# Lab 1 VHE

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#### I. Introduction

Following the Challenger Space Shuttle's destruction in 1986, a commission appointed by President Reagan determined the cause to be a gas leak through a field joint. This problem was well-known to NASA and is frequently referred to as an o-ring failure. In 1989, Dalal et al. collected data from previous space shuttle launches to study the probability of an o-ring failure under conditions similar to those that occured during the Challenger launch in 1986. In this analysis, we will use their dataset to mimic their study and attempt to determine the effect of key explanatory variables (temperature and pressure) on o-ring failure. In the end we specified a logistic regression model on temperature with the following formula:

We first begin our analysis with a thorough exploratory data analysis in order to understand the variables we are working with. Then, we estimate a series of models that we use to predict o-ring failure.

```
# Import libraries
library(dplyr)
library(Hmisc)
library(car)
library(knitr)

df <- read.csv("challenger.csv")</pre>
```

#### II. EDA

#### II (a) Univariate Analysis

```
# Start with basic looks at the data
glimpse(df)
## Observations: 23
## Variables: 5
             <int> 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16...
## $ Flight
             <int> 66, 70, 69, 68, 67, 72, 73, 70, 57, 63, 70, 78, 67, 5...
## $ Temp
## $ Pressure <int> 50, 50, 50, 50, 50, 50, 100, 100, 200, 200, 200, 200,...
## $ 0.ring
             <int> 0, 1, 0, 0, 0, 0, 0, 0, 1, 1, 1, 0, 0, 2, 0, 0, 0, 0, ...
## $ Number
             describe(df[,c("Temp", "Pressure", "0.ring")])
## df[, c("Temp", "Pressure", "O.ring")]
##
##
   3 Variables
                     23
                        Observations
##
##
  Temp
##
         n
            missing distinct
                                Info
                                         Mean
                                                  Gmd
                                                           .05
                                                                    .10
##
        23
                  0
                         16
                               0.992
                                        69.57
                                                7.968
                                                          57.1
                                                                   59.0
##
       .25
                .50
                         .75
                                 .90
                                          .95
                       75.0
##
      67.0
               70.0
                                77.6
                                         78.9
```

```
##
                                             66
                                                    67
                                                                        70
                                                                               72
## Value
                  53
                         57
                                58
                                       63
                                                           68
                                                                 69
## Frequency
                    1
                                        1
                                              1
                                                     3
                                                            1
                                                                         4
  Proportion 0.043 0.043 0.043 0.043 0.043 0.130 0.043 0.043 0.174 0.043
##
## Value
                  73
                                76
                                             79
                                                    81
                         75
                                       78
## Frequency
                   1
                          2
                                 2
                                        1
## Proportion 0.043 0.087 0.087 0.043 0.043 0.043
##
   Pressure
##
                                     Info
                                                           Gmd
              missing distinct
                                               Mean
           n
          23
                                    0.706
                                                        67.59
##
                     0
                               3
                                              152.2
##
## Value
                  50
                        100
                               200
                   6
                          2
## Frequency
                                15
   Proportion 0.261 0.087 0.652
##
##
   0.ring
##
              missing distinct
                                               Mean
          n
                                     Info
                                                           Gmd
##
                     0
                                    0.654
                                             0.3913
                                                       0.6087
##
## Value
                   0
                                 2
## Frequency
                  16
                          5
                                 2
## Proportion 0.696 0.217 0.087
```

A glimpse of the data shows we have 5 variables in our dataset:

- Flight: Flight number
- Temp: Temperature in F at launch
- Pressure: combustion pressure in psi at launch
- O.ring: number of primary field o-ring failures
- Number: total number of primary field o-rings

We are primarily interested in the effects of temperature and pressure on o-ring failure. Seeing as the total number of primary field o-rings does not change for our observations and we have no particular reason to see it change, we discard this variable due to lack of immediate use/differentiating behavior between failed and successful launches. Similarly, we discard flight number due to lack of any immediate use.

