

Firms as Learning Environments: Implications for Earnings Dynamics and Job Search*

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Abstract

This paper studies the interactions between life-cycle career outcomes, workplace heterogeneity, and search frictions. I demonstrate that differences in firms' promotion of human capital accumulation significantly influence life-cycle earnings inequality. This suggests that the increase in inequality over the life cycle reflects not only inherent worker differences, but also differences in luck that arise due to search frictions. Using administrative micro data from Germany, I show that different establishments offer systematically different earnings growth rates for their workers. To rationalize this fact, I develop a life-cycle search model with heterogeneous workers and firms. In the model, a worker's earnings can grow through both human capital accumulation and labor market competition channels. Human capital growth depends on both the worker's ability and the firm's learning environment. I find that differences in firm learning environments account for 41% of the increase in cross-sectional earnings variance over the life cycle, and that this channel is especially important for young workers. I then argue that differences in labor market histories partially shape the worker-specific income profiles estimated by reduced-form statistical earnings processes. Finally, because young workers do not fully internalize the benefits of matching to high-growth firms, I demonstrate that changes to the structure of unemployment insurance policies can incentivize these workers to search for better matches.

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1 Introduction

Earnings dispersion across workers rises over the life cycle: there is more inequality among older workers than among younger workers. Studying the life-cycle patterns of inequality provides clues about the sources of overall earnings dispersion. This paper argues that nearly half of the rise in inequality over the life cycle is caused by differences in the firms by which workers are employed. At some firms, earnings grow systematically faster, even controlling for the growth that is specific to their employees. As different workers spend different amounts of their lives in high wage-growth firms, earnings inequality rises over the life cycle. This finding shows that persistent earnings inequality is not purely a matter of intrinsic heterogeneity among workers, but also a matter of luck.

A long literature has studied the sources of earnings inequality. An important contributor is human capital differences across workers. These differences between individuals may be present at labor market entry and develop further as workers gain job experience.¹ Another source of earnings inequality comes from search frictions. Similar workers looking for jobs differ in the types of offers they receive. This determines whether they are able to match with high-paying firms and how much their earnings grow on the job. As a result, differences in earnings arise due to luck in the search process.²

In this paper, I offer a new insight into the interactions between these two sources of inequality, and quantify how it contributes to the rise in earnings inequality over the life cycle. To do so, I delve into the sources of earnings growth. Motivated by the empirical finding that the growth rate of earnings differs across employers, I argue that luck of the draw in employer, due to search frictions, matters for a worker's growth rate of human capital. I build a search model of the labor market in which earnings can grow due to: differences in ability across workers, labor market competition, and differences in human capital promotion, or "learning environments," across firms. I use the model along with micro data to disentangle these channels and find that the firm component of human capital is a core contributor to the increase in cross-sectional earnings variance over the life cycle. I then show that these results matter for understanding the determinants of the labor income process, and for the role of policy in alleviating the inefficiencies induced by search frictions.

Using an administrative matched employer-employee data set from Germany, I show that establishments offer systematically different earnings growth rates to their workers. My data set allows me to observe the complete workforce of a subset of establishments and track workers through different jobs and through unemployment. I employ a two-way fixed effects specification to attribute growth in earnings to both worker and establishment effects. I find that variation in

¹See Huggett, Ventura and Yaron (2011) for an exploration of how initial human capital levels and differences in human capital growth rates across workers impact lifetime inequality.

²Hornstein, Krusell and Violante (2011) and Bagger et al. (2014) quantify the effect of search frictions on wage dispersion and wage growth, respectively.

the establishment effect is nearly as high as the worker effects. This result suggests that similar workers, even workers who may have inherently similar earnings growth rates, will experience different earnings trajectories depending on the establishment they happen to match with.

To understand the economic mechanisms that lead to this finding, I build a life-cycle search model of the labor market. The model features workers who search for jobs at firms that differ along two dimensions, productivity and learning environment.³ These firm attributes correspond to different reasons that can explain why earnings growth rates differ between firms. The first, productivity, affects a labor market competition channel. More productive firms are better able to raise wages to prevent workers from moving to competitor firms. The second, learning environment, governs the extent to which firms promote human capital accumulation. Some firms offer faster speeds of on-the-job learning, which increases productivity, and therefore wages in both the current job and subsequent jobs.

The key features of the model generate heterogeneity in earnings profiles across workers, even for similar workers employed at different firms. Workers in the model search on and off the job, accumulating human capital via learning-by-doing as they gain job experience. The speed of human capital growth for a given worker depends temporarily on the learning environment of the firm that the worker is matched with and permanently on the worker's level of learning ability. Apart from human capital growth, a worker's earnings growth is also impacted by labor market competition. Because workers can receive outside job offers while employed, they can also obtain earnings increases by moving to better paying firms or by using competing job offers to bargain for raises at their current firm.

The model implies that workers face trade-offs between a firm's productivity and learning environment. Because their ability to accumulate human capital declines over the life cycle, workers change how they value these two components between different ages. Learning environment is highly valued early in life, when human capital accumulation is highest. Workers who match to firms with better learning environments early in life receive permanently higher earnings throughout their lifetime. As human capital accumulation declines later in life, learning environment becomes irrelevant and workers only make decisions based on the firm's productivity. These changes in trade-offs drive the job search dynamics in the model and have quantitative impacts on the major sources of earnings differences across workers.

Identifying the parameters of this model is challenging because there are many distinct components to earnings growth: worker ability, firm productivity, and firm learning environment. In order to discipline the parameters, I construct new moments from the data that are separately informative about each of these growth components and use an indirect inference technique to match them in the model. The first set of moments disentangles firm productivity from learning environment and worker ability by comparing the earnings growth patterns of different-aged

³I focus on these two because in the past literature, both have been identified as major contributors to an *individual's* life-cycle earnings growth. See the survey paper by Rubinstein and Weiss (2006), or for models, Bagger et al. (2014) and Bowlus and Liu (2013).

workers employed at the same firm. Assuming human capital accumulation is low for older workers, I construct an informative measure of human capital accumulation across firms by exploiting the differences in within-job earnings growth of older versus younger workers. The second set of moments disentangles the worker component from the firm components of growth. I use two-way (worker and firm) fixed effects models on earnings growth, while taking into account the biases associated with estimating these statistical models in both the data and structural model.

I use the model to decompose the life-cycle profile of the log earnings variance. I find that the increase in earnings variance is almost entirely driven by dispersion in human capital. This result comes from both the differences in worker learning ability and firm learning environment. These two features mean that human capital grows at different rates across workers. As a result, the dispersion in human capital increases as workers age. On the other hand, the dispersion in the components of earnings coming from labor market competition decreases. This is because workers settle into a more homogeneous set of higher paying firms and extract a larger share of the match surplus. These are the standard forces present in a textbook job ladder model. A version of this model without heterogeneity in the growth rates of human capital would miss the rise in the earnings variance.

I next assess the contribution of differences in firm learning environments and find that they account for 41% of the increase in the life-cycle earnings variance. This result comes from a counterfactual in which I turn off all differences in worker learning ability. In this setting, all human capital differences arise solely due to luck in which firms workers meet. In addition, the impact of firms is concentrated early on in workers' careers. For example, I find that about 85% of earnings dispersion after 15 years in the labor market is due to human capital differences. Of this, half of the additional variance relative to labor market entry comes from the long-term impacts of workers' previous matches. As workers are able to catch up to each other and move to better firms, the role of firms declines.

My findings imply that firms play an important role in the formation of workers' human capital. This result sheds light on the properties of reduced-form labor income processes. Statistical models of earnings estimated from panel data on workers find that individuals appear to face different earnings profiles. These tend to be attributed to permanent worker differences, like learning ability.⁴

Using the earnings "data" generated by the model, I estimate some of the commonly-used labor income processes from the literature.⁵ I found that the model is able to microfound these income processes. I also find that the income processes pick up profile heterogeneity, even in the version of the model without permanent differences in worker ability. This suggests that some of the differences in income profiles come from the series of firms a worker matches with over their lifetime, which is not detectable in the panel data sets that are typically used in this context.

⁴Huggett, Ventura and Yaron (2011)'s model generates this type of profile heterogeneity through differences in worker learning ability and idiosyncratic shocks to human capital.

⁵Specifically, I estimate Guvenen (2009) and Guvenen (2007)'s RIP and HIP processes.

The model also has important implications for worker welfare and the design of unemployment insurance (UI) policies. My findings also imply that some differences in earnings growth come about due to search and matching frictions (or differences in luck), and not due to permanent, individual differences in skill. The jobs workers accept, particularly early on in life, have permanent impacts on human capital and hence lifetime inequality. Because workers do not fully internalize the long-term impacts of human capital accumulation, the decentralized allocation of workers to firms is inefficient. The structure of UI in the model impacts workers' ranking of firms, which means it can be used to affect the allocation.

I find that age-dependent UI schedules can improve welfare and reduce lifetime inequality relative to the benchmark model. The best UI schedules offer the highest benefit levels to young workers and reduce them with age. This induces young workers to be selective in which jobs to accept early on, particularly along the learning environment dimension. Welfare improves since the matches formed result in persistently higher lifetime earnings. Inequality is reduced by giving all workers a chance to find jobs that will boost their earnings throughout their lives. This experiment offers an example in which UI policies impact long-term outcomes, in contrast to most other settings where they are used as insurance for short-term episodes like job loss.

1.1 Related literature

This paper is related to several strands of literature. Understanding the formation of human capital has been a longstanding research goal, going back to Becker (1962), Ben-Porath (1967), and Heckman (1976). A more recent complementary set of work, most notably, Herkenhoff et al. (2018) and Jarosch, Oberfield and Rossi-Hansberg (2019), explores how the quality of one's coworkers impacts human capital. This paper, in contrast, views firm differences in earnings growth as coming from intrinsic firm characteristics. I also emphasize the ability of this channel to account for life-cycle features of earnings, and identify the model via establishment fixed effects.

This paper also relates to the long literature on the determinants of life-cycle earnings profiles (for a survey, see Rubinstein and Weiss (2006)). There has been more recent work, such as Bagger et al. (2014) and Bowlus and Liu (2013), that decomposes the contributions of human capital growth, labor market competition, and bargaining power to life cycle earnings growth. This paper performs a similar decomposition, but emphasizes how heterogeneous firm learning environments shape the earnings *variance* profile.

Another paper that has explored the forces behind the earnings variance profile is Huggett, Ventura and Yaron (2011). They use exogenous human capital shocks and worker learning ability heterogeneity in a consumption/savings model to generate the increase in life-cycle variance. More broadly, the focus of the paper is to study the roles of initial conditions (level of human capital, learning ability, wealth) versus luck (shocks to human capital) in determining differences in life-time income. In contrast, my paper explores another "luck" channel that contributes to the rise in

life-cycle earnings variance: the types of firms workers meet in a frictional labor market. Because my focus is only on forces that could explain the rise in variance, I only concentrate on a single initial condition, differences in learning ability.

This paper also draws features from several prominent labor search models. The wage bargaining protocol adopts the sequential auction framework of Cahuc, Postel-Vinay and Robin (2006). The rest of the model combines parts of Bagger et al. (2014) and Jarosch (2015). Like Bagger et al. (2014), I allow for deterministic human capital growth and adopt piece-rate wage contracts. As in Jarosch (2015), firms differ according to two dimensions: there, productivity and separation rate; here, productivity and learning environment.

The results of this paper also connect to the vast literature that estimates statistical models of the labor income process. Some early examples are MaCurdy (1982); Abowd and Card (1989). I connect my results to this set of work by building a structural model that microfound these earnings processes and highlights the economic mechanisms that generate their main features. In particular, this paper closely relates to the work of Guvenen (2009) and Guvenen (2007) on income profile heterogeneity. Using income and consumption data from the PSID, these papers find evidence that individuals face heterogeneous income profiles. This paper proposes a potential source of profile heterogeneity, in which the earnings profiles of different firms partially piece together a given individual's profile.

Finally, this paper also represents an extension to the existing body of work relating firms and labor market outcomes (Abowd, Kramarz and Margolis (1999); Card, Heining and Kline (2013)). These papers document dispersion in firm-specific wage premia that impact the level of wages for all employees within the firm. In many countries, this firm component of inequality is a major contributor to overall inequality.⁶ This paper documents a similar fact, but for wage *growth*. In addition, this literature has focused on the impacts of contemporaneous firm/worker relationships. This paper introduces one mechanism in which a worker's previous employers impacts his or her earnings in the future.

A related paper that links firms to earnings dynamics is Friedrich et al. (2019). They quantify the transmission of firm-level shocks to workers' stochastic wage processes, finding a large contribution of firms to the cross-sectional variance of wages over the life cycle. In contrast, I study the persistent impacts of firm-specific wage growth trends, yet also find a substantial role for firms in accounting for the cross-sectional variance.

The remainder of this paper proceeds as follows. Section 2 presents some motivating evidence from the data that demonstrates the extent of the establishment heterogeneity in earnings profiles. Section 3 describes the search model that allows for sources of earnings growth to differ between firms. In Section 4, I discuss how I use the data to identify the new features that my

⁶Past findings that support this include Song et al. (2015) for the United States, Card, Heining and Kline (2013) for Germany, Håkanson, Lindqvist and Vlachos (2015) for Sweden, Borovičková and Shimer (2017) for Austria, Schaefer and Singleton (2016) for the United Kingdom, and Alvarez, Engbom and Moser (2015) for Brazil.

model introduces. Section 5 discusses the parameter values and model fit. Section 6 presents the model's predictions and counterfactuals for the life-cycle variance of earnings. Section 7 estimates reduced-form earnings processes from different versions of the model. Section 8 shows how changes in unemployment benefits schedules affect worker outcomes in the model. Section 9 concludes.

2 Motivating Evidence

2.1 Data Description

The main data source is an administrative matched employer-employee dataset from Germany, provided by the Research Data Center of the German Federal Employment Agency at the Institute for Employment Research (IAB). The Linked-Employer-Employee Data (LIAB) longitudinal model combines administrative employment records with unemployment benefit receipts from the German social security system. The structure of this dataset enables me to observe the complete workforce of a random sample of establishments, as well as the employment biographies of the workers employed at these sample establishments.⁷ For a detailed description of this data set, see Klosterhuber et al. (2013), Fischer et al. (2009), and Heining et al. (2014).

