



KTH Computer Science
and Communication

A comparison of visualisation techniques for complex networks

En jämförelse av visualiseringsmetoder för komplexa nätverk

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Abstract

The need to visualise big sets of data and networks within a company is a well-known task. In this thesis, research has been done of techniques used to visualize complex networks in order to find out if there is a generalized optimal technique that can visualize complex networks.

For this purpose an application was implemented containing three different views, that were selected from the research done on the subject. As it turns out, it points toward that there is no one generalized optimal technique one can default use to visualize complex networks in a satisfactory way. A definite conclusion could not be given because of that all different visualization techniques that exists could obviously not be evaluated within the time constraint of this thesis.

Referat

Behovet av att visualisera data inom ett bolag är ett välkänt behov. I denna avhandling har forskning genomförts av tekniker använda för att visualisera komplexa nätverk för att finna om det existerar en generell optimal teknik som kan användas vid visualisering av komplexa nätverk. För detta ändamål implementerades en applikation som hade tre olika vyer, som var valda utifrån den forskning gjord på området. Det visade sig att det pekar åt hållet att det inte existerar en generell optimal teknik en kan använda för att visualisera komplexa nätverk på ett tillfredsställande sätt. En definitiv slutsats kunde inte ges eftersom alla existerande visualiseringstekniker kunde uppenbarligen inte bli utvärderade inom tidsramen för denna avhandling.

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Chapter 1

Introduction

This chapter is intended to give an introduction to the subject of visualizing networks.

1.1 Background

To be able to visualize different networks is an important part in many fields, such as science and technology. For example, computer science that deals with complex networks of relationships between system components, displaying relations in a social network, molecular biology that study the interactions between various systems of cells, e.t.c.

There are different approaches to take when visualizing networks. The most traditional approach is to represent the network as some kind of graph, because many structures in different scientific fields can be represented as a node-link graphs. Where nodes represents different components and are visualized with a shape and edges represents different components relations and are visualized by a connecting line between two nodes.

1.2 Arising problems with growing data

Though the traditional ways of visualizing graphs are pleasing and give an intuitive way of looking at relations, there arises problems when the networks that need to be visualized are of a bigger size. The traditional ways may be sufficient when dealing with networks of small sizes of nodes and relations, but what happens when the networks become complex and have hundreds or thousands of nodes?

1.2.1 Edge and node crossing

When the node count becomes larger the area dedicated to layout these becomes smaller. This can contribute to that nodes start to overlap each other, making it hard to distinguish between a set of different nodes.

A similar problem arises concerning edges. Depending on the layout of the nodes a different amount of edges may overlap, crossing each other. This may not be a problem if the number of crossings is low or the angle between two edges is high. But when this angle decreases and the number of crossings increases it becomes harder to distinguish between specific edges, to see which edge connects to which node. If the relations are of a large enough size the cluster of edges may become as just one big black area.

When dealing with layout techniques one strives to layout the nodes in a way that minimize node- and edge crossings.

1.2.2 Labeling

Labeling nodes and edges in a network becomes more challenging as the network grows. In fact the optimal label placement of a graph has been shown to be NP-Complete[29]. One can see the task of labeling to be divided in to three different labeling tasks:

- Labeling area features (clusters).
- Labeling line features (edges).
- Labeling point features (nodes).

1.2.3 Situation awareness

Human and psychology factors play a role when visualizing a network, situation awareness is a term in this aspect. Endsley[17] defines situation awareness as:

Situation Awareness is the perception of the elements in the environment within a volume of time and space, the comprehension of their meaning, and the projection of their status into the near future

Situation awareness becomes important to consider when choosing visualisation technique.

Figure 1.1 shows what can happen when trying to visualize big networks.

1.2. ARISING PROBLEMS WITH GROWING DATA

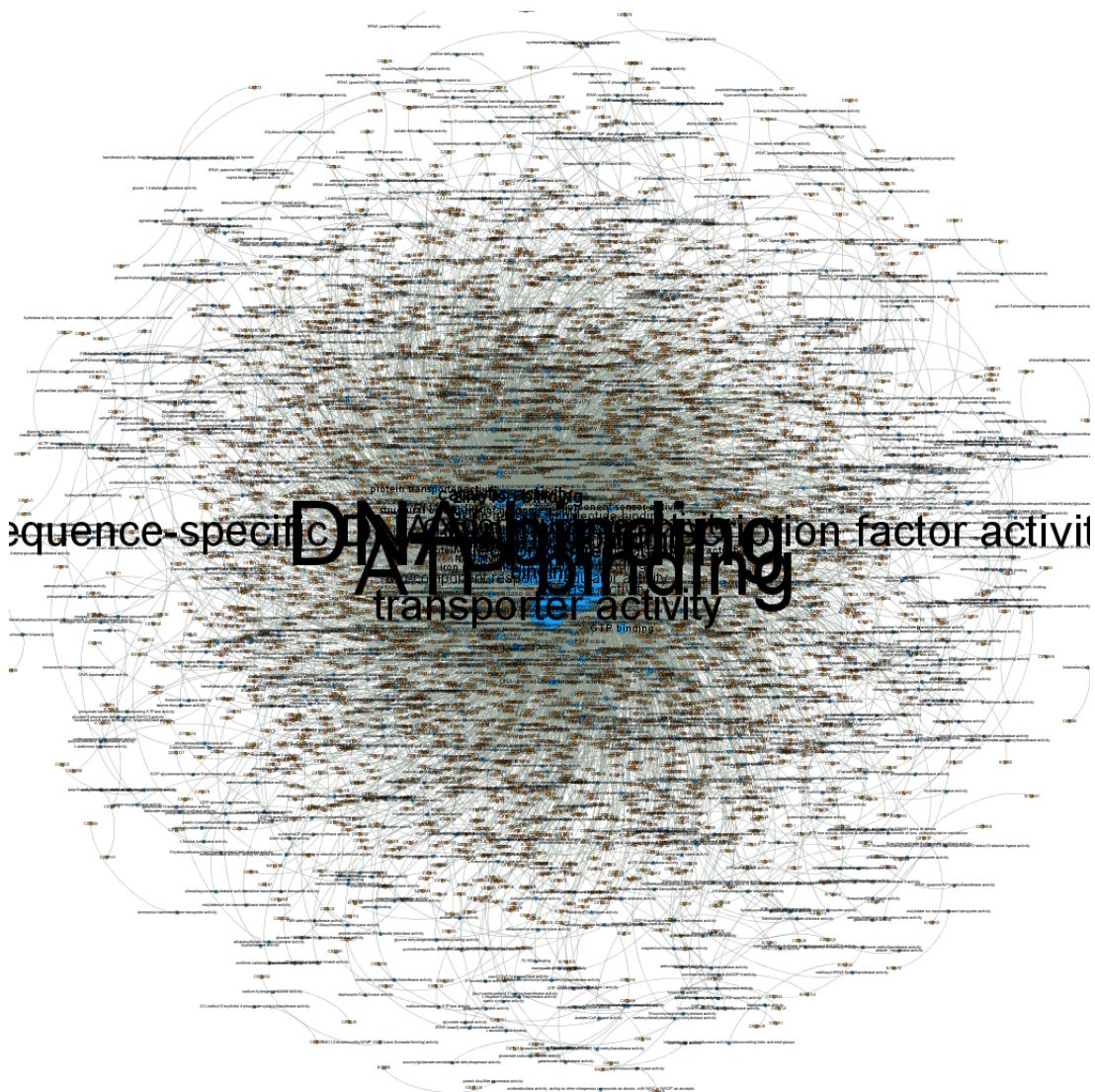


Figure 1.1. Example of a graph where the problem of node- and edge crossing becomes obvious

1.3 This thesis

This thesis revolves around the question:

Which types of visualization techniques are suitable for visualizing large and complex networks?

With the corresponding hypothesis that:

One can conclude that some visualization techniques are better suited than others and that one or several may be best for the task at hand.

In chapter two different common visualisation techniques are described. Chapter three goes through the methodology used to evaluate a set of different techniques. Chapter four provides the results from chapter 3. Chapter five discusses the results and conclusions.

Chapter 2

Visualization techniques and their theory

There exist a number of different approaches and techniques used to visualize large and complex networks. This chapter is intended to introduce some of these and explain how they work.

2.1 Fundamental techniques

Though there exist a number of different approaches many of these are based on some fundamental technique or concept. Two major aspects are important to consider when trying to visualize a network. First is about the part that most probably relate to graph visualization, the actual layout algorithm that decides where each node is to be placed and how the edge routing is made. Second is the aspect of how one is to navigate a graph when it has been generated, that is navigation such as zooming and panning.

2.1.1 Force-Directed

Force-directed is a popular class for a type of algorithm for calculating layouts of graphs. They are constructed to strive towards generating graphs with node positions so that edges in the graph are of equal length and the layout displays as much symmetry as possible. One of the pros with these algorithms is that they are flexible, they do not rely on domain specific knowledge but instead only use the information contained within the structure of the graph. Graphs produced by these algorithms tend to be aesthetically pleasing and exhibit symmetries[26]. Figure 2.1 shows an example of a graph drawn with a force-directed algorithm.

These algorithms are based on assigning forces between nodes and edges in a graph, simulating the motion of the edges and nodes or minimize their energy. One of the first force-directed algorithm dates back to 1963 with the algorithm of Tutte[56] and is based on barycentric representation[26]. Though the more com-

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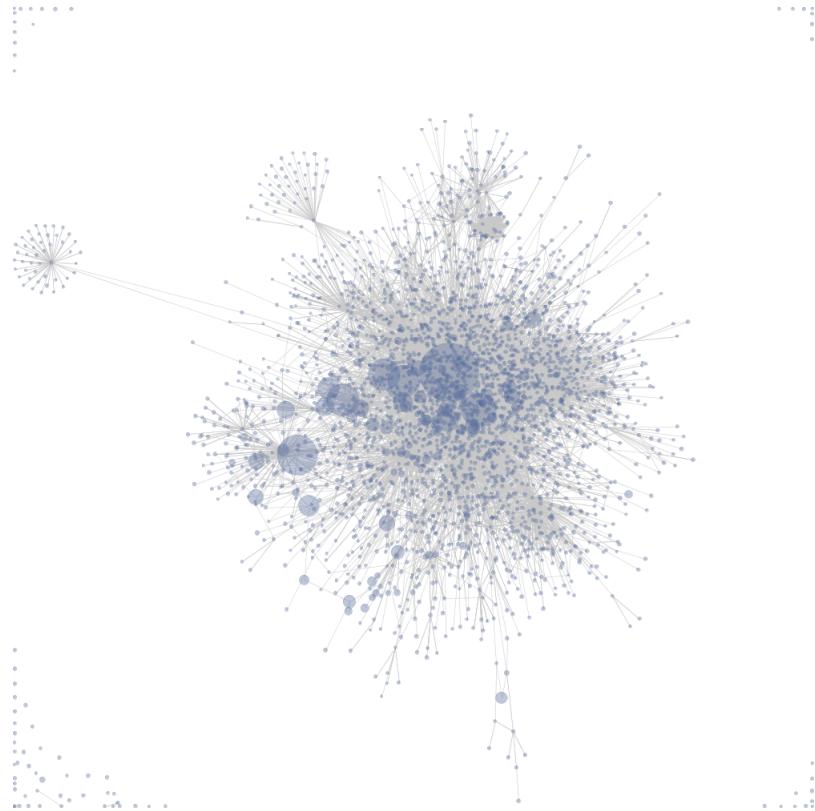


Figure 2.1. Visualization of links between pages on a wiki using a force-directed layout.

monly used algorithms such as Eades[16] and Fruchterman and Reingold[18] both rely on spring forces similar to those in Hooke's law. Here there are repulsive forces between all the nodes in a graph while in the same time attractive forces between nodes and their neighbours. As in the Eades algorithm [26] where they have an initial random layout of nodes. Having nodes represented as steel strings and edges as springs. Then letting the system move towards a state where minimal energy between nodes are achieved.

Besides striving towards equal edge length and displaying symmetry one can argue that the graph layout also should strive to have an even vertex distribution for a more pleasing layout. The algorithm of Fruchterman and Reingold cover this by using a bit of a different physical model, seeing the vertices in a graph as atomic particles or as celestial bodies. Where the attractive forces are defined as [26]:

$$f_a(d) = \frac{d^2}{k}$$

Repulsive as:

2.1. FUNDAMENTAL TECHNIQUES

$$f_r(d) = \frac{-k^2}{d}$$

Where d is the actual distance between two vertices and k is the optimal distance.

K is defined as:

$$k = C \sqrt{\frac{\text{area}}{\text{number of vertices}}}$$

Besides from this the algorithm also uses the notion of temperature as a refining step. This works so that when the algorithm improves the layout the adjustments become smaller from the last iteration of the algorithm.

As the graph size grows bigger, graphs with more than a few hundred vertices, a problem arises with the basic force-directed algorithms. The fact is that the used physical model has multiple local minima, and a graph produced with only a local minima can be much worse than would it be produced with the global minima. There have been developed algorithms to try and avoid local minima, such as the Hadany and Harel algorithm [23], which is based on a multi-level layout technique that works with graphs containing 15000 vertices.

In multi-level techniques the graph structure that is to be drawn is viewed in substructures where each substructure has less complexity than the whole. These substructures are then laid out in order from the most simple structure to the most complex one. Hadany and Halers [23] said it good as that a natural strategy for drawing a graph in a pleasant manner is to first consider an abstraction, disregarding some of the graphs fine details. Afterward add details to correct the layout. They also take up the importance of preserving the essential features of the graph in the abstraction, so it becomes of importance to be able to point out the essential feature of a graph.

2.1.2 Navigation through zooming

The way one zooms becomes a large part when navigating a graph, how one does this greatly affects the situational awareness. When navigating through a graph both global context and local details are of importance. Global context is provided when one can navigate through a graph and still be able to orient oneself according to the graph. Which most often requires one to be far zoomed out to see the whole. Though when zoomed out the local details are not on a high enough level to give any real information. So to get out more detailed information one is needed to zoom in the graph to a specific area, which is when a tunnel vision problem arises. Causing one to easier lose orientation and information of the overall dependencies when the context is lost.

