ignored so erm... yes add lines of comments or trailing comments to your hearts content as shown below (using Shakespeare is optional):

```
# This is the distance between two atoms:
DISTANCE ATOM=1,2 LABEL=d1
UPPER_WALLS ARG=d1 AT=3.0 KAPPA=3.0 LABEL=Snout # In this same interlude it doth befall.
# That I, one Snout by name, present a wall.
```

(see DISTANCE and UPPER\_WALLS)

An alternative to including comments in this way is to use line starting ENDPLUMED. Everything in the PLUMED input after this keyword will be ignored.

#### 10.2 Continuation lines

If your input lines get very long then editing them using vi and other such text editors becomes a massive pain in the arse. We at PLUMED are aware of this fact and thus have provided a way of doing line continuations so as to make your life that much easier - aren't we kind? Well no not really, we have to use this code too. Anyway, you can do continuations by using the "..." syntax as this makes this:

```
DISTANCES ATOMS1=1,300 ATOMS2=1,400 ATOMS3=1,500 LABEL=dist
```

#### (see DISTANCES)

#### equivalent to this:

```
DISTANCES ...

LABEL=dist

# we can also insert comments here
ATOMS1=1,300

# multiple kewords per line are allowed
ATOMS2=1,400 ATOMS3=1,500

#empty lines are also allowed
... DISTANCES
```

Notice that the closing . . . is followed by the word DISTANCES. This is optional, but might be useful to find more easily which is the matching start of the statement. The following is equally correct

```
DISTANCES ...

LABEL=dist

# we can also insert comments here
ATOMS1=1,300

# multiple kewords per line are allowed
ATOMS2=1,400 ATOMS3=1,500

#empty lines are also allowed
...
```

Notice that PLUMED makes a check that the word following the closing . . . is actually identical to the first word in the line with the first . . . . If not, it will throw an error. Also notice that you might put more than one word in the first line. E.g.

```
DISTANCES LABEL=dist ...

# we can also insert comments here
ATOMS1=1,300

# multiple kewords per line are allowed
ATOMS2=1,400 ATOMS3=1,500

#empty lines are also allowed
...
```

## or, equivalently,

```
dist: DISTANCES ...
# we can also insert comments here
  ATOMS1=1,300
# multiple kewords per line are allowed
  ATOMS2=1,400 ATOMS3=1,500
#empty lines are also allowed
...
```

# 10.3 Using VIM syntax file

For the impatients:

· Add the following to your .vimrc file:

```
" This allows including the proper PLUMED syntax file:
:let &runtimepath.=','.$PLUMED_VIMPATH
" This makes autocompletion work in the expected way:
:set completeopt=longest,menuone
" This enables bindings of F2/F3/F4 to plumed specific commands:
:let plumed_shortcuts=1
```

• When you open a PLUMED input file, you can enable syntax highlighting with:

```
:set ft=plumed
```

This will also enable autocompletion. Use <CTRL-X><CTRL-O> to autocomplete a word.

· If you want to fold multiline statements, type

```
:setlocal foldmethod=syntax
```

- While editing a plumed input file, you can use command :PHelp (or shortcut <F2>) to show in a split window a short help about the action defined in the line where the cursor is. Typing :PHelp again (or pushing <F2>) you will close that window. With <CTRL-W><CTRL-W> you go back and forth between the two windows.
- When you open a file starting with #! FIELDS, VIM will automatically understand it is a PLUMED outpt file (VIM filetype = plumedf) and will color fields and data columns with alternating colors. Typing :PPlus and :PMinus (or pushing <F3> and <F4>) you can move a highlighted column.

See below for more detailed instructions.

Configuration

When PLUMED is compiled, directories help and syntax will appear in builddir/vim. They contain a VIM plugin that can be used to highlight proper PLUMED instructions in a PLUMED input file and to quickly retrieve help. There is also a file builddir/vim/scripts.vim that helps VIM in recognizing PLUMED output files.

#### Warning

Notice that these file do not appear if you are cross compiling. In this case, you must copy the plugin files from another machine.

To make VIM aware of these files, you should copy them to your \$HOME/.vim directory. Later you can enable plumed syntax with the command

```
:set ft=plumed
```

If you work in an environment where several PLUMED versions are installed (e.g. using env modules), we recommend the following procedure:

- Install PLUMED
- Add to your .vimrc file the following line:

```
:let &runtimepath.=','.$PLUMED_VIMPATH
```

The modulefile provided with PLUMED should set the PLUMED\_VIMPATH environemnt variable to the proper path. Thus, when working with a given PLUMED module loaded, you should be able to enable to proper syntax by just typing

```
:set ft=plumed
```

in VIM. Notice that the variable PLUMED\_VIMPATH is also set in the sourceme.sh script in the build directory. This, if you modify your .vimrc file as suggested, you will be able to use the correct syntax both when using an installed PLUMED and when running from a just compiled copy.

If you are tired of typing : set ft=plumed, you can use a modeline. Add to your .vimrc file the following commands

```
:set modeline
:set modelines=5
```

Then, at the beginning of your PLUMED input file, put the following comment:

```
# vim:ft=plumed
d: DISTANCE ATOMS=1,2
RESTRAINT ARG=d AT=0.0 KAPPA=1.0
```

Now, every time you open this file, you will see it highlighted.

Syntax highlighting

The syntax file contains a definition of all possible PLUMED actions and keywords. It is designed to allow for a quick validation of the PLUMED input file before running it. As such, all the meaningful words in the input should be highlighted:

- Valid action names (such as METAD) and labels (such as metad: or LABEL=metad) will be highlighted in the brightest way (Type in VIM). Those are the most important words.
- Keyword and flag names (such as ATOMS= or COMPONENTS when part of the action DISTANCE) will be highlighted with a different color (Statement in VIM).
- Values provided by users (such as the number of the atoms following ATOMS=) will be highlighted with a different color (String in VIM).
- Comments (see Comments) will be highlighted as comments (Comment in VIM).

If you see something that is not highlighted and appears in black, this is likely going to result in an error at runtime. Think of this as a sort of preliminary spell-check. For this checks to be effective, we recommend to use a syntax file generated with exactly the same version of PLUMED that you are using. In case you find that parts of an input file that is valid are not highlighted, then please report it as a bug. On the contrary, you cannot expect the VIM syntax file to recognize all possible errors in a PLUMED input. Thus, a file for which the highlighting looks correct might still contain errors.

Multi-line folding

Notice that syntax highlighting also allow VIM to properly fold multi-line actions. Try to do the following:

- · Open a PLUMED input file
- · Enable PLUMED syntax

```
:set ft=plumed
```

· Enable syntax-based folding

```
:setlocal foldmethod=syntax
```

Now look at what happened to all the multi-line statements in PLUMED (i.e. those using Continuation lines). As you can see, they will be folded into single lines. Folded lines can be expanded with  $z \circ$  and folded with  $z \circ$ . Look at VIM documentation to learn more. In case you want to use this feature, we suggest you to put both label and action type on the first line of multi-line statements. E.g.

```
m: METAD ...
ARG=d
HEIGHT=1.0
SIGMA=0.5
PACE=100
...

will be folded to

--- 6 lines: m: METAD ...

ARG=d
HEIGHT=1.0
SIGMA=0.5
PACE=100
...

will be folded to

--- 6 lines: METAD LABEL=m ...

WITAD LABEL=m ...

ARG=d
HEIGHT=1.0
SIGMA=0.5
PACE=100
...

will be folded to
```

This will allow you to easily identify the folded lines by seeing the most important information, that is the action type (METAD) and its label (m). This feature is convenient if you want to browse files that contain a lot of actions defined on multiple lines.

#### Autocompletion

Another VIM feature that comes when you load PLUMED syntax is autocompletion of PLUMED actions and keywords. Open your favorite PLUMED input file and set it to PLUMED syntax highlighting with

```
:set ft=plumed
```

Now go into insert mode pressing i and type DU followed by <CTRL+X><CTRL+O>. Here <CTRL+X> stands for autocompletion and <CTRL+O> for omnifunc autocompletion. You will see a short menu listing the following actions

DUMPATOMS
DUMPDERIVATIVES
DUMPFORCES
DUMPMASSCHARGE
DUMPMULTICOLVAR
DUMPPROJECTIONS

That is, all the actions starting with DU. You can navigate it with up and down arrows so as to choose the best match.

Notice that the default behavior of VIM is to use the first match by default. In the first example (DU<CTRL+X><C 
TRL+O), it would be DUMPATOMS. The following settings make it work as most of the people expect:

```
:set completeopt=longest, menuone
```

With these settings, in the first example (DU < CTRL + X > < CTRL + O) VIM will only complete up to the longest common part (DUMP).

As you can imagine, if you use autocompletion after you have typed the word DISTANCE followed by a space you will see a menu listing LABEL=, COMPONENTS, etc. Basically, all the keywords that are possibly used withint a DISTANCE line will be shown.

Quick help

You can also retrieve quick explanation of the input options for a specific collective variable. Try to do the following. Enable plumed syntax:

```
:set ft=plumed
```

Then add the following line

DISTANCE

Now, in normal mode, go with the cursor on the DISTANCE line and type

:PHelp

A new split window should appear containing some documentation about the DISTANCE collective variable. You can go back and forth between the two windows with <CTRL+W><CTRL+W>, as usually in vim. Notice that if you are in the help window and type :PHelp this window will be closed.

To make the navigation easier, you can add a shortcut in your .vimrc file. For example, adding:

```
: nmap <F2> : PHelp<CR>
```

you should be able to open and close the manual hitting the F2 key. This is done automatically in the PLUMED syntax file if you add let plumed\_shortcuts=1 to your vimrc file.

Displaying output files

Most of the PLUMED output files look like this

```
#! FIELDS A B C
1 2 3
```

This is useful since in the header you can see the name of the quantities that are printed in the data lines. However, when you have an output file with many columns it might be a bit error prone to count them. To simplify this, when PLUMED syntax for VIM is configured properly VIM should be able to:

- Detect that this file is a PLUMED output file with fields, automatically setting its type to plumedf. If not, just type :set ft=plumedf.
- · Show this file with syntax highlighting to increase its readability.

Notice that the syntax file for the output files (plumedf.vim) is not the same one that is used for the PLUMED input file (plumed.vim).

To make output files more readable, vi will show FIELDS and SET words in a different color, and data columns with alternating colors (e.g. dark/light/dark/light). The colors in the columns are consistent with those shown in the FIELD line. In the example above, 1, 2, and 3 will be of the same color as A, B, and C respectively. This should make it much easier to find which columns correspond to a given quantity.

It is also possible to highlight a specific field of the file. Typing

```
:5PCol
```

you will highlight the fifth field. Notice that in the FIELDS line (the first line of the file) the 7th word of the line will be highlighted, which is the one containing the name of the field. This allows for easy matching of values shown in the file and tags provided in the FIELDS line. The highlighted column can be moved back and forth using :PPlus and :PMinus. Adding a count to the command will move the highlighted column more. E.g. :2PPlus will move the column to the right twice.

If you have a long output file, it might be convenient to split it with :split so that one of the two windows will only show the header. The other window can be used to navigate the file.

To make the navigation easier, you can add a shortcut in your .vimrc file. For example, adding:

```
: map <F3> :PMinus<CR>
: map <F4> :PPlus<CR>
```

you should be able to move the highlight column using F3 and F4 buttons. This is done automatically in the PLUMED syntax file if you add let plumed\_shortcuts=1 to your vimrc file.

## 10.4 Including other files

If, for some reason, you want to spread your PLUMED input over a number of files you can use INCLUDE as shown below:

```
INCLUDE FILE=filename
```

So, for example, a single "plumed.dat" file:

```
DISTANCE ATOMS=0,1 LABEL=dist RESTRAINT ARG=dist
```

```
(see DISTANCE and RESTRAINT)
```

could be split up into two files as shown below:

```
DISTANCE ATOMS=0,1 LABEL=dist INCLUDE FILE=toBeIncluded.dat
```

plus a "toBeIncluded.dat" file

```
RESTRAINT ARG=dist
```

However, when you do this it is important to recognise that INCLUDE is a real directive that is only resolved after all the Comments have been stripped and the Continuation lines have been unrolled. This means it is not possible to do things like:

```
# this is wrong:
DISTANCE INCLUDE FILE=options.dat
RESTRAINT ARG=dist
```

#### 10.4.1 INCLUDE

This is part of the generic module

Includes an external input file, similar to "#include" in C preprocessor.

Useful to split very large plumed.dat files.

Compulsory keywords

**FILE** | file to be included

#### **Examples**

#### This input

```
c1: COM ATOMS=1-100
c2: COM ATOMS=101-202
d: DISTANCE ARG=c1,c2
PRINT ARG=d
```

#### can be replaced with

```
INCLUDE FILE=pippo.dat
d: DISTANCE ARG=c1,c2
PRINT ARG=d
```

#### where the content of file pippo.dat is

```
c1: COM ATOMS=1-100
c2: COM ATOMS=101-202
```

(see also COM, DISTANCE, and PRINT).

# 10.5 Loading shared libraries

You can introduce new functionality into PLUMED by placing it directly into the src directory and recompiling the PLUMED libraries. Alternatively, if you want to keep your code independent from the rest of PLUMED (perhaps so you can release it independely - we won't be offended), then you can create your own dynamic library. To use this in conjuction with PLUMED you can then load it at runtime by using the LOAD keyword as shown below:

LOAD FILE=library.so

N.B. If your system uses a different suffix for dynamic libraries (e.g. macs use .dylib) then PLUMED will try to automatically adjust the suffix accordingly.

10.5.1 LOAD

This is part of the setup module

Loads a library, possibly defining new actions.

It is available only on systems allowing for dynamic loading. It can also be fed with a cpp file, in which case the file is compiled first.

Compulsory keywords

FILE file to be loaded

**Examples** 

If you have a shared object named extensions.so and want to use the functionalities implemented in it within PL← UMED you can load it with the following syntax

LOAD FILE=extensions.so

As a more practical example, imagine that you want to make a small change to one collective variable that is already implemented in PLUMED, say DISTANCE. Copy the file src/colvar/Distance.cpp into your work directory, rename it as Distance2.cpp and edit it as you wish. It might be better to also replace any occurence of the string DISTANCE within the file with DISTANCE2, so that both old and new implementation will be available with different names. Then you can compile it into a shared object using

> plumed mklib Distance2.cpp

This will generate a file <code>Distance2.so</code> (or <code>Distance2.dylib</code> on a mac) that can be loaded. Now you can use your new implementation with the following input

```
# load the new library
LOAD FILE=Distance2.so
# compute standard distance
d: DISTANCE ATOMS=1,10
# compute modified distance
d2: DISTANCE2 ATOMS=1,10
# print them on a file
PRINT ARG=d,d2 FILE=compare-them
```

You can even skip the initial step and directly feed PLUMED with the <code>Distance2.cpp</code> file: it will be compiled on the fly.

```
# load the new definition
# this is a cpp file so it will be compiled
LOAD FILE=Distance2.cpp
# compute standard distance
d: DISTANCE ATOMS=1,10
# compute modified distance
d2: DISTANCE2 ATOMS=1,10
# print them on a file
PRINT ARG=d,d2 FILE=compare-them
```

This will allow to make quick tests while developing your own variables. Of course, after your implementation is ready you might want to add it to the PLUMED source tree and recompile the whole PLUMED.

# 10.6 Debugging the code

The DEBUG action provides some functionality for debugging the code that may be useful if you are doing very intensive development of the code of if you are running on a computer with a strange architecture.

#### 10.6.1 **DEBUG**

This is part of the generic module

Set some debug options.

Can be used while debugging or optimizing plumed.

Compulsory keywords

#### **Options**

| logActivity       | ( default=off ) write in the log which actions are inactive and which are inactive    |
|-------------------|---|
| IogRequestedAtoms | ( default=off ) write in the log which atoms have been requested at a given time      |
| NOVIRIAL          | ( default=off ) switch off the virial contribution for the entirity of the simulation |

| DETAILED_TIMERS | ( default=off ) switch on detailed timers                |
|-----------------|--|
| FILE            | the name of the file on which to output these quantities |

#### **Examples**

```
# print detailed (action-by-action) timers at the end of simulation
DEBUG DETAILED_TIMERS
# dump every two steps which are the atoms required from the MD code
DEBUG logRequestedAtoms STRIDE=2
```

# 10.7 Changing exchange patterns in replica exchange

Using the RANDOM\_EXCHANGES keyword it is possible to make exchanges betweem randomly chosen replicas. This is useful e.g. for bias exchange metadynamics ?.

## 10.7.1 RANDOM\_EXCHANGES

This is part of the generic module

Set random pattern for exchanges.

In this way, exchanges will not be done between replicas with consecutive index, but will be done using a random pattern. Typically used in bias exchange?.

**Options** 

| SEED | seed for random exchanges |
|------|---------------------------|
|      |                           |

## **Examples**

Using the following three input files one can run a bias exchange metadynamics simulation using a different angle in each replica. Exchanges will be randomly tried between replicas 0-1, 0-2 and 1-2

Here is plumed.0.dat

```
RANDOM_EXCHANGES
t: TORSION ATOMS=1,2,3,4
METAD ARG=t HEIGHT=0.1 PACE=100 SIGMA=0.3
```

Here is plumed.1.dat

```
RANDOM_EXCHANGES
t: TORSION ATOMS=2,3,4,5
METAD ARG=t HEIGHT=0.1 PACE=100 SIGMA=0.3
```

#### Here is plumed.2.dat

```
RANDOM_EXCHANGES
t: TORSION ATOMS=3,4,5,6
METAD ARG=t HEIGHT=0.1 PACE=100 SIGMA=0.3
```

#### Warning

Multi replica simulations are presently only working with gromacs.

The directive should appear in input files for every replicas. In case SEED is specified, it should be the same in all input files.

## 10.8 List of modules

The functionality in PLUMED 2 is divided into a small number of modules. Some users may only wish to use a subset of the functionality available within the code while others may wish to use some of PLUMED's more complicated features. For this reason the plumed source code is divided into modules, which users can activate or deactivate to their hearts content.

You can activate a module at configure time using the keyword --enable-modules. For example:

```
./configure --enable-modules=modulename
```

will enable module called modulename. A module that is on by default can be disabled using the following syntax

```
./configure --enable-modules=-modulename
```

To enable or disable multiple modules one should provide them as a : separated list. Notice that +modulename and modulename both activate the module, whereas -modulename deactivates it. E.g.

```
./configure --enable-modules=+crystallization:-colvar
```

will disable the colvar module and enable the crystallization module. Also notice that : can be omitted when using + or -. Thus, the same can be obtained with

```
./configure --enable-modules=+crystallization-colvar
```

If you repeat the --enable-modules keyword only the last instance will be used. Thus ./configure --enable-modules=crystallization --enable-modules=-colvar will not do what you expect!

There are also some shortcuts available:

- ./configure --enable-modules=all to enable all optional modules. This includes the maximum number of features in PLUMED, including modules that might not be properly functional.
- ./configure --enable-modules=none or ./configure --disable-modules to disable all optional modules. This produces a minimalistic PLUMED which can be used as a library but has no command line tools and no collective variables or biasing methods.
- ./configure --enable-modules=reset **or** ./configure --enable-modules **to enable** the default modules.

The two kinds of syntax can be combined and, for example, ./configure --enable-modules=none $\leftrightarrow$ :colvar will result in a PLUMED with all the modules disabled with the exception of the colvar module.

Some modules are active by default in the version of PLUMED 2 that you download from the website while others are inactive. The following lists all of the modules that are available in plumed and tells you whether or not they are active by default.

| Module name        | Default behavior |
|--------------------|------------------|
| adjmat             | off              |
| analysis           | on               |
| bias               | on               |
| cltools            | on               |
| colvar             | on               |
| crystallization    | off              |
| function           | on               |
| generic            | on               |
| manyrestraints     | off              |
| mapping            | on               |
| molfile            | on               |
| multicolvar        | on               |
| secondarystructure | on               |
| setup              | on               |
| vatom              | on               |
| ves                | off              |

Until PLUMED 2.2, it was also possible to switch on or off modules by adding files in the plumed2/src directory. Since PLUMED 2.3 this is discouraged, since any choice made in this manner will be overwritten next time ./configure is used.

# 10.9 Frequently used tools

| histogrambead     | INTERNAL | A function that can be used to calculate whether quantities are between fixed |
|-------------------|----------|---|
|                   |          | upper and lower bounds.   |
| kernelfunctions   | INTERNAL | Functions that are used to construct histograms                               |
| landmarkselection | INTERNAL | This is currently a filler page.  |
| switchingfunction | INTERNAL | Functions that measure whether values are less than a certain quantity.       |

| Regular Expressions | POSIX regular expressions can be used to select multiple actions when using ARG (i.e. PRINT). |
|---------------------|---|
| Files               | Dealing with Input/Outpt  |

## 10.9.1 histogrambead

A function that can be used to calculate whether quantities are between fixed upper and lower bounds. A function that can be used to calculate whether quantities are between fixed upper and lower bounds.

If we have multiple instances of a variable we can estimate the probability distribution (pdf) for that variable using a process called kernel density estimation:

$$P(s) = \sum_{i} K\left(\frac{s - s_i}{w}\right)$$

In this equation K is a symmetric funciton that must integrate to one that is often called a kernel function and w is a smearing parameter. From a pdf calculated using kernel density estimation we can calculate the number/fraction of values between an upper and lower bound using:

$$w(s) = \int_{a}^{b} \sum_{i} K\left(\frac{s - s_{i}}{w}\right)$$

All the input to calculate a quantity like w(s) is generally provided through a single keyword that will have the following form:

KEYWORD={TYPE UPPER= a LOWER= b SMEAR=  $\frac{w}{b-a}$ }

This will calculate the number of values between a and b. To calculate the fraction of values you add the word NORM to the input specification. If the function keyword SMEAR is not present w is set equal to 0.5(b-a). Finally, type should specify one of the kernel types that is present in plumed. These are listed in the table below:

| TYPE       | FUNCTION   |
|------------|--|
| GAUSSIAN   | $\frac{1}{\sqrt{2\pi}w} \exp\left(-\frac{(s-s_i)^2}{2w^2}\right)$                  |
| TRIANGULAR | $\frac{1}{2w}\left(1 \left \frac{s - s_i}{w}\right \right)  \frac{s - s_i}{w} < 1$ |

Some keywords can also be used to calculate a descretized version of the histogram. That is to say the number of values between a and b, the number of values between b and c and so on. A keyword that specifies this sort of calculation would look something like

KEYWORD={TYPE UPPER= a LOWER= b NBINS= n SMEAR=  $\frac{w}{n(b-a)}$ }

This specification would calculate the following vector of quantities:

$$w_j(s) = \int_{a + \frac{j-1}{n}(b-a)}^{a + \frac{j}{n}(b-a)} \sum_i K\left(\frac{s - s_i}{w}\right)$$

#### 10.9.2 kernelfunctions

Functions that are used to construct histograms Functions that are used to construct histograms

Constructing histograms is something you learnt to do relatively early in life. You perform an experiment a number of times, count the number of times each result comes up and then draw a bar graph that describes how often each of the results came up. This only works when there are a finite number of possible results. If the result a number between 0 and 1 the bar chart is less easy to draw as there are as many possible results as there are numbers between zero and one - an infinite number. To resolve this problem we replace probability, P with probability density,  $\pi$ , and write the probability of getting a number between a and b as:

$$P = \int_{a}^{b} \mathrm{d}x \pi(x)$$

To calculate probability densities from a set of results we use a process called kernel density estimation. Histograms are accumulated by adding up kernel functions, K, with finite spatial extent, that integrate to one. These functions are centered on each of the n-dimensional data points,  $\mathbf{x}_i$ . The overall effect of this is that each result we obtain in our experiments contributes to the probability density in a finite sized region of the space.

Expressing all this mathematically in kernel density estimation we write the probability density as:

$$\pi(\mathbf{x}) = \sum_{i} K\left[ (\mathbf{x} - \mathbf{x}_{i})^{T} \Sigma (\mathbf{x} - \mathbf{x}_{i}) \right]$$

where  $\Sigma$  is an  $n \times n$  matrix called the bandwidth that controls the spatial extent of the kernel. Whenever we accumulate a histogram (e.g. in HISTOGRAM or in METAD) we use this technique.

There is thus some flexibility in the particular function we use for  $K[\mathbf{r}]$  in the above. The following variants are available.

| TYPE               | FUNCTION   |
|--------------------|--|
| gaussian           | $f(r) = \frac{1}{(2\pi)^n \sqrt{ \Sigma^{-1} }} \exp(-0.5r^2)$   |
| truncated-gaussian | $f(r) = \frac{1}{(2\pi)^n \sqrt{ \Sigma^{-1} } \left(\frac{(-6.25/sqrt2) - (-6.25/sqrt2)}{2}\right)^n} \exp\left(-0.5r^2\right)$ |
| triangular         | $f(r) = \frac{3}{V}(1 -  r )H(1 -  r )$  |
| uniform            | $f(r) = \frac{1}{V}H(1 -  r )$   |

In the above H(y) is a function that is equal to one when y > 0 and zero when  $y \le 0$ . n is the dimensionality of the vector  $\mathbf{x}$  and V is the volume of an elipse in an n dimensional space which is given by:

$$V = |\Sigma^{-1}| \frac{\pi^{\frac{n}{2}}}{(\frac{n}{2})!} \quad \text{for even} \quad n$$

$$V = |\Sigma^{-1}| \frac{2^{\frac{n+1}{2}} \pi^{\frac{n-1}{2}}}{n!!}$$

In METAD the normalization constants are ignored so that the value of the function at r=0 is equal to one. In addition in METAD we must be able to differentiate the bias in order to get forces. This limits the kernels we can use in this method. Notice also that Gaussian kernels should have infinite support. When used with grids, however, they are assumed to only be non-zero over a finite range. The difference between the truncated-gaussian and regular gaussian is that the trucated gaussian is scaled so that its integral over the grid is equal to one when it is normalised. The integral of a regular gaussian when it is evaluated on a grid will be slightly less that one because of the truncation of a function that should have infinite support.

## 10.9.3 landmarkselection

This is part of the analysis module

This is currently a filler page. This is currently a filler page.

Just use LANDMARKS=ALL. More complex versions will appear in later versions.

#### 10.9.4 switchingfunction

Functions that measure whether values are less than a certain quantity. Functions that measure whether values are less than a certain quantity.

Switching functions s(r) take a minimum of one input parameter  $d_0$ . For  $r \le d_0$  s(r) = 1.0 while for  $r > d_0$  the function decays smoothly to 0. The various switching functions available in plumed differ in terms of how this decay is performed.

Where there is an accepted convention in the literature (e.g. COORDINATION) on the form of the switching function we use the convention as the default. However, the flexibility to use different switching functions is always present generally through a single keyword. This keyword generally takes an input with the following form:

```
KEYWORD={TYPE <list of parameters>}
```

The following table contains a list of the various switching functions that are available in plumed 2 together with an example input.

| TYPE     | FUNCTION   | EXAMPLE INPUT   | DEFAULT PARAMETERS  |
|----------|--|---|---|
| RATIONAL | $s(r) = \frac{1 - \left(\frac{r - d_0}{r_0}\right)^n}{1 - \left(\frac{r - d_0}{r_0}\right)^m}$ | $ \begin{cases} \text{RATIONAL R\_0=} \ r_0 \ \text{D\_0=} \ d_0 \\ \text{NN=} \ n \ \text{MM=} \ m \end{cases} $ | $d_0 = 0.0, n = 6, m = 2n$  |
| EXP      | $s(r) = \exp\left(-\frac{r - d_0}{r_0}\right)$   | $\{ \text{EXP R\_0=} \ r_0 \ \text{D\_0=} \ d_0 \}$   | $d_0 = 0.0$   |
| GAUSSIAN | $s(r) = \exp\left(-\frac{(r-d_0)^2}{2r_0^2}\right)$  | {GAUSSIAN R_0= $r_0$ D_0= $d_0$ }   | $d_0 = 0.0$   |
| SMAP     | $s(r) = \left[1 + (2^{a/b} - 1)\left(\frac{r - d_0}{r_0}\right)^a\right]^{-b/c}$               | {SMAP R_0= $r_0$ D_0= $d_0$ A= $a$ B= $b$ }   | $d_0 = 0.0$   |
| Q        | $s(r) = \frac{1}{1 + \exp(\beta(r_{ij} - \lambda r_{ij}^0))}$                                  |   | $\begin{array}{lll} \lambda = 1.8,  \beta = 50nm^-1 \; \text{(all-atom)} \\ \lambda = 1.5,  \beta = 50nm^-1 \\ \text{(coarse-grained)} \end{array}$ |
| CUBIC    | $s(r) = (y - 1)^{2}(1 + 2y)$ where $y = \frac{r - r_{1}}{r_{0} - r_{1}}$                       | {CUBIC D_0= $r_1$ D_MAX= $r_0$ }  |   |
| TANH     | $s(r) = 1 - \tanh\left(\frac{r - d_0}{r_0}\right)$   | {TANH R_0= $r_0$ D_0= $d_0$ }   |   |
| MATHEVAL | s(r) = FUNC  |   |   |

#### Attention

Similarly to the MATHEVAL function, the MATHEVAL switching function only works if libmatheval is installed on the system and PLUMED has been linked to it Also notice that using MATHEVAL is much slower than using e.g. RATIONAL. Thus, the MATHEVAL switching function is useful to perform quick tests on switching functions with arbitrary form before proceeding to their implementation in C++.

For all the switching functions in the above table one can also specify a further (optional) parameter using the parameter keyword D\_MAX to assert that for  $r>d_{\rm max}$  the switching function can be assumed equal to zero. In this case the function is brought smoothly to zero by stretching and shifting it.

```
KEYWORD={RATIONAL R_0=1 D_MAX=3}
```

the resulting switching function will be  $s(r)=\frac{s'(r)-s'(d_{max})}{s'(0)-s'(d_{max})}$  where  $s'(r)=\frac{1-r^6}{1-r^{12}}$  Since PLUMED 2.2 this is the default. The old behavior (no stretching) can be obtained with the NOSTRETCH flag. The NOSTRETCH keyword is only provided for backward compatibility and might be removed in the future. Similarly, the STRETCH keyword is still allowed but has no effect.

Notice that switching functions defined with the simplified syntax are never stretched for backward compatibility. This might change in the future.

#### 10.9.5 Regular Expressions

When you use a collective variable that has many calculated components and you want to refer to them as arguments you can use regular expressions.

Since version 2.1, plumed takes advantage of a configuration scripts that detects libraries installed on your system. If regex library is found, then you will be able to use regular expressions to refer to collective variables or function names.

Regular expressions are enclosed in round braces and must not contain spaces (the components names have no spaces indeed, so why use them?).

As an example then command

```
d1: DISTANCE ATOMS=1,2 COMPONENTS
PRINT ARG=(d1\.[xy]) STRIDE=100 FILE=colvar FMT=%8.4f
```

will cause both the d1.x and d1.y components of the DISTANCE action to be printed out in the order that they are created by plumed. The "." character must be escaped in order to interpret it as a literal ".". An unescaped dot is a wildcard which is matched by any character, So as an example

```
d1: DISTANCE ATOMS=1,2 COMPONENTS
dxy: DISTANCE ATOMS=1,3

# this will match d1.x,d1.y,dxy
PRINT ARG=(d1.[xy]) STRIDE=100 FILE=colvar FMT=%8.4f

# while this will match d1.x,d1.y only
PRINT ARG=(d1\.[xy]) STRIDE=100 FILE=colvar FMT=%8.4f
```

You can include more than one regular expression by using comma separated regular expressions

```
t1: TORSION ATOMS=5,7,9,15
t2: TORSION ATOMS=7,9,15,17
d1: DISTANCE ATOMS=7,17 COMPONENTS
PRINT ARG=(d1\.[xy]),(t[0-9]) STRIDE=100 FILE=colvar FMT=%8.4f
```

(this selects t1,t2,d1.x and d2.x) Be aware that if you have overlapping selection they will be duplicated so it a better alternative is to use the "or" operator "|".

```
t1: TORSION ATOMS=5,7,9,15
t2: TORSION ATOMS=7,9,15,17
d1: DISTANCE ATOMS=7,17 COMPONENTS
PRINT ARG=(d1\.[xy]|t[0-9]) STRIDE=100 FILE=colvar FMT=%8.4f
```

this selects the same set of arguments as the previous example.

You can check the log to see whether or not your regular expression is picking the set of components you desire.

For more information on regular expressions visit  $http://www.regular-expressions.info/reference. \leftarrow html.$ 

#### 10.9.6 Files

We tried to design PLUMED in such a manner that input/output is done consistently irrespectively of the file type. Most of the files written or read by PLUMED thus follow the very same conventions discussed below.

```
10.9.6.1 Restart
```

Whenever the RESTART option is used, all the files written by PLUMED are appended. This makes it easy to analyze results of simulations performed as a chain of several sub-runs. Notice that most of the PLUMED textual files have a header. The header is repeated at every restart. Additionally, several files have time in the first column. PLUMED just takes the value of the physical time from the MD engine. As such, you could have that time starts again from zero upon restart or not.

An exception from this behavior is given by files which are not growing as the simulation proceeds. For example, grids written with METAD with GRID\_WFILE are overwritten by default during the simulation. As such, when restarting, there is no point in appending the file. Internally, PLUMED opens the file in append mode but then rewinds it every time a new grid is dumped.

10.9.6.2 Backup

Whenever the RESTART option is not used, PLUMED tries to write new files. If an old file is found in the way, P← LUMED takes a backup named "bck.X.filename" where X is a progressive number. Notice that by default PLUMED only allows a maximum of 100 backup copies for a file. This behavior can be changed by setting the environment variable PLUMED\_MAXBACKUP to the desired number of copies. E.g. export PLUMED\_MAXBACKUP=10 will fail after 10 copies. PLUMED\_MAXBACKUP=-1 will never fail - be careful since your disk might fill up quickly with this setting.

10.9.6.3 Replica suffix

When running with multiple replicas (e.g., with GROMACS, -multi option) PLUMED adds the replica index as a suffix to all the files. The following command will thus print files named COLVAR.0, COLVAR.1, etc for the different replicas.

```
d: DISTANCE ATOMS=1,2
PRINT ARG=d FILE=COLVAR
```

(see also DISTANCE and PRINT).

When reading a file, PLUMED will try to add the suffix. If the file is not found, it will fall back to the name without suffix. The most important case is the reading of the plumed input file. If you provide a file for each replica (e.g. plumed.0.dat, plumed.1.dat, etc) you will be able to setup plumed differently on each replica. On the other hand, using a single plumed.dat will make all the replicas read the same file.

Notice that when PLUMED adds the replica suffix, it recognizes the file extension and add the suffix *before* the extension. Before PLUMED 2.2, the only recognized suffix was ".gz". Since 2.2, any suffix with length less or equal to five letters is recognized.

This means that using in a multireplica context an input such as

```
d: DISTANCE ATOMS=1,2
PRINT ARG=d FILE=COLVAR.gz
METAD ARG=d FILE=test.HILLS SIGMA=0.1 HEIGHT=0.1
```

(see DISTANCE, PRINT, and METAD) PLUMED will write files named COLVAR.0.gz, COLVAR.1.gz, test.0.HILLS, test.1.HILLS, etc etc. This is useful since the preserved extension makes it easy to process the files later.

# **Chapter 11**

# **Performances**

In this page we collect hints on how to use the features available in PLUMED to speed up your calculations. Please note that PLUMED performs many different tasks, it can calculate a number of different collective variables, functions of collective variables, bias, on-the-fly analysis, etc in a way that is compatible with a number of different molecular dynamics codes. This means that there cannot be a single strategy to speed up all the possible calculations.

PLUMED makes use of MPI and OpenMP to parallelise some of its functions, try to always compile it with these features enabled. Furthermore, newer compilers with proper optimisation flags can provide a drammatic boost to performances.

PLUMED collects atoms from an external code and sends back forces, so it is key to minimise the effect of P← LUMED on highly parallel calculations to keep to the minimum the number of atoms used by PLUMED at every calculation step. The less is the number of atoms you need to send to PLUMED the less will be the overhead in the comunication between PLUMED and the code.

In the following you can find specific strategies for specific calculations, these could help in taking the most by using PLUMED for your simulations.

- · GROMACS and PLUMED with GPU
- Metadynamics
- · Multiple time stepping
- Multicolvar
- · Neighbour Lists
- OpenMP
- Secondary Structure
- Time your Input

460 Performances

## 11.1 GROMACS and PLUMED with GPU

Since version 4.6.x GROMACS can run in an hybrid mode making use of both your CPU and your GPU (either using CUDA or OpenCL for newer versions of GROMACS). The calculation of the short-range non-bonded interactions is performed on the GPU while long-range and bonded interactions are at the same time calculated on the CPU. By varing the cut-off for short-range interactions GROMACS can optimise the balance between GPU/CPU loading and obtain amazing performances.

GROMACS patched with PLUMED takes into account PLUMED in its load-balancing, adding the PLUMED timings to the one resulting from bonded interactions and long- range interactions. This means that the CPU/GPU balance will be optimised automatically to take into account PLUMED!

It is important to notice that the optimal setup to use GROMACS alone on the GPU or GROMACS + PLUMED can be different, try to change the number of MPI/OpenMP processes (OpenMP) used by GROMACS and PLUMED to find optimal performances. Remember that in GROMACS multiple MPI threads can use the same GPU:

i.e. if you have 4 cores and 2 GPU you can:

• use 2 MPI/2GPU/2OPENMP:

export PLUMED NUM THREADS=2

mpiexec -np 2 gmx\_mpi mdrun -nb gpu -ntomp 2 -pin on -gpu\_id 01

· use 4 MPI/2GPU:

export PLUMED\_NUM\_THREADS=1

mpiexec -np 4 gmx\_mpi mdrun -nb gpu -ntomp 1 -pin on -gpu\_id 0011

## 11.2 Metadynamics

Metadynamics can be sped up significantly using grids, which are activated setting the GRID\_MIN and GRID\_MAX keywords of METAD. This makes addition of a hill to the list a bit slower (since the Gaussian has to be evaluated for many grid points) but the evaluation of the potential very fast. Since the latter is usually done every few hundred steps, whereas the former typically ad every step, using grids will make the simulation much faster.

Notice that when restarting a simulation the history is read by default from a file and hills are added again to the grid. This allows one to change the grid boundaries upon restart. However, the first step after restart is usually very slow. Since PLUMED 2.3 you can also store the grid on a file and read it upon restart. This can be particularly useful if you perform many restarts and if your hills file has become very large.

For the precise syntax, see METAD

# 11.3 Multiple time stepping

By setting a STRIDE different from 1, you change how frequently an action is calculated. In the case of actions such as PRINT, this just means how frequently you dump some quantity on the disk. Notice that variables are only computed when necessary. Thus, if a variable is only appearing as the argument of a PRINT statement with STRIDE=10, it will be computed every 10 steps.

In a similar fashion, the STRIDE keyword can be used in a bias potential so as to apply the bias potential every few steps. In this case, forces from this bias potential are scaled up by a factor equal to STRIDE.

This technique can allow your simulation to run faster if you need the apply a bias potential on some very expensive collective variable. Consider the following input:

```
c1: COM ATOMS=1-1000
c2: COM ATOMS=1001-2000
d: DISTANCE ATOMS=c1, c2
METAD ARG=d HEIGHT=1 SIGMA=0.1 BIASFACTOR=5 PACE=500
```

This performs a METAD simulation biasing the distance between two centers of mass. Since computing these centers requires a lot of atoms to be imported from the MD engine, it could slow down significantly the simulation. Notice that whereas the bias is changed every PACE=500 steps, it is applied every STRIDE step, where STRIDE=1 by default. The following input could lead to a significantly faster simulation at the price of a negligible systematic error

```
c1: COM ATOMS=1-1000
c2: COM ATOMS=1001-2000
d: DISTANCE ATOMS=c1,c2
METAD ARG=d HEIGHT=1 SIGMA=0.1 BIASFACTOR=5 PACE=500 STRIDE=2
```

Similarly, the STRIDE keyword can be used with other biases (e.g. RESTRAINT).

The technique is discussed in details here ?. See also EFFECTIVE\_ENERGY\_DRIFT.

#### 11.3.1 EFFECTIVE\_ENERGY\_DRIFT

This is part of the generic module

Print the effective energy drift described in Ref?

Compulsory keywords

| STRIDE       | ( default=1 ) should be set to 1. Effective energy drift computation has to be active at each step. |  |
|--------------|---|--|
| FILE         | file on which to output the effective energy drift.   |  |
| PRINT_STRIDE | PRINT_STRIDE   frequency to which output the effective energy drift on FILE                         |  |

**Options** 

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| ENSEMBLE    | ( default=off ) Set to TRUE if you want to average over multiple replicas. |
|-------------|--|
| RESTART     | allows per-action setting of restart (YES/NO/AUTO)                         |
| UPDATE_FROM | Only update this action from this time                                     |
| UPDATE_UN←  | Only update this action until this time                                    |
| TIL         |  |

#### **Examples**

This is to monitor the effective energy drift for a metadynamics simulation on the Debye-Huckel energy. Since this variable is very expensive, it could be conveniently computed every second step.

```
dh: DHENERGY GROUPA=1-10 GROUPB=11-20 EPSILON=80.0 I=0.1 TEMP=300.0 METAD ARG=dh HEIGHT=0.5 SIGMA=0.1 PACE=500 STRIDE=2 EFFECTIVE_ENERGY_DRIFT PRINT_STRIDE=100 FILE=eff
```

This is to monitor if a restraint is too stiff

```
d: DISTANCE ATOMS=10,20
RESTRAINT ARG=d KAPPA=100000 AT=0.6
EFFECTIVE_ENERGY_DRIFT PRINT_STRIDE=100 FILE=eff
```

## 11.4 Multicolvar

Whenever you have a multicolvar action such as:

```
COORDINATIONNUMBER SPECIES=1-100 SWITCH={RATIONAL R_0=1. D_MAX=3.0} MORE_THAN={RATIONAL R_0=6.0 NN=6 MM=12 D_0
```

You will get a collosal speedup by specifying the D\_MAX keyword in all switching functions that act on distances. D\_MAX tells PLUMED that the switching function is strictly zero if the distance is greater than this value. As a result PLUMED knows that it does not need to calculate these zero terms in what are essentially sums with a very lage number of terms. In fact when D\_MAX is set PLUMED uses linked lists when calculating these coordination numbers, which is what gives you such a dramatic increase in performance.

# 11.5 Neighbour Lists

Collective variables that can be speed up making us of neighbour lists:

- COORDINATION
- DHENERGY
- PATHMSD

By tuning the cut-off for the neighbour list and the frequency for the recalculation of the list it is possible to balance between accuracy and performances.

Notice that for COORDINATION and DHENERGY using a neighbor list could imply that a smaller number of atoms are requested to the host MD engine. This is typically true when considering COORDINATION of a small number of atoms (e.g. a ligand) again many atoms (e.g. water). When the neighbor list is used, only the water atoms close to the ligand will be requested at each step.

#### Warning

Notice that the calculation of the neighbour list is not not parallelized for COORDINATION and DHENERGY. As a consequence, if you run with many processors and/or OpenMP threads, the neighbor list might even make the calculation slower.

11.6 OpenMP 463

## 11.6 OpenMP

PLUMED is partly parallelized using OpenMP. This should be enabled by default if your compiler supports it, and can be disabled with --disable-openmp.. At runtime, you should set the environment variable PLUMED\_N← UM\_THREADS to the number of threads you wish to use with PLUMED. By default (if PLUMED\_NUM\_THREADS is unset) openmp will be disabled at runtime. E.g., to run with gromacs you should do:

```
export PLUMED_NUM_THREADS=8
mdrun -plumed
```

#### Notice that:

- This option is likely to improve the performance, but could also slow down the code in some case.
- Results could be slightly different because of numerical roundoff and different order in summations. This should be harmless.
- The optimum number of threads is not necessary "all of them", nor should be equal to the number of threads used to parallelize MD.
- Only a few CVs are parallelized with opemMP (currently, COORDINATION and DHENERGY).
- You might want to tune also the environmental variable PLUMED\_CACHELINE\_SIZE, by default 512, to set
  the size of cachelines on your machine. This is used by PLUMED to decrease the number of threads to be
  used in each loop so as to avoid clashes in memory access. This variable is expected to affect performance
  only, not results.

# 11.7 Secondary Structure

Secondary Structure collective variables (ALPHARMSD, PARABETARMSD and ANTIBETARMSD) can be particularly demanding if you want to calculate them for all the residues of a protein. This is particularly true for the calculation of beta structures.

The FIRST thing to speed up PARABETARMSD and ANTIBETARMSD is to use the keyword STRANDS\_CUTOFF (i.e. STRANDS\_CUTOFF=1), in this way only a subset of possible fragments, the one less than 1. nm apart, are used in the calculation.

The metric used to calculate the distance from ideal secondary structure elements can also influence the performances, try to use TYPE=OPTIMAL or TYPE=OPTIMAL-FAST instead of TYPE=DRMSD.

At last, try to reduce the number of residues in the calculation.

# 11.8 Time your Input

Once you have prepared your plumed input file you can run a test simulation, or use driver, to see which collective variable, function, bias or analysis is consuming more time and can thus be the target for a different definition (use less atoms, change relevant parameters, or just use somenthing else)

To have an accurate timing of your input you can use the DEBUG DETAILED\_TIMERS.

Performances

# **Chapter 12**

# **Tutorials**

The following pages describe how to perform a variety of tasks using PLUMED

| Belfast tutorial: Analyzing CVs                            | This tutorial explains how to use plumed to analyze CVs  |
|--|--|
| D.K A.L  |  |
| Belfast tutorial: Adaptive variables I                     | How to use path CVs  |
| Belfast tutorial: Adaptive variables II                    | Dimensionality reduction and sketch maps   |
| Belfast tutorial: Umbrella sampling                        | Umbrella sampling, reweighting, and weighted histogram   |
| Belfast tutorial: Out of equilibrium dynamics              | How to run a steered MD simulations and how to estimate the free energy  |
| Belfast tutorial: Metadynamics                             | How to run a metadynamics simulation   |
| Belfast tutorial: Replica exchange I                       | Parallel tempering and Metadynamics, Well-Tempered Ensemble  |
| Belfast tutorial: Replica exchange II and Multiple walkers | Bias exchange and multiple walkers   |
| Belfast tutorial: NMR restraints                           | NMR restraints   |
| Belfast tutorial: Steinhardt Parameters                    | Steinhardt Parameters  |
| Cambridge tutorial   | A short 2 hours tutorial that introduces Well-Tempered Metadynamics, Bias-Exchange Metadynamics and Replica-Average Metadynamics |
| Cineca tutorial  | A short 2 hours tutorial that introduces analysis, well-tempered metadynamics, and multiple-restraints umbrella sampling.        |
| Using Hamiltonian replica exchange with GROMACS            | This tutorial explains how to use Hamiltonian replica exchange in GROMACS  |
| Julich tutorial: Developing CVs in plumed                  | Implementing new collective variables in plumed  |
| Lugano tutorial: Analyzing CVs                             | This tutorial explains how to use PLUMED to analyze CVs  |
| Lugano tutorial: Path CVs                                  | This tutorial explains how to use various kinds of path collective variables   |
| Moving from PLUMED 1 to PLUMED 2                           | This tutorial explains how plumed 1 input files can be translated into the new plumed 2 syntax.                                  |
| Munster tutorial   | A short 3 hours tutorial that introduces analysis, well-tempered metadynamics, and multiple-restraints umbrella sampling.        |

In addition, the following websites contain resources that might be helpful

| http://www.youtube.com/watch?v=iDv↔ ZmbWE5ps   | A short video introduction to the use of multicolvars in PLUMED 2     |
|--|---|
| http://www.youtube.com/watch?v=PxJ↔ P16qNCYs   | A short video introduction to the syntax of the PLUM← ED 2 input file |
| http://en.wikipedia.org/wiki/↔<br>Metadynamics | A wikipedia article on metadynamics                                   |

# 12.1 Belfast tutorial: Analyzing CVs

## 12.1.1 Aims

The aim of this tutorial is to introduce the users to the plumed syntax. We will go through the writing of simple collective variable and we will use them to analyse a trajectory in terms of probability distributions and free energy.

## 12.1.2 Learning Outcomes

Once this tutorial is completed students will:

- · Know how to write a simple plumed input file
- · Know how to analyse a trajectory using plumed

#### 12.1.3 Resources

The tarball for this project contains the following files:

- trajectory-short.xyz: a (short) trajectory for a 16 residue protein in xyz format. All calculations with plumed driver use this trajectory.
- template.pdb: a single frame from the trajectory that can be used in conjuction with the MOLINFO command

## 12.1.4 Instructions

PLUMED2 is a library that can be accessed by multiple codes adding a relatively simple and well documented interface. Once PLUMED is installed you can run a plumed executable that can be used for multiple purposes:

```
plumed --help
```

some of the listed options report about the plumed available functionalities, other can be used to tell plumed to do something: from analysing a trajectory to patch the source code of a MD code and so on. All the commands have further options that can be seen using plumed command –help, i.e.:

```
plumed driver --help
```

In the following we are going to see how to write an input file for plumed2 that can be used to analyse a trajectory.

#### 12.1.4.1 A note on units

By default the PLUMED inputs and outputs quantities in the following units:

- · Energy kJ/mol
- · Length nanometers
- · Time picoseconds

If you want to change these units you can do this using the UNITS keyword.

#### 12.1.4.2 Introduction to the PLUMED input file

A typical input file for PLUMED input is composed by specification of one or more CVs, the printout frequency and a termination line. Comments are denoted with a # and the termination of the input for PLUMED is marked with the keyword ENDPLUMED. Whatever it follows is ignored by PLUMED. You can introduce blank lines. They are not interpreted by PLUMED.

In the following input we will analyse the DISTANCE between the two terminal carbons of a 16 residues peptide, and we will PRINT the results in file named COLVAR.

```
#my first plumed input:
DISTANCE ATOMS=2,253 LABEL=e2edist

#printout frequency
PRINT ARG=e2edist STRIDE=1 FILE=COLVAR

#endofinput
ENDPLUMED
here I can write what I want it won't be read.
```

Now we can use this simple input file to analyse the trajectory included in the RESOURCES:

```
plumed driver --plumed plumed.dat --ixyz trajectory-short.xyz --length-units 0.1
```

NOTE: –length-units 0.1, xyz files, as well as pdb files, are in Angstrom.

You should have a file COLVAR, if you look at it (i.e. more COLVAR) the first two lines should be:

```
#! FIELDS time e2edist 0.000000 2.5613161
```

NOTE: the first line of the file COLVAR tells you what is the content of each column.

