

# GPU Enhancement of the Trigger to Extend Physics Reach at the LHC

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**V. Halyo\*, A. Hunt, P. Jindal, P. LeGresley, P. Lujan**

*Princeton University, Princeton, NJ, USA*

*E-mail:* vhalyo@gmail.com

**ABSTRACT:** Significant new challenges are continuously confronting the High Energy Physics (HEP) experiments, in particular the two detectors at the Large Hadron Collider (LHC) at CERN, where nominal conditions deliver proton-proton collisions to the detectors at a rate of 40 MHz. This rate must be significantly reduced to comply with both the performance limitations of the mass storage hardware and the capabilities of the computing resources to process the collected data in a timely fashion for physics analysis. At the same time, the physics signals of interest must be retained with high efficiency.

The quest for rare new physics phenomena at the LHC leads us to evaluate a Graphics Processing Unit (GPU) enhancement of the existing High-Level Trigger (HLT), made possible by the current flexibility of the trigger system, which not only provides faster and more efficient event selection, but also includes the possibility of new complex triggers that were not previously feasible. A new tracking algorithm is evaluated on a NVIDIA Tesla K20c GPU, allowing for the first time the reconstruction of long-lived particles at the tracker system in the trigger. Preliminary time performance and efficiency will be presented.

**KEYWORDS:** ATLAS; CMS; Level-1 trigger; HLT; Tracker system.

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\*Corresponding Author

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### 1. Introduction

The stunning performance of the LHC, the successful physics results, and the discovery of a new Higgs-like particle will mark in history the first LHC running period not as the beginning of the end but rather the end of the beginning. The first LHC shutdown, scheduled for 2 years, provides a remarkable opportunity to improve our detector performance even further; in particular, to enhance and extend the physics reach by improving the set of events selected and recorded by the trigger.

The Trigger and Data Acquisition (DAQ) systems [1], [2], [3], [4] in a modern collider experiment, such as the ATLAS and CMS experiments at LHC, provide essential preliminary online analysis of the raw data for the purpose of filtering potentially interesting events into the data storage system. At the design luminosity of  $10^{34} \text{ cm}^{-2}\text{s}^{-1}$  this is a formidable task, which requires real-time handling of raw data with beam crossings at 40 MHz, each yielding on average  $\sim 20$  inelastic proton-proton interactions, and producing approximately 1 MB of zero-suppressed data. To keep the overall data rate within the current capability of the archival storage system of  $\sim 100 \text{ MB/s}$ , the trigger system must achieve a rejection ratio for background events of at least  $\sim 400,000 : 1$ .

The required level of performance is achieved in both CMS [3] and ATLAS [4] by implementing a typical trigger system with a hierarchy of multiple levels, ranging from fast and relatively

simple criteria implemented entirely in hardware and firmware, to more sophisticated software-based analysis. While the discussion in this paper focuses principally on the CMS detector, the trigger principles and performances are comparable between the two and the discussions can be generalized to both detectors. The CMS trigger is implemented in 2 levels: a hardware Level-1 trigger reducing the event rate to less than 100 kHz, followed by further processing in the High-Level Trigger (HLT) [5] designed to reduce this maximum Level-1 acceptance rate of 100 kHz to a final output rate of 100 Hz. The primary goal of the HLT is to apply a specific set of physics selection algorithms on the events read out to accept the events with the most interesting physics content. This computationally intensive processing is executed on a farm of commercial CPU processors that constitute the CMS HLT hardware.

By its very nature of being a computing system, the HLT relies on technologies that have evolved extremely rapidly. For many decades, one of the important methods for improving the performance of computing devices has been to increase the clock speed of the processor, and the typical CPU clock speed has increased by nearly a factor of 1000. In the past decade, however, it has become apparent that it is no longer possible to rely solely on increases in processor clock speed as a means for extracting additional computational power from existing architectures. The underlying reasons are complex, but center around reaching what may be fundamental limitations in semiconductor device physics. For this reason, recent innovations have focused around *parallel* processing, either through systems containing multiple processors, processors containing multiple cores, and so on.

One interesting technology which has continued to see exponential growth is graphics processing. A modern Graphic Processing Unit (GPU) is a massively parallel processor with thousands of execution units to handle highly parallel workloads related to computer graphics. By making these execution units highly programmable, manufacturers have made the massive computational power of a modern GPU available for more general-purpose computing, as opposed to being hard-wired for specific graphical operations. In certain applications that can be executed in massively parallel fashion, this can yield several orders of magnitude better performance than a conventional CPU.