All establishments in Germany are required to submit an annual record for each employee that worked there at any time in that year. The annual employment records in the data come in spell format and indicate the exact dates in each year during which the worker was employed at the establishment. Each record contains an establishment identifier and average daily earnings during the spell, as well as other observables like age, gender, education level, occupation, industry, and a full-/part-time indicator. The LIAB dataset contains all employment records for every worker employed at a subset of establishments between the years 2002 and 2010. Therefore, in these years I observe the complete workforce of these sample establishments. Beyond that, I get the employment biographies for each of these workers from 1993 to 2014. This means that I can track the worker through establishments not in the main sample, and through unemployment spells.

My baseline sample only uses the employment records of full-time workers, aged 20 to 60. I reorganize the data by first converting it from spell format to a monthly panel.⁸ Much of the analysis involves constructing a wage for each year of job tenure. To do this, I re-aggregate all the employment spells to the annual level using the average of the wages over each 12 month interval. All wages are in real terms, deflated by the German CPI with base year 2010. In this annual panel

⁷I observe data on establishments, rather than firms, meaning two Starbucks would be considered separate entities. It is not possible in these data to aggregate the establishments into their parent firms.

⁸The level of observation in the original data set is a spell, which is at the longest 1 year for a worker who is employed at a specific establishment for the entire year. There are shorter spells that cover the partial calendar years of employment. For example, if somebody works at an establishment from August 15, 2009 to March 2, 2011, there would be 3 records for the worker: one for August 15, 2009 to December 31, 2009; another for January 1, 2010 to December 31, 2010; another for January 1, 2011 to March 2, 2011.

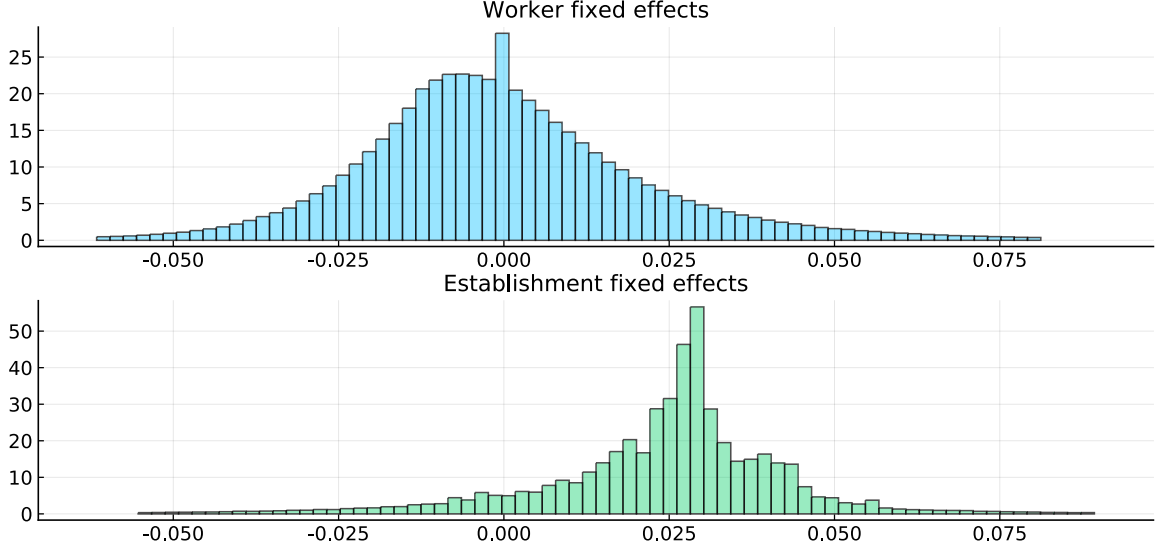


Figure 1: Distributions of worker and establishment wage growth fixed effects. Histograms of the estimated fixed effects for workers, α_i , and establishments, ψ_j , from equation (1) with $\beta = 0$. The α_i were normalized to have mean 0.

of employment spells, I end up with approximately 13.6 million worker-year observations, with approximately 1.1 million unique workers and 381,000 unique establishments.⁹

2.2 Heterogeneity in establishment-level earnings profiles

I begin with a simple empirical exercise which shows that establishments offer systematically different earnings growth profiles. I run regressions that are variations on the two-way fixed effects specification of Abowd, Kramarz and Margolis (1999): instead of the log wage *level* on the left-hand side, I use the *growth* in log wages. For worker i , employed at establishment j in year t , wage growth is defined as $\Delta \log w_{ijt} = \log w_{ijt} - \log w_{ijt-1}$. I run regressions of the following form, with log wage growth as the dependent variable:

$$\Delta \log w_{ijt} = \alpha_i + \psi_j + \gamma_t + \beta \mathbf{X}_{ijt} + \varepsilon_{ijt} \quad (1)$$

The covariates include a worker fixed-effect, α_i , an establishment fixed-effect, ψ_j , a set of year dummies, γ_t , and a set of time-varying worker and establishment characteristics \mathbf{X}_{ijt} . Note that all wage growth observations use only the observations of job-stayers, meaning that they do not include any wage growth that occurs during job-to-job transitions.

The fixed-effects are identified off workers who switch employers across years. When run in levels, these specifications have been widely used for understanding how innate worker and firm differences contribute to overall wage inequality. The correlation between the fixed effects can

⁹The establishment count includes establishments that are not in the core sample from 2002 to 2010.

also be used to measure assortative matching. In this application, I use it to separate worker-specific effects on wage growth, which could arise from differences in learning ability (among others), from establishment-specific wage growth effects, the sources of which will be considered extensively in the model. Worker-specific wage growth effects have been estimated on their own using panel data on workers¹⁰ However, less is known about the extent of the dispersion in the establishment fixed effects.

To get a sense of the dispersion in these fixed effects with a simple interpretation, I first estimate a version of (1) without any of the time-varying worker or establishment observables (imposing $\beta = 0$). This yields a distribution of worker and establishment fixed effects. Histograms of each are depicted in Figure 1. The specification with only year dummies allows for a simple interpretation of the fixed effects as the unconditional annual wage growth for a specific person or establishment.¹¹ I find that the dispersion in establishment effects is almost as large as the dispersion in worker effects: their standard deviations are 0.0262 and 0.0242, respectively.¹²

To better understand the role of this establishment heterogeneity on the wage growth of workers, I put an age and tenure profile in X_{ijt} , common to all workers and establishments. I estimate the following, separately for three different education groups, high school diploma or less, vocational degree, and college degree:

$$\Delta \log w_{ijt} = \alpha_i + \psi_j + \gamma_t + \beta_1 \text{age}_{it} + \beta_2 \text{age}_{it}^2 + \beta_3 \text{tenure}_{it} + \beta_4 \text{tenure}_{it}^2 + \varepsilon_{ijt} \quad (2)$$

Figure 2 provides some examples of how the establishment fixed effect impacts wage growth. Each panel constructs cumulative earnings profiles for identical workers who are employed in establishments at the 10th, 25th, 50th, 75th, and 90th percentiles of the fixed effect distribution.¹³ For instance, the right panel says that a college-educated worker with a given worker fixed-effect, who is hired by an establishment at age 25, can expect to see between a 0.12 and 0.40 increase in log earnings compared to their starting level after staying 6 years at each establishment. The heterogeneity in the slopes of the establishment wage profiles, captured by differences in the establishment fixed effect, means that similar workers will face very different wage trajectories just depending on their employer. These results suggest that employers themselves, as well as frictional barriers to which establishments workers match to, may play an important role in piecing together an individual's lifetime earnings profile.

¹⁰For example, Guvenen (2009)'s HIP (Heterogeneous Income Profiles) process allows workers to experience different permanent growth rates in income, along with some stochastic components.

¹¹In other words, take a worker with a fixed effect of zero employed at a firm with the average fixed effect of 0.024. This would predict an annual change in log wages of 0.024 within the spell.

¹²The correlation coefficient between the worker and establishment effects is -0.49. This should be interpreted with caution as a measure of assortative matching because of the well-known limited mobility bias present in AKM, which biases the covariance downward. See Abowd et al. (2004) and Andrews et al. (2008).

¹³Limited mobility bias also biases the variance of the fixed effect distributions upward. The example trajectories in Figure 2 address this concern by only taking into account establishments with fixed effects estimates between the 10th and 90th, or 25th and 75th percentiles; the outliers greatly inflate the variance.

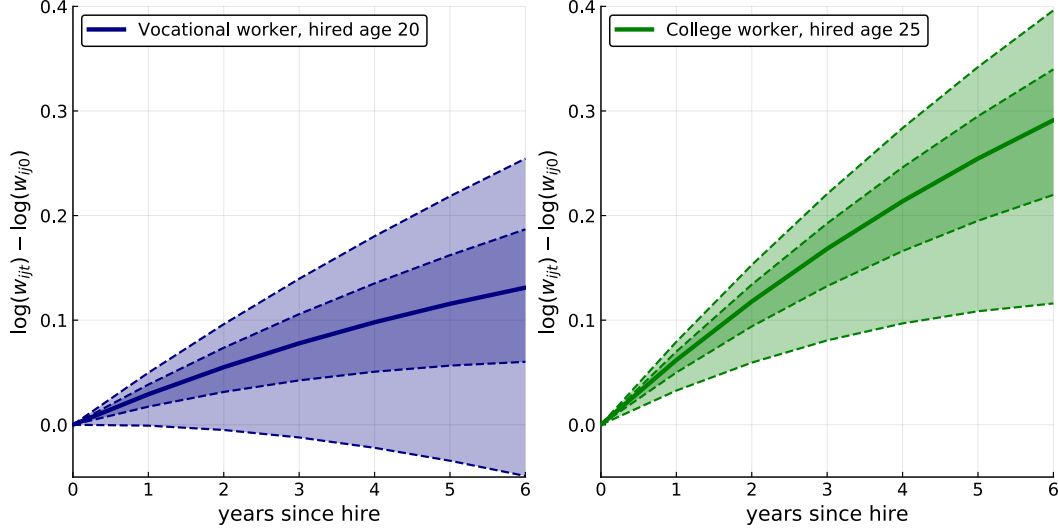


Figure 2: Establishment earnings growth profiles.

Each panel depicts profiles of cumulative earnings growth as a function of tenure for workers with the same education level, age of hire, and fixed effect α_i . Estimates of the age and tenure profiles and fixed effects distributions come from equation (2). Each profile is constructed by computing the predicted values of earnings growth for each implied tenure and age horizon and taking the cumulative sum. Each series from bottom to top corresponds to the earnings growth profile of the establishment at the 10th, 25th, 50th, 75th, and 90th percentiles of the establishment fixed effect, ψ_j , distribution.

The differences in worker and establishment earnings profiles documented thus far have no structural interpretation. The rest of this paper aims to understand the economic mechanisms that generate them. In the next section, I introduce a model that formalizes how and why workers and firms exhibit different earnings growth patterns.

3 Model

This section develops a search model of the labor market, featuring heterogeneity on both the worker and firm side. There is human capital accumulation, on-the-job search, and wage renegotiation.¹⁴ The key feature I add is a new source of firm heterogeneity, learning environment, which impacts the speed of its workers' human capital accumulation, and thus earnings. This new dimension¹⁵ introduces a source of persistence in earnings coming from a worker's history of matches. It also induces workers to change their job search strategies over the life cycle.

¹⁴I adopt the sequential auction framework of Cahuc, Postel-Vinay and Robin (2006). Like in Bagger et al. (2014), earnings depend on this endogenous piece-rate as well as human capital.

¹⁵Like Jarosch (2015), firms differ in two dimensions. In his case, it is productivity and job security; in my case it is productivity and learning environment.

3.1 Environment

One side of the economy consists of a unit mass of overlapping generations of workers. Workers face a deterministic life cycle, participating in the labor market from ages $t = 1, 2, \dots, T$. The age distribution is assumed to be constant at all times, meaning that a fraction $1/T$ of workers of age T leave the labor market each period and are replaced by new entrants. All workers are risk-neutral and consume a single homogeneous good. They discount the future at rate β .

Each period, workers can be either employed or unemployed. They also differ in human capital h , and learning ability a . They enter the labor market unemployed and endowed with the same initial level of human capital¹⁶, but draw learning ability a from a distribution $G(a)$. Learning ability affects an individual's speed of human capital accumulation and is fixed throughout the lifetime.

Search is random and undirected. Unemployed workers receive job offers each period with probability λ_U and employed workers receive offers with probability λ_E . A job offer is a draw from the exogenous cumulative distribution of firms, $F(\theta)$. The vector θ consists of two components, p and q , where p denotes the firm's productivity and q denotes the firm's learning environment.

Human capital accumulation is modeled as learning by doing. Human capital grows whenever a worker is employed, at a rate that depends on the worker's learning ability and age, as well as their employer's learning environment:

$$\log h' - \log h = (a + q) d(t) \quad (3)$$

This function says that the amount of human capital accumulated over a period is additive in the worker's learning ability and the firm's learning environment.¹⁷ $d(t)$ is a depreciation function that takes the form:

$$d(t) = \frac{\nu}{1 + \exp(\gamma(t - \alpha))} \quad (4)$$

The functional form in (4) ensures that human capital grows fastest early on in the life cycle. For the same inputs, a young worker accumulates more human capital compared to an old worker. As workers age, growth gradually slows down until at some point, they can no longer accumulate human capital. This captures the effect of forces such as declines in productivity or incentives to acquire more human capital that come with approaching retirement.¹⁸ To see how firms and the depreciation function impact human capital growth, some example profiles are depicted in Figure

¹⁶This assumption does not affect the increase in the variance profile, the main focus of the paper. Having heterogeneity in initial h would only shift the level of the variance profile. It also simplifies the parameterization because it avoids having to take a stand on the joint distribution of initial (a, h) .

¹⁷I have experimented with a more general form of the human capital accumulation function. One can introduce a CES term over (a, q) with an elasticity of substitution parameter that determines how workers sort to firms along these dimensions. It was difficult to identify the elasticity of substitution because the model is unable to generate much sorting – there is no scarcity of jobs because they are just modeled as draws from an exogenous distribution.

¹⁸Instead of endogenizing the decision to accumulate human capital as in Ben-Porath (1967), this functional form will impose that the earnings profile has the same shape as it would have in a human capital investment model.

