

- ▶ Programming assignment 1: Send me an email if you have doubts.
- ▶ Python tutorial: 31/01/21 (Sunday), 5:30 PM to 7 PM.
 - ▶ Bhargav Prakash
 - ▶ Aditya Suraj Krishnan
 - ▶ Piyush Maheshwari

Simulated Annealing

Simulated Annealing

function SIMULATED-ANNEALING(*problem*, *schedule*)
inputs: *problem*, a problem
 schedule, a mapping from time to “temperature”

current \leftarrow MAKE-NODE(*problem*.INITIAL-STATE)

for $t = 1$ **to** ∞ **do**

T \leftarrow *schedule*(t)

if $T = 0$ **then return** *current*

next \leftarrow a randomly selected successor of *current*

$\Delta E \leftarrow$ *next*.VALUE $-$ *current*.VALUE

if $\Delta E > 0$ **then** *current* \leftarrow *next*

else *current* \leftarrow *next* only with probability $e^{\Delta E/T}$ \leftarrow

$$p = \frac{1}{e^{|\Delta E|/T}}$$

Simulated Annealing

Q. Suppose we are at state A initially and $f(\cdot)$ is the fitness function. There are two successor states B and C such that:

1. $f(B) - f(A) \leq 0$ and $f(C) - f(A) \leq 0$.
2. $|f(B) - f(A)| \ll \underbrace{|f(C) - f(A)|}_{\Delta E}$.

Simulated Annealing

- Q. Suppose we are at state A initially and $f(\cdot)$ is the fitness function. There are two successor states B and C such that:
1. $f(B) - f(A) < 0$ and $f(C) - f(A) < 0$.
 2. $|f(B) - f(A)| \ll |f(C) - f(A)|$.
- a. Initially, if T is large and current state is A , which state is more likely to be the next state: B or C ?

Simulated Annealing

- Q. Suppose we are at state A initially and $f(\cdot)$ is the fitness function. There are two successor states B and C such that:
1. $f(B) - f(A) < 0$ and $f(C) - f(A) < 0$.
 2. $|f(B) - f(A)| \ll |f(C) - f(A)|$.
- a. Initially, if T is large and current state is A , which state is more likely to be the next state: B or C ?
- b. If T is not very large and current state is A , which state becomes more likely to be the next state: B or C ?

Simulated Annealing

- Q. Suppose we are at state A initially and $f(\cdot)$ is the fitness function. There are two successor states B and C such that:
1. $f(B) - f(A) < 0$ and $f(C) - f(A) < 0$.
 2. $|f(B) - f(A)| \ll |f(C) - f(A)|$.
- a. Initially, if T is large and current state is A , which state is more likely to be the next state: B or C ?
 - b. If T is not very large and current state is A , which state becomes more likely to be the next state: B or C ?
 - c. When T becomes close to zero and current state is A , which state becomes more likely to be the next state: B or C ?

- ▶ Chapter 4: Only section 4.1

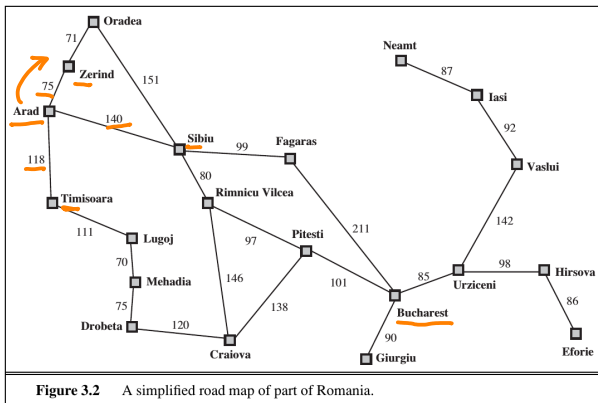
- ▶ Chapter 4: Only section 4.1
- ▶ Problem solving agents (Chapter 3)
 - ▶ Path from initial state to goal state is important.

Problem Solving Agents

- ▶ Focus on problems that have a **fixed sequence of actions** as their solutions.
- ▶ We have a problem solving agent that has to find the shortest path between two cities in Romania.

- ▶ The agent has knowledge about the environment in the form of state space.
- ▶ State space: initial state, actions, transition model.
- ▶ Goal test


State Space Graph



- ▶ Initial state = $In(\text{Arad})$
- ▶ Actions = $\{ go(\text{Sibiu}), go(\text{Timisoara}), go(\text{Zerind}) \}$
- ▶ Goal state = $\{ In(\text{Bucharest}) \}$

- ▶ Step cost = $c(s, a, s')$
- ▶ Step costs are nonnegative.
- ▶ Path cost = sum of step costs
- ▶ **Solution** to a problem is an action sequence that leads from the initial state to a goal state.
- ▶ Performance measure = Path cost
- ▶ **Optimal solution** has the lowest path cost among all solutions.


Eight puzzle problem



7	2	4
5		6
8	3	1

Start State

	1	2
3	4	5
6	7	8



Goal State

Transition

How many states?