In PLUMED2 the commands defined in the input files are executed in the same order in which they are written, this means that the following input file is wrong:

```
#printout frequency
PRINT ARG=e2edist STRIDE=1 FILE=COLVAR
#my first plumed input:
DISTANCE ATOMS=2,253 LABEL=e2edist
#endofinput
ENDPLUMED
here I can write what I want it won't be read.
```

Try to run it.

Sometimes, when calculating a collective variable, you may not want to use the positions of a number of atoms directly. Instead you may wish to use the position of a virtual atom whose position is generated based on the positions of a collection of other atoms. For example you might want to use the center of a group of atoms (CEN TER):

Since PLUMED executes the input in order you need to define the new Virtual Atom before using it:

```
first: CENTER ATOMS=1,2,3,4,5,6
last: CENTER ATOMS=251-256

e2edist: DISTANCE ATOMS=2,253
comdist: DISTANCE ATOMS=first,last

PRINT ARG=e2edist,comdist STRIDE=1 FILE=COLVAR
ENDPLUMED
```

NOTE: an action (i.e. CENTER or DISTANCE here) can be either label using LABEL as we did before or as label: ACTION as we have just done here.

With the above input this is what happen inside PLUMED with a STRIDE=1:

- 1. calculates the position of the Virtual Atom 'first' as the CENTER of atoms from 1 to 6;
- 2. calculates the position of the Virtual Atom 'last' as the CENTER of atoms from 251 to 256;
- 3. calculates the distance between atoms 2 and 253 and saves it in 'e2edist';
- 4. calculates the distance between the two atoms 'first' and 'last' and saves it in 'comdist';
- 5. print the content of 'e2edist' and 'comdist' in the file COLVAR

In the above input we have used to different ways of writing the atoms used in CENTER calculation:

- 1. ATOMS=1,2,3,4,5,6 is the explicit list of the atoms we need
- 2. ATOMS=251-256 is the range of atoms needed

ranges of atoms can be defined with a stride which can also be negative:

```
    ATOMS=from,to:by (i.e.: 251-256:2)
    ATOMS=to,from:-by (i.e.: 256-251:-2)
```

Now by plotting the content of the COLVAR file we can compare the behaviour in this trajectory of both the terminal carbons as well as of the centre of masses of the terminal residues.

```
gnuplot
```

What do you expect to see now by looking at the trajectory? Let's have a look at it

```
vmd template.pdb trajectory-short.xyz
```

Virtual atoms can be used in place of standard atoms everywhere an atom can be given as input, they can also be used together with standard atoms. So for example we can analyse the TORSION angle for a set of Virtual and Standard atoms:

```
first: CENTER ATOMS=1-6
last: CENTER ATOMS=251-256
cvtor: TORSION ATOMS=first,102,138,last
PRINT ARG=cvtor STRIDE=1 FILE=COLVAR
ENDPLUMED
```

The above CV don't look smart to learn something about the system we are looking at. In principle CV are used to reduce the complexity of a system by looking at a small number of properties that could be enough to rationalise its behaviour.

Now try to write a collective variable that measures the Radius of Gyration of the system: GYRATION.

NOTE: if what you need for one or more variables is a long list of atoms and not a virtual atom one can use the keyword GROUP. A GROUP can be defined using ATOMS in the same way we saw before, in addition it is also possible to define a GROUP by reading a GROMACS index file.

```
ca: GROUP ATOMS=9,16,31,55,69,90,102,114,124,138,160,174,194,208,224,238
```

Now 'ca' is not a virtual atom but a simple list of atoms.

#### 12.1.4.3 MULTICOLVAR

Sometimes it can be useful to calculate properties of many similar collective variables at the same time, for example one can be interested in calculating the properties of the distances between a group of atoms, or properties linked to the distribution of the dihedral angles of a chain and so on. In PLUMED2 this kind of collective variables fall under the name of MULTICOLVAR (cf. MultiColvar.) Here we are going to analyse the distances between CA carbons along the chain:

```
ca: GROUP ATOMS=9,16,31,55,69,90,102,114,124,138,160,174,194,208,224,238
dd: DISTANCES GROUP=ca MEAN MIN={BETA=50} MAX={BETA=0.02} MOMENTS=2

PRINT ARG=dd.mean,dd.min,dd.max,dd.moment-2 STRIDE=1 FILE=COLVAR
ENDPLUMED
```

The above input tells PLUMED to calculate all the distances between CA carbons and then look for the mean distance, the minimum distance, the maximum distance and the variance. In this way we have defined four collective variables that are calculated using the distances. These four collective variables are stored as components of the defined action 'dd': dd.mean, dd.min, dd.max, dd.moment-2.

The infrastracture of multicolvar has been used to develop many PLUMED2 collective variables as for example the set of Secondary Structure CVs (ANTIBETARMSD, PARABETARMSD and ALPHARMSD).

```
MOLINFO STRUCTURE=template.pdb
abeta: ANTIBETARMSD RESIDUES=all TYPE=DRMSD LESS_THAN={RATIONAL R_0=0.08 NN=8 MM=12} STRANDS_CUTOFF=1
PRINT ARG=abeta.lessthan STRIDE=1 FILE=COLVAR
ENDPLUMED
```

We have now seen how to write the input some of the many CVs available in PLUMED. More complex CVs will be discussed in the next workshop, Belfast tutorial: Adaptive variables I.

#### 12.1.4.4 Analysis of Collective Variables

Collective variables are usually used to visualize the Free Energy of a system. Given a system evolving at fixed temperature, fixed number of particles and fixed volume, it will explore different conformations with a probability

$$P(q) \propto e^{-\frac{U(q)}{kb_BT}}$$

where q are the microscopic coordinates and  $k_B$  is the Boltzmann constant.

It is possible to analyse the above probability as a function of one or more collective variable s(q):

$$P(s) \propto \int dq e^{-\frac{U(q)}{kb_BT}} \delta(s - s(q))$$

where the  $\delta$  function means that to for a given value s of the collective variable are counted only those conformations for which the CV is s. The probability can be recast to a free energy by taking its logarithm:

$$F(s) = -k_B T \log P(s)$$

This means that by estimating the probability distribution of a CV it is possible to know the free energy of a system along that CV. Estimating the probability distribution of the conformations of a system is what is called 'sampling'.

In order to estimate a probability distribution one needs to make HISTOGRAM from the calculated CVs. PLUMED2 includes the possibility of histogramming data both on the fly as well as a posteriori as we are going to do now.

```
MOLINFO STRUCTURE=template.pdb
abeta: ANTIBETARMSD RESIDUES=all TYPE=DRMSD LESS_THAN={RATIONAL R_0=0.08 NN=8 MM=12} STRANDS_CUTOFF=1
ca: GROUP ATOMS=9,16,31,55,69,90,102,114,124,138,160,174,194,208,224,238
DISTANCES ...
GROUP=ca MEAN MIN={BETA=50} MAX={BETA=0.02} MOMENTS=2 LABEL=dd
... DISTANCES
PRINT ARG-abeta.lessthan,dd.mean,dd.min,dd.max,dd.moment-2 STRIDE=1 FILE=COLVAR
HISTOGRAM ...
ARG=abeta.lessthan,dd.mean
LABEL=hh
KERNEL=DISCRETE
GRID MIN=0,0.8
GRID\_MAX=4,1.2
GRID_BIN=40,40
... HISTOGRAM
DUMPGRID GRID=hh FILE=histo
ENDPLUMED
```

NOTE: HISTOGRAM ... means that what follow is part of the HISTOGRAM function, the same can be done for any action in PLUMED.

The above input tells PLUMED to accumulate the two collective variables on a GRID. In addition the probability can be converted to a free-energy using the CONVERT\_TO\_FES method and then use DUMPGRID to write it. Histograms can be accumulated in a smoother way by using a KERNEL function, a kernel is a normalised function, for example a normalised gaussian is the default kernel in PLUMED, that is added to the histogram centered in the position of the data. Estimating a probability density using kernels can in principle give more accurate results, on the other hand in addition to the choice of the binning one has to choose a parameter that is the WIDTH of the kernel function. As a rule of thumb: the grid spacing should be smaller (i.e. one half or less) than the BANDWIDTH and the BANDWIDTH should be smaller (i.e. one order of magnitude) than the variance observed/expected for the variable.

```
HISTOGRAM ...

LABEL=hh

ARG=abeta.lessthan,dd.mean

GRID_MIN=0,0.8

GRID_MAX=4,1.2

GRID_SPACING=0.04,0.004

BANDWIDTH=0.08,0.008
... HISTOGRAM

DUMPGRID GRID=hh FILE=histo

ENDPLUMED
```

If you have time less at the end of the session read the manual and look for alternative collective variables to analyse the trajectory. Furthemore try to play with the HISTOGRAM parameters to see the effect of using KERNEL in analysing data.

# 12.2 Belfast tutorial: Adaptive variables I

#### 12.2.1 Aim

In this section we want to introduce the concept of adaptive collective variables. These are special variables that are knowledge-based in that are built from a pre-existing notion of the mechanism of the transition under study

#### 12.2.2 Resources

Here is the tarball with the files referenced in the following.

#### 12.2.3 What happens when in a complex reaction?

When you deal with a complex conformational transition that you want to analyze (or bias), very often you cannot just describe it with a single order parameter.

As an example in Figure belfast-2-cdk-fig I consider a large conformational transition like those involved in activating the kinase via open-close transition of the activation loop. In sticks you see the part involved in the large conformational change, the rest is either keeping the structure and just moving a bit or is a badly resolved region in the X-ray structure. This is a complex transition and it is hard to tell which is the order parameter that best describes the transition.

One could identify a distance that can distinguish open from close but

- the plasicity of the loop is such that the same distance can correspond to an almost closed loop and almost open loop. One would like to completely divide these two situations with something which is discriminating what intuitively one would think as open and closed
- the transition state is an important point where one would like to see a certain crucial interaction forming/breaking so to better explain what is really happening. If you capture then hypothetically you would be able to say what is dictating the rate of this conformational transition. A generic distance is a very hybrid measure that is unlikely to capture a salt-bridge formation and a concerted change of many dihedral change or desolvation contribution which are happening while the transition is happening. All these things are potentially important in such transition but none of them is explaining the whole thing.

So basically in these cases you have to deal with an intrinsic multidimensional collective variable where you would need many dimensions. How would you visualize a 10 dimensional CV where you use many distances, coordinations and dihedrals (ouch, they're periodic too!) ?

Another typical case is the docking of a small molecule in a protein cleft or gorge, which is the mechanism of drug action. This involves specific conformational transition from both the small molecule and the protein as the small molecule approaches the protein cavity. This also might imply a specific desolvation pattern.

Other typical examples are chemical reactions. Nucleophiloic attacks typically happen with a role from the solvent (see some nice paper from Nobel-prize winner Arieh Warshel) and sizeable geometric distortions of the neighboring groups.

#### 12.2.4 Path collective variables

One possibility to describe many different thing that happen in a single reaction is to use a dimensional reduction technique and in plumed the simplest example that may show its usefulness can be considered that of the path collective variables.

In a nutshell, your reaction might be very complex and happening in many degree of freedom but intuitively is a sort of track along which the reaction proceeds. So what we need is a coordinate that, given a conformation, just tells which point along the "reactive track" is closest.

For example, in Fig. belfast-2-ab-fig, you see a typical chemical reaction (hydrolisys of methylphosphate) with the two end-points denoted by A and B. If you are given a third point, just by looking at it, you might find that this is more resemblant to the reactant than the product, so, hypothetically, if you would intuitively give a parameter that would be 1 for a configuration in the A state and 2 for a configuration in the B state, you probably would give it something like 1.3, right?

Path collective variables are the extension to this concept in the case you have many conformation that describe your path, and therefore, instead of an index that goes from 1 to 2 you have an index that goes from 1 to N, where N is the number of conformation that you use in input to describe your path.

From a mathematical point of view, that's rather simple. The progress along the path is calculated with the following equation:

$$S(X) = \frac{\sum_{i=1}^{N} i \exp^{-\lambda|X - X_i|}}{\sum_{i=1}^{N} \exp^{-\lambda|X - X_i|}}$$

where in belfast-2-s-eq the  $|X-X_i|$  represents a distance between one configuration X which is analyzed and another from the set that compose the path  $X_i$ . The parameter  $\lambda$  is a positive value that is tuned in a way explaned later. here are a number of things to note to make you think that this is exactly what you want.

- The negative exponential function is something that is 1 whenever the value at the exponent is zero, and is progressively smaller when the value is larger than zero (trivially, the case with the value at the exponent larger than zero never occurs since lambda is a positive quantity and the distance is by definition positive).
- Whenever you sit exactly on a specific images  $X_j$  then all the other terms in the sum disappear (if  $\lambda$  is large enough) and only the value j survives returning exactely S(X)=j.

In order to provide a value which is continuous, the parameter  $\lambda$  should be correctly tuned. As a rule of thumb I use the following formula

$$\lambda = \frac{2.3(N-1)}{\sum_{i=1}^{N-1} |X_i - X_{i+1}|}$$

which imply that one should calculate the average distance between consecutive frames composing the path. Note also that this distance should be more or less similar between the frames. Generally I tolerate fluctuation of the order of 10/15 percent tops. If you have larger, then it is better to have a smaller value of  $\lambda$ .

It is important to note that in principle one could even have a specific  $\lambda$  value associated to each frame of the path but this would provide some distortion in the diffucion coefficient which could potentially harm a straightforward interpretation of the free energy landscape.

So, at this point is better to understand what is meant with "distance" since a distance between two conformations can be calculated in very many ways. The way we refer here is by using mean square deviation after optimal alignment. This means that at each step in which the analisys is performed, a number N of optimal alignments is performed. Namely what is calculated is  $|X-X_i|=d(X,X_i)^2$  where  $d(X,X_i)$  is the RMSD as defined in what you see here RMSD.

Using the MSD instead of RMSD is sometimes more convenient and more stable (you do not have a denominator that gies to zero in the derivatives when biasing.

Anyway this is a matter of choice. Potentially one could equally employ other metrics like a set of coordinations (this was done in the past), and then you would avoid the problem of rototranslations (well, which is not a problem since you have it already in plumed) but for some applications that might become appealing. So in path collective variables (and in all the dimensional reduction based collective variables) the problem is converted from the side of choosing the collective variable in choosing the right way to calculate distances, also called "metrics".

The discussion of this issue is well beyond the topic of this tutorial, so we can move forward in how to tell plumed to calculate the progress along the path whenever the MSD after optimal alignment is used as distance.

```
p1: PATHMSD REFERENCE=all.pdb LAMBDA=50.0
PRINT ARG=p1.sss,p1.zzz STRIDE=100 FILE=colvar FMT=%8.4f
```

Note that reference contains a set of PDB, appended one after the other, with a END field. Note that there is no need to place all the atoms of the system in the PDB reference file you provide. Just put the atoms that you think might be needed. You can leave out big domains, solvent and ions if you think that is not important for your use.

Additionally, note that the measure units of LAMBDA are in the units of the code. In gromacs they are in nm<sup>2</sup> while NAMD is Ang<sup>2</sup>. PATHMSD produces two arguments that can be printed or used in other ActionWithArguments. One is the progress along the path of belfast-2-s-eq, the other is the distance from the closest point along the path, which is denoted with the zzz component. This is defined as

$$Z(X) = -\frac{1}{\lambda} \log(\sum_{i=1}^{N} \exp^{-\lambda|X - X_i|})$$

It is easy to understand that in case of perfect match of  $X=X_i$  this equation gives back the value of  $|X-X_i|$  provided that the lambda is adjusted correctly.

So, the two variables, put together can be visualized as This variable is important because whenever your simulation is running close to the path (low Z values), then you know that you are reproducing reliably the path you provided in input but if by chance you find some other path that goes, say, from S=1, Z=0 to S=N, Z=0 via large Z values, then it might well be that you have just discovered a good alternative pathway. If your path indeed is going from S=1, Z=large to S=N, Z=large then it might well be that you do not have your reaction accomplished, since your reaction, by definition should go from the reactant which is located at S=1, Z=0 to the product, which is located at S=1, Z=N so you should pay attention. This case is exemplified in Fig. belfast-2-ab-sz-nowhere-fig

## 12.2.5 A note on the path topology

A truly important point is that if you get a trajectory from some form of accelerated dynamics (e.g. simply by heating) this cannot simply be converted into a path. Since it is likely that your trajectory is going stochastically back and forth (not in the case of SMD or US, discussed later), your trajectory might be not topologically suitable. To understand that, suppose you simply collect a reactive trajectory of 100 ps into the reference path you give to the PATHMSD and simply you assign the frame of 1 ps to index 1 (first frame occurring in the reference file provided to PATHM← SD), the frame of 2 ps to index 2 and so on: it might be that you have two points which are really similar but one is associated to step, say 5 and the other is associated with frame 12. When you analyse the same trajectory, when you are sitting on any of those points then the calculation of S will be an average like S(X) = (5+12)/2 = 8.5which is an average of the two indexes and is completely misleading sinec it let you think that you are moving between point 8 and 9, which is not the case. So this evidences that your reference frames should be "topologically consecutive". This means that frame 1 should be the closest to frame 2 and all the other frames should be farther apart. Similarly frame 2 should be equally close (in an RMSD sense) to 1 and 3 while all the others should be farther apart. Same for frame 3: this should be closest to frame 2 and 4 and farther apart from all the others and so on. This is equivalent to calculate an "RMSD matrix" which can be conveniently done in vmd (this is a good exercise for a number of reasons) with RMSD Trajectory tools, by choosing different reference system along the set of reference frames.

This is shown in Fig. belfast-2-good-matrix-fig where the matrix has a typical gullwing shape.

On the contrary, whenever you extract the frames from a pdb that you produced via free MD or some biased methods (SMD or Targeted MD for example) then your frame-to-frame distance is rather inhomogeneous and looks something like

Aside from the general shape, which is important to keep the conformation-to-index relation (this, as we will see in the next part is crucial in the multidimensional scaling) the crucial thing is the distance between neighbors.

As a matter of fact, this is not much important in the analysis but is truly crucial in the bias. When biasing a simulation, you generally want to introduce a force that push your system somewhere. In particular, when you add a bias which is based on a path collective variable, most likely you want that your system goes back and forth along your path. The bias is generally applied by an additional term in the hamiltonian, this can be a spring term for Umbrella Sampling, a Gaussian function for Metadynamics or whatever term which is a function of the collective variable s. Therefore the Hamiltonian H(X) where X is the point of in the configurational phase space where your system is takes the following form

$$H'(X) = H(X) + U(S(X))$$

where U(S(X)) is the force term which depends on the collective variable that ultimately is a function of the X. Now, when you use biased dynamics you need to evolve according the forces that this term produces (this only holds for MD, while not in MC) and therefore you need

$$F_{i} = -\frac{dH'(X)}{dx_{i}} = -\frac{dH'(X)}{dx_{i}} - \frac{\partial U(S(X))}{\partial S} \frac{\partial S(X)}{\partial x_{i}}$$

This underlines the fact that, whenever  $\frac{\partial S(X)}{\partial x_i}$  is zero, then you have no force on the system. Now the derivative of the progress along the path is

$$\frac{\partial S(X)}{\partial x_i} = \frac{\sum_{i=1}^N -\lambda \ i \ \frac{\partial |X - X_i|}{\partial x_i} \exp^{-\lambda |X - X_i|}}{\sum_{i=1}^N \exp^{-\lambda |X - X_i|}} - \frac{\left(\sum_{i=1}^N i \ \exp^{-\lambda |X - X_i|}\right) \left(\sum_{j=1}^N -\lambda \frac{\partial |X - X_j|}{\partial x_i} \exp^{-\lambda |X - X_j|}\right)}{\left(\sum_{i=1}^N \exp^{-\lambda |X - X_i|}\right)^2} = \frac{\sum_{i=1}^N -\lambda \ i \ \frac{\partial |X - X_i|}{\partial x_i}}{\sum_{i=1}^N \exp^{-\lambda |X - X_i|}}$$

which can be rewritten as

$$\frac{\partial S(X)}{\partial x_i} = \lambda \frac{\sum_{i=1}^{N} \frac{\partial |X - X_i|}{\partial x_i} \exp^{-\lambda |X - X_i|} [s(X) - i]}{\sum_{i=1}^{N} \exp^{-\lambda |X - X_i|}}$$

It is interesting to note that whenever the  $\lambda$  is too small the force will vanish. Additionally, when  $\lambda$  is too large, then it one single exponential term will dominate over the other on a large part of phase space while the other will vanish. This means that the S(X) will assume almost discrete values that produce zero force. Funny, isn't it?

## 12.2.6 How many frames do I need?

A very common question that comes is the following: "I have my reaction or a model of it. how many frames do I need to properly define a path collective variable?" This is a very important point that requires a bit of thinking. It all depends on the limiting scale in your reaction. For example, if in your process you have a torsion, as the smallest event that you want to capture with path collective variable, then it is important that you mimick that torsion in the path and that this does not contain simply the initial and final point but also some intermediate. Similarly, if you have a concerted bond breaking, it might be that all takes place in the range of an Angstrom or so. In this case you should have intermediate frames that cover the sub-Angstrom scale. If you have both in the same path, then the smallest dominates and you have to mimick also the torsion with sub-Angstrom accuracy.

## 12.2.7 Some tricks of the trade: the neighbors list.

If it happens that you have a very complex and detailed path to use, say that it contains 100 frames with 200 atoms each, then the calculation of a 100 alignment is required every time you need the CV. This can be quite expensive but you can use a trick. If your trajectory is continuous and you are sure that your trajectory does not show jumps where your system suddedly move from the reactant to the product, then you can use a so-called neighbor list. The plumed input shown before then becomes

```
p1: PATHMSD REFERENCE=all.pdb LAMBDA=50.0 NEIGH_STRIDE=100 NEIGH_SIZE=10 PRINT ARG=p1.sss,p1.zzz STRIDE=100 FILE=colvar FMT=%8.4f
```

and in this case only the closest 10 frames from the path will be used for the CV. Then the list of the frames to use is updated every 100 steps. If you are using a biased dynamics this may introduce sudden change in the derivatives, therefore it is better to check the stability of the setup before running production-quality calculations.

## 12.2.8 The molecule of the day: alanine dipeptide

Here and probably in other parts of the tutorial a simple molecule is used as a test case. This is alanine dipeptide in vacuum. This rather simple molecule is useful to make many benchmark that are around for data analysis and free energy methods. It is a rather nice example since it presents two states separated by a high (free) energy barrier.

In Fig. belfast-2-ala-fig its structure is shown.

The two main metastable states are called  $C_7eq$  and  $C_7ax$ .

Here metastable states are intended as states which have a relatively low free energy compared to adjacent conformation. At this stage it is not really useful to know what is the free energy, just think in term of internal energy. This is almost the same for such a small system whith so few degrees of freedom.

It is conventional use to show the two states in terms of Ramachandran dihedral angles, which are denoted with  $\Phi$  and  $\Psi$  in Fig. belfast-2-transition-fig .

## 12.2.9 Examples

Now as a simple example, I want to show you that plotting some free dynamics trajectories shoot from the saddle point, you get a different plot in the path collective variables if you use the right path or if you use the wrong path.

In Fig. belfast-2-good-bad-path-fig I show you two example of possible path that join the  $C_7eq$  and  $C_7ax$  metastable states in alanine dipeptide. You might clearly expect that real (rare) trajectories that move from one basin to the other would rather move along the black line than on the red line.

So, in this example we do a sort of "commmittor analysis" where we start shooting a number of free molecular dynamics from the saddle point located at  $\Phi=0$  and  $\Psi=-1$  and we want to see which way do they go. Intuitively, by assigning random velocities every time we should find part of the trajectories that move woward  $C_7 eq$  and part that move towards  $C_7 ax$ .

I provided you with two directories, each containing a bash script script.sh whose core (it is a bit more complicated in practice...) consists in:

```
#
# set how many runs you want to do
#
ntests=50
for i in 'seq 1 $ntests'
do

#
# assign a random velocity at each timestep by initializing the
# sed s/SEED/$RANDOM/ md.mdp >newmd.mdp
#
# do the topology: this should write a topol.tpr
#
$GROMPP -c start.gro -p topol.top -f newmd.mdp
$GROMACS_BIN/$MDRUN -plumed plumed.dat
mv colvar colvar_$i
```

This runs 50 short MD runs (few hundreds steps) and just saves the colvar file into a labeled colvar file. In each mdrun plumed is used to plot the collective variables and it is something that reads like the follwing:

```
# Phi
t1: TORSION ATOMS=5,7,9,15
# Psi
t2: TORSION ATOMS=7,9,15,17
# The right path
p1: PATHMSD REFERENCE=right_path.dat LAMBDA=15100.
# The wrong path
p2: PATHMSD REFERENCE=wrong_path.dat LAMBDA=8244.4
# Just a printout of all the stuff calculated so far
PRINT ARG=* STRIDE=2 FILE=colvar FMT=%12.8f
```

where I just want to plot  $\Phi$ ,  $\Psi$  and the two path collective variables. Note that each path has a different LAMBDA parameters. Here the Ramachandran angles are plotted so you can realize which path is the system walking in a more confortable projection. This is of course fine in such a small system but whenever you have to deal with larger systems and control hundreds of CVs at the same time, I think that path collective variables produce a more intuitive description for what you want to do.

If you run the script simply with

```
pd@plumed:~> ./script.sh
```

then after a minute or so, you should have a directory which is full of colvar files. Let's revise together how the colvar file is formatted:

```
#! FIELDS time t1 t2 p1.sss p1.zzz p2.sss p2.zzz

#! SET min_t1 -pi

#! SET max_t1 pi

#! SET max_t2 pi

#! SET max_t2 pi

0.000000 -0.17752998 -1.01329788 13.87216908 0.00005492 12.00532256 0.00233905

0.004000 -0.13370142 -1.10611136 13.87613508 0.00004823 12.03390658 0.00255806

0.008000 -0.15633049 -1.14298481 13.88290617 0.00004511 12.07203319 0.00273764

0.012000 -0.23856451 -1.12343958 13.89969608 0.00004267 12.12872544 0.00284883
```

In first column you have the time, then t1 (  $\Phi$ ) , then t2 (  $\Psi$  ) and the path collective variables p1 and p2. Note that the action PATHMSD calculates both the progress along the path (p1.sss) and the distance from it (p1.zzz) . In PLUMED jargon, these are called "components". So a single Action (a line in plumed input) can calculate many components at the same time. This is not always the case: sometimes by default you have one component but specific flags may enable more components to be calculated (see <code>DISTANCE</code> for example). Note that the header (all the part of a colvar file that contains # as first character) is telling already what it inside the file and eventually also tells you if a variable is contained in boundaries (for example torsions, are periodic and their codomain is defined in -Pi and Pi).

At the end of the script, you also have two additional scripts. One is named script\_rama.gplt and the other is named script\_path.gplt. They contain some gnuplot commands that are very handy to visualize all the colvar files without making you load one by one, that would be a pain.

Now, let's visualize the result from the wrong path directory. In order to do so, after having run the calculation, then do

```
pd@plumed:~>gnuplot
gnuplot> load "script_rama.gplt"
```

what you see is that all the trajectories join the reactant and the product state along the low free energy path depicted before.

Now if you try to load the same bunch of trajectories as a function of the progress along the path and the distance from the path in the case of the wrong path then simply do

```
gnuplot> load "script_path_wrong.gplt"
```

What do you see? A number of trajectories move from the middle towards the right bottom side at low distance from the path. In the middle of the progress along the path, you have higher distance. This is expected since the distance zero corresponds to a unlikely, highly-energetic path which is unlikely to occur. Differently, if you now do

```
gnuplot> load "script_path_right.gplt"
```

You see that the path, compared to what happened before, run much closer to small distance from the path. This means that the provided path is highlt resemblant and representative of what happens in the reactive path.

Note that going at high distances can be also beneficial. It might help you to explore alternative paths that you have not explored before. But beware, the more you get far from the path, the more states are accessible, in a similar way as the fact that the surface of a sphere increase with its radius. The surface ramps up much faster than the radius therefore you have a lots of states there. This means also high entropy, so many systems actually tend to drift to high distances while, on the contrary, zero distance is never reached in practice (zero entropy system is impossible to reach at finite temperature). So you can see by yourself that this can be a big can of worms. In particular, my experience with path collective variables and biological systems tells me that most of time is hopeless to go to high distances to find new path in many cases (for example, in folding). While this is worth whenever you think that the paths are not too many (alternative routes in chemical reaction or enzymatic catalysis).

## 12.2.10 How to format my input?

Very often it is asked how to format a set of pdb to be suitably used with path collective variables. Here are some tricks.

- When you dump the files with vmd or (for gromacs users, using trjcat), the pdb you obtain is reindexed from 1. This is also the case when you select a subensemble of atoms of the path (e.g. the heavy atoms only or the backbone atoms). This is rather unfortunate and you have to fix is someway. My preference is to dump the whole pdb but water (when I do not need it) and use some awk script to select the atoms I am interested in.
- Pay attention to the last two column. These are occupancy and beta. With the first (occupancy) you set the atoms which are used to perform the alignment. The atoms which have zero occupancy will not be used in the alignment. The second column is beta and controls which atoms are used for the calculation of the distance after having performed the alignment on the set of atoms which have nonzero occupancy column. In this way you can align all your system by using a part of the system and calculate the distance respect to another set. This is handy in case of protein-ligand. You set the alignment of the protein and you calculate the distance based on the ligand and the part of the protein which is in contact with the protein. This is done for example in this article.
- Plumed-GUI (version > 2.0) provides the *Structure->Build reference structure...* function to generate inputs that conform to the above rules from within VMD.
- Note that all the atoms contained in the REFERENCE must be the same. You cannot have a variable number
  of atoms in each pdb contained in the reference.
- The reference is composed as a set of concatenated PDBs that are interrupted by a TER/END/ENDMDL card. Both HETATM and ATOM cards denote the atoms of the set.
- Include in the reference frames only the needed atoms. For example, if you have a methyl group involved in a conformational transition, it might be that you do not want to include the hydrogen atoms of the methyl since these rotate fast and probably they do not play ant relevant role.

## 12.2.11 Fast forward: metadynamics on the path

This section is actually set a bit foward but I included here for completeness now. It is recommended to be read after you have an introduction on Metadynamics and to well-tempered Metadynamics in particular. Here I want to show a couple of concept together.

- Path collective variables can be used for exploring alternative routes. It is effective in highly structure molecules, while it is tricky on complex molecules whenever you have many competing routes
- Path collective variables suffer from problems at the endpoints (as the higly popular coordinates COORDIN

  ATION for example) that can be cured with flexible hills and an appropriate reweighting procedure within the well-tempered Metadynamics scheme.

Let's go to the last problem. All comes from the derivative belfast-2-sder-eq. Whenever you have a point of phase space which is similar to one of the endpoint than one of the points in the center then you get a s(X) which is 1 or N (where N is the number of frames composing the path collective variable). In this case that exponential will dominate the others and you are left with a constant (since the derivative of RMSD is a constant since it is linear in space). This means that, no matter what happens here, you have small force. Additionally you have small motion in the CV space. You can move a lot in configuration space but if the closest point is one of the endpoint, your CV value will always be one of the endpoint itself. So, if you use a fixed width of your CV which you retrieve from a middle point in your path, this is not suitable at all at the endpoints where your CV flucutates much less. On the contrary if you pick the hills width by making a free dynamics on the end states you might pick some sigmas that are smaller than what you might use in the middle of the path. This might give a rough free energy profile and definitely

more time to converge. A possible solution is to use the adaptive gaussian width scheme. In this scheme you adapt the hills to their fluctuation in time. You find more details in ? Additionally you also adopt a non spherical shape taking into account variable correlation. So in this scheme you do not have to fix one sigma per variable sigma, but just the time in which you calculate this correlation (another possibility is to calculate it from the compression of phase space but will not be covered here). The input of metadynamics might become something like this

```
t1: TORSION ATOMS=5,7,9,15
t2: TORSION ATOMS=7,9,15,17
p1: PATHMSD REFERENCE=right_path.dat LAMBDA=15100.
p2: PATHMSD REFERENCE=wrong_path.dat LAMBDA=8244.4
#
# do a metadynamics on the right path, use adaptive hills whose decay time is 125 steps (250 fs)
# and rather standard WT parameters
# meta: METAD ARG=p1.sss,p1.zzz ADAPTIVE=DIFF SIGMA=125 HEIGHT=2.4 TEMP=300 BIASFACTOR=12 PACE=125
PRINT ARG=* STRIDE=10 FILE=colvar FMT=%12.8f
```

You can find this example in the directory BIASED\_DYNAMICS. After you run for a while it is interesting to have a feeling for the change in shape of the hills. That you can do with

```
pd@plumed:~> gnuplot
gnuplot> p "<head -400 HILLS" u 2:3:4:5 w xyer</pre>
```

that plots the hills in the progress along the path and the distance from the path and add an error bar which reflects the diagonal width of the flexible hills for the first 400 hills (Hey note the funny trick in gnuplot in which you can manipulate the data like in a bash script directly in gnuplot. That's very handy!).

There are a number of things to observe: first that the path explores high distance since the metadynamics is working also in the distance from the path thus accessing the paths that were not explored before, namely the one that goes from the upper left corner of the ramachandran plot and the one that passes through the lower left corner. So in this way one can also explore other paths. Additionally you can see that the hills are changing size rather considerably. This helps the system to travel faster since at each time you use something that has a nonzero gradient and your forces act on your system in an effective way. Another point is that you can see broad hills covering places which you have not visited in practice. For example you see that hills extend so wide to cover point that have negative progress along the path, which is impossible by using the present definition of the progress along the path. This introduced a problem in calculating the free energy. You actually have to correct for the point that you visited in reality.

You can actually use sum\_hills to this purpose in a two-step procedure. First you calculate the negative bias on a given range:

```
pd@plumed:~> plumed sum_hills --hills HILLS --negbias --outfile negative_bias.dat --bin 100,100 --min -5,-0.0
```

and then calculate the correction. You can use the same hills file for that purpose. The initial transient time should not matter if your simulation is long enough to see many recrossing and, secondly, you should check that the hills heigh in the welltempered are small compared to the beginning.

```
pd@plumed:~> plumed sum_hills --histo HILLS --bin 100,100 --min -5,-0.005 --max 25,0.05 --kt 2.5 --sigma 0.5,0
```

Note that in the correction you should assign a sigma, that is a "trust radius" in which you think that whenever you have a point somewhere, there in the neighborhood you assign a bin (it is done with Gaussian in reality, but this does not matter much). This is the important point that compenstates for the issues you might encounter putting excessive large hills in places that you have not visited. It is nice to have a look to the correction and compare with the hills in the same range.

```
gnuplot> set pm3d
gnuplot> spl "correction.dat" u 1:2:3 w 1
gnuplot> set contour
gnuplot> set cntrp lev incremental -20,4.,1000.
gnuplot> set view map
gnuplot> unset clabel
gnuplot> replot
```

You might notice that there are no contour in the unrealistic range, this means that the free energy correction is impossible to calculate since it is too high (see Fig. belfast-2-metadpath-correction-fig).

Now the last thing that one has to do to have the most plausible free energy landscape is to sum both the correction and the negative bias produced. This can be easily done in gnuplot as follows:

```
gnuplot> set pm3d
gnuplot> spl "<paste negative_bias.dat correction.dat " u 1:2:($3+$8) w pm3d
gnuplot> set view map
gnuplot> unset key
gnuplot> set xr [-2:23]
gnuplot> set contour
gnuplot> unset clabel
gnuplot> set cbrange [-140:-30]
gnuplot> set cntrp lev incr -140,6,-30
```

So now we can comment a bit on the free energy surface obtained and note that there is a free energy path that connects the two endpoints and runs very close to zero distance from the path. This means that our input path is actually resemblant of what is really happening in the system. Additionally you can see that there are many comparable routes different from the straight path. Can you make a sense of it just by looking at the free energy on the Ramachandran plot?

## 12.3 Belfast tutorial: Adaptive variables II

## 12.3.1 Aims

The aim of this tutorial is to consolidate the material that was covered during Belfast tutorial: Analyzing CVs and Belfast tutorial: Adaptive variables I on analysing trajectories using collective variables and path collective variables. We will then build on this material by showing how you can use the multidimensional scaling algorithm to automate the process of finding collective variables.

## 12.3.2 Learning Outcomes

Once this tutorial is completed students will:

- Know how to load colvar data into the GISMO plugin
- · Know how to run the multidimensional scaling algorithms on a trajectory
- Be able to explain how we can automate the process of finding collective variables by seeking out an isometry between a high-dimensional and low-dimensional space

## 12.3.3 Resources

The tarball for this project contains the following files:

- trajectory-short.xyz : a (short) trajectory for a 16 residue protein in xyz format. All calculations with plumed driver use this trajectory.
- trajectory-short.pdb: the same trajectory in pdb format, this can be loaded with VMD
- template.pdb: a single frame from the trajectory that can be used in conjuction with the MOLINFO command

#### 12.3.4 Instructions

#### 12.3.4.1 Visualising the trajectory

The aim of this tutorial is to understand the data contained in the trajectory called trajectory-short.pdb. This file contains some frames from a simulation of a 16 residue protein. As a start point then lets load this trajectory with vmd and have a look at it. Type the following command into the command line:

```
vmd trajectory-short.pdb
```

Look at it with the various representations that vmd offers. If you add the instructions below to your .vmdrc file you can make the new cartoon representation update automatically for each frame of the trajectory by pressing the m key - cool huh!

```
proc structure_trace {name index op} {
          vmd_calculate_structure $index
}

user add key m {
    puts "Automatic update of secondary structure, and alignment to first frame"
    trace variable vmd_frame w structure_trace
    rmsdtt
    rmsdtt::doAlign
    destroy $::rmsdtt::w
    clear_reps top
    mol color Structure
    mol selection backbone
    mol representation NewCartoon
    mol addrep top
}
```

What are your impressions about this trajectory based on looking at it with VMD? How many basins in the free energy landscape is this trajectory sampling from? What can we tell from looking at this trajectory that we could perhaps put in a paper?

If your answers to the questions at the end of the above paragraph are I don't know that is good. We can tell very little by just looking at a trajectory. In fact the whole point of the tutorials I referenced at the start of this one was to find ways of analyzing trajectories precisely so that we are not put in this position of staring at trajectories mystified!

## 12.3.4.2 Installing GISMO

You can download and install the GISMO plugin by following the instructions on the page below:

```
http://epfl-cosmo.github.io/sketchmap/index.html?page=code
```

(you don't need to compile the sketch-map code) Once it is installed you should have an option to open it when you open vmd. The option to open GISMO can be found under Extensions>Analysis>GISMO.

## 12.3.4.3 Finding collective variables

Right so lets come up with some CVs to analyse this trajectory with. As some of you may know we can understand the conformation of proteins by looking at the Ramachandran angles. For those of you who don't know here is a Wikkepedia article:

```
http://en.wikipedia.org/wiki/Ramachandran_plot
```

Our protein has 32 ramachandran angles. We'll come back to that. For the time being pick out a couple that you think might be useful and construct a plumed input to calculate them and print them to a file. You will need to use the TORSION and PRINT commands in order to do this. Once you have created your plumed input use driver to calculate the torsional angles using the following command:

```
plumed driver --plumed plumed.dat --ixyz trajectory-short.xyz
```

If you have done this correctly you should have an output file containing your torsional angles. We can use vmd+← GISMO to visualise the relationship between the ramachandran angles and the atomic configurations. To do this first load the trajectory in VMD:

```
vmd trajectory-short.pdb
```

Then click on Extensions>Analysis>GISMO. A new window should open in this window click on File>Load colvars. You will be asked to select a colvar file. Select the file that was output by the plumed calculation above. Once the file is loaded you should be able to select the labels that you gave to the Ramachandran angles you calculated with plumed. If you do so you will see that this data is plotted in the GISMO window so that you can interact with it and the trajectory.

What can you conclude from this exercise. Do the CV values of the various frames appear in clusters in the plane? Do points in different clusters correspond to structures that look the same or different? Are there similar looking structures clustered together or are they always far apart? What can we conclude about the various basins in the free energy landscape that have been explored in this trajectory? How many are there? Would your estimate be the same if you tried the above estimate with a different pair of ramachandran angles?

## 12.3.4.4 Dimensionality reduction

What we have done in most of the other exercises here is seek out a function that takes as input the position of all the atoms in the system - a 3N dimensional vector, where N is the number of atoms. This function then outputs a single number - the value of the collective variable - that tells us where in a low dimensional space we should project that configuration. Problems can arise because this collective-variable function is many-to-one. As you have hopefully seen in the previous exercise markedly different configurations of the protein can actually have quite similar values of a particular ramachandran angle.

We are going to spend the rest of this session introducing an alternative approach to this bussiness of finding collective variables. In this alternative approach we are going to stop trying to seek out a function that can take any configuration of the atoms (any 3N-dimensional vector) and find its low dimensional projection on the collective variable axis. Instead we are going to take a set of configurations of the atoms (a set of 3N-dimensional vectors of atom positions) and try to find a sensible set of projections for these configurations. We already touched on this idea earlier when we looked at paths. Our assumption, when we introduced this idea, was that we could find an ordered set of high-dimensional configurations that represented the transtion pathway the system takes as it crossed a barrier and changed between two particularly interesting configurations. Lets say we have a path defined by four reference configurations - this implies that to travel between the configurations at the start and the end of this path you have to pass through configuration 1, then configuration 2, then configuration 3 and then configuration 4. This ordering means that the numbers 1 through 4 constitute sensible projections of these high-dimensional configurations. The numbers 1 through 4 all lie on a single cartesian axis - a low-dimensional space.

The problem when it comes to applying this idea to the data that we have in the trajectory-short trajectory is that we have no information on the "order" of these points. We have not been told that this trajectory represents the transition between two interesting points in phase space and thus we cannot apply the logic of paths. Hence, to seek out a low dimensional representation we are going to try and find a representation of this data we are going to seek out an <code>isometry</code> between the space containing the 3N-dimensional vectors of atom positions and some lower-dimensional space. This idea is explained in more detail in the following <code>video</code>.

Let's now generate our isometric embedding. You will need to create a plumed input file that contains the following instructions:

```
CLASSICAL_MDS ...
ATOMS=1-256
METRIC=OPTIMAL-FAST
NLOW_DIM=2
OUTPUT_FILE=rmsd-embed
... CLASSICAL_MDS
```

You should then run this calculation using the following command:

```
plumed driver --ixyz trajectory-short.xyz --plumed plumed.dat
```

This should generate an output file called rmsd-embed. You should now be able to use VMD+GISMO to visualise this output. Do the CV values of the various frames appear in clusters in the plane? Do points in different clusters correspond to structures that look the same or different? Are there similar looking structures clustered together or are they always far apart? What can we conclude about the various basins in the free energy landscape that have been explored in this trajectory? How many are there? Do you think this gives you a fuller picture of the trajectory than the ones you obtained by considering ramachandran angles?

#### 12.3.5 Extensions

As discussed in the previous section this approach to trajectory analysis works by calcalating distances between pairs of atomic configurations. Projections corresponding to these configurations are then generated in the low dimensional space in a way that tries to preserve these pairwise distances. There are, however, an infinite number of ways of calculating the distance between two high-dimensional configurations. In the previous section we used the RMSD distance but you could equally use the DRMSD distance. You could even try calculating a large number of collective variables for each of the high-dimensional points and seeing how much these all changed. You can use these different types of distances with the CLASSICAL\_MDS action that was introduced in the previous section. If you have time less at the end of the session read the manual for the CLASSICAL\_MDS action and see if you can calculate an MDS projection using an alternative defintion of the distances between configurations. Some suggestions to try in order of increasing difficulty: DRMSD, how much the full set of 32 ramachandran angles change and the change in the contact map

## 12.3.6 Further Reading

There is a growing community of people using these ideas to analyse trajectory data. Some start points for investigating their work in more detail are:

- http://epfl-cosmo.github.io/sketchmap/index.html?page=main
- http://www.annualreviews.org/doi/abs/10.1146/annurev-physchem-040412-110006

# 12.4 Belfast tutorial: Umbrella sampling

#### 12.4.1 Aims

In the previous lectures we learned how to compute collective variables (CVs) from atomic positions. We will now learn how one can add a bias potential to enforce the exploration of a particular region of the space. We will also see how it is possible to bias CVs so as to enhance the sampling of events hindered by large free-energy barriers and how to analyze this kind of simulation. This technique is known as "umbrella sampling" and can be used in combination with the weighted-histogram analysis method to compute free-energy landscapes. In this tutorial we will use simple collective variables, but the very same approach can be used with any kind of collective variable.

## 12.4.2 Summary of theory

#### 12.4.2.1 Biased sampling

A system at temperature T samples conformations from the canonical ensemble:

$$P(q) \propto e^{-\frac{U(q)}{k_B T}}$$

. Here q are the microscopic coordinates and  $k_B$  is the Boltzmann constant. Since q is a highly dimensional vector, it is often convenient to analyze it in terms of a few collective variables (see Belfast tutorial: Analyzing CVs , Belfast tutorial: Adaptive variables I , and Belfast tutorial: Adaptive variables II ). The probability distribution for a CV s is

$$P(s) \propto \int dq e^{-\frac{U(q)}{k_B T}} \delta(s - s(q))$$

This probability can be expressed in energy units as a free energy landscape F(s):

$$F(s) = -k_B T \log P(s)$$

Now we would like to modify the potential by adding a term that depends on the CV only. That is, instead of using U(q), we use U(q)+V(s(q)). There are several reasons why one would like to introduce this potential. One is to avoid that the system samples some un-desired portion of the conformational space. As an example, imagine that you want to study dissociation of a complex of two molecules. If you perform a very long simulation you will be able to see association and dissociation. However, the typical time required for association will depend on the size of the simulation box. It could be thus convenient to limit the exploration to conformations where the distance between the two molecules is lower than a given threshold. This could be done by adding a bias potential on the distance between the two molecules. Another example is the simulation of a portion of a large molecule taken out from its initial context. The fragment alone could be unstable, and one might want to add additional potentials to keep the fragment in place. This could be done by adding a bias potential on some measure of the distance from the experimental structure (e.g. on root-mean-square deviation).

Whatever CV we decide to bias, it is very important to recognize which is the effect of this bias and, if necessary, remove it a posteriori. The biased distribution of the CV will be

$$P'(s) \propto \int dq e^{-\frac{U(q)+V(s(q))}{k_B T}} \delta(s-s(q)) \propto e^{-\frac{V(s(q))}{k_B T}} P(s)$$

and the biased free energy landscape

$$F'(s) = -k_B T \log P'(s) = F(s) + V(s) + C$$

Thus, the effect of a bias potential on the free energy is additive. Also notice the presence of an undetermined constant C. This constant is irrelevant for what concerns free-energy differences and barriers, but will be important

later when we will learn the weighted-histogram method. Obviously the last equation can be inverted so as to obtain the original, unbiased free-energy landscape from the biased one just subtracting the bias potential

$$F(s) = F'(s) - V(s) + C$$

Additionally, one might be interested in recovering the distribution of an arbitrary observable. E.g., one could add a bias on the distance between two molecules and be willing to compute the unbiased distribution of some torsional angle. In this case there is no straightforward relationship that can be used, and one has to go back to the relationship between the microscopic probabilities:

$$P(q) \propto P'(q)e^{\frac{V(s(q))}{k_BT}}$$

The consequence of this expression is that one can obtained any kind of unbiased information from a biased simulation just by weighting every sampled conformation with a weight

$$w \propto e^{\frac{V(s(q))}{k_B T}}$$

That is, frames that have been explored in spite of a high (disfavoring) bias potential V will be counted more than frames that has been explored with a less disfavoring bias potential.

#### 12.4.2.2 Umbrella sampling

Often in interesting cases the free-energy landscape has several local minima. If these minima have free-energy differences that are on the order of a few times  $k_BT$  they might all be relevant. However, if they are separated by a high saddle point in the free-energy landscape (i.e. a low probability region) than the transition between one and the other will take a lot of time and these minima will correspond to metastable states. The transition between one minimum and the other could require a time scale which is out of reach for molecular dynamics. In these situations, one could take inspiration from catalysis and try to favor in a controlled manner the conformations corresponding to the transition state.

Imagine that you know since the beginning the shape of the free-energy landscape F(s) as a function of one CV s. If you perform a molecular dynamics simulation using a bias potential which is exactly equal to -F(s), the biased free-energy landscape will be flat and barrierless. This potential acts as an "umbrella" that helps you to safely cross the transition state in spite of its high free energy.

It is however difficult to have an a priori guess of the free-energy landscape. We will see later how adaptive techniques such as metadynamics (Belfast tutorial: Metadynamics) can be used to this aim. Because of this reason, umbrella sampling is often used in a slightly different manner.

Imagine that you do not know the exact height of the free-energy barrier but you have an idea of where the barrier is located. You could try to just favor the sampling of the transition state by adding a harmonic restraint on the CV, e.g. in the form

$$V(s) = \frac{k}{2}(s - s_0)^2$$

. The sampled distribution will be

$$P'(q) \propto P(q)e^{\frac{-k(s(q)-s_0)^2}{2k_BT}}$$

For large values of k, only points close to  $s_0$  will be explored. It is thus clear how one can force the system to explore only a predefined region of the space adding such a restraint. By combining simulations performed with different values of  $s_0$ , one could obtain a continuous set of simulations going from one minimum to the other crossing the transition state. In the next section we will see how to combine the information from these simulations.

