

D208_Performance_Assessment_NBM2_Task_1

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1 D208 Performance Assessment NBM2 Task 1

1.1 Multiple Regression for Predictive Modeling

Ryan L. Buchanan Student ID: 001826691 Masters Data Analytics (12/01/2020) Program Mentor: Dan Estes (385) 432-9281 (MST) rbuch49@wgu.edu

1.1.1 A1. Research Question:

How much many GBs of data will a customer use yearly? Can this be predicted accurately from a list of explanatory variables?

1.1.2 A2. Objectives & Goals:

Stakeholders in the company will benefit by knowing, with some measure of confidence, how much data a customer might predictably use. This will provide weight for decisions in whether or not to expand customer data limits, provide unlimited (or metered) media streaming & expand company cloud computing resources for increased bandwidth demands.

1.1.3 B1. Summary of Assumptions:

Assumptions of a multiple regression model include: * There is a linear relationship between the dependent variables & the independent variables. * The independent variables are not too highly correlated with each other. * y_i observations are selected independently & randomly from the population. * Residuals should normally distributed with a mean of zero.

1.1.4 B2. Tool Benefits:

Python & IPython Jupyter notebooks will be used to support this analysis. Python offers very intuitive, simple & versatile programming style & syntax, as well as a large system of mature packages for data science & machine learning. Since, Python is cross-platform, it will work well whether consumers of the analysis are using Windows PCs or a MacBook laptop. It is fast when compared with other possible programming languages like R or MATLAB (Massaron, p. 8). Also, there is strong support for Python as the most popular data science programming language in popular literature & media (CBTNuggets)

1.1.5 B3. Appropriate Technique:

Multiple regression is an appropriate technique to analyze the research question because our target variable, predicting a real number of GBs per year, is a continuous variable (how much data is used). Also, perhaps there are several (versus simply one) explanatory variables (area type, job, children, age, income, etc.) that will add to our understanding when trying to predict how much data a customer will use in a given year. When adding or removing independent variables from our regression equation, we will find out whether or not they have a positive or negative relationship to our target variable & how that might affect company decisions on marketing segmentation.

1.1.6 C1. Data Goals:

My approach will include: 1. Back up my data and the process I am following as a copy to my machine and, since this is a manageable dataset, to GitHub using command line and gitbash. 2. Read the data set into Python using Pandas' read_csv command. 3. Evaluate the data structure to better understand input data. 4. Naming the dataset as a the variable "churn_df" and subsequent useful slices of the dataframe as "df". 5. Examine potential misspellings, awkward variable naming & missing data. 6. Find outliers that may create or hide statistical significance using histograms. 7. Imputing records missing data with meaningful measures of central tendency (mean, median or mode) or simply remove outliers that are several standard deviations above the mean.

Most relevant to our decision making process is the dependent variable of "Bandwidth_GB_Year" (the average yearly amount of data used, in GB, per customer) which will be our continuous target variable. We need to train & then test our machine on our given dataset to develop a model that will give us an idea of how much data a customer may use given the amounts used by known customers given their respective data points for selected predictor variables.

In cleaning the data, we may discover relevance of the continuous predictor variables: * Children * Income * Outage_sec_perweek * Email * Contacts
* Yearly_equip_failure * Tenure (the number of months the customer has stayed with the provider)
* MonthlyCharge * Bandwidth_GB_Year

Likewise, we may discover relevance of the categorical predictor variables (all binary categorical with only two values, "Yes" or "No", except where noted): * Churn: Whether the customer discontinued service within the last month (yes, no) * Techie: Whether the customer considers themselves technically inclined (based on customer questionnaire when they signed up for services) (yes, no) * Contract: The contract term of the customer (month-to-month, one year, two year) * Port_modem: Whether the customer has a portable modem (yes, no) * Tablet: Whether the customer owns a tablet such as iPad, Surface, etc. (yes, no) * InternetService: Customer's internet service provider (DSL, fiber optic, None) * Phone: Whether the customer has a phone service (yes, no) * Multiple: Whether the customer has multiple lines (yes, no) * OnlineSecurity: Whether the customer has an online security add-on (yes, no) * OnlineBackup: Whether the customer has an online backup add-on (yes, no) * DeviceProtection: Whether the customer has device protection add-on (yes, no) * TechSupport: Whether the customer has a technical support add-on (yes, no) * StreamingTV: Whether the customer has streaming TV (yes, no) * StreamingMovies: Whether the customer has streaming movies (yes, no)

Finally, discrete ordinal predictor variables from the survey responses from customers regarding various customer service features may be relevant in the decision-making process. In the surveys, customers provided ordinal numerical data by rating 8 customer service factors on a scale

of 1 to 8 (1 = most important, 8 = least important):

- Item1: Timely response
- Item2: Timely fixes
- Item3: Timely replacements
- Item4: Reliability
- Item5: Options
- Item6: Respectful response
- Item7: Courteous exchange
- Item8: Evidence of active listening

1.1.7 C2. Summary Statistics:

Discuss the summary statistics, including the target variable and all predictor variables that you will need to gather from the data set to answer the research question.

1.1.8 C3. Steps to Prepare Data:

- Import dataset to Python dataframe.
- Rename columns/variables of survey to easily recognizable features (ex: "Item1" to "TimelyResponse").
- Get a description of dataframe, structure (columns & rows) & data types.
- View summary statistics.
- Drop less meaningful identifying (ex: "Customer_id") & demographic columns (ex: zip code) from dataframe.
- Check for records with missing data & impute missing data with meaningful measures of central tendency (mean, median or mode) or simply remove outliers that are several standard deviations above the mean.
- Create dummy variables in order to encoded categorical, yes/no data points into 1/0 numerical values.
- View univariate & bivariate visualizations.
- Place Bandwidth_GB_Year at end of dataframe
- Finally, the prepared dataset will be extracted & provided as "churn_prepared.csv"

```
[1]: # Increase Jupyter display cell-width
from IPython.core.display import display, HTML
display(HTML("<style>.container { width:75% !important; }</style>"))
```

<IPython.core.display.HTML object>

```
[2]: # Standard data science imports
import numpy as np
import pandas as pd
from pandas import Series, DataFrame

# Visualization libraries
import seaborn as sns
```

```

import matplotlib.pyplot as plt
%matplotlib inline

# Statistics packages
import pylab
from pylab import rcParams
import statsmodels.api as sm
import statistics
from scipy import stats

# Scikit-learn
import sklearn
from sklearn import preprocessing
from sklearn.linear_model import LinearRegression
from sklearn.model_selection import train_test_split
from sklearn import metrics
from sklearn.metrics import classification_report

# Import chisquare from SciPy.stats
from scipy.stats import chisquare
from scipy.stats import chi2_contingency

# Ignore Warning Code
import warnings
warnings.filterwarnings('ignore')