Furthermore, leading technology vendors have released supported development APIs, such as NVIDIA CUDA ("Compute Unified Device Architecture") [6], which allow rapid development of software in nearly standard C code. CUDA allows CPU-based applications to access the resources of a GPU for more general-purpose computing without the limitations of using a graphics API. A modern GPU can simultaneously execute many thousands of computations in parallel, and an application using effective collaboration between the CPU and the GPU can see dramatic acceleration in algorithm execution.

A particularly good application for this technology would be executing machine vision and pattern recognition algorithms on detector data. These algorithms are often parallel by their very nature, and the highly controlled data produced by a particle physics detector reduces the pattern recognition task to its purest form. From the physics perspective, such an enhancement of the trigger capabilities would allow inclusion of new tracking triggers; for example, the selection of events with multiple displaced vertices at any location in the silicon tracker, which would be a “smoking gun” for new topological signatures not predicted by the Standard Model. Such a new tracking algorithm would allow us to augment the existing trigger with new types of trigger filters to select events with topological signatures that are currently not efficiently recorded.

In the following, a description of the physics motivation behind GPU enhancement of the HLT is provided. This includes a brief description of the existing High Level Trigger and the tracking algorithm used, the GPU and CUDA architecture, and the additional capabilities which would be enabled by a hybrid GPU/CPU computing farm for the HLT. The authors propose a new tracking reconstruction algorithm, show preliminary results, and discuss proposed new triggers that could trigger on events with a highly distinct signature which would be a clear indicator of new physics at the LHC.

## 2. Physics Motivation

An enhancement of the HLT might permit processing of the new tracking reconstruction on the full event at the Level-1 event rate up to design luminosity. The proposed HLT tracking would have a far-reaching impact on the physics program set by the HLT where the ultimate goal is to select the events of interest for CMS. The new tracking algorithm would introduce new possible trigger paths that are currently not possible due to the extensive processing time that would be required using CPUs alone. The robust parallel processing of the tracking on the hybrid CPU/GPU system would allow reconstruction of not only charged prompt tracks from the interaction point but also reconstruction of displaced vertices in the tracker far beyond what is possible in both CMS and ATLAS. Therefore, the tracking algorithm using the GPU will enrich the physics program and allow for searches on models with of new topological signatures that were not possible or suppressed before.

Only a few of the large selection of topological models can be described here. An example of an interesting class of models which would benefit from such triggers are hidden-valley models [7], in which a new confining gauge group is added to the standard model. The resulting (electrically-neutral) bound states can have low masses and long lifetimes and could be observed at the LHC. The production multiplicities are often large and events with final states with heavy flavor are common. In addition, displaced vertices and missing energy are possible. Accounting for LEP constraints, LHC production cross-sections were estimated to be typically in the 1-100 fb range, though they can be larger.

New tracking triggers would permit us to select at the HLT level events where a Higgs-like particle decays with a substantial branching fraction to long-lived neutral particles decaying at macroscopic distances from the primary vertex [7] in the tracker. The limited experimental constraints on light neutral long-lived particles suggests that we probably should not be surprised if a Higgs-like particle reveals itself through such decays. As the lifetimes of these resonances are not constrained, decays at centimeter and meter scales are equally possible. Each Higgs-like decay may produce two or more resonances with the multiplicity possibly varying from event to event. In many models the resonances will decay to the heaviest fermion pair available, with branching fractions similar to those of the standard model Higgs.

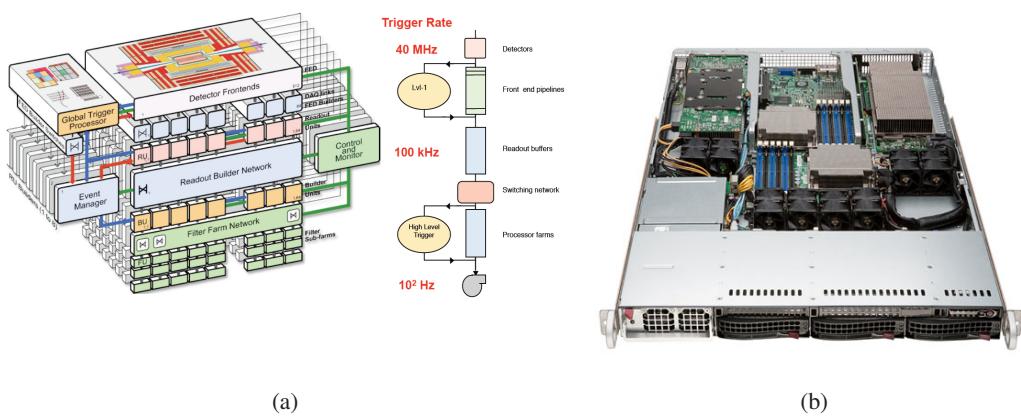
Other models that predict these unusual signatures [7]–[10] include either simple models where a scalar is added to the Higgs potential or superpotential depending whether a nonsupersymmetric or supersymmetric framework was used to build the model. Another possibility is confining hidden valley models, which produce qualitatively similar signals, though the origin of the signals is quite different. A complex Higgs decay in a hidden-valley model could produce, for example,