#### 12.4.2.3 Weighted histogram analysis method

Let's now consider multiple simulations performed with restraints located in different positions. In particular, we will consider the i-th bias potential as  $V_i$ . The probability to observe a given value of the collective variable s is:

$$P_{i}(s) = \frac{P(s)e^{-\frac{V_{i}(s)}{k_{B}T}}}{\int ds' P(s')e^{-\frac{V_{i}(s')}{k_{B}T}}} = \frac{P(s)e^{-\frac{V_{i}(s)}{k_{B}T}}}{Z_{i}}$$

where

$$Z_i = \sum_{q} e^{-(U(q) + V_i(q))}$$

The likelyhood for the observation of a sequence of snapshots  $q_i(t)$  (where i is the index of the trajectory and t is time) is just the product of the probability of each of the snapshots. We use here the minus-logarithm of the likelihood (so that the product is converted to a sum) that can be written as

$$\mathcal{L} = -\sum_{i} \int dt \log P_i(s_i(t)) = \sum_{i} \int dt \left( -\log P(s_i(t)) + \frac{V_i(s_i(t))}{k_B T} + \log Z_i \right)$$

One can then maximize the likelyhood by setting  $\frac{\delta \mathcal{L}}{\delta P(\mathbf{s})} = 0$ . After some boring algebra the following expression can be obtained

$$0 = \sum_{i} \int dt \left( -\frac{\delta_{\mathbf{s}_{i}(t),\mathbf{s}}}{P(\mathbf{s})} + \frac{e^{-\frac{V_{i}(\mathbf{s})}{k_{B}T}}}{Z_{i}} \right)$$

In this equation we aim at finding P(s). However, also the list of normalization factors  $Z_i$  is unknown, and they should be found selfconsistently. Thus one can find the solution as

$$P(\mathbf{s}) \propto \frac{N(\mathbf{s})}{\sum_{i} \int dt \frac{e^{-\frac{V_{i}(\mathbf{s})}{k_{B}T}}}{Z_{i}}}$$

where Z is selfconsistently determined as

$$Z_i \propto \int ds' P(\mathbf{s'}) e^{-\frac{V_i(\mathbf{s'})}{k_B T}}$$

These are the WHAM equations that are traditionally solved to derive the unbiased probability P(s) by the combination of multiple restrained simulations. To make a slightly more general implementation, one can compute the weights that should be assigned to each snapshot, that turn out to be:

$$w_i(t) \propto \frac{1}{\sum_j \int dt \frac{e^{-\beta V_j(\mathbf{s}_i(t))}}{Z_j}}$$

The normalization factors can in turn be found from the weights as

$$Z_i \propto \frac{\sum_j \int dt e^{-\beta V_i(\mathbf{s}_j(t))} w_j(t)}{\sum_j \int dt w_j(t)}$$

This allows to straighforwardly compute averages related to other, non-biased degrees of freedom, and it is thus a bit more flexible. It is sufficient to precompute this factors w and use them to weight every single frame in the trajectory.

## 12.4.3 Learning Outcomes

Once this tutorial is completed students will know how to:

- · Setup simulations with restraints.
- · Use multiple-restraint umbrella sampling simulations to enhance the transition across a free-energy barrier.
- · Analyze the results and compute weighted averages and free-energy profiles.

## 12.4.4 Resources

The tarball for this project contains the following files:

- A gromacs topology (topol.top), configuration (conf.gro), and control file (grompp.mdp). They should not be needed.
- A gromacs binary file (topol.tpr). This is enough for running this system.
- A small C++ program that computes WHAM (wham.cpp) and a script that can be used to feed it (wham.sh)

By working in the directory where the topol.tpr file is stored, one can launch gromacs with the command

```
gmx_mpi mdrun -plumed plumed.dat -nsteps 100000
```

(notice that the -nsteps flag allows the number of steps to be changed).

#### 12.4.5 Instructions

#### 12.4.5.1 The model system

We here use a a model system alanine dipeptide with CHARM27 all atom force field already seen in the previous section.

#### 12.4.5.2 Restrained simulations

The simplest way in which one might influence a CV is by forcing the system to stay close to a chosen value during the simulation. This is achieved with a restraining potential that PLUMED provides via the directive RESTRAINT. In the umbrella sampling method a bias potential is added so as to favor the exploration of some regions of the conformational space and to disfavor the exploration of other regions? . A properly chosen bias potential could allow for example to favor the transition state sampling thus enhancing the transition state for a conformational transition. However, choosing such a potential is not trivial. In a later section we will see how metadynamics can be used to this aim. The simplest way to use umbrella sampling is that to apply harmonic constraints to one or more CVs.

We will now see how to enforce the exploration of a the neighborhood of a selected point the CV space using a RESTRAINT potential.

```
# set up two variables for Phi and Psi dihedral angles
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
#
# Impose an umbrella potential on CV 1 and CV 2
# with a spring constant of 500 kjoule/mol
# at fixed points on the Ramachandran plot
#
restraint-phi: RESTRAINT ARG=phi KAPPA=500 AT=-0.3
restraint-psi: RESTRAINT ARG=psi KAPPA=500 AT=+0.3
# monitor the two variables and the bias potential from the two restraints
PRINT STRIDE=10 ARG=phi,psi,restraint-phi.bias,restraint-psi.bias FILE=COLVAR
```

(see TORSION, RESTRAINT, and PRINT).

The syntax for the command RESTRAINT is rather trivial. The directive is followed by a keyword ARG followed by the label of the CV on which the umbrella potential has to act. The keyword KAPPA determines the hardness of the spring constant and its units are [Energy units]/[Units of the CV]. The additional potential introduced by the UMBRELLA takes the form of a simple Hooke's law:

$$U(s) = \frac{k}{2}(x - x_0)^2$$

.

where  $x_0$  is the value specified following the AT keyword. The choice of AT ( $x_0$ ) is obviously depending on the specific case. KAPPA (k) is typically chosen not to affect too much the intrinsic fluctuations of the system. A typical recipe is  $k \approx \frac{k_B T}{\sigma^2}$ , where  $\sigma^2$  is the variance of the CV in a free simulation). In real applications, one must be careful with values of k larger than  $\frac{k_B T}{\sigma^2}$  because they could break down the molecular dynamics integrator.

The CVs as well as the two bias potentials are shown in the COLVAR file. For this specific input the COLVAR file has in first column the time, in the second the value of  $\phi$ , in the third the value of  $\psi$ , in the fourth the the additional potential introduced by the restraint on  $\phi$  and in the fifth the additional potential introduced by the restraint on  $\psi$ .

It may happen that one wants that a given CV just stays within a given range of values. This is achieved in plumed through the directives UPPER\_WALLS and LOWER\_WALLS that act on specific collective variables and limit the exploration within given ranges.

#### 12.4.5.3 Reweighting the results

Now consider a simulation performed restraining the variable  $\phi$ :

```
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
restraint-phi: RESTRAINT ARG=phi KAPPA=10.0 AT=-2
PRINT STRIDE=10 ARG=phi,psi,restraint-phi.bias FILE=COLVAR10
```

and compare the result with the one from a single simulation with no restraint

```
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
# we use a "dummy" restraint with strength zero here
restraint-phi: RESTRAINT ARG=phi KAPPA=0.0 AT=-2
PRINT STRIDE=10 ARG=phi,psi,restraint-phi.bias FILE=COLVARO
```

Plot the time dependence of  $\phi$  in the two cases and try to understand the difference.

Now let's try to compute the probability that  $\psi$  falls within a given range, say between 1 and 2. This can be done e.g. with this shell script

```
> grep -v \# COLVAR0 | tail -n 80000 |
awk '{if($3>1 && $3<2)a++; else b++;}END{print a/(a+b)}'</pre>
```

Notice that we here considered only the last 80000 frames in the average. Look at the time series for  $\psi$  and guess why. Also notice that the script is removing the initial comments. After this trivial preprocessing, the script is just counting how many times the third column ( $\psi$ ) lies between 1 and 2 and how many times it doesn't. At the end it prints the number of times the variable is between 1 and 2 divided by the total count. The result should be something around 0.40. Now try to do it on trajectories generated with different values of AT. Does the result depend on AT?

We can now try to reweight the result so as to get rid of the bias introduced by the restraint. Since the reweighting factor is just  $\exp(\frac{V}{k_BT})$  the script should be modified as

```
> grep -v \# COLVAR10 | tail -n 80000 | awk '\{w=\exp(\$4/2.5); if(\$3>1 \&\& \$3<2)a+=w; else b+=w;\}END\{print a/(a+b)\}'
```

Notice that 2.5 is just  $k_BT$  in kj/mol units.

Repeat this calculation for different values of AT. Does the result depend on AT?

## 12.4.5.4 A free-energy landscape

One can also count the probability of an angle to be in a precise bin. The logarithm of this quantity, in kbT units, is the free-energy associated to that bin. There are several ways to compute histograms, either with PLUMED or with external programs. Here I decided to use awk.

```
grep -v \# COLVAR10 | tail -n 80000 |
awk 'BEGIN{
 min1=-3.14159265358979
  max1=+3.14159265358979
 min2=-3.14159265358979
  max2=+3.14159265358979
  nh1=100:
  nb2=100:
  for(i1=0;i1<nb1;i1++) for(i2=0;i2<nb2;i2++) f[i1,i2]=0.0;
  i1=int(($2-min1)*nb1/(max1-min1));
  i2=int((\$3-min2)*nb2/(max2-min2));
# we assume the potential is in the last column, and kbT=2.5 kj/mol
  w = \exp(\$NF/2.5);
  f[i1, i2] += w;
END {
  for(i1=0;i1<nb1;i1++){
  for (i2=0; i2<nb2; i2++) print min1+i1/100.0* (max1-min1), min2+i2/100.0* (max2-min2), -2.5*log(f[i1,i2]);
  print "";
}}' > plotme
```

You can then plot the "plotme" file with

```
gnuplot> set pm3d map
gnuplot> splot "plotme"
```

## 12.4.5.5 Combining multiple restraints

In the last paragraph you have seen how to reweight simulations done with restraints in different positions to obtain virtually the same result. Let's now see how to combine data from multiple restraint simulations. A possible choice is to download and use the WHAM software here, which is well documented. This is probably the best idea for analyzing a real simulation.

For the sake of learning a bit, we will use a different approach here, namely we will use a short C++ program that implements the weight calculation. Notice that whereas people typically use harmonic restraints in this framework, PLUMED offers a very large variety of bias potentials. For this reason we will keep things as general as possible and use an approach that can be in principle used also to combine simulation with restraint on different variables or with complicated bias potential.

The first step is to generate several simulations with different positions of the restraint, gradually going from say -2 to +2. You can obtain them using e.g. the following script:

```
for AT in -2.0 -1.5 -1.0 -0.5 +0.0 +0.5 +1.0 +1.5 +2.0
do

cat >plumed.dat << EOF
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
#
# Impose an umbrella potential on CV 1 and CV 2
# with a spring constant of 500 kjoule/mol
# at fixed points on the Ramachandran plot
#
restraint-phi: RESTRAINT ARG=phi KAPPA=40.0 AT=$AT
# monitor the two variables and the bias potential from the two restraints
PRINT STRIDE=10 ARG=phi,psi,restraint-phi.bias FILE=COLVAR$AT
EOF

gmx_mpi mdrun -plumed plumed.dat -nsteps 100000 -x traj$AT.xtc
done</pre>
```

Notice that we are here saving separate trajectories for the separate simulation, as well as separate colvar files. In each simulation the restraint is located in a different position. Have a look at the plot of (phi,psi) for the different simulations to understand what is happening.

An often misunderstood fact about WHAM is that data of the different trajectories can be mixed and it is not necessary to keep track of which restraint was used to produce every single frame. Let's get the concatenated trajectory

```
gmx_mpi trjcat -cat -f traj*.xtc -o alltraj.xtc
```

Now we should compute the value of each of the bias potentials on the entire (concatenated) trajectory

```
for AT in -2.0 -1.5 -1.0 -0.5 +0.0 +0.5 +1.0 +1.5 +2.0
do

cat >plumed.dat << EOF
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
restraint-phi: RESTRAINT ARG=phi KAPPA=40.0 AT=$AT

# monitor the two variables and the bias potential from the two restraints
PRINT STRIDE=10 ARG=phi,psi,restraint-phi.bias FILE=ALLCOLVAR$AT
EOF
plumed driver --mf_xtc alltraj.xtc --trajectory-stride=10 --plumed plumed.dat
done</pre>
```

It is very important that this script is consistent with the one used to generate the multiple simulations above. Now, single files named ALLCOLVARXX will contain on the fourth column the value of the bias centered in XX computed on the entire concatenated trajectory.

Next step is to compile the C++ program that computes weights self-consistently solving the WHAM equations. This is named wham.cpp and can be compiled with

```
g++ -03 wham.cpp -o wham.x
```

and can be then used through a wrapper script wham.sh as

```
./wham.sh ALLCOLVAR* > colvar
```

The resulting colvar file will contain 3 columns: time, phi, and psi, plus the weights obtained from WHAM written in logarithmic scale. That is, the file will contain  $k_BT \log w$ .

Try now to use this file to compute the unbiased free-energy landscape as a function of phi and psi. You can use the script that you used earlier to compute histogram.

## 12.4.6 Comments

## 12.4.6.1 How does PLUMED work

The fact that when you add a force on the collective variable PLUMED can force the atoms to do something depends on the fact that the collective variables implemented in PLUMED has analytical derivatives. By biasing the value of a single CV one turns to affect the time evolution of the system itself. Notice that some of the collective variables could be implemented without derivatives (either because the developers were lazy or because the CVs cannot be derived). In this case you might want to have a look at the NUMERICAL\_DERIVATIVES option.

## 12.4.7 Further Reading

Umbrella sampling method is a widely used technique. You can find several resources on the web, e.g.:

• http://en.wikipedia.org/wiki/Umbrella\_sampling

# 12.5 Belfast tutorial: Out of equilibrium dynamics

In plumed you can bring a system in a specific state in a collective variable by means of the MOVINGRESTRAINT directive. This directive is very flexible and allows for a programmed series of draggings and can be used also to sample multiple events within a single simulation. Here I will explain the concepts of it and show some examples

## 12.5.1 Resources

Here is the tarball with the files referenced in the following .

#### 12.5.2 Steered MD

Steered MD (SMD) is often used to drag the system from an initial configuration to a final one by pulling one or more CVs. Most of time the aim of such simulations is to prepare the system in a particular state or produce nice snapshots for a cool movie. All the CVs present in PLUMED can be used in SMD.

In SMD the Hamiltonian of the system H is modified into  $H_{\lambda}$ . This new Hamiltonian contains now another new term which now depends on time only via a Harmonic potential centered on a point which moves linear with time

$$\begin{array}{lcl} H_{\lambda}(X,t) & = & H(X) + U_{\lambda}(X,t) \\ & = & H(X) + \frac{k(t)}{2}(s(X) - \lambda(t))^2 \\ & = & H(X) + \frac{k(t)}{2}(s(X) - s_0 - vt)^2. \end{array}$$

This means that if the k is tight enough the system will follow closely the center of the moving harmonic spring. But be careful, if the spring constant is too hard your equations of motion will now keep up since they are tuned to the fastest motion in your system so if you artificially introduce a higher frequency in your system you'll screw up the dynamics. The same is true for the pulling speed v. As a matter of fact I never encountered the case where I had to lower the time step and I could all the time be happy just by making a softer spring constant or a slower steering speed. Generally, integrators of equations of motion like velocity-Verlet are very tolerant. Note that one can also make the spring constant depend on time and this, as we will see later in the examples is particularly useful to prepare your state.

In simulations, it is more convenient to adopt a situation where you specify only the starting point, the final point of cvs and the time in which you want to cover the transition. That's why the plumed input is done in such a way.

For example, let's go back to the alanine dipeptide example encountered in The molecule of the day: alanine dipeptide. Let's say that now we want to steer from  $C_7eq$  to  $C_7ax$ . If you think, just by dragging along the  $\Phi$  dihedral angle from a value of -1 to a value 1 should be enough to the state of interest. Additionally, it might be important to you not to stress the system too much, so you might want first to increase the k first so to lock the system in  $\Phi=-1$ , then move it gently to  $\Phi=1$  and then release again your spring constant so to end up to an equilibrated and unconstrained state. This you can program in PLUMED like this

Please note the syntax of MOVINGRESTRAINT: You need one (or more) argument(s) and a set of steps denote by ATX, STEPX, KAPPAX where X is a incremental starting from 0 that assign the center and the harness of the spring at step STEPX. What happens in between is a linear interpolation of the AT and KAPPA parameters. If those are identical in two consecutive steps then nothing is happening to that parameter. So if you put the same KAPPA and AT in two different STEPs then this will give you an umbrella potential placed in the same point between the two time intervals defined by STEP. Note that you need to run a bit more than 6000 steps because after this your system has no more restraints so the actual thermalization period starts here.

The COLVAR file produced has the following shape

```
#! FIELDS time phi psi restraint.bias restraint.force2 restraint.phi_cntr restraint.phi_work
#! SET min_phi -pi
#! SET max_phi pi
#! SET max_psi -pi
#! SET max_psi pi
0.000000 -1.409958 1.246193 0.000000 0.000000 -1.000000 0.000000
0.020000 -1.432352 1.256545 0.467321 4.673211 -1.000000 0.441499
0.040000 -1.438652 1.278405 0.962080 19.241592 -1.000000 0.918101
0.060000 -1.388132 1.283709 1.129846 33.895372 -1.000000 1.344595
0.080000 -1.360254 1.275045 1.297832 51.913277 -1.000000 1.691475
```

So we have time, phi, psi and the bias from the moving restraint. Note that at step 0 is zero since we imposed this to start from zero and ramp up in the first 2000 steps up to a value of 2000 kJ/mol/rad^2. It increases immediately since already at step 1 the harmonic potential is going to be increased in bits towards the value of 1000 which is set by KAPPA. The value of restraint.force2 is the squared force (which is a proxy of the force magnitude, despite the direction) on the CV.

$$-\frac{\partial H_{\lambda}(X,t)}{\partial s} = -(s(X) - s_0 - vt)$$

Note that the actual force on an atom of the system involved in a CV is instead

$$\begin{array}{rcl} -\frac{\partial H_{\lambda}(X,t)}{\partial x_{i}} & = & -\frac{\partial H_{\lambda}(X,t)}{\partial s}\frac{\partial s}{\partial x_{i}} \\ \\ & = & -(s(X)-s_{0}-vt)\frac{\partial s}{\partial x_{i}} \end{array}$$

This is important because in CVs that have a derivative that change significantly with space then you might have regions in which no force is exerted while in others you might have an enormous force on it. Typically this is the case of sigmoids that are used in coordination numbers in which, in the tails, they are basically flat as a function of

particle positions. Additionally note that this happens on any force-based enhanced-sampling algorithm so keep it in mind. Very often people miss this aspect and complain either that a CV or a enhanced-sampling method does not work. This is another good reason to use tight spring force so to compensate in the force the lack of derivative from the CV.

The other argument in colvar is restraint.phi\_cntr which is the center of the harmonic potential. This is a useful quantity so you may know how close the system is follwing the center of harmonic potential (more on this below). The last parameter is restraint.phi\_work. The work is defined as

$$W = \int_0^{t_s} dt \, \frac{\partial H_{\lambda}(t)}{\partial t}$$

so this is changing only when the Hamiltonian is changing with time. There are two time dependent contributions in this integral: one can come from the fact that k(t) changes with time and another from the fact that the center of the spring potential is changing with time.

$$W = \int_{0}^{t_{s}} dt \, \frac{\partial H_{\lambda}(t)}{\partial t}$$

$$= \int_{0}^{t_{s}} dt \, \frac{\partial H_{\lambda}(t)}{\partial \lambda} \frac{\partial \lambda(t)}{\partial t} + \int_{0}^{t_{s}} dt \, \frac{\partial H_{\lambda}(t)}{\partial k} \frac{\partial k}{\partial t}$$

$$= \int_{0}^{t_{s}} -k(t)(s(X) - \lambda(t)) \frac{\partial \lambda(t)}{\partial t} dt + \int_{0}^{t_{s}} \frac{(s(X) - \lambda(t))^{2}}{2} \frac{\partial k}{\partial t} dt$$

$$= \int_{0}^{t_{s}} -k(t)(s(X) - \lambda(t)) v dt + \int_{0}^{t_{s}} \frac{(s(X) - \lambda(t))^{2}}{2} \frac{\partial k}{\partial t} dt$$

$$\simeq \sum_{i} -k(t_{i})(s(X(t_{i})) - \lambda(t_{i})) \Delta \lambda(t_{i}) + \sum_{i} \frac{(s(X(t_{i})) - \lambda(t_{i}))^{2}}{2} \Delta k(t_{i})$$

where we denoted  $\Delta\lambda(t_i)$  the difference of the center of the harmonic potential respect to the step before and  $\Delta k(t_i)$  is the difference in spring constant respect to the step before. So in the exercised proposed in the first phase you see only the second part of the work since this is the part connected with the spring constant increase. After this phase you see the increase due to the motion of the center and then you later the release of the spring constant.

The work profile as function of time when steering ala dipeptide along the  $\Phi$  variable.

This you get with gnuplot:

```
pd@plumed:~>gnuplot
gnuplot> p "COLVAR" u 1:7 w lp
```

Another couple of interesting thing that you can check is

- Is my system finally in the C7ax? Plot the two dihedral to have a sense if we are in the right state. You know the target position what should look like, right?
- Is my system moving close to the center of the harmonic potential? This is important and we will see why in a while.

## 12.5.3 Moving on a more complex path

Very often it is useful to use this movingrestraint to make a fancier schedule by using nice properties of MOVIN $\leftarrow$  GRESTRAINT. For example you can plan a schedule to drive multiple CVs at the same time in specific point of the phase space and also to stop for a while in specific using a fixed harmonic potential. This can be handy in case of an umbrella sampling run where you might want to explore a 1-dimensional landscape by acquiring some statistics in one point and then moving to the next to acquire more statistics. With MOVINGRESTRAINT you can do it in only one file. To give an example of such capabilities, let's say that we want to move from C7eq vertically toward  $\Phi = -1.5$ ;  $\Psi = -1.3$ , stop by for a while (e.g. to acquire a statistics that you might need for an umbrella sampling), then moving toward  $\Phi = 1.3$ ;  $\Psi = -1.3$  which roughly corresponds to C7ax.

This can be programmed conveniently with MOVINGRESTRAINT by adopting the following schedule

```
# set up two variables for Phi and Psi dihedral angles
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
# the movingrestraint
restraint: ...
       MOVINGRESTRAINT
       ARG=phi,psi
       AT0 = -1.5, 1.3
                     STEP0=0
                                  KAPPA0=0.0
       AT1=-1.5,1.3 STEP1=2000
                                  KAPPA1=1000,1000
        AT2=-1.5,-1.3 STEP2=4000
                                  KAPPA2=1000,1000
        AT3=-1.5,-1.3 STEP3=4000
                                  KAPPA3=1000,1000
       AT4=1.3,-1.3 STEP4=6000
                                  KAPPA4=1000,1000
       AT5=1.3,-1.3 STEP5=8000
                                  KAPPA5=0.0
# monitor the two variables and various restraint outputs
PRINT STRIDE=10 ARG=* FILE=COLVAR
```

Note that by adding two arguments for movingrestraint, now I am allowed to put two values (separated by comma, as usual for multiple values in PLUMED) and correspondingly two KAPPA values. One for each variable. Please note that no space must be used bewtween the arguments! This is a very common fault in writing the inputs.

By plotting the instataneous value of the variables and the value of the center of the harmonic potentials we can inspect the pathways that we make the system walk on the Ramachandran plot. (How to do this? Have a look to the header of COLVAR file to plot the right fields)

.png

## Plot of the double steering schedule using MOVINGRESTRAINT

## 12.5.4 Why work is important?

The work as we have seen is the cumulative change of the hamiltonian in time. So it is connected with the change in energy of your system while you move it around. It has also a more important connection with the free energy via the Jarzynski equation which reads

$$\Delta F = -\beta^{-1} \ln \langle \exp^{-\beta W} \rangle$$

This is important and says that potentially you can calculate the free energy even by driving your system very fast and out of equilibrium between two states of your interest. Unfortunately this in practice not possible since the accurate calculation of the quantity  $\langle \exp^{-\beta W} \rangle$  has a huge associated error bar since it involves the average of a noisy quantity (the work) being exponentiated. So, before going wild with SMD, I want to make a small exercise on how tricky that is even for the smallest system.

Now we run, say 30 SMD run and we calculate the free energy difference by using Jarzynski equality and see how this differs from the average. First note that the average  $\langle \exp^{-\beta W} \rangle$  is an average over a number of steered MD runs which start from the same value of CV and reach the final value of CV. So it is important to create initially an

ensemble of states which are compatible with a given value of CVs. Let's assume that we can do this by using a restrained MD in a point (say at Phi=-1.5). In practice the umbrella biases a bit your distribution and the best situation would be to do this with a flat bottom potential and then choosing the snapshot that correspond to the wanted starting value and start from them.

In the directory JARZ/MAKE\_ENSEMBLE you find the script to run. After you generate the constrained ensemble this needs to be translated from xtc format to something that GROMACS is able to read in input, typically a more convenient gro file. To do so just to

```
pd@plumed:~> echo 0 | trjconv_mpi-dp-pl -f traj.xtc -s topol.tpr -o all.gro
pd@plumed:~> awk 'BEGIN{i=1}{if($1=="Generated"){outfile=sprintf("start_%d.gro",i);i++}print >>outfile; if(NF=
```

This will generate a set of numbered gro files. Now copy them in the parallel directory MAKE\_STEER. There you will find a script (script.sh) where you can set the number of runs that you want to go for. Just try 20 and let it run. Will take short time. The script will also produce a script\_rama.gplt that you can use to visualize all the work performed in a single gnuplot session. Just do:

```
pd@plumed:~>gnuplot
gnuplot> load "script_work.gplt"
```

What you see is something like in Fig.

There are a number of interesting fact here. First you see that different starting points may end with very different work values. Not bad, one would say, since Jarzyinsi equality is saying that we can make an average and everything will be ok. So now calculate the average work by using the following bash one-liner:

```
pd@plumed:~> ntest=20; for i in `seq 1 $ntest`; do tail -1 colvar_$i | awk '{print $7 }'; done | awk '{g+=extrapr} awk
```

For my test, what I get is a value of

```
FREE ENERGY ESTIMATE 17.482 STDEV 7.40342
```

and what this is saying is that the only thing that matters is the lowest work that I sampled. This has such an enormous weight over all the other trajectories that will do so that it will be the only other to count, and all the other do not matter much. So it is a kind of a waste of time. Also the standard deviation is rather high and probably it might well be that you obtain a much better result by using a standard umbrella sampling where you can use profitably most of the statistics. Here you waste most of the statistics indeed, since only the lowest work sampled will matter.

Some important point for doing some further exercises:

- How does the work distribution change if you increase the simulation time? Note that you have to increase both the time in the md.mdp file and in the plumed.dat file.
- How the work change if you now use a softer spring constant? And a harder one?
- In particular, what happens when you have softer spring constant, say 10? This does not look like working? Can you guess what is going on there from an analysis of COLVAR files only?
- Have a look of the trajectories in the Ramachandran plot in case of fast simulations and slow simulation. What
  can you observe? Is there a correlation between steering speed and how often you can go on the low energy
  path?

## 12.5.5 Targeted MD

Targeted MD can be seen as a special case of steered MD where the RMSD from a reference structure is used as a collective variable. It can be used for example if one wants to prepare the system so that the coordinates of selected atoms are as close as possible to a target pdb structure.

As an example we can take alanine dipeptide again

```
# set up two variables for Phi and Psi dihedral angles
# these variables will be just monitored to see what happens
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
# creates a CV that measures the RMSD from a reference pdb structure
# the RMSD is measured after OPTIMAL alignment with the target structure
rmsd: RMSD REFERENCE=c7ax.pdb TYPE=OPTIMAL
# the movingrestraint
restraint: ...
        MOVINGRESTRAINT
        ARG=rmsd
        AT0=0.0 STEP0=0
                             KAPPA0=0
        AT1=0.0 STEP1=5000 KAPPA1=10000
# monitor the two variables and various restraint outputs
PRINT STRIDE=10 ARG=* FILE=COLVAR
```

(see TORSION, RMSD, MOVINGRESTRAINT, and PRINT).

Note that RMSD should be provided a reference structure in pdb format and can contain part of the system but the second column (the index) must reflect that of the full pdb so that PLUMED knows specifically which atom to drag where. The MOVINGRESTRAINT bias potential here acts on the rmsd, and the other two variables (phi and psi) are untouched. Notice that whereas the force from the restraint should be applied at every step (thus rmsd is computed at every step) the two torsions are computed only every 10 steps. PLUMED automatically detect which variables are used at every step, leading to better performance when complicated and computationally expensive variables are monitored - this is not the case here, since the two torsions are very fast to compute. Note that here the work always increase with time and never gets lower which is somewhat surprising if you tink that we are moving in another metastable state. One would expect this to bend and give a signal of approaching a minimum like before. Nevertheless consider what you we are doing: we are constraining the system in one specific conformation and this is completely unnatural for a system at 300 kelvin so, even for this small system adopting a specific conformation in which all the heavy atoms are in a precise position is rather unrealistic. This means that this state is an high free energy state.

# 12.6 Belfast tutorial: Metadynamics

## 12.6.1 Aims

The aim of this tutorial is to introduce the users to running a metadynamics simulation with PLUMED. We will set up a simple simulation of alanine dipeptide in vacuum, analyze the output, and estimate free energies from the simulation. We will also learn how to run a well-tempered metadynamics simulation and detect issues related to a bad choice of collective variables.

## 12.6.2 Summary of theory

In metadynamics, an external history-dependent bias potential is constructed in the space of a few selected degrees of freedom  $\vec{s}(q)$ , generally called collective variables (CVs) ?. This potential is built as a sum of Gaussians deposited along the trajectory in the CVs space:

$$V(\vec{s},t) = \sum_{k\tau < t} W(k\tau) \exp\left(-\sum_{i=1}^{d} \frac{(s_i - s_i(q(k\tau)))^2}{2\sigma_i^2}\right).$$

where  $\tau$  is the Gaussian deposition stride,  $\sigma_i$  the width of the Gaussian for the ith CV, and  $W(k\tau)$  the height of the Gaussian. The effect of the metadynamics bias potential is to push the system away from local minima into visiting new regions of the phase space. Furthermore, in the long time limit, the bias potential converges to minus the free energy as a function of the CVs:

$$V(\vec{s}, t \to \infty) = -F(\vec{s}) + C.$$

In standard metadynamics, Gaussians of constant height are added for the entire course of a simulation. As a result, the system is eventually pushed to explore high free-energy regions and the estimate of the free energy calculated from the bias potential oscillates around the real value. In well-tempered metadynamics ?, the height of the Gaussian is decreased with simulation time according to:

$$W(k\tau) = W_0 \exp\left(-\frac{V(\vec{s}(q(k\tau)), k\tau)}{k_B \Delta T}\right),$$

where  $W_0$  is an initial Gaussian height,  $\Delta T$  an input parameter with the dimension of a temperature, and  $k_B$  the Boltzmann constant. With this rescaling of the Gaussian height, the bias potential smoothly converges in the long time limit, but it does not fully compensate the underlying free energy:

$$V(\vec{s}, t \to \infty) = -\frac{\Delta T}{T + \Delta T} F(\vec{s}) + C.$$

where T is the temperature of the system. In the long time limit, the CVs thus sample an ensemble at a temperature  $T+\Delta T$  which is higher than the system temperature T. The parameter  $\Delta T$  can be chosen to regulate the extent of free-energy exploration:  $\Delta T=0$  corresponds to standard molecular dynamics,  $\Delta T\to\infty$  to standard metadynamics. In well-tempered metadynamics literature and in PLUMED, you will often encounter the term "biasfactor" which is the ratio between the temperature of the CVs (  $T+\Delta T$ ) and the system temperature ( T):

$$\gamma = \frac{T + \Delta T}{T}.$$

The biasfactor should thus be carefully chosen in order for the relevant free-energy barriers to be crossed efficiently in the time scale of the simulation.

Additional information can be found in the several review papers on metadynamics???

## 12.6.3 Learning Outcomes

Once this tutorial is completed students will know how to:

- · run a metadynamics simulation using PLUMED
- · analyze the output of the simulation
- · restart a metadynamics simulation
- · calculate free energies from a metadynamics simulation
- · run a well-tempered metadynamics simulation using PLUMED
- · detect issues with the choice of the collective variables

#### 12.6.4 Resources

The tarball for this project contains the following directories:

- · TOPO: it contains the gromacs topology and configuration files to simulate alanine dipeptide in vacuum
- Exercise 1: run a metadynamics simulation with 2 CVs, dihedrals phi and psi, and analyze the output
- Exercise\_2: restart a metadynamics simulation
- Exercise\_3: calculate free energies from a metadynamics simulation and monitor convergence
- · Exercise\_4: run a well-tempered metadynamics simulation with 2 CVs, dihedrals phi and psi
- Exercise 5: run a well-tempered metadynamics simulation with 1 CV, dihedral psi

#### 12.6.5 Instructions

#### 12.6.5.1 The model system

Here we use as model system alanine dipeptide in vacuum with AMBER99SB-ILDN all-atom force field.

## 12.6.5.2 Exercise 1. Setup and run a metadynamics simulation

In this exercise, we will run a metadynamics simulation on alanine dipeptide in vacuum, using as CVs the two backbone dihedral angles phi and psi. In order to run this simulation we need to prepare the PLUMED input file (plumed.dat) as follows.

```
# set up two variables for Phi and Psi dihedral angles
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
#
# Activate metadynamics in phi and psi
# depositing a Gaussian every 500 time steps,
# with height equal to 1.2 kJoule/mol,
# and width 0.35 rad for both CVs.
#
metad: METAD ARG=phi,psi PACE=500 HEIGHT=1.2 SIGMA=0.35,0.35 FILE=HILLS
# monitor the two variables and the metadynamics bias potential
PRINT STRIDE=10 ARG=phi,psi,metad.bias FILE=COLVAR
```

```
(see TORSION, METAD, and PRINT).
```

The syntax for the command METAD is simple. The directive is followed by a keyword ARG followed by the labels of the CVs on which the metadynamics potential will act. The keyword PACE determines the stride of Gaussian deposition in number of time steps, while the keyword HEIGHT specifies the height of the Gaussian in kJoule/mol. For each CVs, one has to specified the width of the Gaussian by using the keyword SIGMA. Gaussian will be written to the file indicated by the keyword FILE.

Once the PLUMED input file is prepared, one has to run Gromacs with the option to activate PLUMED and read the input file:

```
gmx_mpi mdrun -plumed
```

During the metadynamics simulation, PLUMED will create two files, named COLVAR and HILLS. The COLVAR file contains all the information specified by the PRINT command, in this case the value of the CVs every 10 steps of simulation, along with the current value of the metadynamics bias potential. The HILLS file contains a list of the Gaussians deposited along the simulation. If we give a look at the header of this file, we can find relevant information about its content:

```
#! FIELDS time phi psi sigma_phi sigma_psi height biasf
#! SET multivariate false
#! SET min_phi -pi
#! SET max_phi pi
#! SET min_psi -pi
#! SET max_psi pi
```

The line starting with FIELDS tells us what is displayed in the various columns of the HILLS file: the time of the simulation, the value of phi and psi, the width of the Gaussian in phi and psi, the height of the Gaussian, and the biasfactor. This quantity is relevant only for well-tempered metadynamics simulation (see Exercise 4. Setup and run a well-tempered metadynamics simulation, part I) and it is equal to 1 in standard metadynamics simulations. We will use the HILLS file later to calculate free-energies from the metadynamics simulation and assess its convergence. For the moment, we can plot the behavior of the CVs during the simulation.

By inspecting Figure belfast-6-metad-fig, we can see that the system is initialized in one of the two metastable states of alanine dipeptide. After a while (t=0.3 ns), the system is pushed by the metadynamics bias potential to visit the other local minimum. As the simulation continues, the bias potential fills the underlying free-energy landscape, and the system is able to diffuse in the entire phase space.

If we use the PLUMED input file described above, the expense of a metadynamics simulation increases with the length of the simulation as one has to evaluate the values of a larger and larger number of Gaussians at every step. To avoid this issue you can store the bias on a grid. In order to use grids, we have to add some additional information to the line of the METAD directive, as follows.

```
# set up two variables for Phi and Psi dihedral angles
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
#
# Activate metadynamics in phi and psi
# depositing a Gaussian every 500 time steps,
# with height equal to 1.2 kJoule/mol,
# and width 0.35 rad for both CVs.
# The bias potential will be stored on a grid
# with bin size equal to 0.1 rad for both CVs.
# The boundaries of the grid are -pi and pi, for both CVs.
# METAD ...
LABEL=metad
ARG=phi,psi
PACE=500
HEIGHT=1.2
```

```
SIGMA=0.35,0.35
FILE=HILLS
GRID_MIN=-pi,-pi
GRID_MAX=pi,pi
GRID_SPACING=0.1,0.1
... METAD
# monitor the two variables and the metadynamics bias potential
PRINT STRIDE=10 ARG=phi,psi,metad.bias FILE=COLVAR
```

The bias potential will be stored on a grid, whose boundaries are specified by the keywords GRID\_MIN and GR← ID\_MAX. Notice that you should provide either the number of bins for every collective variable (GRID\_BIN) or the desired grid spacing (GRID\_SPACING). In case you provide both PLUMED will use the most conservative choice (highest number of bins) for each dimension. In case you do not provide any information about bin size (neither GRID\_BIN nor GRID\_SPACING) and if Gaussian width is fixed PLUMED will use 1/5 of the Gaussian width as grid spacing. This default choice should be reasonable for most applications.

## 12.6.5.3 Exercise 2. Restart a metadynamics simulation

If we try to run again a metadynamics simulation using the script above in a directory where a COLVAR and HILLS files are already present, PLUMED will create a backup copy of the old files, and run a new simulation. Instead, if we want to restart a previous simulation, we have to add the keyword RESTART to the PLUMED input file (plumed.dat), as follows.

```
# restart previous simulation
RESTART

# set up two variables for Phi and Psi dihedral angles
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17

# Activate metadynamics in phi and psi
# depositing a Gaussian every 500 time steps,
# with height equal to 1.2 kJoule/mol,
# and width 0.35 rad for both CVs.
# metad: METAD ARG=phi,psi PACE=500 HEIGHT=1.2 SIGMA=0.35,0.35 FILE=HILLS
# monitor the two variables and the metadynamics bias potential
PRINT STRIDE=10 ARG=phi,psi,metad.bias FILE=COLVAR
```

#### (see RESTART, TORSION, METAD, and PRINT).

In this way, PLUMED will read the old Gaussians from the HILLS file and append the new information to both COLVAR and HILLS files.

#### 12.6.5.4 Exercise 3. Calculate free-energies and monitor convergence

One can estimate the free energy as a function of the metadynamics CVs directly from the metadynamics bias potential. In order to do so, the utility sum\_hills should be used to sum the Gaussians deposited during the simulation and stored in the HILLS file.

To calculate the two-dimensional free energy as a function of phi and psi, it is sufficient to use the following command line:

```
plumed sum_hills --hills HILLS
```

The command above generates a file called fes.dat in which the free-energy surface as function of phi and psi is calculated on a regular grid. One can modify the default name for the free energy file, as well as the boundaries and bin size of the grid, by using the following options of sum\_hills:

```
--outfile - specify the outputfile for sumhills
--min - the lower bounds for the grid
--max - the upper bounds for the grid
--bin - the number of bins for the grid
--spacing - grid spacing, alternative to the number of bins
```

It is also possible to calculate one-dimensional free energies from the two-dimensional metadynamics simulation. For example, if one is interested in the free energy as a function of the phi dihedral alone, the following command line should be used:

```
plumed sum_hills --hills HILLS --idw phi --kt 2.5
```

The result should look like this:

To assess the convergence of a metadynamics simulation, one can calculate the estimate of the free energy as a function of simulation time. At convergence, the reconstructed profiles should be similar, apart from a constant offset. The option –stride should be used to give an estimate of the free energy every N Gaussians deposited, and the option –mintozero can be used to align the profiles by setting the global minimum to zero. If we use the following command line:

```
plumed sum_hills --hills HILLS --idw phi --kt 2.5 --stride 500 --mintozero
```

one free energy is calculated every 500 Gaussians deposited, and the global minimum is set to zero in all profiles. The resulting plot should look like the following:

To assess the convergence of the simulation more quantitatively, we can calculate the free-energy difference between the two local minima in the one-dimensional free energy along phi as a function of simulation time. We can use the bash script analyze\_FES.sh to integrate the multiple free-energy profiles in the two basins defined by the following intervals in phi space: basin A, -3<phi<-1, basin B, 0.5<phi<1.5.

```
./analyze_FES.sh NFES -3.0 -1.0 0.5 1.5 KBT
```

where NFES is the number of profiles (free-energy estimates at different times of the simulation) generated by the option –stride of sum hills, and KBT is the temperature in energy units (in this case KBT=2.5).

This analysis, along with the observation of the diffusive behavior in the CVs space, suggest that the simulation is converged.

## 12.6.5.5 Exercise 4. Setup and run a well-tempered metadynamics simulation, part I

In this exercise, we will run a well-tempered metadynamics simulation on alanine dipeptide in vacuum, using as CVs the two backbone dihedral angles phi and psi. To activate well-tempered metadynamics, we need to add two keywords to the line of METAD, which specifies the biasfactor and temperature of the simulation. For the first example, we will try a biasfactor equal to 6. Here how the PLUMED input file (plumed.dat) should look like:

```
# set up two variables for Phi and Psi dihedral angles
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
#
# Activate metadynamics in phi and psi
# depositing a Gaussian every 500 time steps,
# with height equal to 1.2 kJoule/mol,
# and width 0.35 rad for both CVs.
# Well-tempered metadynamics is activated,
# and the biasfactor is set to 6.0
# metad: METAD ARG=phi,psi PACE=500 HEIGHT=1.2 SIGMA=0.35,0.35 FILE=HILLS BIASFACTOR=6.0 TEMP=300.0
# monitor the two variables and the metadynamics bias potential
PRINT STRIDE=10 ARG=phi,psi,metad.bias FILE=COLVAR
```

## (see TORSION, METAD, and PRINT).

After running the simulation using the instruction described above, we can have a look at the HILLS file. At variance with standard metadynamics, the last two columns of the HILLS file report more useful information. The last column contains the value of the biasfactor used, while the last but one the height of the Gaussian, which is rescaled during the simulation following the well-tempered recipe.

```
#! FIELDS time phi psi sigma_phi sigma_psi height biasf
#! SET multivariate false
#! SET min_phi -pi
#! SET max_phi pi
#! SET min_psi -pi
#! SET max_psi pi
               -1.3100 0.0525
     1.0000
                                           0.35
                                                            0.35
                                                                     1.4400
                -1.4054
                           1.9742
     2.0000
                                           0.35
                                                            0.35
                                                                      1.4400
                                                                                  6
     3.0000
                -1.9997
                           2.5177
                                           0.35
                                                            0.35
                                                                      1.4302
                                                                                  6
                -2.2256
                           2.1929
                                                                      1.3622
      4.0000
                                           0.35
                                                            0.35
```

If we carefully look at the height column, we will notice that in the beginning the value reported is higher than the initial height specified in the input file, which should be 1.2 kJoule/mol. In fact, this column reports the height of the Gaussian rescaled by the pre-factor that in well-tempered metadynamics relates the bias potential to the free energy. In this way, when we will use <a href="mailto:sum\_hills">sum\_hills</a>, the sum of the Gaussians deposited will directly provide the free-energy, without further rescaling needed.

We can plot the time evolution of the CVs along with the height of the Gaussian.

The system is initialized in one of the local minimum where it starts accumulating bias. As the simulation progresses and the bias added grows, the Gaussian height is progressively reduced. After a while (t=0.8 ns), the system is able to escape the local minimum and explore a new region of the phase space. As soon as this happens, the Gaussian height is restored to the initial value and starts to decrease again. In the long time, the Gaussian height becomes smaller and smaller while the system diffuses in the entire CVs space.

We can now try a different biasfactor and see the effect on the simulation. If we choose a biasfactor equal to 1.5, we can notice a faster decrease of the Gaussian height with simulation time, as expected by the well-tempered recipe. We will also conclude from the plot below that this biasfactor is not large enough to allow for the system to escape from the initial local minimum in the time scale of this simulation.

Following the procedure described for standard metadynamics in the previous example, we can estimate the free energy as a function of time and monitor the convergence of the simulations using the analyze\_FES.sh script. We will do this for the simulation in which the biasfactor was set to 6.0. In this case we will notice that the oscillations observed in standard metadynamics are here damped, and the bias potential converges more smoothly to the underlying free-energy landscape, provided that the biasfactor is sufficiently high for the free-energy barriers of the system under study to be crossed.

## 12.6.5.6 Exercise 5. Setup and run a well-tempered metadynamics simulation, part II

In this exercise, we will study the effect of neglecting a relavant degree of freedom in the choice of metadynamics CVs. We are going to run a well-tempered metadynamics simulation with the psi dihedral alone as CV, using the following PLUMED input file (plumed.dat):

```
# set up two variables for Phi and Psi dihedral angles
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
#
# Activate metadynamics in psi
# depositing a Gaussian every 500 time steps,
# with height equal to 1.2 kJoule/mol,
# and width 0.35 rad.
# Well-tempered metadynamics is activated,
# and the biasfactor is set to 10.0
#
metad: METAD ARG=psi PACE=500 HEIGHT=1.2 SIGMA=0.35 FILE=HILLS BIASFACTOR=10.0 TEMP=300.0
# monitor the two variables and the metadynamics bias potential
PRINT STRIDE=10 ARG=phi,psi,metad.bias FILE=COLVAR
```

(see TORSION, METAD, and PRINT).

Let's look at the HILLS file, in particular at the time serie of the CV psi and of the Gaussian height.

From this plot, we observe a nice diffusive behavior of the CV psi when the Gaussian height is already quite small. This happens until t=3 ns, when the CV seems to be stuck for a while in a small region of the CV space. This behavior is typical of a situation in which a slow variable is not included in the set of CV. When something happens in this hidden degree of freedom, the biased CVs typically cannot access anymore regions of the phase space previously visited. To understand this behavior, we need to visualize the time evolution of both phi and psi stored in the COLVAR file.

It is clear from the plot above that what happened around t=3 ns is a jump of the neglected, slow degree of freedom phi from one free-energy basin to another. The dynamics of phi is not biased by any potential, so we need to equilibrate this degree of freedom, i.e. to observe multiple transitions from the two basins, before declaring convergence of our simulation. Or alternatively we can add phi to the set of CVs. This example demonstrates how to declare convergence of a well-tempered metadynamics simulation it is necessary but not sufficient to observe: 1) Gaussians with very small height, 2) a diffusive behavior in the CV space (as in the first 3 ns of this example). What we should do is repeating the simulation multiple times starting from different initial conformations. If in all simulations, we observe a diffusive behavior in the biased CV when the Gaussian height is very small, and we obtain very similar free-energy surfaces, then we can be quite confident that our simulations are converged to the right value. If this is not the case, a manual inspection of the runs can help us identifying the missing slow degrees of freedom to add to the set of biased CVs.

## 12.7 Belfast tutorial: Replica exchange I

## 12.7.1 Aims

The aim of this tutorial is to introduce the users to running a parallel tempering (PT) simulation using PLUMED. We will set up a simple simulation of alanine dipeptide in vacuum, analyze the output, calculate free energies from the simulation, and detect problems. We will also learn how to run a combined PT-metadynamics simulation (PTMetaD) and introduce the users to the Well-Tempered Ensemble (WTE).

## 12.7.2 Summary of theory

In Replica Exchange Methods ? (REM), sampling is accelerated by modifying the original Hamiltonian of the system. This goal is achieved by simulating N non-interacting replicas of the system, each evolving in parallel according to a different Hamiltonian. At fixed intervals, an exchange of configurations between two replicas is attempted. One popular case of REM is PT, in which replicas are simulated using the same potential energy function, but different temperatures. By accessing high temperatures, replicas are prevented from being trapped in local minima. In PT, exchanges are usually attempted between adjacent temperatures with the following acceptance probability:

$$p(i \to j) = min\{1, \Delta_{i,j}^{PT}\},\$$

with

$$\Delta_{i,j}^{PT} = \left(\frac{1}{k_B T_i} - \frac{1}{k_B T_i}\right) \left(U(R_i) - U(R_j)\right),$$

where  $R_i$  and  $R_j$  are the configurations at temperature  $T_i$  and  $T_j$ , respectively. The equation above suggests that the acceptance probability is ultimately determined by the overlap between the energy distributions of two replicas. The efficiency of the algorithm depends on the benefits provided by sampling at high-temperature. Therefore, an efficient diffusion in temperature space is required and configurational sampling is still limited by entropic barriers. Finally, PT scales poorly with system size. In fact, a sufficient overlap between the potential energy distributions of neighboring temperatures is required in order to obtain a significant diffusion in temperature. Therefore, the number of temperatures needed to cover a given temperature range scales as the square root of the number of degrees of freedom, making this approach prohibitively expensive for large systems.

PT can be easily combined with metadynamics ?. In the resulting PTMetaD algorithm (16), N replicas performed in parallel a metadynamics simulation at different temperatures, using the same set of CVs. The PT acceptance probability must be modified in order to account for the presence of a bias potential:

$$\Delta_{i,j}^{PTMetaD} = \Delta_{i,j}^{PT} + \frac{1}{k_B T_i} \left[ V_G^i(s(R_i),t) - V_G^i(s(R_j),t) \right] + \frac{1}{k_B T_i} \left[ V_G^j(s(R_j),t) - V_G^j(s(R_i),t) \right],$$

where  $V_G^i$  and  $V_G^j$  are the bias potentials acting on the i-th and j-th replicas, respectively.

PTMetaD is particularly effective because it compensates for some of the weaknesses of each method alone. The effect of neglecting a slow degree of freedom in the choice of the metadynamics CVs is alleviated by PT, which allows the system to cross moderately high free-energy barriers on all degrees of freedom. On the other hand, the metadynamics bias potential allows crossing higher barriers on a few selected CVs, in such a way that the sampling efficiency of PTMetaD is greater than that of PT alone.

PTMetaD still suffers from the poor scaling of computational resources with system size. This issue may be circumvented by including the potential energy of the system among the set of well-tempered metadynamics CVs. The well-tempered metadynamics bias leads to the sampling of a well-defined distribution called Well-Tempered Ensemble (WTE)? In this ensemble, the average energy remains close to the canonical value but its fluctuations are enhanced in a tunable way, thus improving sampling. In the so-called PTMetaD-WTE scheme?, each replica diffusion in temperature space is enhanced by the increased energy fluctuations at all temperatures.

## 12.7.3 Learning Outcomes

Once this tutorial is completed students will know how to:

- · run a PT simulation
- · analyze the output of the PT simulation and detect problems
- run a PTMetaD simulation
- · run a PT and PTMetaD in the WTE

### 12.7.4 Resources

The tarball for this project contains the following directories:

- Exercise 1: run a PT simulation using 2 replicas and analyze the output
- · Exercise 2: run a PT simulation using 4 replicas and analyze the output
- Exercise\_3: run a PTMetaD simulation
- Exercise\_4: run a PT, PT-WTE and PTMetaD-WTE simulations

Each directory contains a TOPO subdirectory where topology and configuration files for Gromacs are stored.

### 12.7.5 Instructions

## 12.7.5.1 The model system

Here we use as model systems alanine dipeptide in vacuum and water with AMBER99SB-ILDN all-atom force field.