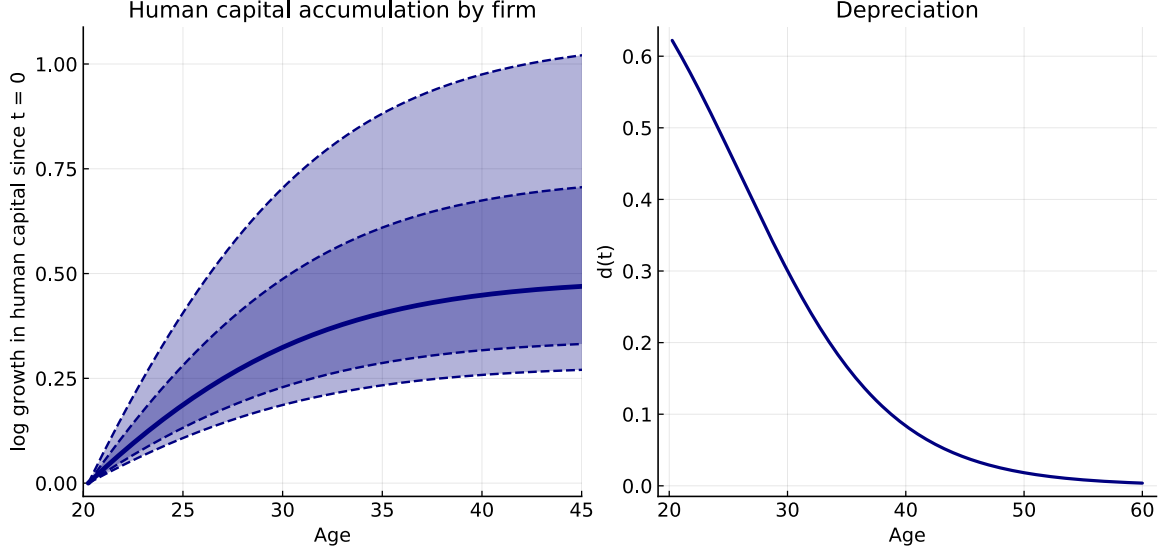


Figure 3: Human capital accumulation and depreciation functions.

The left panel shows how human capital growth in the calibrated model differs by firm, based on equation (3). It plots the log difference in human capital at age t from the log of its starting value at age 20. Each series from bottom to top corresponds to the human capital profile of the firm at the 10th, 25th, 50th, 75th, and 90th percentiles of the distribution of q , if that worker stays at the firm. Each compares the human capital growth of a worker with the same learning ability a . The right panel shows how the depreciation function $d(t)$ changes with age.

3.

The CES portion and the depreciation function together imply that the human capital production function in (3) will generate an increasing and concave life-cycle pattern of human capital for a given worker. This will help the match the life-cycle mean earnings profile in the data. The steepness of a worker's earnings profile permanently depends on learning ability and temporarily on the learning environment of the firm that the worker is matched with at a particular time. Human capital transfers perfectly across jobs¹⁹ and does not depreciate in unemployment.²⁰

If a worker and a firm form a match, they produce a flow of output ph . While employed, workers earn a flow of income phw , where w is an endogenously determined piece-rate, set according to the rules below. Matches break up with probability δ , and the worker subsequently flows to unemployment, where they earn a flow bh of income.

¹⁹I abstract from firm-specific human capital because of past literature that has shown that it is unlikely to be as important as general human capital, at least in the long-term. Bagger et al. (2014) do the same, motivated by an argument from Lazear (2009). Also, Nagypál (2007) finds that the impacts of match-specific human capital are only relevant during the first six months of an employment relationship.

²⁰This is for simplicity and does not affect any of the main outcomes. All that is needed is that human capital is always growing *less* in unemployment compared to any employment relationship.

3.2 Wage Determination

Wages, $w \leq 1$,²¹ are piece-rate contracts that determine the share of output paid to the worker. They are fixed and can only be re-bargained when workers move directly from one firm to another (a job-to-job transition) or when the worker receives a sufficiently good offer from another firm. Workers have bargaining power σ .

Let $M_t(a, h, \theta)$ denote the joint (worker + firm) value of a match between firm θ and a worker of learning ability a , human capital h , and age t . Additionally, let $V_t(w, a, h, \theta)$ be the value of employment to worker (a, h, t) at firm θ and current piece-rate w . Both $M_t(\cdot)$ and $V_t(\cdot)$ are increasing in all arguments.

The rules for updating the wage rate come from Cahuc, Postel-Vinay and Robin (2006) and Dey and Flinn (2005). When a worker employed at incumbent firm θ is contacted by poaching firm θ' , the two firms compete for the worker. The outcome is always that the firm who values the worker the most (has the highest joint match value) gets the worker.

Specifically, one of three cases will apply. In the first case, where $M_{t+1}(a, h, \theta') > M_{t+1}(a, h, \theta)$, the worker will move from firm θ to firm θ' . The worker's new piece-rate, w'_M will satisfy:

$$V_{t+1}(w'_M, a, h', \theta') = M_{t+1}(a, h', \theta) + \sigma (M_{t+1}(a, h', \theta') - M_{t+1}(a, h', \theta)) \quad (5)$$

In other words, the poaching firm delivers a wage that gives the worker the entire joint value at the incumbent firm plus share σ of the additional rents offered by matching with the poaching firm. The previous firm at which the worker was employed, θ , now becomes the worker's relevant outside option.

A second possibility is that the incumbent firm values the worker more than the poacher, but the poacher is able to offer a wage that delivers a value that is greater than the worker's current value. This happens when $M_{t+1}(a, h, \theta') < M_{t+1}(a, h, \theta)$ but there exists a w'_R that satisfies $V_{t+1}(w'_R, a, h', \theta) > V_{t+1}(w, a, h', \theta) \geq M_{t+1}(a, h, \theta')$. In this case, the worker stays at the incumbent firm θ , but the wage is re-bargained to make the worker indifferent between staying at θ and moving to θ' while extracting the full output of the match there. w'_R satisfies:

$$V_{t+1}(w'_R, a, h', \theta) = M_{t+1}(a, h', \theta') + \sigma (M_{t+1}(a, h', \theta) - M_{t+1}(a, h', \theta')) \quad (6)$$

In this case, the worker is using the outside offer to bargain an increase in the piece-rate. The worker's new relevant outside option is now firm θ' , the last job offer received that was used to bargain a piece-rate increase.

The third case is that the outside offer is dominated by a previous one. In that situation, the worker discards the job offer and continues at wage w .

²¹In principle, these can be negative: workers may be willing to accept negative starting piece-rates for the opportunity to work at a firm with a particularly high productivity or learning environment.

The process is similar for unemployed workers exiting unemployment and accepting a job at firm θ . Their starting piece-rate w'_u satisfies:

$$V_{t+1}(w'_u, a, h', \theta') = U_{t+1}(a, h) + \sigma(M_{t+1}(a, h, \theta') - U_{t+1}(a, h)) \quad (7)$$

In all cases, the new re-bargained piece-rate implicitly depends on the type of firm that the worker most recently used in a wage negotiation.²² As workers remain continuously employed, they build up more and better quality outside offers, resulting in higher piece-rates. This process will be referred to as search capital accumulation and I will think of the on-the-job piece-rate increases as the returns to search capital.

3.3 Bellman Equations

All value functions have terminal value 0 when the worker reaches age $T + 1$. The value function for an employed worker is:

$$\begin{aligned} V_t(w, a, h, \theta) = & phw + \underbrace{\beta\delta U_{t+1}(a, h)}_{\text{unemployment}} + \underbrace{\beta(1 - \lambda_E)(1 - \delta)V_{t+1}(w, a, h', \theta)}_{\text{no outside offer arrives}} \\ & + \underbrace{\beta\lambda_E(1 - \delta) \int \max\{V_{t+1}(w'_M(\theta'), a, h', \theta'), V_{t+1}(w'_R(\theta'), a, h', \theta), V_{t+1}(w, a, h', \theta)\} dF(\theta')}_{\text{worker gets outside offer and decides whether to leave, stay and rebargain, or do nothing}} \end{aligned} \quad (8)$$

At age t , the worker's earnings are phw . With probability δ , the worker receives a separation shock and moves to unemployment, without getting to accumulate human capital. If no separation shock and no outside offer arrives, the worker stays at firm θ on piece-rate w . Human capital increases to h' , as governed by (3) and depends on the current firm's learning environment, q . If an outside offer from firm θ' arrives, the worker will either accept it and move to firm θ' on piece-rate w'_M , stay at θ and renegotiate the piece-rate to w'_R , or discard it. The value function in the first two cases corresponds to the promised values from the wage determination rules in (5) and (6). In any of these three cases, human capital is always updated according to the learning environment q of the incumbent firm θ .

The value function of an unemployed worker is the following:

$$U_t(a, h) = bh + \beta\lambda_U \underbrace{\int \max\{V_{t+1}(w'_u(\theta'), a, h, \theta'), U_{t+1}(a, h)\} dF(\theta')}_{\text{accept or reject job offer}} + \beta(1 - \lambda_U)U_{t+1}(a, h) \quad (9)$$

²²As shown by Cahuc, Postel-Vinay and Robin (2006), these wage setting rules microfound the bargaining game of Rubinstein (1982).

Each period, unemployed workers earn benefits proportional to their human capital, bh . With probability λ_U , they receive a job offer which they can choose to accept or reject. The starting piece-rate is determined by (7). If no offer arrives or it is rejected, the worker continues to age $t + 1$ with the same level of human capital h .

Finally, the value function for firm θ paired with worker (a, h, t) is:

$$\begin{aligned}
J_t(w, a, h, \theta) = & ph(1 - w) + \underbrace{\beta\lambda_E(1 - \delta) \int_{\Gamma_R^t(w, a, h, \theta)} J_{t+1}(w'_R(\theta'), a, h', \theta) dF(\theta')}_{\text{worker stays and renegotiates piece-rate}} \\
& + \underbrace{\beta(1 - \delta) \left(1 - \lambda_E \int_{\Gamma_R^t(w, a, h, \theta)} dF(\theta)\right) J_{t+1}(w, a, h', \theta)}_{\text{no outside offer arrives, or it is discarded}}
\end{aligned} \tag{10}$$

The firm's profit is what it produces, ph , minus what it pays its worker, phw , where $w \leq 1$. If the worker leaves, whether to unemployment or to a poaching firm, the firm's continuation value is zero. The continuation value will be updated if the worker receives a job offer which is used to renegotiate the piece-rate. For worker (w, a, h, t) employed at θ , this set of firms is denoted by:

$$\Gamma_R^t(w, a, h, \theta) = \{\theta' | M_{t+1}(a, h', \theta) > M_{t+1}(a, h', \theta'), V_{t+1}(w'_2, a, h', \theta) > V_{t+1}(w, a, h', \theta) \geq M_{t+1}(a, h', \theta')\}$$

In other words, the worker renegotiates his or her wage at firm θ if firm θ values the worker more than firm θ' , but θ can afford to match the maximum value that θ' can offer. If no outside offer arrives, or it is discarded, the match continues with the same piece-rate and human capital is updated according to firm θ 's learning environment.

3.4 Joint Match Value

The joint value of the match, $M_t(a, h, \theta)$, is defined as the sum of the worker's value function and the firm's value function: $M_t(a, h, \theta) = V_t(w, a, h, \theta) + J_t(w, a, h, \theta)$. Using equations (8) and (10) and the surplus splitting rules, (5), (6), and (7), we arrive at the following recursive expression for the joint value:

$$\begin{aligned}
M_t(a, h, \theta) = & ph + \underbrace{\beta\delta U_{t+1}(a, h)}_{\text{unemployment}} + \underbrace{\beta(1 - \delta) \left(1 - \lambda_E \int_{\Gamma_M^t(a, h, \theta)} dF(\theta)\right) M_{t+1}(a, h', \theta)}_{\text{worker stays; wage may be rebargained}} \\
& + \underbrace{\beta(1 - \delta)\lambda_E \int_{\Gamma_M^t(a, h, \theta)} [M_{t+1}(a, h', \theta) + \sigma(M_{t+1}(a, h', \theta') - M_{t+1}(a, h', \theta))] dF(\theta')}_{\text{worker moves to firm with higher match value}}
\end{aligned} \tag{11}$$

Aside from the impact of human capital accumulation, the joint match value only changes if the

worker transitions to unemployment or to another firm, in the set $\Gamma_M^t(a, h, \theta)$, defined as:

$$\Gamma_M^t(a, h, \theta) = \{\theta' | M_{t+1}(a, h', \theta') > M_{t+1}(a, h', \theta)\}$$

This is the set of firms who value the worker more than firm θ . In this case, the updated joint value reflects the value as delivered by the wage setting rule in equation (5). If the worker remains at firm θ , the joint match value is only updated to reflect human capital accumulation, even if the piece-rate changes. This is because changes in the piece-rate are only reflective of a transfer of value from firm to worker. As a consequence, this value function does not depend on the piece-rate.

This function characterizes all job acceptance decisions in the economy and thus is sufficient for determining the steady-state allocation of workers to firms. Once this equation is solved, piece-rates can be backed out from the wage setting equations (5), (6), and (7).

3.5 Equilibrium

A **stationary equilibrium** consists of:

- (a) a match value function $M_t(a, h, \theta)$, an employed worker value function $V_t(w, a, h, \theta)$, an unemployed worker value function $U_t(a, h)$, and a firm value function $J_t(w, a, h, \theta)$,
- (b) a piece-rate function which depends on (w, a, h, t) and the types of the incumbent and poaching firms, (θ, θ') ,
- (c) steady state distributions of workers over the state variables (w, a, h, θ, t)

such that:

- (i) the value functions are the solutions to the Bellman equations,
- (ii) the piece-rates evolve according to the wage setting rules,
- (iii) the distributions evolve according to the wage setting rules and the transitions determined by the joint match value function,
- (iv) and inflows of worker $(w, a, h, \theta, t) =$ outflows of worker (w, a, h, θ, t)

3.6 Properties of the Model

Sources of earnings growth. Earnings in the model are phw . The dynamics of each component play into the growth of overall earnings.