four resonances: one decaying promptly to jets, one escaping the detector giving missing energy, and two decaying to  $b\bar{b}$ , each with a displaced vertex.

Other obvious channels that would benefit from the new tracking algorithm or displaced jets or vertex triggers are inclusive and exclusive  $b$ -decay channels, or various topologies with boosted jets that will be more frequent as we increase our center of mass energy of the collision at design luminosity. These new triggers will allow us to be sensitive to a larger parameter space, including lower-mass Higgs, that could have evaded detection in previous experiments.

### 3. Trigger System

The LHC delivers proton-proton collisions to the CMS [11] detector at a rate of 40 MHz. This rate must be significantly reduced to comply with the performance limitations of the mass-storage hardware and the ability of the offline computing resources to process the collected data in a timely fashion for physics analysis. At the same time, the physics signals of interest must be retained with high efficiency. CMS features a two-level trigger system to reduce the rate to approximately 100 Hz. The Level-1 trigger [12] is based on custom hardware and designed to reduce the rate to about 100 kHz, corresponding to 100 GB/s, assuming an average event size of 1 MB. The High Level Trigger (HLT) [1],[5] is purely software-based and must achieve the remaining rate reduction by executing sophisticated offline-quality algorithms. An HLT path consists of algorithms that are executed in order of increasing complexity, so that the execution of a path can stop quickly as soon as evidence for the signal of interest is not found. This optimization means that the more sophisticated and time-consuming reconstruction algorithms are only applied when necessary. The ability to select the events of interest is the foundation of our quest for rare new physics phenomena, and thanks to the flexibility of the CMS HLT software and hardware computing farm we are able to propose an enhancement for the HLT a few years down the road after startup.



**Figure 1.** Left: CMS DAQ architecture. The size of the event builder (72 Readout Units, 288 Builder Units) represents one slice; the system can be equipped with up to eight slices. Right: Integrated GPU/CPU 1U server (image courtesy of NVIDIA).

The architecture of the CMS HLT [1],[5] combines the flexibility gained by using the offline reconstruction [13] with the robustness required for reliable online operation of the DAQ. Figure 1(a) shows a schematic of the architecture of the CMS DAQ system. Event fragments are read out and stored in Readout Units (RU) for each event accepted by the Level-1 trigger. The fragments are subsequently assembled into complete events by an Event Builder through a complex of switched networks into event buffers (BU). The full event content is then handed to one of the HLT Filter Units (FU). The FU execute a series of physics reconstruction and filter algorithms and events that are found to be sufficiently interesting for offline analysis are forwarded to the Storage Manager (SM). The decoupling of physics algorithm execution from data flow allows each FU to continue operation in the case of a problematic event, recover the content of the problematic event, and forward it to be stored unprocessed. The FU architecture consists of two separate applications, the ResourceBroker, which exchanges data with the DAQ, and the EventProcessor, which integrates the reconstruction software. Given the involved event sizes and rates, reformatting raw events consisting of a large number of small data fragments into the physical memory of a Filter Unit requires high bandwidth I/O, while the subsequent HLT processing is mostly CPU-intensive. The EventProcessor previously mentioned encapsulates the event processing machinery of the CMS reconstruction, providing the full flexibility required to execute complex physics algorithms.

As the farms of machines where these event selections are executed are commercial servers, GPUs can be easily integrated into them. A simple solution is shown in Figure 1(b) with a 1U server containing dual multicore CPUs and two NVIDIA Tesla GPUs. While this would provide a single, integrated 1U GPU/CPU server, this of course implies replacing the existing servers, evaluating the new power consumption, and the cost of these servers relative to any other options.