We can see that the O.ring variable has 3 distinct values: 0, 1, and 2. We are going to be nuanced in our analysis and say we want to find the conditions that lead to at least one o-ring failure. Therefore, we will recategorize those flights with 2 failures as having 1 failure for the purposes of this study.

```
# We don't want to eliminate raw data
df$0.ring.total = df$0.ring
df$0.ring[df$0.ring > 1] = 1
```

In addition, we see that the dataset contains 23 data points from other shuttle launches and none of the variables are missing any entries. Interestingly, pressure is generally considered to be a continuous variable, however, we see three distinct values of 50, 100, and 200. We could potentially see reason to use this as a categorical variable in the regression estimation below.

```
#quick check for potential collinearity as well as surface level relations
kable(cor(df[,c("Temp", "Pressure", "0.ring")]))
```

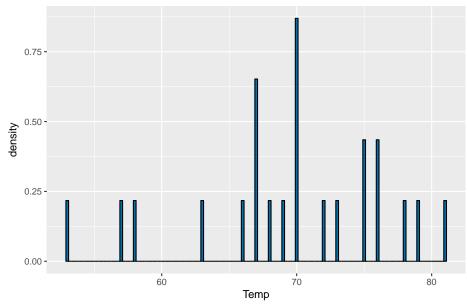
	Temp	Pressure	O.ring
Temp	1.0000000	0.0398177	-0.5607143

	Temp	Pressure	O.ring
Pressure	0.0398177	1.0000000	0.2616884
O.ring	-0.5607143	0.2616884	1.0000000

We take a quick look at correlation between variables to assess wether there might be collinearity as well as a rough gauge of predictive power between these variables prior to any transformations. We see a moderate negative correlation between O.ring failures and temperature and a weakly positive correlation between pressure and failures. We see negligible positive correlation between temperature and pressure and thus don't worry about colliniearity.

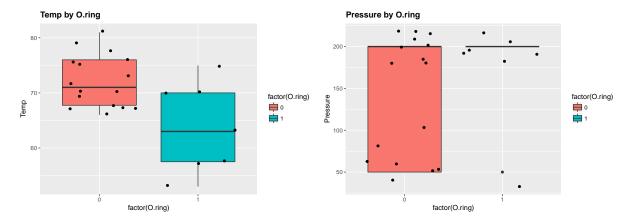
```
#What does the distribution of temperatures look like?
ggplot(df, aes(x = Temp)) +
  geom_histogram(aes(y = ..density..), binwidth = 0.2, fill="#0072B2", colour="black") +
  ggtitle("Histogram of Temperature") +
  theme(plot.title = element_text(lineheight=1, face="bold"))
```

# **Histogram of Temperature**



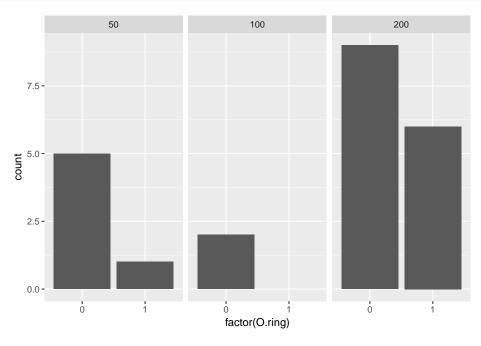
The distribution of the temperature explanatory variable looks to faintly resemble a normal distribution with a very slight negative skew. Due to this, we see no compelling reason to take a log transformation of the variable at this stage. The mode of temperatures is 70 and the range is 53, 81.

#### II (b) Bivariate Analysis



The boxplot above of temperature grouped by o-ring failure shows the average temperature when o-rings failed was lower than when they did not. Also, the overlay scatterplot shows the mismatch of data: there's much more data for non-failures than failures. The second boxplot for pressure shows that all but 2 o-ring failures occured under high pressure conditions. Also, for non-failures, the mean and 75th percentile are overlapping, indicating that the data is skewed.

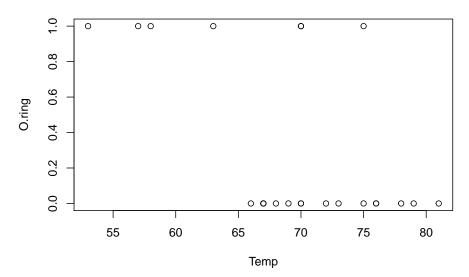




The above plot reinforces the aforementioned finding that the data has a negative skew with most of the data for both failures and non-failures occurring under pressure of 200 psi.