FishEye view is a technique that address this problem of tunnel vision. One can compare the technique to a fisheye lens used by cameras for the creation of wide panoramic images. The techniques allows one to show high detail at focus while displaying less and less detail about information that are further away from focus, how much depending on how far away it lies. Figure 2.2 shows an example of this. Extra effective this becomes if the data one works with has a clear structure so that

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one can cluster this data.



Figure 2.2. Picture of the Eiffel Tower displaying the fisheye effect. Where the base of the tower are in focus and one can see some details while still the whole tower is in the picture.

Next we show an implementation where a FishEye method was used that was done from [47], there they assume that the nodes are represented by squares and that no overlapping of nodes is present. It is based on data that is clustered in a way that one node can contain a subset of different nodes. Figure 2.3 shows an example of such a graph and a possible clustering of it.

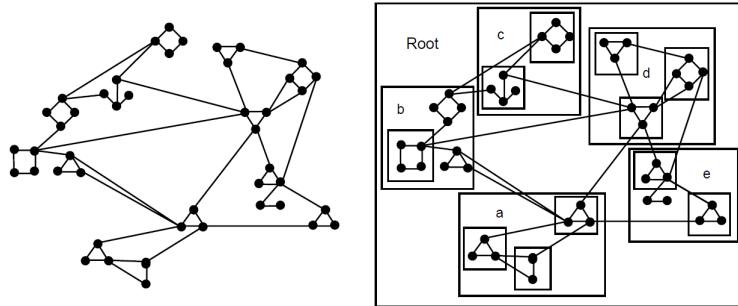


Figure 2.3. Graph that are divided into clusters.

When zooming one actually zooms a node/nodes (cluster/clusters). This translate into the FishEye view that the zooming node/nodes are in focus, getting larger, and the other node/nodes being outside focus and are getting shrunken. Figure 2.4 shows an example of a graph before a zooming action and after.

2.2. TWO-DIMENSIONAL SPACE

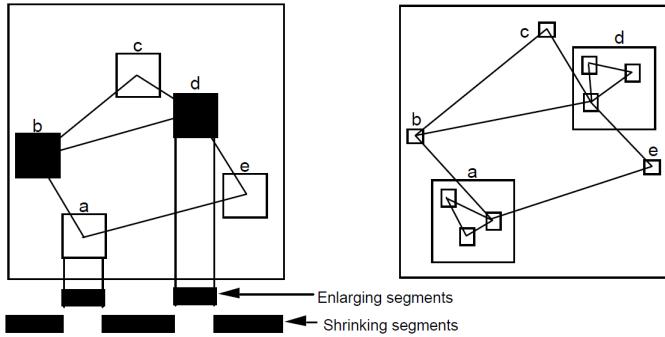


Figure 2.4. Example of graph when zoomed. Left hand shows the graph before zooming and which segments are being enlarge and which are being shrunken. Right hand shows the graph after zoom.

2.2 Two-dimensional space

Next we will introduce methods used to visualize large networks in the two-dimensional space. One benefit when using a layout in the two-dimensional space is that one can get away from the problem of nodes concealing each other.

2.2.1 BioFabric

BioFabric[28] is a method that uses a different approach to represent a graph than the traditional way where one represents nodes as a shape, like a circle or a rectangle, and edges as lines between nodes. Instead nodes are represented as one-dimensional horizontal lines and edges as one-dimensional vertical lines. These vertical lines start at one of the horizontal lines (one specific node) and end at another, representing a connection between these lines (nodes). This different approach lets one get away from the problem of node and edge crossings. It guarantees no edge overlapping and no node overlapping.

A difficulty that can arise with many methods is when one handles updates of graphs, which can result in major alterations of a graphs layout when only a few nodes are introduced. This problem exists in BioFabric as well, but because of adding one node is the same as adding one horizontal line and adding a edge equal to adding a vertical line this can help to not having such a big affect on the graphs appearance. Though how much it alters the graph is dependent on how many nodes are added and how many connections to other nodes are added.

As for how to layout the node and edges there are different approaches one can take. One basic approach is to do a breadth first traversal of the data to be displayed, where neighbouring nodes are visited in the order determined by their degree (the data are structured by degree of nodes). Next follows an example of a way of assigning nodes and edges that uses this approach [28].

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Node assignment:

1. Set row 1 as the next available row.
2. Find the highest degree node not yet processed, and assign it to the next available row. Make that row the current row; increment the next available row.
3. Take the node assigned to the current row and order its neighbors based upon their degree, highest degree first.
4. Traversing the neighbor nodes using that order, if the node has not yet been assigned, assign it to the next available row and increment the next available row.
5. Increment the current row. If a node has been assigned to that row, go to step 3. If not, go to step 2.

Edge assignment:

1. Set column 1 as the next available column. Make row 1 the current row c.
2. For current row c, get all the unassigned edges for the node in that row. Note that since we are not dealing with shadow links, all unassigned edges must connect to rows $\geq c$.
3. For each row $r \geq c$, create a set S of edges incident on c and r. Order these sets by increasing row number r, so that edges will be assigned in order of increasing length.
4. Iterating through the ordered list of sets, for each set S, order those edges in S based on lexicographic ordering of the link relation description, and assign them to the next available columns in this order; increment next available column appropriately. If there is a pair of directed edges with the same link relation description, downward links are assigned before upward links.
5. Increment the current row, and go to step 2.

Figure 2.5 is an example of a big network visualized with BioFabric using the basic approach.

One can also use approaches that try to group nodes based on similarity and difference between their connectivity. The way to represent similarity could be to use cosine similarity[50] or Jaccard similarity[52]. Figure 2.6 shows a network visualized using using similarity weights, resulting in a less compact layout than the basic approach.

BioFabric has one release which is an open-source Java application with some documentation that can be found at[3]. Though BioFabric is built on a relatively easy and intuitive algorithm, one could take the option of implementing an own version. Having their own customized features that suits one's purpose.

2.2. TWO-DIMENSIONAL SPACE

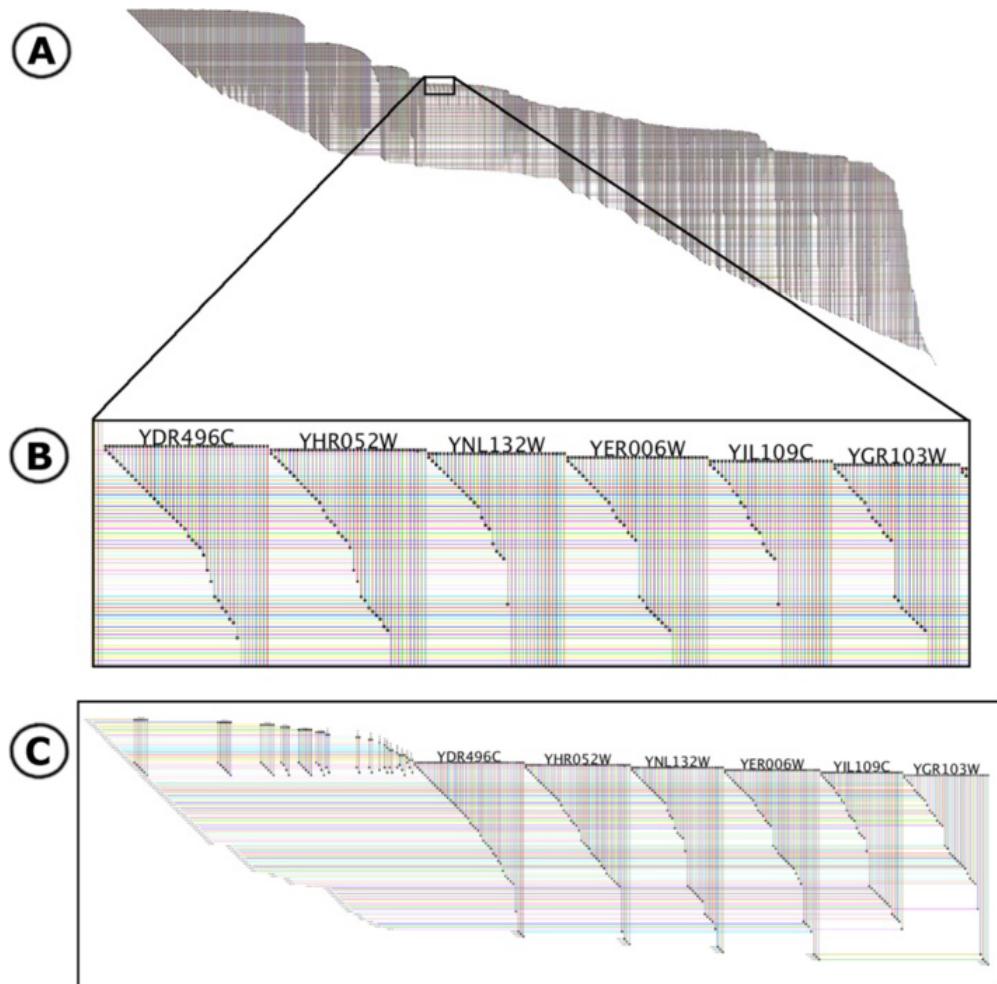


Figure 2.5. This is a depiction of the yeastHighQuality.sif data set [3-5] containing over 3000 nodes and 6,800 edges. The key feature of the BioFabric presentation is that nodes are depicted as horizontal lines, one per row; edges are presented as vertical lines, each arranged in a unique column. Note how the use of darker colors for rendering edges and lighter colors for rendering nodes insures that the former stand out despite the crossover. A) The view of the full network, laid out with the default algorithm. B) Detail of network shown boxed in network A, which highlights one advantage of the BioFabric presentation technique: similarities, and differences, in the connectivity of different nodes are immediately apparent. C) The six nodes and first neighbors depicted in a subset view, where all extra space has been squeezed out, creating a compact presentation that still retains all the relative positioning from the full view. Note how the full inventory of edges incident on the six nodes also includes those on the left originating from higher node rows.

CHAPTER 2. VISUALIZATION TECHNIQUES AND THEIR THEORY

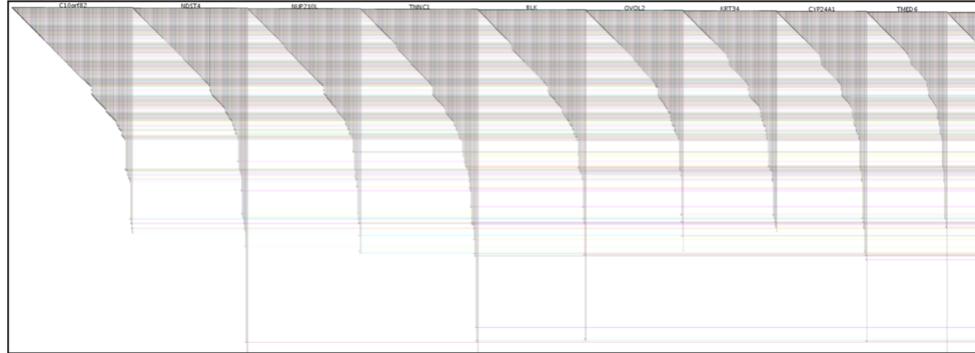


Figure 2.6. Layout that tries to place nodes with similar connectivity next to each other in the linear ordering of nodes.

2.2.2 HivePlots

HivePlots is a visualisation algorithm that uses a number of radially oriented linear axes that have a coordinate system that is based on nodes properties. A networks nodes are layed out on these axes. Connecting nodes are shown with edges between them, visualized as curves between nodes. Figure 2.7 shows an example of a HivePlot.

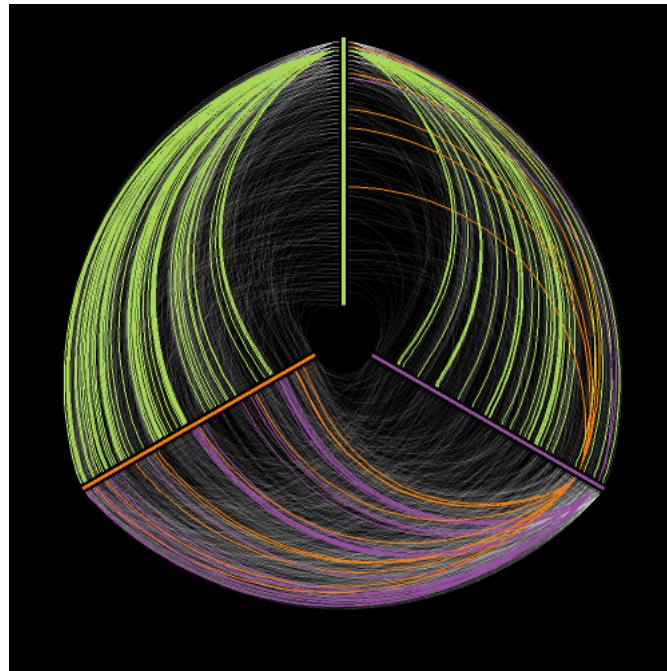


Figure 2.7. Example of a HivePlot containing 2500 vertices and 5900 edges.

Initially before the layout is made a number of structural parameters are calcu-

2.3. THREE-DIMENSIONAL SPACE

lated. Such as degree, flow, Page rank, clustering coefficient etc. Which parameters to use is up to the user to decide to fit with the network to be visualized. For example one would use the clustering coefficient to distinguish between hubs and clusters. Next these parameters are used to set up rules that are used to assign nodes to an axis and decide its coordinate. These rules are often boolean rules. Example of rules could be:

- Is the node a sink?
- Is the node a source?
- Clustering coefficient < 0.5 ?

If a HivePlot can be created with three axes this is preferred [27], laying the axis with a uniform radial distribution. Because with three axis you get a layout that is edge crossing free. In addition to this three axis makes it possible for each edge between each axis pair not to cross another axis. Though this is not restrained to only three axis, it can be hard to partition nodes to axis so that nodes on axis are only connected to neighbouring axes.

For hive plots there are some choices of use, one used is a Java based library [2]. There are also libraries for R[45], HiveR[1], that supports hive plots in the two-dimensional and three-dimensional space. The framework D3.JS[14] is an other option that is a JavaScript to create hive plots. And pyveplot[43] that is a library for hiveplots in Python[44].