The firm productivity component, p will change whenever the worker makes a job-to-job transition. Thus, the model accounts for the notion of “high” and “low” paying firms, or the job ladder in the traditional sense. In conjunction with each job-to-job transition, as well as on-the-job, the piece-rate w grows as workers obtain outside offers. Increases in the piece-rate reflect increases

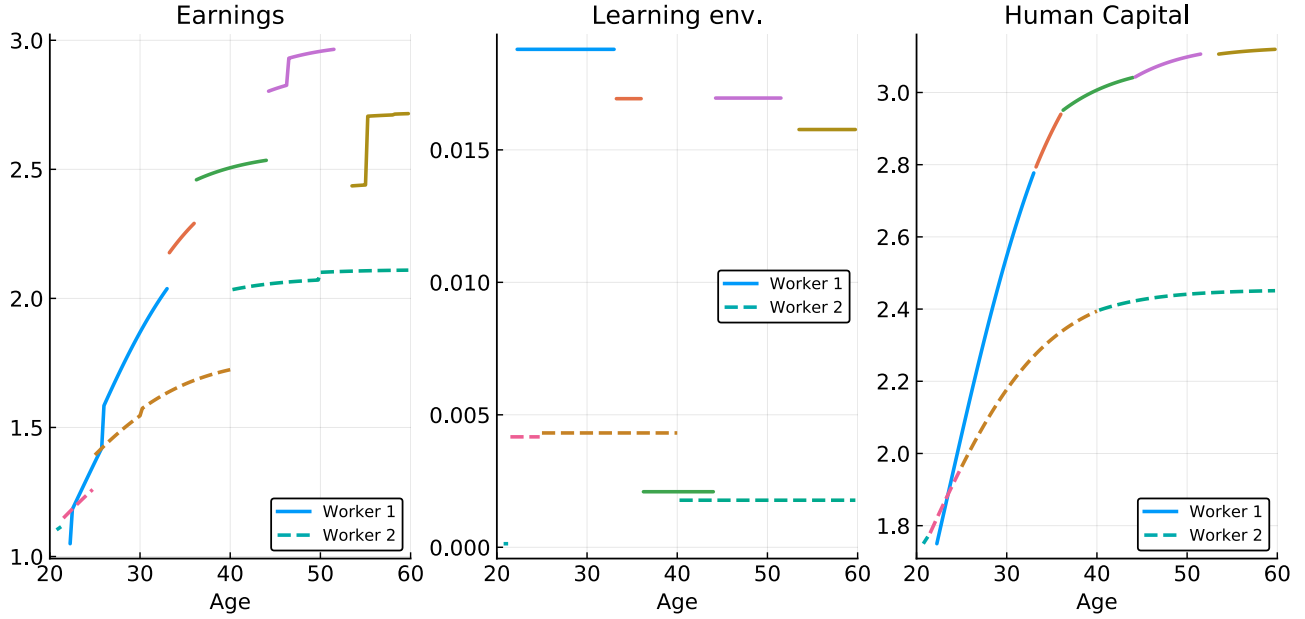


Figure 4: Example paths for workers with same learning ability.

The left panel shows earnings paths for two workers in the solid and dashed lines. Both have the same learning ability, but receive a different series of shocks over their lifetimes. Each different color represents a spell in a different firm. Gaps (can be seen best in the human capital paths) represent unemployment spells. The middle panel shows the corresponding learning environments of the firms the workers match to. The right panel shows each worker's human capital profile.

in search capital as workers accumulate and improve on the outside options they use to renegotiate. This source of growth introduces an indirect effect of firm tenure on earnings growth because workers with longer tenure tend to have received better outside offers throughout the employment spell.

The bargaining setup induces backloaded w contracts. As long as the firm has some bargaining power, it is optimal for it to backload wages and pay the worker well below their marginal product initially. This is because the firm anticipates that the worker will get outside offers in the future and can raise wages to retain them only when they have a credible threat to leave. As a consequence, matches with higher joint values will exhibit steeper earnings profiles, because these firms are better able to compete with others. In a model without learning environment heterogeneity, the slope of a firm's earnings profile would be dictated only by p . But here, much of the future value of the match also depends on the firm's learning environment q through its impact on human capital accumulation. As a result, for a given level of p , workers are willing to accept lower starting piece-rates in order to work at a firm with a better q .

Finally, increases in human capital, h , directly feed into earnings.²³ Human capital growth de-

²³An alternative modeling choice would have been to allow for human capital to impact earnings only through increases in the piece-rate. In this setting, earnings would not directly depend on human capital, but increases in the piece-rate would also reflect human capital accumulation since the last outside offer.

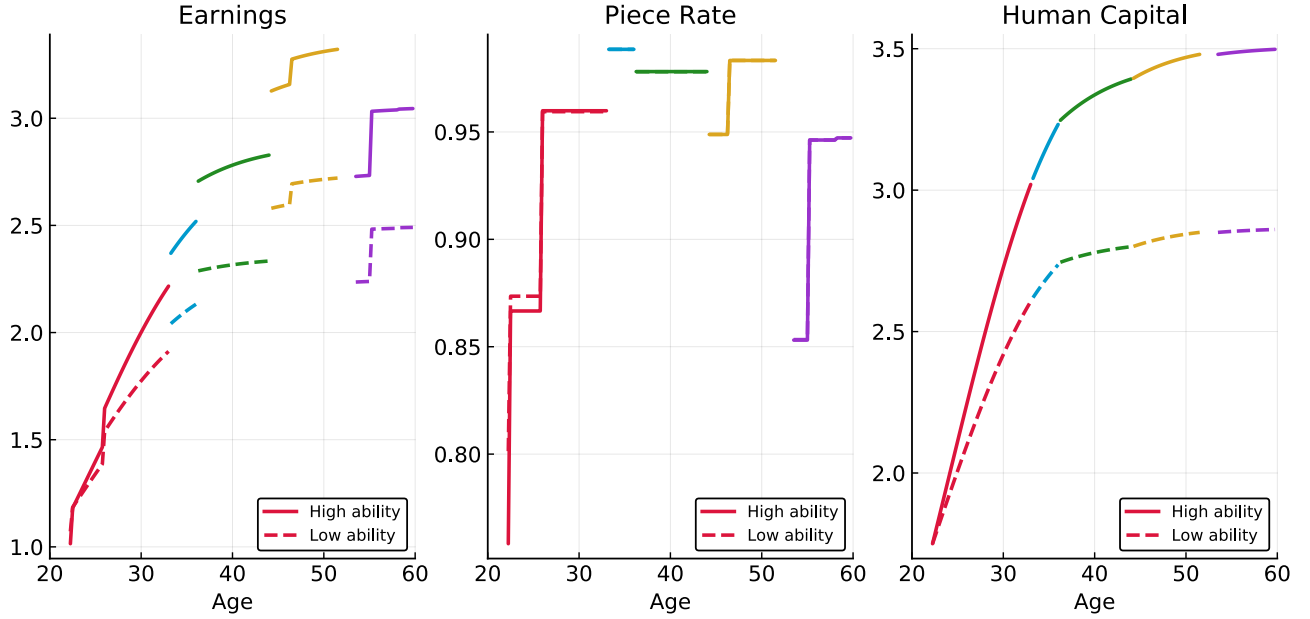


Figure 5: Example paths for workers with different learning abilities, but with the same shocks. The left panel shows earnings paths for two workers. The worker in the solid line has a high a , whereas the worker in the dashed line has a low a . The workers receive the same sets of shocks, and thus meet the same firms. Each different color represents a spell in a different firm. Gaps (can be seen best in the human capital paths) represent unemployment spells. The middle panel shows the corresponding piece-rates. The right panel shows each worker's human capital profile.

depends on the worker's age and learning ability and the firm's learning environment.

To understand the effects of age and learning environment on human capital and earnings, see Figure 4. This figure shows the earnings profiles in the model of two workers with the same learning ability, but who receive different shocks (job offers and separation shocks). Each different-colored line segment represents a spell at a different firm. The middle and right panels also show the learning environment of each match and the corresponding worker's human capital profile. Because Worker 1 consistently meets firms with better learning environments at young ages, his earnings profile is steeper than Worker 2's. In addition, human capital growth flattens for both workers at older ages, regardless of the firms they match with. The outcomes depicted here are an example of the novel mechanism that I explore in this paper: the labor market outcomes of *ex-ante* identical workers differ solely because of luck in which kinds of firms they match with. The main driver is differences in the firms' learning environments. This is one channel that will impact the life-cycle variance profile of earnings.

Figure 5 highlights the impacts of learning ability and disentangles the sources of earnings growth at different ages. In this figure, there are two agents with different abilities but they meet the same firms over their lifetime. Late in the life cycle, earnings changes during a spell are solely driven by changes in the piece-rate. For example, the changes in the piece-rate that the workers get in the last firm is solely driven by an increase in the piece-rate, but not human capital. In contrast, at

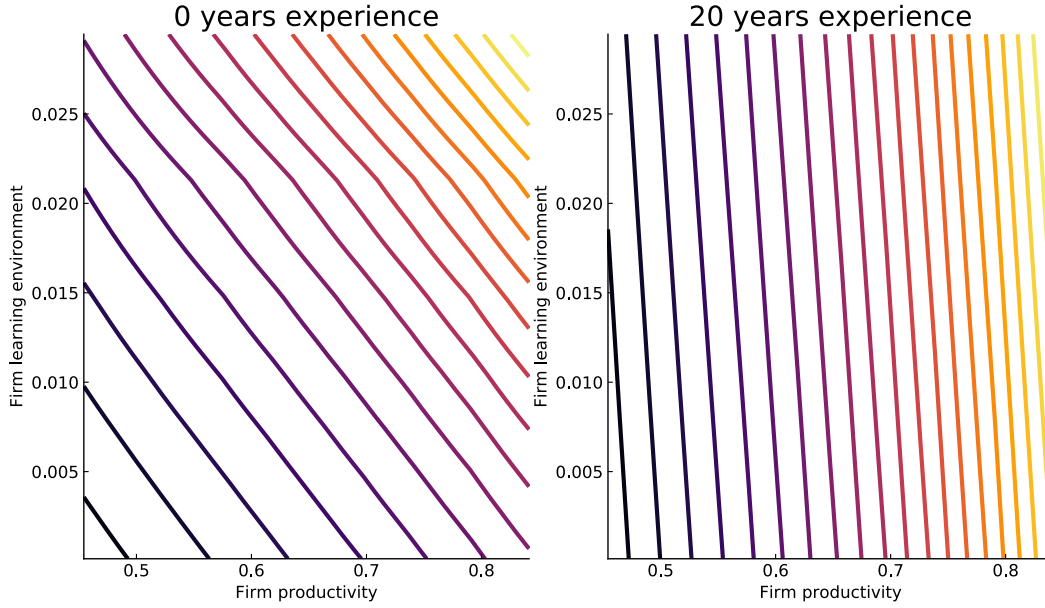


Figure 6: (p, q) indifference curves

Traces out indifference curves in (p, q) space where p corresponds to firm productivity and q to firm learning environment. These are generated for the baseline calibration outlined in Section 4.

The contours are defined based on the joint match value as a function of (p, q) , which is increasing in both arguments. Worker learning ability and human capital are fixed at the same arbitrary values in the two panels.

younger ages, both the piece-rate and human capital play a role. This insight is going to guide the identification strategy which will aim to separate the contributions of search capital and human capital within firms. Additionally, the earnings of the high ability worker are always growing faster than those of the low ability worker, even though they are always employed by the same firm. This idea will also be used in the identification to quantify the extent of worker versus firm effects on human capital growth.

Job search. The decision to accept a job offer in the model is solely dependent on the comparison between the joint value of the current job (or unemployment) versus the new job. An important determinant of the present value of the match is the growth in human capital that the worker expects to receive over the match. Because human capital growth is highly age dependent, the model creates trade-offs across firms that vary over a worker's life cycle.

Figure 6 illustrates this. Each contour traces out an indifference curve over firm characteristics productivity and learning environment. In each panel, the learning ability and human capital of the worker is held constant; the left panel is for a new labor market entrant and the right panel is for a worker with 20 years of experience in the labor market. The indifference curves earlier in life are flatter than those later on. When young, workers highly value a firm's learning environment because the ability to accumulate human capital diminishes over the life cycle. It is important to match to a high q firm early on in order to receive permanently higher earnings throughout life.

When workers are much older, however, the learning environment of the firm becomes irrelevant. Workers only weigh job acceptance decisions by p , generating the nearly vertical indifference curves in the right panel. These changes in workers' job acceptance strategies are crucial for the model's life-cycle dynamics and are the channel through which policies impact the allocation of workers to firms.

4 Identification

Identifying the parameters that determine the outcomes of this model is challenging. An individual's earnings growth contains both worker and firm components. The firm-specific components come from the firm's productivity and learning environment, governed by the joint distribution $F(\theta)$. The worker-specific component comes from the distribution of learning ability, $G(a)$.

Because the relevance of the different sources of earnings growth changes over the life cycle, my identification strategy exploits the differences in earnings patterns over the life cycle. I use an indirect inference method in which I match a set of reduced-form moments in both the model and the data. Using insights from the model, I show why these particular moments are separately informative about the distributions of worker and firm heterogeneity.

I construct two sets of moments. The first aims to separate firm productivity and learning environment. It relies on comparing the earnings growth patterns of different-aged workers within the same establishment (this contains three sub-steps).²⁴ The second group of moments adds information that helps inform the relative amounts of worker and firm heterogeneity.

I discuss each of these in detail below, and then describe how to identify the more standard features of the model.

4.1 Residual earnings growth of young workers by establishment

First step: establishment-specific returns to search capital. In the first step, I construct a measure of the returns to search capital by establishment. This comes down to estimating establishment-specific earnings profiles with respect to tenure for older workers who are hired out of an unemployment spell. The logic is that this is a group of workers who start off with the same outside option (unemployment) and who can no longer accumulate human capital. As a result, any earnings growth they experience should come only from accumulation of search capital. Through the lens of the model, I am isolating the growth of w in earnings, phw . Because these are estimated on job-stayers p is not growing, and with the assumption on human capital, h is not growing.

The assumption that little to no human capital is accumulated late in life has been used by Heck-

²⁴One could think of proxying human capital with labor market experience and search capital with job tenure and constructing firm earnings profiles as a function of experience and tenure. However, it is difficult to separate the two effects because whenever tenure increases, experience increases by the same amount.

man, Lochner and Taber (1998) and later, Huggett, Ventura and Yaron (2011) and Lagakos et al. (2018). The reasoning comes from declines in productivity or the proximity to retirement for older workers. Using properties of the earnings of these workers has enabled these authors to estimate inputs for structural models.