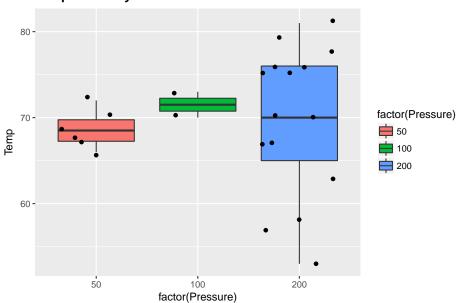
```
plot(0.ring~Temp,data=df, main="0-ring Failures vs Temperature")
```

# **O-ring Failures vs Temperature**

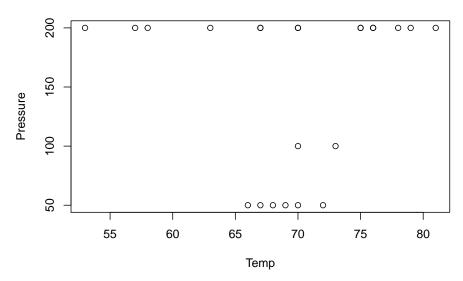


Directly looking at the distribution of o-ring failures to temperature, we can determine our data is not completely separated (hence traditional logistic regression is still a valid possibility for model selection).

# **Temperature by Pressure**

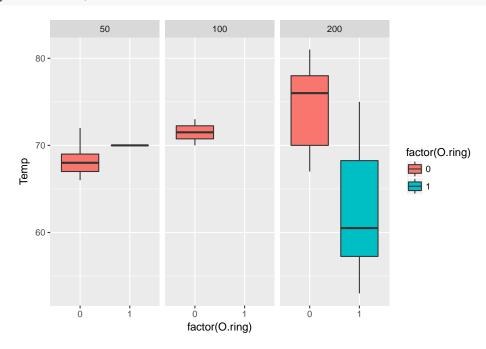


# **Pressure vs Temperature**



Comparing temperature and pressure directly, we can see that there is a vaguely positive relationship between temperature and pressure. Under basic gas laws, temperature is proportional to pressure, however, this relationship doesn't appear to hold in all cases of o-ring failure.

```
#slicing by pressure, any distinct relations between failure and temperature?
ggplot(df, aes(x = factor(0.ring), y = Temp, fill = factor(0.ring))) + geom_boxplot() +
facet_wrap(~ Pressure, ncol = 3)
```



# III. Book Questions

#### Question 4

#### 4 (a) Why is independence of each observation necessary?

This independence assumption is necessary for deriving the likelihood-based solution as we can take products of the probabilities. Potential issues is that the quality/durability of the O-ring might be dependent on the factory or even batch that it came from (clustering) and could interfere with producing a more accurate estimate when left unaccounted for. Moreover damage in one O-ring could affect the probability of damage in subsequent O-rings (might be easier for the system to collapse as a whole).