2.2.3 TreeMap

TreeMap is a technique to present graphs in sequences of nested boxes [24]. TreeMap requires the data to be hierarchy structured as a tree. Figure 2.8 shows an example. The size of individual boxes becomes significant in a TreeMap layout, where the user specifies how they should grow. Take for example if figure 2.8 shows data that represents a file system. The size of a box could then be proportional to the size of the file it represents. The colors of the boxes represents the hierarchy, same color of boxes belongs to the same file.

For Treemaps there is some choices for use. For .Net, which is this thesis working environment, there is the WPF Treemaps & SquarifiedTreeMaps control library[11], though it has poor documentation. Another alternative is the .NET Treemap Control library[15]. Here again the problem lies in little documentation and hard to get information about the library where this was part of an old Microsoft research project called Netscan.

2.3 Three-dimensional space

In the hope of acquire more space for the layout of a network one can take the approach to go from a 2D to a 3D environment. In other words one can strive

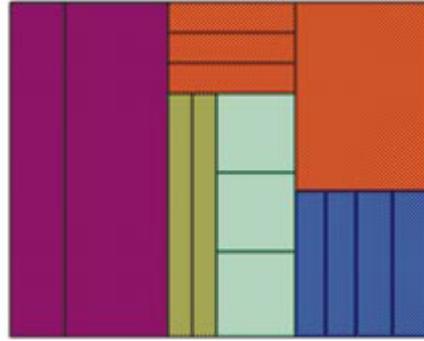


Figure 2.8. Example of a Tree-map

to get away from the euclidean space to another space that provides more space. An important aspect that follows going to a 3D view is that the system should be navigatable. This because in a 3D view, node and edge occlusions is bound to happen. Being able to change one view by navigating one can find a view of ones perspective that is without occlusions.

Hyperbolic space

The hyperbolic space has the property that it has more room compared to the familiar euclidean space [37]. [60] states that the fifth postulate in the Euclidean plane geometry can be formulated as:

Through a given point, not on a given line, one and only one line can be drawn which does not intersect the given line.

As in the hyperbolic plane geometry they introduce the Characteristic Postulate:

Through a given point, not on a given line, more than one line can be drawn not intersecting the given line.

Moreover two lines that are parallel in the euclidean space are always the same distance apart. As in the hyperbolic space parallel lines are not equidistant. For instance two parallel lines in the hyperbolic space that do not intersect can be separated by increasing distance the further away one moves from the origin. Figure 2.9 shows this compared to the euclidean geometry.

Normally to make use of the hyperbolic space, to use the extra space, one goes about to perform an layout algorithm in the hyperbolic plane or space and then display the results in the Euclidean plane or space. Some models to do this have been created. Best known are the Klein and the Poincaré models [24].

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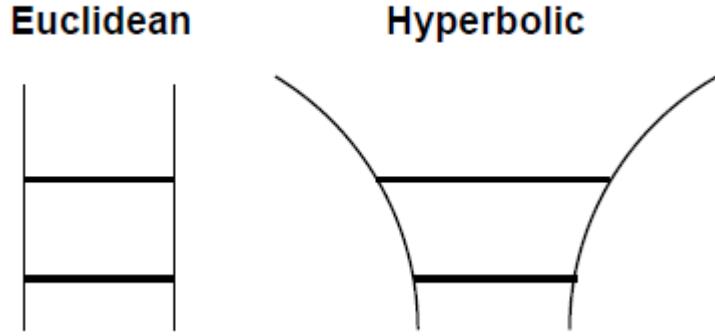


Figure 2.9. Parallel lines in euclidean space are always the same distance apart. In hyperbolic space the distance between two lines that never meet does indeed change. Here we show two geodesics which never meet but are not equidistant: the further they extend away from the origin, the more room there is between them.

2.3.1 GerbilSphere

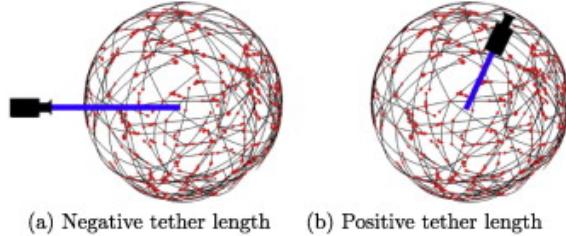
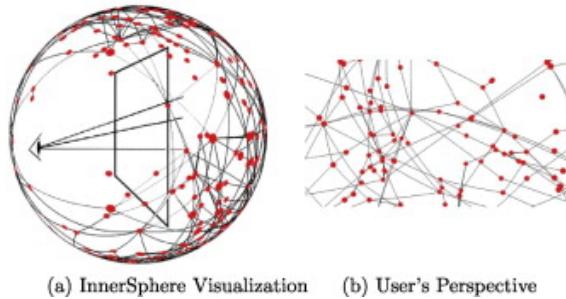
There have been studies on 2D vs 3D user interfaces that have shown that in many cases 2D exceeds 3D. Though the more space in 3D is still compelling. GerbilSphere is an inner sphere 2D system that tries to use the benefits from both a 2D approach as well as a 3D approach.

GerbilSphere works in a way that it lets the observer be able to places themselves inside a sphere while projecting the network on the surface of the sphere. As part of the layout, GerbilSphere uses an extended version of the Fruchterman and Reingold force-directed algorithm to apply to the three dimensional space. However this is not enough to work on the surface of a sphere. To apply the forces to the surface of a sphere, GerbilSphere uses a algorithm described by Kobeourov and Wampler [25]. For more technical information about the data structure and how their layout algorithm works see [48].

Zooming in GerbilSphere is viewed as having a world camera attached to one end of a tether and having the other end attached to the center of the sphere. Zooming in and out can be seen as moving the world camera along this tether. Figure 2.10 shows when zoomed out respectively zoomed in.

GerbilSphere implements a 2 1/2D interface, advocated by Ware[58]. When a user is positioned inside the sphere and zoom in, the part of the network when zoomed in will be visualized on a flat 2D surface, as seen in Figure 2.11. When zooming out one can still have there point of interest in view, trying to gain more global context of the network. Lastly one can zoom out enough to place the view outside the sphere, seeing the network on a 3D sphere.

GerbilSphere is an open source project. No API is available, though good documentation is presented within the code.

**Figure 2.10.** Spherical volume grid based**Figure 2.11.** Spherical volume grid based

2.3.2 H3: laying out large directed graphs in 3d hyperbolic space

[37] visualize graphs in the three-dimensional hyperbolic space by placing the network, represented as a spanning trees, inside a sphere. Exploiting the property that the amount of space covered by a sphere in the three-dimensional hyperbolic space increases exponentially with respect to the radius of the sphere, rather than polynomially. They compare using the traditional cone trees with their use of a layout on spherical caps, see figure 2.12. Figure 2.13 shows an example of a network being displayed from [37].

2.3. THREE-DIMENSIONAL SPACE

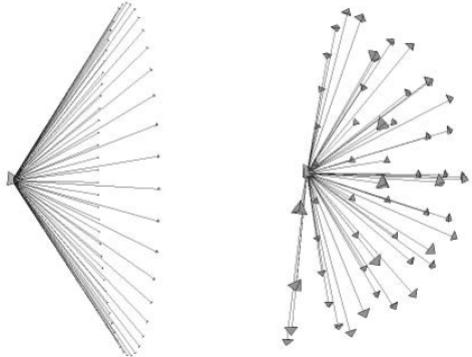


Figure 2.12. Comparison of the traditional cone tree layout along the circumference of a circle with the H3 layout on the surface of the spherical cap. Both pictures show 54 child nodes in hyperbolic space, represented by pyramids of the same size. Left: The traditional perimeter layout requires a large cone radius and is quite sparse. Right: A quite small cone radius suffices for the H3 spherical cap, so the layout is reasonably dense.

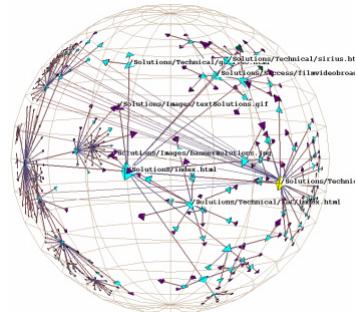


Figure 2.13. Link structure of a Web site laid out in Three-dimensional hyperbolic space by [37]. The nodes represent documents, which are coloured according to MIME type: HTML is cyan, images are purple, and so on.

2.4 Looking forward

After the information that has been undergone in this chapter how do we proceed in the future chapters of this thesis? When this thesis has been done within a time constraint all relative methods of visualisation could not be implemented and evaluated due to the great number of existing methods. Still measures need to be taken so that no major or relevant visualisation method gets overlooked. With the information presented in this chapter as a basis, the visualisation techniques of the highest relevance will be chosen for evaluation.

Space

One big choice of consideration is in what space is one to use for displaying their data? In this chapter the reader were introduced to a number of different spaces where also different visualisation methods have been evaluated with specific data as described.

One can conclude that the two most common spaces, the two- and three-dimensional space are of great importance and need to be included for this thesis purpose. Depending on which visualisation technique one chooses to use, they will have different aspects and characteristics that have different behaviours depending on which space one uses. Which can then be compared for evaluation purposes. Such as how layout of nodes and edges differs and what impact the space has on zooming and panning. Also how label clutter behave in these spaces may be of interest.

Layout method

When it comes to choosing which layout methods to evaluate, the same aspects mentioned in the previous section needs to be considered here as well. Which layout method one chooses to use can have a big impact on these aspects. Their results may also differ depending on which space one use and needs to be taken into consideration.

In addition to the effects on visualisation from different selection on spaces and layout methods there are other more practical aspects to be considered. Aspects revolving around one enforcing some pretension on the performance of the chosen methods implemented. This to ensure smooth usage so that a slow visualisation application will not impact the result in a negative way when evaluating a visualisation technique. More about this in section 3.2.

Chosen views

From the research and study in this chapter a selection narrowed down to three different views where made to be used for a implementation of an application. In this selection both the two-dimensional and the three-dimensional space were

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covered. We will show the resulting application and for each view give an account of why that view was selected and how it was implemented in 4.2.

Chapter 3

Method

When one is to display data using graphs one is confronted with the task of choosing between a large range of different visualisation techniques. This chapter is intended to show how which methods and areas have been chosen to be investigated for this thesis. In section 4.2 the way found to implement these choices for further evaluation is shown. In section 3.2 the way taken for evaluation is described.

3.1 Implementation

It is difficult to compare and evaluate different visualisation techniques only on the information found in scientific thesis and books concerning them. One cause to this arises when one looks at the data used. Different theses use different data, often different kinds of data even. In some cases data might seem bias, having been chosen to fit better with the visualisation method concerned for the purpose of that particular thesis, making it hard to compare performance between techniques. Different visualisation methods perform differently on different data, making it only helpful if one wants to establish some form of knowledge around that a specific technique can be good on a specific kind of data. For this thesis we have the need to have a more generalized unbiased approach.

To work around this an implementation were to be made that incorporates a selection of the studied techniques. Following the methodologies of selection for spaces and layout methods discussed earlier. This in order to make it possible to display the same networks (same data), using these different techniques and then be able to compare and evaluate performance on these techniques.

3.1.1 Programming environment

The implementation was to be developed in the programming language C# (C-sharp)[34] within Visual Studio[33]. The main application was to be made as an WPF (Windows Presentation Foundation)[36]. Other programming languages that have been used and incorporated in to the main WPF application is C++[13] and

Java[53]. For database retrieval LINQ (Language-Integrated Query)[32] has been used.

3.2 Evaluation

In order to draw some relevant results from this thesis it is necessary to evaluate the different visualisation techniques chosen to be investigated. In section 3.2.1 you will read about different aspects that needs to be considered when evaluating the different layout methods. In section 3.2.2 you will read about the necessity about adding tests concerning not only layout methods but also on the pre-requisites you have when implementing these, which programming libraries you choose to use.

3.2.1 Layout views

The different views will be evaluated on a number of characteristics that deemed to be of great importance for a general visualisation system, based on the study done in chapter 2:

- Navigation
- Situational awareness
- Ease of recognizing important parts as sub-networks, nodes and connections
- Labelling

The evaluation will be executed by using the implemented application to try and complete tasks similar to the following:

- Identify cluster/node X. Navigate to cluster/node Y. Can one navigate back to X?
- Identify the biggest cluster
- Identify node X
- Identify the node with highest degree

The tasks will be viewed as completed correctly, incorrectly or uncompleted. In addition to this, time will be taken in to consideration as a measurement of performance. The results and drawn conclusions from these evaluations can be found in chapter 5.

3.2.2 Programming libraries

An evaluation of different programming libraries was made to find a good starting point for the implementation of an application. First a study that investigates what different libraries exists that supports visualisation for different networks was made.

3.2. EVALUATION

In this research a comparison of which different functionality these libraries supports were retrieved in form of data structures and algorithms, layout algorithms and so on.

From this first initial study a selection of possible libraries to use for implementation were needed to be made. From here one could then evaluate the different selections to be able to make a final choice of which libraries to use.

The library evaluation will test for the libraries capacity in speed, how long time does it take to set up and draw networks of different sizes? And then as the last step was to evaluate the performance of the libraries after the networks had been drawn. This by taking measurements of smoothness while traversing a network. Were smoothness was represented by the applications FPS while navigating the network at different stages. The evaluation of programming libraries can be found in appendix D.

3.2.3 Data

To be able to perform these evaluations some data needs to be at hand, data that fits this thesis purpose. This thesis has been performed at a company that provided the necessary data to be visualized.

3.2.4 Data for layout views

For the layout views, data in the form of electronical units found inside trucks called ECUs (Electronic Control Units) are used. Also variables used within these systems called AEs (allocation elements) are used to be visualized.

This data have a complex form with a great number of relations and communications, not suiting some visualisation techniques more than others, thus making it suitable as data for this thesis purpose.

3.2.5 Data for evaluation of programming libraries

For the performance evaluation of programming libraries data was needed to be generated. To generate this data the program Gephi[19] was used. This program was to be used to generate a number of different graphs of different sizes which was then saved as a plain text file. The following graphs were generated:

- Graph with 50 vertices with 592 edges. Referred as G50.
- Graph with 100 vertices with 3941 edges. Referred as G100.
- Graph with 500 vertices with 99641 edges. Referred as G500.
- Graph with 1000 vertices with 399969 edges. Referred as G1000.