The restriction that these workers must be in their first job after an unemployment spell also relies on economic theory. When workers lose their jobs in a sequential auction model like this one, their bargaining position is wiped out. All workers who find new jobs start from the same negotiation benchmark, the value of unemployment, and must get raises by obtaining outside offers. Using workers coming out of unemployment spell ensures that all of them start from the same benchmark and that workers at the same establishment have in expectation received similar outside offers conditional on tenure. Combined with the older workers restriction, this ensures that the earnings growth of this group of workers is informative about the firm-specific returns to search capital.

In order to implement this, I restrict older workers in the data to be ages 50 and up. I locate UE transitions by taking workers who are employed in a given month, but were receiving unemployment benefits in the previous month, or who were not registered in the social security system for between 21 and 365 days.

Finally, to construct the establishment-specific returns to search capital, I run the following random coefficients model:

$$\Delta \log \text{earnings}_{ijt} = \alpha_j + \beta_j^1 \text{tenure}_{it} + \beta_2 \text{tenure}_{it}^2 + \varepsilon_{ijt} \quad (12)$$

Importantly, both the intercept and first-order coefficient on tenure differ across establishments, which allows for rich variation in the profiles. Moreover, rather than running OLS separately by establishment, I use a random coefficients model. Intuitively, these models construct earnings profiles for specific establishments by using information about the profiles of other establishments, a concept known as partial pooling. This reduces the noise involved with having small or relatively homogeneous workers employed in some establishments: for establishments like this, the estimates will shift towards the overall mean profile.²⁵ The statistical model assumes that (α^j, β_1^j) are distributed bivariate normal across the population of establishments and estimates the mean and covariance matrix of that distribution. Using the predicted values of the coefficients, I can construct predicted values for the amount of earnings growth coming from search capital accumulation at each establishment and tenure horizon. These will be used in the next step.

Second step: establishment-specific returns to human capital. In the second step, I focus on

²⁵Nevertheless, I do apply some weak establishment size restrictions on the establishments I include in this regression. I include only establishments who have at least 5 worker spells for whom I can compute yearly wage growth, and for which one of these spells lasts at least 5 years. The resulting pattern of earnings profiles looks similar to establishment-by-establishment OLS where I use a stricter sample selection with establishments who have at least 5 workers who stay longer than 5 years.

younger workers in order to construct a set of moments that is informative about the returns to human capital. The main idea is to isolate growth in h in phw . As before, I will be using job stayers, so p is not growing. To separate h from w , I use the establishment's returns from search capital estimated in the first step. The residual is informative about human capital growth patterns in the establishment.

To ensure that I focus on the part of the life cycle with the fastest human capital growth, the first several years in the labor market, I make restrictions on the ages of the workers and the job spells I include. I want to include a worker's first "real" job in the labor market and use this starting point to construct a measure of experience.²⁶ I restrict each first job to be the first time the worker appears in the data set, is in a reasonable age range depending on the education of the worker,²⁷ and lasts at least 90 days.

Using these job spells, I first compute annual earnings growth at each year of tenure on the job, $\Delta \log \text{earnings}_{ijt}$. Then, using the predicted values, $(\hat{\alpha}_j, \hat{\beta}_j^1)$, obtained in the first step, I can predict how much earnings growth the worker should be getting from search capital accumulation based on the establishment that employs the worker. I construct the residual part of earnings growth as $\widehat{\Delta \log \text{earnings}_{ijt}} = \Delta \log \text{earnings}_{ijt} - \alpha_j - \beta_j^1 \text{tenure}_{it} - \beta_2 \text{tenure}_{it}^2$. Finally, like in step 1, I construct establishment-specific human capital returns profiles by estimating another random coefficients model on the residuals:

$$\widehat{\Delta \log \text{earnings}_{ijt}} = \gamma_j + \delta_j^1 \text{experience}_{it} + \delta_2 \text{experience}_{it}^2 + \varepsilon_{ijt} \quad (13)$$

The moments that I target are based on the cumulative earnings growth profiles constructed from (13). Using the predicted values $(\hat{\gamma}_j, \hat{\delta}_j^1, \hat{\delta}_2)$, I compute predicted earnings growth from human capital at experience horizons 1 to 10 for each establishment. Cumulating these gives a predicted cumulative earnings growth at each establishment for each horizon. I target the 10th percentile, 90th percentile, and mean of these distributions at each horizon, obtaining 30 moments.

Because these moments pick up differences in human capital growth patterns across establishments, they are informative about the distribution of learning environments, q . The shape of these profiles is also informative about γ and α , which control the shape of the depreciation function. γ determines how steeply human capital declines and α controls the age around which the decline is steepest. Their values are restricted to ones such that human capital growth is zero past age 50, which is necessary to match the assumptions I made with the data.

Third step: correlation between returns to human capital and search capital. I also use the

²⁶I am careful here about using experience rather than age because in the model, human capital only starts growing upon labor market entry which is interpreted as age 20 for everyone. In the data, this not necessarily the case, so I want to ensure that I am capturing for everyone the right place in the life cycle where human capital (or job experience) starts to grow.

²⁷Between ages 17 and 21 for workers with less than a high school degree; 19 and 23 for workers with a high school degree or vocational degree; 21 and 27 for workers with both a high school degree and vocational degree; 24 to 30 for workers with a college degree; 19 to 23 for workers with a missing education level.

results from step 1 and step 2 to inform how correlated productivity and learning environment should be in the joint distribution $F(\theta)$. I consolidate the results from each step to give me just one measure of each per establishment. To do this, I construct for each establishment the predicted earnings growth that comes from (12) and (13) at tenure and experience levels 1 through 10. I take the average over these 10 to obtain one measure of search capital returns and one measure of human capital returns per establishment. I then target the establishment-level correlation coefficient.

4.2 AKM moments

The moments described in Section 4.1 do not account for differences in worker ability. For instance, if high ability workers sort into high learning environment firms, this will be picked up in these moments. Next, I add additional moments designed to separate the effects of workers versus firms on earnings growth.

For this, I use the AKM two-way fixed effects model from Section 2. I run the following regression in both the data and the model:

$$\Delta \log w_{ijt} = \alpha_i + \psi_j + \gamma_t + \beta_1 \text{age}_{it} + \beta_2 \text{age}_{it}^2 + \beta_3 \text{tenure}_{it} + \beta_4 \text{tenure}_{it}^2 + \varepsilon_{ijt} \quad (14)$$

In order to ensure that the moments from the data and the model are comparable, I need to address the limited mobility bias present in AKM. This bias arises because of a small sample problem, in the sense that each worker is only employed by few firms, and each firm may only employ a small number of workers. This means that the estimated fixed effects are noisy estimates, biasing their variances upward. In addition, the covariance between the fixed effects is biased downward. Intuitively, if a worker fixed effect is overestimated, the firm fixed effect will be underestimated, and vice-versa.

This bias exists in both the data and the model, but to different degrees. The first difference comes from the length of worker histories. The model-simulated data is a balanced panel with exactly 40 years of data per worker. The real data is an unbalanced panel. It only contains on average 14 years of data per worker, with each worker employed in 3 establishments on average. The differences in the lengths of worker histories impacts the precision of the estimates of the worker fixed effects – the more firms I observe a worker in, the better the estimate. To put the model and the data on equal grounding, I randomly truncate the worker histories in the model-simulated data so that I only use on average 14 years of data per worker and 3 establishments per worker when estimating (14).

The establishment sizes also affect the magnitude of the bias. The smaller the establishments, the larger the bias. In the model, workers are matched to firms one-to-one, so to mimic multi-worker firms, I group similar firms together. I bin firms based on their quantiles in the $p \times y$ distribution.

I choose the number of quantiles small enough so that I have on average 9 workers per firm like in the real data set.

I target the relative variance of the worker-fixed effect to the establishment fixed-effect, $\text{var}(\alpha_i)/\text{var}(\psi_j)$, and their correlation, $\text{corr}(\alpha_i, \psi_j)$. The variances inform the dispersion in the distributions of worker learning ability and firm learning environment. The correlation informs the degree of sorting on the (a, q) dimension, which is controlled by the levels in the support of the ability and learning environment distributions, as well as the levels in the depreciation function.

4.3 Firm productivity and bargaining power

Unlike the distribution of learning ability, q , heterogeneity in firm productivity, p , is a more standard feature of my model. It informs the dispersion of firm wage premia, and along with the bargaining power σ , how backloaded wages are due to labor market competition forces. Like Jarosch (2015) and Bagger et al. (2014), I will use moments about between- and within-job earnings growth to discipline these. But because early in life these moments are also influenced by human capital accumulation, I will focus on moments from workers above age 50. These moments give me cleaner measures of the forces of the model that are unrelated to human capital.

For between-job growth, I target the mean earnings growth upon a job-to-job transition.²⁸ For within-job growth, I use the average annual earnings change for job-stayers, the average growth from start to end of a job spell, and the ratio of starting wages to average wages.

4.4 Transition and replacement rates

I use standard labor market flow moments to identify the arrival rates of job offers on and off the job, λ_E and λ_U , respectively. The job-to-job transition rate identifies λ_E and the job-finding rate identifies λ_U . Because all separations are exogenous, δ can be taken straight from the data. b , the level of unemployment benefits is chosen to match the net replacement rate in Germany as reported by the OECD.²⁹ In the model, I compare the average earnings in unemployment with the average earnings in employment. The model's period is quarterly, and workers participate in the labor market for 40 years (corresponding to ages 20 through 60 in the data), implying $T = 160$. I follow Herkenhoff et al. (2018) by setting β to a 15% annual discount rate to avoid the problem of negative wages.

²⁸Because at later ages, the model is not capable of generating job-to-job transitions with wage cuts, I target the mean wage growth of workers aged 50+, conditional on getting a wage increase.

²⁹See the table [here](#).

4.5 Parameterization

I use Pareto distributions to parameterize a and q .³⁰ These distributions have shape parameters χ_a and χ_q , respectively. The distribution of p is parameterized as a Beta distribution with parameters χ_p^1 and χ_p^2 , with the support shifted by χ_p^3 . To further characterize the joint distribution of firms, I introduce a correlation between firm attributes (p, q) , called ρ . All together, draws from $F(\theta)$ are correlated draws from the marginal distributions of p and q , the Beta and Pareto distributions defined above.³¹ ρ is identified by the correlation of the two firm attributes obtained from each step of the procedure outlined in step 3 of Section 4.1.

Because the moments that identify the parameters are more complicated than just simple functions of the data, the calibration is reminiscent of the indirect inference procedure of Gourieroux, Monfort and Renault (1993). This is a simulated method of moments procedure where the moments can be parameters from reduced form econometric models. These reduced form models, called auxiliary models, can be misspecified, but should be informative about the structural parameters of the model. The structural parameters are chosen to minimize the distance between the auxiliary models estimated on real data and the same ones estimated on simulated data. In this case, the auxiliary models are the cumulative residual earnings growth moments described Section 4.1, the relative variances and the correlation coefficient from the AKM model in growth rates in Section 4.2, as well as the simpler moments described in Sections 4.3 and 4.4. On top of this, I also target the increase in the variance of earnings (from its minimum point to age 60) because I decompose this in the results section as a starting point for my main counterfactual.

5 Parameter estimates and model fit

5.1 Targeted moments

Table 1 presents a summary of the parameter values and targets. The model fits the data well on most dimensions.

Figure 7 compares the residual earnings growth moments, described in Section 4.1, in the model and the data. The bold lines in the middle show the mean of the cumulative residual earnings growth distribution across firms, and the two dashed lines show the 10th and 90th percentiles. The model fit is excellent, although it implies a little bit too much growth coming from human capital at the mean firm and at the best firms for long experience horizons.

These moments should be interpreted as being informative about differences in returns to human capital accumulation across firms. The amount of growth and heterogeneity in growth rates is

³⁰Both are shifted so that their support starts at 0 rather than 1.

³¹In practice, I take draws from a bivariate standard normal with correlation ρ , map the draws back to quantiles of the standard normal, and then map these quantiles to the corresponding points in the marginal distributions of p and q . To discretize this for the model solution, I need to assign probabilities to each point on a 2-D grid over these variables. I do this a similar way, making use of approximations of the cdf of the bivariate normal.

Parameter	Value	Target	Data	Model
χ_q	79	$\frac{\text{var}(\alpha_i)}{\text{var}(\psi_j)}$	1.09	1.09
χ_a	77	resid. growth young workers	see Figure 7	see Figure 7
γ	0.04	increase life cycle variance	0.14	0.13
α	6 years	$\text{corr}(\alpha_i, \psi_j)$	-0.49	-0.37
ν	0.87			
χ_p^1	5	between job growth	0.154	0.119
χ_p^2	10	within job growth	0.005	0.003
χ_p^3	0.35	growth over entire spell	0.0	0.013
σ	0.66	starting to avg. wage ratio	0.795	0.848
ρ	-0.02	correlation (p, q) in $F(\theta)$	-0.1202	-0.1276
δ	0.0186	EU rate	0.0186	0.0186
λ_U	0.225	UE rate	0.2025	0.1960
λ_E	0.12	EE rate	0.0288	0.0265
b	0.5	avg U earnings/avg E earnings	0.61	0.58

Table 1: Summary of calibration

The first block of the table corresponds to the parameters that identify the moments informative about human capital accumulation, as described in Sections 4.1 and 4.2. The second block corresponds to the moments that inform the distribution of firm productivity and bargaining power, as described in Section 4.3. Note that the all of the identification within the first two blocks is *joint*, i.e., the parameters in the first two columns do not necessarily map to the moment in the corresponding row. The last block corresponds to the moments that identify the transition rates and replacement rates, described in Section 4.4.