## 4. GPU Architecture

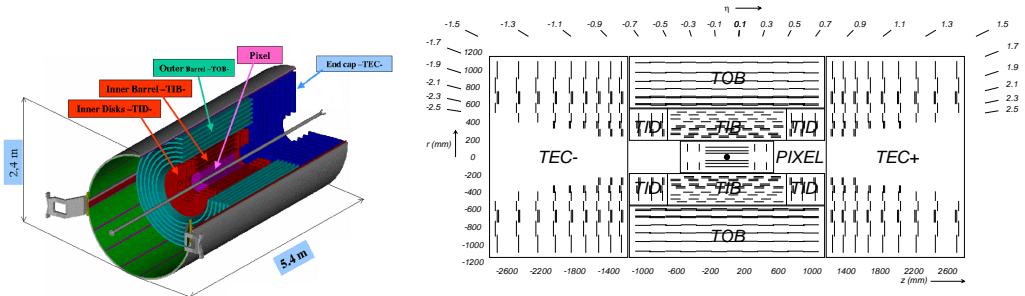
The NVIDIA GPU architecture consists of a number of general purpose floating point processors: *stream processors*. The stream processors are fully programmable and can be utilized as general purpose compute cores for computationally intensive purposes outside of graphics. Multiple stream processors, a parallel data cache (a user managed on-chip cache), and on some processors a hardware managed L1 cache are grouped together into a multiprocessor. Typical high end GPUs feature tens of multiprocessors with hundreds of stream processors.

The streaming processors can be utilized for general purpose computations using CUDA ("Compute Unified Device Architecture") [6]. Unlike past efforts to harness the computational power found in GPUs using a graphics API, CUDA specifies a few simple extensions to the C programming language and a parallel programming model to enable full access to the GPU hardware.

The programmer writes a CPU program that invokes functions called *kernels* that execute on the GPU. A kernel consists of many thousands of threads that execute in parallel across the stream processors. Groups of threads called *blocks* are scheduled on a single multiprocessor and can cooperate among themselves through access to a parallel data cache. Each block is independent by design so the many blocks of a kernel, called a *grid*, can be executed in parallel on several multiprocessors.

## 5. Inner Tracker

Both the CMS and ATLAS inner trackers include a silicon pixel detector and a silicon strip detector. All tracker layers provide two-dimensional hit position measurements, but only the pixel tracker and a subset of the strip tracker layers provide three-dimensional hit position measurements. Only the CMS tracker is considered; however, the detector performances are comparable in the CMS and ATLAS experiments, and the tracking algorithm and results discussed are applicable for both of these experiments as well. The CMS pixel detector includes three barrel layers and two forward disks on either end of the detector; outside the pixel detector is the strip detector, consisting of ten layers in the barrel plus three inner disks and nine forward disks at each end of the detector. Owing to the strong magnetic field and the high granularity of the silicon tracker, promptly-produced charged particles with transverse momentum  $p_T = 100$  GeV/c are reconstructed with a resolution in  $p_T$  of 1.5% and in transverse impact parameter  $d_0$  of 15 mm. The track reconstruction algorithms are able to reconstruct displaced tracks with transverse impact parameters up to 25 cm from particles decaying up to 50 cm from the beam line. The performance of the track reconstruction algorithms has been studied with data [14]. The silicon tracker is also used to reconstruct the primary vertex position with a precision of  $\sigma_d = 20$  mm in each dimension. Figure 2 shows the layout of the CMS tracker.



**Figure 2.** The CMS tracker in a 3-D view (left) and a 2-D view (right), showing the pixel detector and the silicon strip tracker.

## 6. Current Tracking Algorithm

The CMS track reconstruction, known as the Combinatorial Track Finder (CTF), uses an iterative algorithm, with earlier iterations searching for tracks that are more easily found (relatively higher  $p_T$  tracks close to the interaction region). The hits in these tracks are then removed, allowing later iterations to search for lower momentum or highly displaced tracks without the combinatorial possibilities becoming too large. Each iteration consists of four steps: a seeding step, a track finding step, a track fitting step, and a selection step.