```

/usr/local/lib/python3.7/dist-packages/statsmodels/tools/_testing.py:19:
FutureWarning: pandas.util.testing is deprecated. Use the functions in the
public API at pandas.testing instead.
import pandas.util.testing as tm

```

[3]: # Change color of Matplotlib font
import matplotlib as mpl

COLOR = 'white'
mpl.rcParams['text.color'] = COLOR
mpl.rcParams['axes.labelcolor'] = COLOR
mpl.rcParams['xtick.color'] = COLOR
mpl.rcParams['ytick.color'] = COLOR

```

```

[4]: # Load data set into Pandas dataframe
churn_df = pd.read_csv('churn_clean.csv')

# Rename last 8 survey columns for better description of variables
churn_df.rename(columns = {'Item1': 'TimelyResponse',
                           'Item2': 'Fixes',
                           'Item3': 'Replacements',

```

```

        'Item4': 'Reliability',
        'Item5': 'Options',
        'Item6': 'Respectfulness',
        'Item7': 'Courteous',
        'Item8': 'Listening'},
    inplace=True)

```

```

[5]: # Display Churn dataframe
     churn_df

```

```

[5]:   CaseOrder  Customer_id  ...  Courteous  Listening
0         1      K409198  ...         3         4
1         2      S120509  ...         4         4
2         3      K191035  ...         3         3
3         4       D90850  ...         3         3
4         5      K662701  ...         4         5
...     ...      ...  ...     ...     ...
9995    9996      M324793  ...         2         3
9996    9997      D861732  ...         2         5
9997    9998      I243405  ...         4         5
9998    9999      I641617  ...         5         4
9999   10000      T38070  ...         4         1

```

[10000 rows x 50 columns]

```

[6]: # List of Dataframe Columns
     df = churn_df.columns
     print(df)

```

```

Index(['CaseOrder', 'Customer_id', 'Interaction', 'UID', 'City', 'State',
      'County', 'Zip', 'Lat', 'Lng', 'Population', 'Area', 'TimeZone', 'Job',
      'Children', 'Age', 'Income', 'Marital', 'Gender', 'Churn',
      'Outage_sec_perweek', 'Email', 'Contacts', 'Yearly equip_failure',
      'Techie', 'Contract', 'Port_modem', 'Tablet', 'InternetService',
      'Phone', 'Multiple', 'OnlineSecurity', 'OnlineBackup',
      'DeviceProtection', 'TechSupport', 'StreamingTV', 'StreamingMovies',
      'PaperlessBilling', 'PaymentMethod', 'Tenure', 'MonthlyCharge',
      'Bandwidth_GB_Year', 'TimelyResponse', 'Fixes', 'Replacements',
      'Reliability', 'Options', 'Respectfulness', 'Courteous', 'Listening'],
      dtype='object')

```

```

[7]: # Find number of records and columns of dataset
     churn_df.shape

```

```

[7]: (10000, 50)

```

```

[8]: # Describe Churn dataset statistics
     churn_df.describe()

```

```
[8]:
```

	CaseOrder	Zip	...	Courteous	Listening
count	10000.00000	10000.000000	...	10000.000000	10000.000000
mean	5000.50000	49153.319600	...	3.509500	3.495600
std	2886.89568	27532.196108	...	1.028502	1.028633
min	1.00000	601.000000	...	1.000000	1.000000
25%	2500.75000	26292.500000	...	3.000000	3.000000
50%	5000.50000	48869.500000	...	4.000000	3.000000
75%	7500.25000	71866.500000	...	4.000000	4.000000
max	10000.00000	99929.000000	...	7.000000	8.000000

[8 rows x 23 columns]

```
[9]: # Remove less meaningful demographic variables from statistics description
churn_df = churn_df.drop(columns=['CaseOrder', 'Customer_id', 'Interaction',
    → 'UID', 'City',
    → 'Population',
    → 'Area', 'TimeZone', 'Job', 'Marital',
    → 'PaymentMethod'])
churn_df.describe()
```

```
[9]:
```

	Children	Age	...	Courteous	Listening
count	10000.0000	10000.000000	...	10000.000000	10000.000000
mean	2.0877	53.078400	...	3.509500	3.495600
std	2.1472	20.698882	...	1.028502	1.028633
min	0.0000	18.000000	...	1.000000	1.000000
25%	0.0000	35.000000	...	3.000000	3.000000
50%	1.0000	53.000000	...	4.000000	3.000000
75%	3.0000	71.000000	...	4.000000	4.000000
max	10.0000	89.000000	...	7.000000	8.000000

[8 rows x 18 columns]

```
[10]: # Discover missing data points within dataset
data_nulls = churn_df.isnull().sum()
print(data_nulls)
```

Children	0
Age	0
Income	0
Gender	0
Churn	0
Outage_sec_perweek	0
Email	0
Contacts	0
Yearly_equip_failure	0
Techie	0
Contract	0
Port_modem	0

Tablet	0
InternetService	0
Phone	0
Multiple	0
OnlineSecurity	0
OnlineBackup	0
DeviceProtection	0
TechSupport	0
StreamingTV	0
StreamingMovies	0
PaperlessBilling	0
Tenure	0
MonthlyCharge	0
Bandwidth_GB_Year	0
TimelyResponse	0
Fixes	0
Replacements	0
Reliability	0
Options	0
Respectfulness	0
Courteous	0
Listening	0

dtype: int64

1.1.9 Dummy variable data preparation

Turn all yes/no into dummy variables a la Performance Lab Python.

```
[11]: churn_df['DummyGender'] = [1 if v == 'Male' else 0 for v in churn_df['Gender']]
churn_df['DummyChurn'] = [1 if v == 'Male' else 0 for v in churn_df['Churn']]
churn_df['DummyTechie'] = [1 if v == 'Yes' else 0 for v in churn_df['Techie']]
churn_df['DummyContract'] = [1 if v == 'Two Year' else 0 for v in churn_df['Contract']]
churn_df['DummyPort_modem'] = [1 if v == 'Yes' else 0 for v in churn_df['Port_modem']]
churn_df['DummyTablet'] = [1 if v == 'Yes' else 0 for v in churn_df['Tablet']]
churn_df['DummyInternetService'] = [1 if v == 'Fiber Optic' else 0 for v in churn_df['InternetService']]
churn_df['DummyPhone'] = [1 if v == 'Yes' else 0 for v in churn_df['Phone']]
churn_df['DummyMultiple'] = [1 if v == 'Yes' else 0 for v in churn_df['Multiple']]
churn_df['DummyOnlineSecurity'] = [1 if v == 'Yes' else 0 for v in churn_df['OnlineSecurity']]
churn_df['DummyOnlineBackup'] = [1 if v == 'Yes' else 0 for v in churn_df['OnlineBackup']]
churn_df['DummyDeviceProtection'] = [1 if v == 'Yes' else 0 for v in churn_df['DeviceProtection']]
```

```
churn_df['DummyTechSupport'] = [1 if v == 'Yes' else 0 for v in churn_df['TechSupport']]
churn_df['DummyStreamingTV'] = [1 if v == 'Yes' else 0 for v in churn_df['StreamingTV']]
churn_df['DummyStreamingMovies'] = [1 if v == 'Yes' else 0 for v in churn_df['StreamingMovies']]
churn_df['DummyPaperlessBilling'] = [1 if v == 'Yes' else 0 for v in churn_df['PaperlessBilling']]
```

```
[12]: # Drop original categorical features from dataframe
churn_df = churn_df.drop(columns=['Gender', 'Churn', 'Techie', 'Contract', 'Port_modem', 'Tablet',
                                'InternetService', 'Phone', 'Multiple', 'OnlineSecurity',
                                'OnlineBackup', 'DeviceProtection', 'TechSupport',
                                'StreamingTV', 'StreamingMovies', 'PaperlessBilling'])
churn_df.describe()
```

```
[12]:
```