## 4 (b) Estimate logistic regression model

```
# Initial model
mod.fit1<-glm(formula=0.ring~Pressure+Temp,data=df,family=binomial(link = logit))</pre>
summary(mod.fit1)
##
## Call:
## glm(formula = 0.ring ~ Pressure + Temp, family = binomial(link = logit),
##
       data = df)
##
## Deviance Residuals:
##
                 10
                      Median
                                    3Q
                                            Max
## -1.1993
           -0.5778 -0.4247
                               0.3523
                                         2.1449
##
## Coefficients:
##
                Estimate Std. Error z value Pr(>|z|)
## (Intercept) 13.292360
                           7.663968
                                       1.734
                                               0.0828 .
## Pressure
                0.010400
                           0.008979
                                       1.158
                                               0.2468
               -0.228671
                           0.109988
                                     -2.079
                                               0.0376 *
## Temp
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 28.267 on 22 degrees of freedom
## Residual deviance: 18.782 on 20 degrees of freedom
## AIC: 24.782
##
## Number of Fisher Scoring iterations: 5
# Include interaction between temperature and pressure to capture
# positive relationship between those variables
mod.fit2<-glm(formula=0.ring~Pressure+Temp+Pressure:Temp,data=df,family=binomial(link = logit))</pre>
summary(mod.fit2)
##
## Call:
## glm(formula = 0.ring ~ Pressure + Temp + Pressure: Temp, family = binomial(link = logit),
##
       data = df)
##
## Deviance Residuals:
       Min
                 1Q
                      Median
                                    3Q
                                            Max
```

```
## -1.2083 -0.5879 -0.4178 0.3049
                                        2.0406
##
## Coefficients:
##
                   Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                -27.217458 50.238881 -0.542
                             0.258398 0.856
                                                  0.392
## Pressure
                   0.221088
                            0.720644 0.497
## Temp
                   0.358212
                                                  0.619
## Pressure:Temp -0.003054
                              0.003711 -0.823
                                                  0.410
##
##
  (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 28.267 on 22 degrees of freedom
##
## Residual deviance: 18.075 on 19 degrees of freedom
## AIC: 26.075
##
## Number of Fisher Scoring iterations: 5
# Turn Pressure into a factor
mod.fit3<-glm(formula=0.ring~factor(Pressure)+Temp,data=df,family=binomial(link = logit))</pre>
summary(mod.fit3)
##
## Call:
## glm(formula = 0.ring ~ factor(Pressure) + Temp, family = binomial(link = logit),
       data = df
##
## Deviance Residuals:
                     Median
##
                1Q
                                   3Q
       Min
                                           Max
## -1.2093 -0.6044 -0.4151 0.3635
                                        2.0479
##
## Coefficients:
##
                        Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                        13.5106
                                     7.4288
                                             1.819 0.0690
## factor(Pressure)100 -15.2969 2761.7586 -0.006
                                                      0.9956
## factor(Pressure)200
                        1.3774
                                     1.3154
                                             1.047
                                                      0.2950
## Temp
                         -0.2211
                                    0.1078 -2.050 0.0403 *
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 28.267 on 22 degrees of freedom
## Residual deviance: 18.214 on 19 degrees of freedom
## AIC: 26.214
##
## Number of Fisher Scoring iterations: 16
Our first estimated logistic regression model is
                      logit(\hat{\pi}) = 13.292360 + 0.0104 Pressure - 0.228671 Temp
We include an interaction variable in the second
        logit(\hat{\pi}) = -27.217458 + 0.221088Pressure + 0.358212Temp - 0.003054Pressure x Temp
```

4 (c) Perform LRTs to judge the importance of the explanatory variables in the model.

```
#Anova(mod.fit1, Test='LRT')
Anova(mod.fit2, Test='LRT')
```

```
## Analysis of Deviance Table (Type II tests)
##
## Response: O.ring
##
                 LR Chisq Df Pr(>Chisq)
                   1.5331 1
                               0.215648
## Pressure
                   7.7542 1
                               0.005359 **
## Temp
                   0.7069
                               0.400478
## Pressure: Temp
                           1
                  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
```

The likelihood ratio test evaluates the importance of each explanatory variable and interaction variable. For the first explanatory variable, pressure, we test the hypothesis:  $H_0: \beta_1 = 0$  vs  $H_a: \beta_1 \neq 0$ . The test statistic is  $-2log(\Lambda) = 1.5331$  and the p-value is 0.215648 so we fail to reject the null hypothesis that pressure has no effect on o-ring failure. For the second explanatory variable, temperature, we test the hypothesis:  $H_0: \beta_2 = 0$  vs  $H_a: \beta_2 \neq 0$ . The test statistic is  $-2log(\Lambda) = 7.7542$  and the p-value is 0.005359 so we reject the null hypothesis and conclude that there is evidence of an interaction between temperature and o-ring failure. Finally, we test the interaction variable, Pressure x Temp, with the hypothesis:  $H_0: \beta_3 = 0$  vs  $H_a: \beta_3 \neq 0$ . The test statistic is  $-2log(\Lambda) = 0.7069$  and the p-value is 0.400478 so we fail to reject the null hypothesis that the effect of temperature and pressure on o-ring failure depend on each other.

#### 4 (d) Why did they remove pressure? Why could this be a problem?

In terms of statistical significance, pressure wasn't found to be statistically significant. Potential problems could be losing precision on temp as well as in probability, especially for edge cases.

