

Iterative Deepening Search

$O(b^d)$

$O(bd)$

```
function ITERATIVE-DEEPENING-SEARCH(problem) returns a solution, or failure
  for depth = 0 to  $\infty$  do
    result  $\leftarrow$  DEPTH-LIMITED-SEARCH(problem, depth)
    if result  $\neq$  cutoff then return result
```



Figure 3.18 The iterative deepening search algorithm, which repeatedly applies depth-limited search with increasing limits. It terminates when a solution is found or if the depth-limited search returns *failure*, meaning that no solution exists.

Iterative Deepening Search

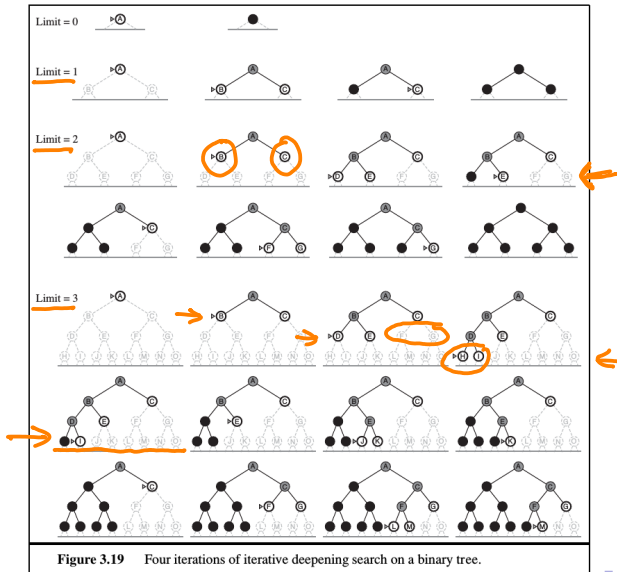


Figure 3.19 Four iterations of iterative deepening search on a binary tree.

Iterative Deepening Search

Time complexity:

$$N(\text{IDS}) = \underbrace{(d)b} + \underbrace{(d-1)b^2} + \cdots + \underbrace{(1)b^d}, \quad \begin{matrix} \downarrow \downarrow \downarrow \\ = \underline{O(b^d)} \end{matrix}$$

if $b = 10$ and $d = 5$, the numbers are

$$N(\text{IDS}) = \underline{50} + \underline{400} + 3,000 + 20,000 + \underline{100,000} = \underline{123,450} \quad \leftarrow$$

$$\underline{N(\text{BFS})} = 10 + 100 + 1,000 + 10,000 + \underline{100,000} = \underline{111,110} \quad \leftarrow$$

$\uparrow \quad \uparrow$

Iterative Deepening Search

Time complexity:

$$N(\text{IDS}) = (d)b + (d-1)b^2 + \dots + (1)b^d,$$

if $b = 10$ and $d = 5$, the numbers are

$$N(\text{IDS}) = 50 + 400 + 3,000 + 20,000 + 100,000 = 123,450$$

$$N(\text{BFS}) = 10 + 100 + 1,000 + 10,000 + 100,000 = 111,110$$

► Complete and optimal?

Iterative Deepening Search

Time complexity:

$$N(\text{IDS}) = (d)b + (d-1)b^2 + \dots + (1)b^d,$$

if $b = 10$ and $d = 5$, the numbers are

$$N(\text{IDS}) = 50 + 400 + 3,000 + 20,000 + 100,000 = 123,450$$

$$N(\text{BFS}) = 10 + 100 + 1,000 + 10,000 + 100,000 = 111,110$$

- ▶ Complete and optimal?
- ▶ Space complexity?

$$O(b^d)$$

Iterative Deepening Search

Time complexity:

$$N(\text{IDS}) = (d)b + (d-1)b^2 + \dots + (1)b^d,$$

if $b = 10$ and $d = 5$, the numbers are

$$N(\text{IDS}) = 50 + 400 + 3,000 + 20,000 + 100,000 = 123,450$$

$$N(\text{BFS}) = 10 + 100 + 1,000 + 10,000 + 100,000 = 111,110$$

- ▶ Complete and optimal?
- ▶ Space complexity? $O(\underbrace{bd})$

Bidirectional Search

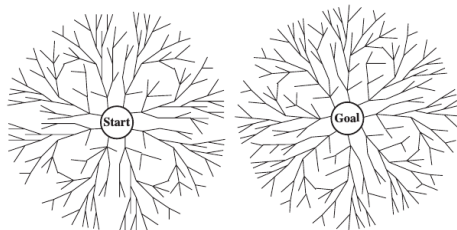


Figure 3.20 A schematic view of a bidirectional search that is about to succeed when a branch from the start node meets a branch from the goal node.

