001	PyTorchGeoNodes: Enabling Differentiable Shape	001
002	Programs for 3D Shape Reconstruction –	002
003	Supplementary Material	003
004	Anonymous ECCV 2024 Submission	004
005	Paper ID $\#5158$	005
006	We provide additional evaluations of our search algorithm in Section 1, and	006
007	provide more details regarding our PyTorchGeoNodes framework in Section 2,	007
800	regarding our search algorithm in Section 3, and regarding our shape program	800
009	designs in Section 4.	009
010	In addition, we provide a video showing the reconstruction progress	010
011	of our approach through MCTS iterations for scenes of the ScanNet	011
012	dataset [2].	012
013	1 Additional Validation	013
014	In this section, we provide additional results to show that our method is applica-	014
015	ble to different shape programs. Tables 1, 2, 3 show quantitative evaluations for	015
016	the 'Sofa', 'Chair', and 'Table' categories. Table 4 shows evaluations for the 'Ta-	016
017	ble' and 'Cabinet' categories for scenes from the ScanNet dataset. Note that in	017

the 'Sofa', 'Chair', and 'Table' categories. Table 4 shows evaluations for the 'Table' and 'Cabinet' categories for scenes from the ScanNet dataset. Note that in the case of 'Cabinet', we discarded 'Has Back' and 'Number of Dividing Boards' from the ScanNet evaluations as they could not be quantitatively evaluated: This is because the large majority of cabinets have drawers, therefore the back of cabinets are not visible and we cannot estimate the number of dividing boards based on geometric objective terms in the presence of drawers. In the case of bookshelves, objects on shelves induce noise in instance segmentation. Therefore, the objective term does not handle such settings well. We note these are general limitations for reconstructing cabinets and are present also for state-of-the-art methods [1]. Qualitative results in Figure 1, 2 show additional examples where our approach is able to reconstruct a variety of 3D shapes that are geometrically consistent with the input scene.

	Parameter	Full Method	No Refinement	No Refinement No Exploitation Term		
		Mean Absolute Difference to Ground Truth (\downarrow)				
	Width [cm]	8.042	16.301	15.761		
S	Height [cm]	2.304	4.012	4.646		
Continuous Parameters	Depth [cm]	6.214	6.792	7.128		
ш	Leg Size [cm]	1.623	1.711	1.711		
are	Arm Width [cm]	5.383	6.478	6.478		
S P	Arm Height [cm]	$\bf 8.235$	8.84	9.807		
no	${\rm Arm\ Depth\ [cm]}$	12.769	14.747	14.863		
inu	Back Height [cm]	2.488	5.127	5.531		
nt	Back Depth [cm]	5.1	6.813	6.813		
$\ddot{\circ}$	L Width [cm]	4.317	5.341	5.341		
	L Depth [cm]	11.495	12.879	12.502		
	Rotation [°]	3.252	26.559	26.63		
			Classification Acc	curacy (†)		
Discrete Parameters	Has Legs	68.0	70.0	60.0		
me	Has Left Arm	88.0	65.0	64.0		
ara	Has Right Arm	89.0	65.0	60.0		
D.	Has Arm Legs	62.7	56.0	52.0		
ete	Has Back	99.0	97.0	98.0		
$_{ m SCr}$	Is L-Shaped	81.0	81.0	81.0		
Di	Flip L Around Y	93.6	53.2	63.8		

Table 1: Accuracy of the retrieved shape parameters for 'Sofa' on synthetic scenes. For continuous parameters, we report the mean absolute difference to the ground truth parameters. For discrete parameters, we report the classification accuracy. We provide the results for the three variants described in Section 5.3 of the main paper.

