

Assignment-2

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Q2. $h(x, y) = \exp\left(-\frac{x^2 + y^2}{2\sigma^2}\right)$. Expression for Wiener filter?

Given ratio of power spectra of the noise and undegraded signal is a constant.

$$W(u, v) = \frac{H^*(u, v)}{|H(u, v)|^2 + P(u, v)}$$

$$P(u, v) = S_n(u, v) / S_f(u, v) = \text{constant (Given)}$$

$$S_f(u, v) = |H(u, v)|^2 \text{ power spectral density of signal}$$

$$S_n(u, v) = |N(u, v)|^2 \text{ power spectral density of noise}$$

$$H(u, v) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} h(x, y) e^{-2\pi j(ux + vy)} dx dy$$

$$= \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \exp\left(-\frac{x^2 + y^2}{2\sigma^2}\right) \exp\left(-2\pi j(ux + vy)\right) dx dy$$

$$= \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \exp\left(-\frac{(x + 2\pi j u \sigma^2)^2}{2\sigma^2}\right) \exp\left(-\frac{(y + 2\pi j v \sigma^2)^2}{2\sigma^2}\right)$$

$$\exp\left(-\frac{1}{2\sigma^2} (4\pi^2 u^2 \sigma^4 + 4\pi^2 v^2 \sigma^4)\right) dx dy$$

$$= e^{-2\pi^2\sigma^2(u^2+v^2)} (\sqrt{2\pi\sigma^2})(\sqrt{2\pi\sigma^2})$$

$$= 2\pi\sigma^2 e^{-2\pi^2\sigma^2(u^2+v^2)}$$

$$H(u, v) = 2\pi\sigma^2 e^{-2\pi^2\sigma^2(u^2+v^2)}$$

$$H^*(u, v) = H(u, v)$$

∴ Wiener filter expression

$$W(u, v) = \frac{2\pi\sigma^2 e^{-2\pi^2\sigma^2(u^2+v^2)}}{4\pi^2\sigma^4 e^{-4\pi^2\sigma^2(u^2+v^2)} + \text{constant}}$$

(Q3)

i) Calculate the Local Binary Pattern (LBP)

ii) " " Local Derivative Pattern (LDP)

for 4 neighbours ~~(0°, 45°, 90°, 135°)~~ → (0°, 45°, 90°, 135°)

Image Patch →

$$\begin{bmatrix} 2 & 5 & 3 & 5 & 1 \\ 6 & 7 & 9 & 1 & 5 \\ 2 & 3 & 4 & 8 & 2 \\ 3 & 2 & 3 & 2 & 9 \\ 1 & 2 & 3 & 2 & 1 \end{bmatrix}$$

i) Local Binary pattern

$$\begin{bmatrix}
 2 & 5 & 3 & 5 & 1 \\
 6 & 7 & 9 & 1 & 5 \\
 2 & 3 & 4 & 8 & 9 \\
 3 & 2 & 3 & 2 & 9 \\
 1 & 2 & 3 & 2 & 1
 \end{bmatrix} \xrightarrow{z_0} \begin{bmatrix}
 1 & 1 & 0 \\
 0 & 1 & 1 \\
 0 & 0 & 0
 \end{bmatrix}$$

$$\text{Binary representation} = (11010000)_2$$

$$= (208)_{10}$$

ii) Local Derivative Pattern

$$\left. \begin{aligned}
 I_0' &= 4 - 8 = -4 \\
 I_{45^\circ}' &= 4 - 1 = 3 \\
 I_{90^\circ}' &= 4 - 9 = -5 \\
 I_{135^\circ}' &= 4 - 7 = -3
 \end{aligned} \right\} \begin{array}{l} \text{First order} \\ \text{derivative} \end{array}$$

$$\begin{aligned}
 LDP_\alpha^2(z_0) = & \left\{ f(I_\alpha'(z_0), I_\alpha'(z_1)), \right. \\
 & f(I_\alpha'(z_0), I_\alpha'(z_2)), \\
 & \left. f(I_\alpha'(z_0), I_\alpha'(z_3)) \right\}
 \end{aligned}$$

Second-order Local Derivative Pattern

$$LDP^2(z) = \{LDP_{\alpha}^2(z) \mid \alpha = 0^\circ, 45^\circ, 90^\circ, 135^\circ\}$$

$$LDP_{0^\circ}^2(z_0) = 01010100$$

$$LDP_{45^\circ}^2(z_0) = 00101111$$

$$LDP_{90^\circ}^2(z_0) = 11010000$$

$$LDP_{135^\circ}^2(z_0) = 11000110$$

$$LDP^2(z_0) = \underline{01010100} \quad \underline{00101111} \quad \underline{11010000} \quad \underline{11000110}$$