In the first step, a seed, consisting of either three hits or two hits and a primary vertex constraint, is constructed to create an initial estimate of the trajectory parameters for the track. Second, the track finding is performed using a global Kalman filter [15]. This step performs a fast propagation of the track candidate to propagate the track through the layers of the detector, search for

compatible nearby hits, and attach them to the candidate. After all candidates in this step have been found, the track candidate collection is then cleaned to remove duplicate tracks or tracks which share a large number of hits. The third step is to perform a full Kalman fit over the whole track to obtain the best estimate of the track parameters at all points along the trajectory. The filter begins at the innermost hits, and then iterates outward through each hit to update the track trajectory estimate and its uncertainty. After this first fit is complete, a smoothing stage is then performed running backwards from the last hit to apply the information from the later hits to the earlier ones. This step uses a Runge-Kutta propagator to account for the effect of material interactions and an inhomogeneous magnetic field. Finally, track selection requirements are applied to reduce the fake rate of the resulting track candidates.

## 7. Proposed Fast Tracking Algorithm

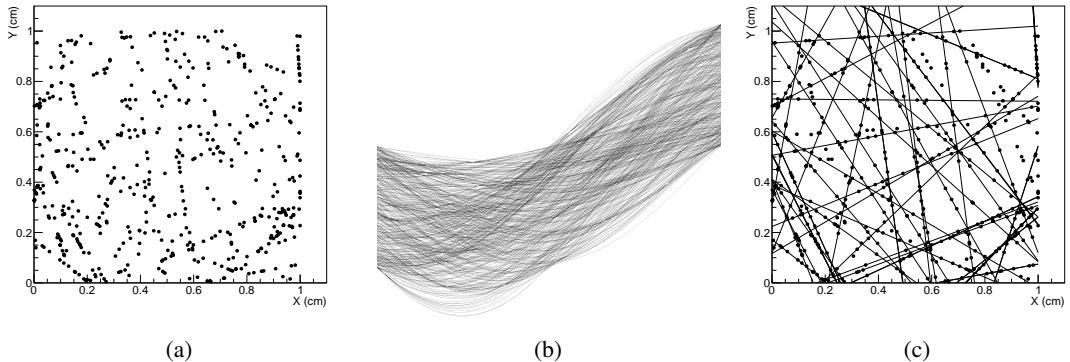
One possible application of the GPU-enabled parallelism would be to accelerate the performance of the existing combinatorial track finder. Since the finding and fitting process for each track is largely independent of the other tracks, parallelization should not be conceptually difficult. However, the use of GPU-based computing in the HLT also enables the possibility of running tracking algorithms which are dramatically and qualitatively different in nature to the current CTF, thus enhancing the discovery potential.

The Hough transform is a well-known algorithm used in various machine vision applications that differs from the CTF approach in that it does not operate on localized features of a data set. Rather, the technique is in some sense more holistic, operating on an entire image as a whole. The technique is described at length in existing literature [16], [17], but the concept as it would be applicable to the tracking problem is to consider the parameterization of any given track. Any given set of hits observed in the detector, for example, the simulated straight line track data shown in Figure 3(a), can correspond to many different possible tracks in parameter space as shown in Figure 3(b). When integrated over the entire data set, peaks appear in parameter space at the values corresponding to the actual, physical trajectories as shown in Figure 3(c).

## 8. Preliminary Results

As was briefly discussed previously, the traditional combinatoric track finder approach is constrained by the need to keep the number of possible track combinations under control, which means that displaced vertices and other odd tracks are often not reconstructed due to the extensive processing time required to consider them. It is hoped that a more holistic algorithm can be used to supplement the existing tracking algorithm in a significant way. As a demonstration of this, a simple tracking algorithm based on the Hough transform was developed and run against a standalone Monte Carlo simulation with a simple tracker geometry file. The preliminary investigation was performed using Intel multicore CPUs and NVIDIA Tesla C2075 and K20c GPUs.

