

Mathematical Expression for Probability in Monty Hall Problem for N doors and K doors opened by host:

Given N doors the probability of choosing the door with a car is $1/N$.

Hence **the probability of winning the car if the player chooses to stick is $1/N$** , as this doesn't change anything.

We know that the probability that the car is present is any door other than the one we chose is $N-1/N$. Since k doors without the car are opened by the host and the probability of the car being present in any of the remaining $N-K-1$ doors is $1/N-K-1$,

The probability of winning the car upon switching is the probability of not having the car on the initial choice times the probability of picking it from the $N-K-1$ doors which is $(N-1/N)*(1/N-K-1)$.