On the account that different libraries use different ways of representing data this text file can not be presumed to work as input for all libraries. On that fact

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parsers were needed to be developed to attend to that the input was on the right format for the corresponding library.

Chapter 4

Results

In this chapter the reader will be introduced to the results given from the literature studies and an implementation. The results from an evaluation of existing programming libraries are given in section 4.1.2. For a more in-depth review of these libraries and how they were evaluated see appendix D.

Section 4.2 shows the resulting application from the implementation. Here we go through the chosen views from the literature studies to be implemented and show how they were developed. Lastly in this section, developed data parsers that were needed to be implemented for these views are described.

4.1 Library performance

To be able to make a solid application that can be used for this thesis evaluations, not only the need (though it is most of importance) of choosing what layout methods to be used needs to be considered. Under which prerequisites one chooses to use while implementing said application needs to be considered. Here we bring this up by considering which libraries one can use when implementing the different visualisation methods.

4.1.1 Attribute matrix

The following matrix, Figure 4.1, lists important functionality one looks for when considering a programming library for implementing visualisation methods. The matrix gives an overview of what the different libraries supports from the start. This matrix helps as a basis when selecting libraries for the implementation.

<u>Library</u>	<u>Own layout algorithm</u>	<u>Documentation</u>	<u>External layout algorithm</u>	<u>Zoom functionality</u>	<u>Highlight functionality</u>	<u>Nested Graph support</u>	<u>User editable graphs</u>
QuickGraph	<input type="checkbox"/>	Good	<input type="checkbox"/>				
yFiles	<input checked="" type="checkbox"/>	Good	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>
GraphX	<input checked="" type="checkbox"/>	Good	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>
MSGAL	<input type="checkbox"/>	Good	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>
GraphViz	<input type="checkbox"/>	Decent	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>

Figure 4.1. Attribute matrix

4.1.2 Results from library tests

Speed

Each graph have been drawn ten times and the arithmetic mean value of the time has been calculated and given as result. Time is displayed on the form of minutes:seconds.

Table 4.1. Speed results

	G50	G100	G500	G1000
GraphX	00:00.51461281	00:07.41482771	22:33.4573175	Out of memory
VTK	00:00.01546258	00:00.04138581	00:00.88301525	00:03.53977976
yFiles	00:00.54974544	00:01.68249026	00:49.60542746	12:11.535764772

Smoothness - FPS

There are three fps measurements for each library were panning actions was being performed for each one. One zoomed out far away, giving an overview of the graph (Z1), one zoomed in half way to the centre of the graph (Z2) and a third were you are zoomed far in to the graph, being able to distinguish between vertices (Z3).

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Table 4.2. GraphX

	Z1	Z2	Z3
G50	17 fps	23 fps	35 fps
G100	1 fps	3 fps	5 fps
G500	Undetectable	Undetectable	Undetectable
G1000	Non-executable	Non-executable	Non-executable

Table 4.3. VTK

	Z1	Z2	Z3
G50	1000 fps	1000 fps	1000 fps
G100	500 fps	500 fps	500 fps
G500	35 fps	11 fps	3 fps
G1000	11 fps	7 fps	2 fps

Table 4.4. yFiles

	Z1	Z2	Z3
G50	22 fps	20 fps	25 fps
G100	2 fps	3 fps	5 fps
G500	Undetectable	Undetectable	Undetectable
G1000	Undetectable	Undetectable	2 fps

4.2 Application

In this section we will show the resulting application implemented with the corresponding views chosen from the research done in chapter 2.

4.2.1 Main application

At the start up of this application the user will be taken to the main application where the user will be prompted to make some choices before being able to visualize data. These choices are concerning which data to be used.

In this application the user are constrained to choosing between visualising ECUs or AEs, see section 3.2.4. The user is also prompted to chose which SOP date to use. Next the user will need to load the data from the database by pressing a button, labeled "Load Data". After that is done the user can then go on and choose which view to display. The user is not restrained to one view at the time but can bring up multiple views at the same time, making it easy to compare views.

Force-Directed(FD) based view

Force-directed algorithms is, as shown in chapter 2, an important part when it comes to visualising networks. There are many visualisation techniques based solely on force-directed algorithms. While other visualisation techniques that uses different approaches often incorporate some kind of force-directed algorithm to their visualisation method. As for example by computing a base graph using a force-directed algorithm. Therefore the first view of the implementation is a view that uses a force-directed algorithm for the vertices layout and edge routing. Figure 4.2 through Figure 4.7 shows examples of the application using this view.

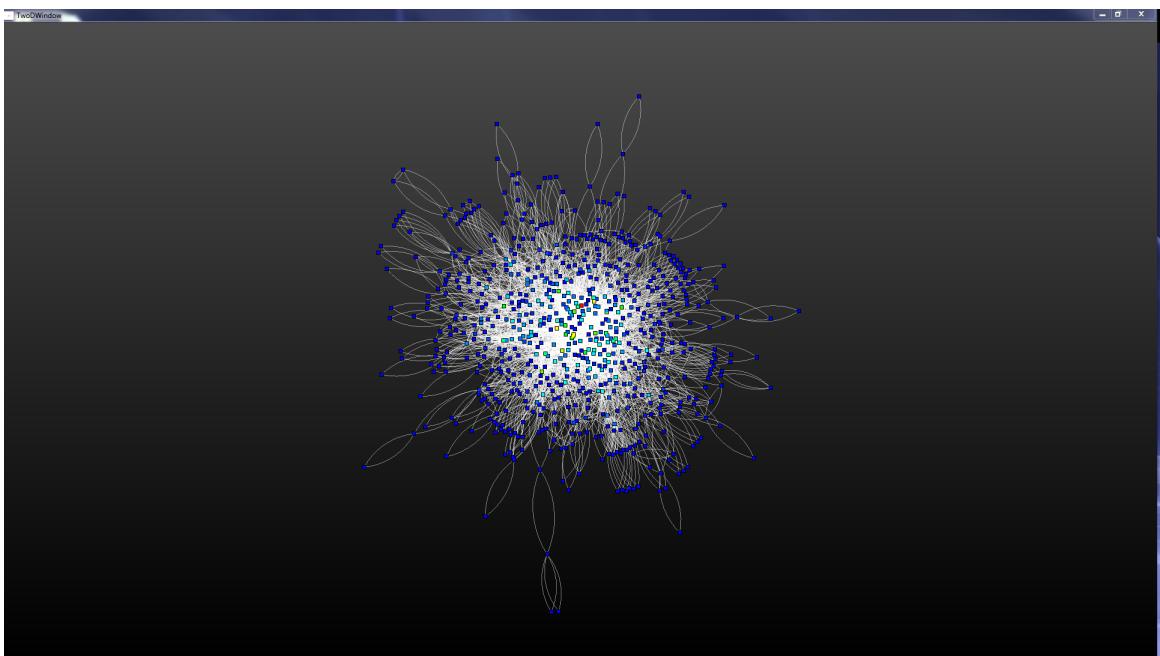


Figure 4.2. An unlabeled overview of a network were all AE was chosen.

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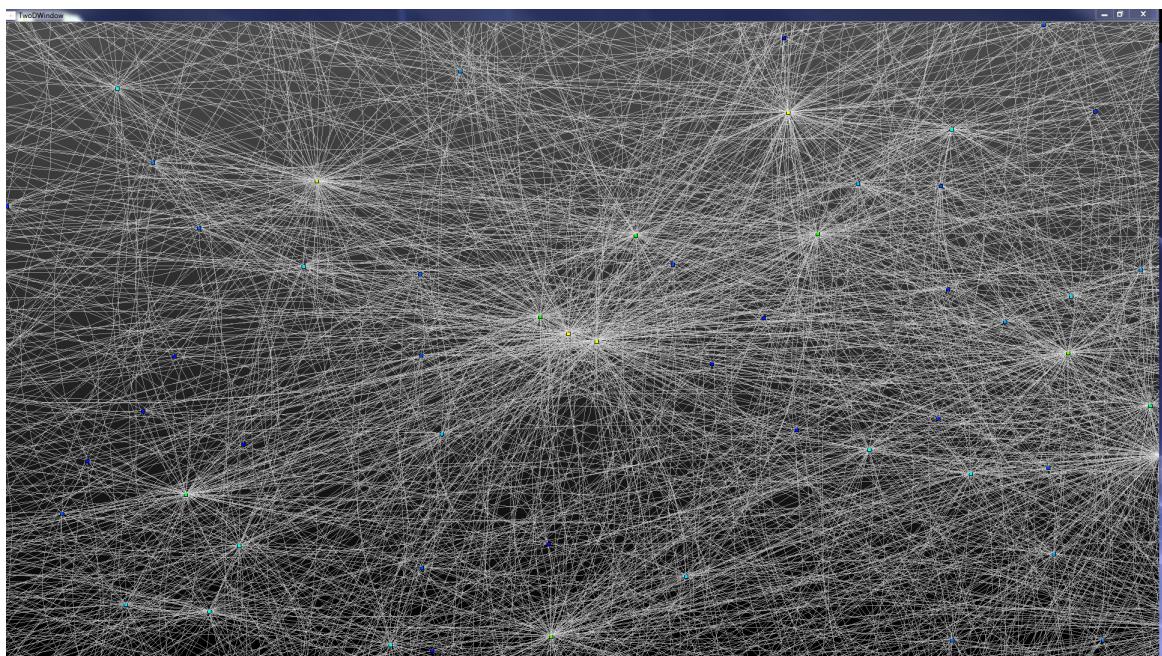


Figure 4.3. Same network as in 4.2 after zooming actions where preformed.

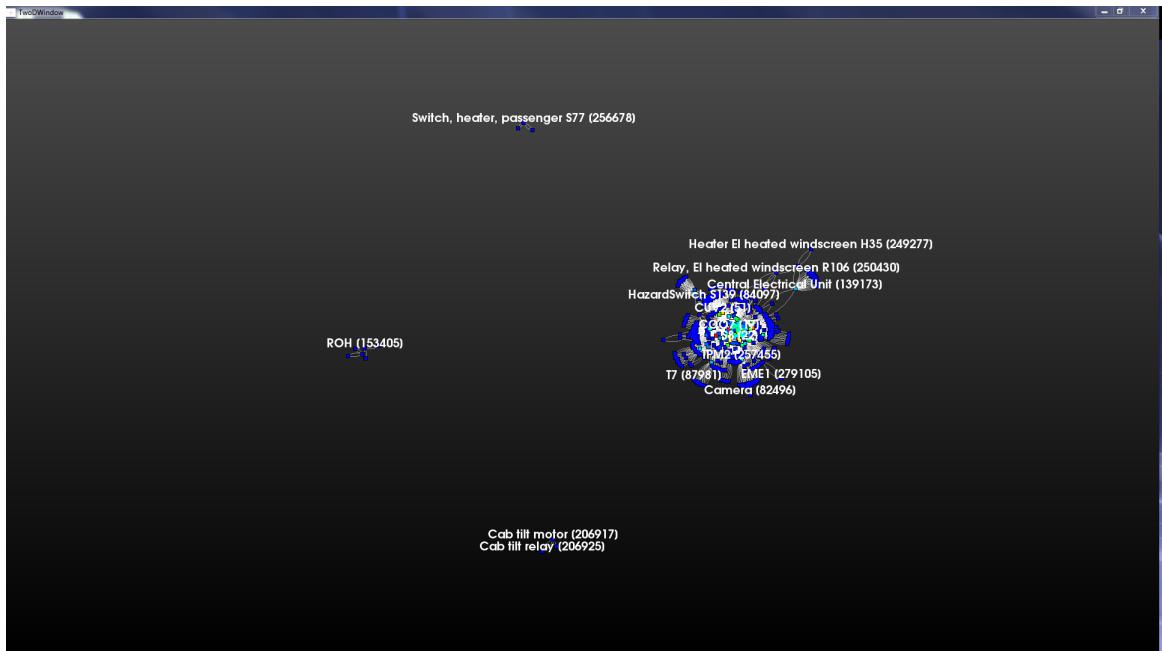


Figure 4.4. A labeled overview of a network were all ECUs was chosen.

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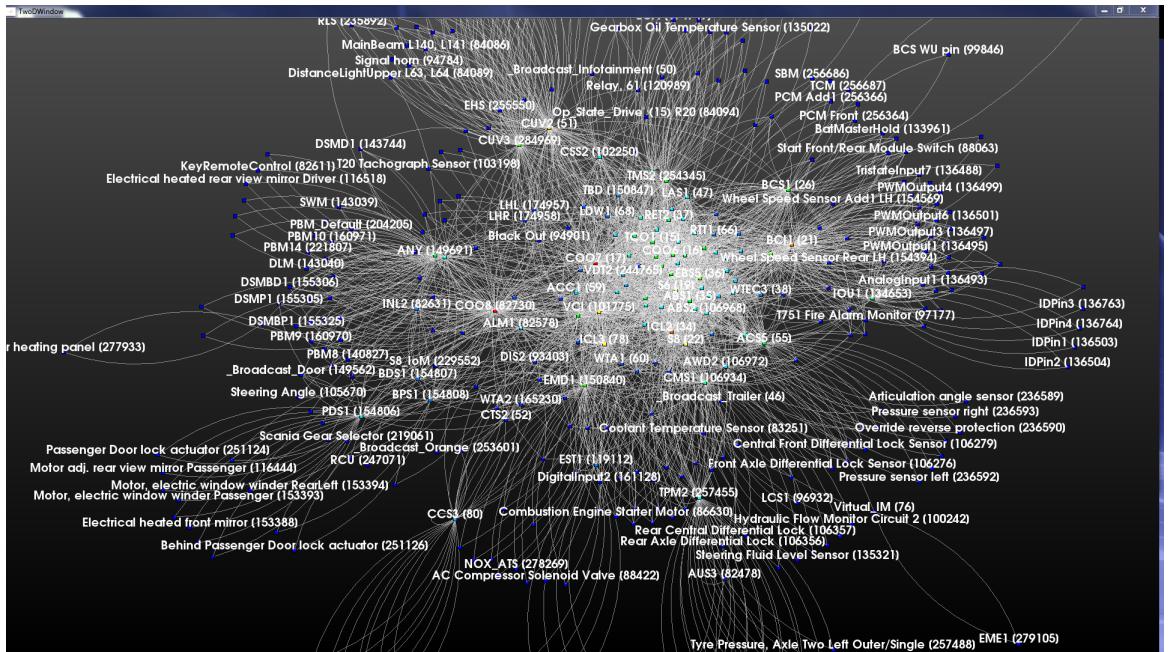


Figure 4.5. Same network as in 4.4 after zooming actions where preformed.