Bidirectional Search

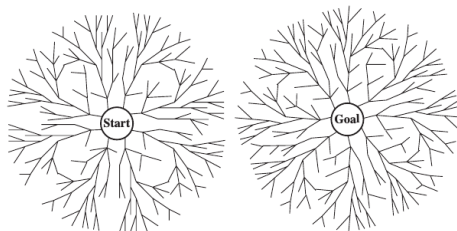


Figure 3.20 A schematic view of a bidirectional search that is about to succeed when a branch from the start node meets a branch from the goal node.

- Can we do bidirectional search for 8 puzzle problem?

Bidirectional Search

- ▶ Will bidirectional search be useful? Why?

$$\frac{d}{b}$$

$$2^{10} = \underline{1024}$$

$$2 \cdot \frac{d}{b}$$

↑

$$2^5 = 32$$

64

$$d = 10$$
$$b = 2$$

Bidirectional Search

- ▶ Will bidirectional search be useful? Why?
- ▶ Can bidirectional search be used for all problems?

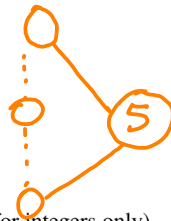
Bidirectional Search

- ▶ Will bidirectional search be useful? Why?
- ▶ Can bidirectional search be used for all problems?
- ▶ Knuth's problem

Bidirectional Search

- ▶ Will bidirectional search be useful? Why?
- ▶ Can bidirectional search be used for all problems?
- ▶ Knuth's problem

[5, 6]



The problem definition :

-
- **States:** Positive numbers.
 - **Initial state:** 4.
 - **Actions:** Apply factorial, square root, or floor operation (factorial for integers only).
 - **Transition model:** As given by the mathematical definitions of the operations.
 - **Goal test:** State is the desired positive integer.



$$\lfloor \sqrt{\sqrt{\sqrt{\sqrt{\sqrt{(4!)!}}}}} \rfloor = 5$$

Uninformed Search Strategies

Criterion	Breadth-First	Uniform-Cost	Depth-First	Depth-Limited	Iterative Deepening	Bidirectional (if applicable)
Complete?						
Time						
Space						
Optimal?						

Figure 3.21 Evaluation of tree-search strategies. b is the branching factor; d is the depth of the shallowest solution; m is the maximum depth of the search tree; l is the depth limit. Superscript caveats are as follows: ^a complete if b is finite; ^b complete if step costs $\geq \epsilon$ for positive ϵ ;

Uninformed Search Strategies


Criterion	Breadth-First	Uniform-Cost	Depth-First	Depth-Limited	Iterative Deepening	Bidirectional (if applicable)
Complete?	Yes ^a 					
Time	$O(b^d)$					
Space	$O(b^d)$					
Optimal?	Yes ^c					

Figure 3.21 Evaluation of tree-search strategies. b is the branching factor; d is the depth of the shallowest solution; m is the maximum depth of the search tree; l is the depth limit. Superscript caveats are as follows: ^a complete if b is finite; ^b complete if step costs $\geq \epsilon$ for positive ϵ ;

Uninformed Search Strategies

Criterion	Breadth-First	Uniform-Cost	Depth-First	Depth-Limited	Iterative Deepening	Bidirectional (if applicable)
Complete?	Yes ^a	Yes ^{a,b}				
Time	$O(b^d)$	$O(b^{1+\lceil C^*/\epsilon \rceil})$				
Space	$O(b^d)$	$O(b^{1+\lceil C^*/\epsilon \rceil})$				
Optimal?	Yes ^c	Yes				

Figure 3.21 Evaluation of tree-search strategies. b is the branching factor; d is the depth of the shallowest solution; m is the maximum depth of the search tree; l is the depth limit. Superscript caveats are as follows: ^a complete if b is finite; ^b complete if step costs $\geq \epsilon$ for positive ϵ ; ^c optimal if step costs are all identical; ^d if both directions use breadth-first search.