#### Question 5

### 5 (a) Estimate the model

```
logit(\pi) = \beta_0 + \beta_1 Temp
```

```
mod.fit2<-glm(formula=0.ring~Temp,data=df,family=binomial(link = logit))
summary(mod.fit2)</pre>
```

```
##
## Call:
  glm(formula = 0.ring ~ Temp, family = binomial(link = logit),
##
       data = df)
##
## Deviance Residuals:
##
      Min
                 1Q
                      Median
                                   30
                                           Max
  -1.0611 -0.7613 -0.3783
                               0.4524
                                        2.2175
##
## Coefficients:
##
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) 15.0429
                            7.3786
                                     2.039
                                             0.0415 *
                                             0.0320 *
## Temp
                -0.2322
                            0.1082 -2.145
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
```

```
## (Dispersion parameter for binomial family taken to be 1)
##
                              on 22 degrees of freedom
##
       Null deviance: 28.267
## Residual deviance: 20.315 on 21
                                     degrees of freedom
## AIC: 24.315
##
## Number of Fisher Scoring iterations: 5
The estimated logistic regression model is
```

 $logit(\hat{\pi}) = 15.0429 - 0.2322Temp$ 

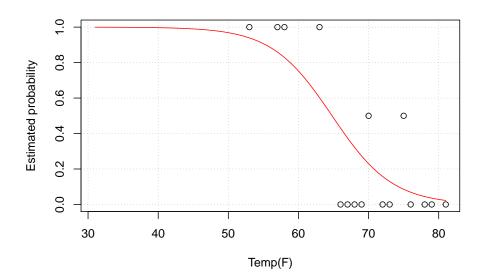
# 5 (b)

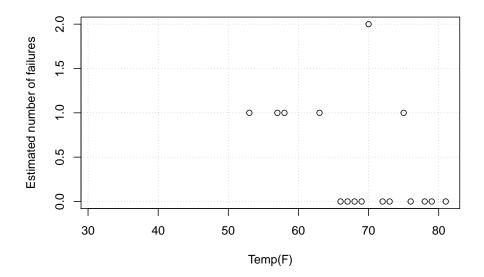
Construct two plots:  $(1)\pi$  vs. Temp and (2) Expected number of failures vs. Temp. Use a temperature range of 31 to 81 on the x-axis even though the minimum temperature in the data set was 53.

```
w<-aggregate(formula=0.ring~Temp, data=df, FUN=sum)</pre>
n<-aggregate(formula=0.ring~Temp, data=df, FUN=length)</pre>
w.n<-data.frame(Temperature=w$Temp, Failure=w$0.ring, trials=n$0.ring,
                 proportion=round(w$0.ring/n$0.ring,4))
kable(head(w.n))
```

Temperature	Failure	trials	proportion
53	1	1	1
57	1	1	1
58	1	1	1
63	1	1	1
66	0	1	0
67	0	3	0

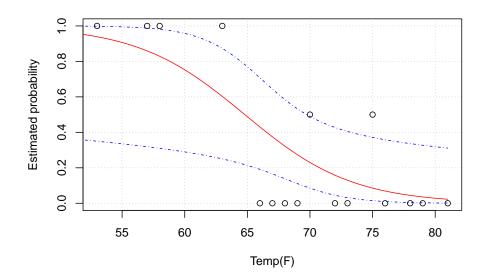
```
# Plot pi vs Temp
plot(x=w$Temp, y=w$0.ring/n$0.ring, xlab="Temp(F)", ylab="Estimated probability",
     panel.first=grid(col="gray", lty="dotted"), xlim=c(31,81))
curve(expr=predict(object=mod.fit2, newdata=data.frame(Temp=x),
                   type="response"), col="red", add=TRUE)
```





#curve(expr=predict(object=mod.fit2, newdata=data.frame(Temp=x), type="response"), col="red", add=TRUE)

5 (c) Include the 95% Wald confidence interval bands for  $\pi$  on the plot. Why are the bands much wider for lower temperatures than for higher temperatures?



Bands are wider due to change in probability across temperature gradient. There is a much steeper drop in temperature below and above 65 (similar to complete separation problem). Less of a drastic change in higher temperatures due to two "middle" values between 70 and 75.