	Children	Age	...	DummyStreamingTV	DummyPaperlessBilling
count	10000.0000	10000.000000	...	10000.000000	10000.000000
mean	2.0877	53.078400	...	0.492900	0.588200
std	2.1472	20.698882	...	0.499975	0.492184
min	0.0000	18.000000	...	0.000000	0.000000
25%	0.0000	35.000000	...	0.000000	0.000000
50%	1.0000	53.000000	...	0.000000	1.000000
75%	3.0000	71.000000	...	1.000000	1.000000
max	10.0000	89.000000	...	1.000000	1.000000

[8 rows x 33 columns]

```
[13]: df = churn_df.columns
print(df)
```

```
Index(['Children', 'Age', 'Income', 'Outage_sec_perweek', 'Email', 'Contacts',
      'Yearly_equip_failure', 'Tenure', 'MonthlyCharge', 'Bandwidth_GB_Year',
      'TimelyResponse', 'Fixes', 'Replacements', 'Reliability', 'Options',
      'Respectfulness', 'Courteous', 'Listening', 'DummyGender', 'DummyChurn',
      'DummyTechie', 'DummyContract', 'DummyPort_modem', 'DummyTablet',
      'DummyInternetService', 'DummyPhone', 'DummyMultiple',
      'DummyOnlineSecurity', 'DummyOnlineBackup', 'DummyDeviceProtection',
      'DummyTechSupport', 'DummyStreamingTV', 'DummyPaperlessBilling'],
      dtype='object')
```

```
[14]: # Move Bandwidth_GB_Year to end of dataset as target
churn_df = churn_df[['Children', 'Age', 'Income', 'Outage_sec_perweek', 'Email', 'Contacts',
```



```
'Yearly_equip_failure', 'Tenure', 'MonthlyCharge',
'TimelyResponse', 'Fixes', 'Replacements',
'Reliability', 'Options', 'Respectfulness', 'Courteous', 'Listening',
'DummyGender', 'DummyChurn', 'DummyTechie', 'DummyContract',
'DummyPort_modem', 'DummyTablet', 'DummyInternetService', 'DummyPhone',
'DummyMultiple', 'DummyOnlineSecurity', 'DummyOnlineBackup',
'DummyDeviceProtection', 'DummyTechSupport', 'DummyStreamingTV',
'DummyPaperlessBilling', 'Bandwidth_GB_Year']]
```

```
[15]: df = churn_df.columns
print(df)
```

```
Index(['Children', 'Age', 'Income', 'Outage_sec_perweek', 'Email', 'Contacts',
'Yearly_equip_failure', 'Tenure', 'MonthlyCharge', 'TimelyResponse',
'Fixes', 'Replacements', 'Reliability', 'Options', 'Respectfulness',
'Courteous', 'Listening', 'DummyGender', 'DummyChurn', 'DummyTechie',
'DummyContract', 'DummyPort_modem', 'DummyTablet',
'DummyInternetService', 'DummyPhone', 'DummyMultiple',
'DummyOnlineSecurity', 'DummyOnlineBackup', 'DummyDeviceProtection',
'DummyTechSupport', 'DummyStreamingTV', 'DummyPaperlessBilling',
'Bandwidth_GB_Year'],
dtype='object')
```

1.1.10 C4. Visualizations:

Generate univariate and bivariate visualizations of the distributions of variables in the cleaned data set. Include the target variable in your bivariate visualizations.

```
[16]: # Visualize missing values in dataset

# Install appropriate library
!pip install missingno

# Importing the libraries
import missingno as msno

# Visualize missing values as a matrix
msno.matrix(churn_df);
```

Requirement already satisfied: missingno in /usr/local/lib/python3.7/dist-packages (0.4.2)

Requirement already satisfied: numpy in /usr/local/lib/python3.7/dist-packages (from missingno) (1.19.5)

Requirement already satisfied: seaborn in /usr/local/lib/python3.7/dist-packages (from missingno) (0.11.1)

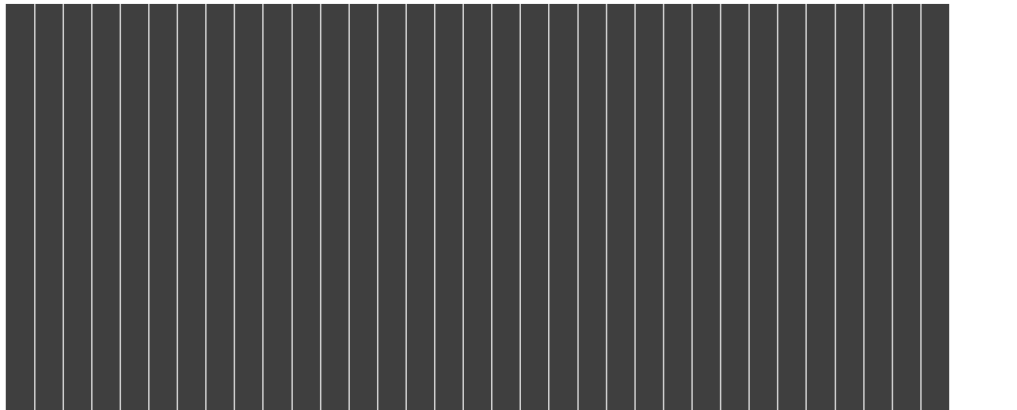
Requirement already satisfied: scipy in /usr/local/lib/python3.7/dist-packages (from missingno) (1.4.1)