Uninformed Search Strategies

Criterion	Breadth-First	Uniform-Cost	Depth-First	Depth-Limited	Iterative Deepening	Bidirectional (if applicable)
Complete?	Yes ^a	Yes ^{a,b}	No			
Time	$O(b^d)$	$O(b^{1+\lceil C^*/\epsilon \rceil})$	$O(b^m)$			
Space	$O(b^d)$	$O(b^{1+\lceil C^*/\epsilon \rceil})$	<u>$O(bm)$</u>			
Optimal?	Yes ^c	Yes	No			

Figure 3.21 Evaluation of tree-search strategies. b is the branching factor; d is the depth of the shallowest solution; m is the maximum depth of the search tree; l is the depth limit. Superscript caveats are as follows: ^a complete if b is finite; ^b complete if step costs $\geq \epsilon$ for positive ϵ ; ^c optimal if step costs are all identical; ^d if both directions use breadth-first search.

Uninformed Search Strategies

Criterion	Breadth-First	Uniform-Cost	Depth-First	Depth-Limited	Iterative Deepening	Bidirectional (if applicable)
Complete?	Yes ^a	Yes ^{a,b}	No	No		
Time	$O(b^d)$	$O(b^{1+\lceil C^*/\epsilon \rceil})$	$O(b^m)$	$O(b^\ell)$		
Space	$O(b^d)$	$O(b^{1+\lceil C^*/\epsilon \rceil})$	$O(bm)$	$O(b\ell)$		
Optimal?	Yes ^c	Yes	No	No		

Figure 3.21 Evaluation of tree-search strategies. b is the branching factor; d is the depth of the shallowest solution; m is the maximum depth of the search tree; ℓ is the depth limit. Superscript caveats are as follows: ^a complete if b is finite; ^b complete if step costs $\geq \epsilon$ for positive ϵ ; ^c optimal if step costs are all identical; ^d if both directions use breadth-first search.

Uninformed Search Strategies

Criterion	Breadth-First	Uniform-Cost	Depth-First	Depth-Limited	Iterative Deepening	Bidirectional (if applicable)
Complete?	Yes ^a	Yes ^{a,b}	No	No	Yes ^a	
Time	$O(b^d)$	$O(b^{1+\lceil C^*/\epsilon \rceil})$	$O(b^m)$	$O(b^\ell)$	$O(b^d)$	
Space	$O(b^d)$	$O(b^{1+\lceil C^*/\epsilon \rceil})$	$O(bm)$	$O(b\ell)$	$O(bd)$	
Optimal?	Yes ^c	Yes	No	No	Yes ^c	

Figure 3.21 Evaluation of tree-search strategies. b is the branching factor; d is the depth of the shallowest solution; m is the maximum depth of the search tree; ℓ is the depth limit. Superscript caveats are as follows: ^a complete if b is finite; ^b complete if step costs $\geq \epsilon$ for positive ϵ ; ^c optimal if step costs are all identical; ^d if both directions use breadth-first search.

Uninformed Search Strategies

Criterion	Breadth-First	Uniform-Cost	Depth-First	Depth-Limited	Iterative Deepening	Bidirectional (if applicable)
Complete?	Yes ^a	Yes ^{a,b}	No	No	Yes ^a	Yes ^{a,d}
Time	$O(b^d)$	$O(b^{1+\lceil C^*/\epsilon \rceil})$	$O(b^m)$	$O(b^\ell)$	$O(b^d)$	$O(b^{d/2})$
Space	$O(b^d)$	$O(b^{1+\lceil C^*/\epsilon \rceil})$	$O(bm)$	$O(b\ell)$	$O(bd)$	$O(b^{d/2})$
Optimal?	Yes ^c	Yes	No	No	Yes ^c	Yes ^{c,d}

Figure 3.21 Evaluation of tree-search strategies. b is the branching factor; d is the depth of the shallowest solution; m is the maximum depth of the search tree; ℓ is the depth limit. Superscript caveats are as follows: ^a complete if b is finite; ^b complete if step costs $\geq \epsilon$ for positive ϵ ; ^c optimal if step costs are all identical; ^d if both directions use breadth-first search.