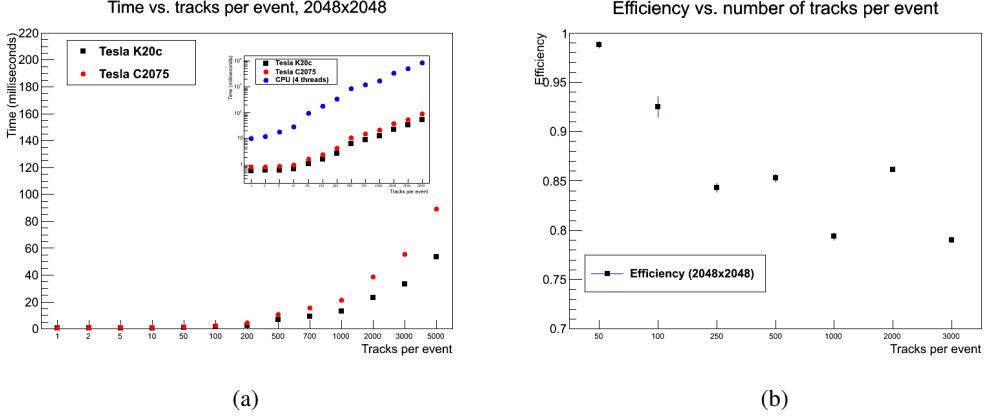
The Hough transform algorithm is not trivial to implement in parallel because the computation of the parameter space is subject to race conditions, where it is not necessarily safe to have multiple threads arbitrarily make updates as hits are processed. The Intel Performance Primitives (IPP) library contains an implementation of the Hough transform, but as it is not parallelized, it would



**Figure 3.** The Hough transform algorithm applied to a simple example. Left: Hits in a simulated event with 50 straight-line tracks and 10 hits per track. Center: Each hit results in a sinusoidal curve in the parameter space. Locations where many of these sinusoidal lines cross are likely to be tracks in the original data. Right: Candidate tracks identified from finding local maxima in the parameter space.

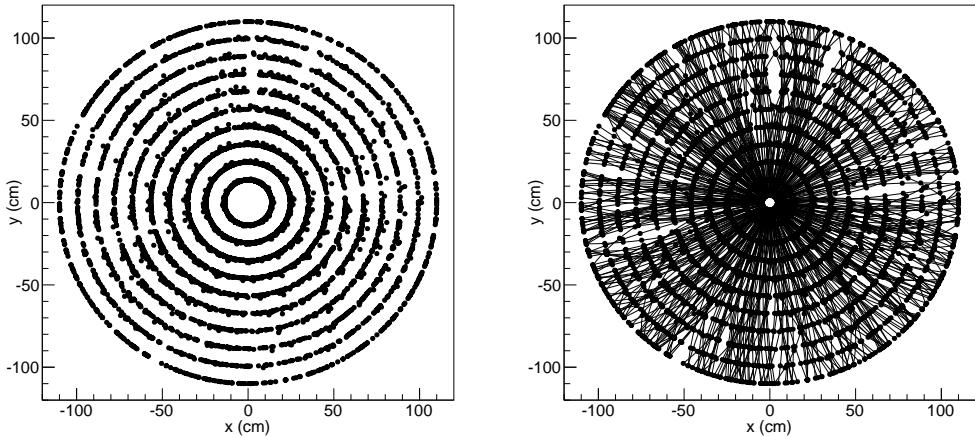
be difficult to compare this fairly to a GPU-based implementation. In order to provide a more fair performance comparison, a parallel implementation of the Hough transform for the CPU has been developed as part of this work. This CPU implementation is parallelized using OpenMP threads and speedups of 2.6 – 3.6 were achieved on a Intel Core i7-3770 (Ivy Bridge, quad core, 3.4 GHz) processor. The CPU used for the performance results is physically a quad core CPU but supports up to two threads per physical core using Simultaneous Multithreading (SMT), with the Intel implementation of SMT known as HyperThreading (HT). SMT did not show any performance advantage for this application, because the speedup actually dropped as the number of threads exceeded the number of physical cores. Figure 4(a) shows the results of the CPU compared to the two NVIDIA GPUs. Throughout the event processing, all of the data associated with the hits, parameter space, and peak detection fit within the memory of the GPU. This eliminates the need to perform expensive movements of the data back and forth between the CPU and GPU over PCI Express, helping to achieve a GPU implementation that is up to 100x faster than the multithreaded CPU implementation. Figure 4(b) shows the efficiency defined as the fraction of simulated tracks successfully reconstructed by the algorithm as a function of the number of tracks present in the event. As this is only a preliminary implementation, the efficiency and purity are not yet optimized, with the efficiency about 80% for events with a few thousand tracks and comparable values for the purity. More work is obviously needed to improve the performance of the algorithm.