### 12.7.5.2 Exercise 1. Setup and run a PT simulation, part I

In this exercise, we will run a PT simulation of alanine dipeptide in vacuum, using only two replicas, one at 300K, the other at 305K. During this simulation, we will monitor the time evolution of the two dihedral angles phi and psi. In order to do that, we need the following PLUMED input file (plumed.dat).

```
# set up two variables for Phi and Psi dihedral angles
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17

# monitor the two variables
PRINT STRIDE=10 ARG=phi,psi FILE=COLVAR
```

(see TORSION, and PRINT).

To submit this simulation with Gromacs, we need the following command line.

```
mpirun -np 2 gmx_mpi mdrun -s TOPO/topol -plumed -multi 2 -replex 100
```

This command will execute two MPI processess in parallel, using the topology files topol0.tpr and topol1.tpr stored in the TOPO subdirectory. These two binary files have been created using the usual Gromacs procedure (see Gromacs manual for further details) and setting the temperature of the two simulations at 300K and 305K in the configuration files. An exchange between the configurations of the two simulations will be attempted every 100 steps.

When Gromacs is executed using the -multi option and PLUMED is activated, the output files produced by PLU← MED will be renamed and a suffix indicating the replica id will be appended. We will start inspecting the output file COLVAR.0, which reports the time evolution of the CVs at 300K.

The plot above suggests that during the PT simulation the system is capable to access both the relevant basins in the free-energy surface. This seems to suggest that our simulation is converged. We can use the COLVAR.0 and COLVAR.1 along with the tool sum\_hills to estimate the free energy as a function of the CV phi. We will do this a function of simulation time to assess convergence more quantitatively, using the following command line:

```
plumed sum_hills --histo COLVAR.0 --idw phi --sigma 0.2 --kt 2.5 --outhisto fes_ --stride 1000
```

As we did in our previous tutorial, we can now use the script analyze\_FES.sh to calculate the free-energy difference between basin A (-3.0 < phi < -1.0) and basin B (0.5 < phi < 1.5), as a function of simulation time.

The estimate of the free-energy difference between these two basins seems to be converged. This consideration, along with the observation that the system is exploring all the relevant free-energy basins, might lead us to declare convergence and to state that the difference in free energy between basin A and B is roughly 0 kJoule/mol. Unfortunately, in doing so we would make a big mistake.

In PT simulations we have to be a little bit more careful, and examine the time evolution of each replica diffusing in temperature space, before concluding that our simulation is converged. In order to do that, we need to reconstruct the continuous trajectories of the replicas in temperature from the two files (typically traj0.trr and traj1.trr) which contain the discontinuous trajectories of the system at 300K and 305K. To demux the trajectories, we need to use the following command line:

```
demux.pl md0.log
```

which will create two files, called replica\_temp.xvg and replica\_index.xvg. We can plot the first file, which reports the temperature index of each configuration at a given time of the simulation. This file is extremely useful, because it allows us monitoring the replicas diffusion in temperature. As we discussed in Summary of theory, in order for the PT algorithm to be effective, we need an efficient diffusion of the replicas in temperature space. In this case, both replicas are rapidly accessing the highest temperature, so there seems not to be any problem on this side.

We can use the second file to reconstruct the continuous trajectories of each replica in temperature:

```
gmx_mpi trjcat -f traj0.trr traj1.trr -demux replica_index.xvg
```

and the following PLUMED input file (plumed\_demux.dat) to recalculate the value of the CVs on the demuxed trajectories, typically called 0\_trajout.xtc and 1\_trajout.xtc.

```
# set up two variables for Phi and Psi dihedral angles
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
# monitor the two variables
PRINT STRIDE=1 ARG=phi,psi FILE=COLVAR_DEMUX
```

(see TORSION, and PRINT).

For the analysis of the demuxed trajectories, we can use the -rerun option of Gromacs, as follows:

```
# rerun Gromacs on replica 0 trajectory
gmx_mpi mdrun -s TOPO/topol0.tpr -plumed plumed_demux.dat -rerun 0_trajout.xtc
# rename the output
mv COLVAR_DEMUX COLVAR_DEMUX.0
# rerun Gromacs on replica 1 trajectory
gmx_mpi mdrun -s TOPO/topol1.tpr -plumed plumed_demux.dat -rerun 1_trajout.xtc
# rename the output
mv COLVAR_DEMUX COLVAR_DEMUX.1
```

We can now plot the time evolution of the two CVs in the two demuxed trajectories.

This plot shows clearly that each replica is sampling only one of the two basins of the free-energy landscape, and it is never able to cross the high barrier that separates them. This means that what we considered an exhaustive exploration of the free energy landscape at 300K (Figure belfast-7-pt-fig), was instead caused by an efficient exchange of configurations between replicas that were trapped in different free-energy basins. The results of the present simulation were then influenced by the initial conformations of the two replicas. If we had initialized both of them in the same basin, we would have never observed "transitions" to the other basin at 300K.

To declare convergence of a PT simulation, it is thus mandatory to examine the behavior of the replicas diffusing in temperature and check that these are exploring all the relevant basins. Another good practice is repeating the PT simulation starting from different initial conformations, and check that the results are consistent.

## 12.7.5.3 Exercise 2. Setup and run a PT simulation, part II

We will now repeat the previous exercise, but with a different setup. The problem with the previous exercise was that replicas were never able to interconvert between the two metastable states of alanine dipeptide in vacuum. The reason was that the highest temperature used (305K) was too low to accelerate barrier crossing in the time scale of the simulation. We will now use 4 replicas at the following temperatures: 300K, 400K, 600K, and 1000K.

We can use the same PLUMED input file described above (plumed.dat), and execute Gromacs using the following command line:

```
mpirun -np 4 gmx_mpi mdrun -s TOPO/topol -plumed -multi 4 -replex 100
```

At the end of the simulation, we first monitor the diffusion in temperature space of each replica. We need to create the replica\_temp.xvg and replica\_index.xvg:

```
demux.pl md0.log
```

and plot the content of replica\_temp.xvg. Here how it should look for Replica 0:

From this analysis, we can conclude that replicas are diffusing effectively in temperature. Now, we need to monitor the space sampled by each replica while diffusing in temperature space and verify that they are interconverting between the different basins of the free-energy landscape. The demux is carried out as in the previous example:

```
trjcat_mpi -f traj0.trr traj1.trr traj2.trr traj3.trr -demux replica_index.xvg
```

and so is the analysis of the demuxed trajectories using the -rerun option of Gromacs and the plumed\_demux.dat input file. Here is the space sampled by two of the four replicas:

It is clear that in this case replicas are able to interconvert between the two metastable states, while efficiently diffusing in temperature. We can then calculate the free-energy difference between basin A and B as a function of simulation time at 300K:

and conclude that in this case the PT simulation is converged.

## 12.7.5.4 Exercise 3. Setup and run a PTMetaD simulation

In this exercise we will learn how to combine PT with metadynamics. We will use the setup of the previous exercise, and run a PT simulations with 4 replicas at the following temperatures: 300K, 400K, 600K, and 1000K. Each simulation will perform a well-tempered metadynamics calculation, using the dihedral psi alone as CV and a biasfactor equal to 10 (see Exercise 5. Setup and run a well-tempered metadynamics simulation, part II).

Previously, we prepared a single PLUMED input file to run a PT simulation. This was enough, since in that case the same task was performed at all temperatures. Here instead we need to have a slightly different PLUMED input file for each simulation, since we need to use the keyword TEMP to specify the temperature on the line of the METAD directory. We will thus prepare 4 input files, called plumed.0.dat, plumed.1.dat, plumed.2.dat, and plumed.3.dat, with a different value for the keyword TEMP.

## Warning

Notice that the rules for replica suffix are changed with version 2.2. With PLUMED versions 2.0 and 2.1 these files should have been named plumed.dat.0, plumed.dat.1, etc.

Here how plumed.3.dat should look like:

```
# set up two variables for Phi and Psi dihedral angles
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
#
# Activate metadynamics in psi
# depositing a Gaussian every 500 time steps,
# with height equal to 1.2 kJoule/mol,
# and width 0.35 rad.
# Well-tempered metadynamics is activated,
# and the biasfactor is set to 10.0
# metad: METAD ARG=psi PACE=500 HEIGHT=1.2 SIGMA=0.35 FILE=HILLS BIASFACTOR=10.0 TEMP=1000.0
# monitor the two variables and the metadynamics bias potential
PRINT STRIDE=10 ARG=phi,psi,metad.bias FILE=COLVAR
```

(see TORSION, METAD, and PRINT).

The PTMetaD simulation is executed in the same way as the PT:

```
mpirun -np 4 gmx_mpi mdrun -s TOPO/topol -plumed -multi 4 -replex 100
```

and it will produce one COLVAR and HILLS file per temperature (COLVAR.0, HILLS.0, ...). The analysis of the results requires what we have learned in the previous exercise for the PT case (analysis of the replica diffusion in temperature and demuxing of each replica trajectory), and the post-processing of a well-tempered metadynamics simulation (FES calculation using sum\_hills and convergence analysis).

Since in the previous tutorial we performed the same well-tempered metadynamics simulation without the use of PT (see Exercise 5. Setup and run a well-tempered metadynamics simulation, part II), here we can focus on the differences with the PTMetaD simulation. Let's compare the behavior of the biased variable psi in the two simulations:

In well-tempered metadynamics (left panel), the biased variable psi looked stuck early in the simulation (t=3 ns). The reason was the transition of the other hidden degree of freedom phi from one free-energy basin to the other. In the PTMetaD case (right panel), this seems not to happen. To better appreciate the difference, we can plot the time evolution of the hidden degree of freedom phi in the two cases.

Thanks to the excursions at high temperature, in the PTMetaD simulation the transition of the CV phi between the two basins is accelerate. As a result, the convergence of the reconstructed free energy in psi will be accelerated. This simple exercise demonstrates how PTMetaD can be used to cure a bad choice of metadynamics CVs and the neglecting of slow degrees of freedom.

### 12.7.5.5 Exercise 4. The Well-Tempered Ensemble

In this exercise we will learn how to run a PT-WTE and PTMetaD-WTE simulations of alanine dipeptide in water. We will start by running a short PT simulation using 4 replicas in the temperature range between 300K and 400K. We will use a geometric distribution of temperatures, which is valid under the assumption that the specific heat of the system is constant across temperatures. Replicas will thus be simulated at T=300, 330.2, 363.4, and 400K. In this simulation, we will just monitor the two dihedral angles and the total energy of the system, by preparing the following PLUMED input file (plumed\_PT.dat):

```
# set up three variables for Phi and Psi dihedral angles
# and total energy
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
ene: ENERGY
# monitor the three variables
PRINT STRIDE=10 ARG=phi,psi,ene FILE=COLVAR_PT
```

(see TORSION, ENERGY, and PRINT).

As usual, the simulation is run for 400ps using the following command:

```
mpirun -np 4 gmx_mpi mdrun -s TOPO/topol -plumed plumed_PT.dat -multi 4 -replex 100
```

At the end of the run, we want to analyze the acceptance rate between exchanges. This quantity is reported at the end of the Gromacs output file, typically called md.log, and it can be extracted using the following bash command line:

```
grep -A2 "Repl average probabilities" md0.log
```

From the line above, we will find out that none of the attempted exchanges has been accepted. The reason is that the current setup (4 replicas to cover the temperature range 300-400K) resulted in a poor overlap of the energy distributions at different temperatures. We can easily realize this by plotting the time series of the total energy in the different replicas:

To improve the overlap of the potential energy distributions at different temperatures, we enlarge the fluctuations of the energy by sampling the Well-Tempered Ensemble (WTE). In order to do that, we need to setup a well-tempered metadynamics simulation using energy as CV. In WTE, fluctuations - the standard deviation of the energy time serie measured above - will be enhanced by a factor equal to the square root of the biasfactor. In this exercise, we will enhance fluctuations of a factor of 4, thus we will set the biasfactor equal to 16. We need to prepare 4 PLUM← ED input files (plumed\_PTWTE.dat.0, plumed\_PTWTE.dat.1,...), which will be identical to the following but for the temperature specified in the line of the METAD directive:

```
# set up three variables for Phi and Psi dihedral angles
# and total energy
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
ene: ENERGY
# Activate metadynamics in ene
# depositing a Gaussian every 250 time steps,
# with height equal to 1.2 kJoule/mol,
# and width 140 kJoule/mol.
# Well-tempered metadynamics is activated,
# and the biasfactor is set to 16.0
#
wte: METAD ARG=ene PACE=250 HEIGHT=1.2 SIGMA=140.0 FILE=HILLS_PTWTE BIASFACTOR=16.0 TEMP=300.0
# monitor the three variables and the metadynamics bias potential
PRINT STRIDE=10 ARG=phi,psi,ene,wte.bias FILE=COLVAR_PTWTE
```

```
(see TORSION, ENERGY, METAD, and PRINT).
```

Here, we use a Gaussian width larger than usual, and of the order of the fluctuations of the potential energy at 300K, as calculated from the preliminary PT run.

We run the simulation following the usual procedure:

```
mpirun -np 4 gmx_mpi mdrun -s TOPO/topol -plumed plumed_PTWTE.dat -multi 4 -replex 100
```

If we analyze the average acceptance probability in this run:

```
grep -A2 "Repl average probabilities" md0.log
```

we will notice that now on average 18% of the exchanges are accepted. To monitor the diffusion of each replica in temperature, we can examine the file replica\_temp.xvg created by the following command line:

```
demux.pl md0.log
```

This analysis assures us that the system is efficiently diffusing in the entire temperature range and no bottlenecks are present.

Finally, as done in the previous run, we can visualize the time serie of the energy CV at all temperatures:

If we compare this plot with the one obtained in the PT run, we can notice that now the enlarged fluctuations caused by the use of WTE lead to a good overlap between energy distributions at different temperatures, thus increasing the exchange acceptance probability. At this point, we can extend our PT-WTE simulation and for example converge the free energy as a function of the dihedral angles phi and psi. Alternatively, we can accelerate sampling of the phi and psi dihedrals by combining PT-WTE with a metadynamics simulation using phi and psi as CVs (PTMetaD-WTE ?). This can be achieved by preparing 4 PLUMED input files (plumed\_PTMetaDWTE.dat.0, plumed\_PTMetaDW TE.dat.1,...), which will be identical to the following but for the temperature specified in the two lines containing the METAD directives:

```
# reload WTE bias
RESTART
# set up three variables for Phi and Psi dihedral angles
# and total energy
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
ene: ENERGY
# Activate metadynamics in ene
# Old Gaussians will be reloaded to perform
# the second metadynamics run in WTE.
wte: METAD ARG-ene PACE-99999999 HEIGHT=1.2 SIGMA=140.0 FILE-HILLS_PTWTE BIASFACTOR=16.0 TEMP=300.0
# Activate metadynamics in phi and psi
# depositing a Gaussian every 500 time steps,
# with height equal to 1.2 kJoule/mol,
# and width 0.35 rad for both CVs.
# Well-tempered metadynamics is activated,
\# and the biasfactor is set to 6.0
metad: METAD ARG=phi,psi PACE=500 HEIGHT=1.2 SIGMA=0.35,0.35 FILE=HILLS_PTMetaDWTE BIASFACTOR=6.0 TEMP=300.0
# monitor the three variables, the wte and metadynamics bias potentials
PRINT STRIDE=10 ARG=phi,psi,ene,wte.bias,metad.bias FILE=COLVAR_PTMetaDWTE
```

## (see TORSION, ENERGY, METAD, and PRINT).

These scripts activate two metadynamics simulations. One will use the energy as CV and will reload the Gaussians deposited during the preliminary PT-WTE run. No additional Gaussians on this variable will be deposited during the PTMetaD-WTE simulation, due to the large deposition stride. A second metadynamics simulation will be activated on the dihedral angles. Please note the different parameters and biasfactors in the two metadynamics runs.

The simulation is carried out using the usual procedure:

```
mpirun -np 4 gmx_mpi mdrun -s TOPO/topol -plumed plumed_PTMetaDWTE.dat -multi 4 -replex 100
```

# 12.8 Belfast tutorial: Replica exchange II and Multiple walkers

## 12.8.1 Aims

The aim of this tutorial is to introduce the users to the use of Bias-Exchange Metadynamics. We will go through the writing of the input files for BEMETA for a simple case of three peptide and we will use METAGUI to to analyse them. We will compare the results of WT-BEMETA and STANDARD-BEMETA with four independent runs on the four Collective Variables. Finally we will use a simplified version of BEMETA that is Multiple Walkers Metadynamics.

### 12.8.1.1 Learning Outcomes

Once this tutorial is completed students will:

- Know how to run a Bias-Exchange simulation using PLUMED and GROMACS
- · Know how to analyse the results of BEMETA with the help of METAGUI
- · Know how to run a Multiple Walker simulation

### 12.8.2 Resources

The tarball for this project contains the following files:

- · system folder: a starting structure for Val-Ile-Leu system
- WTBX: a run of Well-Tempered Bias-Exchange Metadynamics ready for the analysis

## 12.8.3 Instructions

## 12.8.3.1 Bias-Exchange Metadynamics

In all variants of metadynamics the free-energy landscape of the system is reconstructed by gradually filling the local minima with gaussian hills. The dimensionality of the landscape is equal to the number of CVs which are biased, and typically a number of CVs smaller than three is employed. The reason for this is that qualitatively, if the CVs are not correlated among them, the simulation time required to fill the free-energy landscape grows exponentially with the number of CVs. This limitation can be severe when studying complex transformations or reactions in which more than say three relevant CVs can be identified.

A possible technique to overcome this limitation is parallel-tempering metadynamics, Belfast tutorial: Replica exchange I. A different solution is performing a bias-exchange simulation: in this approach a relatively large number N of CVs is chosen to describe the possible transformations of the system (e.g., to study the conformations of a peptide one may consider all the dihedral angles between amino acids). Then, N metadynamics simulations (replicas) are run on the same system at the same temperature, biasing a different CV in each replica.

Normally, in these conditions, each bias profile would converge very slowly to the equilibrium free-energy, due to hysteresis. Instead, in the bias-exchange approach every fixed number of steps (say 10,000) an exchange is attempted between a randomly selected pair of replicas a and b. The probability to accept the exchange is given by a Metropolis rule:

$$\min (1, \exp \left[\beta (V_G^a(x^a, t) + V_G^b(x^b, t) - V_G^a(x^b, t) - V_G^b(x^a, t))\right])$$

where  $x^a$  and  $x^b$  are the coordinates of replicas a and b and  $V_G^{a(b)}\left(x,t\right)$  is the metadynamics potential acting on the replica a(b). Each trajectory evolves through the high dimensional free energy landscape in the space of the CVs sequentially biased by different metadynamics potentials acting on one CV at each time. The results of the simulation are N one-dimensional projections of the free energy.

In the following example, a bias-exchange simulation is performed on a VIL peptide (zwitterionic form, in vacuum with  $\epsilon=80$ , force field amber03), using the four backbone dihedral angles as CVs.

Four replicas of the system are employed, each one biased on a different CV, thus four similar Plumed input files are prepared as follows:

• a common input file in which all the collective variables are defined:

```
MOLINFO STRUCTURE=VIL.pdb RANDOM_EXCHANGES

cv1: TORSION ATOMS=@psi-1 cv2: TORSION ATOMS=@phi-2 cv3: TORSION ATOMS=@psi-2 cv4: TORSION ATOMS=@phi-3
```

## NOTE:

- 1. By using MOLINFO we can use shortcut to select atoms for dihedral angles (currently @phi, @psi, @omega and @chi1 are available).
- 2. We use cv# as labels in order to make the output compatible with METAGUI.
- 3. RANDOM EXCHANGES generates random exchanges list that are sent back to GROMACS.
- four additional input files that INCLUDE the common input and define the four METAD along the four CVs, respectively.

```
INCLUDE FILE=plumed-common.dat
be: METAD ARG=cv1 HEIGHT=0.2 SIGMA=0.2 PACE=100 GRID_MIN=-pi GRID_MAX=pi
PRINT ARG=cv1,cv2,cv3,cv4 STRIDE=1000 FILE=COLVAR
```

## NOTE:

- in COLVAR we PRINT only the four collective variables, always in the same order in such a way that COL

  VARs are compatible with METAGUI
- 2. if you want to print additional information, like the METAD bias it is possibile to use additional PRINT keyword

```
PRINT ARG=cv1, be.bias STRIDE=xxx FILE=BIAS
```

The four replicas start from the same GROMACS topology file replicated four times: topol0.tpr, topol1.tpr, topol2.tpr, topol3.tpr. Finally, GROMACS is launched as a parallel run on 4 cores, with one replica per core, with the command

```
mpirun -np 4 gmx_mpi mdrun -s topol -plumed plumed -multi 4 -replex 2000 >& log &
```

where -replex 2000 indicates that every 2000 molecular-dynamics steps all replicas are randomly paired (e.g. 0-2 and 1-3) and exchanges are attempted between each pair (as printed in the GROMACS \*.log files).

The same simulation can be run using WELLTEMPERED metadynamics.

## 12.8.3.2 Convergence of the Simulations

In the resources for this tutorial you can find the results for a 40ns long Well-Tempered Bias Exchange simulation. First of all we can try to assess the convergence of the simulations by looking at the profiles. In the "convergence" folder there is a script that calculates the free energy from the HILLS.0 file at incresing simulation lengths (i.e. every more 0.8 ns of simulation). The scripts also generate two measures of the evolution of the profiles in time:

- 1. time-diff.HILLS.0: where it is stored the average deviation between two successive profiles
- 2. KL.HILLS.0: where it is stored the average deviation between profiles correctly weigheted for the free energy of the profiles themselves (Symmetrized Kullback-Lieber divergence)

From both plots one can deduce that after 8 ns the profiles don't change significantly thus suggesting that averaging over the range 8-40ns should result in a accurate profile (we will test this using metagui). Another test is that of looking at the fluctuations of the profiles in a time window instead of looking at successive profiles:

### 12.8.3.3 Bias-Exchange Analysis with METAGUI

In principle Bias-Exchange Metadynamics can give as a results only N 1D free energy profiles. But the information contained in all the replicas can be used to recover multidensional free energy surfaces in >=N dimensions. A simple way to perform this analysis is to use METAGUI. METAGUI performs the following operations:

- 1. Clusterizes the trajectories on a multidimensional GRID defined by at least the biased coordinates.
- 2. By using the 1D free energy profiles and the clustering assigns a free energy to the cluster using a WHAM procedure.
- 3. Lets the user visualize the clusters.
- 4. Approximates the kinetics among clusters.

METAGUI (Biarnes et. al) is a plugin for VMD that implements the approch developed by Marinelli et. al 2009. It can be downloaded from the PLUMED website.

In order for the colvar and hills file to be compatible with METAGUI their header must be formatted as following:

### COLVAR.#:

```
#! FIELDS time cv1 cv2 cv3 cv4
#! ACTIVE 1 1 A
#! ..
...
```

## NOTE:

- 1. the COLVAR.# files should contain ALL the collective variables employed (all those biased in at least one replica plus those additionally analysed). They MUST be named cv1 ... cvN.
- the COLVAR.# files must be synchronised with the trajectories, this means that for each frame in the trajectory at time t there must be a line in each colvar at time t and viceversa. The best option is usually to analyse the trajectories a posteriori using plumed driver.

3. a keyword #! ACTIVE NBIASEDCV BIASEDCV LABEL is needed, where NBIASEDCV is the number of biased cv in that replica (not overall), BIASEDCV is the index of the biased cv in that replica (i.e. 1 for the first replica and so on); LABEL is a letter that identify the replica (usually is simply A for the first, B for the second and so on) this is usufull if two replicas are biasing the same collective variable:

```
COLVAR.0:
#! FIELDS time cv1 cv2 cv3
#! ACTIVE 1 1 A
#! ..
COLVAR.1:
#! FIELDS time cv1 cv2 cv3
#! ACTIVE 1 2 B
#! ..
COLVAR.2:
#! FIELDS time cv1 cv2 cv3
#! ACTIVE 1 2 C
#! ..
COLVAR.3:
#! FIELDS time cv1 cv2 cv3
#! ACTIVE 0
#! ..
```

In the above case Replica 0 biases cv1; replicas 1 and 2 biases cv2 while replica 3 is a neutral (unbiased) replica. cv3 is unbiased in all the replicas.

The ACTIVE keyword must be the FIRST LINE in the HILLS.# files:

## HILLS.#:

```
#! ACTIVE 1 1 A
#! FIELDS time cv1 sigma_cv1 height biasf
#! ..
...
```

The above notes hold for the HILLS files as well. In the folder metagui the script check\_for\_metagui.sh checks if the header of your file is compatible with METAGUI, but remember that this is not enough! Synchronisation of COLVAR and trajectory files is also needed. HILLS files can be written with a different frequency but times must be consistent.

NOTE: It is important to copy HILLS files in the metagui folder.

```
./check_for_metagui.sh ../COLVAR.0
```

will tell you that the ACTIVE keyword is missing, you need to modify all the header BEFORE proceeding with the tutorial!!

In the metagui folder there is a metagui.input file:

```
WHAM_EXE wham_bemeta.x
BASINS_EXE kinetic_basins.x
KT 2.4900
HILLS_FILE HILLS.0
HILLS_FILE HILLS.1
HILLS_FILE HILLS.2
HILLS_FILE HILLS.3
GRO_FILE VIL.pdb
COLVAR_FILE COLVAR.0 ../traj0.xtc "psi-1"
```

```
COLVAR_FILE COLVAR.1 ../traj1.xtc "phi-2"
COLVAR_FILE COLVAR.2 ../traj2.xtc "psi-2"
COLVAR_FILE COLVAR.3 ../traj3.xtc "phi-3"
TRAJ_SKIP 10
CVGRID 1 -3.1415 3.1415 15 PERIODIC
CVGRID 2 -3.1415 3.1415 15 PERIODIC
CVGRID 3 -3.1415 3.1415 15 PERIODIC
CVGRID 4 -3.1415 3.1415 15 PERIODIC
CVGRID 4 -3.1415 3.1415 15 PERIODIC
ACTIVE 4 1 2 3 4
T_CLUSTER 0.
T_FILL 8000.
DELTA 4
GCORR 1
TR_N_EXP 5
```

where are defined the temperature in energy units, the place where to find COLVAR, HILLS and trajectory files. A reference gro or pdb file is needed to load the trajectories. The definition of the ranges and the number of bins for the available collective variables.

Now let's start with the analysis:

- 1. run VMD and load metagui
- 2. in metagui load the metagui.input file belfast-8-mg1-fig
- 3. In the left section of the interface "load all" the trajectories
- 4. Find the Microstates

In order to visualise the microstate it is convenient to align all the structures using the VMD RMSD Trajectory tool that can be found in Extensions->Analysis.

One or more microstates can be visualised by selecting them and clicking show.

You can sort the microstates using the column name tabs, for example by clicking on size the microstates will be ordered from the larger to the smaller. If you look at the largest one it is possible to observe that by using the four selected collective variables the backbone conformation of the peptide is well defined while the sidechains can populate different rotameric states.

The equilibrium time in the analysis panel should be such that by averaging over the two halves of the remind of the simulation the profiles are the same (i.e the profile averaged between Teq and Teq+(Ttot-Teq)/2 should be the same of that averaged from Teq+(Ttot-Teq)/2 and Ttot). By clicking on COMPUTE FREE ENERGIES, the program will first generate the 1D free energy profiles from the HILLS files and then run the WHAM analysis on the microstates. Once the analysis is done it is possible to visually check the convergence of the 1D profiles one by one by clicking on the K bottons next to the HILLS.# files. The BLUE and the RED profiles are the two profiles just defined, while the GREEN is the average of the two. Now it is possible for example to sort the microstates as a function of the free energy and save them by dumping the structures for further analysis.

If you look in the metagui folder you will see a lot of files, some of them can be very usefull:

metagui/MICROSTATES: is the content of the microstates list table metagui/WHAM\_RUN/VG\_HILLS.#: are the opposite of the free energies calculated from the hills files metagui/WHAM\_RUN/\*.gnp: are gnuplot input files to plot the VG\_HILLS.# files (i.e. gnuplot -> load "convergence..") metagui/WHAM\_RUN/FES: is the result of the WHAM, for each cluster there is its free energy and the error estimate from WHAM

```
gnuplot> plot [0:40]'FES' u 2:3
```

plots the microstate error in the free energy estimate as a function of the microstates free energy. Finally in the folder metagui/FES there is script to integrate the multidimensional free energy contained in the MICROSTATES files to a 2D FES as a function of two of the used CV. To use it is enough to copy the MICROSTATES file in FES:

```
cp MICROSTATES FES/FES.4D
```

and edit the script to select the two columns of MICROSTATES on which show the integrated FES.

### 12.8.3.4 Multiple Walker Metadynamics

Multiple Walker metadynamics is the simplest way to parallelise a MetaD calculation: multiple simulation of the same system are run in parallel using metadynamics on the same set of collective variables. The deposited bias is shared among the replicas in such a way that the history dependent potential depends on the whole history.

We can use the same common input file defined above and then we can define four metadynamics bias in a similar way of what was done above for bias-exchange but now all the biases are defined on the same collective variables:

```
plumed.#.dat
INCLUDE FILE=plumed-common.dat

METAD ...
LABEL=mw
ARG=cv2,cv3
SIGMA=0.3,0.3
HEIGHT=0.2
PACE=100
BIASFACTOR=8
GRID_MIN=-pi,-pi
GRID_MAX=pi,pi
WALKERS_MPI
... METAD

PRINT ARG=cv1,cv2,cv3,cv4 STRIDE=1000 FILE=COLVAR
```

and the simulation can be run in a similar way without doing exchanges:

```
mpirun -np 4 gmx_mpi mdrun -s topol -plumed plumed -multi 4 >& log &
```

alternatively Multiple Walkers can be run as independent simulations sharing via the file system the biasing potential, this is usefull because it provides a parallelisation that does not need a parallel code. In this case the walkers read with a given frequency the gaussians deposited by the others and add them to their own METAD.

## 12.8.4 Reference

This tutorial is freely inspired to the work of Biarnes et al.

More materials can be found in

- 1. Marinelli, F., Pietrucci, F., Laio, A. & Piana, S. A kinetic model of trp-cage folding from multiple biased molecular dynamics simulations. PLoS Comput. Biol. 5, e1000452 (2009).
- 2. Biarnés, X., Pietrucci, F., Marinelli, F. & Laio, A. METAGUI. A VMD interface for analyzing metadynamics and molecular dynamics simulations. Comput. Phys. Commun. 183, 203–211 (2012).
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- 4. Granata, D., Camilloni, C., Vendruscolo, M. & Laio, A. Characterization of the free-energy landscapes of proteins by NMR-guided metadynamics. Proc. Natl. Acad. Sci. U.S.A. 110, 6817–6822 (2013).
- 5. Raiteri, P., Laio, A., Gervasio, F. L., Micheletti, C. & Parrinello, M. Efficient reconstruction of complex free energy landscapes by multiple walkers metadynamics. J. Phys. Chem. B 110, 3533–3539 (2006).

## 12.9 Belfast tutorial: NMR restraints

## 12.9.1 Aims

This tutorial is about the use of experimental data, in particular NMR data, either as collective variables or as replica-averaged restraints in MD simulations. While the first is a just a simple extension of what we have been already doing in previous tutorials, the latter is an approach that can be used to increase the quality of a force-field in describing the properties of a specific system.

### 12.9.1.1 Learning Outcomes

Once this tutorial is completed students will:

- · know why and how to use experimental data to define a collective variable
- · know why and how to use experimental data as replica-averaged restraints in MD simulations

### 12.9.2 Resources

The tarball for this project contains the following:

- system: the files use to generate the topol?.tpr files of the first and second example (the setup is for simulations in vacuum)
- first: an example on the use of chemical shifts as a collective variable
- · second: an example on the use of chemical shifts as replica-averaged restraints
- · third: an example on the use of RDCs (calculated with the theta-method) as replica-averaged restraints

## 12.9.3 Instructions

### 12.9.3.1 Experimental data as Collective Variables

In the former tutorials it has been often discussed the possibility of measuring a distance with respect to a structure representing some kind of state for a system, i.e. Belfast tutorial: Out of equilibrium dynamics. An alternative possibility is to use as a reference a set of experimental data that represent a state and measure the current deviation from the set. In plumed there are currently implemented the following NMR experimental observables: Chemical Shifts (only for proteins) CS2BACKBONE, NOE distances, JCOUPLING, PRE intensities, and Residual Dipolar couplings/pseudocontact shifts RDC.

In the following we will write the CS2BACKBONE collective variable similar to the one used in Granata et al. (2013) (while the collective variable is still proportional to the square sum of the deviation of the calculated and experimental chemical shifts divided by a typical error, the exact definition is not the same. The sum is not done anymore with a flat bottom difference and the error used are not the one published, so the exact result of the scoring function can be different).

As a general rule, when using CS2BACKBONE or other experimental restraints it is better to increase the accuracy of the constraint algorithm due to the increased strain on the bonded structure. In the case of GROMACS it is safer to use lincs-iter=2 and lincs-order=6.

```
prot: GROUP ATOMS=1-862
cs: CS2BACKBONE ATOMS=prot DATA=data NRES=56 CAMSHIFT
PRINT ARG=cs FILE=COLVAR STRIDE=100
ENDPLUMED
```

In this case the chemical shifts are those measured for the native state of the protein and can be used, together with other CVs and Bias-Exchange Metadynamics, to guide the system back and forth from the native structure. The experimental chemical shifts are in six files inside the "data/" folder (see first example in the resources tarball), one file for each nucleus. A 0 chemical shift is used where a chemical shift doesn't exist (i.e. CB of GLY) or where it has not been assigned. Additionally the data folder contains:

- camshift.db: this file is a parameter file for camshift, it is a standard file needed to calculate the chemical shifts from a structure
- template.pdb: this is a pdb file for the protein we are simulating (i.e. editconf -f conf.gro -o template.pdb) where atoms are ordered in the same way in which are included in the main code and again it is used to map the atom in plumed with those in almost.

This example can be executed as

```
gmx_mpi mdrun -s topol -plumed plumed
```

## 12.9.3.2 Replica-Averaged Restrained Simulations

NMR data, as all the equilibrium experimental data, are the result of a measure over an ensemble of structures and over time. In principle a "perfect" molecular dynamics simulations, that is a simulations with a perfect force-field and a perfect sampling can predict the outcome of an experiments in a quantitative way. Actually in most of the cases obtaining a qualitative agreement is already a fortunate outcome. In order to increase the accuracy of a force field in a system dependent manner it is possible to add to the force-field an additional term based on the agreement with a set of experimental data. This agreement is not enforced as a simple restraint because this would mean to ask the system to be always in agreement with all the experimental data at the same time, instead the restraint is applied over an AVERAGED COLLECTIVE VARIABLE where the average is performed over multiple independent simulations of the same system in the same conditions. In this way the is not a single replica that must be in agreement with the experimental data but they should be in agreement on average. It has been shown that this approach is equivalent to solving the problem of finding a modified version of the force field that will reproduce the provided set of experimental data withouth any additional assumption on the data themselves.

The second example included in the resources show how the amber force field can be improved in the case of protein domain GB3 using the native state chemical shifts a replica-averaged restraint. By the fact that replica-averaging needs the use of multiple replica simulated in parallel in the same conditions it is easily complemented with BIAS-EXCHANGE or MULTIPLE WALKER metadynamics to enhance the sampling.

```
prot: GROUP ATOMS=1-862
cs: CS2BACKBONE ATOMS=prot DATA=data NRES=56
enscs: ENSEMBLE ARG=(cs\.hn_.*),(cs\.nh_.*),(cs\.ca_.*),(cs\.cb_.*),(cs\.co_.*),(cs\.ha_.*)
stcs: STATS ARG=enscs.* SQDEVSUM PARARG=(cs\.exphn_.*),(cs\.expnh_.*),(cs\.expca_.*),(cs\.expcb_.*),(cs\.expcd_res: RESTRAINT ARG=stcs.sqdevsum AT=0. KAPPA=0. SLOPE=12

PRINT ARG=(cs\.hn_.*),(cs\.nh_.*),(cs\.ca_.*),(cs\.cb_.*),(cs\.co_.*),(cs\.ha_.*) FILE=CS STRIDE=1000
PRINT ARG=res.bias FILE=COLVAR STRIDE=10
```

ENDPLUMED

with respect to the case in which chemical shifts are used to define a standard collective variable, in this case CS2BACKBONE is a collective variable with multiple components, that are all the backcalculated chemical shifts, plus all the relative experimental values. The keyword function ENSEMBLE tells plumed to calculate the average of the arguments over the replicas (i.e. 4 replicas) and the function STATS compare the averaged back calculated chemical shifts with the experimental values and calculates the sum of the squared deviation. On this latter number it is possible to apply a linear RESTRAINT (because the variable is already a sum of squared differences) that is the new term we are adding to the underlying force field.

This example can be executed as

```
mpiexec -np 4 gmx_mpi mdrun -s topol -plumed plumed -multi 4
```

The third example show how RDC (calculated with the theta-methods) can be employed in the same way, in this case to describe the native state of Ubiquitin. In particular it is possible to observe how the RDC averaged restraint applied on the correlation between the calculated and experimental N-H RDCs result in the increase of the correlation of the RDCs for other bonds already on a very short time scale.

```
RDC ...
GYROM=-72.5388
SCALE=0.001060
ADDCOUPLINGS
LABEL=nh
ATOMS1=20,21 COUPLING1=8.17
ATOMS2=37,38 COUPLING2=-8.271
ATOMS3=56,57 COUPLING3=-10.489
ATOMS4=76,77 COUPLING4=-9.871
#continue...
```

In this input the first four N-H RDCs are defined.

This example can be executed as

```
mpiexec -np 8 gmx_mpi mdrun -s topol -plumed plumed -multi 8
```

## 12.9.4 Reference

- Granata, D., Camilloni, C., Vendruscolo, M. & Laio, A. Characterization of the free-energy landscapes of proteins by NMR-guided metadynamics. Proc. Natl. Acad. Sci. U.S.A. 110, 6817–6822 (2013).
- Cavalli, A., Camilloni, C. & Vendruscolo, M. Molecular dynamics simulations with replica-averaged structural restraints generate structural ensembles according to the maximum entropy principle. J. Chem. Phys. 138, 094112 (2013).
- 3. Camilloni, C., Cavalli, A. & Vendruscolo, M. Replica-Averaged Metadynamics. JCTC 9, 5610-5617 (2013).
- 4. Roux, B. & Weare, J. On the statistical equivalence of restrained-ensemble simulations with the maximum entropy method. J. Chem. Phys. 138, 084107 (2013).
- 5. Boomsma, W., Lindorff-Larsen, K. & Ferkinghoff-Borg, J. Combining Experiments and Simulations Using the Maximum Entropy Principle. PLoS Comput. Biol. 10, e1003406 (2014).
- 6. Camilloni, C. & Vendruscolo M. A Tensor-Free Method for the Structural and Dynamical Refinement of Proteins using Residual Dipolar Couplings. J. PHYS. CHEM. B 119, 653 (2015).

## 12.10 Belfast tutorial: Steinhardt Parameters

#### 12.10.1 Aims

This tutorial is concerned with the collective variables that we use to study order/disorder transitions such as the transition between the solid and liquid phase. In this tutorial we will look at the transition from solid to liquid as this is easier to study using simulation. The CVs we will introduce can, and have, been used to study the transition from liquid to solid. More information can be found in the further reading section.

You will need to ensure that you have compiled PLUMED with the crystalisation module enabled in order to complete this tutorial. To learn how to activate this module consult the information in the manual about the List of modules.

## 12.10.1.1 Learning Outcomes

Once this tutorial is completed students will:

- Know of the existence of the Steinhardt Parameters and know how to create plumed input files for calculating them.
- Appreciate that the Steinhardt Parameter for a particular atom is a vector quantity and that you can thus
  measure local order in a material by taking dot products of the Steinhardt Parameter vectors of adjacent
  atoms. Students will know how to calculate such quantities using plumed.

## 12.10.2 Resources

The tarball for this project contains the following files:

- in : An input file for the simplemd code that forms part of plumed
- input.xyz : A configuration file for Lennard-Jones solid with an fcc solid structure

## 12.10.3 Instructions

### 12.10.3.1 Simplemd

For this tutorial we will be using the MD code that is part of plumed - simplemd. This code allows us to do the simulations of Lennard-Jones that we require here but not much else. We will thus start this tutorial by doing some simulations with this code. You should have two files from the tarball, the first is called input.xyz and is basically an xyz file containing the posisitions of the atoms. The second meanwhile is called in and is the input to simplemd. If you open the file the contents should look something like this:

```
inputfile input.xyz
outputfile output.xyz
temperature 0.2
tstep 0.005
friction 1
forcecutoff 2.5
listcutoff 3.0
nstep 50000
nconfig 100 trajectory.xyz
nstat 10 energies.dat
```

Having run some molecular dynamics simulations in the past it should be pretty obvious what each line of the file does. One thing that might be a little strange is the units. Simplemd works with Lennard-Jones units so energy is in units of  $\epsilon$  and length is in units of  $\sigma$ . This means that temperature is in units of  $\frac{k_BT}{\epsilon}$ , which is why the temperature in the above file is apparently so low.

Use simplemd to run 50000 step calculations at 0.2, 0.8 and 1.2  $\frac{k_BT}{\epsilon}$ . (N.B. You will need an empty file called plumed.dat in order to run these calculations.) Visualise the trajectory output by each of your simulations using V $\leftarrow$  MD. Please be aware that simplemd does not wrap the atoms into the cell box automatically. If you are at the tutorial we have resolved this problem by making it so that if you press w when you load all the atoms they will be wrapped into the box. At what temperatures did the simulations melt? What then is the melting point of the Lennard-Jones potential at this density?

#### 12.10.3.2 Coordination Numbers

At the end of the previous section you were able to make very sophisticated judgements about whether or not the arrangment of atoms in your system was solid-like or liquid-like by simply looking at the configuration. The aim in the rest of this tutorial is to see if we can derive collective variables that are able to make an equally sophisticated judgement. For our first attempt lets use a CV which we have encountered elsewhere, the COORDINATIONNU MBER. Rerun the calculations from the previous section but at variance with the previous section use the plumed input file below instead of a empty file. This input will ensure that the average COORDINATIONNUMBER of the atoms in your system is computed and printed.

```
cc: COORDINATIONNUMBER SPECIES=1-108 SWITCH={RATIONAL D_0=1.3 R_0=0.2 D_MAX=3.0} MEAN PRINT ARG=cc.* FILE=colvar STRIDE=100
```

Rerun the simpled simulations described at the end of the previous section. Is the average coordination number good at differentiaing between solid and liquid configurations? Given your knowledge of physics/chemistry is this result surprising?

## 12.10.3.3 Steinhard parameter

The solid and liquid phases of a material are both relatively dense so the result at the end of the last section - the fact that the coordination number is not particularly good at differentiating between them - should not be that much of a surprise. As you will have learnt early on in your scientific education when solids melt the atoms rearrange themselves in a much less ordered fashion. The bonds between them do not necessarily break it is just that, whereas in a the solid the bonds were all at pretty well defined angles to each other, in a liquid the spread of bond angles is considerably larger. To detect the transition from solid to liquid what we need then is a coordinate that is able to recognise whether or not the geometry in the coordination spheres around each of the atoms in the system are the same or different. If these geometries are the same the system is in a solid-like configuration, whereas if they are different the system is liquid-like. The Steinhardt parameters Q3, Q4 and Q6 are coordinates that allow us to examine the coordination spheres of atoms in precisely this way. The way in which these coordinates are able to do this is explained in the video .

Repeat the calculations from the end of the previous section but using the plumed.dat file below.

```
cc: COORDINATIONNUMBER SPECIES=1-108 SWITCH={RATIONAL D_0=1.3 R_0=0.2 D_MAX=3.0} MEAN q6: Q6 SPECIES=1-108 SWITCH={RATIONAL D_0=1.3 R_0=0.2 D_MAX=3.0} MEAN PRINT ARG=cc.*,q6.* FILE=colvar STRIDE=100
```

This will output the average Q6 parameter and the average COORDINATIONNUMBER. In the Steinhardt parameter implementation in plumed the set of atoms in the coordination sphere of a particular atom are defined using a continuous switching function. Is the average Q6 parameter able to differentiate between the solid and liquid states?

#### 12.10.3.4 Local versus Global

At the end of the previous section you showed that the average Q6 parameter for a system of atoms is able to tell you whether or not that collection of atoms is in a solid-like or liquid-like configuration. In this section we will now ask the question - can the Steinhardt parameter always, unambiously tell us whether particular tagged atoms are in a solid-like region of the material or whether they are in a liquid-like region of the material? This is an important question that might come up if we are looking at nucleation of a solid from the melt. Our question in this context reads - how do we unambigously identify those atoms that are in the crystalline nucleus? A similar question would also come up when studying an interface between the solid and liquid phases. In this guise we would be asking about the extent of interface; namely, how far from the interface do we have to go before we can start thinking of the atoms as just another atom in the solid/liquid phase?

With these questions in mind our aim is to look at the distribution of values for the Q6 parameters of atoms in our system of Lennard-Jones have. If Q6 is able to unambigously tell us whether or not an atom is in a solid-like pose or a liquid-like pose then there should be no overlap in the distributions obtained for the solid and liquid phases. If there is overlap, however, then we cannot use these coordinates for the applications described in the previous paragraph. To calculate these distributions you will need to run two simulations - one at 0.2  $\frac{k_BT}{\epsilon}$  and one at 1.2  $\frac{k_Bt}{\epsilon}$  using now the following PLUMED input file:

```
q6: Q6 SPECIES=1-108 SWITCH={RATIONAL D_0=1.3 R_0=0.2 D_MAX=3.0} hh: HISTOGRAM DATA=q6 GRID_MIN=0 GRID_MAX=1.0 GRID_BIN=100 BANDWIDTH=0.05 STRIDE=100 DUMPGRID GRID=hh FILE=histo STRIDE=50000
```

Do the distributions of Q6 parameters in the solid and liquid phase overlap?

## 12.10.3.5 Local Steinhardt parameters

Hopefully you saw that the distribution of Q6 parameters for the solid and liquid phase overlap at the end of the previous section. Again this is not so surprising - as you go from solid to liquid the distribution of the geometries of the coordination spheres widens. The system is now able to arrange the atoms in the coordination spheres in a much wider variety of different poses. Importantly, however, the fact that an atom is in a liquid does not preclude it from having a very-ordered, solid-like coordination environment. As such in the liquid state we will find the occasional atom with a high value for the Q6 parameter. Consequently, an ordred coordination environment does not always differentiate solid-like atoms from liquid-like atoms. The major difference is in the liquid the ordered atoms will always be isolated. That is to say in the liquid atoms with an ordered coordination will always be surrounded by atoms with a disordered coordination sphere. By contrast in the solid each ordered atom will be surrounded by further ordered atoms. This observation forms the basis of the local Steinhardt parameters and the locally averaged Steinhardt parameters that are explained in this video .

Lets use plumed to calculate the distribution of LOCAL\_Q6 parameters in the solid and liquid phases. We can do this using the input file shown below:

```
q6: Q6 SPECIES=1-108 SWITCH={RATIONAL D_0=1.3 R_0=0.2 D_MAX=3.0} lq6: LOCAL_Q6 SPECIES=q6 SWITCH={RATIONAL D_0=1.3 R_0=0.2 D_MAX=3.0} hh: HISTOGRAM DATA=lq6 GRID_MIN=0 GRID_MAX=1.5 GRID_BIN=150 BANDWIDTH=0.05 STRIDE=10 DUMPGRID GRID=hh FILE=histo STRIDE=50000
```

Do the distributions of LOCAL Q6 parameter for the solid and liquid phases overlap?

Lectner and Dellago have designed an alternative to the LOCAL\_Q6 parameter that is based on taking the LOC← AL\_AVERAGE of the Q6 parameter arround a central atom. This quantity can be calcualted using plumed. If you have time try to use the manual to work out how.

## 12.10.4 Further Reading

There is a substantial literature on simulation of nucleation. Some papers are listed below but this list is far from exhaustive.

- F. Trudu, D. Donadio and M. Parrinello Freezing of a Lennard-Jones Fluid: From Nucleation to Spinodal Regime, Phys. Rev. Lett. 97 105701 (2006)
- D. Quigley and P. M. Rodger A metadynamics-based approach to sampling crystallization events , Mol. Simul. 2009
- W. Lechner and C. Dellago Accurate determination of crystal structures based on averaged local bond order parameters J. Chem. Phys 129 114707 (2008)
- B. Cheng, G. A. Tribello and M. Ceriotti Solid-liquid interfacial free energy out of equilibrium

## 12.11 Cambridge tutorial

**Authors** 

Max Bonomi and Carlo Camilloni, part of the tutorial is based on other tutorials.

Date

March 4, 2015

This document describes the PLUMED tutorial held for the Computational Biology MPhil, University of Cambridge, March 2015. The aim of this tutorial is to learn how to use PLUMED to run well-tempered and bias-exchange simulations and how to run replica-averaged metadynamics to incorporate experimental data into your simulation. Although the presented input files are correct, the users are invited to refer to the literature to understand how the parameters of enhanced sampling methods should be chosen in a real application.

Users are also encouraged to follow the links to the full PLUMED reference documentation and to wander around in the manual to discover the many available features and to do the other, more complete, tutorials. Here we are going to present only a very narrow selection of methods.

Users are expected to write PLUMED input files based on the instructions below.

## 12.11.1 Alanine dipeptide: our toy model

In this tutorial we will play with alanine dipeptide (see Fig. cambridge-1-ala-fig). This rather simple molecule is useful to make many benchmark that are around for data analysis and free energy methods. It is a rather nice example since it presents two metastable states separated by a high (free) energy barrier. Here metastable states are intended as states which have a relatively low free energy compared to adjacent conformation. It is conventional use to show the two states in terms of Ramachandran dihedral angles, which are denoted with  $\Phi$  and  $\Psi$  in Fig. cambridge-1-transition-fig .

## 12.11.2 Exercise 1. Metadynamics

## 12.11.2.1 Resources

The tarball for this project contains all the files needed to run this exercise.