Parameter		Full Method	No Refinement	No Refinement No Exploitation Term		
		Mean Absolute Difference to Ground Truth (\downarrow)				
	Legs Size [cm]	1.239	1.484	1.484		
	Leg Offset [cm]	3.483	2.667	6.562		
	Bottom Thickness [cm]	1.278	1.602	1.602		
	Bottom Size Scale	3.35	4.926	6.767		
Continuous Parameters	Seat Height [cm]	1.971	3.332	2.853		
net	Seat Width [cm]	1.793	4.089	4.559		
ran	Seat Depth [cm]	3.802	5.049	5.049		
Ра	Seat Thickness [cm]	1.08	1.333	1.333		
as	Back Height [cm]	$\bf 5.525$	7.329	10.273		
non	Backrest Scale	0.12	0.12	0.22		
tin	Back Thickness [cm]	1.296	1.424	1.424		
, On	Backrest Offset Scale	0.19	0.25	0.29		
\circ	Arm Depth Scale	0.78	0.83	0.92		
	Arm Height [cm]	3.401	4.579	4.579		
	Arm Width [cm]	1.708	1.845	1.845		
	Arm Thickness [cm]	0.766	0.777	0.777		
	Rotation [°]	0.506	17.148	17.192		
		Classification Accuracy (↑)				
Discrete P.	Legs Type	100.0	100.0	100.0		
reti	Has Leg Support	96.3	94.4	90.7		
iscı	Has Back	95.0	97.0	96.0		
D	Has Arms	94.0	90.0	81.0		

Table 2: Accuracy of the retrieved shape parameters for 'Chair' on synthetic scenes. For continuous parameters, we report the mean absolute difference to the ground truth parameters. For discrete parameters, we report the classification accuracy. We provide the results for the three variants described in Section 5.3 of the main paper.

	Parameter	Full Method	No Refinement	No Refinement No Exploitation Term		
92	2	Mean Absolute Difference to Ground Truth (\downarrow)				
Continuous Parameters	Width	17.842	33.853	35.956		
т	Height	2.361	3.671	2.67		
are	Depth	16.923	24.328	26.387		
S P	Top Thickness	1.132	1.471	1.471		
no	Mid Leg X Scale	0.17	0.2	0.21		
nu	Mid Leg Y Scale	0.15	0.19	0.21		
nti	Mid Board Z Scale	0.16	0.16	0.16		
ပိ	Rotation	1.462	24.316	27.207		
Ъ.		Classification Accuracy (↑)				
Discrete	Top Shape	90.5	64.0	60.0		
	Legs Type	87.8	68.0	70.0		
D	Has Mid Board	100.0	96.2	96.2		

Table 3: Accuracy of the retrieved shape parameters for 'Table' on synthetic scenes. For continuous parameters, we report the mean absolute difference to the ground truth parameters. For discrete parameters, we report the classification accuracy. We provide the results for the three variants described in Section 5.3 of the main paper.

		Classification accuracy [%] (\uparrow)			Chamfer
		Top Shape	Legs Type	Has Mid Board	Dist. [cm] (\downarrow)
a)	Random SP	50.65	32.04	47.87	58.6
table	w/o refinement	93.78	50.67	82.03	11.8
Ŧ	Full (Ours)	96.52	52.17	84.92	11.7
		Has Legs	Has Drawers		
Capinet	Random SP	54.167	43.75		19.7
	w/o refinement	56.25	68.75		0.6
	Full (Ours)	62.5	64.583		0.9

Table 4: Results of shape reconstruction for 'Cabinet' and 'Table' categories on the ScanNet scenes. An interesting observation is that in contrast to 'Sofa', 'Chair', and 'Table', we did not observe significant advantages when adding the refinement step to our search algorithm for the 'Cabinet' category. Even without refinement, MCTS performs very well which is indicated by a very low chamfer distance. The accuracy for 'Has Drawers' is somewhat low considering that it influences the 3D shape considerably. The shape of cabinets is ambiguous in terms of drawers, especially when we estimate the rotation as well. As the back side of cabinets is never shown in scenes from ScanNet, rotating cabinets by 180° will still result in geometrically consistent reconstruction.



Fig. 1: Additional qualitative results show that our method generalizes to a variety of scenarios. We observe that for all examples, retrieved models are geometrically consistent with the scene.