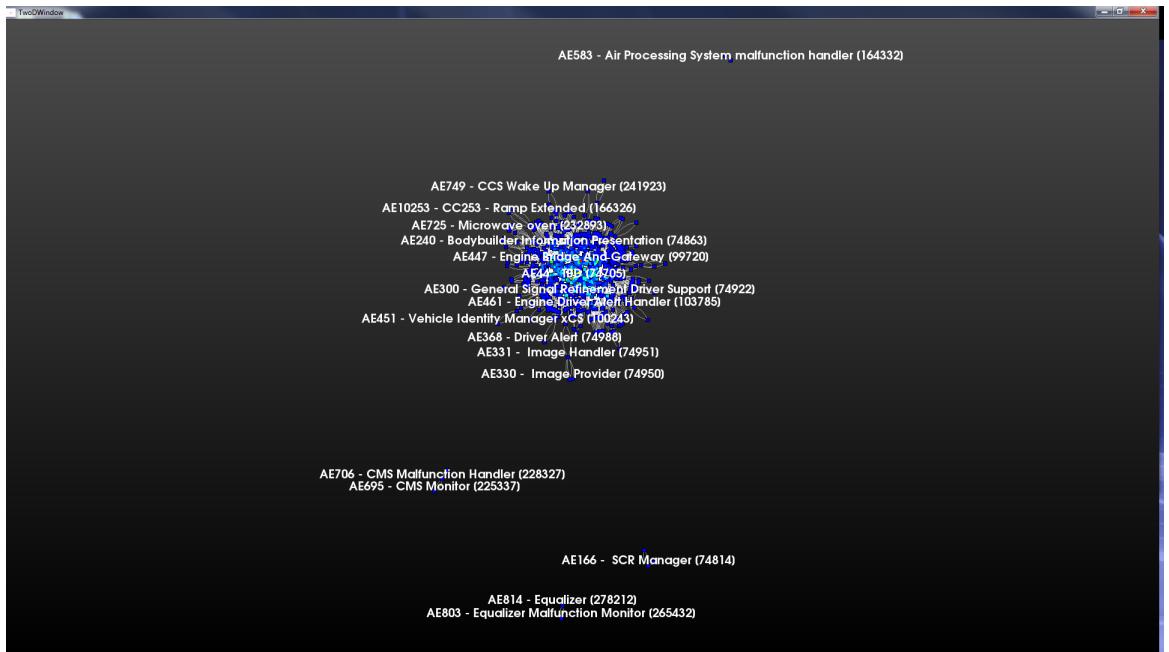


Figure 4.6. Showing data with labels enabled.

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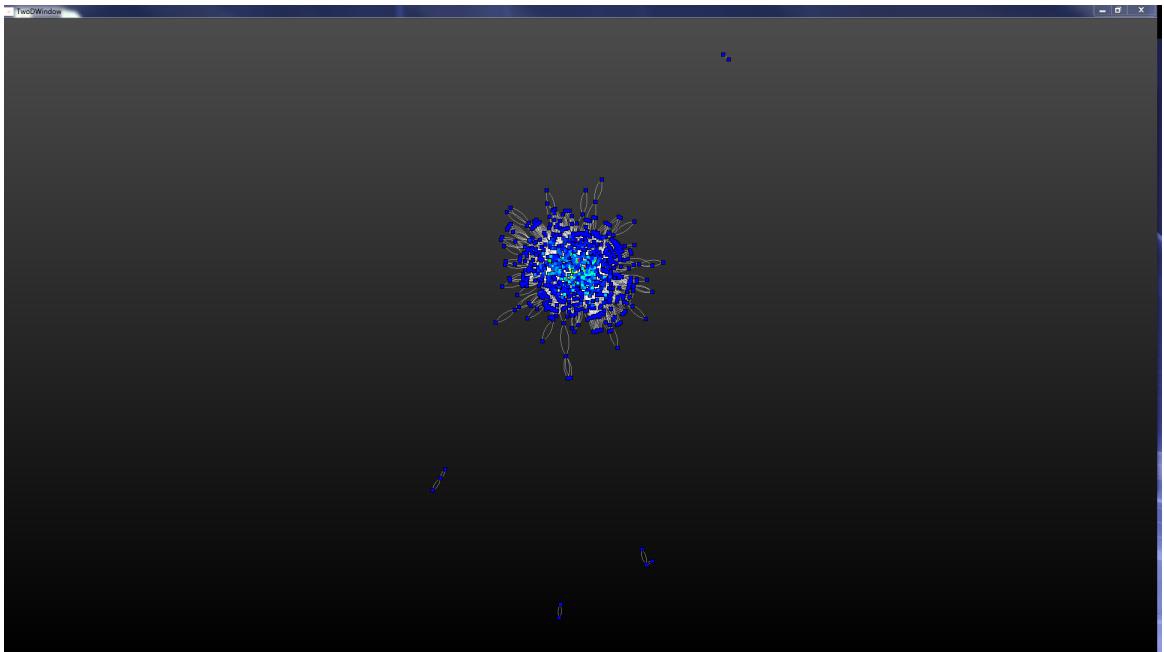


Figure 4.7. Showing same data as in picture 4.6 but with lables unenabled.

Labeling

As mentioned in section E.1.1, the VTK library displays labels according to their weights, the higher the weight the higher priority a given vertex label will have. This combined with that force-directed algorithm by nature is good at evenly spreading out vertices, label obscuration becomes lesser of a problem. An example of this is shown in figure 4.5 where a fairly large network is being displayed.

Of course this comes at a price. By allowing a prioritizing of which labels to display one is left with a loss of information, in this case a loss of labels. This can have a large effect on the outcome result when using this application. Depending on what tasks one wants to solve by using this visualization technique, important data may be missed and/or be more difficult to locate. It comes down to what data one is attempting to extract from the view. If for instance one is out to identify the vertices with a large number of connections and greater subnets this view might work terrific. On the other hand if one is to find a specific data part that may be smaller weighted this view can make it difficult and uneasy to use.

Navigation - Situational awareness

The effect on the situational awareness of a user in this view depends highly on what stage in a task the user is on and what type of task said user is performing. Because the view provides a highly zoomable network a user can with a far out zoomed view, combined with the labeling enabled, acquire a good overlook of a given network.

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Though when zooming in using this view there comes a point when some data are lost, there is only so much data that can fit on a screen at the same time. This can diminish the situational awareness for a user. Resulting in a loss of orientation, forcing a user to zoom out to try and see correlations from one part of the network to another. And they might even have a loss in orientation trying to get back to the same spot as before a given zooming action was made. One can draw the conclusion that this view provides a poor solution for problems having a need for global context and local details at the same time. Resulting in a user loosing orientation or specific information at different stages performing tasks.

In this view one have the option to navigate through the x- and y-axis or x-, y- and z-axis. This can be helpful when looking closer on how a subpart of a network joints with another. But one needs to be careful when going from two axes to three, when it can result in easier loss of orientation.

Two-dimensional view - BioFabric

For a view in the two dimensional space BioFabric was chosen to be used. BioFabric provides a non conventional approach to visualize data and have worthy attributes to be evaluated for visualization. Such as the layout algorithm for vertices and edges, the labelling of vertices and how one navigate the network. Figure 4.8 through Figure 4.10 shows examples when using the Biofabric view.

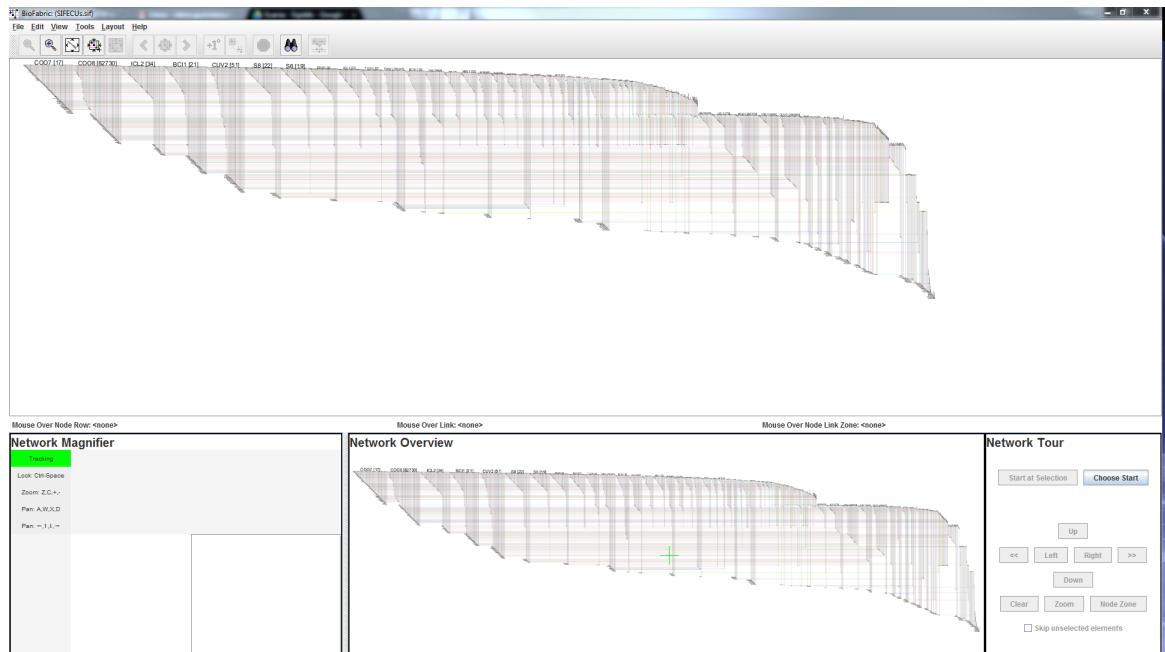


Figure 4.8. An overview of a network using the BioFabric view were all ECUs were chosen.

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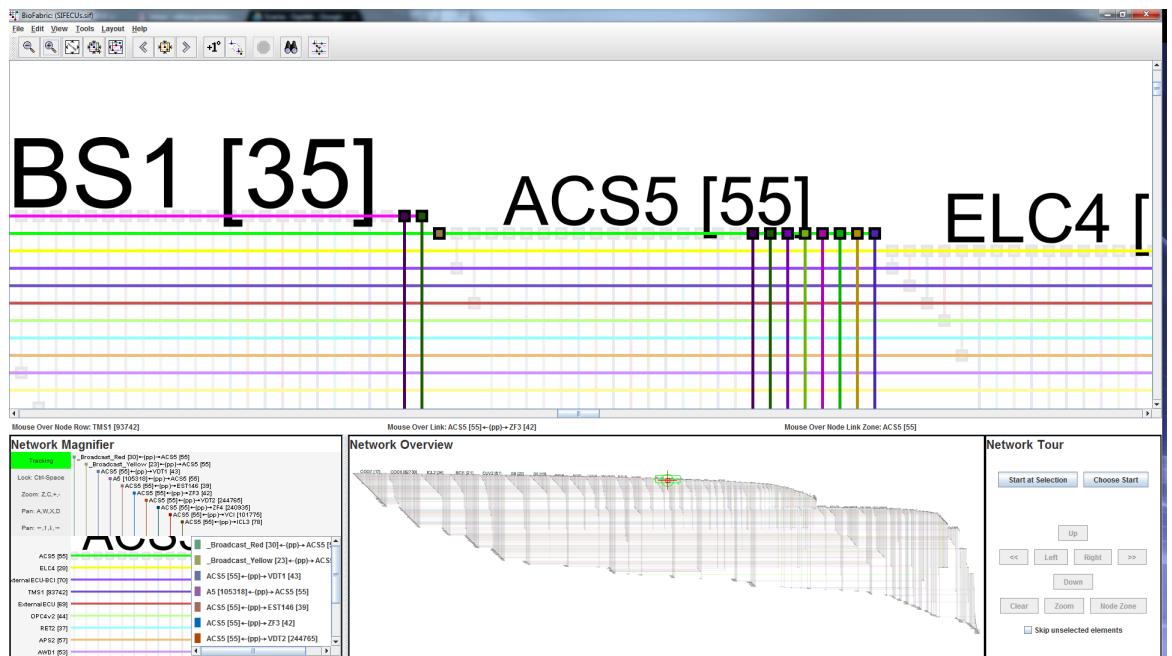


Figure 4.9. Same network as in 4.8 after zooming and selection actions were performed.

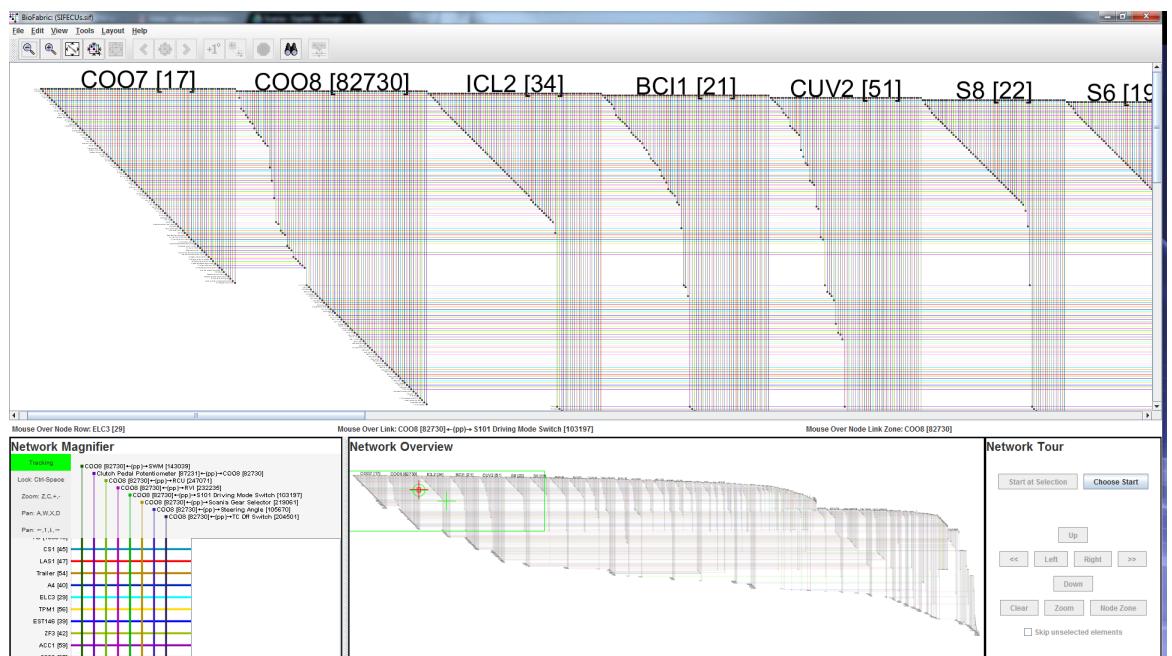


Figure 4.10. Another example of a selection within the network.