Informed (Heuristic) Search Strategies

- ▶ Evaluation function $f(n)$
- ▶ Heuristic function $h(n)$

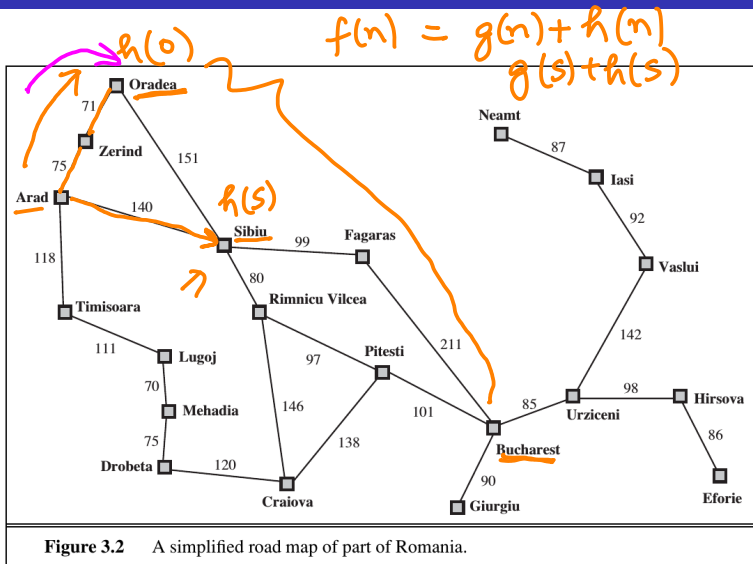
$g(n)$

$f(n)$

A^* search

$$f(n) = g(n) + h(n)$$

Informed (Heuristic) Search Strategies



Straight Line Distances

h_c



	Arad	<u>366</u>	Mehadia	241	
	Bucharest	<u>0</u>	Neamt	234	
	Craiova	160	Oradea	380	
	Drobeta	242	Pitesti	100	
	Eforie	161	Rimnicu Vilcea	193	
	Fagaras	176	Sibiu	253	
	Giurgiu	77	Timisoara	329	
	Hirsova	151	Urziceni	80	
	Iasi	226	Vaslui	199	
	Lugoj	244	Zerind	374	

Figure 3.22 Values of h_{SLD} —straight-line distances to Bucharest.

Greedy Best-first Search

- ▶ Evaluation function $f(n) = h(n)$

Greedy Best-first Search

- Evaluation function $f(n) = h(n)$

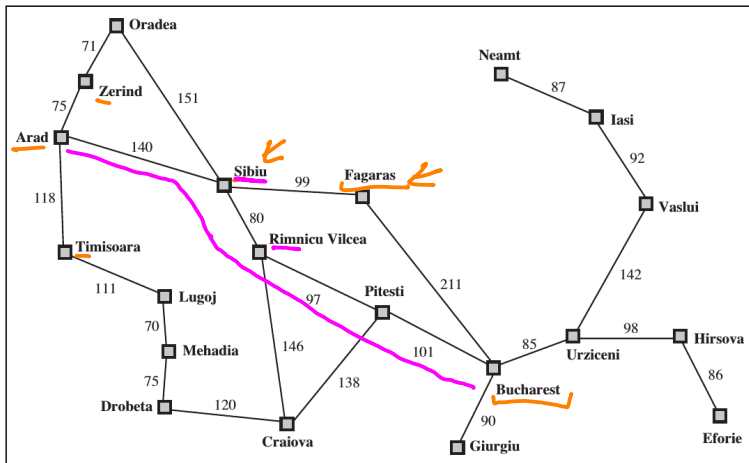


Figure 3.2 A simplified road map of part of Romania.