Requirement already satisfied: matplotlib in /usr/local/lib/python3.7/dist-

```

packages (from missingno) (3.2.2)
Requirement already satisfied: pandas>=0.23 in /usr/local/lib/python3.7/dist-
packages (from seaborn->missingno) (1.1.5)
Requirement already satisfied: python-dateutil>=2.1 in /usr/local/lib/python3.7
/dist-packages (from matplotlib->missingno) (2.8.1)
Requirement already satisfied: cycler>=0.10 in /usr/local/lib/python3.7/dist-
packages (from matplotlib->missingno) (0.10.0)
Requirement already satisfied: kiwisolver>=1.0.1 in /usr/local/lib/python3.7
/dist-packages (from matplotlib->missingno) (1.3.1)
Requirement already satisfied: pyparsing!=2.0.4,!=2.1.2,!=2.1.6,>=2.0.1 in
/usr/local/lib/python3.7/dist-packages (from matplotlib->missingno) (2.4.7)
Requirement already satisfied: pytz>=2017.2 in /usr/local/lib/python3.7/dist-
packages (from pandas>=0.23->seaborn->missingno) (2018.9)
Requirement already satisfied: six>=1.5 in /usr/local/lib/python3.7/dist-
packages (from python-dateutil>=2.1->matplotlib->missingno) (1.15.0)

```



```

[17]: '''No need to impute an missing values as the dataset appears complete/
      →cleaned'''
      # Impute missing fields for variables Children, Age, Income, Tenure and
      →Bandwidth_GB_Year with median or mean
      # churn_df['Children'] = churn_df['Children'].fillna(churn_df['Children'].
      →median())
      # churn_df['Age'] = churn_df['Age'].fillna(churn_df['Age'].median())
      # churn_df['Income'] = churn_df['Income'].fillna(churn_df['Income'].median())
      # churn_df['Tenure'] = churn_df['Tenure'].fillna(churn_df['Tenure'].median())
      # churn_df['Bandwidth_GB_Year'] = churn_df['Bandwidth_GB_Year'].
      →fillna(churn_df['Bandwidth_GB_Year'].median())

```

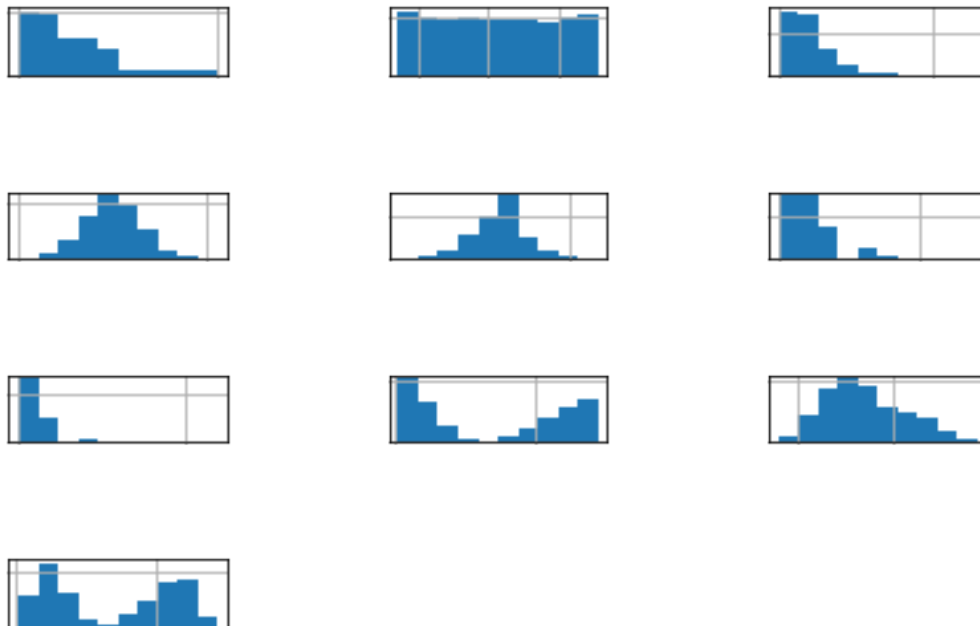
```

[17]: 'No need to impute an missing values as the dataset appears complete/cleaned'

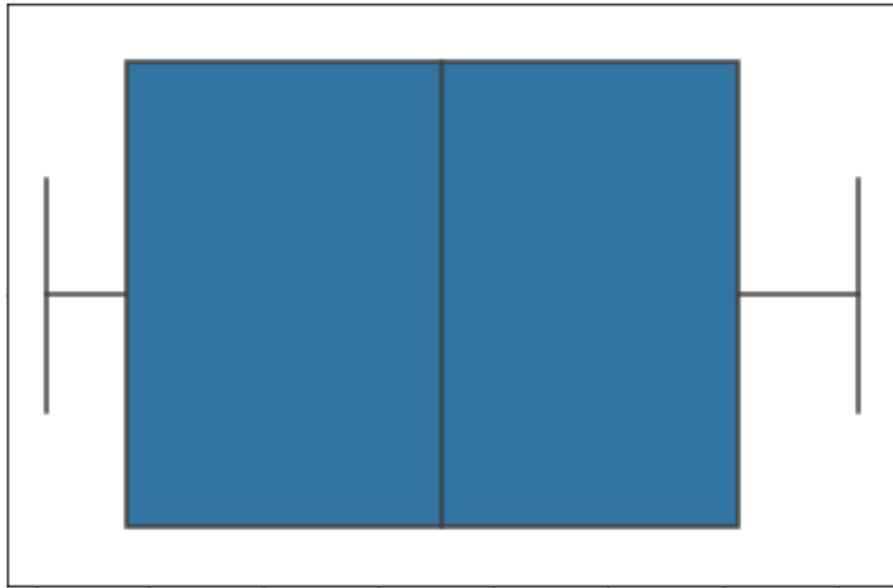
```

1.2 Univariate Statistics

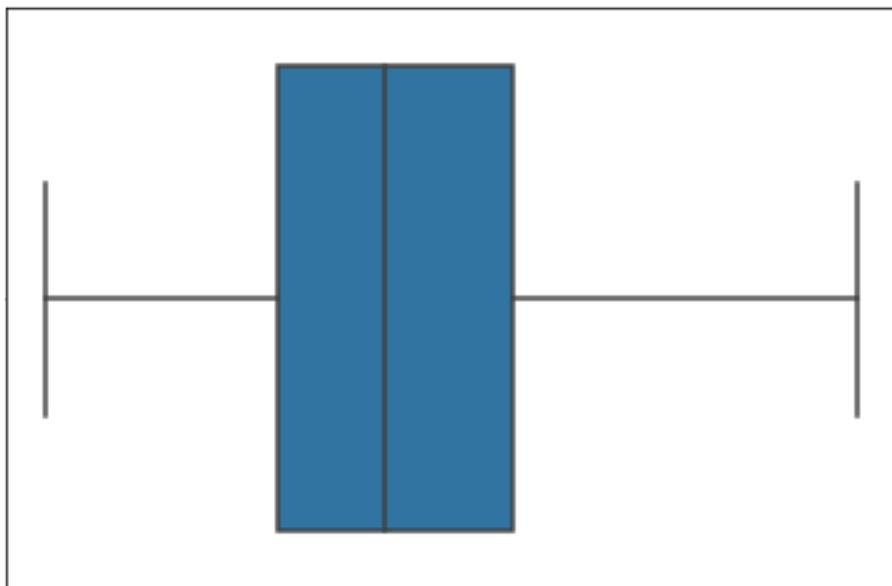
```
[18]: # Create histograms of continuous variables
churn_df[['Children', 'Age', 'Income', 'Outage_sec_perweek', 'Email',
          'Contacts', 'Yearly equip_failure', 'Tenure', 'MonthlyCharge',
          'Bandwidth_GB_Year']].hist()
plt.savefig('churn_pyplot.jpg')
plt.tight_layout()
```



```
[19]: # Create Seaborn boxplots for continuous variables
sns.boxplot('Tenure', data = churn_df)
plt.show()
```



```
[20]: sns.boxplot('MonthlyCharge', data = churn_df)  
plt.show()
```



```
[21]: sns.boxplot('Bandwidth_GB_Year', data = churn_df)
plt.show()
```



1.2.1 It appears that anomalies have been removed from the dataset present "churn_clean.csv" as there are no remaining outliers.