### 12.11.2.2 Summary of theory

In metadynamics, an external history-dependent bias potential is constructed in the space of a few selected degrees of freedom  $\vec{s}(q)$ , generally called collective variables (CVs) ?. This potential is built as a sum of Gaussians deposited along the trajectory in the CVs space:

$$V(\vec{s},t) = \sum_{k\tau < t} W(k\tau) \exp\left(-\sum_{i=1}^{d} \frac{(s_i - s_i(q(k\tau)))^2}{2\sigma_i^2}\right).$$

where  $\tau$  is the Gaussian deposition stride,  $\sigma_i$  the width of the Gaussian for the ith CV, and  $W(k\tau)$  the height of the Gaussian. The effect of the metadynamics bias potential is to push the system away from local minima into visiting new regions of the phase space. Furthermore, in the long time limit, the bias potential converges to minus the free energy as a function of the CVs:

$$V(\vec{s}, t \to \infty) = -F(\vec{s}) + C.$$

In standard metadynamics, Gaussians of constant height are added for the entire course of a simulation. As a result, the system is eventually pushed to explore high free-energy regions and the estimate of the free energy calculated from the bias potential oscillates around the real value. In well-tempered metadynamics ?, the height of the Gaussian is decreased with simulation time according to:

$$W(k\tau) = W_0 \exp\left(-\frac{V(\vec{s}(q(k\tau)), k\tau)}{k_B \Delta T}\right),$$

where  $W_0$  is an initial Gaussian height,  $\Delta T$  an input parameter with the dimension of a temperature, and  $k_B$  the Boltzmann constant. With this rescaling of the Gaussian height, the bias potential smoothly converges in the long time limit, but it does not fully compensate the underlying free energy:

$$V(\vec{s}, t \to \infty) = -\frac{\Delta T}{T + \Delta T} F(\vec{s}) + C.$$

where T is the temperature of the system. In the long time limit, the CVs thus sample an ensemble at a temperature  $T+\Delta T$  which is higher than the system temperature T. The parameter  $\Delta T$  can be chosen to regulate the extent of free-energy exploration:  $\Delta T=0$  corresponds to standard molecular dynamics,  $\Delta T\to\infty$  to standard metadynamics. In well-tempered metadynamics literature and in PLUMED, you will often encounter the term "biasfactor" which is the ratio between the temperature of the CVs (  $T+\Delta T$ ) and the system temperature ( T):

$$\gamma = \frac{T + \Delta T}{T}.$$

The biasfactor should thus be carefully chosen in order for the relevant free-energy barriers to be crossed efficiently in the time scale of the simulation.

Additional information can be found in the several review papers on metadynamics???

### 12.11.2.3 Setup, run, and analyse a well-tempered metadynamics simulation

In this exercise, we will run a well-tempered metadynamics simulation on alanine dipeptide in vacuum, using as CVs the two backbone dihedral angles phi and psi.

In order to run this simulation we need to prepare the PLUMED input file (plumed.dat) as follows.

```
# set up two variables for Phi and Psi dihedral angles
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
#
# Activate metadynamics in phi and psi
# depositing a Gaussian every 500 time steps,
# with height equal to 1.2 kJoule/mol,
# and width 0.35 rad for both CVs.
# Well-tempered metadynamics is activated,
# and the biasfactor is set to 6.0
#
metad: METAD ARG=phi,psi PACE=500 HEIGHT=1.2 SIGMA=0.35,0.35 FILE=HILLS BIASFACTOR=6.0
# monitor the two variables and the metadynamics bias potential
PRINT STRIDE=10 ARG=phi,psi,metad.bias FILE=COLVAR
```

```
(see TORSION, METAD, and PRINT).
```

The syntax for the command METAD is simple. The directive is followed by a keyword ARG followed by the labels of the CVs on which the metadynamics potential will act. The keyword PACE determines the stride of Gaussian deposition in number of time steps, while the keyword HEIGHT specifies the height of the Gaussian in kJoule/mol. To run well-tempered metadynamics, we need two additional keywords BIASFACTOR and TEMP, which specify how fast the bias potential is decreasing with time and the temperature of the simulation, respectively. For each CVs, one has to specify the width of the Gaussian by using the keyword SIGMA. Gaussian will be written to the file indicated by the keyword FILE.

Once the PLUMED input file is prepared, one has to run Gromacs with the option to activate PLUMED and read the input file:

```
gmx_mpi mdrun -plumed
```

During the metadynamics simulation, PLUMED will create two files, named COLVAR and HILLS. The COLVAR file contains all the information specified by the PRINT command, in this case the value of the CVs every 10 steps of simulation, along with the current value of the metadynamics bias potential. The HILLS file contains a list of the Gaussians deposited along the simulation. If we give a look at the header of this file, we can find relevant information about its content. The last column contains the value of the biasfactor used, while the last but one the height of the Gaussian, which is rescaled during the simulation following the well-tempered recipe.

```
#! FIELDS time phi psi sigma_phi sigma_psi height biasf
#! SET multivariate false
#! SET min_phi -pi
#! SET max_phi pi
#! SET min_psi -pi
#! SET max_psi pi
             -1.3100
                                                                    1.4400
     1.0000
                          0.0525
                                          0.35
                                                          0.35
                                                                                6
     2.0000
               -1.4054 1.9742
                                          0.35
                                                          0.35
                                                                    1.4400
                                                                                6
     3.0000
               -1.9997
                         2.5177
                                          0.35
                                                          0.35
                                                                   1.4302
                                                                                6
     4.0000
                -2.2256
                          2.1929
                                                          0.35
                                                                    1.3622
                                                                                6
```

If we carefully look at the height column, we will notice that in the beginning the value reported is higher than the initial height specified in the input file, which should be 1.2 kJoule/mol. In fact, this column reports the height of the Gaussian rescaled by the pre-factor that in well-tempered metadynamics relates the bias potential to the free energy. In this way, when we will use <a href="mailto:sum\_hills">sum\_hills</a>, the sum of the Gaussians deposited will directly provide the free-energy, without further rescaling needed.

We can plot the time evolution of the CVs along with the height of the Gaussian.

The system is initialized in one of the local minimum where it starts accumulating bias. As the simulation progresses and the bias added grows, the Gaussian height is progressively reduced. After a while (t=0.8 ns), the system is able to escape the local minimum and explore a new region of the phase space. As soon as this happens, the Gaussian height is restored to the initial value and starts to decrease again. In the long time, the Gaussian height becomes smaller and smaller while the system diffuses in the entire CVs space.

### 12.11.2.4 Calculate free-energies and monitor convergence

One can estimate the free energy as a function of the metadynamics CVs directly from the metadynamics bias potential. In order to do so, the utility sum\_hills should be used to sum the Gaussians deposited during the simulation and stored in the HILLS file.

To calculate the two-dimensional free energy as a function of phi and psi, it is sufficient to use the following command line:

```
plumed sum_hills --hills HILLS
```

The command above generates a file called fes.dat in which the free-energy surface as function of phi and psi is calculated on a regular grid. One can modify the default name for the free energy file, as well as the boundaries and bin size of the grid, by using the following options of sum\_hills:

```
--outfile - specify the outputfile for sumhills
--min - the lower bounds for the grid
--max - the upper bounds for the grid
--bin - the number of bins for the grid
--spacing - grid spacing, alternative to the number of bins
```

It is also possible to calculate one-dimensional free energies from the two-dimensional metadynamics simulation. For example, if one is interested in the free energy as a function of the phi dihedral alone, the following command line should be used:

```
plumed sum_hills --hills HILLS --idw phi --kt 2.5
```

The result should look like this:

To assess the convergence of a metadynamics simulation, one can calculate the estimate of the free energy as a function of simulation time. At convergence, the reconstructed profiles should be similar. The option –stride should be used to give an estimate of the free energy every N Gaussians deposited, and the option –mintozero can be used to align the profiles by setting the global minimum to zero. If we use the following command line:

```
plumed sum_hills --hills HILLS --idw phi --kt 2.5 --stride 500 --mintozero
```

one free energy is calculated every 500 Gaussians deposited, and the global minimum is set to zero in all profiles. Try to visualize the different estimates of the free energy as a function of time.

To assess the convergence of the simulation more quantitatively, we can calculate the free-energy difference between the two local minima in the one-dimensional free energy along phi as a function of simulation time. We can use the bash script analyze\_FES.sh to integrate the multiple free-energy profiles in the two basins defined by the following intervals in phi space: basin A, -3<phi<-1, basin B, 0.5<phi<1.5.

```
./analyze_FES.sh NFES -3.0 -1.0 0.5 1.5 KBT
```

where NFES is the number of profiles (free-energy estimates at different times of the simulation) generated by the option –stride of sum\_hills, and KBT is the temperature in energy units (in this case KBT=2.5).

This analysis, along with the observation of the diffusive behavior in the CVs space, suggest that the simulation is converged.

## 12.11.3 Exercise 2. Bias-Exchange Metadynamics

## 12.11.3.1 Resources

The tarball for this project contains all the files needed to run this exercise.

## 12.11.3.2 Summary of theory

In well-tempered metadynamics the free-energy landscape of the system is reconstructed by gradually filling the local minima with gaussian hills. The dimensionality of the landscape is equal to the number of CVs which are biased, and typically a number of CVs smaller than four is employed. The reason for this is that qualitatively, if the CVs are not correlated among them, the simulation time required to fill the free-energy landscape grows exponentially with the number of CVs. This limitation can be severe when studying complex transformations or reactions in which more than say three relevant CVs can be identified.

Alternative solutions employ metadynamics together with other enhanced sampling techniques (i.e. Parallel Tempering or more generally Hamiltionan Replica Exchange). In particular in Bias-Exchange metadynamics the problem of sampling a multi-dimensional free-energy surface is recast in that of sampling many one-dimensional free-energies. In this approach a relatively large number N of CVs is chosen to describe the possible transformations of the system (e.g., to study the conformations of a peptide one may consider all the dihedral angles between amino acids). Then, N metadynamics simulations (replicas) are run on the same system at the same temperature, biasing a different CV in each replica. Normally, in these conditions, each bias profile would converge very slowly to the equilibrium free-energy, due to hysteresis.

In order to tackle this problem, in the bias-exchange approach every fixed number of steps (say 10,000) an exchange is attempted between a randomly selected pair of replicas a and b. The exchanges allow the replicas to gain from the sampling of the other replicas and enable the system to explore the conformational space along a large number of different directions.

The probability to accept the exchange is given by a Metropolis rule:

$$\min (1, \exp \left[\beta (V_G^a(x^a, t) + V_G^b(x^b, t) - V_G^a(x^b, t) - V_G^b(x^a, t))\right])$$

where  $x^a$  and  $x^b$  are the coordinates of replicas a and b and  $V_G^{a(b)}\left(x,t\right)$  is the metadynamics potential acting on the replica a(b). Each trajectory evolves through the high dimensional free energy landscape in the space of the CVs sequentially biased by different metadynamics potentials acting on one CV at each time. The results of the simulation are N one-dimensional projections of the free energy.

12.11.3.3 Setup, run, and analyse a well-tempered bias-exchange metadynamics simulation

In the following example, a bias-exchange simulation is performed on Alanine di-peptide. A typical input file for BE-WTMetaD is the following:

• a common input file in which all the collective variables are defined:

```
plumed-common.dat:
# read a pdb file to get topology info
MOLINFO STRUCTURE=ALAD.pdb

# tell PLUMED to generate random exchange trials
RANDOM_EXCHANGES

# set up four variables for Phi, Psi, Theta, Xi dihedral angles
phi: TORSION ATOMS=@phi-2
psi: TORSION ATOMS=@psi-2
theta: TORSION ATOMS=6,5,7,9
xi: TORSION ATOMS=16,15,17,19

PRINT ARG=phi,psi,theta,xi STRIDE=250 FILE=COLVAR
```

## (see MOLINFO and RANDOM EXCHANGES).

• additional input files that INCLUDE the common input and define the METAD along the selected CVs:

```
plumed.dat.0:

INCLUDE FILE=plumed-common.dat
METAD ARG=phi HEIGHT=1.2 SIGMA=0.25 PACE=100 GRID_MIN=-pi GRID_MAX=pi BIASFACTOR=10.0
ENDPLUMED

plumed.dat.1:

INCLUDE FILE=plumed-common.dat
METAD ARG=psi HEIGHT=1.2 SIGMA=0.25 PACE=100 GRID_MIN=-pi GRID_MAX=pi BIASFACTOR=10.0
ENDPLUMED

plumed.dat.2:

INCLUDE FILE=plumed-common.dat
METAD ARG=theta HEIGHT=1.2 SIGMA=0.50 PACE=100 GRID_MIN=-pi GRID_MAX=pi BIASFACTOR=10.0
ENDPLUMED

plumed.dat.3:

INCLUDE FILE=plumed-common.dat
METAD ARG=xi HEIGHT=1.2 SIGMA=0.50 PACE=100 GRID_MIN=-pi GRID_MAX=pi BIASFACTOR=10.0
ENDPLUMED
```

The, in this case, two replicas start from the same GROMACS topology file replicated twice: topol0.tpr, topol1.tpr, topol2.tpr and topol3.tpr. Finally, GROMACS is launched as a parallel run on 4 cores, with one replica per core, with the command

```
mpirun -np 4 gmx_mpi mdrun -s topol -plumed plumed -multi 4 -replex 10000 >& log &
```

where -replex 10000 indicates that every 10000 molecular-dynamics steps exchanges are attempted (as printed in the GROMACS \*.log files).

In order to have an idea of how Bias-Exchange Metadynamics works we can compare the sampling of the four replicas along the first two collective variables with respect to a free energy surface obtained by sampling in two dimensions.

The main features are that all the replicas can sample all the relevant free energy minima even if their collective variable is not meant to sample them, only the replicas with a collective variable meant to pass a barrier can sample that transition, so high energy regions are sampled only locally. This can seem a weakness in the case of alanine dipeptide but is the real strength of BE-MetaD, indeed by not knowing anything of a system it is possible to choose as many collective variables as possible and even if most of them are not particularly usefull a posteriori, they all gain from the good ones and nothing is lost.

### 12.11.3.4 Calculate free-energies and monitor convergence

As for the former case, one can estimate the free energy as a function of the metadynamics CVs directly from the metadynamics bias potential. This approach can only be used to recover one-dimensional free-energy profiles:

```
plumed sum_hills --hills HILLS.0 --mintozero
```

The command above generates a file called fes.dat in which the free-energy surface as function of phi is calculated on a regular grid.

It is also possible to calculate one-dimensional free energies from the two-dimensional metadynamics simulation. For example, if one is interested in the free energy as a function of the phi dihedral alone, the following command line should be used:

The result should look like this (compared with the one obtained before):

As above we can assess the convergence of a metadynamics simulation by calculating the estimate of the free energy as a function of simulation time. At convergence, the reconstructed profiles should be similar. The option –stride should be used to give an estimate of the free energy every N Gaussians deposited, and the option – mintozero can be used to align the profiles by setting the global minimum to zero. If we use the following command line:

```
plumed sum_hills --hills HILLS.0 --stride 500 --mintozero
```

Try to visualize the different estimates of the free energy as a function of time.

To assess the convergence of the simulation more quantitatively, we can calculate the free-energy difference between the two local minima in the one-dimensional free energy along phi as a function of simulation time. We can use the bash script analyze\_FES.sh to integrate the multiple free-energy profiles in the two basins defined by the following intervals in phi space: basin A, -3<phi<-1, basin B, 0.5<phi<1.5.

```
./analyze_FES.sh NFES -3.0 -1.0 0.5 1.5 KBT
```

where NFES is the number of profiles (free-energy estimates at different times of the simulation) generated by the option –stride of sum\_hills, and KBT is the temperature in energy units (in this case KBT=2.5).

In addition to check for the convergence of the one dimesional profiles, it is important to verify the rate of exchange among the replicas. In fact if the rate is too low or if it is not enough homegenues then the replicas can still suffer from histeris problems (ie with one replica trapped somewhere in the conformational space). Generally speaking a good probability of exchange is between 10 and 30%.

It is possible to check the exchange statistics and the detailed diffusion of the replicas among the different biases using a script provided:

```
./demux_m.pl md0.log
```

which will create two files, called replica\_temp.xvg and replica\_index.xvg. We can plot the first file, which reports the bias index of each configuration at a given time of the simulation. This file is extremely useful, because it allows us monitoring the replicas diffusion in bias.

## 12.11.4 Exercise 3. Replica-Average Metadynamics

#### 12.11.4.1 Resources

The tarball for this project contains all the files needed to run this exercise.

## 12.11.4.2 Summary of theory

Equilibrium experimental data are the result of a measure over an ensemble of structures and over time. In principle a "perfect" molecular dynamics simulations, that is a simulations with a perfect force-field and a perfect sampling can predict the outcome of an experiment in a quantitative way. Actually in most of the cases obtaining a qualitative agreement is already a fortunate outcome. In order to increase the accuracy of a force field in a system dependent manner it is possible to add to the force-field an additional term based on the agreement with a set of experimental data. This agreement is not enforced as a simple restraint because this would mean to ask the system to be always in agreement with all the experimental data at the same time, instead the restraint is applied over an AVERAGED COLLECTIVE VARIABLE where the average is performed over multiple identical simulations (replicas). In this way there is not a single replica that must be in agreement with the experimental data but they should be in agreement on average. It has been shown that this approach is equivalent to solve the problem of finding a modified version of the force field that reproduces the provided set of experimental data without any additional assumption on the data themselves ? ? ? ?

### 12.11.4.3 The system: Chignolin

In this exercise we will model the equilibrium ensemble of Chignolin by combining an implicit solvent force-field (Amber99sb) with synthetic experimental data derived from an experimentally determined ensemble of structures.

The experimental data are the following distances among CA carbons that have been averaged over the whole ensemble.

```
#RES RES DISTANCE (nm)
         0.656214
         0.963703
1
     5
         1.197160
         1.219970
1
         1.206760
1
     8
         1.060110
1
     9
         0.858911
   1.0
1
         0.872988
2
         0.656913
2
         0.931405
2
     6
         0.953046
         0.901493
2
     8
         0.809623
2
     9
         0.716444
   10
         0.882070
3
     5
         0.588322
3
         0.660023
3
         0.704165
3
     8
         0.720063
3
         0.799961
3
   10
         0.981838
4
     6
         0.550374
4
         0.572299
     8
         0.764540
4
4
     9
         0.939752
4
    10
         1.186040
5
         0.613088
         0.847734
5
         1.084080
5
    10
         1.296630
         0.591571
6
     9
         0.888388
   10
         1.102920
         0.701717
7
   10
         0.987368
8
   10
         0.654310
```

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## 12.11.4.4 Setup, run and analysis

Here we will give partial information on how to setup the simulations. Users should refer to the manual and the literature cited on how to complete the information provided and thus successfully perform the exercise.

Step 1: Add the collective variables that describe the distances averaged over the ensemble to the template input files provided.

For each of the above experimental data one should define:

```
\#this is the distance between CA atoms 5 and 33 belonging to residues 1 and 3, respectively. d1: DISTANCE ATOMS=5,33 \# this is the averaging of the distance among the replicas ed1: ENSEMBLE ARG=d1 \# this is the restraint applied on the averaged distance to match the experimental one RESTRAINT ARG=ed1.d1 KAPPA=100000 AT=0.656214
```

### (see DISTANCE, ENSEMBLE, and RESTRAINT).

## Step 2: Setup the Bias-Exchange simulations

We will run Bias-Exchange simulations using four CVs, two of them have already been chosen (see plumed-common.dat) while the others should be selected by you. Additionally Metadynamics parameters METAD for the two selected cvs should be added in the plumed.dat.0 and plumed.dat.1 files. In particular while the PACE, HEIGHT and BIASFACTOR can be kept the same of those defined for the preselected CVs, the SIGMA should be half of the fluctuations of the chosen CV in an unbiased run (>1 ns).

#### Step 3: Run

The simulation should be run until convergence of the four monodimensional free energies, this will tipically take more than 200 ns per replica.

### Step 4: Analysis

The user should check the diffusion of the replicas among the biases (see above) and send the converged free energy profiles.

### Step 5: Only for the brave!

The same simulation without experimental restraints could be performed in such a way to compare the free energy profiles obtained with and without the inclusion of experimental data.

## 12.12 Cineca tutorial

## **Authors**

Max Bonomi, stealing most of the material from other tutorials. Alejandro Gil Ley is acknowledged for betatesting this tutorial.

## Date

November 20, 2015

This document describes the PLUMED tutorial held at CINECA, November 2015. The aim of this tutorial is to learn how to use PLUMED to analyze molecular dynamics (MD) simulations on-the-fly, to analyze existing trajectories, and to perform enhanced sampling. Although the presented input files are correct, the users are invited to **refer to the literature to understand how the parameters of enhanced sampling methods should be chosen in a real application.** 

Users are also encouraged to follow the links to the full PLUMED reference documentation and to wander around in the manual to discover the many available features and to do the other, more complete, tutorials. Here we are going to present only a very narrow selection of methods.

All the tests here are performed on a toy system, alanine dipeptide, simulated in vacuum using the AMBER99SB force field. Simulations are carried out with GROMACS 5.0.4, which is here assumed to be already patched with PLUMED 2.2 and properly installed. However, these examples could be easily converted to other MD software.

### 12.12.1 Resources

All the GROMACS input files and analysis scripts are provided in this tarball. Users are expected to write PLUMED input files based on the instructions below.

We can start by downloading the tarball and uncompressing it:

```
> tar xzvf cineca.tar.gz
```

#### Warning

Exercises should be run inside the newly-created cineca directory, by creating new subdirectories, one per exercise

### 12.12.2 Alanine dipeptide: our toy model

In this tutorial we will play with alanine dipeptide (see Fig. cineca-1-ala-fig). This rather simple molecule is useful to benchmark data analysis and free-energy methods. This system is a nice example because it presents two metastable states separated by a high free-energy barrier. It is conventional use to characterize the two states in terms of Ramachandran dihedral angles, which are denoted with  $\Phi$  and  $\Psi$  in Fig. cineca-1-transition-fig.

## 12.12.3 Monitoring collective variables

The main goal of PLUMED is to compute collective variables, which are complex descriptors of a system than can be used to analyze a conformational change or a chemical reaction. This can be done either on-the-fly, that is during MD, or a posteriori, using PLUMED as a post-processing tool. In both cases one should create an input file with a specific PLUMED syntax. A sample input file is below:

```
# compute distance between atoms 1 and 10
d: DISTANCE ATOMS=1,10
# create a virtual atom in the center between atoms 20 and 30
center: CENTER ATOMS=20,30
# compute torsional angle between atoms 1,10,20 and center
phi: TORSION ATOMS=1,10,20,center
# print d and phi every 10 step
PRINT ARG=d,phi STRIDE=10
```

## (see DISTANCE, CENTER, TORSION, and PRINT)

PLUMED works using kJ/nm/ps as energy/length/time units. This can be personalized using UNITS. Notice that variables should be given a name (in the example above, d, and phi), which is then used to refer to these variables. Lists of atoms should be provided as comma separated numbers, with no space. Virtual atoms can be created and assigned a name for later use. You can find more information on the PLUMED syntax at Getting started page of the manual. The complete documentation for all the supported collective variables can be found at the Collective variables page.

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## 12.12.3.1 Exercise 1: on-the-fly analysis

Here we will run a plain MD simulation on alanine dipeptide and compute two torsional angles on-the-fly. GRO← MACS needs a .tpr file, which is a binary file containing initial positions as well as force-field parameters. For this tutorial, it is sufficient to use the .tpr files provided in the SETUP directory of the package:

- · topolA.tpr setup in vacuum, initialized in state A
- · topolB.tpr setup in vacuum, initialized in state B

However, we also provide .gro, .mdp, and .top files, that can be modified and used to generate a new .tpr file.

GROMACS can be run (interactively) using the following command:

```
> gmx_mpi mdrun -s ../SETUP/topolA.tpr -nsteps 10000 -x traj.xtc
```

The nsteps flags can be used to change the number of timesteps and topolA.tpr is the name of the tpr file. While running, GROMACS will produce a md.log file, with log information, and a traj.xtc file, with a binary trajectory. The trajectory can be visualized with VMD using:

```
> vmd confout.gro traj.xtc
```

To activate PLUMED during a GROMACS MD simulation, you need to add the -plumed flag

```
> gmx_mpi mdrun -s ../SETUP/topolA.tpr -nsteps 10000 -plumed plumed.dat -x traj.xtc
```

Here plumed.dat is the name of the PLUMED input file. Notice that PLUMED will write information in the md.log that could be useful to verify if the simulation has been set up properly.

In this exercise, we will run a plain MD simulation and monitor the  $\Phi$  and  $\Psi$  dihedral angles on-the-fly. In order to do so, you need to prepare the following PLUMED input file:

```
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
PRINT ARG=phi,psi STRIDE=100 FILE=COLVAR
```

## (see TORSION and PRINT)

PLUMED is going to compute the collective variables only when necessary, that is, in this case, every 100 steps. This is not very relevant for simple variables such as torsional angles, but provides a significant speed-up when using expensive collective variables.

PLUMED will write a textual file named COLVAR containing three columns: simulation time,  $\Phi$  and  $\Psi$ . Results can be plotted using gnuplot:

```
> gnuplot
# this shows phi as a function of time
gnuplot> plot "COLVAR" u 2
# this shows psi as a function of time
gnuplot> plot "COLVAR" u 3
# this shows psi as a function of phi
gnuplot> plot "COLVAR" u 2:3
```

Now try to do the same using the two different initial configurations that we provided (topolA.tpr and topol $\leftarrow$ B.tpr). Results from 200ps (100000 steps) trajectories in vacuum are shown in Figure cineca-ala-traj.

Notice that the result depends heavily on the starting structure. For the simulation in vacuum, the two free-energy minima are separated by a large barrier so that the system cannot cross it in such short simulation time. Also notice that the two clouds are well separated, indicating that these two collective variables are appropriate to properly distinguish the two minima.

As a final comment, consider that if you run twice the same calculation in the same directory, you might overwrite the output files. GROMACS takes automatic backup of these files, and PLUMED does it as well. In case you are restarting a simulation, you can add the keyword RESTART at the beginning of the PLUMED input file. This will tell PLUMED to *append* files instead of taking a backup copy.

## 12.12.3.2 Exercise 2: analysis with the driver tool

Imagine you have already run a simulation, with or without PLUMED. You might want to compute the collective variables a posteriori, i.e. from the trajectory file. You can do this by using the PLUMED executable on the command line. Type

```
> plumed driver --help
```

to have an idea of the possible options. See driver for the full documentation.

Here we will use the driver the compute  $\Phi$  and  $\Psi$  on the trajectory previously generated. Let's assume the trajectory is named traj.xtc. You should prepare a PLUMED input file named analysis.dat as:

```
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
PRINT ARG=phi,psi FILE=COLVAR_ANALYSIS
```

(see TORSION and PRINT) Notice that typically when using the driver we do not provide a STRIDE keyword to PRINT. This implies "print at every step" which, analyzing a trajectory, means "print for all the available snapshots". Then, you can use the following command:

```
> plumed driver --mf_xtc traj.xtc --plumed analysis.dat
```

Notice that PLUMED has no way to now the value of physical time from the trajectory. If you want physical time to be printed in the output file you should give more information to the driver, e.g.:

```
> plumed driver --mf_xtc traj.xtc --plumed analysis.dat --timestep 0.002 --trajectory-stride 1000
```

(see driver)

In this case we inform the driver that the traj.xtc file was produced in a run with a timestep of 0.002 ps and saving a snapshop every 1000 timesteps.

You might want to analyze a different collective variable, such as the gyration radius. The gyration radius tells how extended is a molecule in space. You can do it with the following PLUMED input file

```
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17

heavy: GROUP ATOMS=1,5,6,7,9,11,15,16,17,19
gyr: GYRATION ATOMS=heavy

# the same could have been achieved with
# gyr: GYRATION ATOMS=1,5,6,7,9,11,15,16,17,19

PRINT ARG=phi,psi,gyr FILE=analyze
```

(see TORSION, GYRATION, GROUP, and PRINT)

Now try to compute the time serie of the gyration radius.

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## 12.12.4 Biasing collective variables

We have seen that PLUMED can be used to compute collective variables. However, PLUMED is most often use to add forces on the collective variables. To this aim, we have implemented a variety of possible biases acting on collective variables. A bias works in a manner conceptually similar to the PRINT command, taking as argument one or more collective variables. However, here the STRIDE is usually omitted (that is equivalent to setting it to 1), which means that forces are applied at every timestep. Starting from PLUMED 2.2 you can change the STRIDE also for bias potentials, but that's another story. In the following we will see how to build an adaptive bias potential with metadynamics and how to apply harmonic restraints. The complete documentation for all the biasing methods available in PLUMED can be found at the Bias page.

### 12.12.4.1 Metadynamics

### 12.12.4.1.1 Summary of theory

In metadynamics, an external history-dependent bias potential is constructed in the space of a few selected degrees of freedom  $\vec{s}(q)$ , generally called collective variables (CVs) **?**. This potential is built as a sum of Gaussians deposited along the trajectory in the CVs space:

$$V(\vec{s},t) = \sum_{k\tau < t} W(k\tau) \exp\left(-\sum_{i=1}^{d} \frac{(s_i - s_i(q(k\tau)))^2}{2\sigma_i^2}\right).$$

where  $\tau$  is the Gaussian deposition stride,  $\sigma_i$  the width of the Gaussian for the ith CV, and  $W(k\tau)$  the height of the Gaussian. The effect of the metadynamics bias potential is to push the system away from local minima into visiting new regions of the phase space. Furthermore, in the long time limit, the bias potential converges to minus the free energy as a function of the CVs:

$$V(\vec{s}, t \to \infty) = -F(\vec{s}) + C.$$

In standard metadynamics, Gaussians of constant height are added for the entire course of a simulation. As a result, the system is eventually pushed to explore high free-energy regions and the estimate of the free energy calculated from the bias potential oscillates around the real value. In well-tempered metadynamics ?, the height of the Gaussian is decreased with simulation time according to:

$$W(k\tau) = W_0 \exp\left(-\frac{V(\vec{s}(q(k\tau)), k\tau)}{k_B \Delta T}\right),$$

where  $W_0$  is an initial Gaussian height,  $\Delta T$  an input parameter with the dimension of a temperature, and  $k_B$  the Boltzmann constant. With this rescaling of the Gaussian height, the bias potential smoothly converges in the long time limit, but it does not fully compensate the underlying free energy:

$$V(\vec{s}, t \to \infty) = -\frac{\Delta T}{T + \Delta T} F(\vec{s}) + C.$$

where T is the temperature of the system. In the long time limit, the CVs thus sample an ensemble at a temperature  $T+\Delta T$  which is higher than the system temperature T. The parameter  $\Delta T$  can be chosen to regulate the extent of free-energy exploration:  $\Delta T=0$  corresponds to standard MD,  $\Delta T\to\infty$  to standard metadynamics. In well-tempered metadynamics literature and in PLUMED, you will often encounter the term "biasfactor" which is the ratio between the temperature of the CVs (  $T+\Delta T$ ) and the system temperature ( T):

$$\gamma = \frac{T + \Delta T}{T}.$$

The biasfactor should thus be carefully chosen in order for the relevant free-energy barriers to be crossed efficiently in the time scale of the simulation.

Additional information can be found in the several review papers on metadynamics???

If you do not know exactly where you would like your collective variables to go, and just know (or suspect) that some variables have large free-energy barriers that hinder some conformational rearrangement or some chemical reaction, you can bias them using metadynamics. In this way, a time dependent, adaptive potential will be constructed that tends to disfavor visited configurations in the collective-variable space. The bias is usually built as a sum of Gaussian deposited in the already visited states.

### 12.12.4.1.2 Exercise 3

In this exercise, we will run a well-tempered metadynamics simulation on alanine dipeptide in vacuum, using as CV the backbone dihedral angle phi. In order to run this simulation we need to prepare the PLUMED input file (plumed.dat) as follows.

```
# set up two variables for Phi and Psi dihedral angles
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
# Activate well-tempered metadynamics in phi depositing
# a Gaussian every 500 time steps, with initial height equal
# to 1.2 kJoule/mol, biasfactor equal to 10.0, and width to 0.35 rad
METAD ...
LABEL=metad
ARG=phi
PACE=500
HEIGHT=1.2
SIGMA=0.35
FILE=HILLS
BIASFACTOR=10.0
TEMP=300.0
GRID_MIN=-pi
GRID_MAX=pi
GRID_SPACING=0.1
... METAD
# monitor the two variables and the metadynamics bias potential
PRINT STRIDE=10 ARG=phi, psi, metad.bias FILE=COLVAR
```

## (see TORSION, METAD, and PRINT).

The syntax for the command METAD is simple. The directive is followed by a keyword ARG followed by the labels of the CVs on which the metadynamics potential will act. The keyword PACE determines the stride of Gaussian deposition in number of time steps, while the keyword HEIGHT specifies the height of the Gaussian in kJoule/mol. For each CVs, one has to specified the width of the Gaussian by using the keyword SIGMA. Gaussian will be written to the file indicated by the keyword FILE.

The bias potential will be stored on a grid, whose boundaries are specified by the keywords GRID\_MIN and GR ← ID\_MAX. Notice that you should provide either the number of bins for every collective variable (GRID\_BIN) or the desired grid spacing (GRID\_SPACING). In case you provide both PLUMED will use the most conservative choice (highest number of bins) for each dimension. In case you do not provide any information about bin size (neither GRID\_BIN nor GRID\_SPACING) and if Gaussian width is fixed PLUMED will use 1/5 of the Gaussian width as grid spacing. This default choice should be reasonable for most applications.

Once the PLUMED input file is prepared, one has to run GROMACS with the option to activate PLUMED and read the input file:

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```
gmx_mpi mdrun -s ../SETUP/topolA.tpr -plumed plumed.dat -nsteps 5000000 -x traj.xtc
```

During the metadynamics simulation, PLUMED will create two files, named COLVAR and HILLS. The COLVAR file contains all the information specified by the PRINT command, in this case the value of the CVs every 10 steps of simulation, along with the current value of the metadynamics bias potential. We can use COLVAR to visualize the behavior of the CV during the simulation:

By inspecting Figure cineca-metad-phi-fig, we can see that the system is initialized in one of the two metastable states of alanine dipeptide. After a while (t=0.1 ns), the system is pushed by the metadynamics bias potential to visit the other local minimum. As the simulation continues, the bias potential fills the underlying free-energy landscape, and the system is able to diffuse in the entire phase space.

The HILLS file contains a list of the Gaussians deposited along the simulation. If we give a look at the header of this file, we can find relevant information about its content:

```
#! FIELDS time phi psi sigma_phi sigma_psi height biasf
#! SET multivariate false
#! SET min_phi -pi
#! SET max_phi pi
#! SET min_psi -pi
#! SET max_psi pi
```

The line starting with FIELDS tells us what is displayed in the various columns of the HILLS file: the time of the simulation, the value of phi and psi, the width of the Gaussian in phi and psi, the height of the Gaussian, and the biasfactor. We can use the HILLS file to visualize the decrease of the Gaussian height during the simulation, according to the well-tempered recipe:

If we look carefully at the scale of the y-axis, we will notice that in the beginning the value of the Gaussian height is higher than the initial height specified in the input file, which should be 1.2 kJoule/mol. In fact, this column reports the height of the Gaussian rescaled by the pre-factor that in well-tempered metadynamics relates the bias potential to the free energy. In this way, when we will use <a href="mailto:sum\_hills">sum\_hills</a>, the sum of the Gaussians deposited will directly provide the free-energy, without further rescaling needed (see below).

One can estimate the free energy as a function of the metadynamics CVs directly from the metadynamics bias potential. In order to do so, the utility sum\_hills should be used to sum the Gaussians deposited during the simulation and stored in the HILLS file. To calculate the free energy as a function of phi, it is sufficient to use the following command line:

```
plumed sum hills --hills HILLS
```

The command above generates a file called fes.dat in which the free-energy surface as function of phi is calculated on a regular grid. One can modify the default name for the free energy file, as well as the boundaries and bin size of the grid, by using the following options of sum\_hills:

```
--outfile - specify the outputfile for sumhills
--min - the lower bounds for the grid
--max - the upper bounds for the grid
--bin - the number of bins for the grid
--spacing - grid spacing, alternative to the number of bins
```

The result should look like this:

To assess the convergence of a metadynamics simulation, one can calculate the estimate of the free energy as a function of simulation time. At convergence, the reconstructed profiles should be similar. The option –stride should be used to give an estimate of the free energy every N Gaussians deposited, and the option –mintozero can be used to align the profiles by setting the global minimum to zero. If we use the following command line:

```
plumed sum_hills --hills HILLS --stride 100 --mintozero
```

one free energy is calculated every 100 Gaussians deposited, and the global minimum is set to zero in all profiles. The resulting plot should look like the following:

To assess the convergence of the simulation more quantitatively, we can calculate the free-energy difference between the two local minima of the free energy along phi as a function of simulation time. We can use following script to integrate the multiple free-energy profiles in the two basins defined by the following regions in phi space: basin A, -3<phi<-1, basin B, 0.5<phi<1.5.

```
# number of free-energy profiles
 nfes= # put here the number of profiles
  # minimum of basin A
minA=-3
  # maximum of basin A
maxA=1
  # minimum of basin B
minB=0.5
  # maximum of basin B
maxB=1.5
  # temperature in energy units
 kbt=2.5
  for((i=0;i<nfes;i++))
  do
        # calculate free-energy of basin A
       A = `wk' BEGIN\{tot=0.0\}\{if(\$1!="\#!" \&\& \$1>min \&\& \$1<max\}tot+=exp(-\$2/kbt)\}END\{print -kbt*log(tot)\}' min=\$\{minB(tot)\}' 
          # and basin B
       B=\text{`awk 'BEGIN\{tot=0.0\}\{if(\$1!="\#!" \&\& \$1>min \&\& \$1<max)\}tot+=exp(-\$2/kbt)\}END\{print -kbt*log(tot)\}' min=\$\{minB(tot)\} = (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0) + (10.0)
          # calculate difference
        Delta=$(echo "${A} - ${B}" | bc -1)
          # print it
          echo $i $Delta
  done
```

Please notice that nfes should be set to the number of profiles (free-energy estimates at different times of the simulation) generated by the option –stride of sum hills.

This analysis, along with the observation of the diffusive behavior in the CVs space, suggest that the simulation is converged.

## 12.12.4.1.3 Exercise 4

In this exercise, we will run a well-tempered metadynamics simulation on alanine dipeptide in vacuum, using as CV the backbone dihedral angle psi. In order to run this simulation we need to prepare the PLUMED input file (plumed.dat) as follows.

```
# set up two variables for Phi and Psi dihedral angles
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
#
# Activate well-tempered metadynamics in psi depositing
# a Gaussian every 500 time steps, with initial height equal
# to 1.2 kJoule/mol, biasfactor equal to 10.0, and width to 0.35 rad

METAD ...
LABEL=metad
ARG=psi
PACE=500
HEIGHT=1.2
SIGMA=0.35
FILE=HILLS
BIASFACTOR=10.0
```

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```
TEMP=300.0

GRID_MIN=-pi

GRID_MAX=pi

GRID_SPACING=0.1
... METAD

# monitor the two variables and the metadynamics bias potential
PRINT STRIDE=10 ARG=phi,psi,metad.bias FILE=COLVAR
```

(see TORSION, METAD, and PRINT).

Once the PLUMED input file is prepared, one has to run GROMACS with the option to activate PLUMED and read the input file. We will submit this job using the PBS queue system, as done for the previous exercise.

As we did in the previous exercise, we can use COLVAR to visualize the behavior of the CV during the simulation. Here we will plot at the same time the evolution of the metadynamics CV psi and of the other dihedral phi:

By inspecting Figure cineca-metad-psi-phi-fig, we notice that something different happened compared to the previous exercise. At first the behavior of psi looks diffusive in the entire CV space. However, around t=1 ns, psi seems trapped in a region of the CV space in which it was previously diffusing without problems. The reason is that the non-biased CV phi after a while has jumped into a different local minima. Since phi is not directly biased, one has to wait for this (slow) degree of freedom to equilibrate before the free energy along psi can converge. Try to repeat the analysis done in the previous exercise (calculate the estimate of the free energy as a function of time and monitor the free-energy difference between basins) to assess the convergence of this metadynamics simulation.

12.12.4.2 Restraints

12.12.4.2.1 Biased sampling theory

A system at temperature T samples conformations from the canonical ensemble:

$$P(q) \propto e^{-\frac{U(q)}{k_B T}}$$

. Here q are the microscopic coordinates and  $k_B$  is the Boltzmann constant. Since q is a highly dimensional vector, it is often convenient to analyze it in terms of a few collective variables (see Belfast tutorial: Analyzing CVs , Belfast tutorial: Adaptive variables I , and Belfast tutorial: Adaptive variables II ). The probability distribution for a CV s is

$$P(s) \propto \int dq e^{-\frac{U(q)}{k_B T}} \delta(s - s(q))$$

This probability can be expressed in energy units as a free energy landscape F(s):

$$F(s) = -k_B T \log P(s)$$

.

Now we would like to modify the potential by adding a term that depends on the CV only. That is, instead of using U(q), we use U(q) + V(s(q)). There are several reasons why one would like to introduce this potential. One is to avoid that the system samples some un-desired portion of the conformational space. As an example, imagine that you want to study dissociation of a complex of two molecules. If you perform a very long simulation you will be able to see association and dissociation. However, the typical time required for association will depend on the size of the simulation box. It could be thus convenient to limit the exploration to conformations where the distance between the two molecules is lower than a given threshold. This could be done by adding a bias potential on the distance between the two molecules. Another example is the simulation of a portion of a large molecule taken out from its initial context. The fragment alone could be unstable, and one might want to add additional potentials to keep the fragment in place. This could be done by adding a bias potential on some measure of the distance from the experimental structure (e.g. on root-mean-square deviation).

Whatever CV we decide to bias, it is very important to recognize which is the effect of this bias and, if necessary, remove it a posteriori. The biased distribution of the CV will be

$$P'(s) \propto \int dq e^{-\frac{U(q)+V(s(q))}{k_B T}} \delta(s-s(q)) \propto e^{-\frac{V(s(q))}{k_B T}} P(s)$$

and the biased free energy landscape

$$F'(s) = -k_B T \log P'(s) = F(s) + V(s) + C$$

Thus, the effect of a bias potential on the free energy is additive. Also notice the presence of an undetermined constant C. This constant is irrelevant for what concerns free-energy differences and barriers, but will be important later when we will learn the weighted-histogram method. Obviously the last equation can be inverted so as to obtain the original, unbiased free-energy landscape from the biased one just subtracting the bias potential

$$F(s) = F'(s) - V(s) + C$$

Additionally, one might be interested in recovering the distribution of an arbitrary observable. E.g., one could add a bias on the distance between two molecules and be willing to compute the unbiased distribution of some torsional angle. In this case there is no straightforward relationship that can be used, and one has to go back to the relationship between the microscopic probabilities:

$$P(q) \propto P'(q)e^{\frac{V(s(q))}{k_BT}}$$

The consequence of this expression is that one can obtained any kind of unbiased information from a biased simulation just by weighting every sampled conformation with a weight

$$w \propto e^{\frac{V(s(q))}{k_B T}}$$

That is, frames that have been explored in spite of a high (disfavoring) bias potential V will be counted more than frames that has been explored with a less disfavoring bias potential.

#### 12.12.4.2.2 Umbrella sampling theory

Often in interesting cases the free-energy landscape has several local minima. If these minima have free-energy differences that are on the order of a few times  $k_BT$  they might all be relevant. However, if they are separated by a high saddle point in the free-energy landscape (i.e. a low probability region) than the transition between one and the other will take a lot of time and these minima will correspond to metastable states. The transition between one minimum and the other could require a time scale which is out of reach for MD. In these situations, one could take inspiration from catalysis and try to favor in a controlled manner the conformations corresponding to the transition state.

Imagine that you know since the beginning the shape of the free-energy landscape F(s) as a function of one CV s. If you perform a MD simulation using a bias potential which is exactly equal to -F(s), the biased free-energy landscape will be flat and barrierless. This potential acts as an "umbrella" that helps you to safely cross the transition state in spite of its high free energy.

It is however difficult to have an a priori guess of the free-energy landscape. We will see later how adaptive techniques such as metadynamics (Belfast tutorial: Metadynamics) can be used to this aim. Because of this reason, umbrella sampling is often used in a slightly different manner.

Imagine that you do not know the exact height of the free-energy barrier but you have an idea of where the barrier is located. You could try to just favor the sampling of the transition state by adding a harmonic restraint on the CV, e.g. in the form

$$V(s) = \frac{k}{2}(s - s_0)^2$$

. The sampled distribution will be

$$P'(q) \propto P(q)e^{\frac{-k(s(q)-s_0)^2}{2k_BT}}$$

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For large values of k, only points close to  $s_0$  will be explored. It is thus clear how one can force the system to explore only a predefined region of the space adding such a restraint. By combining simulations performed with different values of  $s_0$ , one could obtain a continuous set of simulations going from one minimum to the other crossing the transition state. In the next section we will see how to combine the information from these simulations.

If you want to just bring a collective variables to a specific value, you can use a simple restraint. Let's imagine that we want to force the  $\Phi$  angle to visit a region close to  $\Phi=\pi/2$ . We can do it adding a restraint in  $\Phi$ , with the following input

```
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
res: RESTRAINT ARG=phi AT=0.5pi KAPPA=5
PRINT ARG=phi,psi,res.bias
```

(see TORSION, RESTRAINT, and PRINT).

Notice that here we are printing a quantity named res.bias. We do this because RESTRAINT does not define a single value (that here would be theoretically named res) but a structure with several components. All biasing methods (including METAD) do so, as well as many collective variables (see e.g. DISTANCE used with COMP ONENTS keyword). Printing the bias allows one to know how much a given snapshop was penalized. Also notice that PLUMED understands numbers in the form {number}pi. This is convenient when using torsions, since they are expressed in radians.

Now you can plot your trajectory with gnuplot and see the effect of KAPPA. You can also try different values of KAPPA. The stiffer the restraint, the less the collective variable will fluctuate. However, notice that a too large kappa could make the MD integrator unstable.

# 12.12.4.3 Using multiple replicas

#### Warning

Notice that multireplica simulations with PLUMED are fully supported with GROMACS, but only partly supported with other MD engines.

Some free-energy methods are intrinsically parallel and requires running several simultaneous simulations. This can be done with GROMACS using the multi replica framework. That is, if you have 4 tpr files named topol0.tpr, topol1.tpr, topol2.tpr, topol3.tpr you can run 4 simultaneous simulations.

```
> mpirun -np 4 gmx_mpi mdrun -s topol.tpr -plumed plumed.dat -multi 4 -nsteps 500000
```

Each of the 4 replicas will open a different topol file, and GROMACS will take care of adding the replica number before the .tpr suffix. PLUMED deals with the extra number in a slightly different way. In this case, for example, PLUMED first look for a file named plumed.X.dat, where X is the number of the replica. In case the file is not found, then PLUMED looks for plumed.dat. If also this is not found, PLUMED will complain. As a consequence, if all the replicas should use the same input file it is sufficient to put a single plumed.dat file, but one has also the flexibility of using separate files named plumed.0.dat, plumed.1.dat etc.

Also notice that providing the flag <code>-replex</code> one can instruct GROMACS to perform a replica exchange simulation. Namely, from time to time GROMACS will try to swap coordinates among neighboring replicas and accept of reject the exchange with a Monte Carlo procedure which also takes into account the bias potentials acting on the replicas, even if different bias potentials are used in different replicas. That is, PLUMED allows to easily implement many forms of Hamiltonian replica exchange.

#### 12.12.4.4 Using multiple restraints with replica exchange

# 12.12.4.4.1 Weighted histogram analysis method theory

Let's now consider multiple simulations performed with restraints located in different positions. In particular, we will consider the i-th bias potential as  $V_i$ . The probability to observe a given value of the collective variable s is:

$$P_i(s) = \frac{P(s)e^{-\frac{V_i(s)}{k_BT}}}{\int ds' P(s')e^{-\frac{V_i(s')}{k_BT}}} = \frac{P(s)e^{-\frac{V_i(s)}{k_BT}}}{Z_i}$$

where

$$Z_i = \sum_{q} e^{-(U(q) + V_i(q))}$$

The likelyhood for the observation of a sequence of snapshots  $q_i(t)$  (where i is the index of the trajectory and t is time) is just the product of the probability of each of the snapshots. We use here the minus-logarithm of the likelihood (so that the product is converted to a sum) that can be written as

$$\mathcal{L} = -\sum_{i} \int dt \log P_i(s_i(t)) = \sum_{i} \int dt \left( -\log P(s_i(t)) + \frac{V_i(s_i(t))}{k_B T} + \log Z_i \right)$$

One can then maximize the likelyhood by setting  $\frac{\delta \mathcal{L}}{\delta P(\mathbf{s})} = 0$ . After some boring algebra the following expression can be obtained

$$0 = \sum_{i} \int dt \left( -\frac{\delta_{\mathbf{s}_{i}(t),\mathbf{s}}}{P(\mathbf{s})} + \frac{e^{-\frac{V_{i}(\mathbf{s})}{k_{B}T}}}{Z_{i}} \right)$$

In this equation we aim at finding P(s). However, also the list of normalization factors  $Z_i$  is unknown, and they should be found selfconsistently. Thus one can find the solution as

$$P(\mathbf{s}) \propto \frac{N(\mathbf{s})}{\sum_{i} \int dt \frac{e^{-\frac{V_{i}(\mathbf{s})}{k_{B}T}}}{Z_{i}}}$$

where Z is selfconsistently determined as

$$Z_i \propto \int ds' P(\mathbf{s'}) e^{-\frac{V_i(\mathbf{s'})}{k_B T}}$$

These are the WHAM equations that are traditionally solved to derive the unbiased probability P(s) by the combination of multiple restrained simulations. To make a slightly more general implementation, one can compute the weights that should be assigned to each snapshot, that turn out to be:

$$w_i(t) \propto \frac{1}{\sum_j \int dt \frac{e^{-\beta V_j(\mathbf{s}_i(t))}}{Z_j}}$$

The normalization factors can in turn be found from the weights as

$$Z_i \propto \frac{\sum_j \int dt e^{-\beta V_i(\mathbf{s}_j(t))} w_j(t)}{\sum_j \int dt w_j(t)}$$

This allows to straighforwardly compute averages related to other, non-biased degrees of freedom, and it is thus a bit more flexible. It is sufficient to precompute this factors w and use them to weight every single frame in the trajectory.

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#### 12.12.4.4.2 Exercise 5

In this exercise we will run multiple restraint simulations and learn how to reweight and combine data with WHAM to obtain free-energy profiles. We start with running in a replica-exchange scheme 32 simulations with a restraint on phi in different positions, ranging from -3 to 3. We will instruct GROMACS to attempt an exchange between different simulations every 1000 steps.