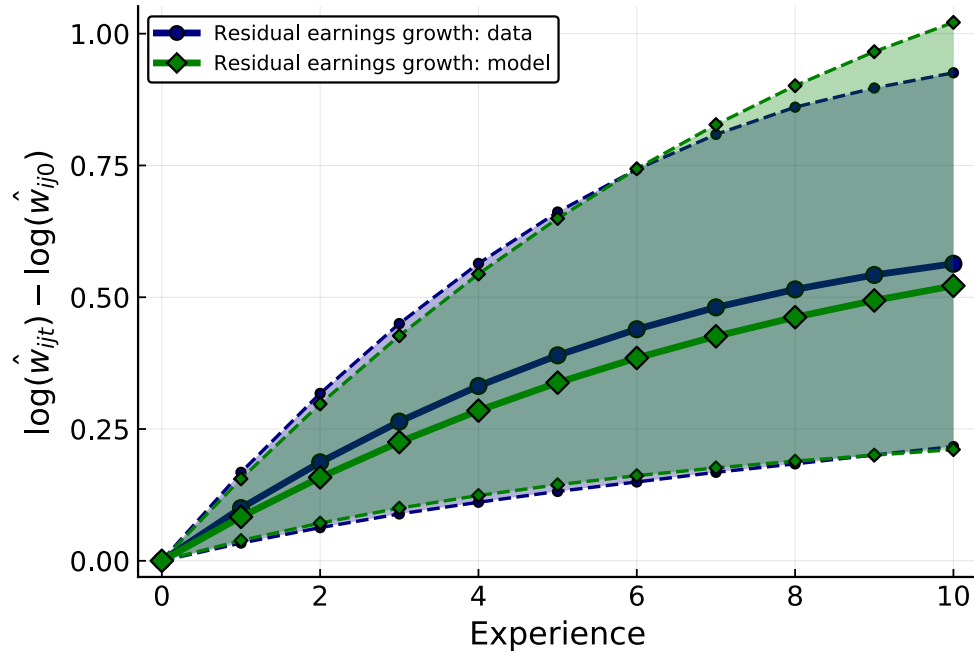


Figure 7: Residual earnings growth moments: model vs. data.

This figure depicts the distribution of earnings growth profiles across firms, when earnings growth due to search capital accumulation is removed, as in the process outlined in Section 4.1.

Each marker represents one moment targeted in the calibration procedure.

striking and is crucial for the quantitative results. One feature is that the mean shape of this profile looks similar to the overall mean earnings profile which takes into account job-to-job transitions. Thus in general, I find that there is a lot of on-the-job growth to be had early in life, which attributes less overall earnings growth to job-to-job transitions.³²

These moments still pick up differences in worker composition within firms – adding the AKM moments to the estimation separates these and informs how much of the heterogeneity is truly coming from firms. Because the variances in the data are quite close to each other (the ratio of the variance of the worker to the firm effect is 1.09), I will find only slightly more heterogeneity in a , the worker component, than in q , the firm component. This will also be an important driver of the results because there will be a large part of human capital heterogeneity coming from firms.

The values of γ and α in the depreciation function imply a very gradual decline in human capital accumulation: see Figure 3. The levels of the inputs to the human capital production function, primarily controlled by ν in the numerator of the depreciation function, impact the measured degree of sorting – the correlation of the AKM fixed effects. However, the large negative value in the model, -0.37, is almost entirely determined by the degree of bias introduced into the model. In contrast, the model’s theoretical measure of sorting, the correlation between a and q is zero.

The variance of the distribution of firm productivity is similar to what Jarosch (2015) estimates.³³ The estimate of the worker bargaining power implies that two-thirds of the joint value goes to the worker and generates less earnings growth coming through the search capital channel compared with other papers. I attribute this result to the inclusion of human capital growth. Like in Bagger et al. (2014), the model does not need to attribute so much on-the-job growth to piece-rate increases when human capital growth is allowed.

Finally, the aggregate labor market flow rates match well. As usual, the offer arrival rate is higher in unemployment. This will imply some loss of the option value of search when workers accept employment which will mean that workers sometimes reject job offers.

5.2 Untargeted moments

For further validation, I examine the model’s fit to a set of untargeted moments. These are depicted in Figure 8.

Even though I only target the aggregate EE and UE rates, the model can mostly account for their entire life-cycle profiles. In the data, both decline over the life cycle. The model matches the decline in the EE rate well. For the UE rate, I get a decline for the first 30 years and then an increase. The UE rate in the model in the first 10 years is too low: workers in the model are too selective with

³²In contrast, Bagger et al. (2014) find that most of the earnings growth early on is due to “job shopping.”

³³It is going to generate less ladder climbing than in Bagger et al. (2014). This is because the model does not take into account permanent differences in the *level* of earnings across workers. The extent to which high-wage (in level) workers climb to high-wage (in level) firms will not be captured here. Jarosch (2015)’s model also does not account for this, so it is reassuring that we both find similar productivity distributions.

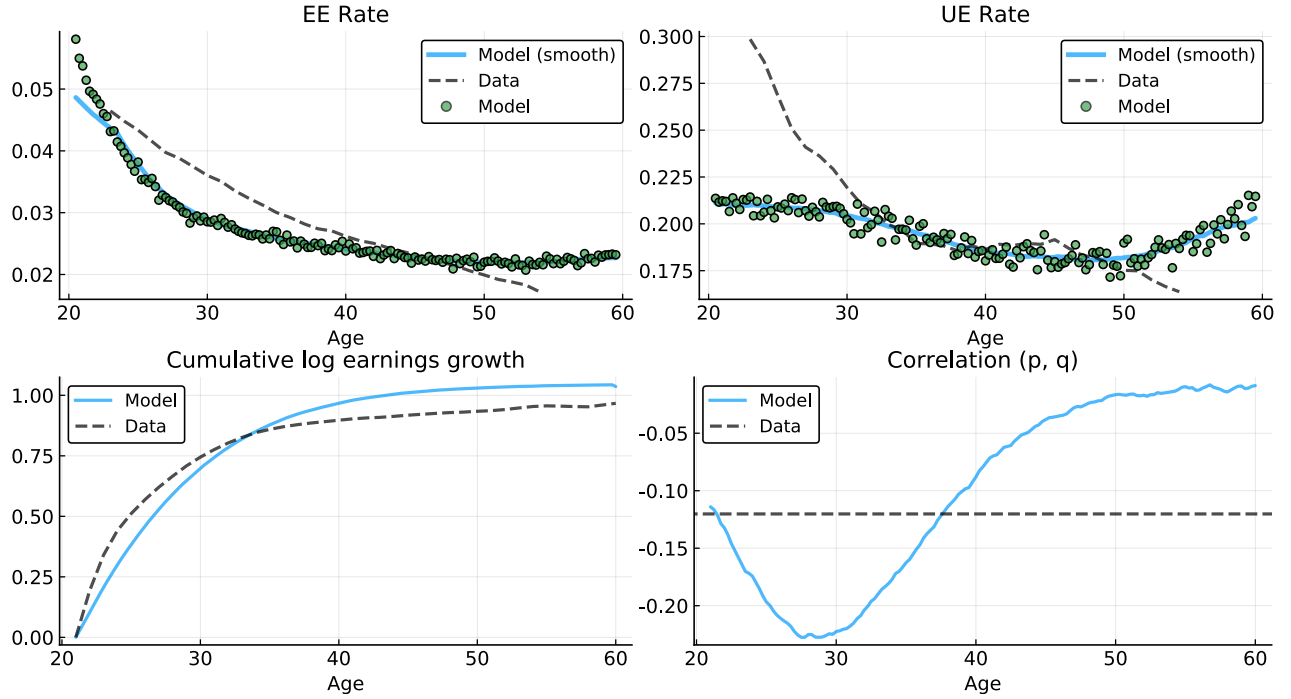


Figure 8: Untargeted moments.

The top left panel compares the job-to-job transition rate by age in the model and the data. In the data, I define a job-to-job transition as two consecutive employment spells with less than 21 days in between them. Because the model is quarterly, I also plot “Model (smooth)”, which is a 3-year moving average. The top right panel is the unemployment-to-employment rate. The lower left plots cumulative log earnings growth, which at a given age is defined as the difference in mean log earnings from the log value at age 20. The lower right shows the correlation of productivity and learning environment among the accepted jobs at each age. The “data” line corresponds to the singular correlation measure derived from step 3 in Section 4.1.

which jobs they accept early on. The increase at the end comes from workers becoming much less selective at older ages.

I do not target the overall earnings profile, but the model can match this well. This is because I already match the shape of the residual growth moments in Figure 7 from the parameters of the human capital depreciation function. Finally, I compare the life-cycle profile of the correlation in (p, q) . The overall mean of this is targeted (the dashed horizontal line), but the model implies that the negative correlation found in the data is driven by young workers. These are precisely the young workers who face the relevant trade-off between productivity and learning environment: workers who go to firms with a low learning environment early on must be compensated by a high productivity, generating the negative correlation.

6 Quantitative Results: Life-Cycle Earnings Profiles

In this section, I use the model to understand the patterns in the life-cycle earnings profile. To quantify the importance of the firm learning environment channel, I study the model with and without heterogeneity in worker learning ability. By removing *ex-ante* differences in workers, I create an environment in which the only source of heterogeneity in the labor market outcomes of workers comes from the series of firms they happen to match with. Put differently, search frictions not only affect how rents are split, but also translate to persistent worker differences. This is the novel interaction put forth by this paper.³⁴

6.1 Life-cycle mean profile

Where does the growth in life-cycle earnings come from? In this section, I use the model to explore the sources of life-cycle earnings growth. Since log earnings in the model are the sum of human capital, the productivity of the firm, and the piece-rate, I can decompose the earnings profile into these three components.

The left panel of Figure 9 shows the earnings profile in the data, as well as the model counterpart and its three components. Each series is normalized to zero at age 20, so that the interpretation of the y -axis is the log growth in earnings since age 20. Most of the increase comes from human capital: it drives about 2/3 of growth, whereas the productivity and piece-rate equally drive the remaining 1/3.

Bagger et al. (2014) perform almost the same decomposition in a model with differences in firm productivity, idiosyncratic shocks to match output, and deterministic human capital growth that

³⁴I have also done the opposite exercise, in which I turn off differences in firm learning environments but keep the *ex-ante* differences across workers. However, I argue that this counterfactual is less relevant because it introduces different job search behavior on the part of workers. Workers' job search strategies change because these depend on the distribution of q , but not a . Shutting down a , as done in this section, does not have this effect, and thus truly isolates the effect of one source of heterogeneity.

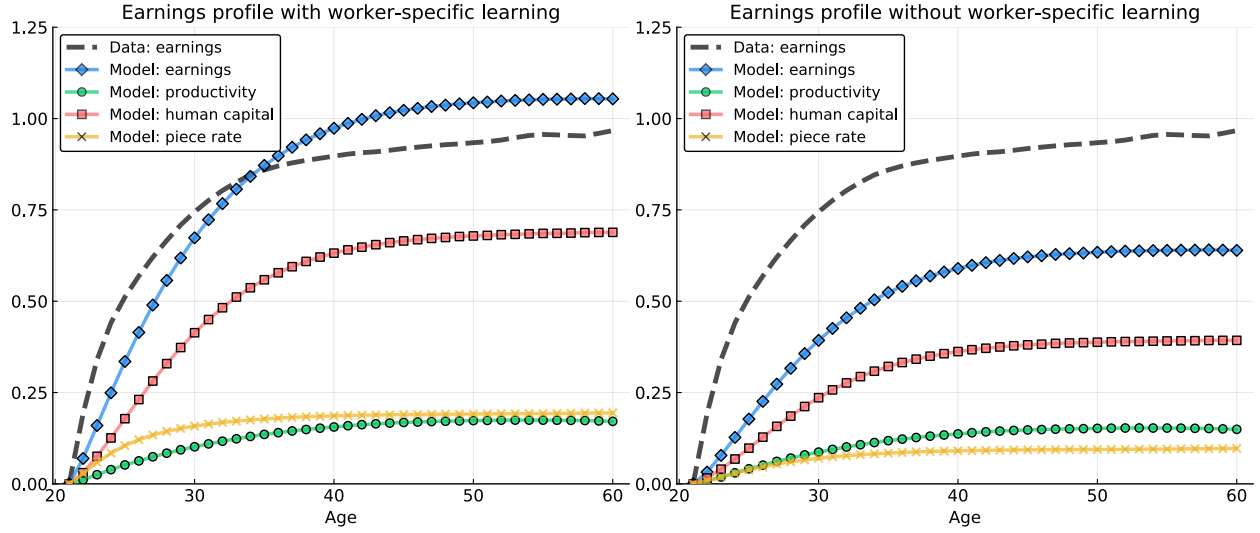


Figure 9: Life-cycle mean of log earnings and decomposition.

The left panel plots the mean of log earnings in the data and in the model where workers are heterogeneous in a . The right panel plots the corresponding means in the version of the model in which there is no worker-specific component of human capital accumulation: all growth in human capital solely comes from firm learning environments. Each series is derived from the profile of mean log earnings by age. Each is normalized to zero at the start by subtracting the value at age 20.

only depends on age. In contrast to my results, they find a larger role for growth in firm productivity early in life, as workers make a lot of transitions to climb the ladder into a good match, or “job shopping.” The differences between our results mainly come from the inclusion of a firm-specific component of human capital growth. I attribute more of the earnings differences between firms to the human capital of its workers, which was partially picked up through the firm’s learning environment. This means that is less earnings dispersion leftover to come from other sources, captured by the firm’s productivity. As a result, the workers in my model have less of a ladder to climb in productivity. Other differences may come from the data used. Bagger et al. (2014) use Danish micro data. I find in that in Germany there is a lot of on-the-job earnings growth, dampening the role of job-to-job transitions (see Figure 7). Their findings for Denmark indicate that this may not be the case there. However, I do find that the role of the productivity and piece-rate, the standard job search channels, is highest early on in life, consistent with their results. To see this, note that the share of earnings growth coming from these two sources is highest in the first few years, and then diminishes from then on as human capital keeps growing.

What is the contribution of firms? How much of a worker’s stock of human capital comes from the component they accumulate that is firm-specific? To assess this, I solve a version of the model in which there is no worker-specific component to human capital growth: all workers have learning ability a equal to zero. The earnings profiles generated by this version of the model are depicted in the right panel of Figure 9.