Although the Hough transform is most often associated with finding straight lines in data, it is applicable to any feature which can be represented by a finite number of parameters. For example, circles of unknown location and radius and location can be identified in a three-dimensional parameter space representing the x and y location of the center plus a third parameter for the radius. Figure 5 shows an example of results for our Hough transform implementation used for identifying curved tracks. In this case, the tracks are constrained to pass through the interaction point, reducing the parameter space to a two-dimensional space similar to that used for straight tracks. The computational cost of the Hough transform is strongly dependent on the total number of parameters,



**Figure 4.** Left: Time performance comparison of the Intel CPU (using 4 threads), NVIDIA Tesla C2075, and NVIDIA Tesla K20c. The inset shows the same data on a logarithmic scale. Right: Efficiency of the track-finding algorithm on the GPU implementation as a function of the number of tracks present in the event.

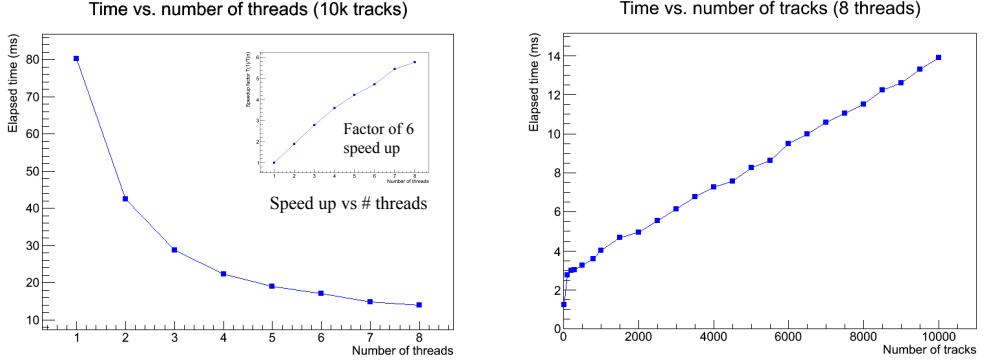
while the details of the particular parameterization have essentially no effect on the performance.



**Figure 5.** The Hough transform algorithm applied to a case with curved tracks. Left: Hits from Monte Carlo simulation for curved tracks originating from the interaction point. Right: Curved tracks identified using the Hough transform.

While the Hough transform is a critical part of the proposed tracking algorithm, it is not the only aspect of the computation. After candidate tracks have been identified from analysis of the parameter space, it may be necessary to perform a fit of the hits to the candidate tracks. This fitting operation is well suited to parallelization on the GPU, but the performance results in Figure 6 show that a multithreaded CPU implementation requires only a few milliseconds. In comparison the Hough transform on the GPU requires many tens of milliseconds, so the fitting operation is relatively low priority for performance optimization. If or when fitting becomes a significant

performance bottleneck, it could certainly be run on the GPU to further increase performance.



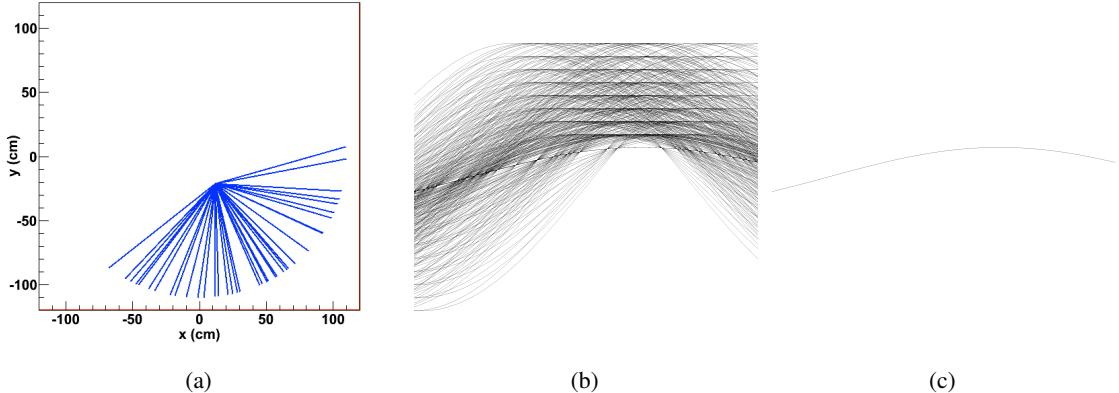
**Figure 6.** Time performance of a CPU-based algorithm for the fitting step of the tracking. Left: Speed-up observed as a function of number of threads used for the fitting. Right: Time required as a function of the number of tracks present in the event.