5 (d) The temperature was 31 at launch for the Challenger in 1986. Estimate the probability of an O-ring failure using this temperature, and compute a corresponding confidence interval. Discuss what assumptions need to be made in order to apply the inference procedures.

```
CI.lin.pred = linear.pred$fit + qnorm(p = c(alpha/2, 1-alpha/2))*linear.pred$se
#confidence interval before exponentiation
CI.pi = exp(CI.lin.pred)/(1+exp(CI.lin.pred)) #actual interval
```

The estimated probability of o-ring failure at 31 F is 0.9996 and the corresponding confidence interval is 0.4816, 1.

5 (e) Rather than using Wald or profile LR intervals for the probability of failure, Dalalet al. (1989) use a parametric bootstrap to compute intervals. Their process was to (1) simulate a large number of data sets (n=23 for each) from the estimated model of

$$logit(\pi) = \beta_0 + \beta_1 * Temp$$

;(2)estimate new models for each dataset,say

$$logit(\pi) = Beta_0 + Beta_1 * Temp$$

; and (3) compute at a specific temperature of interest. The authors used the 0.05 and 0.95 observed quantiles from the simulated distribution as their 90% confidence interval limits. Using the parametric bootstrap, compute 90% confidence intervals separately at temperatures of 31 and 72.27

```
library(boot)
##
## Attaching package: 'boot'
## The following object is masked from 'package:car':
##
##
       logit
## The following object is masked from 'package:survival':
##
##
       aml
## The following object is masked from 'package:lattice':
##
##
       melanoma
# Necessary because we're calculating a parametric bootstrap
# interval and this library is referenced in the book.
# Get probs from mod.fit2
predict.data <- data.frame(Temp=31:81)</pre>
linear.pred=predict(object = mod.fit2, newdata = predict.data, #linear part of model
                    type = "link", se = TRUE)
pis = exp(linear.pred$fit)/(1+exp(linear.pred$fit))
# Function to calculate desired statistic
pi.hat.star <- function(data){</pre>
  model <- glm(formula=0.ring~Temp,data=df,family=binomial(link = logit))</pre>
  predict.data <- data.frame(Temp=c(31,72.27)) #data to predict on
  linear.pred=predict(object = model, newdata = predict.data, #linear part of model
```

## [1] "All values of t are equal to 0.999608782884929 \n Cannot calculate confidence intervals"
## NULL

5 (f) Determine if a quadratic term is needed in the model for the temperature.

```
mod.fit.Ha<-glm(formula=0.ring~Temp+I(Temp^2),data=df,family=binomial(link = logit))
anova(mod.fit2,mod.fit.Ha,test="Chisq")
## Analysis of Deviance Table</pre>
```

```
## Analysis of Deviance Table
##
## Model 1: 0.ring ~ Temp
## Model 2: 0.ring ~ Temp + I(Temp^2)
## Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1 21 20.315
## 2 20 19.389 1 0.92649 0.3358
```

Quadratic term fails to produce significant effect in change in residual deviance and so we fail to reject that the coefficient is actually 0 for the quadratic term.

#### **Final Question**

- 3. In addition to the questions in Question 4 and 5, answer the following questions:
- a. Interpret the main result of your final model in terms of both odds and probability of failure
- b. With the same set of explanatory variables in your final model, estimate a linear regression model. Explain the model results; conduct model diagnostic; and assess the validity of the model assumptions. Would you use the linear regression model or binary logistic regression in this case. Please explain.