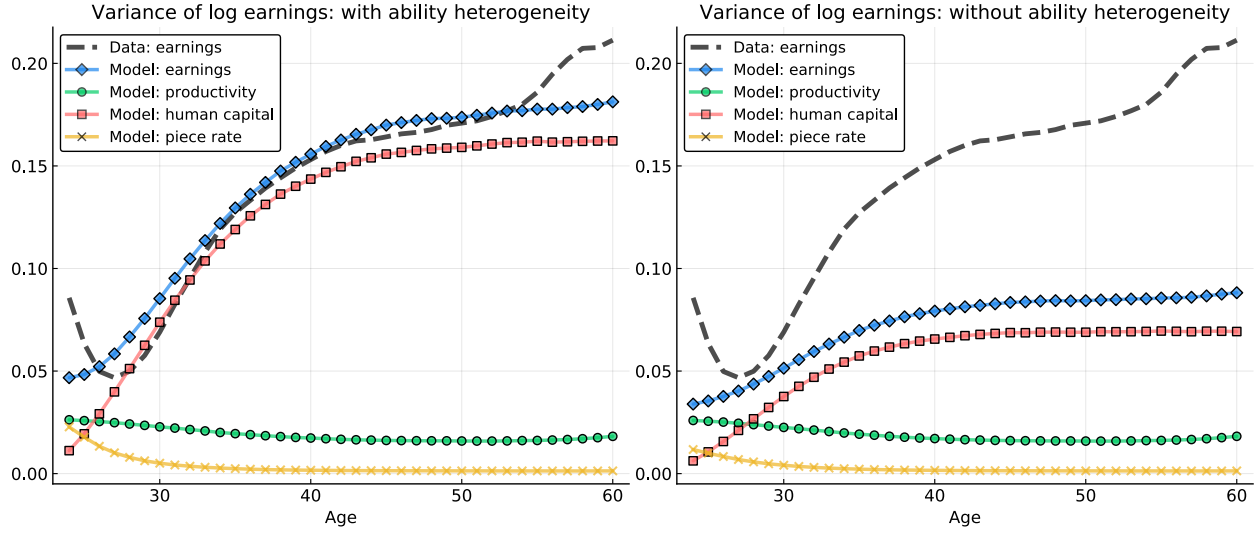


Figure 10: Life-cycle variance of log earnings and decomposition.

The left panel plots the variance of log earnings in the data and in the model where workers are heterogeneous in a . The right panel plots the corresponding variances in the version of the model without heterogeneity in a .

In this economy, there is less human capital acquired, translating to less earnings growth over the life cycle. This is mainly driven by the difference in the human capital profile. Here, the growth in average log human capital is 0.397, compared with 0.689 in the full model. This suggests that 57.6% of the human capital stock is acquired through firms.

Thus, I find that a large proportion of the human capital stock is driven by firm learning environments, despite the fact that I estimate a higher average worker learning ability than average firm learning environment.³⁵ The reason is the endogenous job choices of workers. Workers have the opportunity to visit several firms over their lifetime. Their decisions steer them towards high growth firms, which means they have the opportunity to accumulate more human capital than they would if their ability to learn was completely pre-determined when they enter the labor market.

6.2 Life-cycle variance profile

In this section, I use the model to explore the sources of the patterns of life-cycle inequality. Just as I found for the life-cycle mean earnings profile, I find here that firms and their contribution to human capital accumulation are a core contributor to the increase in life-cycle earnings variance. This result offers a new explanation for rising earnings inequality over the life cycle.

Where does the growth in life-cycle variance come from? The black dashed lines in Figure 10

³⁵Doing the opposite exercise, setting all firm learning environments to zero, gives exactly the opposite, 42.4% of acquired human capital coming from workers.

represent the variance in log earnings at each age from the data.³⁶ The blue line with the diamonds is the variance profile in the model. It matches by construction because I targeted the increase in life-cycle variance. However, despite the fact that I did not target the general shape, the model accounts for a flattening off after age 40, but not the increase after age 55 or so.

The variance of log earnings in the model can be decomposed into:

$$\begin{aligned} \text{var}(\log \text{ earnings}) &= \text{var}(\log p) + \text{var}(\log h) + \text{var}(\log w) \\ &+ 2\text{cov}(\log p, \log h) + 2\text{cov}(\log p, \log w) + 2\text{cov}(\log w, \log h) \end{aligned} \quad (15)$$

Each of the variance terms in (15) from the full model are plotted in the left panel of Figure 10 as the green, pink, and yellow lines, respectively.³⁷ The increase in the variance of human capital clearly drives the overall increase in the variance. The dispersion in human capital increases because workers accumulate human capital at different rates, both because of their different learning abilities and the learning environments of the firms they match with. The flattening out of the variance of human capital roughly coincides with the time at which human capital accumulation is no longer operative, at age 50.

Without human capital accumulation, this model would miss the increase in life-cycle earnings variance. In this scenario, only the firm productivity and piece-rate channels would be operative – the green and yellow lines, respectively. The variance of firm productivity component measures the dispersion in firm wage premia in *levels*. It declines slightly as workers move to higher paying firms over their lives. They settle into a smaller set of firms compared to where they started out. The variance in the piece-rate also declines. As workers build up outside offers and improve their bargaining positions, the distribution of piece-rates shifts towards 1, its upper bound. Together, these would imply a decrease in the variance of earnings in a model with only these two forces present. Here, however, the increase in human capital dispersion takes over these channels and drives the increase in overall earnings variance.

What is the contribution of firms? The following exercise quantifies the importance of the firm learning environment channel. I shut down the heterogeneity in worker learning ability a , meaning I simulate a version of the model in which everyone has the median learning ability from the original distribution $G(a)$.³⁸ In this version, all human capital differences arise only from the

³⁶This series is shifted down to match the lowest point achieved by the corresponding profile in the model. In the data, some fraction of the variance is captured by worker fixed effects in the level of earnings. These are not present in the model. In either case, whether the profile is shifted or not, the increase in variance is the same.

³⁷Most of the covariance terms are small. The only quantitatively large covariance term is the one between human capital and the piece-rate for the first 10 years after labor market entry. This arises because workers with low human capital have even greater incentive to match to firms with better learning environments, and therefore accept very low piece-rates in order to work there.

³⁸When I do the opposite exercise in which I turn off differences in firm learning environments but keep the *ex-ante* differences across workers, I find that worker differences account for about 59% of the increase in variance. This is exactly the remaining share of the 41%. In general, these shares do not have to add to 1. If there were any meaningful sorting in the model, workers could change their job search decisions enough such that the allocations in the two counterfactuals look significantly different.

kinds of firms that workers match with – a new “luck” channel that impacts workers’ earnings outcomes. I then recompute the earnings variance profile and decomposition.

The corresponding variances for each component in the version of the model without heterogeneity in learning ability are shown in the right panel of Figure 10. In this counterfactual, the variance of log earnings increases from 0.032 to 0.088. This increase is 41.4% of the increase of the variance of log earnings in the full model, implying that this channel is responsible for about 41% of the increase in life-cycle inequality.

Another way to interpret this result says that the importance of firms is highest early on in worker’s lives. This is because early on, workers have limited employment histories and also because they are accumulating human capital very quickly. As a result, a worker’s initial match is important. By age 30, 85% of new earnings dispersion comes from human capital. Of the additional variance accumulated since entry, 51% arises due to firm differences. Despite their own abilities, workers who get lucky early on and match to a firm with a better learning environment get a head start over their peers, contributing to inequality among their cohort. But as workers have time to catch up, the influence of firms declines because workers have had time to find better matches. This mechanism also means that there are permanent differences in lifetime earnings that can be traced back to early labor market experiences; in particular, the identity of a worker’s initial match.³⁹

This finding offers a new explanation for rising earnings inequality over the life cycle. Two major insights emerge. First, it is not just a matter of inherent differences across workers. Firms too have an effect on a given worker’s earning growth rates and thus contribute to the increased heterogeneity between workers that becomes more pronounced over the life cycle. Second, luck manifests itself in a novel way. Search frictions impact the amount of human capital workers are able to accumulate. This effect goes beyond the standard role for search in only affecting how rents are split. As a result, there is an interaction between luck and worker differences, since persistent heterogeneity across workers comes about due to differences in labor market histories.

7 Reduced-Form Earnings Process Estimation

The results thus far imply that employers play an important role in the formation of the human capital of their workers. Next, I show how this fact matters for the statistical properties of the labor income process. I find that the properties of workers’ earnings in the model are similar in other dimensions to the data. In doing so, I demonstrate how the mechanisms introduced here can provide economic interpretations of some features of the labor income process.

The stochastic processes of labor income estimated in the literature are characterized by two features: highly persistent shocks or heterogeneity in income profiles. Guvenen (2007) and Guvenen (2009) distinguish between the RIP (Restricted Income Profile) and HIP (Heterogeneous Income

³⁹For further evidence of a similar phenomenon, see Arellano-Bover (2019). He links the size of the firm in which a worker gets their first job to lifetime income, and finds evidence of human capital being a driver of this relationship.

Profile) processes. In RIP, all workers have the same life-cycle income profile, but face large and persistent shocks. In HIP, individuals face more moderate shocks, but exhibit individual-specific income profiles. Either process can account for the rise in income variance over the life cycle. In RIP, it comes from the accumulation of different, yet large and persistent shocks. In HIP, the individual-specific growth rates are more important than the shocks.

The earnings process generated by my model produces both of these features endogenously. The shocks are persistent because they reflect changes in employment status or firms, both of which are long-lived.⁴⁰ Individuals also face different income growth rates, because of a combination of their own learning ability and the learning environments of their employers. The following exercise will estimate RIP and HIP processes on the model-generated earnings data. I do this in the versions of the model with and without worker learning ability heterogeneity, to quantify how much of the profile heterogeneity is driven by firms.

7.1 The Earnings Process

As in Guvenen (2009), the log earnings of individual i at age h , y_h^i are given by:

$$y_h^i = \alpha^i + \beta^i h + z_h^i + \varepsilon_h^i \quad (16)$$

$$z_h^i = \rho z_{h-1}^i + \eta_h^i \quad (17)$$

where α_i is an individual-specific level of labor income and β_i is an individual-specific growth rate of income. The vector (α_i, β_i) is distributed across workers with zero mean, variances σ_α^2 and σ_β^2 , and covariance $\sigma_{\alpha\beta}$. Aside from these permanent components of worker heterogeneity, the income process also contains an AR(1) component, z_h^i with persistence parameter ρ , and a purely transitory component, ε_h^i . The shocks to the AR(1) and transitory components are assumed to be independent, with zero mean and variances σ_η^2 and σ_ε^2 . Under RIP, the heterogeneity in individual growth rates is shut down: $\sigma_\beta^2 = 0$ and $\sigma_{\alpha\beta} = 0$. Thus the parameters to be estimated are $[\sigma_\alpha, \sigma_\varepsilon, \sigma_\eta, \rho, \sigma_\beta, \sigma_{\alpha\beta}]$ in HIP and $[\sigma_\alpha, \sigma_\varepsilon, \sigma_\eta, \rho]$ in RIP.

With panel data on individuals, the parameters can be identified by using the cross-covariances of labor earnings at different ages. The variances and covariances implied by the income process in (16) and (17) are:

$$\text{var}(y_h^i) = \sigma_\alpha^2 + \sigma_\varepsilon^2 + \left(\frac{1 - \rho^{2h+1}}{1 - \rho^2} \right) \sigma_\eta^2 + 2\sigma_{\alpha\beta}h + \sigma_\beta^2 h^2 \quad (18)$$

$$\text{cov}(y_h^i, y_{h+n}^i) = \sigma_\alpha^2 + \sigma_{\alpha\beta}(2h+n) + \sigma_\beta^2 h(h+n) + \rho^n \left(\frac{1 - \rho^{2h+1}}{1 - \rho^2} \right) \sigma_\eta^2 \quad (19)$$

⁴⁰ Another way to get this would be explicitly including shocks to human capital. However, my estimates imply that changes in earnings due to unemployment and job switches, the forces present in my model, are sufficient to get shock variances close to what are found in the data.

	Guvenen (2009) (U.S.)		Model with a het.		Model w/o a het.	
	(1) RIP	(2) HIP	(3) RIP	(4) HIP	(5) RIP	(6) HIP
ρ	0.988	0.821	0.9944	0.9561	0.9688	0.9268
σ_α^2	0.058	0.022	0	0	0	0
σ_ε^2	0.061	0.047	0.0758	0.0713	0.0747	0.0695
σ_η^2	0.015	0.029	0.0093	0.0110	0.0078	0.0101
$\text{corr}_{\alpha\beta}$	-	-0.23	-	0	-	0
σ_β^2	-	0.00038	-	0.00016	-	0.00007

Table 2: Estimating the parameters of the earnings process

Estimates refer to the parameters of the process in equations (16) and (17). In RIP, σ_β and $\sigma_{\alpha\beta}$ are restricted to be zero, thus they are not estimated.

To estimate these income processes in the model, I first need to construct a panel of worker earnings which I will use to compute the analogues of (18) and (19). Importantly, this panel will look more like the PSID, rather than a matched employer-employee data set. I throw out information on firms, and only keep earnings data for each worker by age.

I impose restrictions that are similar to the ones used on real-life panel data. I aggregate to yearly observations by focusing on the total earnings in employment in each year, as long as the worker was employed for at least one quarter. By construction, the model also contains 40 years of data for each worker. All cross-covariances are computed on income residuals, obtained by regressing earnings on an age profile. Because the specification of the income growth profile is linear, to keep with the literature I focus on only the first 25 years of income data in the model when human capital accumulation as a source of earnings growth is still active.

I use a GMM procedure to obtain parameter estimates. I search for the parameter set that minimizes the distance between the theoretical moments (18) and (19) and the cross-sectional covariances created from the panel. This amounts to 351 moments and either 4 or 6 parameters.