## 9. New Trigger Capabilities

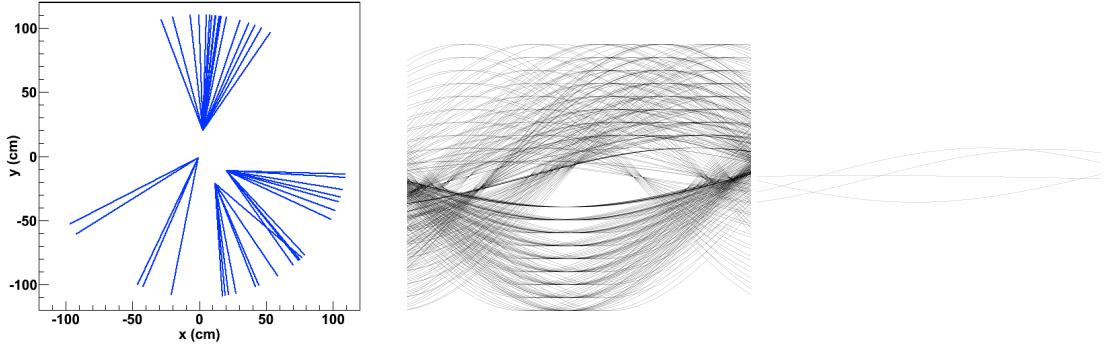
The ability to handle displaced vertices provides the opportunity to identify interesting new physics such as non-prompt jets and black holes. Figure 7 shows an example of the Hough transform applied to a jet originating from a displaced vertex. First, we simulate a set of tracks in the jet, as shown in Figure 7(a). Again, the Hough transform is applied to the corresponding hits making up these tracks to generate the parameter space displayed in Figure 7(b). Recall that the parameter space identifies candidate tracks as locations where many sinusoids cross one another. In Figure 7(b) the locations of these crossings are visually apparent as the bright spots in the parameter space. However, the analysis is taken one step further by noting that the crossings all lie along a single sinusoidal curve in the parameter space. This single sinusoidal curve has been isolated in Figure 7(c) and is significant because that one sinusoidal curve in the parameter space corresponds to a point in the original x-y space. More importantly, that point in the original x-y space corresponds to the vertex of the displaced jet. Interestingly, the most convenient way to implement this process is to use the Hough transform a second time, this time applying it not to the hits in the x-y space but the crossings in the parameter space. Using the appropriate parameterization to look for sinusoidal curves instead of straight lines, the curve in Figure 7(c) is identified and the vertex of the jet is now located. Figure 8 illustrates the same technique applied to an event with multiple displaced jets.

## 10. Summary

The quest for rare new physics phenomena has motivated the authors to propose a GPU-based enhancement of the trigger system, made possible by the flexibility of the current trigger systems of the general-purpose detectors at the LHC. The Hough transform algorithm, originally designed



**Figure 7.** Hough transform algorithm applied to a displaced jet. Left: Simulated tracks originating from a displaced jet. Center: In the parameter space, the maxima are on a single sinusoid. Right: The second Hough transform identifies the sinusoid corresponding to the jet vertex.



**Figure 8.** Hough transform algorithm applied to an event with multiple displaced jets. Left: Simulated tracks in the event. Center: The parameter space is difficult to visually interpret. Right: The second Hough transform identifies the sinusoids corresponding to the jet vertices.

for machine vision problems, can be used as a tracking algorithm to provide a different, complementary technique, which is a more holistic picture of the image as a whole. The algorithm not only permits us to find simultaneously any combination of prompt and non-prompt tracks, but to develop new trigger algorithms for exotic phenomena such as highly-displaced jets or black holes. These new topologies would represent a “smoking gun” for new physics, and so extending the trigger algorithm to be able to efficiently recognize them would dramatically increase the reach of physics at the LHC. The proposed tracking algorithm would not replace the existing combinatoric track finger, but will enhance its capabilities at the trigger level. The results presented here are our first preliminary results meant to demonstrate the feasibility of the algorithm and its potential impact. Although it is feasible to complete the testing of the new triggers proposed by the end of the shutdown, extensive work must be done to improve tracking efficiency and purity for the general full tracking algorithm. In addition, to better understand the relative performance of

CPUs and GPUs, we intend to implement vectorization on the CPU to fully utilize the Advanced Vector Extensions (AVX) capability present on modern CPUs from Intel and AMD. Although the GPU might still show a compelling performance advantage for this class of computations, the 256 bit AVX capabilities should increase the CPU performance and allow us to better quantify that advantage.

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