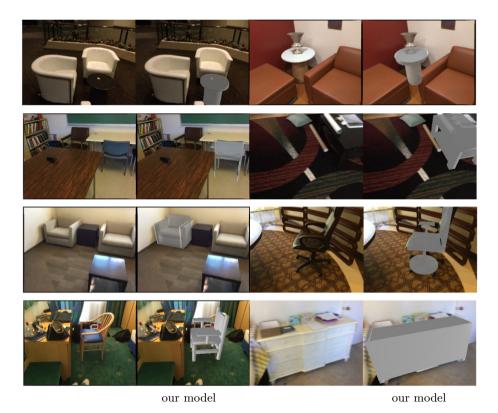


Fig. 2: Additional qualitative results show that our method generalizes to a variety of scenarios. The last row shows two failure cases, first a minor failure due to limitations in the design of our shape program for the chair category, and second, our reconstructed cabinet model is rotated by 180°. We observe that for all examples, retrieved models are geometrically consistent with the scene.

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2 PyTorchGeoNodes – Implementation Details

In this section, we provide additional details regarding the implementation of our PyTorchGeoNodes framework.

2.1 Computational Graph

Shape programs in PyTorchGeoNodes are represented as computational graphs. Therefore, for every functionality in the main paper, PyTorchGeoNodes implements a class with the corresponding functionality.

These functionalities are implemented in the form of nodes and edges:

- Nodes in our graphs are child classes of PyTorch base class torch.nn.Module to enable seamless integration into PyTorch code. Every node in the graph is associated with a unique id. When performing a forward pass, a node can take either default constants or outputs of other nodes as input. Therefore, nodes can contain multiple input and output sockets to enable flow of information through the computational graph.
- Edge is a data structure with four attributes. 'Input node' and 'Output node' define the identifiers of individual nodes that are connected by the edge. 'Input socket' and 'Output socket' define the corresponding sockets. Therefore, a node can be associated with several input and output edges, and an edge is always shared between exactly two nodes.

During a forward pass, we use a hash map that keeps track of the output sockets of individual nodes such that they can be easily accessed by nodes by simply querying the correct hash. Every 'Input node' in the graph parses named parameters, or shape parameters, and initializes the hash map that is updated with each forward call of nodes in the graph. Finally, we accumulate outputs of 'Output nodes' as a list of output geometries. Note that in our experiments we only consider computational graphs that have one output.

2.2 Efficient Implementation

As computational graphs increase in size (in our experiments, graphs can have between 100 and 200 nodes) so does the computational time which is why we considered different ways to improve the efficiency of PyTorchGeoNodes.

Note that, by default, computational nodes are not necessarily pre-sorted in optimal order. A node could request an input that has not been computed yet. As this would lead to several complications and the usage of recursive calls, which would in turn lead to computational bottlenecks, we implement a different solution. During the generation of the computational graph, nodes are sorted into a list using topological sort: Based on dependencies in a graph, we ensure that a node always appears after nodes that it is dependent on. For example, 'Input nodes' and other nodes that do not require any inputs will appear first, and 'Output nodes' will be the last nodes after sorting. Then during inference, we

can simply iterate this list, as inputs for nodes will be readily available once the forward pass of the nodes is invoked.

In addition, we observed that some nodes in a graph do not necessarily depend on any inputs. For example, instantiating an initial geometric primitive does not necessarily depend on any parameters. In this case, we implement caching such that the output of such nodes does not need to be recomputed during every forward pass.

Search Algorithm – Implementation Details

In this section, we discuss implementation details regarding our search algorithm.

Discretizing continuous parameters. When organizing our search tree, along with discrete shape parameters we also include discretized values for continuous parameters. For a given valid range of a parameter, we generate discrete values in linear steps of 0.1. This value is fitting for all parameters since they are represented in meters, or as aspect ratio relative to other parameters. In the case of object rotation, we use discrete steps of size 45°.

Shape parameter tree. As briefly mentioned in the main paper, it is beneficial to organize the search tree in such a way that geometrically more similar objects are part of the same subtree. The order in which different shape parameters appear in the tree is defined based on the influence of the parameter on the final geometry. More exactly, first, we randomly initialize shape parameters \mathcal{P} and generate the corresponding initial 3D shape $Sh(\mathcal{P})$. Then for a parameter p and its discrete values $v_p \in p$, we modify the initial shape parameters $\mathcal{P}(v_p)$, generate the 3D shape $Sh(\mathcal{P}(v_n))$, and calculate the chamfer distance CD to the initial 3D shape. Then, the influence of a shape parameter is calculated as:

$$\mathcal{I}(P) = \sum_{v_p \in p} \left(CD(Sh(\mathcal{P}), Sh(\mathcal{P}(v_p))) - \mu_{CD} \right)^2, \tag{1}$$

where μ_{CD} is the mean of chamfer distances for parameter p. We average \mathcal{I} over 100 instances of initial shapes to obtain the final influence of the parameter. This equation ensures that both geometric influence, as well as the number of individual discrete values for a parameter, are taken into account when determining the order of nodes in a tree.