Labeling

BioFabric also uses a weighted labels solution. Here the vertices with highest degree, as in BioFabric becomes the horizontal lines at the top of the view, will be of the greatest size. In figure 4.8 one can see this clearly. The reason behind weighting labels becomes fairly obvious when one starts to think about how it would turn out if BioFabric would try to show all their labels of all vertices at the same size. There would be so many labels occluding each other that one would not be able to distinguish which label belongs to which vertex. Furthermore most part of the graph would have labels occluding each other making it difficult to see what label says what.

Navigation - Situational awareness

BioFabric have taken the approach to have more active views in their application at the same time. One main view, a view that works as an overview of the network, showing ones selection, and one that they call the network magnifier. The network magnifier displays a sub selection of the network made by the user (a selection) where the user can see all the labels and connections of vertices in their selection. Figure 4.10 shows all three views where an selection has been made.

Having these different views, especially the relation between the overview and network magnifier, tries to help toward good situational awareness. The user can go in more depth of a subpart of a network using the network magnifier while trying to maintain the global context by looking at the network overview and main view.

Having this setup one can argue that their approach goes toward data on demand. Requiring the user to have good knowledge about the network being displayed and have a good idea of the where and how the information searched is localized. Putting the pressure on the user to beforehand have a good situational awareness orientation, which is not always the case.

Three-dimensional view - GerbilSphere

The direction many new visualisation techniques are going in are attempting to take advantage of the extra space in the three-dimensional space. And thus it is of significance for this thesis to incorporate a tree-dimensional visualisation technique.

Many of these tree-dimensional techniques uses a sphere shape to visualize networks in/on. And common is that they use some sort of force-directed algorithm to layout the vertices and edges in this spherical space.

For this application tree-dimensional view a layout method that uses the spherical space was used. The view is based on GerbilSphere [48] where the vertices of a network are laid out on the surface of a sphere and one navigates from a point of view inside the sphere (though one can zoom out to see the sphere from the outside). For more details about GerbilSpheer see chapter 2 section 2.3.1. Figure 4.11 and 4.12 shows the view in use zoomed outside the sphere while Figure 4.13 shows the view from inside the sphere.

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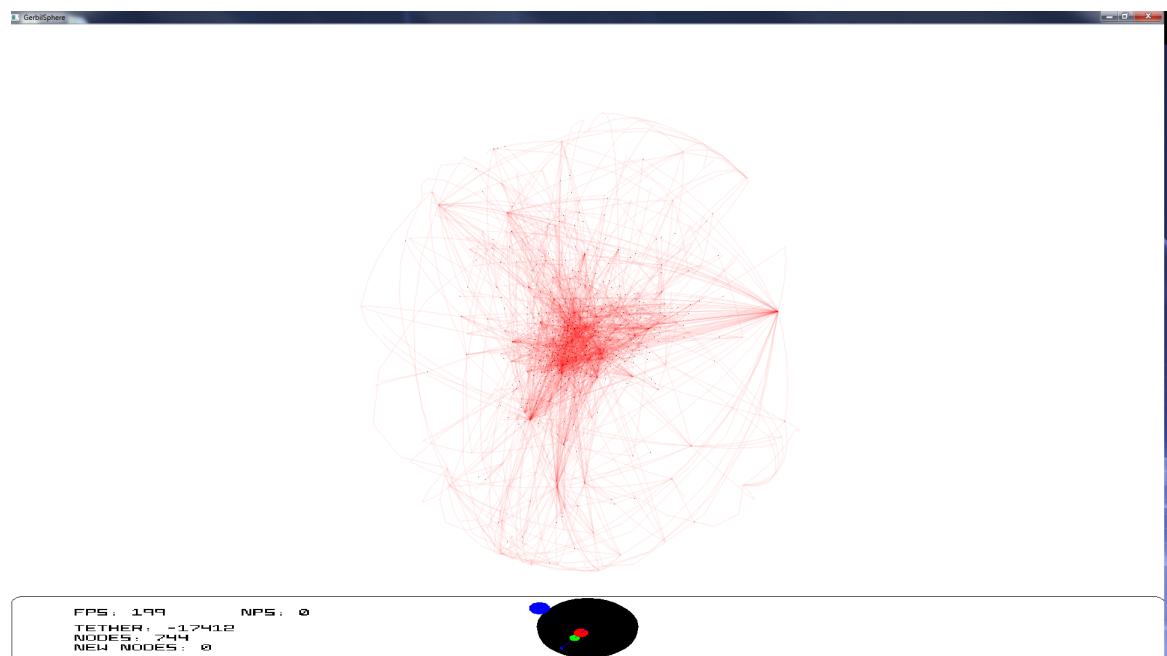


Figure 4.11. An overview with GirbilSphere of a network were all AEs were chosen.

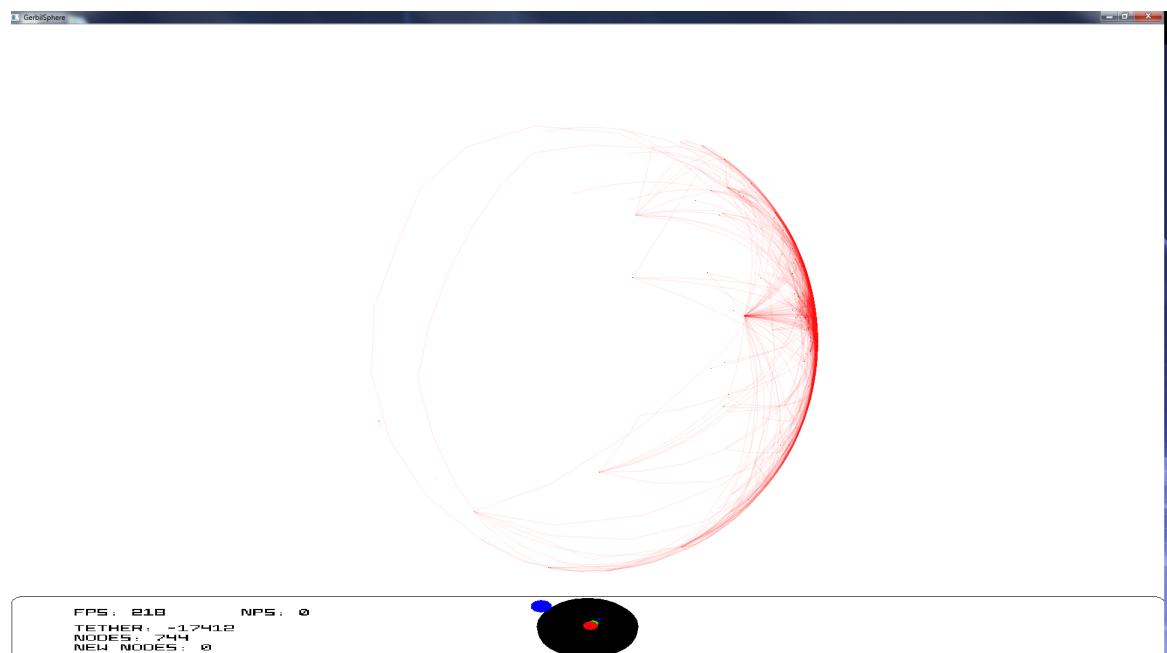


Figure 4.12. Same network as in figure 4.11 rotated ninety degrees.

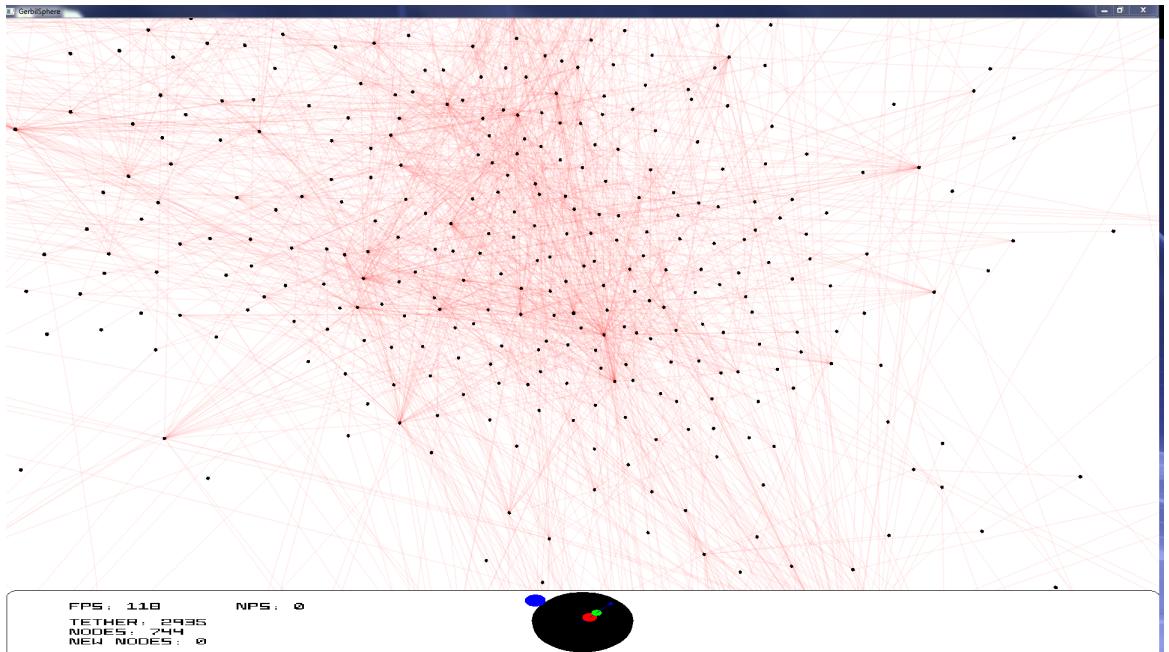


Figure 4.13. View of the network in figure 4.11 and 4.12 from inside of the sphere.

Labeling

The greatest advantage to this approach is the extra space one gains by using the hyperbolic space. So one might be enticed to draw the conclusion that this is good, now we have more space for both labels and vertices and we should be able to lay out our data points in a satisfactory way. While the fact about more space might be true one will soon see that obscuration of data becomes a much more severe problem fast. Now labels and vertices can be obscuring each other in a wider range, laying in front or behind each other etc.

Presumably GerbilSphereAlpha have in an attempt to work around obscuration taken an information on demand approach. Choosing not to display labels on the sphere and instead have a separate window that displays information about a vertice when that specific vertice is chosen by the user. This results in a lower risk of obscuration of labels but at the same time demands more from the user. More in the sense that the user needs to have a greater knowledge about the network and its structure before hand to be able to navigate and retrieve desirable data from the visualized network. It also causes a delay in identifying vertices when a user needs to click a specific vertex to get information about it. Finally a user might loose orientation if the user forgets which vertice the user clicked to get information about in previous steps.

4.2. APPLICATION

Navigation - Situational awareness

It has already been indicated that drawing networks in the hyperbolic space offers more space compared to the 2D-space, which is an positive thing. Though this comes with a price, which has to be paid by the end user with a worsened sense of situational awareness. This because of the fact that with more space and axis to navigate through results in a harder time to keep ones orientation. For example a user might take a too large of a step in the sphere, loosing track of where the user came from which might result in forcing the user to go further back or even start over in the task currently being performed.

This becomes a problematic downside when going from a two-dimensional - to a three-dimensional space view, and needs to be considered and handled. GerbilSphereAlpha tries to solve this by using a developed navigation feature that is displayed at the bottom of the sphere. See [48] for further details.

This navigation feature becomes a good first step in trying to help the situational awareness of a user. Though it is not too intuitive to use at first and take some practice to become familiar with. This and the fact that if one goes over to the hyperbolic space they do this because of a need for more space, larger networks to display, results here in large number of small vertices being displayed. Trying to use this to be able to find specific vertices can become unfeasible. Worth mentioning also is that while the hyperbolic space provide more space and is good for larger networks it can have an negative effect if used on smaller networks. Resulting in a small number of vertices on a greater surface, making long distances between vertices and making it hard to identify edges etc.

In the next chapter we will discuss and try to draw conclusions from the results given in this chapter.

Chapter 5

Discussion and Conclusions

In this chapter we will try to give an account of plausible conclusions from the studies and results in previous chapters. We will try to go through and answer the question this thesis revolves around, *Which type of visualisation technique is best suited to visualize big and complex networks?*

5.1 Which type of visualisation technique is then best suited to visualize big and complex networks?

One thing that becomes fairly clear when one reads the research from this thesis is that answering this question is not an easy task. Though this thesis is nowhere near to go through all visualisation techniques that exists, the evidence from this thesis points toward that there is no one correct solution answering this question. It points more to that there are no one best choice of technique to display a complex network that is independent of the kind of and form of data one uses.

It boils down to that when one wants to visualize a complex network one must consider all the features and demands that the given network needs. Do we need more space for the data? A clean and clear structural way of traversing the network? How does the need for labeling our vertices look? Do we need to find out how sub-networks looks like or get more information about specific vertices and connections? And so on. There exists an indefinite number of different complex networks and one can not find a generalisation saying that one visualisation technique satisfies all the needs of all networks and displays them in an optimal way.