First we need to create the 32 PLUMED input files and .tpr files, using the following script:

```
nrep=32
dx='echo "6.0 / ( $nrep - 1 )" | bc -1'
for((i=0;i<nrep;i++))
# center of the restraint
AT= 'echo "$i * $dx - 3.0" | bc -1'
cat >plumed.${i}.dat << EOF</pre>
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
# Impose an umbrella potential on phi
# with a spring constant of 200 kjoule/mol
# and centered in phi=AT
restraint-phi: RESTRAINT ARG=phi KAPPA=200.0 AT=$AT
# monitor the two variables and the bias potential
PRINT STRIDE=100 ARG=phi,psi,restraint-phi.bias FILE=COLVAR
# we initialize some replicas in A and some in B:
if((i%2==0)); then
  cp ../SETUP/topolA.tpr topol$i.tpr
  cp ../SETUP/topolB.tpr topol$i.tpr
fi
done
```

And then run GROMACS with the following command:

```
mpirun -np 32 gmx_mpi mdrun -plumed plumed.dat -s topol.tpr -multi 32 -replex 1000 -nsteps 500000 -x traj.xtc
```

To be able to combine data from all the simulations, it is necessary to have an overlap between statistics collected in two adjacent umbrellas. Have a look at the plots of (phi,psi) for the different simulations to understand what is happening. To visualize them all at once as in Fig. cineca-usrem-phi-all, you can prepare the following script:

```
awk 'BEGIN{print ""; ORS=""; print "p \"COLVAR.0\" u 2:3 notitle,"; for(i=1;i<=30;i++) print "\"COLVAR."i"\" u
```

and then open gnuplot and load it:

```
gnuplot> load "plot.plt"
```

An often misunderstood fact about WHAM is that data of the different trajectories can be mixed and it is not necessary to keep track of which restraint was used to produce every single frame. Let's get the concatenated trajectory

```
trjcat_mpi -cat -f traj*.xtc -o alltraj.xtc
```

Now we should compute the value of each of the bias potentials on the entire (concatenated) trajectory.

```
nrep=32
dx='echo "6.0 / ( $nrep - 1 )" | bc -1'

for i in 'seq 0 $(( $nrep - 1 ))' 
    do
    # center of the restraint
    AT='echo "$i * $dx - 3.0" | bc -1'

cat >plumed.dat << EOF
    phi: TORSION ATOMS=5,7,9,15
    psi: TORSION ATOMS=7,9,15,17
    restraint-phi: RESTRAINT ARG=phi KAPPA=200.0 AT=$AT

# monitor the two variables and the bias potential
PRINT STRIDE=100 ARG=phi,psi,restraint-phi.bias FILE=ALLCOLVAR.$i
EOF

plumed driver --mf_xtc alltraj.xtc --trajectory-stride=10 --plumed plumed.dat
done</pre>
```

It is very important that this script is consistent with the one used to generate the multiple simulations above. Now, single files named ALLCOLVAR.XX will contain on the fourth column the value of the bias centered in a given position, computed on the entire concatenated trajectory.

Next step is to compute the weights self-consistently solving the WHAM equations, using the python script "wham. ← py" contained in the SCRIPTS directory. We will run this script as follows:

```
bash ../SCRIPTS/wham.sh ALLCOLVAR.*
```

This script will produce several files. Let's visualize "phi\_fes.dat", which contains the free energy as a function of phi, and compare this with the result previously obtained with metadynamics.

# 12.12.4.4.3 Exercise 6

In the previous exercise, we use multiple restraint simulations to calculate the free energy as a function of the dihedral phi. The resulting free energy was in excellent agreement with our previous metadynamics simulation. In this exercise we will repeat the same procedure for the dihedral psi. At the end of the steps defined above, we can plot the free energy "psi\_fes.dat" and compare it with the profile calculated from a metadynamics simulations using both phi and psi as CVs.

We can easily spot from the plot above that something went wrong in this multiple restraint simulations, despite we used the very same approach we adopted for the phi dihedral. The problem here is that psi is a "bad" collective variable, and the system is not able to equilibrate the missing slow degree of freedom phi in the short time scale of the umbrella simulation (1 ns). In the metadynamics exercise in which we biased only psi, we detect problems by observing the behavior of the CV as a function of simulation time. How can we detect problems in multiple restraint simulations? This is slightly more complicated, but running this kind of simulation in a replica-exchange scheme offers a convenient way to detect problems.

The first thing we need to do is to demux the replica-exchange trajectories and reconstruct the continous trajectories of the replicas across the different restraint potentials. In order to do so, we can use the following script:

```
demux.pl md0.log
trjcat_mpi -f traj?.xtc traj??.xtc -demux replica_index.xvg
```

This commands will generate 32 continuous trajectories, named XX\_trajout.xtc. We will use the driver to calculate the value of the CVs phi and psi on these trajectories.

```
nrep=32

for i in 'seq 0 $(( $nrep - 1 )) '
do

cat >plumed.dat << EOF
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17

# monitor the two variables
PRINT STRIDE=100 ARG=phi,psi FILE=COLVARDEMUX.$i
EOF

plumed driver --mf_xtc ${i}_trajout.xtc --trajectory-stride=10 --plumed plumed.dat
done</pre>
```

The COLVARDEMUX.XX files will contain the value of the CVs on the demuxed trajectory. If we visualize these files (see previous exercise for instructions) we will notice that replicas sample the CVs space differently. In order for each umbrella to equilibrate the slow degrees of freedom phi, the continuous replicas must be ergodic and thus sample the same distribution in phi and psi.

# 12.13 Using Hamiltonian replica exchange with GROMACS

When patching GROMACS with PLUMED, it is also possible to perform Hamiltonian replica exchange with different topologies. Although this feature is provided together with PLUMED, it is actually a new feature for GROMACS itself that can be enabled using the -hrex flag of mdrun. This implementation is very close to the one used to produce the data in this paper? In case you find it useful, please cite this paper.

# Warning

This feature is currently used by several groups and should be robust enough. However, be sure that you understand its limitations and to perform all the tests discussed in this page before using it in production.

In this short tutorial you will learn how to do two things:

- Generate scaled topologies with plumed partial\_tempering. This is actually not directly related to the -hrex flag.
- · Run GROMACS with replica exchange and multiple topologies.

## 12.13.1 Generate scaled topologies

Plumed comes with a partial\_tempering command line tool that can be used to generate scaled topologies. Notice that you might want to generate these topologies by yourself. This step is totally independent from the use of the -hrex flag.

The partial\_tempering tool can be invoked as follows:

```
plumed partial_tempering scale < processed.top</pre>
```

where scale is the Hamiltonian scaling factor and processed.top is a post-processed topology file (i.e. produced with grompp -pp) where each "hot" atom has a  $"\_"$  appended to the atom type, e.g. change this

```
НС
                                                1
                                                       0.1123
                                                                     1.008
     1
                              ACE
                                     HH31
                                                                             ; qtot 0.1123
to this:
     1
                 HC_
                        1
                              ACE
                                     HH31
                                                       0.1123
                                                                    1.008
                                                                              ; qtot 0.1123
```

Notice that the section that should be edited is the [atoms] section for all the molecules that you wish to affect (typically only for the solute, but you may also want to change solvent parameters). If you select all the atoms of the solute, you will be able to prepare topologies such as those needed in a REST2 simulation?.

Also remember to first produce the processed.top file with grompp -pp. Editing a normal topol.top file will not work, because it does not contain all the parameters. The processed.top file should not have any "#include" statement.

```
# produce a processed topology
grompp -pp
# choose the "hot" atoms
vi processed.top
# generate the actual topology
plumed partial_tempering $scale < processed.top > topol$i.top
```

### Warnings:

- It's not very robust and there might be force-field dependent issues!
- It certainly does not work with charmm cmap

#### Suggested tests:

1. Compare partial\_tempering with scale=1.0 to non-scaled force field. E.g.

```
grompp -o topol-unscaled.tpr
grompp -pp
vi processed.top # choose the "hot" atoms appending "_". You can choose whatever.
plumed partial_tempering 1.0 < processed.top > topol-scaled.top # scale with factor 1
grompp -p topol-scaled.top -o topol-scaled.tpr
# Then do a rerun on a trajectory
mdrun -s topol-unscaled.tpr -rerun rerun.trr
mdrun -s topol-scaled.tpr -rerun rerun.trr
# and compare the resuling energy files. they should be identical
```

2. Compare partial\_tempering with scale=0.5 to non-scaled force field. Repeat the same procedure but using "plumed partial\_tempering 0.5". Choose all the atoms in all the relevant [atoms] sections (e.g. solute, solvent and ions). In the two resulting energy files you should see: long range electrostatics, LJ, and dihedral energy is half in the scaled case all other terms (bonds/bends) are identical.

#### 12.13.2 Run GROMACS

If GROMACS has been patched with PLUMED it should accept the -hrex option in mdrun. Please double check this (mdrun -h should list this possibility). Notice that not all the versions of GROMACS allow this feature. First of all prepare separate topologies for each replicas using plumed partial\_tempering tool as shown above (or using some other tool). Then run a normal replica exchange with gromacs adding the flag "-hrex" on the command line.

A complete run script could be adapted from the following

```
# five replicas
nrep=5
# "effective" temperature range
t.min=300
t.max = 1000
# build geometric progression
list=$(
awk -v n=$nrep \
    -v tmin=$tmin \
    -v tmax=$tmax \
  'BEGIN{for(i=0;i<n;i++){
    t=tmin*exp(i*log(tmax/tmin)/(n-1));
    printf(t); if(i < n-1)printf(",");
} ′
# clean directory
rm -fr \#*
rm -fr topol*
for((i=0;i<nrep;i++))
do
# choose lambda as T[0]/T[i]
# remember that high temperature is equivalent to low lambda
  lambda=$(echo $list | awk 'BEGIN{FS=",";}{print $1/$'$((i+1))';}')
# process topology
 (if you are curious, try "diff topol0.top topol1.top" to see the changes)
 plumed partial_tempering $lambda < processed.top > topol$i.top
# prepare tpr file
 -maxwarn is often needed because box could be charged
  grompp_mpi_d -maxwarn 1 -o topol$i.tpr -f grompp$i.mdp -p topol$i.top
done
mpirun -np $nrep gmx_mpi mdrun_d -v -plumed plumed.dat -multi $nrep -replex 100 -nsteps 15000000 -hrex
```

Notice that total cell could be charged. This happens whenever the scaled portion of the system is not neutral. There should be no problem in this. When used with pbc, GROMACS will add a compensating background.

#### Suggested check:

• Try with several identical force fields (hardcode the same lambda for all replicas in the script above) and different seed/starting point. Acceptance should be 1.0

Notice that when you run with GPUs acceptance could be different from 1.0. The reason is that to compute the acceptance GROMACS is sending the coordinates to the neighboring replicas which then recompute energy. If all the tpr files are identical, one would expect energy to be identically to the originally computed one. However, calculations made with GPUs are typically not reproducible to machine precision. For a large system, even an error in the total energy for the last significant digit could be on the order of a kJ. This results in practice in a lower acceptance. The error induced on the final ensemble is expected to be very small.

### Warnings:

- Topologies should have the same number of atoms, same masses and same constraint topology. Some of these differences (e.g. masses) are not explicitly checked and might lead to unnoticed errors in the final results.
- Choose neighbor list update (nstlist) that divides replex. Notice that running with GPUs GROMACS is going to change nstlist automatically, be sure that it still divides replex.
- Option -hrex requires also option -plumed. If you do not care about plumed, just provide an empty plumed.dat file.
- It should work correctly if replicas have different force-field, temperature, lambda, pressure, in any combination. However, not all these combinations have been tried in practice, so please first test the code on a system for which you know the result.

# 12.14 Julich tutorial: Developing CVs in plumed

#### 12.14.1 Aims

The aim of this tutorial is to introduce users to the tutorials in the developer manual of PLUMED. We will learn a little bit about the structure of the code and how this structure can be visualised using the tree diagrams in the developer manual. You will then learn how to implement a new collective variable in a way that uses as much of the functionality that is already within the code and that thus avoids the duplication of code. Finally, you will learn how to write regression tests and how these can be used for continuous integration.

### 12.14.2 Learning Outcomes

By the end of this session you will know how to:

- · access the developer manual for PLUMED.
- find the tutorial information for implementing new collective variables, multicolvars, functions, biases and analysis routines.
- find the tree diagrams showing the class structure in the PLUMED developer manual.
- exploit the functionality within PLMD::multicolvar in order to write a reasonably complex collective variable quickly.
- · write regression tests for PLUMED and understand how these are used for continuous integration.

To do this module you must understand the basics of object-oriented programming. Information on object oriented programming and how it is used within plumed can be found here.

### 12.14.3 Resources

The tarball for this project contains the following directories:

- · rt-coord: a directory containing input files for doing a regtest on an already existing collective variable.
- rt-second-shell: a directory containing input files for doing a regtest on the collective variable you will implement within this tutorial

At the start of the exercise you should move these two directories to the plumed2/regtest/multicolvar directory of your PLUMED source. You should see many other directories called rt... within the same directory. If you change into any of these directories and issue the following set of commands:

```
source ../../sourceme.sh make
```

Then you will have run one of the regression tests of PLUMED. If the test runs without a hitch you should get an output something like this:

```
../../scripts/run
Thu Aug 20 14:33:00 IST 2015
Running regtest in /Users/gareth/Projects/CVception/plumed2/regtest/multicolvar/rt22
cp: ../tmp is a directory (not copied).
++ Test type: driver
++ Arguments: --plumed plumed.dat --trajectory-stride 10 --timestep 0.005 --ixyz trajectory.xyz --dump-forces
++ Processors: 0
/Users/gareth/Projects/CVception/plumed2/regtest/multicolvar/rt22/tmp
Run driver
Done. Here is the error file:
```

#### 12.14.4 Introduction

PLUMED has two manuals: a manual that is for users of the code and a manual that is for developers of the code. If you are interested in implementing new features in the code your first point of call should thus be the developer manual, which can be found <a href="here">here</a>. Alternatively, you can get to the front page of the developer manual by clicking the USER/DEVELOPER logo in the top right hand corner of any page of the user manual.

One of PLUMED's nicest features for the developer is that all the code and documentation for any new PLUMED command all appears together in a single file. When you come to implement a new feature it is thus relatively unlikely that you will have to modify any of the files you downloaded. Adding a new feature is simply a matter of adding one further cpp file containing the new method and the documentation for this method. We are able to achieve this by exploiting abstract base classes and polymorphism. All classes that calculate collective variables, print these variables or calculate biases thus inherit from a single base class called Action. You can read about the Action class here. Notice also that this page also shows how all the various classes within the code inherit from this single base class. It is perhaps worth spending a little while browsing through the various branches of this tree and understanding how the classes at each level become increasingly specialised and thus fit for particular purposes.

Lets say you want to implement a new collective variable in PLUMED. One way to start this task would be to write a new class that inherits from the PLMD::Colvar base class. If you click on the box in the tree for PLMD::Colvar and follow various links on the various subject pages you will eventually get to the following page, which will give you a step-by-step set of instructions for implementing a new collective variable. If you look through the manual you can find similar pages that provide you with instructions for implementing new analysis methods, functions and so on. Our suggestion when you implement something new would thus be to find some similar functionality in the code, look at how it is implemented and to look in the developer manual at the descriptions of the classes that have been inheritted. This process is what we will try and take you through in this short tutorial.

#### 12.14.5 Instructions

#### 12.14.5.1 Calculating a reasonably complex collective variable

In this first exercise I would like you to look through the manual and work out how to use the functionality that is already available in PLUMED to calculate the following collective variable:

$$s = \sum_{i=1}^{108} 1 - \frac{1 - \left(\frac{c_i}{4}\right)^6}{1 - \left(\frac{c_i}{4}\right)^{12}}$$

where  $c_i$  is equal to the coordination number of atom i, i.e.:

$$c_i = \sum_{j \neq i} \frac{1 - \left(\frac{r_{ij}}{1}\right)^6}{1 - \left(\frac{r_{ij}}{1}\right)^{12}}$$

So  $r_{ij}$  is the distance between atom i and atom j. This collective variable measures the number of coordination numbers that are more than 4 so the summations in the above expressions run over all 108 atoms in this particular system.

Write an input file that computes s and outputs its value to a file called colvar and that computes both the analytical and numerical derivatives of s and outputs this information to a file called deriv. You are going to run this calculation in the rt-coord directory that you downloaded with the tarball for this exercise so you should create this input file within that directory. You will need to output the quantities in the colvar and deriv files with only four decimal places. When you are content with your input run the calculation by typing make. If you have done everything correctly you should see the output that was discussed above.

In setting up your input files you may find it useful to watch our introductory video and this video on some of the features that are available in the code. Obviously, the user manual will be indespensible as well.

### 12.14.5.2 Implementing a new collective variable

In this second exercise I would like you to implement the following collective variable:

$$s = \sum_{i=1}^{108} \int_{57}^{59} \exp\left(-\frac{(x_i - x)^2}{2}\right) dx$$

where  $x_i$  is number of atoms in the second coordination sphere of the *i*th atom, i.e.:

$$s = \sum_{i \neq j} \int_2^4 \exp\left(-\frac{(r_{ij} - r)^2}{2}\right) dr$$

So  $r_{ij}$  is the distance between atom i and atom j. This collective variable measure the number of atoms that have between 57 and 59 atoms in their second coordination sphere. There are a number of observations we can make here that will help you enormously:

- Notice that CV is similar to the coordination number CV you calculated in the first example. For both CVs
  there is a sum over a quantity that is calculated for different sets of atoms. You should thus look at what was
  done by the routines that calculate the first CV and see what you can reuse.
- Notice that with the first CV we can calculate the number of coordination numbers that are within a certain range as well as the number of coordination numbers that are less than a certain threshold.
- · You can set the link cell cutoff equal to

std::numeric\_limits<double>::max()

• Lastly, this tool will prove very useful.

Write an input file that computes s and outputs its value to a file called colvar and that computes both the analytical and numerical derivatives of s and outputs this information to a file called deriv. When outputting numbers to colvar and deriv you should output numbers to four and three decimal places repsectively. You are going to run this calculation in the rt-second-shell directory that you downloaded with the tarball for this exercise so you should create this input file within that directory. When you are content with your input run the calculation by typing make. If you have done everything correctly you should see the output that was discussed above.

If you have sufficient time try use doxygen within PLUMED to write the documentation for your new collective variable.

### 12.14.6 Final thoughts

The aim of this tutorial is not so much to implement the CV. I do not think it is a particularly interesting or useful CV. Instead the hope is that by doing it you will get some idea of how to implement things within PLUMED. Based on my experience there are three key things I wish I could go back and tell my younger self about programming, which I would urge you to learn now:

- Write less code The more code you write the more bugs you generate. To be totally clear this is not me trying to say I am better at coding than you are the same statement holds true if I replace each you in the above with an I it holds true for everyone. In addition, there are lots of smart people out in the world writing code (and again I am not talking about the developers of plumed). Their code is properly tested and faster than anything that you will write so spend your time learning how it works so that you can re-use it.
- Test your code Notice that I set up directories that you could use to test your code for this tutorial. Testing should always be part of your development workflow and coming up with ways to test your code is hard, which is why we often don't do it enough. Also don't develop stuff in a vacuum get in touch with people who are using the code. You need to test your code on systems that people actually want to simulate and not just on dummy problems. In addition, you should learn to use profiling tools such as valgrind and instruments on the mac so that you can find memory leaks and bottlenecks in your code. When you start doing this properly you will realise that you cannot possibly properly maintain all the code that you have written and you will see clearly that you that you need to write less code.
- Write documentation for your code Undocumented software is useless. You need to explain how to use your code and to fill your manual with examples of how the code can be used to solve specific and interesting problems. That is to say that you need to provide examples of calculations that users actually want to perform. To be clear here writing a manual that tells users how something like the shake algorithm works in general terms is actually pretty useless. After all a user can go off and find out this information from a textbook, you could thus replace your description with a link to a textbook. What users want from you is an example that is similar to the calculation they actually want to set up. If I were providing documentation for an implementation of shake in an MD code I would thus explain in detail how to set up shake to constrain all the angles and bonds in all the water molecules in my system as it is a fair bet that this is how it will be being used by many users.

I hope you have seen from this tutorial that PLUMED tries to help you with all of these aims. We have a developer manual where we try to explain how to use the code that is already there. In addition, you can quite quickly generate nicely formatted user documentation for new CVs and it is easy to add new regression tests that allow you to test new features. Notice also that whenever commits are made on the origin git repository we use a website called travis-ci to test that the code works across a range of platforms.

# 12.15 Lugano tutorial: Analyzing CVs

#### 12.15.1 Aims

The aim of this tutorial is to introduce you to the PLUMED syntax. We will go through the writing of input files to calculate and print simple collective variables. We will then discuss how we can use PLUMED to analyse a trajectory by calculating ensemble averages, histograms and free energy surfaces.

### 12.15.2 Learning Outcomes

Once this tutorial is completed students will:

- Know how to write PLUMED input files that can be used to calculate and print collective variables.
- · Be able to calculate a collective variable that take the position of center of mass as input.
- · Know how to write a PLUMED input file that can be used to calculate an ensemble average.
- Know how to write a PLUMED input file that can be used to calculate a histogram. Students will also learn how this histogram can be converted into a free energy surface.

### 12.15.3 Resources

The tarball for this project contains the following files:

• trajectory-short.xyz: a (short) trajectory for a 16 residue protein in xyz format. All the calculations with plumed driver that will be performed during this tuturial will use this trajectory.

- template.pdb: a single frame from the trajectory that can be used in conjuction with the MOLINFO command
- · in : An input file for the simplemd code that forms part of PLUMED
- input.xyz: A configuration file for Lennard-Jones solid with an fcc solid structure

#### 12.15.4 Instructions

PLUMED2 is a library that can be incorporated into many MD codes by adding a relatively simple and well documented interface. Once it is incorporated you can use PLUMED2 to perform a variety of different analyses on the fly and to bias the sampling in the molecular dynamics engine. PLUMED2 can also, however, be used as a standalone code for analysing trajectories. If you are using the code in this way you can, once PLUMED2 is compiled, run the plumed executable by issuing the command:

```
plumed <instructions>
```

Let's start by getting a feel for the range of calculations that we can use PLUMED2 to perform. Issue the following command now:

```
plumed --help
```

What is output when this command is run is a list of the tasks you can use PLUMED2 to perform. There are commands that allow you to patch an MD code, commands that allow you to run molecular dynamics and commands that allow you to build the manual. In this tutorial we will mostly be using PLUMED2 to analyse trajectories, however. As such most of the calculations we will perform will be performed using the driver tool. Let's look at the options we can issue to plumed driver by issuing the following command:

```
plumed driver --help
```

As you can see we can do a number of things with plumed driver. For all of these options, however, we are going to need to write a PLUMED input file. Before we get on to writing input files for PLUMED there is information Codes interfaced with PLUMED here which provides details on what the other PLUMED2 tools do and instructions for how to interface PLUMED with an MD code. You may like to look at this information now or you might prefer to return after you have finished the exercises here.

# 12.15.4.1 PLUMED2's internal units

By default the PLUMED inputs and outputs quantities in the following units:

- Energy kJ/mol
- · Length nanometers
- · Time picoseconds

If you want to change these units you can do this using the UNITS keyword.

### 12.15.4.2 Introduction to the PLUMED input file

Many input files for PLUMED provides specifications for one or more CVs. These specifications are then followed by an instruction to PLUMED to PRINT these CVs and a termination line. Comments are denoted with a # and the termination of the input for PLUMED is marked with the keyword ENDPLUMED. Any words that follow the E $\leftarrow$  NDPLUMED line are ignored by PLUMED. You can also introduce blank lines as these will not be interpreted by PLUMED.

The following input can be used analyse the DISTANCE between the two terminal carbons of a 16 residues peptide. The PRINT command after the DISTANCE command ensures that the results (i.e. the distances calculated) are printed into the file named COLVAR.

```
#my first PLUMED input:
e2edist: DISTANCE ATOMS=2,253

#printout frequency
PRINT ARG=e2edist STRIDE=1 FILE=COLVAR

#endofinput
ENDPLUMED
here I can write what I want it won't be read.
```

Let's use this simple input file to analyse the trajectory included in the RESOURCES. To do so copy the input above into a file called plumed.dat and then issue the command below:

```
plumed driver --plumed plumed.dat --ixyz trajectory-short.xyz --length-units 0.1
```

Notice the —length-units 0.1 flag here. This tells PLUMED to convert the positions in the xyz file here, which are in Angstroms, into nm, which remember are PLUMED2's internal units

When this command finishes running you should have a file called COLVAR. If you look at it's contents (using the command more COLVAR for instance) you will find that the first two lines read:

```
#! FIELDS time e2edist 0.000000 2.5613161
```

The first line of the COLVAR files tells you what values are in each of the columns. The remaining lines then tell you the values these quantities took in the various trajectory frames. We can plot this data using gnuplot (or our favourite graphing program) by issuing the following commands:

```
gnuplot
p 'COLVAR' u 1:2 w 1
```

What this graph shows is the value of the distance that we calculated using PLUMED as a function of time. As you can see the distance fluctuates about as the atoms in our system move about in accordance with the various forces that act upon them.

Right so hopefully that wasn't too hard. What we are going to next is we are going to try to understand the input file that we have written a bit better.

### 12.15.4.3 The PLUMED input syntax

The input file that we issued in the last section looked something like this:

```
e2edist: DISTANCE ATOMS=2,253
PRINT ARG=e2edist STRIDE=1 FILE=COLVAR
```

What happens if we reverse the order of the two commands in the input file. In other words, what would have happened if we had run with an input file that looked like this:

```
PRINT ARG=e2edist STRIDE=1 FILE=COLVAR e2edist: DISTANCE ATOMS=2.253
```

Run the input file above using the commands described in the previous section to find out.

If everything is working correctly the input above should crash with the following error message:

```
+++ Internal PLUMED error
+++ file Action.cpp, line 234
+++ message: ERROR in input to action PRINT with label @0 : cannot find action named e2edist (hint! the action
```

Take a moment to read that error message and to try to think what it might mean before reading on.

To understand the error lets look at the correct input again:

```
e2edist: DISTANCE ATOMS=2,253
PRINT ARG=e2edist STRIDE=1 FILE=COLVAR
```

You should think of the PLUMED input syntax as a kind of scripting language with commands and variables. The first line in the above file thus tells PLUMED to calculate the distance between atoms 2 and 253 and to store the value of this distance in a variable called e2edist. The fact that this quantity is stored in a variable is important as it ensures that we can access this quantity when we come to issue commands later in the input file. So in the second line above we print a quantity. What quantity should be printed? e2edist - the distance between atom 2 and atom 253. Easy!

So why does the second input, that has the order of these two commands reversed, not work? Well the variable e2edist has to be defined before it can be used because in PLUMED2 the commands are executed in the same order as they are defined in the input file. We thus cannot do anything with e2edist (i.e. PRINT it) without first explaining how it is calculated.

This input demonstrates the key idea of the PLUMED syntax. Quantities calculated by commands such as  $DI \leftarrow STANCE$  are given labels (e2edist) so that they can be reused when performing other commands. This idea is discussed in more depth in the following video https://www.youtube.com/watch?v=PxJP16qNCYs. If you understand this idea though you are 90% of the way to understanding how to used PLUMED. Well done.

### 12.15.4.4 Center of mass positions

When calculating many collective variables it is useful to not think in terms of calculating them directly based on the positions of a number of atoms. It is useful to instead think of them as being calculated from the position of one or more virtual atoms whose positions are generated based on the position of a collection of other atoms. For example you might want to calculate the distance between the center of masses of two molecules. In this case it is useful to calculate the two positions of the centers of mass first and to then calculate the distance between the centers of mass. The PLUMED input that you would use for such a calculation reflects this way of thinking. An example of a PLUMED input that can be used to perform this sort of calculation is shown below:

```
first: CENTER ATOMS=1,2,3,4,5,6
last: CENTER ATOMS=251-256

e2edist: DISTANCE ATOMS=2,253
comdist: DISTANCE ATOMS=first,last

PRINT ARG=e2edist,comdist STRIDE=1 FILE=COLVAR
ENDPLUMED
```

Make a PLUMED input containing the above input and execute it on the trajectory that you downloaded at the start of the exercise by making use of the commands in section Introduction to the PLUMED input file

Before we turn to analysing what is output from this calculation there are a few things to note about this input file. Firstly, I should describe what this file instructs PLUMED to do. It tells PLUMED to:

- 1. calculate the position of the Virtual Atom 'first' as the CENTER of atoms from 1 to 6;
- 2. calculate the position of the Virtual Atom 'last' as the CENTER of atoms from 251 to 256;
- 3. calculate the distance between atoms 2 and 253 and saves it in 'e2edist';
- 4. calculate the distance between the two atoms 'first' and 'last' and saves it in 'comdist';
- 5. print the content of 'e2edist' and 'comdist' in the file COLVAR

Notice that in the input above we have used two different ways of writing the atoms used in the CENTER calculation:

- 1. ATOMS=1,2,3,4,5,6 is the explicit list of the atoms we need
- 2. ATOMS=251-256 is the range of atoms needed

Notice also that ranges of atoms can be defined with a stride which can also be negative as shown by the commands below, which are both equivalent:

```
    ATOMS=from,to:by (i.e.: 251-256:2)
    ATOMS=to,from:-by (i.e.: 256-251:-2)
```

Lets now return to the business of analysing what was output by the calculation. Lets begin by looking at the contents of the COLVAR file that was output. When you do so you should find that the first few lines of this file read:

```
#! FIELDS time e2edist comdist 0.000000 2.516315 2.464043
```

Notice that at variance with the file that was output in the previous section we now have three columns of numbers in the output file. Given the PRINT command that we used in the input to this calculation though this new behavior makes a lot of sense.

Lets now plot contents of the COLVAR file so we can compare the behaviour of the distance between the two terminal carbons and the distance between the centers of the mass of the two terminal residues in this trajectory (these two distances are what the above input is calculating). To plot this data issue the following commands:

```
gnuplot
p 'COLVAR' u 1:2 w 1, '' u 1:3 w 1
```

Given what you observe for the behavior of these two distance what do you now expect to see in the trajectory? Let's look at the trajectory to see if we are right. To look at the trajectory issue the following commands:

```
vmd template.pdb trajectory-short.xyz
```

Lets summarise what we have learnt from these sections thus far. We have seen that:

- PLUMED provides a simple syntax that can be used to calculate the DISTANCE between any pair of atoms in our system.
- PLUMED also allows us to calculate the positions of virtual atom (e.g. CENTER) and that we can calculate the DISTANCE between these quantities.
- Calculating these quantities is useful because it allows us to simplify the high-dimensional information contained in a trajectory.

Now, obviously, PLUMED can do much more than calculate the distances between pairs of atoms as we will start to see that in the following sections.

#### 12.15.4.5 Calculating torsions

In the previous sections we have seen how we can use PLUMED to calculate distances and how by plotting these distances we can begin to simplify the high dimensional data contained in a trajectory. Obviously, calculating a DISTANCE is not always the best way to simplify the information contained in a trajectory and we often find we have to work with other more-complex quantities. PLUMED thus started as a libraray that was used to gather all the various implementations people had written for different collective variables (CVs) that people had used to "analyse" trajectories over the years (analyse is in inverted commas here because, as you will see if you continue to use P LUMED, we use CVs to do much more than simply analyse trajectories). Now we will not have time to go over all the quantities that can be calculated in this tutorial. Once you understand the basic principles, however, you should be able to use the manual to work out how to calculate other quantities of interest. With this in mind then lets learn how to calculate a TORSION. As with DISTANCE the atoms that we specify in our TORSION command can be real or virtual. In the example below two real atoms and a virtual atom are used:

```
first: CENTER ATOMS=1-6
last: CENTER ATOMS=251-256
cvtor: TORSION ATOMS=first,102,138,last
PRINT ARG=cvtor STRIDE=1 FILE=COLVAR
ENDPLUMED
```

Copy this input to a PLUMED input file and use it to analyse the trajectory you downloaded at the start of this exercise by using the commands descibred in section Introduction to the PLUMED input file then plot the CV output using gnuplot.

As you can hopefully see calculating TORSION values and other CVs is no more difficult than calculating DISTA  $\leftarrow$  NCE values. In fact it is easier as generally when you calculate the torsions of a protein you often wish to calculate particular, named torsions (i.e. the  $\phi$  and  $\psi$  angles). The MOLINFO command makes it particularly easy to do this. For instance suppose that you want to calculate and print the  $\phi$  angle in the 6th residue of the protein and the  $\psi$  angle in the 8th residue of the protein. You can do so using the following input:

```
MOLINFO STRUCTURE=template.pdb
phi6: TORSION ATOMS=@phi-6
psi8: TORSION ATOMS=@psi-8
PRINT ARG=phi6,psi8 FILE=colvar
```

Copy this input to a PLUMED input file and use it to analyse the trajectory you downloaded at the start of this exercise by using the commands descibred in section Introduction to the PLUMED input file then plot the CV output using gnuplot. Notice that you will need the template.pdb file you downloaded at the start of this exercise in order for this to run.

### 12.15.4.6 An exercise with the radius of gyration

Lets now see if you can use everything you have learnt to setup a PLUMED input file of your own. What I would like you to do is to write a PLUMED input file that measures the Radius of Gyration GYRATION for the configurations in each of the frames in the trajectory that you downloaded at the start of this exercise. This radius of gyration will be calculated using the positions of all the atoms in that trajectory.

NOTE: if what you need for one or more variables is a long list of atoms and not a virtual atom you can use the keyword GROUP. A GROUP can be defined using ATOMS in the same way we saw before, in addition it is also possible to define a GROUP by reading a GROMACS index file.

```
ca: GROUP ATOMS=9,16,31,55,69,90,102,114,124,138,160,174,194,208,224,238
```

Now 'ca' is not a virtual atom but a simple list of atoms.

# 12.15.4.7 Coordination numbers

In the previous sections we have learnt how PLUMED can be used to calculate simple functions of atomic positions such as the DISTANCE between pairs of atoms. As discussed here (https://www.youtube.com/watch?v=iDvZmbWE5ps) many of the more complicated collective variables that we use to analyse simulations can be calculated by computing these simple quantities multiple times for different sets of atoms. That is to say we can calculate many more complicated collective variables using:

$$s = \sum_{i} g[f(\{\mathbf{X}_i\})]$$

Here g is a function of a scalar and f is a function that takes in the positions of a set of atoms  $\{X\}$  and outputs a scalar. The sum then runs over the different sets of atoms from which the quantity f can be calculated. This is all rather abstract so lets make it more concrete by considering an example. Suppose that we want to calculate the coordination number of atom k. What we need to do is:

1. We need to calculate the distance between atom k and every atom in the system that is not atom k. This will be the set of sets of atoms that we have to perform the sum above on. Furthermore, the function f in the above will be pythagoras theorem, which is the function we use to calculate the distance between a pair of atoms.

2. We need to transform the distances calculated by a switching function (f in the above) that is equal to one if the distance is less than or equal to the typical length of a chemical bond and zero otherwise.

Lets thus use PLUMED to calculate the coordination number of atom 9. We can do this as follows:

```
d1: DISTANCES GROUPA=9 GROUPB=1-8,10-256 LESS_THAN={RATIONAL D_0=0.16 R_0=0.01 D_MAX=0.2} PRINT ARG=d1.* FILE=colvar
```

Copy this input file to a PLUMED input file. Before using it to analyse the trajectory that you downloaded at the start of the exercise using the commands described in section Introduction to the PLUMED input file try to guess what value this coordination number will take. Hint: what element is atom 9?

Now see if you can adjust the above input to calculate the coordination number of atom 5. What is the coordination number of this atom and why does it take this value?

```
12.15.4.8 Multicolvar
```

In the previous section we exploited a feature of PLUMED known as multicolvar when calculating the coordination number. When using this feature we are not confined to simply calculating coordination numbers. For instance the input below allows us to calculate a number of distances and to then calculate the mean of the distribution of distances, the minimum distance in the distribution, the maximum distance in the distribution and the second moment of the distribution (the variance).

```
ca: GROUP ATOMS=9,16,31,55,69,90,102,114,124,138,160,174,194,208,224,238
dd: DISTANCES GROUP=ca MEAN MIN={BETA=50} MAX={BETA=0.02} MOMENTS=2

PRINT ARG=dd.mean,dd.min,dd.max,dd.moment-2 STRIDE=1 FILE=COLVAR
ENDPLUMED
```

Try to copy this input now and to use it to analyse the trajectory you downloaded at the start of the exercise using the commands described in section Introduction to the PLUMED input file.

Multicolvar is not just for DISTANCES though. The infrastracture of multicolvar has been used to develop many PLUMED2 collective variables. One interesting example is the set of Secondary Structure CVs (ANTIBETAR MSD, PARABETARMSD) and ALPHARMSD). You can use the input below to calculate the degree of anti-beta secondary structure in each of the trajectory frames by copying this input to a PLUMED input file and by exploiting the commands to run driver that were described in section Introduction to the PLUMED input file.

```
MOLINFO STRUCTURE=template.pdb
abeta: ANTIBETARMSD RESIDUES=all TYPE=DRMSD LESS_THAN={RATIONAL R_0=0.08 NN=8 MM=12} STRANDS_CUTOFF=1
PRINT ARG=abeta.lessthan STRIDE=1 FILE=COLVAR
ENDPLUMED
```

We can do a large number of other things with multicolvar. If you are interested this topic is described in more detail in the tutorial: Belfast tutorial: Steinhardt Parameters.

### 12.15.4.9 Understanding the need for ensemble averages

In the previous sections we have learnt how we can use PLUMED to calculate collective variables from simulation trajectories and have seen how, by plotting how these collective variables change as a function of time, we can get a handle on what happens during the trajectory. Generally this level of analysis is not sufficient for us to publish a paper about the simulations we have run, however. In this section we are going to run some molecular dynamics simulations in order to understand why.

You are going to need to do the following set of things in order to do this exercise:

- 1. Take the two files you downloaded at the start of this exercise that are called called in and input.xyz and place them in a directory.
- 2. In the same directory write an input file for PLUMED called plumed.dat that calculates and prints the distance between atoms 2 and 3 to a file called colvar.
- 3. Run simplemd by issuing the command:

```
plumed simplemd < in
```

- 1. Open the file called input.xyz and modify the z-coordinate of the 1st atom. It should currently be equal to zero. Set it equal to 0.1.
- 2. Run simplemd again using the command above.
- 3. Plot the colvar files output during the two calculations using:

```
gnuplot
p 'colvar' w l, 'bck.0.colvar' w l
```

If you have done everything correctly you should see that the values of the distance in the early parts of the simulation are similar but that the values of the distance in the two simulations are very different by the end of the simulations.

Allow me to explain what we have just done. simplemd is a tool for running molecular dynamics using the Lennard-Jones potential. We have thus just run two very similar molecular dynamics calculations. The only difference between these two calculations was in the z-coordinate of the first atom in the input structure. The initial velocities of all the atoms were the same and the initial positions of all other atoms were identical. In spite of these similarities, however, the trajectories that we obtain in the two calculations are very different. This is important as it tells us that the time series of CV values that we get from a single MD simulation is (in and of itself) not particularly valuable as we would have got a completely different time series of values if we had run the calculation with only a slightly different input structure. We should, therefore, think of the trajectory output from a molecular dynamics simulations as a time series of random variables and analyse it accordingly.

The justification for thinking of a trajectory as a time series of random variables is based on statistical mechanics which tells us that a system with a constant number of atoms and a constant volume evolving at a fixed temperature has a probability:

$$P(q) \propto e^{-\frac{U(q)}{k_B T}}$$

of being in a microstate q with internal energy U(q) as discussed and explained in the videos that can be found on the following pages:

• http://gtribello.github.io/mathNET/PRINCIPLE\_OF\_EQUAL\_APRIORI\_PROBABIL← ITIES.html

- http://gtribello.github.io/mathNET/GENERALIZED\_PARTITION\_FUNCTION.html
- http://gtribello.github.io/mathNET/CANONICAL ENSEMBLE.html

Now, and as already explained above, given that each microstate is sampled with this particular probability it makes sense to think of the microstates, and by extension the collective variables values that we calculate from these microstates, as random variables. We can thus define the ensemble average for a particular collective variable, A, using:

$$\langle A \rangle = \int A(q)P(q)\mathrm{d}q$$

where the integral here runs over all possible microstates, A(q) is the function that allows us to calculate the value of the CV from the positions of the atoms in microstate q and where P(q) is the "probability" (as it appears in an integral it is, strictly speaking, a probability density) of being in microstate q which was introduced above. For more information on this business of random variables and ensemble averages (or expectations) check out the videos that can be found on the following pages:

- http://gtribello.github.io/mathNET/RANDOM\_VARIABLES.html
- http://gtribello.github.io/mathNET/EXPECTATION.html

Instead of using the formula for the ensemble average given above we can estimate an ensemble averages by taking a time series of random variables (like our trajectory) adding all the values of the random variable together (in our case the CV values in each of the trajectory frames) and dividing by the number of random variables that were added together. This works because of results known as the law of large numbers and the central limit theorem, which you can find videos on here:

- http://gtribello.github.io/mathNET/LAW OF LARGE NUMBERS.html
- http://gtribello.github.io/mathNET/CENTRAL\_LIMIT\_THEOREM.html

Alternatively, we can justify this way of analysing our trajectory by thinking of the set of sampled frames as random variables generated from Markov chain. These mathematical objects are discussed here:

- http://gtribello.github.io/mathNET/MARKOV\_PROPERTY.html
- http://gtribello.github.io/mathNET/CHAPMAN\_KOLMOGOROV\_RELATION.html
- http://gtribello.github.io/mathNET/TRANSIENT\_RECURRENT\_STATES.html
- http://gtribello.github.io/mathNET/STATIONARY\_DIST\_MARKOV.html

Regardlessly, however, and as we will see in the following section we can estimate ensemble averages of collective variables using:

$$\langle A \rangle \approx \frac{1}{T} \sum_t A[q(t)]$$

where the sum runs over the set of T microstates, q(t), in our trajectory and where A[q(t)] is the function that is used to calculate the value of the collective variable from the positions of the atoms in the microstate. When we do so we find that the values of the ensemble averages from different trajectories are reasonably consistent and certainly much more consistent than the set of instantaneous CV values.

#### 12.15.4.10 Calculating ensemble averages using PLUMED

Repeat the steps from the previous section that were used to run the two MD calculations with slightly different input configurations. This time, however, your PLUMED input should look like this:

```
d1: DISTANCE ATOMS=2,3
d1a: AVERAGE ARG=d1 STRIDE=10
PRINT ARG=d1,d1a FILE=colvar STRIDE=10
```

If you now plot the values of the CV output from these two calculations together with the estimates of the ensemble averages using something like the commands below:

```
gnuplot
p 'colvar' u 1:2 w 1, '' u 1:3 w 1, 'bck.0.colvar' u 1:2 w 1, '' u 1:3 w 1
```

You should see that, although the instantaneous values of the CVs differ greatly in the two simulations, the average values of the CVs are relatively similar for both simulations.

Lets discuss the AVERAGE command that we have added here and what this does. In essence it accumulates the sum of all the distances calculated by the DISTANCE command labelled d1. When it comes time to output this accumulated average (every 10 trajectory steps) this accumulated sum is divided by the number of trajectory frames that have been summed in calculated the current sum. In other words, the average allows us to compute the following quantity:

$$a = \frac{1}{N} \sum_{i=1}^{N} d(t_i)$$

where  $d(t_i)$  is the value of the distance at time  $t_i$ . Now you may reasonably ask: what the keyword STRIDE=10 is doing in this command? Well this is telling PLUMED to only add distances into the accumulated average every 10 steps. In other words, when calculating the average we are disregarding the value of the distance in frames 1,2,3,4,5,6,7,8 and 9. Why are we disregarding this information though? Well because there are correlations between the values the CV takes in two adjacent trajectory frames. Ideally, we want the values of the distance we are averaging to be independent and identical random variables.

Before we move on to calculating histograms and free energy surfaces I have a little challenge for you. If you are able to answer the following question then you really understand what the AVERAGE command is doing. Try running the calculation above using the following input:

```
d1: DISTANCE ATOMS=2,3
d1a: AVERAGE ARG=d1 STRIDE=10 CLEAR=10
PRINT ARG=d1,d1a FILE=colvar STRIDE=10
```

Based on what you see when you plot the colvar file and the information on the page about the AVERAGE command what is the CLEAR=10 keyword telling PLUMED to do?

### 12.15.4.11 Calculating histograms

Most of the time, we are not really interested in calculating ensemble averages for particular collective variables. What we would really like is the probability that the collective variable takes a particular value or set of values. In other words, and as discussed in the following video, we would like the probability as a function of collective variable value:

```
• https://www.youtube.com/watch?v=-1NLaqOJKS0
```

We can calculate approximate histograms like these using PLUMED. Furthermore, and as discussed in the video below, when we do this what we are really doing is we are calculating multiple ensemble averages at once:

```
• http://gtribello.github.io/mathNET/histogram-video.html
```

To calculate these ensemble averages we must make use of the HISTOGRAM command. An input file for a calculation of this sort is provided below. Use this input now and the input files for simple MD from the previous two sections to calculate the histogram of DISTANCE values that are explored in these trajectories.

```
d1: DISTANCE ATOMS=2,3
hh: HISTOGRAM ARG=d1 BANDWIDTH=0.05 GRID_MIN=0 GRID_MAX=4.0 GRID_BIN=200 STRIDE=10
DUMPGRID GRID=hh FILE=histo STRIDE=25000
```

You can plot the histogram output from this simulation using:

```
gnuplot
p 'histo' w l
```

You should see that there is a large peak in the histogram at around 2.0 indicating that this is the value of the distance that the atoms were most likely to have during the course of the simulation. N.B. The histogram is unlikely to be converged with a trajectory this short.

Lets now look at the syntax of the HISTOGRAM command. The first thing to note is the similarities between what is done with this command and what is done with the AVERAGE command. Once again we have a STRIDE keyword for HISTOGRAM (and a CLEAR keyword for that matter) that tells us how often data should be added to to the accumulated averages. Furthermore, in both these commands we have an additional instruction with its own STRIDE keyword (PRINT for AVERAGE and DUMPGRID for HISTOGRAM) that tells us how frequently the accumulated averages should be output to human readable files.

A substantial difference between these two input files is the object the label hh refers to. In all previous examples the label of an action has referred to a scalar quantity that was calculated by that action. In the example above, however, the label hh refers to the function accumulated on a grid that is evaluated by the HISTOGRAM command. This is why we cannot print this quantity using PRINT - it is not a simple scalar valued function anymore. As you become more familiar with PLUMED you will find that these labels can refer to a range of different types of mathematical object.

Lets now see if we can bring together everything we have learnt in this tutorial in order to analyse the protein trajectory that was downloaded at the start of the exercise.

### 12.15.4.12 A histogram for the protein trajectory

We are going to calculate the HISTOGRAM from our protein trajectory as a function of two different collective variables: ANTIBETARMSD and the average distance between the ca atoms of our protein backbone. The input that allows us to claculate perform this analysis is shown below:

```
# Read in protein structure template
MOLINFO STRUCTURE=template.pdb
# Calculate collective variables
abeta: ANTIBETARMSD RESIDUES=all TYPE=DRMSD LESS_THAN={RATIONAL R_0=0.08 NN=8 MM=12} STRANDS_CUTOFF=1
ca: GROUP ATOMS=9,16,31,55,69,90,102,114,124,138,160,174,194,208,224,238
DISTANCES GROUP=ca MEAN MIN={BETA=50} MAX={BETA=0.02} MOMENTS=2 LABEL=dd
# Print instaneous values of collective variables
PRINT ARG=abeta.lessthan,dd.mean,dd.min,dd.max,dd.moment-2 STRIDE=1 FILE=COLVAR
# Accumulate histogram of collective variables
hh: HISTOGRAM ARG=abeta.lessthan,dd.mean KERNEL=DISCRETE GRID_MIN=0,0.8 GRID_MAX=4,1.2 GRID_BIN=40,40
# Output histogram - N.B. when we are running with driver we can not provide a STRIDE.
# The histogram will then only be output once all the trajectory frames have been read in and analysed
DUMPGRID GRID=hh FILE=histo
```

Try running the input above on the trajectory that you downloaded at the start of this exercise by using the commands detailed in section Introduction to the PLUMED input file. You can plot the two dimensional histogram output using the following commands:

```
gnuplot
set pm3d map
sp 'histo' w pm3d
```

If you do so though, you will probably find that the structure in the histogram, H(s), is a bit difficult to visualise because the probability changes from point to point by multiple orders of magnitude. This is why we often convert the histogram, H(s), to a free energy surface, F(s), using:

$$F(s) = -k_B T \ln H(s)$$

If you want to use PLUMED to output the free energy rather than the histogram you need to use the CONVERT\_

TO\_FES command as shown below:

```
# Read in protein structure template
MOLINFO STRUCTURE=template.pdb
# Calculate collective variables
abeta: ANTIBETARMSD RESIDUES=all TYPE=DRMSD LESS_THAN={RATIONAL R_0=0.08 NN=8 MM=12} STRANDS_CUTOFF=1
ca: GROUP ATOMS=9,16,31,55,69,90,102,114,124,138,160,174,194,208,224,238
DISTANCES GROUP=ca MEAN MIN={BETA=50} MAX={BETA=0.02} MOMENTS=2 LABEL=dd
# Print instaneous values of collective variables
PRINT ARG=abeta.lessthan,dd.mean,dd.min,dd.max,dd.moment-2 STRIDE=1 FILE=COLVAR
# Accumulate histogram of collective variables
hh: HISTOGRAM ARG=abeta.lessthan,dd.mean KERNEL=DISCRETE GRID_MIN=0,0.8 GRID_MAX=4,1.2 GRID_BIN=40,40
fes: CONVERT_TO_FES GRID=hh TEMP=300
# Output free energy - N.B. when we are running with driver we can not provide a STRIDE.
# The histogram will then only be output once all the trajectory frames have been read in and analysed
```

Notice though that even when we do this complicated looking calculation we are still, underneath it all, calculating functions of a large number of ensemble averages.

DUMPGRID GRID=fes FILE=fes.dat

### 12.15.5 Conclusions and further work

If you have worked through all of this tutorial make sure that you have understood it by ensuring that you understand what the list of learning outcomes in section Learning Outcomes means and that you can use PLUMED to perform all these tasks. In terms of further work you should investigate issues related to the convergence of estimates of ensemble averages such as block averaging. You might like to investigate how long your simulations have to be in order to obtain reliable estimates of the ensemble average for a collective variable and reliable estimates for the free energy as a function of a collective variable. Alternatively, you might like to explore other collective variables that could be used to analyse the protein trajectory that you have worked on in this tutorial.