Search details. As discussed in the main paper, MCTS depends on several different hyper-parameters. Based on empirical observations from our synthetic experiments, we use the following configuration:

- Total number of iterations is set to 300;
- Number of simulations is set to 50. Setting this number high helps avoid local minima in early iterations of MCTS. However, this number is only used in early iterations of MCTS, as every time a simulation selects a solution that was already visited, we conclude the simulation as it is likely that this subtree is already well-explored;
- We set $\lambda = 0.2$ to weight the exploration term during the selection phase;

111	fore, we only perform optimization if a leaf node is reached during the se-	111
112	lection phase, and skip optimization if the solution is reached during the	112
113	simulation phase of MCTS. This way, we make sure that we only optimize	113
114	good solutions.	114
115	4 Shape Program Designs for Validation	115
116	Here, we provide more details on our designs of individual shape programs.	116
117	'Cabinet' consists of 12 parameters, 8 continuous, 3 boolean, and 1 integer	117
118	parameter:	118
110	- 'Width', 'Height', and 'Depth' are continuous parameters that control the	110
119	width, height and depth of a cabinet in meters. The valid ranges of values	119
120		120
121	are [0.3, 2.0], [0.3, 2.5] and [0.1, 0.6], respectively;	121
122	- 'Board Thickness' is a continuous parameter that controls the thickness of	122
123	side boards. The valid range of values is [0.01, 0.09];	123
124	- 'Has Back' is a boolean parameter that controls whether a cabinet has a	124
125	back board;	125
126	- 'Has Legs' is a boolean parameter that controls whether a cabinet has legs;	126
127	- 'Leg Width', 'Leg Height', 'Leg Depth' are continuous parameters that con-	127
128	trol the width, height, and depth of legs in meters. The valid range is	128
129	[0.03, 0.1].	129
130	- 'Number of Dividing Boards' is an integer parameter that controls the num-	130
131	ber of dividing boards on a cabinet. The valid range of values is in [2, 5];	131
132	- 'Dividing Board Thickness' is a continuous parameter that controls the thick-	132
133	ness of dividing boards in meters. The valid range of values is in [0.01, 0.05];	133
134	- 'Has Drawers' is a boolean parameter that controls whether the cabinet has	134
135	drawers.	135

'Chair' consists of 20 parameters, 16 continuous, and 4 boolean parameters:

- 'Legs Type' is a boolean parameter that determines whether a chair has four

- 'Legs Size' is a continuous parameter that determines the thickness of a chair

- 'Has Leg Support' is a boolean parameter that controls whether legs of a

- 'Support Offset' is a continuous parameter that controls the height offset of

- 'Bottom Thickness' is a continuous parameter that controls the thickness of

- 'Bottom Size Scale' is a continuous parameter that controls the radius of the

bottom surface relative to seat width. The valid range is in [0.7, 1.0];

leg support relative to the seat height. The valid range of values is in [0, 0.5];

the bottom cylindric surface of one-legged chairs in meters. The valid range

in meters. The valid range of values is in [0.02, 0.08];

four-legged chair are connected with support elements;

legs or one leg in the middle.

of values is in [0.02, 0.08];

- We use the Adam optimizer during the optimization phase with the learning

Optimization is the computational bottleneck in our search algorithm. There-

rate set to $5e^{-2}$:

whether the sofa has arms;

directly under the arms:

[0.05, 0.3];

the 'L' extension;

in [0.05, 0.3], [0.5, 0.8], [0.6, 1.0];