Instead one needs to tailor a specified solution for a specific network and the accompanied requirements of visualisation with it. One needs to become very familiar with the data that is going to be displayed along with getting an excellent knowledge of the visualisation needs for the specific application. Then use this knowledge to develop features that comply with these needs. Features such as complex filters that trims the network to specific data, search functions, highlights etc. It all boils down too the needs of the specific application.

CHAPTER 5. DISCUSSION AND CONCLUSIONS

For further research one could be interested in see how these different visualisation approaches would cooperate. To see how one users situational awareness is affected by navigating through one view and seeing at the same time that change in the different views. How it would affect if one take a sub-selection of a network in one view and see that same sub-selection marked in the other views simultaneously.

Appendix A

GraphElement

```
using System;
using System.Collections.Generic;
using System.Linq;
using System.Text;
using System.Threading.Tasks;

public class GraphElement : IEquatable<GraphElement>
{
    /*
     * id that is a sequential id, 0,1,2... and so on
     * Needed because some datastructures requers the
     * elements to have ids on this form.
     */
    private int internalID;
    //Actual id taken from database.
    private int elementID;

    //Constructor that sets the name and internal id.
    public GraphElement(string name, int id)
    {
        this.name = name;
        this.elementID = id;
    }

    public override int GetHashCode()
    {
        return elementID.GetHashCode();
    }

    //Return name of GraphElement.
    public string GetName()
    {
```

APPENDIX A. GRAPHELEMENT

```
        return name;
    }

    //Return internal sequential id of GraphElement.
    public int GetInternalID()
    {
        return internalID;
    }

    //Return internal id of GraphElement.
    public int GetElementID()
    {
        return elementID;
    }

    //Set the internal id of GraphElement.
    public void SetInternalID(int newID)
    {
        internalID = newID;
    }

    /*
     * Methods used for comparing two GraphElements
     */
    public bool Equals(GraphElement element)
    {
        return elementID == element.elementID;
    }

    public override bool Equals(object obj)
    {
        GraphElement element = (GraphElement)obj;
        return elementID == element.elementID;
    }
}
```

Appendix B

Parsers

```
using System;
using System.Collections.Generic;
using System.Linq;
using System.Text;
using System.Threading.Tasks;
using System.IO;

namespace GraphParser
{
    public class graph
    {
        //Dictionary for VTK evaluation
        public Dictionary<int,LinkedList<int>> vtkDic;

        //Method to read a graph from given file, path.
        private Dictionary<int, LinkedList<int>> readGraph(String path)
        {
            string edge;
            vtkDic = new Dictionary<int, LinkedList<int>>();
            try
            {
                using (StreamReader sr = new StreamReader(path))
                {
                    int? nrNodes = convertString(sr.ReadLine());
                    for (int i = 0; i < nrNodes; i++)
                    {
                        int id = i + 1;
                        vtkDic.Add(id, new LinkedList<int>());
                    }

                    while ((edge = sr.ReadLine()) != null)
                    {
                        string[] edges = edge.Split(',');
                        int? source;
```

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```

        int? sink;
        if ((source = convertString(edges[0])) != null &&
            (sink = convertString(edges[1])) != null)
        {
            LinkedList<int> getEdges =
                vtkDic[(int)source];
            getEdges.AddLast((int)sink);
            vtkDic[(int)source] = getEdges;
        }
    }
}
catch(Exception e)
{
    Console.WriteLine("File could not be read:");
    Console.WriteLine(e.Message);
}
return vtkDic;
}

//Helpmethod to convert a string to an int
private int? convertString(string obj)
{
    int? numVal;
    try
    {
        numVal = Convert.ToInt32(obj);
    }
    catch (FormatException e)
    {
        Console.WriteLine("Input string is not a sequence of
            digits.");
        numVal = null;
    }
    catch (OverflowException e)
    {
        Console.WriteLine("The number cannot fit in an Int32.");
        numVal = null;
    }
    return numVal;
}
//Get method for dictionary.
public Dictionary<int,LinkedList<int>> dictionary
{
    get
    {
        return vtkDic;
    }
}

```

```

//Get method for size of dictionary.
    public int size
    {
        get
        {
            return vtkDic.Keys.Count;
        }
    }

//Method for use at evaluation of libraries. Get a test graph of size
//of vertices 50, 100, 500 or 1000.
    public Dictionary<int, LinkedList<int>> getGraph(int size)
    {
        switch (size)
        {
            case 50:
                return
                    readGraph("C:/Users/VGUXT8/Documents/VisualizeSystem/Performance
                    review of libraries/Data/50_Nodes.txt");
            case 100:
                return
                    readGraph("C:/Users/VGUXT8/Documents/VisualizeSystem/Performance
                    review of libraries/Data/100_Nodes.txt");
            case 500:
                return
                    readGraph("C:/Users/VGUXT8/Documents/VisualizeSystem/Performance
                    review of libraries/Data/500_Nodes.txt");
            case 1000:
                return
                    readGraph("C:/Users/VGUXT8/Documents/VisualizeSystem/Performance
                    review of libraries/Data/1000_Nodes.txt");
            default:
                return null;
        }
    }

//GML Parser
    public void To_graphMl(StreamWriter writer,
        Dictionary<GraphElement, LinkedList<GraphElement>> GraphData)
    {
        writer.WriteLine("<?xml version=\"1.0\" encoding=\"UTF-8\"?>");
        writer.WriteLine("<graphml
            xmlns=\"http://graphml.graphdrawing.org/xmlns\"");
        writer.WriteLine("xmlns:xsi=\"http://www.w3.org/2001/XMLSchema-instance\"");
        writer.WriteLine("xsi:schemaLocation=\"http://graphml.graphdrawing.org/xmlns\"");

```

APPENDIX B. PARSERS

```

writer.WriteLine(
    "http://graphml.graphdrawing.org/xmlns/1.0/graphml.xsd\">\"");
writer.WriteLine(" <graph id=\"G\""
    "edgedefault=\"undirected\">");

foreach (var key in GraphData.Keys)
{
    writer.WriteLine("  <node id=\"" + key.GetInternalID() +
        "\"/>");
}
foreach (var key in GraphData.Keys)
{
    foreach (var neighbour in GraphData[key])
    {
        writer.WriteLine("  <edge source=\"" + 
            key.GetInternalID() + "\" target=\"" + 
            neighbour.GetInternalID() + "\"/>");
    }
}

writer.WriteLine(" </graph>");
writer.WriteLine("</graphml>");
writer.Close();
}

//GerbilSphereAlpha parser.
public void To_Pajek(StreamWriter writer, Dictionary<GraphElement,
    LinkedList<GraphElement>> GraphData)
{
    writer.WriteLine("*Vertices " + GraphData.Keys.Count);
    foreach(var node in GraphData.Keys)
    {
        writer.WriteLine(" " + (node.GetInternalID()+1) + " " + "\\"+
            node.GetName() + "\\"");
    }
    writer.WriteLine("*Edges");
    foreach (var node in GraphData.Keys)
    {
        foreach(var to in GraphData[node]) {
            writer.WriteLine((node.GetInternalID() + 1) + " " +
                (to.GetInternalID() + 1) + " 1");
        }
    }
    writer.WriteLine();
    writer.Close();
}