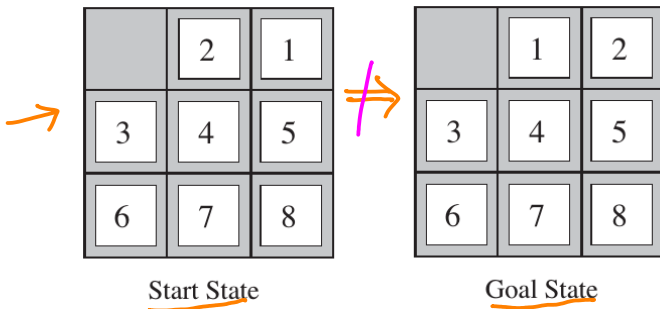
- ▶ How many starting positions are possible for Eight puzzle problem?

How many states?

- ▶ How many starting positions are possible for Eight puzzle problem?
- ▶ All of them are not solvable.

How many states?

- ▶ How many starting positions are possible for Eight puzzle problem?
- ▶ All of them are not solvable.



How many states?

- ▶ How many starting positions are possible for Eight puzzle problem?
- ▶ All of them are not solvable.

9

B	2	1
3	4	5
6	7	8

Start State

	1	2
3	4	5
6	7	8

Goal State

- ▶ Number of states in state space = $9!/2$

State Space for Eight puzzle problem

- ▶ Number of states = $9!/2$

$$20! = 2.433 \times 10^{18}$$

State Space for Eight puzzle problem

- ▶ Number of states = $9!/2$
- ▶ Initial state can be any state

State Space for Eight puzzle problem

- ▶ Number of states = $9!/2$
- ▶ Initial state can be any state
- ▶ Transition model tells how a state is affected by each action.

State Space for Eight puzzle problem

- ▶ Number of states = $9!/2$
- ▶ Initial state can be any state
- ▶ Transition model tells how a state is affected by each action.
- ▶ Actions = $\{Left, Right, Up, Down\}$

State Space for Eight puzzle problem

- ▶ Number of states = $9!/2$
- ▶ Initial state can be any state
- ▶ Transition model tells how a state is affected by each action.
- ▶ Actions = $\{Left, Right, Up, \underline{Down}\}$

What is the result state for actions *Left* and *Down*?

7	2	4
5	B	6
8	3	1

Start State

State Space for Eight puzzle problem

- ▶ Number of states = $9!/2$
- ▶ Initial state can be any state
- ▶ Transition model tells how a state is affected by each action.
- ▶ Actions = $\{Left, Right, Up, Down\}$

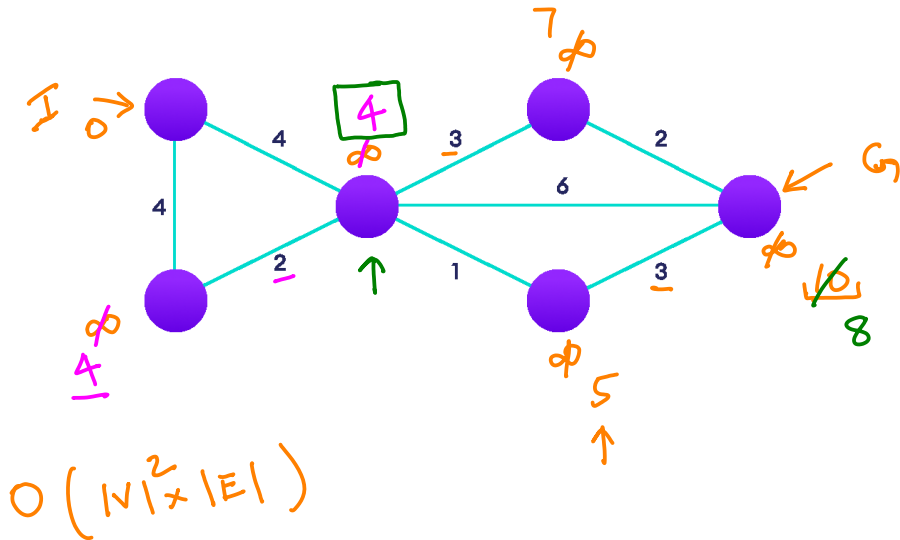
What is the result state for actions *Left* and *Down*?

7	2	4
5		6
8	3	1

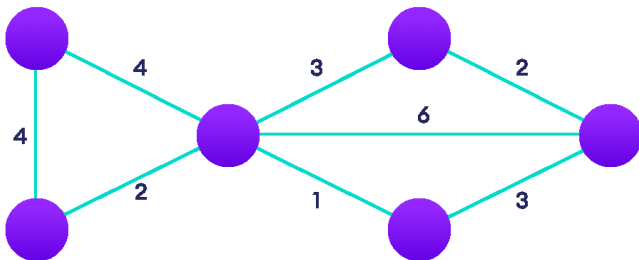
Start State

- ▶ Each step costs 1, and path cost is the number of steps from initial state to the goal state.

Dijkstra's algorithm



Dijkstra's algorithm



- Can we use Dijkstra's algorithm to solve the problems that we have discussed? Will the algorithm run in polynomial time?