153	- 'Has Back' is a boolean parameter that controls whether a chair has back	153
154	elements;	154
155	 'Back Height' is a continuous parameter that controls the height of the chair 	155
156	back in meters. The valid range is in $[0.3, 1.0]$;	156
157	- 'Backrest Scale' is a continuous parameter that scales length of backrest	157
158	relative to the height of the backrest. The valid range is in $[0.1, 1.0]$;	158
159	- 'Back Thickness' is a continuous parameter that controls the thickness of	159
160	the back elements in meters. The valid range is in $[0.02, 0.08]$;	160
161	 'Backrest Offset Scale' is a continuous parameter that positions the backrest 	161
162	relative to the height of the back. The valid range is in $[0.0, 1.0]$;	162
163	 'Has Arms' is a boolean parameter that controls whether a chair has arms; 	163
164	- 'Arm Depth Scale' is a continuous parameter that controls the arm depth	164
165	relative to the seat depth. The valid range is in $[0.5, 0.8]$;	165
166	- 'Arm Height' is a continuous parameter that controls the height of arms in	166
167	meters. The valid range is in $[0.1, 0.3]$;	167
168	- 'Arm Width' is a continuous parameter that controls the width of arms in	168
169	meters. The valid range is in $[0.08, 0.15]$;	169
170	- 'Arm Thickness' is a continuous parameter that controls the thickness of	170
171	arms in meters. The valid range is in $[0.02, 0.05]$.	171
172	'Sofa' consists of 18 parameters, 11 continuous parameters and 7 boolean	172
173	parameters:	173
113	parameters.	175
174	- 'Width', 'Height', 'Depth' are continuous parameters that control width,	174
175	height and depth of the base of a sofa in meters. The valid ranges are in	175
176	[0.5, 2.7], [0.3, 0.6] and [0.3, 0.6], respectively;	176
177	 'Has Legs' is a boolean parameter that controls whether the sofa has legs; 	177
178	- 'Leg Size' is a continuous parameter that controls the size of legs in meters.	178
179	The valid range is in $[0.03, 0.1]$;	179
180	- 'Has Left Arm' and 'Has Right Arm' are boolean parameters that control	180

- 'Arm Width', 'Arm Height', 'Arm Depth' are continuous parameters that

- 'Has Arm Legs' is a boolean parameter that controls whether a sofa has legs

- 'Has Back' is a boolean parameter that controls whether a sofa has a back;

- 'Back Height' and 'Back Depth' are continuous parameters that control the

- 'Is L-Shaped' is a boolean parameter that controls whether the sofa contains

- 'L Width' and 'L Depth' control the width and depth of the 'L' extension in

meters. The valid ranges are in [0.3, 0.5], [0.3, 1.0];

height and depth of the back in meters. The valid ranges are in [0.3, 0.7] and

control the width, height, and depth of arms in meters. The valid ranges are

- 'Seat Height', 'Seat Width', 'Seat Depth', 'Seat Thickness' are continuous

are [0.3, 0.9], [0.4, 0.8], [0.4, 0.6] and [0.04, 0.1], respectively:

parameters that control the geometry of the seat in meters. The valid ranges

197 198	'Table' consists of 10 parameters, 6 continuous, 2 boolean and 1 integer parameters:	197 198
199	- 'Width', 'Depth' and 'Height' are continuous parameters that control the	199
200	width, depth, and height of a table in meters. The valid ranges are in	200
201	[0.4, 4.0], [0.4, 1.3], [0.4, 1.5];	201
201	- 'Top' is a boolean that controls whether the shape of the top board of a	201
202	table is cylindrical or cuboidal;	202
203	- 'Top thickness' is a continuous parameter that controls the thickness of the	203
205	top in meters. The valid range is in [0.04, 0.1];	204
206	- 'Legs Type' is an integer parameter that controls whether a table has 1 in	206
207	the middle, or 2 legs, or 4 legs on the side.	207
208	- 'Mid Leg X Scale' and 'Mid Leg Y Scale' are continuous parameters that	208
209	scale the middle leg relative to the width and depth of the table. The valid	209
210	range for both parameters is in [0.05, 1.0];	210
211	- 'Has Mid Board' is a boolean parameter that controls whether a table has a	211
212	second board underneath the top;	212
213	- 'Mid Board Z Scale' is a continuous parameter that controls the offset of	213
214	the middle board relative to the height of the table. The valid range is in	214
215	[0.05, 0.5].	215
213	[0.00, 0.0].	213
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- 'Flip L Around Y' is a boolean parameter that controls whether the 'L'

extension is on the left or the right side of the couch.

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