//BioFabric Parser.

```

```
public void To_SIF(StreamWriter writer, Dictionary<GraphElement,
    LinkedList<GraphElement>> GraphData)
{
    foreach (var node in GraphData.Keys)
    {
        foreach (var to in GraphData[node])
        {
            string nodeName =
                node.GetName().Replace(System.Environment.NewLine,
                string.Empty);
            string toName =
                to.GetName().Replace(System.Environment.NewLine,
                string.Empty);
            writer.WriteLine(nodeName + "\tpp\t" + toName);
        }
    }
    writer.WriteLine();
    writer.Close();
}
}
```

Appendix C

Test data

G50: 50 vertices, 592 edges. 

G100: 100 vertices, 3941 edges. 

G500: 500 vertices, 99641 edges. 

G1000: 1000 vertices, 399969 edges. 

Appendix D

Library evaluation

D.0.1 Libraries of interest

For the considered libraries of use for the implementation, we classify them to one of four different categories. Open-source libraries, closed-source libraries, 3D-approaches and non-conventional graph visualisation approaches.

Open-source libraries

QuickGraph

QuickGraph[9] is a library containing generic graph data structures and algorithms for a range of graph problems, developed for .Net[55] use. Such as classical problems like maximum flow, topological sort, shortest path, depth search, etc.

Supports:[8]

1. Graph data structures
 - 1.1. Directed graph
 - 1.2. Undirected graph
 - 1.3. Dense graph
 - 1.4. Sparse graph
2. Graph computational Algorithms
 - 2.1. Topological sort
 - 2.2. Strongly connected components
 - 2.3. Minimum spanning tree

Notes:

QuickGraph does not support an option to use an own solution for visualisation of graphs but points to the layout library Graphviz[22] that they claim works well with their data structures[10]. This applies to layout algorithms as well.

Graphviz

Graphviz[22] - graph visualization software. Graphviz provides different layout algorithms and take descriptions of graphs in an text language as input. Normal usage with Graphviz is by using DOT (graph description language)[51].

It can be used with QuickGraph as a C# wrapper. Other wrappers for C# and .Net one could use are graphviznet[6] and graphviz4net[7].

Supports:

1. Layout algorithms[22]
 - 1.1. Dot
 - 1.2. Neato
 - 1.3. Fdp
 - 1.4. Sfdp
 - 1.5. Twopi
 - 1.6. Circo
 - 1.7. Osage

GraphX

GraphX is an advanced open-source .Net library for graph visualization with capabilities to rend large graphs with large amount of vertices and edges which depends on the QuickGraph library[42]. It also uses partial code from Graph#[21], WPFExtensions[12], NodeXL[38] and Extended WPF Toolkit[62], which are open-source projects.

It is based on WPF for rendering graphs and can be seen as the successor too Graph#. GraphX is the new Apache Sparks API for graphs and graph-parallel computation. It introduces a new API that operates on both tables and graphs and incorporate this API as a library using graph parallel techniques to be as fast as specialize systems (such as GraphLab, Giraph and Pregel). By embedding this graph-parallel model in Spark it enables GraphX to integrate easily with RDDS (Resilient Distributed Datasets: A Fault-Tolerant Abstraction for In-Memory Cluster Computing) and perform data parallel operation while also enabling the speed of specialize graph systems[63].

Supports:[42]

1. Layout algorithms
 - 1.1. BoundedFR (Fruchterman Reingold).
 - 1.2. Circular.
 - 1.3. CompoundFDP.
 - 1.4. EfficientSugiyama.
 - 1.5. Sugiyama.
 - 1.6. FR.
 - 1.7. ISOM.
 - 1.8. KK (Kamanda and Kawai).
 - 1.9. LinLog.
 - 1.10. Tree.
2. Possibility to implement an own layout algorithm (external layout algorithm).
3. Visual control
 - 3.1. Delete animation of vertices and edges.
 - 3.2. Mouse over control animation
 - 3.3. Custom animations
 - 3.4. Highlighting of vertices and edges.
 - 3.5. Zoom control.
 - 3.6. Area selection of vertices.
 - 3.7. Area zooming and smooth animations.

Notes:

There is no documentation implemented functions for nested graphs or how one go about doing this. And by nested graph we mean a graph which vertices can contain subgraphs within themselves.

MSAGL

MSAGL[46], Microsoft Automatic Graph Layout, is a .Net tool for graph layout and viewing. It is built on the Sugiyama scheme[54] that produce hierarchical layouts. Where the vertices are drawn in horizontal layers and the edges often drawn in a downward fashion between vertices. MSAGL contains its own layout engine.

Supports:[46]

1. Layout algorithms.
 - 1.1. Sugiyama.
2. Editable layout after initial layout.
3. Navigation of graph
 - 3.1. Zoom.
 - 3.2. Pan.
 - 3.3. Search and focus function.
4. Visual control.
 - 4.1. Highlighting of vertices.
 - 4.2. Zoom.

Closed-source libraries

yFiles(yWorks)

yFiles[67] provides data structures and algorithms for graph handling. Including automatically layouts for graphs and visualization controls for those graphs. yFiles are supported for different platforms, including .Net where one can either use a library for Windows Forms[35], WPF[36] or Silverlight[49].

Supports:[66][65][64]

1. Layout algorithms
 - 1.1. Circular layout.
 - 1.2. Hierarchical layout.
 - 1.3. Organic layout.
 - 1.4. Orthogonal layout.
 - 1.5. Tree layout.
 - 1.6. Incremental layout.
2. Edge routing algorithms.
 - 2.1. Organic routing.
 - 2.2. Orthogonal routing.
3. Visual control.

3.1. Highlighting controls.

3.2. Zoom.

3.3. Smooth change animations.

Notes:

yFiles also supports incremental layout, meaning that when a graph needs to be updated (addition/removal of vertices or edges) the whole graph is not re-computed but tries to maintain as much as possible of the same layout as before. Also yFiles tries to support nested graphs, but has some restraints on the data to be able to use it. Their function is called collapsible tree, which requires the data to be able to be structured as a tree.

An comparison of given libraries.

Attribute matrix:

The following matrix, Figure D.1, lists important functionality one looks for when considering a programming library for implementing visualisation methods. The matrix gives an overview of what the different libraries supports from the start. This matrix helps as a basis when selecting libraries for the implementation.

<u>Library</u>	<u>Own layout algorithm</u>	<u>Documentation</u>	<u>External layout algorithm</u>	<u>Zoom functionalit</u>	<u>Highlight functionalit</u>	<u>Nested Graph support</u>	<u>User editabile graphs</u>
QuickGraph	<input type="checkbox"/>	Good	<input type="checkbox"/>				
yFiles	<input checked="" type="checkbox"/>	Good	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>
GraphX	<input checked="" type="checkbox"/>	Good	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>
MSGAL	<input type="checkbox"/>	Good	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>
GraphViz	<input type="checkbox"/>	Decent	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>

Figure D.1. Attribute matrix

3D approaches

So far we have only looked at libraries that utilize the two-dimensional space, next we are going to look at some for the three-dimensional space.

Libraries

For developing advanced 3D graphics the two most common approaches is to use

APPENDIX D. LIBRARY EVALUATION

either OpenGL[41] or Direct3D[31]. To use OpenGL in windows one has a few options, one can for example use OpenTK that wraps OpenGL, OpenCL[39] and OpenAL[40].

Direct3D is part of the DirectX API that uses hardware acceleration (if available on the graphics card).

Differences between OpenGL and Direct3D

OpenGL is being developed largely by a consortium of different parties and follows a largely open standard. While Direct3D are being developed and maintained by Microsoft and is completely proprietary in its implementation. Resulting in a big platform difference, where OpenGL is supported on a wide range of platforms and languages, while Direct3D is bound to Microsoft Windows systems.

At last there is the different methods used to introduce new hardware and features. OpenGL do this by allowing hardware manufactures to be able to implement special functions, called extensions that give immediate access to features of new hardware. As for Direct3D, Microsoft needs to process theses features and then release access to these in forms of new functions. Here OpenGL allows new features to be accessible quicker then Direct3D, though reduces the overall compatibility of a program using the extensions. And the other way around, Direct3D takes longer to give access to the new features but compatibility across different systems is being maintained.

The aspect of hardware managing differs in these two libraries. OpenGL hides the hardware and works so that the implementation handles hardware resources, users of OpenGL uses functions for drawing which relies on drivers to directly access the hardware. Direct3D on the other hand lets the application handle the hardware resources. The trade off become that with OpenGL it becomes easier to write applications but unable to see the status of hardware resources and thus must hope that the implementation uses the resources in a way that suits your application. While with Direct3D the writing of the application may be more complex but have the possibility to use hardware resources in the most efficient way for the application.[59]

Both these differs a bit form previous discussed libraries in the sense that there are no (known) support for graph visualization. So for instance no layout algorithms for graphs like force directed or data structures to represent a graph. This implies that all that has to be implemented from scratch, taking more time but open ups for less restrictions on what one can do.

VTK

VTK (Visualization Toolkit)[57] is an open-source software system for 3D computer graphics, image processing and visualization. At its core VTK is implemented as a C++ toolkit and it supports parallel processing which help in performance. VTK

is a popular library when it comes to visualize scientific data, which is often big and complex.

There are a number of wrapper languages making it possible to addition to C++ use VTK through for instance Python, Java and .NET.

Non conventional graph visualization approaches

When it comes to the visualisation techniques like BioFabric, Hive Plots and Treemap (as described in chapter 2) there are few libraries that support this compared to the amount of libraries there are to visualize the classical node/edge graphs. Here we go through these approaches and give an account to which ways one can take to use these.

BioFabric:

BioFabric has one release which is an open-source Java application with some documentation that can be found at[3]. Though BioFabric is built on a relatively easy and intuitive algorithm, one could take the option of implementing an own version. Having their own customized features that suits one's purpose.

Hive Plots:

For hive plots there are some choices, one used is a Java based library[2]. There are also libraries for R[45], HiveR[1], that supports hive plots in the two dimensional and three dimensional space. The framework D3.JS[14] is an other option that is a JavaScript to create hive plots. And pyveplot[43] that is a library for hiveplots in Python[44].

Tree Map:

As for Treemaps there are some choices as well. For .Net, which is this thesis working environment, there is the WPF Treemaps & SquarifiedTreeMaps control library[11], though it has poor documentation. Another alternative is the .NET Treemap Control library[15]. Here again the problem lies in little documentation and hard to get information about the library where this was part of an old Microsoft research project called Netscan.

GerbilSphere:

GerbilSphere visualize graphs by projecting nodes and edges to the surface of a sphere, defined as an inner sphere 2D system. It differs from other graph visualisation techniques that also uses spheres in the way that in GerbilSphere the observers point of view is from inside the sphere.

GerbilSphere is an open source project. No API is available, though good documentation is presented within the code.

Supports:[48]

1. Specialised layout algorithm that is based on force-directed algorithms.
 - 1.1. Static layout when adding/removing nodes.
2. Labelling.
3. Menus when choosing specific nodes.
4. Visual control.
 - 4.1. Zoom.
 - 4.2. Paning.
 - 4.3. Fisheye view.
 - 4.4. Variablezoom.

Notes:

While GerbilSphere does not support nested graphs this becomes of less interest when the whole graph is being visualized.

D.0.2 Library selection for evaluation

From the matrix in figure D.1 one conclude that GraphX and yFiles are two possible candidates for usable libraries. They both support more functionality than QuickGraph, MSGAL and GraphViz. Therefore they will be included in the evaluation.

Needed is also an option for implementing three dimensional views. For this purpose we include the VTK library when it has support for graph visualisation.

D.0.3 Test set up

The libraries have been tested on two different aspects, rendering speed and smoothness. Rendering speed is measured as the time it takes a specific library to draw up a given graph. As for smoothness the frames per second (fps) rate has been measured during navigation through corresponding graphs. Navigation actions such as panning and zooming.

Data

The data used for these tests has been produced with the use of Gephi[19]. Four different graphs were created for testing:

- 50 vertices with 592 edges. Referred as G50.
- 100 vertices with 3941 edges. Referred as G100.
- 500 vertices with 99641 edges. Referred as G500.
- 1000 vertices with 399969 edges. Referred as G1000.

Given graphs can be found in appendix C.

Hardware

The evaluations were run on the same computer for each graph and library with the following hardware:

Processor:	Intel(R) Core(TM) i5-3470 CPU @ 3.20GHz
Video Card:	Intel(R) HD Graphics. 64 MB Dedicated Memory, 1.7 GB Total Memory
Memory:	6.1 GB
Operating System:	Microsoft Windows 7 Enterprise Edition Service Pack 1 (build 7601), 64-bit

D.0.4 Results from library tests

Two kinds of users need to be considered when talking about the results from the library evaluations. First take the users that will indirectly use the libraries by using the application built using these libraries. We will call these users end users. Second is the kind of user that will use these libraries to build an application for visualisation. We call these users developer users.

The needs one have on the libraries differs depending on what kind of user one are. For an end user the speed and smoothness are the two things that shows most. Developer users must also take into consideration what the different libraries supports and not.

Speed

Each graph have been drawn ten times and the arithmetic mean value of the time has been calculated and given as result. Time is displayed on the form of minutes:seconds.

Table D.1. Speed results

	G50	G100	G500	G1000
GraphX	00:00.51461281	00:07.41482771	22:33.4573175	Out of memory
VTK	00:00.01546258	00:00.04138581	00:00.88301525	00:03.53977976
yFiles	00:00.54974544	00:01.68249026	00:49.60542746	12:11.535764772

APPENDIX D. LIBRARY EVALUATION

Here one can see that the VTK library is far superior to the other libraries, especially on the larger sized graphs. On the smallest graphs the difference are not as significant. For the end users the difference on drawing speed on graphs of size with 50 nodes would not be to notable. Though the developer users might wanna take this into consideration. On larger than 50 nodes graphs the difference between these libraries shows fairly clear. GraphX drawing speed decreases rapidly and are not able to draw graphs with a size of 1000 vertices with the hardware used. yFiles do manage to draw this graph, though it took over 12 minutes compared to VTKs 3 seconds.

Smoothness - FPS

There are three fps measurements for each library were panning actions was being performed for each one. One zoomed out far away, giving an overview of the graph (Z1), one zoomed in half way to the centre of the graph (Z2) and a third were you are zoomed far in to the graph, being able to distinguish between vertices (Z3).

Table D.2. GraphX

	Z1	Z2	Z3
G50	17 fps	23 fps	35 fps
G100	1 fps	3 fps	5 fps
G500	Undetectable	Undetectable	Undetectable
G1000	Non-executable	Non-executable	Non-executable

Table D.3. VTK

	Z1	Z2	Z3
G50	1000 fps	1000 fps	1000 fps
G100	500 fps	500 fps	500 fps
G500	35 fps	11 fps	3 fps
G1000	11 fps	7 fps	2 fps

Table D.4. yFiles

	Z1	Z2	Z3
G50	22 fps	20 fps	25 fps
G100	2 fps	3 fps	5 fps
G500	Undetectable	Undetectable	Undetectable
G1000	Undetectable	Undetectable	2 fps

From theese tables one can see that GraphX and yFiles perform close to equal, though VTK outperforms both these libraries with quite a big margin. VTK is also the only one that could detect a readable FPS value when maneuvering the largest sized graph. Both GraphX and yFiles displays a better smoothness (higher FPS) at a deeper zoom, which can at first seem a bit strange. The reason for this is that once you are zoomed far enough in the graph, you come to a point where there is less nodes and edges to display on the screen then previous zoom where the low FPS value starts to increase after this point.

To take into consideration

One thing that becomes overlooked when talking about these different libraries is how one wants to draw graphs. For instance if one wants small or big representation of nodes. If one is planing on just drawing smaller graphs with big nodes one might be fine using yFiles or GraphX. Though if one wants to draw graphs of the larger kind one might be better suited with the VTK library. These aspects of course affect the speed and smoothness when using these libraries. In this study the basic common configuration for each library has been used.

For the end user the speed and smoothness is what becomes most important, that is what they see when using an application. The developer user must of course take this in to account when developing an application. More than that the developer user must also take in to consideration what different features different libraries supports.

Appendix E

Implementation details.

E.1 Views

E.1.1 Force-directed(FD) based view

This view was implemented using the VTK library for C# on the basis from the evaluation done in section 4.1.

In this view the user of the application can choose between showing labels and not. The labelling of the vertices in this view are weighted with a weight based on their degree. This in such a way that the higher the degree of a vertice, the higher weight that vertices label will be given. Based on the vertices weights, a priority of which labels to be displayed at a certain point in the network are made. Giving vertices with higher degree higher priority. This also results in that depending on which zoom level in a network one are, different labels will be prioritised.

When it comes to the space this view is using, it is actually up to the user to chose. By holding down shift when navigating an network in this view the z-axle becomes fixed, making it appear as a two dimensional view. Otherwise it works in the three dimensional space, where one can navigate through the x-, y- and z-axes. This is unique to this view, the next two views works in the two- or three-dimensional space.

E.1.2 Two-dimensional view - BioFabric

BioFabric is an open-source Java application which makes it applicable to use for this thesis. Though some changes was needed to be done for it to work with our implementation. Changes concerning the code that conducts the where and how the input of data for the application were made, changes so that BioFabric becomes compatible with our application. Also additions concerning making sure that the data converts to the correct form for BioFabric to handle after data had been input where needed. More about this in E.2.3.

E.1.3 Three-dimensional view - GerbilSphere

GerbilSphere is an open source application developed in C++. Again the data handling needs to be modified to match the form of data input GerbilSphere uses, again more about this in E.2.3.

GerbilSphere handles labels a bit differently than previous views. Instead of trying to place visible labels in the spherical space they have taken an information on demand approach, making it up to the user to prompt for specific information at need. This by having a secondary window up that keeps track of actions made in the sphere. As when clicking on a specific vertex getting the information (the label) about that vertex showing in this window.

E.2 Data representation

In this section we will go over how we have chosen to represent our data that we want to visualise.

E.2.1 GraphElement

To be able to represent data in the earlier stages, before displaying any views, a small class called GraphElement was created. This represents, as its name suggests, an element of a graph such as a vertex or an edge.

The class holds parameters about the name and ids and implements functions making it possible to distinguish between two different GraphElements. See Appendix A for the source code.

E.2.2 Data representation within application - DataManager

DataManager is a class developed to do the actual data retrieval from the working database. To represent a graph internal in the application the DataManager class retrieves the data one wants to visualise and creates GraphElement objects that are put into an object of the data structure called Dictionary [30]. This in such a way that each object (can be seen as a vertice) of a network will be set as a key in the dictionary and have a tied value in form of a list of GraphElements. Thus one can see the dataset as that a given key (vertice) in the dictionary (network) has a corresponding list Y (neighbours). For instance say that GraphElement X is a key and are associated to a list Y, then an object y in Y can be seen as that there exists an edge between X and y.

Then when it comes to actually visualise data one needs to convert the data to the appropriate form for the corresponding view. More about this in the next section.

E.2. DATA REPRESENTATION

E.2.3 Data parsers

This section will give account for the resulting data parser written for each of the three views. Parser for the VTK library for the force-directed view, a parser for BioFabric and lastly a parser for GerbilSphereALpha. The code for the parsers can be find in Appendix B.

VTK data parser

The VTK library uses a straightforward simple way of representing a graph. It works such as first all the vertices are added getting sequential ids starting from 1. Then one can add edges between these by calling a function with parameters saying between which two vertices the edge connects, using the vertices ids. Making it very compatible with the DataManager class and GraphElement object.

Because VTK represents their data in such a way and one needs to build the data structure in code behind there was no need to implement a parser for VTK. One could simply retain the necessary information from your network and use it directly to functions for building graphs in the VTK library. Though a parser was implemented, reading a text file containing information about a network and storing it in a dictionary. Much such as in the DataManager class. This parser was implemented for the evaluation stage for the VTK library. Making it possible to take a text file, generated from Gephi as input and returning a dictionary that could then be used to generate a graph with VTK to be evaluated. See appendix B for the source code of the parser.

BioFabric data parser

BioFabric supports tab-delimited .sif files [4] as input, therefore a parser for transforming data from our DataManager class to SIF files were created. A SIF file has the following form:

From vertice name, tab pp (indicating an edge), and tab followed by to vertice name. For example:

2 pp 4,

meaning there exists an edge between vertice 2 and vertice 4.

Where it states vertex name, the information in that field will be what displays in the BioFabric view as the labels. The source code for the parser can be found in appendix B.

GerbilSphere data parser

GerbilSphere supports two different file formats as input. First is Pajek[20] and second the Extensible Graph Markup Language (XGMML)[5]. Pajek is on a text based format with the file extension .Net. Which first states the number of nodes

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N, followed by N lines with the vertices id and labels. Next comes "*Edges" followed by X lines defining the networks edges. Where you first have the vertice from id followed by the to vertice id. The edges can also be weighted, in that case a third value with the weight are added.

In GerbilSphereAlpha these nodes can have attributes such as positioning for the sphere, the file is then called baked. See [48] for further information.

XGMML is based on the Graph Modelling Language, GML, which is a hierarchical ASCII-based file format for describing graphs. Using tags to describing different graph components. Though both Pajek and XGMML where usable for this thesis application the Pajek format was in the end used.

A parser for both these file formats where created, following the syntax described above. See appendix B for the source code of these parsers.

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