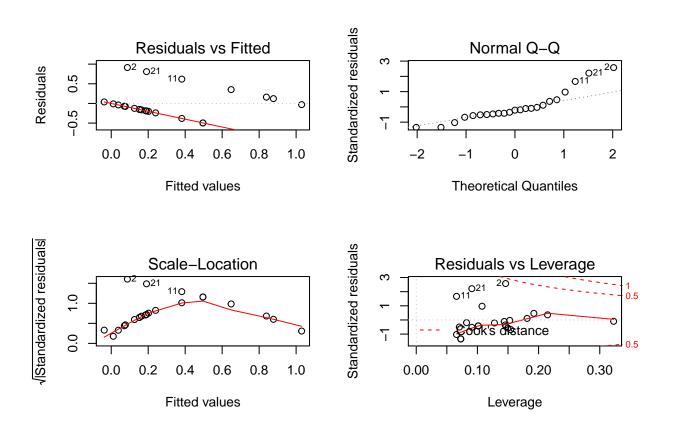
```
mod.lm <- lm(as.numeric(0.ring) ~ Pressure + Temp, data = df)
summary(mod.lm)</pre>
```

```
##
## Call:
  lm(formula = as.numeric(0.ring) ~ Pressure + Temp, data = df)
##
##
  Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
   -0.49600 -0.18816 -0.07650 0.08027
                                         0.91267
##
##
  Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
##
  (Intercept)
                2.658765
                           0.824297
                                       3.225
                                              0.00424 **
                0.001962
                           0.001200
                                       1.635
## Pressure
                                              0.11779
               -0.038136
                           0.011602
                                      -3.287
                                              0.00369 **
##
  Temp
##
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.3837 on 20 degrees of freedom
## Multiple R-squared: 0.3952, Adjusted R-squared: 0.3347
## F-statistic: 6.534 on 2 and 20 DF, p-value: 0.006549
```

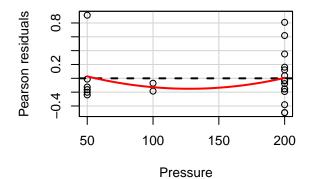
The estimated linear regression model is

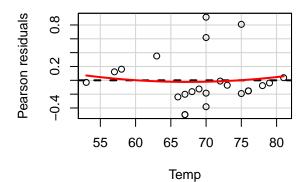
 $\hat{\pi} = 2.658765 + 0.001962$ Pressure -0.038136Temp

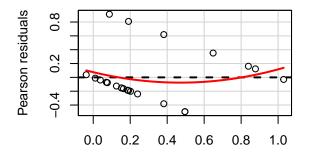
```
par(mfrow=c(2,2))
plot(mod.lm)
```



# par(mfrow=c(1,1)) residualPlots(mod.lm)



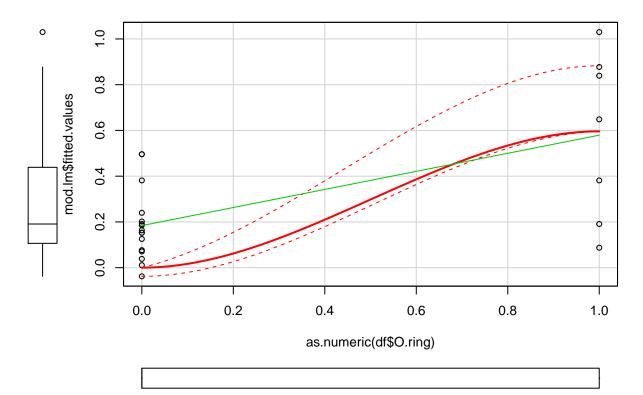




Fitted values

```
## Pressure 0.502 0.621
## Temp 0.387 0.703
## Tukey test 0.676 0.499
```

scatterplot(as.numeric(df\$0.ring), mod.lm\$fitted.values)