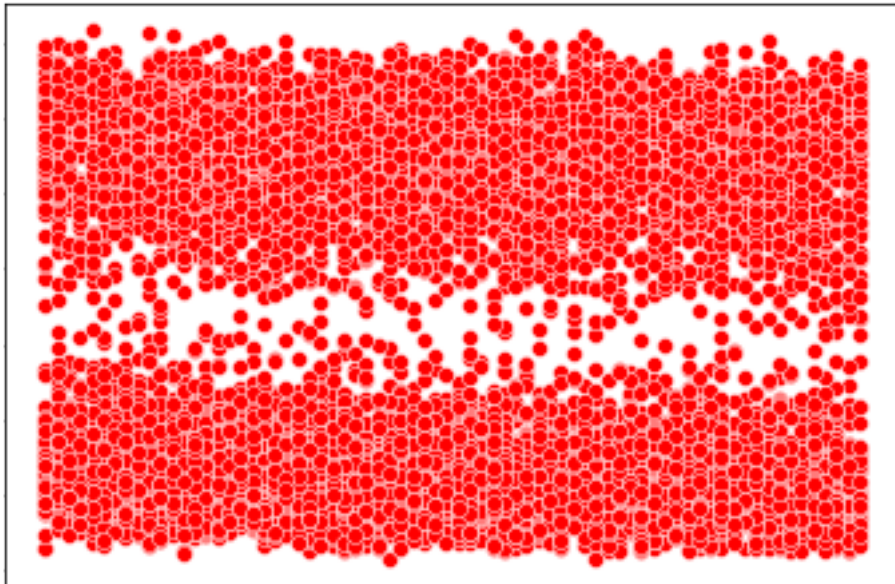
1.3 Bivariate Statistics

1.3.1 Let's run some scatterplots to get an idea of our linear relationships with our target variable of "Bandwidth_GB_Year" usage & some of the respective predictor variables.

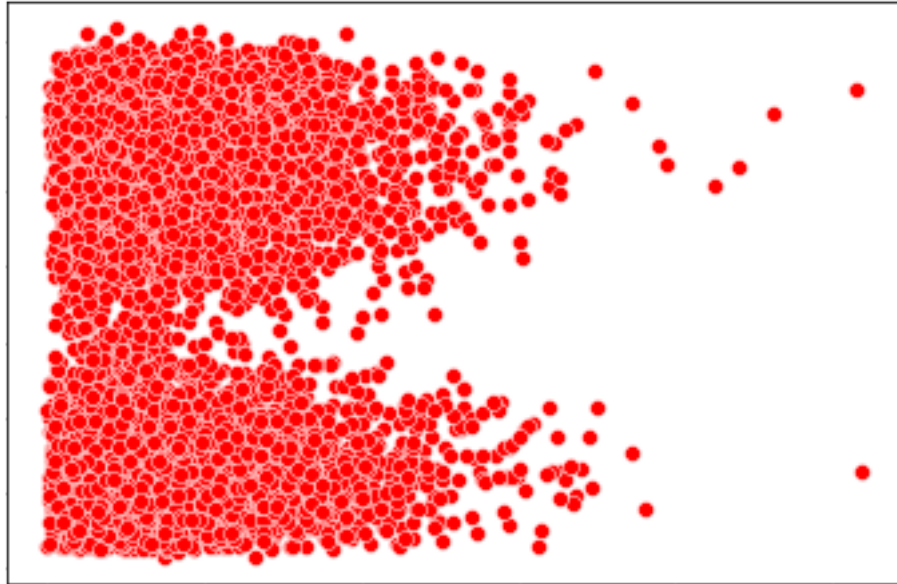
```
[22]: # Run scatterplots to show direct or inverse relationships between target &
      ↪ independent variables
sns.scatterplot(x=churn_df['Children'], y=churn_df['Bandwidth_GB_Year'],
      ↪ color='red')
plt.show();
```



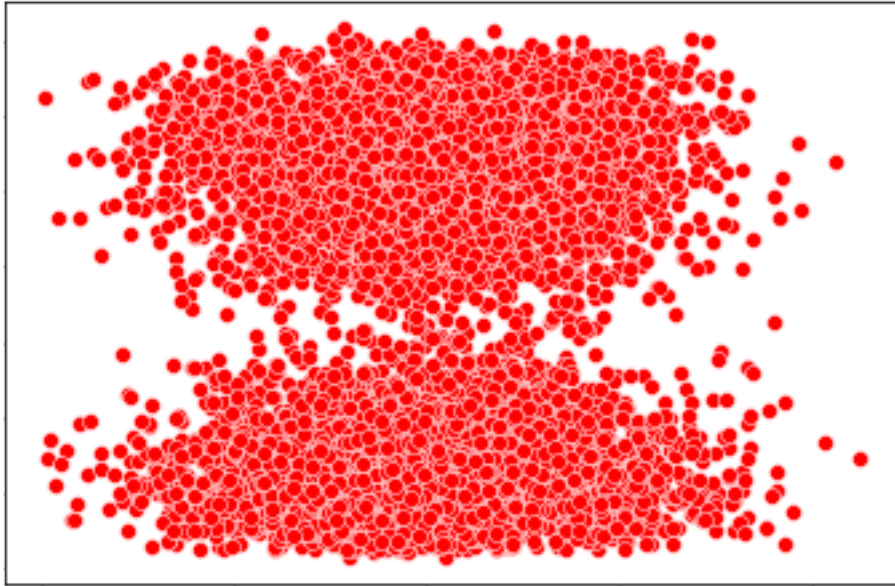
```
[23]: sns.scatterplot(x=churn_df['Age'], y=churn_df['Bandwidth_GB_Year'], color='red')  
plt.show();
```



```
[24]: sns.scatterplot(x=churn_df['Income'], y=churn_df['Bandwidth_GB_Year'],  
    →color='red')  
plt.show();
```