7.2 Estimates

Columns (1) and (2) of Table 2 report Guvenen (2009)'s baseline estimates for the RIP and HIP processes for the U.S. Columns (3) and (4) show the corresponding estimates from my model with heterogeneity in worker ability.⁴¹ The RIP processes in columns (1) and (3) are remarkably similar. Moving to HIP in columns (2) and (4) brings down the estimate of the persistence parameter ρ , reflecting a bias that is present when ignoring profile heterogeneity. In HIP, allowing for $\sigma_\beta^2 > 0$ reduces the persistence parameter and attributes more differences in individuals to heterogeneity in income profiles. In the version of the model in column (4), the profile heterogeneity is coming

⁴¹Note that in the model, the variances of all terms involving σ_α^2 are zero because there are no permanent differences in the level of earnings across workers.

from both worker-specific learning ability and firm learning environments.⁴²

Next, as I did for the counterfactual exercise in the last section, I turn off all heterogeneity in worker learning ability and give each worker the median value from the original distribution. I re-estimate the labor income processes and present the results in columns (5) and (6) of Table 2. This version still exhibits the bias in ρ and also estimates some dispersion in worker-specific growth rates: about half of what was found in the model with heterogeneity in learning ability.⁴³

In this version of the model, all income profile heterogeneity is due to the series of firms a worker matches with. An individual's income profile is pieced together by different growth rates offered by different firms. In previous literature, the findings about heterogeneous income profiles across workers were mainly interpreted as fixed worker differences, for instance, coming from learning ability. However, I find that even in a version of the model with no *ex-ante* differences across workers, the earnings process still picks up this kind of heterogeneity in growth rates. This suggests that some of these estimated differences are coming from firms, and are not permanent differences at all.

8 Policy Experiments

So far, the findings suggest that many labor market outcomes are not due to permanent differences across workers, but rather come about because of search and matching frictions. This means there is a way for policy to affect the allocation of workers to firms. In this section, I use the model to conduct policy experiments in which the structure of unemployment insurance (UI) impacts the types of jobs that workers are willing to accept.

The trade-offs that workers face between jobs at different points in the life cycle is key to understanding why the types of jobs held by workers affect aggregate outcomes in the model. On one hand, young workers would like to be very selective about which jobs they accept. The learning environment is important to them because finding good firms along this dimension early in life will boost earnings for their entire lifetime. Moreover, if workers have access to firms with good learning environments, aggregate output is boosted because matches produce more when workers have been able to accumulate more human capital early on in life. Generous unemployment benefits, especially for young workers, would incentivize them to wait longer for these types of jobs when they enter the labor market. On the other hand, if workers are waiting too long to accept jobs their human capital stagnates, unemployment is high, and output is lower for both of these reasons. Unemployment insurance policies can be used to balance these trade-offs.

⁴²It is not surprising that the estimate of σ_{β}^2 , the extent of profile heterogeneity, in the model is smaller than that of the data because the variance of earnings rises less in Germany than it does in the U.S.

⁴³In fact, the estimate of ρ goes down by more and so this model will actually attribute more income variance to the β^i . This is because some of the negative sorting in the full model cancels this out, whereas the experiment turns off any sorting.

8.1 Setup

In the baseline model, unemployment benefits replace some fraction b of a worker's human capital.⁴⁴ I will consider two types of policies. The first type is a flat benefits schedule in which I simply vary the value of b . In the second type, the replacement rate b depends on age:

$$b(t) = b_1 t^{-\frac{1}{b_2}}$$

Therefore an age-dependent schedule will be characterized by a pair (b_1, b_2) .

The unemployment benefits are funded by a lump sum tax on earnings, B , paid by employed workers.⁴⁵ I consider revenue-neutral changes in policy, meaning that for each UI schedule I consider, both flat and age-dependent, I find the level of B that ensures that the government's budget deficit is the same as in the baseline model.

8.2 Outcomes

I will study the impact of the policies on four different model objects, which are computed in the following ways:

1. **Output:** ph , aggregated across all workers (zero for unemployed workers).
2. **Welfare of new entrants:** The value functions for new labor market entrants. Since all workers enter unemployed and with the same level of human capital, it is the value of unemployment at the initial human capital level integrated over the distribution of worker ability types.
3. **Lifetime income inequality:** Lifetime income is the discounted sum of pre-tax labor income earnings throughout a worker's life. The discount rate is β and inequality is measured as the variance of the log of this object across workers. This is a long-run measure of worker outcomes that takes into account all the events that happen over a worker's career.
4. **Cross-sectional variance of log earnings:** Pre-tax variance of log earnings.

In some cases, I will compare these outcomes to an efficient benchmark in which $\sigma = 1$ and $b = 0$. When $\sigma = 1$, all of the joint match value goes to the worker. Therefore, workers fully internalize the entire future value of the match and the allocations of workers to firms coincides with what a social planner would choose. The planner's benchmark maximizes the welfare of new entrants, taken as given the search frictions. Like in Jarosch (2015), the planner arrives at an efficient allocation by altering the hierarchy of firms across the ladder. Here, UI benefits impact this margin and have the potential to achieve an allocation closer to that of the planner.

⁴⁴In the end, there is a negative relationship between earnings in the past job and subsequent benefits because earnings are also determined by p and w . This relationship is consistent with the data.

⁴⁵A proportional tax on labor income would be ideal, but it makes the model intractable as the joint match value would depend on the piece-rate.

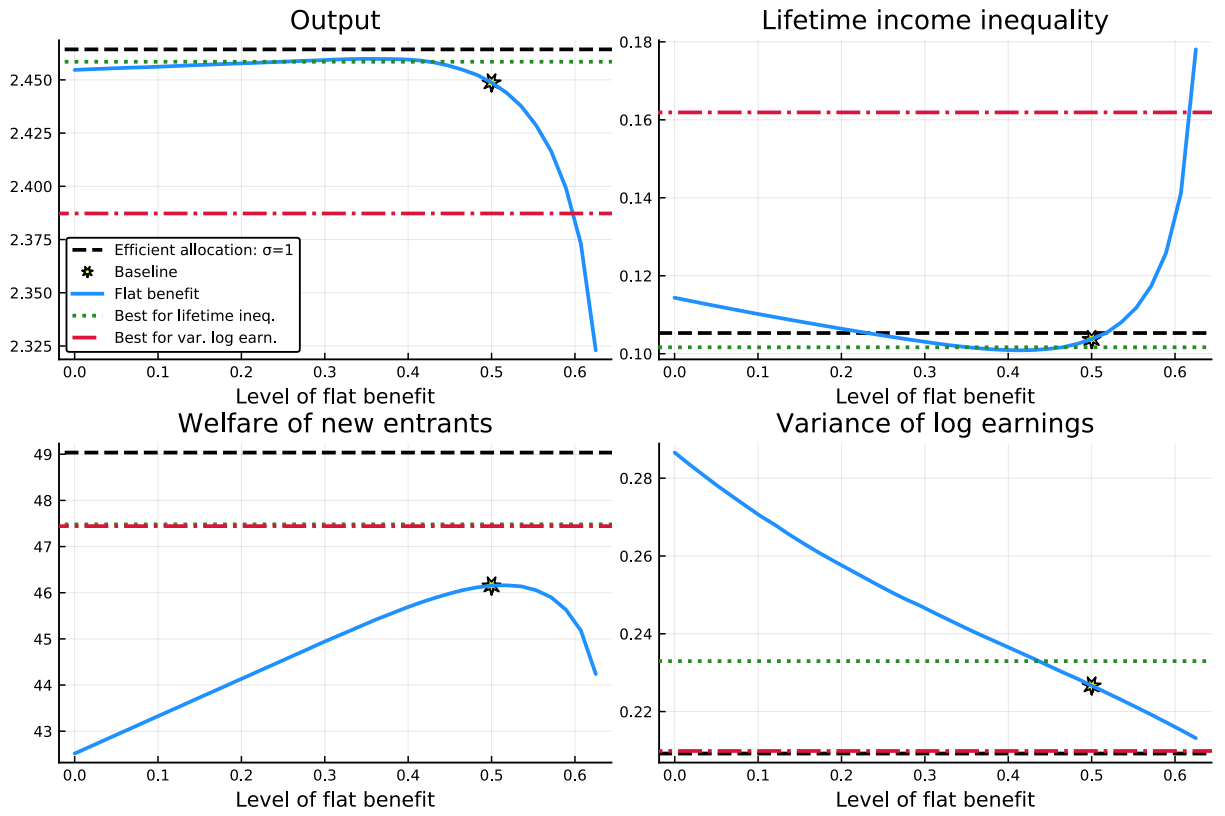


Figure 11: Output, welfare, lifetime inequality, and cross-sectional inequality across different UI benefit schedules.

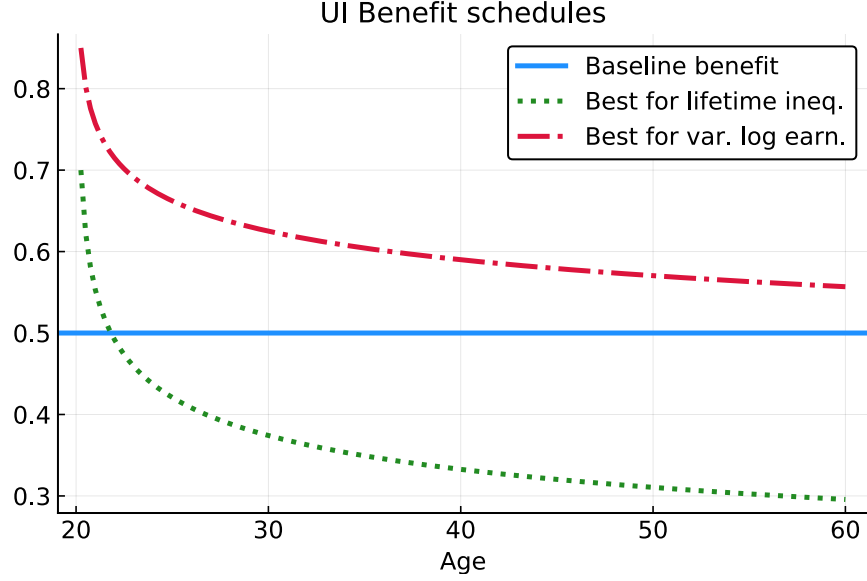


Figure 12: Age-dependent policies that achieve different outcomes

Figure 11 shows the impacts of different policies on output, welfare of new entrants, lifetime income inequality, and the variance of log earnings. The dashed black line indicates the level achieved by the planner's allocation. First, to understand the impacts of changing the level of flat UI benefits, consider the paths drawn by the solid blue lines. The starred points indicate the outcomes from the baseline model with $b = 0.5$. As benefits are raised, output rises as workers prefer to accept better jobs that enable them to produce more and accumulate more human capital. It drops off steeply if benefits get too high because unemployment goes up, directly impacting output. It also indirectly impacts output as less human capital is accumulated because workers spend more time in unemployment. The welfare of new entrants exhibits a similar pattern: it maxes out at some point beyond which lifetime utility starts to decrease as workers expect to be unemployed for longer and accumulate less human capital. The U-shaped pattern of lifetime income inequality arises because higher benefits initially induce all workers to take up jobs that boost their lifetime earnings. Eventually, however, inequality rises because some workers luck out and find good initial jobs quickly, whereas others are induced to wait a long time to find good jobs, which means their human capital stagnates in the meantime. The variance of log earnings declines with the benefit level. This is because in the cross-section workers accept a smaller set of jobs, reducing inequality among employed workers. In the case of output and lifetime income, the best flat benefit does better than the baseline, but the differences are quantitatively small. Neither can come close to achieving the welfare in the efficient allocation.

Next, I ask whether I can find an age-dependent UI schedule that can achieve similar or lower levels of inequality, but also improve welfare at the same time. I searched over the parameter space (b_1, b_2) to find one policy that improved lifetime income inequality and one that improved cross-sectional income inequality. These policies, along with the baseline flat policy, are depicted

in Figure 12.

In both cases, the benefits schedule is front-loaded: younger workers receive higher UI. These schedules encourage workers to spend more time searching early on in life compared to the baseline. However, they drop off quickly in order to incentivize workers to become less selective and accept a job before the window to accumulate human capital runs out. This is a similar result to Michelacci and Ruffo (2015), who find that higher UI is optimal for younger workers. Their result is driven by the fact that the young tend to be unable to smooth consumption during unemployment, and want jobs anyway to accumulate human capital. In this paper, the human capital accumulation incentive is also there, but here higher benefits while young insures workers for the risk of not finding a good match. Workers in this model need to search over a set of jobs in which some offer better returns to human capital accumulations compared to others.

The red and green dashed lines in Figure 11 indicate the levels of output, welfare, lifetime inequality, and cross-sectional inequality achieved by each of the age-dependent policies in Figure 12. Quantitatively, neither improves inequality by much, but they are both able to get welfare to about halfway to the planner's benchmark. This happens because the frontloaded schedule helps young workers get into good matches early on. At the same time, it does not exacerbate unemployment too much because benefits for all other workers become much lower, especially for the schedule that improves lifetime inequality. So these schedules help balance the tradeoffs associated with unemployment benefits in this model, by giving the highest levels to the workers who need them the most.

In all cases, changes in the UI benefits schedule work by altering job acceptance strategies. Because these are most important for young workers, and because so many worker outcomes are determined by events early on in the life cycle, unemployment benefits have impacts on aggregates like output and unemployment, as well as earnings inequality. These experiments therefore highlight an important role for unemployment insurance design beyond just insuring workers against short-term job loss.

9 Conclusion

This paper argues that firms impact the earnings growth of their workers and that differences in learning environments between firms are major drivers of firm earnings growth differentials. Starting from the fact that firms offer systematically different earnings trajectories to the workers they employ, I develop a search model in order to disentangle the effects of different sources of earnings growth heterogeneity. Earnings can grow due to differences in worker ability, firm learning environment, and firm productivity.

The model introduces key trade-offs between jobs that drive workers' decisions over the life cycle, and thus the resulting earnings dynamics. Because the ability to accumulate human capital is highest for the young, they highly value a match with a firm with a good learning environment;

eventually this firm attribute becomes irrelevant and workers switch to climbing the ladder in productivity. I exploit these age differences in sources of earnings growth in the data to discipline the relevant sources of heterogeneity in the model.

I show that this new firm learning environment channel is responsible for 41% of the increase in the cross-sectional earnings variance experienced by workers over the life cycle. This implies an important role for firms in shaping workers' human capital. These effects are especially important for younger workers. Although workers do eventually catch up to each other by moving to better firms, early labor market experiences persistently impact lifetime earnings. My results speak to the importance of initial conditions upon labor market entry and offer a channel through which firm/worker matches have long-term impacts. I then explore two settings that illustrate the broader importance of these findings. I show that firms shape some of the estimated profile heterogeneity across workers, suggesting that labor income processes should account more explicitly for temporary firm/worker matches and incorporate matched employer-employee data. I also demonstrate how policy can balance the tradeoffs between search and human capital accumulation, and improve welfare at the same time.

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