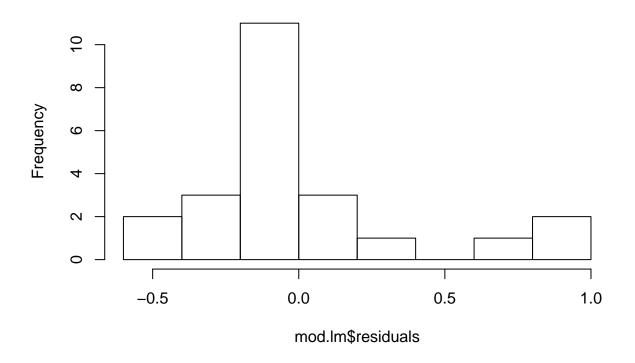


# summary(mod.lm\$fitted.values)

## Min. 1st Qu. Median Mean 3rd Qu. Max. ## -0.03791 0.10640 0.19091 0.30435 0.43879 1.02990

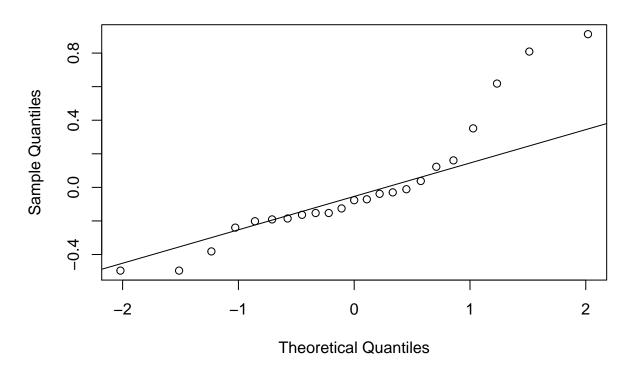
hist(mod.lm\$residuals)

# Histogram of mod.lm\$residuals

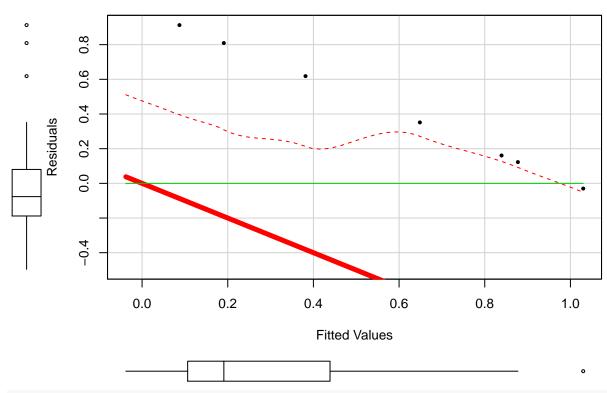


qqnorm(mod.lm\$residuals)
qqline(mod.lm\$residuals)

# Normal Q-Q Plot



# **Residuals vs Fitted Values**



#### shapiro.test(mod.lm\$residuals)

studentized Breusch-Pagan test

## ##

##

```
##
##
    Shapiro-Wilk normality test
##
## data: mod.lm$residuals
## W = 0.86797, p-value = 0.005864
ncvTest(mod.lm)
## Non-constant Variance Score Test
## Variance formula: ~ fitted.values
## Chisquare = 0.1214155
                            Df = 1
                                       p = 0.7275044
library(lmtest)
## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
       as.Date, as.Date.numeric
bptest(mod.lm)
```

```
## data: mod.lm
## BP = 0.086582, df = 2, p-value = 0.9576
durbinWatsonTest(mod.lm)
## lag Autocorrelation D-W Statistic p-value
     1
           -0.01079033
                            1.993267
                                       0.734
## Alternative hypothesis: rho != 0
library(gvlma)
gv.mod.lm <- gvlma(mod.lm)</pre>
summary(gv.mod.lm)
##
## Call:
## lm(formula = as.numeric(0.ring) ~ Pressure + Temp, data = df)
## Residuals:
       Min
                  1Q
                     Median
                                            Max
                                    3Q
## -0.49600 -0.18816 -0.07650 0.08027 0.91267
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 2.658765 0.824297
                                     3.225 0.00424 **
## Pressure
              0.001962
                           0.001200 1.635 0.11779
## Temp
               -0.038136
                         0.011602 -3.287 0.00369 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.3837 on 20 degrees of freedom
## Multiple R-squared: 0.3952, Adjusted R-squared: 0.3347
## F-statistic: 6.534 on 2 and 20 DF, p-value: 0.006549
##
## ASSESSMENT OF THE LINEAR MODEL ASSUMPTIONS
## USING THE GLOBAL TEST ON 4 DEGREES-OF-FREEDOM:
## Level of Significance = 0.05
##
## Call:
##
   gvlma(x = mod.lm)
##
##
                                                       Decision
                      Value p-value
## Global Stat
                      6.4795 0.16609
                                        Assumptions acceptable.
## Skewness
                     5.1920 0.02269 Assumptions NOT satisfied!
## Kurtosis
                     0.6279 0.42814
                                        Assumptions acceptable.
## Link Function
                     0.5405 0.46222
                                        Assumptions acceptable.
## Heteroscedasticity 0.1191 0.72996
                                        Assumptions acceptable.
```