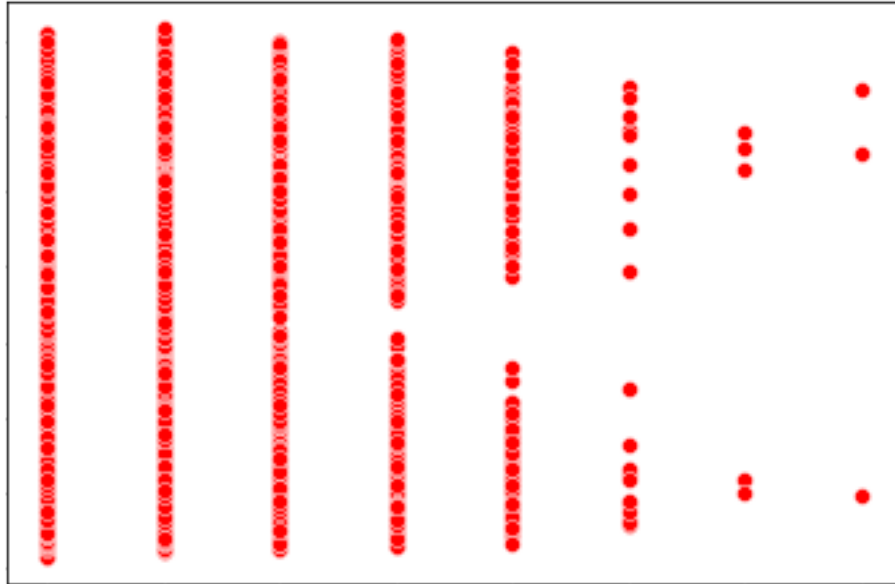
```
[25]: sns.scatterplot(x=churn_df['Outage_sec_perweek'], y=churn_df['Bandwidth_GB_Year'],  
    →color='red')  
plt.show();
```



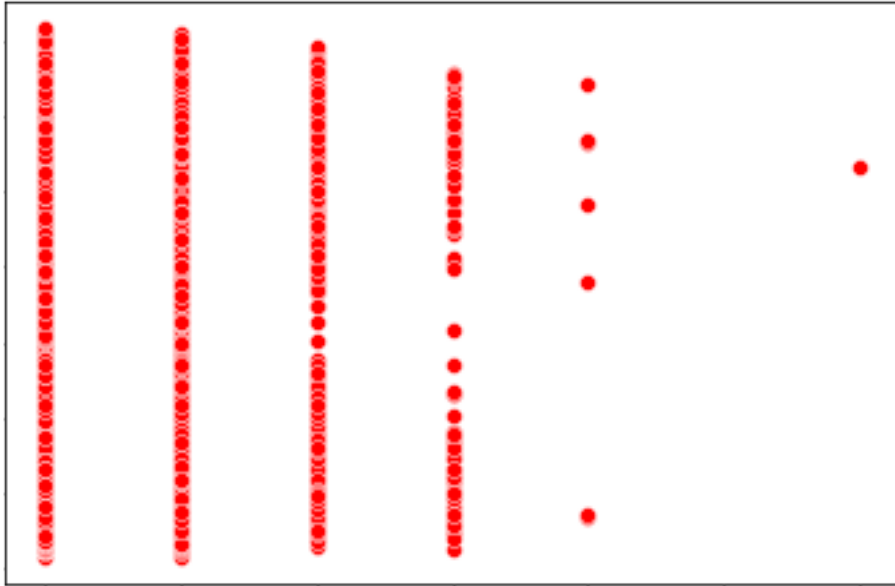
```
[26]: sns.scatterplot(x=churn_df['Email'], y=churn_df['Bandwidth_GB_Year'],  
    ↪color='red')  
plt.show();
```



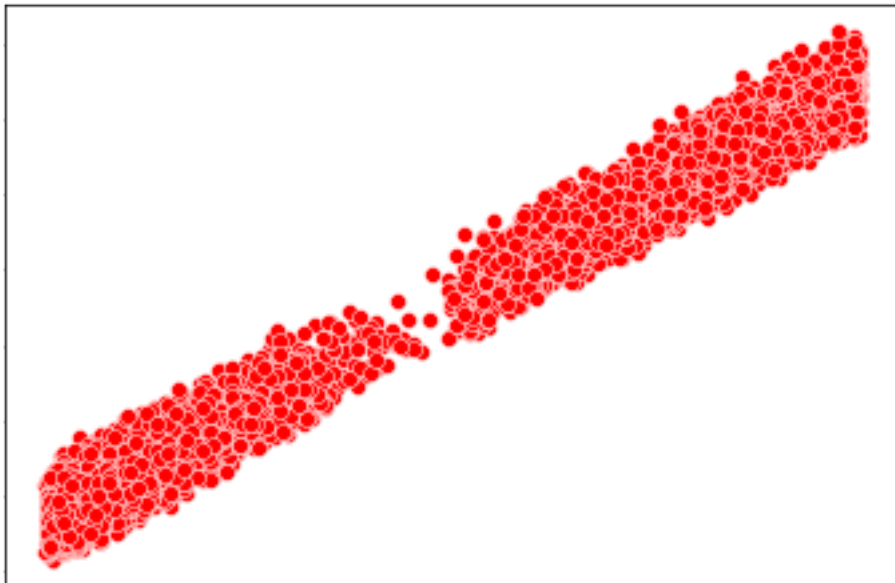

```
[27]: sns.scatterplot(x=churn_df['Contacts'], y=churn_df['Bandwidth_GB_Year'],
    →color='red')
plt.show();
```



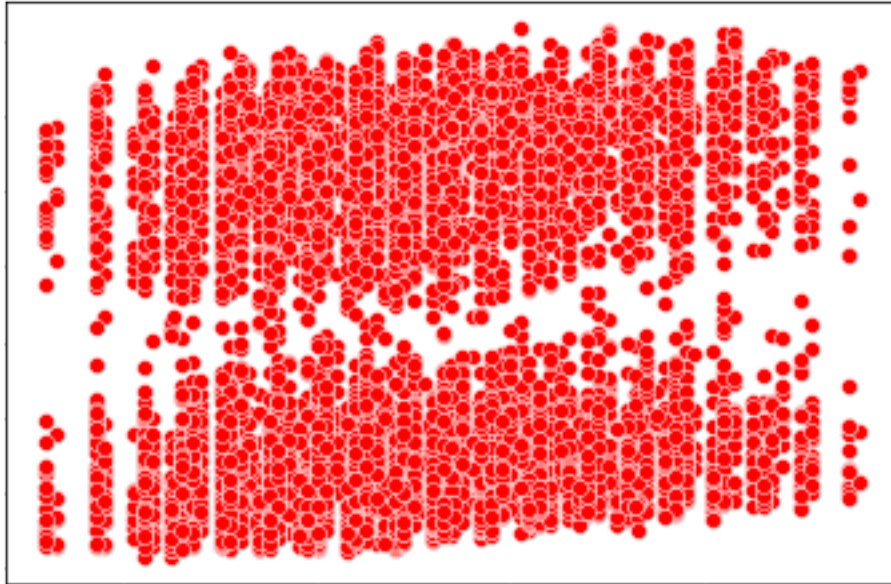
```
[28]: sns.scatterplot(x=churn_df['Yearly equip_failure'],
    →y=churn_df['Bandwidth_GB_Year'], color='red')
plt.show();
```