# 12.16 Lugano tutorial: Path CVs

# 12.16.1 Aims

Consider the two overlain protein structures that are shown in the figure below. Can you see the difference between these two structures? Can you think of a collective variable that could be used to study the substantial change in structure?

Your answers to the questions posed above are hopefully: yes I can see the difference between the two structures - the upper loop is radically different in the two cases - and no I have absolutely no idea as to how to create a collective variable that might be used to study the change in structure.

These answers are interesting as they cut to the very heart of what is interesting about biomolecular systems. In fact this difficulty is one of the reasons why such systems are so widely studied. If you think for a moment about solid state systems any transition usually involves a substantial change in symmetry. Low energy configurations are usually high symmetry while higher energy configurations have a low symmetry. This makes it easy to design collective variables to study solid state transitions - you simply measure the degree of symmetry in the system (see Belfast tutorial: Steinhardt Parameters). In biomolecular systems by constrast the symmetry does not change substantially during a folding transition. The unfolded state has a low symmetry but the folded state also has a low symmetry, which is part of the reason that it is so difficult to find the folded state from the amino acid sequence alone.

With all this in mind the purpose of this tutorial is to learn about how we can design collective variables that can be used to study transitions between different states of these low-symmetry systems. In particular, we are going to learn how we can design collective variables that describe how far we have progressed along some pathway between two configurations with relatively low symmetry. We will in most of this tutorial study how these coordinates work in a two-dimensional space as this will allow us to visualise what we are doing. Hopefully, however, you will be able to use what you learn from this tutorial to generalise these ideas so that you can use PATH and PCAVARS in higher-dimensional spaces.

# 12.16.2 Learning Outcomes

Once this tutorial is completed students will:

- be able to explain what is computed by a PCAVARS coordinate and write down expressions for these quantities.
- be able to write a PLUMED input file that calculates and prints a PCAVARS coordinate.
- be able to write down an expression for the quantity contained in the s and z components of a PATH collective variable.
- be able to write PLUMED input files that calculate PATH collective variables for a range of different metrics.
- · be able to measure the quality of a transition state by calculating the isocommittor.

#### 12.16.3 Resources

The tarball for this project contains the following files:

- transformation.pdb: a trajectory that shows the transition between the C7ax and C7eq conformers of alanine dipeptide.
- pca-reference.pdb: a file that gives the start and end points of the vector that connects the C7ax and C7eq conformers. This file contains the positions of the atoms in these two structures.
- PCA-isocommittor : a directory containing the files required to run isocommitor simulations that monitor the values of  $\phi$ ,  $\psi$  and the PCA coordinate.
- PATH-isocommittor : a directory containing the files required to run isocommitor simulations that monitor the values of the PATH collective variable S(X).
- 2CV-isocommittor : a directory containing the files required to run isocommitor simulations that monitor the values of the PATH collective variables S(X) and Z(X)

#### 12.16.4 Instructions

In this tutorial we are going to be considering a conformational transition of alanine dipeptide. In particular we are going to be considering the transition between the two conformers of this molecule shown below:

Alanine dipeptide is a rather well-studied biomolecule (in fact it is an overstudied molecule!). It is well known that you can understand the interconversion of the two conformers shown above by looking at the free energy surface as a function of the  $\phi$  and  $\psi$  ramachandran angles as shown below:

In this tutorial we are not going to use these coordinates to study alanine dipeptide. Instead we are going to see if we can find a single collective variable that can distinguish between these two states.

# 12.16.4.1 PCA coordinates

Consider the free energy surface shown in figure belfast-2-rama-fig. It is clear that either the  $\phi$  ( x-axis) or the  $\psi$  ( y-axis) angle of the molecule can be used to distinguish between the two configurations shown in figure belfast-2-transition-fig. Having said that, however, given the shape of landscape and the associated thermal fluctuations we would expect to see in the values of these angles during a typical simulation, it seems likely that  $\phi$  will do a better job at distinguishing between the two configurations.  $\psi$  would most likely be a bad coordinate as when the molecule is in the C7eq configuration the  $\psi$  angle can fluctuate to any value with only a very small energetic cost. If we only had information on how the  $\psi$  angle changed during a simulation we would thus struggle to distinguish a transition to the C7ax configuration from a thermal fluctuations. Unsurprinsgly then it has been shown that metadynamics simulations that use just the  $\phi$  angle as a collective variable can effectively drive the system from the C7ax configuration to the C7eq configuration. We will not repeat these calculations here but will instead use driver to determine how the values of  $\phi$  and  $\psi$  change as we move between along the transition path that connects the C7ax configuration to the C7eq state.

```
t1: TORSION ATOMS=2,4,6,9
t2: TORSION ATOMS=4,6,9,11
PRINT ARG=t1,t2 FILE=colvar
```

Lets run this now on trajectory that describes the transition from the C7ax configuration to the C7eq configuration. To run this calculation copy the input file above into a file called plumed.dat and run the command below:

```
plumed driver --mf_pdb transformation.pdb
```

Try plotting each of the two torsional angles in this file against time in order to get an idea of how good a job each one of these coordinates at distinguishing between the various configurations along the pathway connecting the C7ax and C7eq configurations. What you will see is that in both cases the CV does not increase/decrease monotonically as the transition progresses.

We can perhaps come up with a better coordinate that incorporates changes in both  $\phi$  and  $\psi$  by using the coordinate illustrated in the figure below.

We can even use PLUMED to calculate this coordinate by using the input shown below:

```
t1: TORSION ATOMS=2,4,6,9
t2: TORSION ATOMS=4,6,9,11
tc: COMBINE ARG=t1,t2 COEFFICIENTS=2.621915,-2.408714 PERIODIC=NO
PRINT ARG=t1,t2,tc FILE=colvar
```

Try calculating the values of the above collective variables for each of the configurations in the transformation.pdb file by using the command that was given earlier.

Notice that what we are using here are some well known results on the dot product of two vectors here. Essentially if the values of the ramachandran angles in the C7eq configuration are  $(\phi_1, \psi_1)$  and the ramachandran angles in the C7ax configuration are  $(\phi_2, \psi_2)$ . If our instantaneous configuration is  $(\phi_3, \psi_3)$  we can thus calculate the following projection on the vector connecting the C7eq state to the C7ax state:

$$s = (\phi_2 - \phi_1).(\phi_3 - \phi_1) + (\psi_2 - \psi_1).(\psi_3 - \psi_1)$$

which is just the dot product between the vector connecting the point  $(\phi_1, \psi_1)$  to  $(\phi_2, \psi_2)$  and the vector connecting the point  $(\phi_1, \psi_1)$  to  $(\phi_3, \psi_3)$ . If we call these two vectors  $\mathbf{v}_1$  and  $\mathbf{v}_2$  we can write this dot product as:

$$\mathbf{v}_1 \cdot \mathbf{v}_2 = |\mathbf{v}_1| |\mathbf{v}_2| cos(\alpha)$$

where  $|\mathbf{v}_1|$  and  $|\mathbf{v}_2|$  are the magnitudes of our two vectors and where  $\alpha$  is the angle between the two of them. Elementary trignometry thus tells us that if  $\mathbf{v}_1$  is a unit vector (i.e. if it has magnitude 1) the dot product is thus equal to the projection of the vector  $\mathbf{v}_2$  on  $\mathbf{v}_2$  as shown in figure pca-figure.

This is an useful idea. In fact it is the basis of the PCAVARS collective variable that is implemented in PLUMED so we can (almost) calculate the projection on this vector by using the input shown below:

```
t1: TORSION ATOMS=2,4,6,9
t2: TORSION ATOMS=4,6,9,11
pca: PCAVARS REFERENCE=angle-pca-reference.pdb TYPE=EUCLIDEAN
PRINT ARG=t1,t2,pca.* FILE=colvar
```

We cannot, however, do this in practise (we also shouldn't really use the previous input either) as the TORSION angles that we use to define our vectors here are periodic. In this next section we will thus look at how we can avoid this problem of periodicity by working in a higher dimensional space.

#### 12.16.4.2 PCA with the RMSD metric

In the previous section I showed how we can use the projection of a displacement on a vector as a collective variable. I demonstrated this in a two dimensional space as this makes it easy to visualize the vectors involved. We are not forced to work with two dimensional vectors, however. We can instead find the vector that connects the C7eq and C7ax states in some higher dimensional space and project our current coordinate on that particular vector. In fact we can even define this vector in the space of the coordinates of the atoms. In other words, if the 3 N coordinate of atomic positions is  $\mathbf{x}^{(1)}$  for the C7eq configuration and  $\mathbf{x}^{(2)}$  for the C7ax configuration and if the instanenous configuration of the atoms is  $\mathbf{x}^{(3)}$  we can use the following as a CV:

$$s = \sum_{i=1}^{3N} (x_i^{(2)} - x_i^{(1)})(x_i^{(3)} - x_i^{(1)})$$

where the sum here runs over the 3N-dimensional vector that defines the positions of the N atoms in the system. This is what (in a manner of speaking - I will return to this point momentarily) is calculated by this PLUMED input:

```
t1: TORSION ATOMS=2,4,6,9
t2: TORSION ATOMS=4,6,9,11
pca: PCAVARS REFERENCE=pca-reference.pdb TYPE=OPTIMAL
PRINT ARG=t1,t2,pca.* FILE=colvar
```

Use this input to analyse the set of configurations that are in the transformation.pdb file.

Let's now look further at the caveat that I alluded to before we ran the calculations. I stated that we are only calculating:

$$s = \sum_{i=1}^{3N} (x_i^{(2)} - x_i^{(1)})(x_i^{(3)} - x_i^{(1)})$$

in a manner of speaking. The point is that we would not want to calculate exactly this quantity because the vectors of displacements that are calculated in this way includes both rotational and translational motion. This is a problem as the majority of the change in moving from the C7ax configuration shown in figure belfast-2-transition-fig to the C7eq configuration shown in figure belfast-2-transition-fig comes from the translation of all the atoms. To put this another way if I had, in figure belfast-2-transition-fig, shown two images of the C7ax configuration side by side the displacement in the positions of the atoms in those two structures would be similar to the displacement of the atoms in belfast-2-transition-fig as as the majority of the displacement in the vector of atomic positions comes about because I have translated all the atoms in the molecule rightwards by a fixed amount. I can, however, remove these translational displacements from consideration when calculating these vectors. In addition, I can also remove any displacements due rotation in the frame of reference of the molecule. If you are interested in how this is done in practise you can read about it on the manual page about the RMSD collective variable. For what concerns us here, however, all we need to know is that when we use the OPTIMAL metric we are calculating a vector which tells us how far the atoms have been displaced in moving from structure A to structure B in a way that excludes any displacements due to translation of the center of mass of the molecule or any displacements that occur due to rotation of the cartesian frame.

### 12.16.4.3 The isocommitor surface

In the previous sections I have been rather loose when talking about better and worse collective variables in that I have not been clear in my distinction between what makes a collective variable good and what makes a collective variable bad. In this section I thus want to discuss one method that we can use to judge the quality of a collective variable. This method involves calculating the so called isocommitor. The essential notion behind this technique is that there will be a saddle point between the two states of interest (the C7ax and C7eq configurations in our alanine dipeptide example). If the free energy is plotted as a function of a good collective variable the location of this dividing surface - the saddle point - will appear as a maximum.

Lets suppose that we now start a simulation with the system balanced precariously on this maximum. The system will, very-rapidly, fall off the maximum and move towards either the left or the right basin. Furthermore, if this maximum provides a good representation of the location of the transition state ensemble - in other words if the position

of maximum in the low-dimensional free energy surface tells us something about the structure in the transition state ensemble - then 50% of trajectories started from this point will fall to the left and 50% will fall to the right. If by contrast the maximum in the free energy surface does not represent the location of the transition state well then there will be an imbalance between the number of trajectories that move rightwards and the number that move leftwards.

We can think of this business of the isocomittor one further way, however. If in the vicinity of the transition state between the two basins the collective variable is perpendicular to the surface separating these two states half of the trajectories that start from this configuration will move to the left in CV space while the other half will move to the right. If the dividing surface and the CV are not perpendicular in the vicinity of the transition state, however, there will be an imbalance between the number of trajectories that move rightwards and the number of trajectories that move leftwards. We can thus determine the goodness of a collective variable by shooting trajectories from what we believe is the transition state and examining the number of trajectories that move into the left and right basins.

Lets make all this a bit more concrete by looking at how we might calculate isocomittors by using some of the collective variables we have introduced in this exercise. You will need to go into the directory in the tar ball that you downloaded that is called PCA-isocommittor. In this directory you will find a number of files that will serve as input to gromacs 5 and PLUMED. You thus need to ensure that you have an installed version of gromacs 5 patched with PLUMED on your computer in order to perform this exercise. In addition to these input files you will find a bash script called script.sh, which we are going to use in order to set of a large number of molecular dynamics simualtions. If you open script.sh you will find the following lines near the top:

```
GROMACS_BIN=/Users/gareth/MD_code/gromacs-5.1.1/build/bin
GROMACS=$GROMACS_BIN/gmx
source $GROMACS_BIN/GMXRC.bash
```

These will need to be adjusted so that the GROMACS\_BIN variable points at the bin directory of the gromacs build on your computer. Once you have made this modification though you can run the calculation by issuing the following command in the PCA-isocommittor directory:

```
./script.sh
```

This command submits 50 molecular dynamics simulations that all start from a configuration that lies between the C7eq and C7ax configurations of alanine dipeptide. In addition, this command also generates some scripts that allow us to visualise how the  $\phi$ ,  $\psi$  and PCA coordinates that we introduced in the previous sections change duing each of these 50 simulations. If you load gnuplot and issue the command:

```
load "script_psi.gplt"
```

you see how  $\psi$  changes during the course of the 50 simulations. Similarly the gnuplot command:

```
load "script_phi.gplt"
```

will show how how  $\phi$  changes during the course of the 50 simulations and:

```
load "script_pca.gplt"
```

gives you the information on the pca coordinates. If you look at the  $\psi$  and pca data first you can see clearly that it is very difficult to distinguish the configurations that moved to the C7eq basin from the trajectories that moved to the C7ax basin. By contrast if you look at the data on the  $\phi$  angles you can indeed use these plots to distinguish the trajectories that moved to C7eq from the trajectories that moved to C7ax. It is abundantly clear, however, that the number of trajectories that moved to C7eq is not equal to the number of trajectories that moved to C7ax. This CV, therefore, is not capturing the transition state ensemble.

One thing you will have seen from these examples is that the PCAVARS coordinate that were introduced in the previous sections provides an extremely poor model for the transition state ensemble. The value of the isocommittor at the maximum for both of these variables is not at all close to 50%. In fact the CV is not even particularly good at capturing the difference between these two states. If you look at the free energy surface shown below it is perhaps clear why.

You can see the location of the saddle point between these two states in this surface and it is very clear that the vector connecting the C7eq state to the C7ax state does not pass through this point. In fact it would be extremely fortuitous if a vector connecting an initial state and a final state also passed through the intermediate transition state between them. We can, after all, define the equation of straight line (a vector) if we are given only two points on it. In the next section we are thus going to see how we can resolve this problem by introducing a non-linear (or curvilinear) coordinate.

#### 12.16.4.4 Path collective variables

Consider the black path that connects the C7ax and C7eq states in the free energy shown below:

This black pathways appears to be the "perfect" coordinate for modelling this conformational transition as it passes along the lowest energy pathway that connects the two states and because it thus passes over the lowest saddle point that lies between them. We can calculate such a coordinate with PLUMED by using the input file below (I will return to the mathematical details of how this works momentarily)

```
path: PATH REFERENCE=path-reference.pdb TYPE=OPTIMAL LAMBDA=15100.
PRINT ARG=* STRIDE=2 FILE=colvar FMT=%12.8f
```

Lets thus use this input and run an isocomittor analysis using the location of the maximum in this coordinate as the start point for all our trajectories. Everything you need to do this analysis is in the PATH-isocommittor directory. Once again you will find that there is a script.sh bash script inside this directory, which, as in the previous section, you can use to run a large number of molecular dynamics simulation. Furthermore, similarly to the last section you will need to begin this exercise by modifying the location of path to gromacs within this script. Once you have made this modification submit your molecular dynamics jobs by issuing the command:

```
./script.sh
```

You can then plot the data output using gnuplot and the command:

```
load "script_path.gplt"
```

Unlike what we saw for the PCAVARS variables in the previous section we find that it is easy to use these PATH variables to distinguish those configurations that moved to C7ax from those that moved to C7eq. Having said that, however, we still have a large imbalance between the number of trajectories that move rightwards and the number that move leftwards. We are thus still a long way from unambiguously identifying the location of the transition state ensemble for this system.

### 12.16.4.5 The mathematics of path collective variables

Let's now take a moment to discuss the mathematics of these coordinates, which is not so complicated if we think about what they do through an analogy. Suppose that you were giving your friend instructions as to how to get to your house and lets suppose these instructions read something like this:

- 1. Take the M1 motorway and get off at junction 5
- 2. At the roundabout you need to take the third exit towards Crumlin
- 3. Follow the road as far as the farmers arms then take the next left
- 4. The house is on the corner by the garage.

If you think about these instructions in the abstract what you have is a set of way markers (the item I have put in bold) in a particular order. The list of way markers is important as is the order they appear in in the instructions so we incorporate both these items in the PATH coordinates that we have just used to study the transition between the transition between C7eq and C7ax. In these coordinates the way markers are a set of interesting points in a high dimensional space. In other words, these are like the configurations of C7eq and C7ax that we used in the previous sections when talking about PCAVARS. Each of these configurations lies along the path connecting C7eq and C7ax and, as in the directions example above, one must pass them in a particular order in order to pass between these two conformations. The final CV that we have used above is thus:

$$S(X) = \frac{\sum_{i=1}^{N} i \exp^{-\lambda|X - X_i|}}{\sum_{i=1}^{N} \exp^{-\lambda|X - X_i|}}$$

In this expression  $|X-X_i|$  is the distance between the instaneous coordinate of the system, X, in the high-dimensional space and  $X_i$  is the coordinate of the ith waymark in the path. The largest exponential in the sum that appears in the numerator and the denominator will thus be the one that corresponds to the point that is closest to where the system currently lies. In other words, S(X), measures the position on a (curvilinear) path that connects two states of interest as shown in red in the figure below:

#### 12.16.4.6 The Z(X) collective variable

You may reasonably ask what the purpose these PATH collective variables variables serve given that in this case they seem to do no better than  $\phi$  when it comes to the tests we have performed on calculating the isocomittor. To answer this question we are going to run one final set of isocommittor simulations. The input for these calculations are in the directory called 2GV-isocommitor. Once again you will find that there is a script.sh bash script inside this directory, which, as in the previous section, you can use to run a large number of molecular dynamics simulation. Furthermore, similarly to the last section you will need to begin this exercise by modifying the location of path to gromacs within this script. Once you have made this modification submit your molecular dynamics jobs by issuing the command:

```
./script.sh
```

You can then plot the data output using gnuplot and the commands:

```
load "script_pca.gplt"
and
```

load "script\_path.gplt"

What is plotted by these commands is slightly different from what was plotted in the previous exercises where we calculated the isocommittor. Instead of plotting the value of the CV against simulation time the above commands plot the values that 2CVs take during the simulation. The script called script\_path.gplt plots the value of the S(X) collective variable on the x-axis and the value of the following quantity on the y-axis:

$$Z(X) = -\frac{1}{\lambda} \log(\sum_{i=1}^{N} \exp^{-\lambda|X - X_i|})$$

What this quantity measures is shown in green in the figure belfast-2-ab-sz-fig. Essentially it measures the distance between the instantaneous configuration the system finds itself in and the path that is marked out using the way-markers. If you plot the data using script\_path.gplt what you thus see is that the system never moves very far from the path that is defined using the PATH command. In short the system follows this path from the transition state back to either the C7eq or C7ax configuration.

We can calculate a quantity similar to Z(X) for the PCAVARS collective variables. Furthermore, when we plot the data we have generated using this exercise using script\_pca.gplt the value this quantity takes is shown plotted against the instantaneous value of the PCAVARS collective variable. If you compare this graph with what was obtained when you plotted the output from PATH above you see that the system has moved very far from the PCAVARS coordinate.

This exercise illustrates the strength of these PATH collective variables. We can use a PATH to monitor how a large number of coordinates change during a chemical transition. Furthermore, we can use Z(X) to measure how much real trajectories deviate from our PATH and thus have a quantitative measure of how well our PATH represents the true transition mechanism. Compare this with using a single CV such as  $\phi$ . When use use a single CV we map the high-dimensional data from the traejctory into a lower dimensional space. We thus lose some information on what occurs during the transition. To be clear we also loose information on the what occurs during the transition when we use PATH as any mapping into a lower dimensional space deletes information. In the PATH case, however, we can use the value of Z(X) to measure how much data has been lost in mapping the trajectory onto S(X).

These two coordinates, S(X) and Z(X), are very flexible. They are thus been used widely in the literature on modelling conformational changes of biomolecules. A part of this flexibility comes because one can use any set of waymarkers to define the PATH. Another flexibility comes, however, when you recognise that you can also change the way in which the distance,  $|X-X_i|$ , is calculated in the two formulas above. For example this distance can be calculated using the RMSD distance or it can be calculated by mesauring the sum of the squares of a set of displacements in collective variable values (see TARGET). Changing the manner in which the distance between path way points is calculated thus provides a way to control the level of detail that is incorporated in the description of the reaction PATH.

### 12.16.4.7 Optimising path collective variables

Hopefully the previous sections have allowed you to understand how PATH collective variables work and the sorts of problems they might be used to solve. If you have one of these problems to solve the next reasonable question to ask is: how to collect the set of reference frames that serve as the waymarkers on your PATH. Unfortunately, there is no single answer to this question. Different researchers have used different methods including using packages that morph one protein structure into another, using information from prior molecular dynamics or ehnanced sampling calculations and even using PATH collective variables that change adaptively as the simulation progresses. Ultimately, you will need to find the best method for solving your particular problem. Having said that, however, there is some general guidance on setting up PATH collective variable and it is this that we will focus on in this section. The first thing that you will need to double check is the set of spacings between all the frames in your PATH. Lets suppose that your PATH has N of these way markers upon it you will need to calculate is the  $N \times N$  matrix of distances between way markers. That is to say you will have to calculate the distance  $|X_j - X_i|$  between each pair of frames. The values of the distance in this matrix for a good PATH are shown in the figure below:

For contrast the values of the distances in this matrix for a bad PATH are shown in the figure below:

If the distance matrix looks like the second of the two figures shown above this is indicates that the frames in the PATH that have been chosen are not particularly effective. Lets suppose that we have a PATH with four way markers upon it. In order for the S(x) CV that was defined earlier to work well frame number 3 must be further from frame number 1 than frame number 2. Similarly frame number 4 must be still further from frame number 1 than frame number 3. This is what the gullwing shape in belfast-2-good-matrix-fig is telling us. The order of the frames in the rows and columns of the matrix is the same as the order that they are run through in the sums in the equation for S(X). The shape of the surface in this figure shows that the distance between frames i and j increases monotonically as the magnitude of the difference between i and j is increased, which is what is required.

A second important requirement of a good PATH is shown in the figure below:

A good PATH has an approximately equal spacing between the neighbouring frames along it. In other words, the distance between frame 1 and frame 2 is approximately equal to the distance between frame 2 and frame 3 as shown above. When this condition is satisfied a good criterion for selecting a suitable  $\lambda$  parameter to use is:

$$\lambda = \frac{2.3(N-1)}{\sum_{i=1}^{N-1} |X_i - X_{i+1}|}$$

### 12.16.5 Conclusions and further work

If you have worked through all of this tutorial make sure that you have understood it by ensuring that you understand what the list of learning outcomes in section Learning Outcomes means and that you can use PLUMED to perform all these tasks. You might then want to read the original paper on the PATH collective variable method as well as a few other articles in which these coordinates have been used to analyse simulations and to accelerate sampling.

 Davide Branduardi and Francesco Luigi Gervasio and Michele Parrinello From A to B in free energy space J. Chem. Phys., 126, 054103 (2007)

If you are interested in learning more about isocommitor surfaces and the transition state ensemble you should read up on the transition path sampling method.

# 12.17 Moving from PLUMED 1 to PLUMED 2

Syntax in PLUMED 2 has been completely redesigned based on our experience using PLUMED 1, hopefully makeing it clearer, more flexible, and less error prone. The main difference is that whereas in PLUMED 1 lines could be inserted in any order, in PLUMED 2 the order of the lines matters. This is due to a major change in the internal architecture of PLUMED. In version 2, commands (or "actions") are executed in the order they are found in the input file. Because of this, you must e.g. first compute a collective variable and then print it later. More information can be found in the Section about Getting started.

Other important changes are in the way groups and units are used, as discussed below. Finally, many features appear under a different name in the new version.

### 12.17.1 New syntax

We know that changing the input syntax requires a lot of work from the user side to update their input files. However, we believe that the new syntax is easier to read and that it allows for more flexibility. As an example, something that in PLUMED 1.3 was:

```
HILLS HEIGHT 0.4 W_STRIDE 600
WELLTEMPERED SIMTEMP 300 BIASFACTOR 15
RGYR LIST <all>
all->
1 5 6 7 9 11 15 16 17 19
all<-
TORSION LIST 5 7 9 15 SIGMA 0.1
TORSION LIST 7 9 15 17
PRINT W_STRIDE 100
```

#### in PLUMED 2.x becomes:

```
all: GROUP ATOMS=1,5,6,7,9,11,15,16,17,19
rg: GYRATION ATOMS=all
t1: TORSION ATOMS=5,7,9,15
METAD ...
LABEL=meta
ARG=t1 SIGMA=0.1 HEIGHT=0.4 PACE=600
BIASFACTOR=15 TEMP=300
... METAD
t2: TORSION ATOMS=7,9,15,17
PRINT ARG=t1,t2,meta.bias STRIDE=100 FILE=COLVAR
```

Giving all quantities an explicit name makes the input easier to interpret. Additionally, all the parameters related to METAD are placed on a single line (actually, this is done here exploiting continuation lines). Also notice that one can customize the name of the COLVAR file. By specifying to PRINT which collective variables should be printed, one can easily decide what to print exactly and using which stride. By repeating the PRINT line one can also monitor very expensive variables with a larger stride, just putting the result on a separate file.

You might have noticed that ideas that were very difficult to implement in PLUMED 1.3 now become immediately available. As an example, one can now apply concurrently several METAD potentials ? .

## 12.17.2 Groups

In PLUMED 1 groups (lists) were used for two tasks:

- To provide centers of masses to collective variables such as distances, angles, etc. This is now done by defining virtual atoms using either CENTER or COM
- To provide lists of atoms to collective variables such as coordination, gyration radius, etc. This is now done directly in the line that defines the collective variable.

If you would still like to use groups you can use the GROUP commands. Whenever the label for a GROUP action appears in the input it is replaced by the list of atoms that were specified in the GROUP.

A restraint on the distance between centers of mass in PLUMED 1 was something like:

```
DISTANCE LIST <g1> <g2> g1->
17 20 22 30 g1<-
g2->
LOOP 37 40 g2<-
UMBRELLA CV 1 KAPPA 200 AT 1.0
PRINT W_STRIDE 100
```

#### The same in PLUMED 2.x reads:

```
g1: COM ATOMS=17,20,22,30
g2: COM ATOMS=37-40
d: DISTANCE ATOMS=g1,g2
r: RESTRAINT ARG=d KAPPA=200 AT=1.0
PRINT STRIDE=100 FILE=COLVAR ARG=d,r.*
```

Notice that virtual atoms are very powerful tools in PLUMED 2. Actually, they can be used in any collective variable where normal atoms can be used, just by calling them by name. This allows to straightforwardly define variables such as coordination between centers of mass, which would have required an ad hoc implementation in PLUMED 1

In the example above you can also appreciate the advantage of calling collective variables by name. It is obvious here that RESTRAINT is acting on distance d, whereas in PLUMED 1 one had to keep track of the number of the collective variables. This was easy for a single collective variable, but could become cumbersome for complex input files.

## 12.17.3 Names in output files

Another advantage of having names is that when PLUMED produces an output file it can insert explicit names in the file. Consider for example this PLUMED 1 input

```
DISTANCE LIST 1 2
ANGLE LIST 3 4 5
PRINT W_STRIDE 100
```

The first line of the COLVAR file was then

```
#! FIELDS time cv1 cv2
```

The equivalent input file in PLUMED 2 is

```
d: DISTANCE ATOMS=1,2
a: ANGLE ATOMS=3,4,5
PRINT ARG=d,a FILE=COLVAR STRIDE=100
```

The first line of the COLVAR file now is

```
#! FIELDS time d a
```

This makes it easy to remember what's the meaning of each column of the COLVAR file without the need to always go back to the PLUMED input to check in which order the variables were declared.

## 12.17.4 Units

In PLUMED 1 the input file of PLUMED was expected to be written using the same units of the MD code. This choice was made to allow users to adopt the same units they were used to. However, we realized later that this choice was not allowing the PLUMED input files to be ported between different MD code. Let's say that one was using this keyword with GROMACS (kj/mol - nm)

```
UMBRELLA CV 1 KAPPA 200 AT 1.0
```

Let's assume the variable CV 1 was a distance. The same keyword in NAMD (kcal/mol - A) should have been converted to

```
UMBRELLA CV 1 KAPPA .4780 AT 10.0
```

The conversion of AT is straightforward (1nm=10A), but the conversion on KAPPA is more error prone. This is because KAPPA is measured in units of energy divided by distance squared. Notice that a different factor should have been used if the CV was an angle.

Learning from this, we designed PLUMED 2 in a way that units in the PLUMED input are independent of the MD code. Technically, this is achieved by doing the conversion when coordinates and forces are passed back and forth. In this way, the same PLUMED input could be used with GROMACS and NAMD.

We decided to use as standard units in PLUMED kj/mol, nm, and ps. Perhaps this is because most of the developers are using GROMACS, which also adopts these units. However, we still allow the personalization of units by means of the UNITS keyword. Since this keyword is included directly in the PLUMED input file, even when using personalized units the input files remains perfectly portable across different MD engines.

## 12.17.5 Directives

What follows is a list of all the documented directives of PLUMED 1 together with their plumed 2 equivalents. Be aware that the input syntaxes for these directives are not totally equivalent. You should read the documentation for the PLUMED 2 Action.

| HILLS            | METAD  |
|------------------|--|
| WELLTEMPERED     | METAD with BIASFACTOR  |
| GRID             | METAD with GRID_MIN, GRID_MAX, and GRID_BIN  |
| WRITE_GRID       | METAD with GRID_WFILE, GRID_WSTRIDE  |
| READ_GRID        | METAD with GRID_RFILE  |
| MULTIPLE_WALKERS | METAD with options WALKERS_ID, WALKERS_N, WALKERS_DIR, and WALKE⇔ RS_RSTRIDE   |
| NOHILLS          | not needed (collective variables are not biased by default)  |
| INTERVAL         | METAD with INTERVAL  |
| INVERT           | currently missing  |
| PTMETAD          | not needed (replica exchange detected from MD engine)  |
| BIASXMD          | not needed (replica exchange detected from MD engine); one should anyway use RANDOM_EXCHANGES to get the normal behavior |
| UMBRELLA         | RESTRAINT  |
| STEER            | MOVINGRESTRAINT  |
| STEERPLAN        | MOVINGRESTRAINT  |
| ABMD             | ABMD   |
| UWALL            | UPPER_WALLS  |
| LWALL            | LOWER_WALLS  |
| EXTERNAL         | EXTERNAL   |

| COMMITMENT   | COMMITTOR   |  |  |
|--------------|---|--|--|
| PROJ_GRAD    | DUMPPROJECTIONS   |  |  |
| DAFED        | a similar method using a Langevin thermostat, with EXTENDED_LAGRANGIAN  |  |  |
| DISTANCE     | DISTANCE - POINT_FROM_AXIS and PROJ_ON_AXIS can be reproduced with D←   |  |  |
|              | ISTANCE and MATHEVAL  |  |  |
| POSITION     | POSITION  |  |  |
| MINDIST      | DISTANCES with keyword MIN  |  |  |
| ANGLE        | ANGLE   |  |  |
| TORSION      | TORSION   |  |  |
| COORD        | COORDINATION  |  |  |
| HBOND        | currently missing, can be emulated with COORDINATION                    |  |  |
| WATERBRIDGE  | BRIDGE  |  |  |
| RGYR         | GYRATION  |  |  |
| DIPOLE       | DIPOLE  |  |  |
| DIHCOR       | DIHCOR  |  |  |
| ALPHABETA    | ALPHABETA   |  |  |
| ALPHARMSD    | ALPHARMSD   |  |  |
| ANTIBETARMSD | ANTIBETARMSD  |  |  |
| PARABETARMSD | PARABETARMSD  |  |  |
| ELSTPOT      | currently missing, but a related quantity can be obtained with DHENERGY |  |  |
| PUCKERING    | PUCKERING   |  |  |
| S_PATH       | PATHMSD, s component  |  |  |
| Z_PATH       | PATHMSD, z component  |  |  |
| TARGETED     | RMSD  |  |  |
| ENERGY       | ENERGY  |  |  |
| HELIX        | currently missing   |  |  |
| PCA          | PCARMSD   |  |  |
| SPRINT       | SPRINT  |  |  |
| RDF          | DISTANCES, used in combination with HISTOGRAM / BETWEEN keyword         |  |  |
| ADF          | ANGLES, used in combination with HISTOGRAM / BETWEEN keyword            |  |  |
| POLY         | COMBINE   |  |  |
| FUNCTION     | MATHEVAL  |  |  |
| ALIGN_ATOMS  | WHOLEMOLECULES  |  |  |

## 12.18 Munster tutorial

## **Authors**

Max Bonomi and Giovanni Bussi, stealing a lot of material from other tutorials. Richard Cunha is acknowledged for beta-testing this tutorial.

#### Date

March 11, 2015

This document describes the PLUMED tutorial held in Munster, March 2015. The aim of this tutorial is to learn how to use PLUMED to analyze molecular dynamics simulations on the fly, to analyze existing trajectories, and to perform enhanced sampling. Although the presented input files are correct, the users are invited to **refer to the literature to understand how the parameters of enhanced sampling methods should be chosen in a real application.** 

Users are also encouraged to follow the links to the full PLUMED reference documentation and to wander around in the manual to discover the many available features and to do the other, more complete, tutorials. Here we are going to present only a very narrow selection of methods.

We here use PLUMED 2.1 syntax and we explicitly note if some syntax is expected to change in PLUMED 2.2, which will be released later in 2015. All the tests here are performed on a toy system, alanine dipeptide, simulated using the AMBER99SB force field. We provide both a setup that includes explicit water, which is more realistic but slower, and a setup in gas phase, which is much faster. Simulations are made using GROMACS 4.6.7, which is here assumed to be already patched with PLUMED and properly installed. However, these examples could be easily converted to other MD software.

All the gromacs input files and analyss scripts are provided in this tarball.

Users are expected to write PLUMED input files based on the instructions below.

## 12.18.1 Alanine dipeptide: our toy model

In this tutorial we will play with alanine dipeptide (see Fig. munster-1-ala-fig). This rather simple molecule is useful to make benchmark that are around for data analysis and free energy methods. It is a nice example since it presents two metastable states separated by a high (free) energy barrier. Here metastable states are intended as states which have a relatively low free energy compared to adjacent conformations. It is conventional use to show the two states in terms of Ramachandran dihedral angles, which are denoted with  $\Phi$  and  $\Psi$  in Fig. munster-1-transition-fig.

#### 12.18.2 Monitoring collective variables

The main goal of PLUMED is to compute collective variables, which are complex descriptors than can be used to analyze a conformational change or a chemical reaction. This can be done either on the fly, that is during molecular dynamics, or a posteriori, using PLUMED as a post-processing tool. In both cases one should create an input file with a specific PLUMED syntax. A sample input file is below:

```
# compute distance between atoms 1 and 10
d: DISTANCE ATOMS=1,10
# create a virtual atom in the center between atoms 20 and 30
center: CENTER ATOMS=20,30
# compute torsional angle between atoms 1,10,20 and center
phi: TORSION ATOMS=1,10,20,center
# compute some function of previously computed variables
d2: MATHEVAL ARG=phi FUNC=cos(x) PERIODIC=NO
# print both of them every 10 step
PRINT ARG=d,phi,d2 STRIDE=10
```

## (see DISTANCE, CENTER, TORSION, MATHEVAL, and PRINT)

PLUMED works using kJ/nm/ps as energy/length/time units. This can be personalized using UNITS. Notice that variables should be given a name (in the example above, d, phi, and d2), which is then used to refer to these variables. Lists of atoms should be provided as comma separated numbers, with no space. Virtual atoms can be created and assigned a name for later use. You can find more information on the PLUMED syntax at Getting started page of the manual. The complete documentation for all the supported collective variables can be found at the Collective variables page.

#### 12.18.2.1 Analyze on the fly

Here we will run a plain MD on alanine dipeptide and compute two torsional angles on the fly. GROMACS needs a .tpr file, which is a binary file containing initial positions as well as force-field parameters. We also provide .gro, .mdp, and .top files, that can be modified and used to generate a new .tpr file. For this tutorial, it is sufficient to use the provided .tpr files. You will find several tpr files, namely:

- · topolAwat.tpr setup in water, initialized in state A
- · topolBwat.tpr setup in water, initialized in state B
- topolA.tpr setup in vacuum, initialized in state A
- · topolB.tpr setup in vacuum, initialized in state B

Gromacs md can be run using on the command line:

```
> gmx_mpi mdrun -s topolA.tpr -nsteps 10000
```

The nsteps flags can be used to change the number of timesteps and topolA.tpr is the name of the tpr file. While running, gromacs will produce an md.log file, with log information, and a traj.xtc file, with a binary trajectory. The trajectory can be visualized with VMD using a command such as

```
> vmd confout.gro tra.xtc
```

To run a simulation with gromacs+plumed you just need to add a -plumed flag

```
> gmx_mpi mdrun -s topolA.tpr -nsteps 10000 -plumed.dat
```

Here plumed.dat is the name of the plumed input file. Notice that PLUMED will write information in the md.log that could be useful to verify if the simulation has been set up properly.

#### 12.18.2.1.1 Exercise 0

In this exercise, we will run a plain molecular dynamics simulation and monitor the  $\Phi$  and  $\Psi$  dihedral angles on the fly. Using the following PLUMED input file you can monitor  $\Phi$  and  $\Psi$  angles during the MD simulation

```
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
PRINT ARG=phi,psi STRIDE=100 FILE=colvar
```

## (see TORSION and PRINT)

Notice that PLUMED is going to compute the collective variables only when necessary, that is, in this case, every 100 steps. This is not very relevant for simple variables such as torsional angles, but provides a significant speedup when using expensive collective variables.

PLUMED will write a textual file named colvar containing three columns: physical time,  $\Phi$  and  $\Psi$ . Results can be plotted using gnuplot:

```
> gnuplot
# this shows phi as a function of time
gnuplot> plot "colvar" u 2
# this shows psi as a function of time
gnuplot> plot "colvar" u 3
# this shows psi as a function of phi
gnuplot> plot "colvar" u 2:3
```

Now try to do the same using the two different initial configurations that we provided (topolA.tpr and topol  $\leftarrow$  B.tpr). You can try both setup (water and vacuum). Results from 200ps (100000 steps) trajectories in vacuum are shown in Figure munster-ala-traj.

Notice that the result depends heavily on the starting structure. For the simulation in vacuum, the two free-energy minima are separated by a large barrier and, in such a short simulation, the system cannot cross it. In water the barrier is smaller and you might see some crossing. Also notice that the two clouds are well separated, indicating that these two collective variables are good enough to properly distinguish among the two minima.

As a final comment, notice that if you run twice the same calculation in the same directory, you might overwrite the resulting files. GROMACS takes automatic backup of the output files, and PLUMED does it as well. In case you are restarting a simulation, you can add the keyword RESTART at the beginning of the PLUMED input file. This will tell PLUMED to *append* files instead of taking a backup copy.

## 12.18.2.2 Analyze using the driver

Imagine you already made a simulation, with or without PLUMED. You might want to compute the collective variables a posteriori, from the trajectory file. You can do this by using the plumed executable on the command line. Type

```
> plumed driver --help
```

to have an idea of the possible options. See driver for the full documentation.

Here we will use the driver the compute  $\Phi$  and  $\Psi$  on the already generated trajectory. Let's assume the trajectory is named traj.xtc. You should prepare an PLUMED input file named analysis.dat as:

```
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
PRINT ARG=phi,psi FILE=analysis
```

(see TORSION and PRINT) Notice that typically when using the driver we do not provide a STRIDE keyword to PRINT. This implies "print at every step" which, analyzing a trajectory, means "print for all the available snapshots". Then, you can use the following command:

```
> plumed driver --mf_xtc traj.xtc --plumed analysis.dat
```

Notice that PLUMED has no way to now the value of physical time from the trajectory. If you want physical time to be printed in the analysis file you should give more information to the driver, e.g.:

```
> plumed driver --mf_xtc traj.xtc --plumed analysis.dat --timestep 0.002 --trajectory-stride 1000
```

(see driver)

In this case we inform the driver that the traj.xtc file was produced in a run with a timestep of 0.002 ps and saving a snapshop every 1000 timesteps.

You might want to analyze a different collective variable, such as the gyration radius. The gyration radius tells how extended is the molecules in space. You can do it with the following plumed input file

```
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17

heavy: GROUP ATOMS=1,5,6,7,9,11,15,16,17,19
gyr: GYRATION ATOMS=heavy

# the same could have been achieved with
# gyr: GYRATION ATOMS=1,5,6,7,9,11,15,16,17,19

PRINT ARG=phi,psi,gyr FILE=analyze
```

(see TORSION, GYRATION, GROUP, and PRINT)

Now try to compute the time series of the gyration radius.

#### 12.18.2.3 Periodic boundaries and explicit water

In case you are running the simulation in water, you might see that at some point this variable shows some crazy jump. The reason is that the trajectory containes coordinates where molecules are broken across periodic-boundary conditions. This happens with GROMACS and some other MD code. These codes typically have tools to process trajecories and restore whole molecules. This trick is ok for the a-posteriori analysis we are trying now, but cannot used when one needs to compute a collective variable on-the-fly or, as we will see later, one wants to add a bias to that collective variable. For this reason, we implemented a workaround in PLUMED, that is the molecule should be made whole using the WHOLEMOLECULES command. What this command is doing is making a loop over all the atoms (in the order they are provided) and set the coordinates of each of them in the periodic image which is as close as possible to the coordinates of the preceeding atom. In most cases it is sufficient to list all atoms of a molecule in order. Look in the WHOLEMOLECULES page to get more information. Here this will be enough:

```
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17

# notice the 1-22 syntax, a shortcut for a list 1,2,3,...,22
WHOLEMOLECULES ENTITY0=1-22
heavy: GROUP ATOMS=1,5,6,7,9,11,15,16,17,19
gyr: GYRATION ATOMS=heavy
PRINT ARG=phi,psi,gyr FILE=analyze
```

(see TORSION, WHOLEMOLECULES, GROUP, GYRATION, and PRINT)

This is a very important issue that should be kept in mind when using PLUMED. Notice that starting with version 2.2 PLUMED will make molecules used in GYRATION (as well as in other variables) whole automatically, so that this extra command will not be necessary.

Notice that you can instruct PLUMED to dump on a file not only the collective variables (as we are doing with PRINT) but also the atomic positions. This is a very good way to understand what WHOLEMOLECULES is actually doing. Try the following input

```
MOLINFO STRUCTURE=../TOPO/reference.pdb
DUMPATOMS FILE=test1.gro ATOMS=1-22
WHOLEMOLECULES ENTITY0=1-22
DUMPATOMS FILE=test2.gro ATOMS=1-22
```

(see MOLINFO, DUMPATOMS, and WHOLEMOLECULES).

DUMPATOMS writes on a gro file the coordinates of the alanine dipeptide atoms. Here PLUMED will produce two files, one with coordinates *before* the application of WHOLEMOLECULES, and one with coordinates after\* the application of WHOLEMOLECULES. You can load both trajectories in VMD to see the difference. The MOLINFO command is here used to provide atom names to PLUMED so that the resulting gro file looks nicer in VMD.

Notice that PLUMED has several commands that manipulate atomic coordinates. One example is WHOLEMOL ECULES, that fixes problems with periodic boundary conditions. COM and CENTER add new atoms, and FIT TO\_TEMPLATE can actually move atoms from their original position to align them on a template. DUMPATOMS is this very useful to check what these commands are doing and for using the PLUMED driver to manipulate MD trajectories.

## 12.18.2.4 Other analysis tools

PLUMED also allows you to make some analyis on the collective variables you are calculating. For example, you can compute a histogram with an input like this one

```
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
heavy: GROUP ATOMS=1,5,6,7,9,11,15,16,17,19
gyr: GYRATION ATOMS=heavy
PRINT ARG=phi,psi,gyr FILE=analyze
HISTOGRAM ...
ARG=gyr
USE_ALL_DATA
KERNEL=discrete
GRID_MIN=0
GRID_MAX=1
GRID_BIN=50
GRID_WFILE=histogram
... HISTOGRAM
```

#### (see TORSION, WHOLEMOLECULES, GROUP, GYRATION, PRINT, and HISTOGRAM)

An histogram with 50 bins will be performed on the gyration radius. Try to compute the histogram for the  $\Phi$  and  $\Psi$  angles.

PLUMED can do much more than a histogram, more information on analysis can be found at the page Analysis

Notice that the plumed driver can also be used directly from VMD taking advantage of the PLUMED collective variable tool developed by Toni Giorgino (http://multiscalelab.org/utilities/PlumedGUI). Just open a recent version of VMD and go to Extensions/Analysis/Collective Variable Analysis (PLUMED). This graphical interface can also be used to quickly build PLUMED input files based on template lines.

#### 12.18.3 Biasing collective variables

We have seen that PLUMED can be used to compute collective variables. However, PLUMED is most often use to add forces on the collective variables. To this aim, we have implemented a variety of possible biases acting on collective variables. A bias works in a manner conceptually similar to the PRINT command, taking as argument one or more collective variables. However, here the STRIDE is usually omitted (that is equivalent to setting it to 1), which means that forces are applied at every timestep. In PLUMED 2.2 you will be able to change the STRIDE also for bias potentials, but that's another story. In the following we will see how to apply harmonic restraints and how to build an adaptive bias potential with metadynamics. The complete documentation for all the biasing methods available in PLUMED can be found at the Bias page.

## 12.18.3.1 Metadynamics

## 12.18.3.1.1 Summary of theory

In metadynamics, an external history-dependent bias potential is constructed in the space of a few selected degrees of freedom  $\vec{s}(q)$ , generally called collective variables (CVs) ?. This potential is built as a sum of Gaussians deposited along the trajectory in the CVs space:

$$V(\vec{s},t) = \sum_{k\tau < t} W(k\tau) \exp\left(-\sum_{i=1}^{d} \frac{(s_i - s_i(q(k\tau)))^2}{2\sigma_i^2}\right).$$

where  $\tau$  is the Gaussian deposition stride,  $\sigma_i$  the width of the Gaussian for the ith CV, and  $W(k\tau)$  the height of the Gaussian. The effect of the metadynamics bias potential is to push the system away from local minima into visiting new regions of the phase space. Furthermore, in the long time limit, the bias potential converges to minus the free energy as a function of the CVs:

$$V(\vec{s}, t \to \infty) = -F(\vec{s}) + C.$$

In standard metadynamics, Gaussians of constant height are added for the entire course of a simulation. As a result, the system is eventually pushed to explore high free-energy regions and the estimate of the free energy calculated from the bias potential oscillates around the real value. In well-tempered metadynamics ?, the height of the Gaussian is decreased with simulation time according to:

$$W(k\tau) = W_0 \exp\left(-\frac{V(\vec{s}(q(k\tau)), k\tau)}{k_B \Delta T}\right),\,$$

where  $W_0$  is an initial Gaussian height,  $\Delta T$  an input parameter with the dimension of a temperature, and  $k_B$  the Boltzmann constant. With this rescaling of the Gaussian height, the bias potential smoothly converges in the long time limit, but it does not fully compensate the underlying free energy:

$$V(\vec{s}, t \to \infty) = -\frac{\Delta T}{T + \Delta T} F(\vec{s}) + C.$$

where T is the temperature of the system. In the long time limit, the CVs thus sample an ensemble at a temperature  $T+\Delta T$  which is higher than the system temperature T. The parameter  $\Delta T$  can be chosen to regulate the extent of free-energy exploration:  $\Delta T=0$  corresponds to standard molecular dynamics,  $\Delta T\to\infty$  to standard metadynamics. In well-tempered metadynamics literature and in PLUMED, you will often encounter the term "biasfactor" which is the ratio between the temperature of the CVs ( $T+\Delta T$ ) and the system temperature (T):

$$\gamma = \frac{T + \Delta T}{T}.$$

The biasfactor should thus be carefully chosen in order for the relevant free-energy barriers to be crossed efficiently in the time scale of the simulation.

Additional information can be found in the several review papers on metadynamics???

If you do not know exactly where you would like your collective variables to go, and just know (or suspect) that some variables have large free-energy barriers that hinder some conformational rearrangement or some chemical reaction, you can bias them using metadynamics. In this way, a time dependent, adaptive potential will be constructed that tends to disfavor visited configurations in the collective-variable space. The bias is usually built as a sum of Gaussian deposited in the already visited states.

#### 12.18.3.1.2 Exercise 1

Now run a metadynamics simulation with the following input

```
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
METAD ARG=phi,psi HEIGHT=1.0 BIASFACTOR=10 SIGMA=0.35,0.35 PACE=100 GRID_MIN=-pi,-pi GRID_MAX=pi,pi
```

(see TORSION and METAD) Thus, a single METAD line will contain all the metadynamics related options, such as Gaussian height (HEIGHT, here in kJ/mol), stride (PACE, here in number of time steps), bias factor (BIASFAC TOR, here indicates that we are going to effectively boost the temperature of the collective variables by a factor 10), and width (SIGMA, an array with same size as the number of collective variables).

There are two additional keywords that are optional, namely GRID\_MIN and GRID\_MAX. These keywords sets the range of the collective variables and tell PLUMED to keep the bias potential stored on a grid. This affects speed but, in principle, not the accuracy of the calculation. You can try to remove those keywords and see the difference.

Now, run a metadynamics simulations and check the explored collective variable space. Results from a 200ps (100000 steps) trajectory in vacuum are shown in Figure munster-ala-traj-metad.