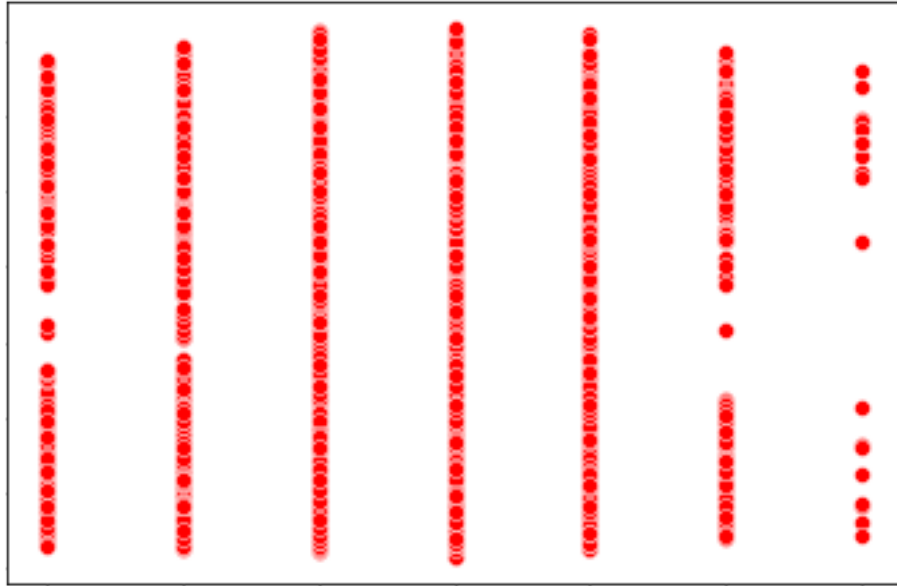
```
[29]: sns.scatterplot(x=churn_df['Tenure'], y=churn_df['Bandwidth_GB_Year'],  
    ↪color='red')  
plt.show();
```



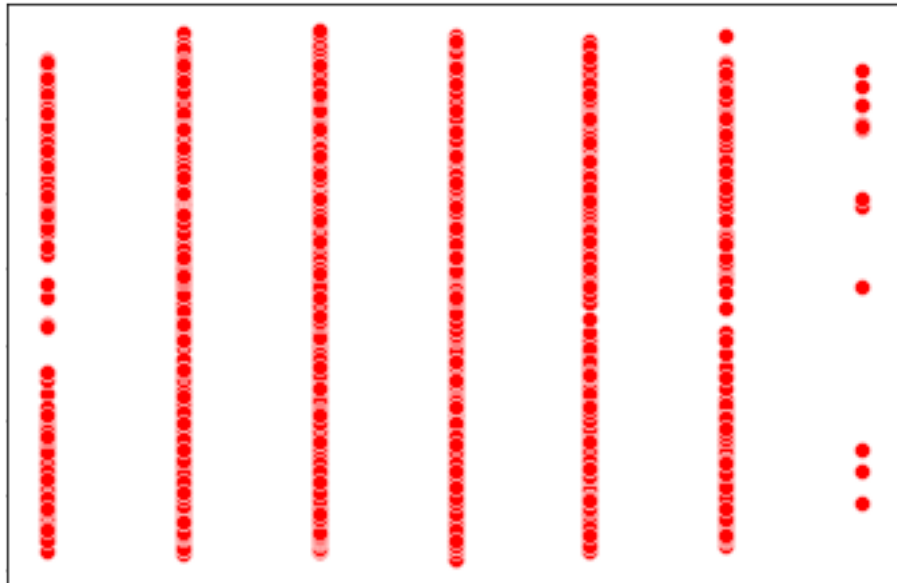
```
[30]: sns.scatterplot(x=churn_df['MonthlyCharge'], y=churn_df['Bandwidth_GB_Year'],  
    ↪color='red')  
plt.show();
```



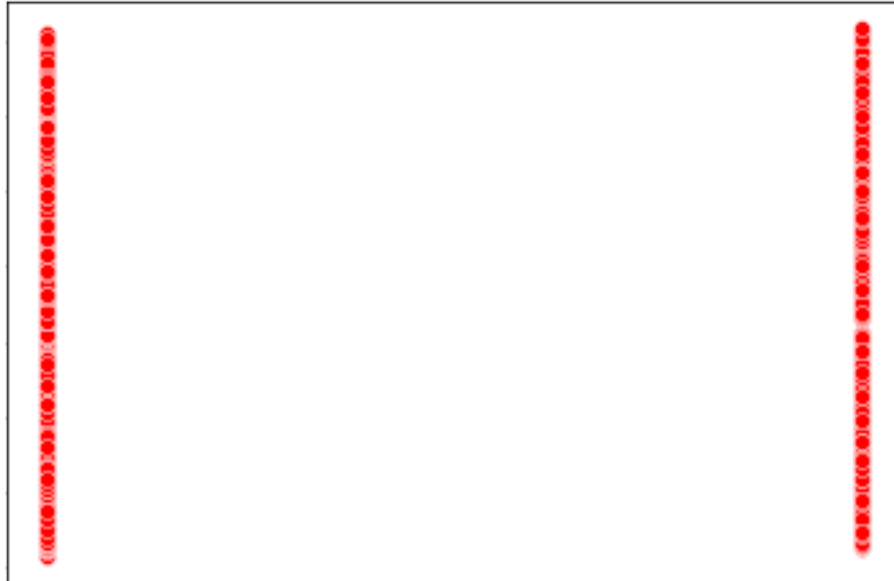
```
[31]: sns.scatterplot(x=churn_df['TimelyResponse'], y=churn_df['Bandwidth_GB_Year'],  
    ↪color='red')  
plt.show();
```



```
[32]: sns.scatterplot(x=churn_df['Fixes'], y=churn_df['Bandwidth_GB_Year'],
    ↪color='red')
plt.show();
```



```
[33]: sns.scatterplot(x=churn_df['DummyTechie'], y=churn_df['Bandwidth_GB_Year'],
    →color='red')
plt.show();
```



1.3.2 C5. Prepared Dataset:

Provide a copy of the prepared data set.

```
[34]: # Extract Clean dataset
churn_df.to_csv('churn_prepared.csv')
```