As you can see, exploration is greatly enhanced. Notice that the explored ensemble can be tuned using the biasfactor  $\gamma$ . Larger  $\gamma$  implies that the system will explore states with higher free energy. As a rule of thumb, if you expect a barrier of the order of  $\Delta G^*$ , a reasonable choice for the biasfactor is  $\gamma \approx \frac{\Delta G}{2k_BT}$ .

Finally, notice that METAD potential depends on the previously visited trajectories. As such, when you restart a previous simulation, it should read the previously deposited HILLS file. This is automatically triggered by the RESTART keyword.

#### 12.18.3.1.3 Exercise 2

In this exercise, we will run a well-tempered metadynamics simulation on alanine dipeptide in vacuum, using as CV the backbone dihedral angle phi. In order to run this simulation we need to prepare the PLUMED input file (plumed.dat) as follows.

```
# set up two variables for Phi and Psi dihedral angles
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
# Activate well-tempered metadynamics in phi depositing
# a Gaussian every 500 time steps, with initial height equal
# to 1.2 kJoule/mol, biasfactor equal to 10.0, and width to 0.35 rad
METAD ...
LABEL=metad
ARG=phi
PACE=500
HEIGHT=1.2
SIGMA=0.35
FILE=HILLS
BIASFACTOR=10.0
TEMP=300.0
GRID_MIN=-pi
GRID_MAX=pi
GRID_SPACING=0.1
... METAD
# monitor the two variables and the metadynamics bias potential
PRINT STRIDE=10 ARG=phi,psi,metad.bias FILE=COLVAR
```

```
(see TORSION, METAD, and PRINT).
```

The syntax for the command METAD is simple. The directive is followed by a keyword ARG followed by the labels of the CVs on which the metadynamics potential will act. The keyword PACE determines the stride of Gaussian deposition in number of time steps, while the keyword HEIGHT specifies the height of the Gaussian in kJoule/mol. For each CVs, one has to specified the width of the Gaussian by using the keyword SIGMA. Gaussian will be written to the file indicated by the keyword FILE.

The bias potential will be stored on a grid, whose boundaries are specified by the keywords GRID\_MIN and GR ← ID\_MAX. Notice that you should provide either the number of bins for every collective variable (GRID\_BIN) or the desired grid spacing (GRID\_SPACING). In case you provide both PLUMED will use the most conservative choice (highest number of bins) for each dimension. In case you do not provide any information about bin size (neither GRID\_BIN nor GRID\_SPACING) and if Gaussian width is fixed PLUMED will use 1/5 of the Gaussian width as grid spacing. This default choice should be reasonable for most applications.

Once the PLUMED input file is prepared, one has to run Gromacs with the option to activate PLUMED and read the input file:

```
gmx\_mpi mdrun -s ../TOPO/topolA.tpr -plumed plumed.dat -nsteps 5000000
```

During the metadynamics simulation, PLUMED will create two files, named COLVAR and HILLS. The COLVAR file contains all the information specified by the PRINT command, in this case the value of the CVs every 10 steps of simulation, along with the current value of the metadynamics bias potential. We can use COLVAR to visualize the behavior of the CV during the simulation:

By inspecting Figure munster-metad-phi-fig, we can see that the system is initialized in one of the two metastable states of alanine dipeptide. After a while (t=0.1 ns), the system is pushed by the metadynamics bias potential to visit the other local minimum. As the simulation continues, the bias potential fills the underlying free-energy landscape, and the system is able to diffuse in the entire phase space.

The HILLS file contains a list of the Gaussians deposited along the simulation. If we give a look at the header of this file, we can find relevant information about its content:

```
#! FIELDS time phi psi sigma_phi sigma_psi height biasf
#! SET multivariate false
#! SET min_phi -pi
#! SET max_phi pi
#! SET min_psi -pi
#! SET max_psi pi
```

The line starting with FIELDS tells us what is displayed in the various columns of the HILLS file: the time of the simulation, the value of phi and psi, the width of the Gaussian in phi and psi, the height of the Gaussian, and the biasfactor. We can use the HILLS file to visualize the decrease of the Gaussian height during the simulation, according to the well-tempered recipe:

If we look carefully at the scale of the y-axis, we will notice that in the beginning the value of the Gaussian height is higher than the initial height specified in the input file, which should be 1.2 kJoule/mol. In fact, this column reports the height of the Gaussian rescaled by the pre-factor that in well-tempered metadynamics relates the bias potential to the free energy. In this way, when we will use <a href="mailto:sum\_hills">sum\_hills</a>, the sum of the Gaussians deposited will directly provide the free-energy, without further rescaling needed (see below).

One can estimate the free energy as a function of the metadynamics CVs directly from the metadynamics bias potential. In order to do so, the utility sum\_hills should be used to sum the Gaussians deposited during the simulation and stored in the HILLS file. To calculate the free energy as a function of phi, it is sufficient to use the following command line:

```
plumed sum_hills --hills HILLS
```

The command above generates a file called fes.dat in which the free-energy surface as function of phi is calculated on a regular grid. One can modify the default name for the free energy file, as well as the boundaries and bin size of the grid, by using the following options of sum\_hills:

```
--outfile - specify the outputfile for sumhills
--min - the lower bounds for the grid
--max - the upper bounds for the grid
--bin - the number of bins for the grid
--spacing - grid spacing, alternative to the number of bins
```

The result should look like this:

To assess the convergence of a metadynamics simulation, one can calculate the estimate of the free energy as a function of simulation time. At convergence, the reconstructed profiles should be similar. The option –stride should be used to give an estimate of the free energy every N Gaussians deposited, and the option –mintozero can be used to align the profiles by setting the global minimum to zero. If we use the following command line:

```
plumed sum_hills --hills HILLS --stride 100 --mintozero
```

one free energy is calculated every 100 Gaussians deposited, and the global minimum is set to zero in all profiles. The resulting plot should look like the following:

To assess the convergence of the simulation more quantitatively, we can calculate the free-energy difference between the two local minima of the free energy along phi as a function of simulation time. We can use following script to integrate the multiple free-energy profiles in the two basins defined by the following intervals in phi space: basin A, -3<phi<-1, basin B, 0.5<phi<1.5.

```
# number of free-energy profiles
nfes= # put here the number of profiles
# minimum of basin A
minA=-3
# maximum of basin A
maxA=1
# minimum of basin B
minB=0.5
# maximum of basin B
maxB=1.5
# temperature in energy units
kbt=2.5
for((i=0;i<nfes;i++))
 # calculate free-energy of basin A
# and basin B
B='awk 'BEGIN{tot=0.0}{if($1!="#!" && $1>min && $1<max)tot+=exp(-$2/kbt)}END{print -kbt*log(tot)}' min=${minE
 # calculate difference
 Delta=$(echo "${A} - ${B}" | bc -1)
 # print it
 echo $i $Delta
done
```

notice that nfes should be set to the number of profiles (free-energy estimates at different times of the simulation) generated by the option –stride of sum\_hills.

This analysis, along with the observation of the diffusive behavior in the CVs space, suggest that the simulation is converged.

#### 12.18.3.1.4 Exercise 3

In this exercise, we will run a well-tempered metadynamics simulation on alanine dipeptide in vacuum, using as CV the backbone dihedral angle psi. In order to run this simulation we need to prepare the PLUMED input file (plumed.dat) as follows.

```
# set up two variables for Phi and Psi dihedral angles
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
# Activate well-tempered metadynamics in psi depositing
# a Gaussian every 500 time steps, with initial height equal
\# to 1.2 kJoule/mol, biasfactor equal to 10.0, and width to 0.35 rad
METAD ...
LABEL=metad
ARG=psi
PACE=500
HEIGHT=1.2
SIGMA=0.35
FILE=HILLS
BIASFACTOR=10.0
TEMP = 300.0
GRID_MIN=-pi
GRID_MAX=pi
GRID SPACING=0.1
... METAD
# monitor the two variables and the metadynamics bias potential
PRINT STRIDE=10 ARG=phi,psi,metad.bias FILE=COLVAR
```

(see TORSION, METAD, and PRINT).

Once the PLUMED input file is prepared, one has to run Gromacs with the option to activate PLUMED and read the input file:

```
gmx_mpi mdrun -s ../TOPO/topolA.tpr -plumed plumed.dat -nsteps 5000000
```

As we did in the previous exercise, we can use COLVAR to visualize the behavior of the CV during the simulation. Here we will plot at the same time the evolution of the metadynamics CV psi and of the other dihedral phi:

By inspecting Figure munster-metad-psi-phi-fig, we notice that something different happened compared to the previous exercise. At first the behavior of psi looks diffusive in the entire CV space. However, around t=1 ns, psi seems trapped in a region of the CV space in which it was previously diffusing without problems. The reason is that the non-biased CV phi after a while has jumped into a different local minima. Since phi is not directly biased, one has to wait for this (slow) degree of freedom to equilibrate before the free energy along psi can converge. Try to repeat the analysis done in the previous exercise (calculate the estimate of the free energy as a function of time and monitor the free-energy difference between basins) to assess the convergence of this metadynamics simulation.

12.18.3.2 Restraints

12.18.3.2.1 Biased sampling theory

A system at temperature T samples conformations from the canonical ensemble:

$$P(q) \propto e^{-\frac{U(q)}{k_B T}}$$

. Here q are the microscopic coordinates and  $k_B$  is the Boltzmann constant. Since q is a highly dimensional vector, it is often convenient to analyze it in terms of a few collective variables (see Belfast tutorial: Analyzing CVs, Belfast tutorial: Adaptive variables I, and Belfast tutorial: Adaptive variables II). The probability distribution for a CV s is

$$P(s) \propto \int dq e^{-\frac{U(q)}{k_B T}} \delta(s - s(q))$$

This probability can be expressed in energy units as a free energy landscape F(s):

$$F(s) = -k_B T \log P(s)$$

.

Now we would like to modify the potential by adding a term that depends on the CV only. That is, instead of using U(q), we use U(q)+V(s(q)). There are several reasons why one would like to introduce this potential. One is to avoid that the system samples some un-desired portion of the conformational space. As an example, imagine that you want to study dissociation of a complex of two molecules. If you perform a very long simulation you will be able to see association and dissociation. However, the typical time required for association will depend on the size of the simulation box. It could be thus convenient to limit the exploration to conformations where the distance between the two molecules is lower than a given threshold. This could be done by adding a bias potential on the distance between the two molecules. Another example is the simulation of a portion of a large molecule taken out from its initial context. The fragment alone could be unstable, and one might want to add additional potentials to keep the fragment in place. This could be done by adding a bias potential on some measure of the distance from the experimental structure (e.g. on root-mean-square deviation).

Whatever CV we decide to bias, it is very important to recognize which is the effect of this bias and, if necessary, remove it a posteriori. The biased distribution of the CV will be

$$P'(s) \propto \int dq e^{-\frac{U(q)+V(s(q))}{k_B T}} \delta(s-s(q)) \propto e^{-\frac{V(s(q))}{k_B T}} P(s)$$

and the biased free energy landscape

$$F'(s) = -k_B T \log P'(s) = F(s) + V(s) + C$$

Thus, the effect of a bias potential on the free energy is additive. Also notice the presence of an undetermined constant C. This constant is irrelevant for what concerns free-energy differences and barriers, but will be important later when we will learn the weighted-histogram method. Obviously the last equation can be inverted so as to obtain the original, unbiased free-energy landscape from the biased one just subtracting the bias potential

$$F(s) = F'(s) - V(s) + C$$

Additionally, one might be interested in recovering the distribution of an arbitrary observable. E.g., one could add a bias on the distance between two molecules and be willing to compute the unbiased distribution of some torsional angle. In this case there is no straightforward relationship that can be used, and one has to go back to the relationship between the microscopic probabilities:

$$P(q) \propto P'(q)e^{\frac{V(s(q))}{k_BT}}$$

The consequence of this expression is that one can obtained any kind of unbiased information from a biased simulation just by weighting every sampled conformation with a weight

$$w \propto e^{\frac{V(s(q))}{k_B T}}$$

That is, frames that have been explored in spite of a high (disfavoring) bias potential V will be counted more than frames that has been explored with a less disfavoring bias potential.

## 12.18.3.2.2 Umbrella sampling theory

Often in interesting cases the free-energy landscape has several local minima. If these minima have free-energy differences that are on the order of a few times  $k_BT$  they might all be relevant. However, if they are separated by a high saddle point in the free-energy landscape (i.e. a low probability region) than the transition between one and the other will take a lot of time and these minima will correspond to metastable states. The transition between one minimum and the other could require a time scale which is out of reach for molecular dynamics. In these situations, one could take inspiration from catalysis and try to favor in a controlled manner the conformations corresponding to the transition state.

Imagine that you know since the beginning the shape of the free-energy landscape F(s) as a function of one CV s. If you perform a molecular dynamics simulation using a bias potential which is exactly equal to -F(s), the biased free-energy landscape will be flat and barrierless. This potential acts as an "umbrella" that helps you to safely cross the transition state in spite of its high free energy.

It is however difficult to have an a priori guess of the free-energy landscape. We will see later how adaptive techniques such as metadynamics (Belfast tutorial: Metadynamics) can be used to this aim. Because of this reason, umbrella sampling is often used in a slightly different manner.

Imagine that you do not know the exact height of the free-energy barrier but you have an idea of where the barrier is located. You could try to just favor the sampling of the transition state by adding a harmonic restraint on the CV, e.g. in the form

$$V(s) = \frac{k}{2}(s - s_0)^2$$

. The sampled distribution will be

$$P'(q) \propto P(q)e^{\frac{-k(s(q)-s_0)^2}{2k_BT}}$$

For large values of k, only points close to  $s_0$  will be explored. It is thus clear how one can force the system to explore only a predefined region of the space adding such a restraint. By combining simulations performed with different values of  $s_0$ , one could obtain a continuous set of simulations going from one minimum to the other crossing the transition state. In the next section we will see how to combine the information from these simulations.

If you want to just bring a collective variables to a specific value, you can use a simple restraint. Let's imagine that we want to force the  $\Phi$  angle to visit a region close to  $\Phi=\pi/2$ . We can do it adding a restraint in  $\Phi$ , with the following input

```
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
res: RESTRAINT ARG=phi AT=0.5pi KAPPA=5
PRINT ARG=phi,psi,res.bias
```

## (see TORSION, RESTRAINT, and PRINT).

Notice that here we are printing a quantity named res.bias. We do this because RESTRAINT does not define a single value (that here would be theoretically named res) but a structure with several components. All biasing methods (including METAD) do so, as well as many collective variables (see e.g. DISTANCE used with COMP ONENTS keyword). Printing the bias allows one to know how much a given snapshop was penalized. Also notice that PLUMED understands numbers in the for  $\{number\}pi$ . This is convenient when using torsions, since they are expressed in radians.

Now you can plot your trajectory with gnuplot and see the effect of KAPPA. You can also try different values of KAPPA. The stiffer the restraint, the less the collective variable will fluctuate. However, notice that a too large kappa could make the MD integrator unstable.

## 12.18.3.3 Moving restraints

A restraint can also be modified as a function of time. For example, if you want to bring the system from one minimum to the other, you can use a moving restraint on  $\Phi$ :

```
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
# notice that a long line can be splitted with this syntax
MOVINGRESTRAINT ...
# also notice that a LABEL keyword can be used and is equivalent
# to adding the name at the beginning of the line with colon, as we did so far
LABEL=res
ARG=phi
STEP0=0 AT0=-0.5pi KAPPA0=5
STEP1=10000 AT0=0.5pi
...
PRINT ARG=phi,psi,res.work,res.phi_cntr FILE=colvar
```

## (see TORSION, MOVINGRESTRAINT, and PRINT).

Notice that here we are plotting a few new components, namely work and phi\_cntr. The former gives the work performed in pulling the restraint, and the latter the position of the restraint. Notice that if pulling is slow enough one can compute free energy profile from the work. You can plot the putative free-energy landscape with

```
> gnuplot
# column 5 is res.phi_cntr
# column 4 is res.work
gnuplot> p "colvar" u 5:4
```

#### 12.18.3.4 Using multiple replicas

## Warning

Notice that multireplica simulations with PLUMED are fully supported with GROMACS, but only partly supported with other MD engines.

Some free-energy methods are intrinsically parallel and requires running several simultaneous simulations. This can be done with gromacs using the multi replica framework. That is, if you have 4 tpr files named topol0.tpr, topol1.tpr, topol2.tpr, topol3.tpr you can run 4 simultaneous simulations.

```
> mpirun -np 4 gmx_mpi mdrun -s topol.tpr -plumed plumed.dat -multi 4 -nsteps 500000
```

Each of the 4 replicas will open a different topol file, and GROMACS will take care of adding the replica number before the .tpr suffix. PLUMED deals with the extra number in a slightly different way. In this case, for example, PLUMED first look for a file named plumed.dat.X, where X is the number of the replica. In case the file is not found, then PLUMED looks for plumed.dat. If also this is not found, PLUMED will complain. As a consequence, if all the replicas should use the same input file it is sufficient to put a single plumed.dat file, but one has also the flexibility of using separate files named plumed.dat.0, plumed.dat.1 etc. Finally, notice that the way PLUMED adds suffixes will change in version 2.2, and names will be plumed.0.dat etc.

Also notice that providing the flag <code>-replex</code> one can instruct gromacs to perform a replica exchange simulation. Namely, from time to time gromacs will try to swap coordinates among neighboring replicas and accept of reject the exchange with a Monte Carlo procedure which also takes into account the bias potentials acting on the replicas, even if different bias potentials are used in different replicas. That is, PLUMED allows to easily implement many forms of Hamiltonian replica exchange.

12.18.3.5 Using multiple restraints with replica exchange

## 12.18.3.5.1 Weighted histogram analysis method theory

Let's now consider multiple simulations performed with restraints located in different positions. In particular, we will consider the i-th bias potential as  $V_i$ . The probability to observe a given value of the collective variable s is:

$$P_i(s) = \frac{P(s)e^{-\frac{V_i(s)}{k_BT}}}{\int ds' P(s')e^{-\frac{V_i(s')}{k_BT}}} = \frac{P(s)e^{-\frac{V_i(s)}{k_BT}}}{Z_i}$$

where

$$Z_i = \sum_{q} e^{-(U(q) + V_i(q))}$$

The likelyhood for the observation of a sequence of snapshots  $q_i(t)$  (where i is the index of the trajectory and t is time) is just the product of the probability of each of the snapshots. We use here the minus-logarithm of the likelihood (so that the product is converted to a sum) that can be written as

$$\mathcal{L} = -\sum_{i} \int dt \log P_i(s_i(t)) = \sum_{i} \int dt \left( -\log P(s_i(t)) + \frac{V_i(s_i(t))}{k_B T} + \log Z_i \right)$$

One can then maximize the likelyhood by setting  $\frac{\delta \mathcal{L}}{\delta P(\mathbf{s})} = 0$ . After some boring algebra the following expression can be obtained

$$0 = \sum_{i} \int dt \left( -\frac{\delta_{\mathbf{s}_{i}(t),\mathbf{s}}}{P(\mathbf{s})} + \frac{e^{-\frac{V_{i}(\mathbf{s})}{k_{B}T}}}{Z_{i}} \right)$$

In this equation we aim at finding P(s). However, also the list of normalization factors  $Z_i$  is unknown, and they should be found selfconsistently. Thus one can find the solution as

$$P(\mathbf{s}) \propto \frac{N(\mathbf{s})}{\sum_{i} \int dt \frac{e^{-\frac{V_{i}(\mathbf{s})}{k_{B}T}}}{Z_{i}}}$$

where Z is selfconsistently determined as

$$Z_i \propto \int ds' P(\mathbf{s'}) e^{-\frac{V_i(\mathbf{s'})}{k_B T}}$$

These are the WHAM equations that are traditionally solved to derive the unbiased probability P(s) by the combination of multiple restrained simulations. To make a slightly more general implementation, one can compute the weights that should be assigned to each snapshot, that turn out to be:

$$w_i(t) \propto \frac{1}{\sum_j \int dt \frac{e^{-\beta V_j(\mathbf{s}_i(t))}}{Z_j}}$$

The normalization factors can in turn be found from the weights as

$$Z_i \propto \frac{\sum_j \int dt e^{-\beta V_i(\mathbf{s}_j(t))} w_j(t)}{\sum_j \int dt w_j(t)}$$

This allows to straighforwardly compute averages related to other, non-biased degrees of freedom, and it is thus a bit more flexible. It is sufficient to precompute this factors w and use them to weight every single frame in the trajectory.

#### 12.18.3.5.2 Exercise 4

In this exercise we will run multiple restraint simulations and learn how to reweight and combine data with WHAM to obtain free-energy profiles. We start with running in a replica-exchange scheme 32 simulations with a restraint on phi in different positions, ranging from -3 to 3. We will instruct gromacs to attempt an exchange between different simulations every 1000 steps.

```
dx='echo "6.0 / ( $nrep - 1 )" | bc -1'
for((i=0;i<nrep;i++))
# center of the restraint
AT='echo "$i * $dx - 3.0" | bc -1'
cat >plumed.dat.$i << EOF
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
# Impose an umbrella potential on phi
# with a spring constant of 200 kjoule/mol
# and centered in phi=AT
restraint-phi: RESTRAINT ARG=phi KAPPA=200.0 AT=$AT
# monitor the two variables and the bias potential
PRINT STRIDE=100 ARG=phi,psi,restraint-phi.bias FILE=COLVAR
EOF
# we initialize some replicas in A and some in B:
if((i%2==0)); then
  cp ../TOPO/topolA.tpr topol$i.tpr
else
  cp ../TOPO/topolB.tpr topol$i.tpr
fi
done
# run REM
mpirun -np $nrep gmx_mpi mdrun -plumed plumed.dat -s topol.tpr -multi $nrep -replex 1000 -nsteps 500000
```

To be able to combine data from all the simulations, it is necessary to have an overlap between statistics collected in two adjacent umbrellas. Have a look at the plot of (phi,psi) for the different simulations to understand what is happening.

An often misunderstood fact about WHAM is that data of the different trajectories can be mixed and it is not necessary to keep track of which restraint was used to produce every single frame. Let's get the concatenated trajectory

```
trjcat_mpi -cat -f traj*.xtc -o alltraj.xtc
```

Now we should compute the value of each of the bias potentials on the entire (concatenated) trajectory.

```
nrep=32
dx='echo "6.0 / ( $nrep - 1 )" | bc -1'

for i in 'seq 0 $(( $nrep - 1 ))' do
    # center of the restraint
AT='echo "$i * $dx - 3.0" | bc -1'

cat >plumed.dat << EOF
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17
restraint-phi: RESTRAINT ARG=phi KAPPA=200.0 AT=$AT

# monitor the two variables and the bias potential
PRINT STRIDE=100 ARG=phi,psi,restraint-phi.bias FILE=ALLCOLVAR.$i
EOF

plumed driver --mf_xtc alltraj.xtc --trajectory-stride=10 --plumed plumed.dat
done</pre>
```

It is very important that this script is consistent with the one used to generate the multiple simulations above. Now, single files named ALLCOLVAR.XX will contain on the fourth column the value of the bias centered in a given position, computed on the entire concatenated trajectory.

Next step is to compute the weights self-consistently solving the WHAM equations, using the python script "wham. ← py" contained in the SCRIPTS directory. To use this code:

```
../SCRIPTS/wham.sh ALLCOLVAR.*
```

This script will produce several files. Let's visualize "phi\_fes.dat", which contains the free energy as a function of phi, and compare this with the result previously obtained with metadynamics.

```
12.18.3.5.3 Exercise 5
```

In the previous exercise, we use multiple restraint simulations to calculate the free energy as a function of the dihedral phi. The resulting free energy was in excellent agreement with our previous metadynamics simulation. In this exercise we will repeat the same procedure for the dihedral psi. At the end of the steps defined above, we can plot the free energy "psi\_fes.dat" and compare it with the reference profile calculated from a metadynamics simulations using both phi and psi as CVs.

We can easily spot from the plot above that something went wrong in this multiple restraint simulations, despite we used the very same approach we adopted for the phi dihedral. The problem here is that psi is a "bad" collective variable, and the system is not able to equilibrate the missing slow degree of freedom phi in the short time scale of the umbrella simulation (1 ns). In the metadynamics exercise in which we biased only psi, we detect problems by observing the behavior of the CV as a function of simulation time. How can we detect problems in multiple restraint simulations? This is slightly more complicated, but running this kind of simulation in a replica-exchange scheme offers a convenient way to detect problems.

The first thing we need to do is to demux the replica-exchange trajectories and reconstruct the continuous trajectories of the replicas across the different restraint potentials. In order to do so, we can use the following script:

```
demux.pl md0.log
trjcat_mpi -f traj*.xtc -demux replica_index.xvq
```

This commands will generate 32 continous trajectories, named XX\_trajout.xtc. We will use the driver to calculate the value of the CVs phi and psi on these trajectories.

```
nrep=32
for i in 'seq 0 $(( $nrep - 1 )) '
do

cat >plumed.dat << EOF
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17

# monitor the two variables
PRINT STRIDE=100 ARG=phi,psi FILE=COLVARDEMUX.$i
EOF
plumed driver --mf_xtc ${i}_trajout.xtc --trajectory-stride=10 --plumed plumed.dat
done</pre>
```

The COLVARDEMUX.XX files will contain the value of the CVs on the demuxed trajectory. If we visualize these files we will notice that replicas sample the CVs space differently. In order for each umbrella to equilibrate the slow degrees of freedom phi, the continuous replicas must be ergodic and thus sample the same distribution in phi and psi.

# **Chapter 13**

# **Index of Actions**

The following page contains an alphabetically ordered list of all the Actions and command line tools that are available in PLUMED 2. For lists of Actions classified in accordance with the particular tasks that are being performed see:

- Collective variables tells you about the ways that you can calculate functions of the positions of the atoms.
- Analysis tells you about the various forms of analysis you can run on trajectories using PLUMED.
- Bias tells you about the methods that you can use to bias molecular dynamics simulations with PLUMED.

## 13.1 Full list of actions

| ABMD                  | BIAS     | Adds a ratchet-and-pawl like restraint on one or more variables.  |
|-----------------------|----------|---|
| ALIGNED_MATRIX        | MATRIX   | Adjacency matrix in which two molecule are adjacent if they are within a certain cutoff and if they have the same orientation.  |
| ALPHABETA             | COLVAR   | Measures a distance including pbc between the instantaneous values of a set of torsional angles and set of reference values.  |
| ALPHARMSD             | COLVAR   | Probe the alpha helical content of a protein structure.   |
| ANGLES                | MCOLVAR  | Calculate functions of the distribution of angles .   |
| ANGLE                 | COLVAR   | Calculate an angle.   |
| ANTIBETARMSD          | COLVAR   | Probe the antiparallel beta sheet content of your protein structure.  |
| AROUND                | VOLUMES  | This quantity can be used to calculate functions of the distribution of collective variables for the atoms that lie in a particular, user-specified part of the cell. |
| AVERAGE               | GRIDCALC | Calculate the ensemble average of a collective variable   |
| BIASVALUE             | BIAS     | Takes the value of one variable and use it as a bias  |
| BRIDGE                | MCOLVAR  | Calculate the number of atoms that bridge two parts of a structure  |
| CAVITY                | VOLUMES  | This quantity can be used to calculate functions of the distribution of collective variables for the atoms that lie in a box defined by the positions of four atoms.  |
| CELL                  | COLVAR   | Calculate the components of the simulation cell   |
| CENTER_OF_MULTICOLVAR | VATOM    | Calculate a a weighted average position based on the value of some multicolvar.   |

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| CENTER               | VATOM              | Calculate the center for a group of atoms, with arbitrary  |
|----------------------|--------------------|--|
|                      |                    | weights.   |
| CLASSICAL_MDS        | DIMRED             | Create a low-dimensional projection of a trajectory using the classical multidimensional scaling algorithm.  |
| CLUSTER_DIAMETER     | CONCOMP            | Print out the diameter of one of the connected components  |
| CLUSTER_DISTRIBUTION | CONCOMP            | Calculate functions of the distribution of properties in your connected components.  |
| CLUSTER_NATOMS       | CONCOMP            | Gives the number of atoms in the connected component   |
| CLUSTER_PROPERTIES   | CONCOMP            | Calculate properties of the distribution of some quantities that are part of a connected component   |
| CLUSTER_WITHSURFACE  | MATRIXF            | Find the various connected components in an adjacency matrix and then output averageproperties of the atoms in those connected components.   |
| COLUMNSUMS           | MATRIXF            | Sum the columns of a contact matrix  |
| COMBINE              | FUNCTION           | Calculate a polynomial combination of a set of other variables.  |
| COMMITTOR            | PRINTANALY↔<br>SIS | Does a committor analysis.   |
| COM                  | VATOM              | Calculate the center of mass for a group of atoms.   |
| CONSTANT             | COLVAR             | Return one or more constant quantitieswith or without derivatives.   |
| CONTACTMAP           | COLVAR             | Calculate the distances between a number of pairs of atoms and transform each distance by a switching function. The transformed distance can be compared with a reference value in order to calculate the squared distance between two contact maps. Each distance can also be weighted for a given value. CONTACTMAP can be used togetherwith FUNCPATHMSD to define a path in the contactmap space. |
| CONTACT_MATRIX       | MATRIX             | Adjacency matrix in which two atoms are adjacent if they are within a certain cutoff.  |
| CONVERT_TO_FES       | GRIDANALYSIS       | Convert a histogram, $H(x)$ , to a free energy surface using $F(x) = -k_BT \ln H(x)$ .   |
| COORDINATIONNUMBER   | MCOLVAR            | Calculate the coordination numbers of atoms so that you can then calculate functions of the distribution of-coordination numbers such as the minimum, the number less than a certain quantity and so on.   |
| COORDINATION         | COLVAR             | Calculate coordination numbers.  |
| CS2BACKBONE          | COLVAR             | This collective variable calculates the backbone chemical shifts for a protein.  |
| DEBUG                | GENERIC            | Set some debug options.  |
| DENSITY              | MCOLVAR            | Calculate functions of the density of atoms as a function of the box. This allows one to calculate the number of atoms in half the box.  |
| DFSCLUSTERING        | MATRIXF            | Find the connected components of the matrix using the DFS clustering algorithm.  |
| DHENERGY             | COLVAR             | Calculate Debye-Huckel interaction energy among G←   |
|                      |                    | ROUPA and GROUPB.  |
| DIHCOR               | COLVAR             | Measures the degree of similarity between dihedral angles.   |

13.1 Full list of actions 595

| DISTANCE_FROM_CONTOUR  | COLVAR              | Calculate the perpendicular distance from a Willard-← Chandler dividing surface.  |
|------------------------|---------------------|---|
| DISTANCES              | MCOLVAR             | Calculate the distances between one or many pairs of atoms. You can then calculate functions of the distribution of distances such as the minimum, the number less than a certain quantity and so on. |
| DISTANCE               | COLVAR              | Calculate the distance between a pair of atoms.   |
| driver-float           | TOOLS               | Equivalent to driver, but using single precision reals.   |
| driver                 | TOOLS               | driver is a tool that allows one to to use plumed to post-<br>process an existing trajectory.   |
| DRMSD                  | DCOLVAR             | Calculate the distance RMSD with respect to a reference structure.  |
| DUMPATOMS              | PRINTANALY↔<br>SIS  | Dump selected atoms on a file.  |
| DUMPCUBE               | GRIDANALYSIS        | Output a three dimensional grid using the Gaussian cube file format.  |
| DUMPDERIVATIVES        | PRINTANALY↔<br>SIS  | Dump the derivatives with respect to the input parameters for one or more objects (generally CVs, functions or biases).   |
| DUMPFORCES             | PRINTANALY↔<br>SIS  | Dump the force acting on one of a values in a file.   |
| DUMPGRAPH              | CONCOMP             | Write out the connnectivity of the nodes in the graph in dot format.  |
| DUMPGRID               | GRIDANALYSIS        | Output the function on the grid to a file with the PLU← MED grid format.  |
| DUMPMASSCHARGE         | PRINTANALY↔<br>SIS  | Dump masses and charges on a selected file.   |
| DUMPMULTICOLVAR        | PRINTANALY↔<br>SIS  | Dump atom positions and multicolvar on a file.  |
| DUMPPROJECTIONS        | PRINTANALY ←<br>SIS | Dump the derivatives with respect to the input parameters for one or more objects (generally CVs, functions or biases).   |
| EFFECTIVE_ENERGY_DRIFT | GENERIC             | Print the effective energy drift described in Ref ?   |
| ENERGY                 | COLVAR              | Calculate the total energy of the simulation box.   |
| ENSEMBLE               | FUNCTION            | Calculates the replica averaging of a collective variable over multiple replicas.   |
| ERMSD                  | COLVAR              | Calculate eRMSD with respect to a reference structure.  |
| EXTENDED_LAGRANGIAN    | BIAS                | Add extended Lagrangian.  |
| EXTERNAL               | BIAS                | Calculate a restraint that is defined on a grid that is read during start up  |
| FAKE                   | COLVAR              | This is a fake colvar container used by cltools or various other actions and just support input and period definition   |
| FCCUBIC                | MCOLVAR             | Measure how similar the environment around atoms is to that found in a FCC structure.   |
| FIND_CONTOUR_SURFACE   | GRIDANALYSIS        | Find an isocontour by searching along either the x, y or direction.   |
| FIND_CONTOUR           | GRIDANALYSIS        | Find an isocontour in a smooth function.  |
| FIND_SPHERICAL_CONTOUR | GRIDANALYSIS        | Find an isocontour in a three dimensional grid by searching over a Fibonacci sphere.  |
| FIT_TO_TEMPLATE        | GENERIC             | This action is used to align a molecule to a template.  |
| FIXEDATOM              | VATOM               | Add a virtual atom in a fixed position.   |
| FLUSH                  | GENERIC             | This command instructs plumed to flush all the open files with a user specified frequency. Notice that all files are flushed anyway every 10000 steps.  |

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| FOURIER_TRANSFORM      | GRIDANALYSIS | Compute the Discrete Fourier Transform (DFT) by means of FFTW of data stored on a 2D grid.  |
|------------------------|--------------|---|
| FRET                   | COLVAR       | Calculate the FRET efficiency between a pair of atoms. The efficiency is calculated using the Forster relation:   |
| FUNCPATHMSD            | FUNCTION     | This function calculates path collective variables.   |
| FUNCSUMHILLS           | FUNCTION     | This function is intended to be called by the command line tool sum_hillsand it is meant to integrate a HIL← LS file or an HILLS file interpreted as a histogram i a variety of ways. Therefore it is not expected that you use this during your dynamics (it will crash!)    |
| gentemplate            | TOOLS        | gentemplate is a tool that you can use to construct template inputs for the variousactions  |
| GHOST                  | VATOM        | Calculate the absolute position of a ghost atom with fixed coordinatesin the local reference frame formed by three atoms. The computed ghost atom is stored as a virtual atom that can be accessed inan atom list through the the label for the GHOST action that creates it. |
| GPROPERTYMAP           | COLVAR       | Property maps but with a more flexible framework for the distance metric being used.  |
| GRADIENT               | MCOLVARF     | Calculate the gradient of the average value of a multi-<br>colvar value   |
| GRID_TO_XYZ            | GRIDANALYSIS | Output the function on the grid to an xyz file  |
| GROUP                  | GENERIC      | Define a group of atoms so that a particular list of atoms can be referenced with a single labelin definitions of CVs or virtual atoms.   |
| GYRATION               | COLVAR       | Calculate the radius of gyration, or other properties related to it.  |
| HBOND_MATRIX           | MATRIX       | Adjacency matrix in which two atoms are adjacent if there is a hydrogen bond between them.  |
| HISTOGRAM              | GRIDCALC     | Accumulate the average probability density along a few CVs from a trajectory.   |
| IMPLICIT               | COLVAR       |   |
| INCLUDE                | GENERIC      | Includes an external input file, similar to "#include" in C preprocessor.   |
| INCYLINDER             | VOLUMES      | This quantity can be used to calculate functions of the distribution of collective variables for the atoms that lie in a particular, user-specified part of the cell.   |
| info                   | TOOLS        | This tool allows you to obtain information about your plumed version  |
| INPLANEDISTANCES       | MCOLVAR      | Calculate distances in the plane perpendicular to an axis   |
| INSPHERE               | VOLUMES      | This quantity can be used to calculate functions of the distribution of collective variables for the atoms that lie in a particular, user-specified part of the cell.   |
| INTEGRATE_GRID         | GRIDANALYSIS | Calculate the total integral of the function on the input grid  |
| INTERMOLECULARTORSIONS | MCOLVARF     | Calculate torsions between vectors on adjacent molecules  |
| INTERPOLATE_GRID       | GRIDANALYSIS | Interpolate a smooth function stored on a grid onto a grid with a smaller grid spacing.   |
| JCOUPLING              | COLVAR       | Calculates $^3J$ coupling constants for a dihedral angle.   |
| kt                     | TOOLS        | Print out the value of $k_BT$ at a particular temperature   |

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| LOAD               | GENERIC     | Loads a library, possibly defining new actions.   |
|--------------------|-------------|---|
| LOCAL_AVERAGE      | MCOLVARF    | Calculate averages over spherical regions centered on   |
| LOCALENSEMBLE      | FUNCTION    | atoms  Calculates the average over multiple arguments.  |
| LOCAL_Q3           | MCOLVARF    | Calculates the average over multiple arguments.  Calculate the local degree of order around an atoms by taking the average dot product between the $q_3$ vector on the central atom and the $q_3$ vector on the atoms in the first coordination sphere. |
| LOCAL_Q4           | MCOLVARF    | Calculate the local degree of order around an atoms by taking the average dot product between the $q_4$ vector on the central atom and the $q_4$ vectoron the atoms in the first coordination sphere.   |
| LOCAL_Q6           | MCOLVARF    | Calculate the local degree of order around an atoms by taking the average dot product between the $q_6$ vector on the central atom and the $q_6$ vectoron the atoms in the first coordination sphere.   |
| LOWER_WALLS        | BIAS        | Defines a wall for the value of one or more collective variables, which limits the region of the phase space accessible during the simulation.  |
| LWALLS             | MCOLVARB    | Add LOWER_WALLS restraints on all the multicolvar values  |
| manual             | TOOLS       | manual is a tool that you can use to construct the man-<br>ual page for a particular action   |
| MATHEVAL           | FUNCTION    | Calculate a combination of variables using a matheval expression.   |
| METAD              | BIAS        | Used to performed MetaDynamics on one or more collective variables.   |
| METAINFERENCE      | BIAS        | Calculate the Metainference Score for a set of back calculated experimental data.   |
| MFILTER_BETWEEN    | MFILTERS    | This action can be used to filter the colvar values cal-<br>culated by a multicolvar so that one can compute the<br>mean and so on for only those multicolvars within a<br>certain range.   |
| MFILTER_LESS       | MFILTERS    | This action can be used to filter the distribution of colvar values in a multicolvar so that one can compute the mean and so on for only those multicolvars less than a tolerance.  |
| MFILTER_MORE       | MFILTERS    | This action can be used to filter the distribution of colvar values in a multicolvar so that one can compute the mean and so on for only those multicolvars more than a tolerance.  |
| MOLECULES          | MCOLVAR     | Calculate the vectors connecting a pair of atoms in order to represent the orientation of a molecule.   |
| MOLINFO            | TOPOLOGY    | This command is used to provide information on the molecules that are present in your system.   |
| MOVINGRESTRAINT    | BIAS        | Add a time-dependent, harmonic restraint on one or more variables.  |
| MTRANSFORM_BETWEEN | MTRANSFORMS | This action can be useed to transform the colvar values calculated by a multicolvar using a histogrambead   |
| MTRANSFORM_LESS    | MTRANSFORMS | This action can be useed to transform the colvar values calculated by a multicolvar using a switchingfunction   |
| MTRANSFORM_MORE    | MTRANSFORMS | This action can be useed to transform the colvar values calculated by a multicolvar using one minus a switchingfunction   |
| MULTICOLVARDENS    | GRIDCALC    | Evaluate the average value of a multicolvar on a grid.  |

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| MULTI-RMSD       | DCOLVAR            | Calculate the RMSD distance moved by a number of separated domains from their positions in a reference structure.  |
|------------------|--------------------|--|
| NLINKS           | MCOLVARF           | Calculate number of pairs of atoms/molecules that are "linked"   |
| NOE              | COLVAR             | Calculates NOE intensities as sums of $1/r^{\wedge}6$ , also averaging over multiple equivalent atomsor ambiguous N $\leftarrow$ OE.   |
| OUTPUT_CLUSTER   | CONCOMP            | Output the indices of the atoms in one of the clusters identified by a clustering object   |
| PARABETARMSD     | COLVAR             | Probe the parallel beta sheet content of your protein structure.   |
| PATHMSD          | COLVAR             | This Colvar calculates path collective variables.  |
| PATH             | COLVAR             | Path collective variables with a more flexible framework for the distance metric being used.   |
| pathtools        | TOOLS              | pathtools can be used to construct paths from pdb data   |
| PBMETAD          | BIAS               | Used to performed Parallel Bias MetaDynamics.  |
| PCARMSD          | DCOLVAR            | Calculate the PCA components ( see ? and ? ) for a number of provided eigenvectors and an average structure. Performs optimal alignment at every step and reports the rmsd so you know if you are far or close   |
|                  |                    | from the average structure. It takes the average structure and eigenvectors in form of a pdb. Note that beta and occupancy values in the pdb are neglected and all the weights are placed to 1 (differently from the RMSD colvar for example)  |
| PCA              | DIMRED             | Perform principal component analysis (PCA) using either the positions of the atoms a large number of collective variables as input.  |
| PCAVARS          | COLVAR             | Projection on principal component eigenvectors or other high dimensional linear subspace   |
| PIECEWISE        | FUNCTION           | Compute a piecewise straight line through its arguments that passes througha set of ordered control points.  |
| PLANES           | MCOLVAR            | Calculate the plane perpendicular to two vectors in order to represent the orientation of a planar molecule.   |
| POSITION         | COLVAR             | Calculate the components of the position of an atom.   |
| PRE              | COLVAR             | Calculates the Paramegnetic Resonance Enhancement intensity ratio between two atoms. The reference atom for the spin label is added with SPINLABEL, the affected atom(s) are give as numbered GROUPA1, G← ROUPA2, The additional parameters needed for the calculation are given as INEPT, the inepttime, TAUC the correlation time, OMEGA, the larmor frequency and RTWO for the relaxation time. |
| PRINT            | PRINTANALY↔<br>SIS | Print quantities to a file.  |
| PROPERTYMAP      | COLVAR             | Calculate generic property maps.   |
| PUCKERING        | COLVAR             | Calculate sugar pseudorotation coordinates.  |
| Q3               | MCOLVAR            | Calculate 3rd order Steinhardt parameters.   |
| Q4               | MCOLVAR            | Calculate 4th order Steinhardt parameters.   |
| Q6               | MCOLVAR            | Calculate 6th order Steinhardt parameters.   |
| RANDOM_EXCHANGES | GENERIC            | Set random pattern for exchanges.  |
| RDC              | COLVAR             | Calculates the (Residual) Dipolar Coupling between two atoms.  |

13.1 Full list of actions 599

| READ            | GENERIC     | Read quantities from a colvar file.  |
|-----------------|-------------|--|
| RESET_CELL      | GENERIC     | This action is used to rotate the full cell  |
| RESTART         | GENERIC     | Activate restart.  |
| RESTRAINT       | BIAS        | Adds harmonic and/or linear restraints on one or more variables.   |
| REWEIGHT_BIAS   | REWEIGHTING | Calculate weights for ensemble averages that negate the effect the bias has on the region of phase space explored  |
| REWEIGHT_METAD  | REWEIGHTING | Calculate the weights configurations should contribute to the histogram in a simulation in which a metadynamics bias acts upon the system.   |
| REWEIGHT_TEMP   | REWEIGHTING | Calculate weights for ensemble averages allow for the computing of ensemble averages at temperatures lower/higher than that used in your original simulation.  |
| RMSD            | DCOLVAR     | Calculate the RMSD with respect to a reference structure.  |
| ROWSUMS         | MATRIXF     | Sum the rows of a contact matrix   |
| SIMPLECUBIC     | MCOLVAR     | Calculate whether or not the coordination spheres of atoms are arranged as they would be in a simplecubic structure.   |
| simplemd        | TOOLS       | simplemd allows one to do molecular dynamics on systems of Lennard-Jones atoms.  |
| SMAC_MATRIX     | MATRIX      | Adjacency matrix in which two molecules are adjacent if they are within a certain cutoff and if the angle between them is within certain ranges.   |
| SMAC            | MCOLVARF    | Calculate a variant on the SMAC collective variable discussed in ?   |
| SORT            | FUNCTION    | This function can be used to sort colvars according to their magnitudes.   |
| SPRINT          | MATRIXF     | Calculate SPRINT topological variables from an adjacency matrix.   |
| STATS           | FUNCTION    | Calculates statistical properties of a set of collective variables with respect to a set of reference values.  In particular it calculates and store as components the sum of the squared deviations, the correlation, theslope and the intercept of a linear fit. |
| sum_hills       | TOOLS       | sum_hills is a tool that allows one to to use plumed to post-process an existing hills/colvar file   |
| TARGET          | DCOLVAR     | This function measures the pythagorean distance from a particular structure measured in the space defined by some set of collective variables.   |
| TEMPLATE        | COLVAR      | This file provides a template for if you want to introduce a new CV.   |
| TETRAHEDRALPORE | VOLUMES     | This quantity can be used to calculate functions of the distribution of collective variablesfor the atoms lie that lie in a box defined by the positions of four atoms at the corners of a tetrahedron.  |
| TETRAHEDRAL     | MCOLVAR     | Calculate the degree to which the environment about ions has a tetrahedral order.  |
| TIME            | GENERIC     | retrieve the time of the simulation to be used elsewere  |
| TOPOLOGY_MATRIX | MATRIX      | Adjacency matrix in which two atoms are adjacent if they are connected topologically   |
| TORSIONS        | MCOLVAR     | Calculate whether or not a set of torsional angles are within a particular range.  |
| TORSION         | COLVAR      | Calculate a torsional angle.   |

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| UNITS          | GENERIC            | This command sets the internal units for the code. A  |
|----------------|--------------------|---|
|                |                    | new unit can be set by eitherspecifying how to convert from the plumed default unit into that new unit or by usingthe shortcuts described below. This directive M← UST appear at the BEGINNING of the plumed.dat file. The same units must be used througout the plumed.dat file. |
| UPDATE_IF      | PRINTANALY←<br>SIS | Conditional update of other actions.  |
| UPPER_WALLS    | BIAS               | Defines a wall for the value of one or more collective variables, which limits the region of the phase space accessible during the simulation.  |
| UWALLS         | MCOLVARB           | Add UPPER_WALLS restraints on all the multicolvar values  |
| VOLUME         | COLVAR             | Calculate the volume of the simulation box.   |
| WHOLEMOLECULES | GENERIC            | This action is used to rebuild molecules that can become split by the periodicboundary conditions.  |
| WRAPAROUND     | GENERIC            | Rebuild periodic boundary conditions around chosen atoms.   |
| XANGLES        | MCOLVAR            | Calculate the angles between the vector connecting two atoms and the x axis.  |
| XDISTANCES     | MCOLVAR            | Calculate the x components of the vectors connecting one or many pairs of atoms. You can then calculate functions of the distribution ofvalues such as the minimum, the number less than a certain quantity and so on.  |
| XYDISTANCES    | MCOLVAR            | Calculate distance between a pair of atoms neglecting the z-component. You can then calculate functions of the distribution ofvalues such as the minimum, the number less than a certain quantity and so on.  |
| XYTORSIONS     | MCOLVAR            | Calculate the torsional angle around the x axis from the positive y direction.  |
| XZDISTANCES    | MCOLVAR            | Calculate distance between a pair of atoms neglecting the y-component. You can then calculate functions of the distribution ofvalues such as the minimum, the number less than a certain quantity and so on.  |
| XZTORSIONS     | MCOLVAR            | Calculate the torsional angle around the x axis from the positive z direction.  |
| YANGLES        | MCOLVAR            | Calculate the angles between the vector connecting two atoms and the y axis.  |
| YDISTANCES     | MCOLVAR            | Calculate the y components of the vectors connecting one or many pairs of atoms. You can then calculate functions of the distribution ofvalues such as the minimum, the number less than a certain quantity and so on.  |
| YXTORSIONS     | MCOLVAR            | Calculate the torsional angle around the y axis from the positive x direction.  |
| YZDISTANCES    | MCOLVAR            | Calculate distance between a pair of atoms neglecting the x-component. You can then calculate functions of the distribution ofvalues such as the minimum, the number less than a certain quantity and so on.  |
| YZTORSIONS     | MCOLVAR            | Calculate the torsional angle around the y axis from the positive z direction.  |
| ZANGLES        | MCOLVAR            | Calculate the angles between the vector connecting two atoms and the z axis.  |

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| ZDISTANCES | MCOLVAR | Calculate the z components of the vectors connecting one or many pairs of atoms. You can then calculate functions of the distribution ofvalues such as the minimum, the number less than a certain quantity and so on. |
|------------|---------|--|
| ZXTORSIONS | MCOLVAR | Calculate the torsional angle around the z axis from the positive x direction.   |
| ZYTORSIONS | MCOLVAR | Calculate the torsional angle around the z axis from the positive y direction.   |

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## **Chapter 14**

# **Bug List**

## Page CENTER\_OF\_MULTICOLVAR

The virial contribution for this type of virtual atom is not currently evaluated so do not use in bias functions unless the volume of the cell is fixed

## Page **ENERGY**

Acceptance for replica exchange when ENERGY is biased is computed correctly only of all the replicas has the same potential energy function. This is for instance not true when using GROMACS with lambda replica exchange of with plumed-hrex branch.

#### Page MOLINFO

At the moment the HA1 atoms in a GLY residues are treated as if they are the CB atoms. This may or may not be true - GLY is problematic for secondary structure residues as it is achiral.

If you use WHOLEMOLECULES RESIDUES=1-10 for a 18 amino acid protein (18 amino acids + 2 terminal groups = 20 residues) the code will fail as it will not be able to interpret terminal residue 1.

## Page namd-2.8

NAMD does not currently take into account virial contributions from PLUMED. Please use constant volume simulations only

## Page namd-2.9

NAMD does not currently take into account virial contributions from PLUMED. Please use constant volume simulations only

## Page PCAVARS

It is not possible to use the DRMSD metric with this variable. You can get around this by listing the set of distances you wish to calculate for your DRMSD in the plumed file explicitally and using the EUCLIDEAN metric. MAHALONOBIS and NORM-EUCLIDEAN also do not work with this variable but using these options makes little sense when projecting on a linear subspace.

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