1.3.3 D1. Initial Model

Construct an initial multiple regression model from all predictors that were identified in Part C2.

```
[35]: """Develop the initial estimated regression equation that could be used to
    →predict the Bandwidth_GB_Year, given the only continuous variables"""
churn_df['intercept'] = 1
lm_bandwidth = sm.OLS(churn_df['Bandwidth_GB_Year'], churn_df[['Children',
    →'Age',
    →'Income',
    →'Outage_sec_perweek',
    →'Email',
    →'Contacts'],
```

```

→'Yearly_equip_failure',
→'MonthlyCharge',
→'TimelyResponse', 'Fixes',
→'Reliability',
→'Respectfulness',
→'Listening',
→fit()
print(lm_bandwidth.summary())

```

OLS Regression Results

```

=====
Dep. Variable:      Bandwidth_GB_Year    R-squared:              0.989
Model:              OLS                  Adj. R-squared:         0.989
Method:             Least Squares        F-statistic:           5.329e+04
Date:               Thu, 15 Jul 2021     Prob (F-statistic):    0.00
Time:               00:48:12             Log-Likelihood:        -68489.
No. Observations:   10000                AIC:                   1.370e+05
Df Residuals:       9982                 BIC:                   1.371e+05
Df Model:           17
Covariance Type:    nonrobust
=====

```

```

=====
                                coef    std err          t      P>|t|      [0.025
0.975]
-----
Children                30.9275      1.065     29.050      0.000     28.841
33.014
Age                   -3.3206      0.110    -30.065      0.000     -3.537
-3.104
Income                 9.976e-05    8.1e-05      1.231     0.218    -5.91e-05
0.000
Outage_sec_perweek    -0.3501      0.768     -0.456     0.649     -1.856
1.156
Email                 -0.2792      0.755     -0.370     0.712     -1.759
1.201
Contacts               2.9707      2.312      1.285     0.199     -1.562
7.503
Yearly_equip_failure   0.9080      3.593      0.253     0.801     -6.136
7.952

```

Tenure	82.0113	0.086	948.882	0.000	81.842
82.181					
MonthlyCharge	3.2768	0.053	61.585	0.000	3.173
3.381					
TimelyResponse	-8.8961	3.271	-2.720	0.007	-15.308
-2.484					
Fixes	3.4660	3.064	1.131	0.258	-2.541
9.473					
Replacements	-0.1771	2.812	-0.063	0.950	-5.690
5.335					
Reliability	-0.2697	2.515	-0.107	0.915	-5.199
4.659					
Options	2.7199	2.611	1.042	0.298	-2.398
7.838					
Respectfulness	1.7157	2.689	0.638	0.523	-3.554
6.986					
Courteous	-1.3482	2.543	-0.530	0.596	-6.333
3.637					
Listening	5.7844	2.420	2.390	0.017	1.040
10.529					
intercept	95.8754	26.146	3.667	0.000	44.624
147.127					

Omnibus:	12280.983	Durbin-Watson:	1.979
Prob(Omnibus):	0.000	Jarque-Bera (JB):	968.853
Skew:	0.449	Prob(JB):	4.13e-211
Kurtosis:	1.768	Cond. No.	5.60e+05

Warnings:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 5.6e+05. This might indicate that there are strong multicollinearity or other numerical problems.

```
[36]: churn_df_dummies = churn_df.columns
      print(churn_df_dummies)
```

```
Index(['Children', 'Age', 'Income', 'Outage_sec_perweek', 'Email', 'Contacts',
      'Yearly_equip_failure', 'Tenure', 'MonthlyCharge', 'TimelyResponse',
      'Fixes', 'Replacements', 'Reliability', 'Options', 'Respectfulness',
      'Courteous', 'Listening', 'DummyGender', 'DummyChurn', 'DummyTechie',
      'DummyContract', 'DummyPort_modem', 'DummyTablet',
      'DummyInternetService', 'DummyPhone', 'DummyMultiple',
      'DummyOnlineSecurity', 'DummyOnlineBackup', 'DummyDeviceProtection',
      'DummyTechSupport', 'DummyStreamingTV', 'DummyPaperlessBilling',
      'Bandwidth_GB_Year', 'intercept'],
      dtype='object')
```

1.3.4 Now, let's run a model including all encoded categorical dummy variables.

```
[37]: """Model including all dummy variables"""
churn_df['intercept'] = 1
lm_bandwidth = sm.OLS(churn_df['Bandwidth_GB_Year'], churn_df[['Children',
→ 'Age',
→ 'Outage_sec_perweek',
→ 'Contacts',
→ 'Yearly_equip_failure',
→ 'DummyContract',
→ 'DummyPort_modem', 'DummyTablet',
→ 'DummyInternetService', 'DummyPhone',
→ 'DummyOnlineSecurity',
→ 'DummyOnlineBackup', 'DummyDeviceProtection',
→ 'DummyTechSupport', 'DummyStreamingTV',
→ 'DummyPaperlessBilling',
→ 'MonthlyCharge',
→ 'TimelyResponse', 'Fixes',
→ 'Reliability',
→ 'Respectfulness',
→ 'Listening',
→ 'Income',
→ 'Email',
→ 'Tenure',
→ 'Replacements',
→ 'Options',
→ 'Courteous',
→ 'intercept']]
→ fit()
print(lm_bandwidth.summary())
```

OLS Regression Results

```
=====
Dep. Variable:      Bandwidth_GB_Year      R-squared:      0.996
Model:              OLS                    Adj. R-squared:  0.996
Method:             Least Squares          F-statistic:    8.675e+04
Date:               Thu, 15 Jul 2021        Prob (F-statistic): 0.00
```


Time: 00:48:28 Log-Likelihood: -63241.
 No. Observations: 10000 AIC: 1.265e+05
 Df Residuals: 9969 BIC: 1.268e+05
 Df Model: 30
 Covariance Type: nonrobust

	coef	std err	t	P> t	[0.025
0.975]					
Children	30.4177	0.631	48.226	0.000	29.181
31.654					
Age	-3.3153	0.065	-50.671	0.000	-3.444
-3.187					
Income	9.27e-06	4.8e-05	0.193	0.847	-8.48e-05
0.000					
Outage_sec_perweek	-0.5259	0.455	-1.156	0.248	-1.418
0.366					
Email	0.1812	0.448	0.405	0.686	-0.696
1.058					
Contacts	2.1263	1.370	1.552	0.121	-0.559
4.811					
Yearly equip_failure	1.2859	2.129	0.604	0.546	-2.887
5.459					
DummyTechie	0.6193	3.621	0.171	0.864	-6.478
7.717					
DummyContract	3.9328	3.151	1.248	0.212	-2.244
10.110					
DummyPort_modem	0.4710	2.707	0.174	0.862	-4.835
5.777					
DummyTablet	-1.9813	2.959	-0.670	0.503	-7.781
3.819					
DummyInternetService	-373.7111	2.980	-125.411	0.000	-379.552
-367.870					
DummyPhone	-2.1515	4.658	-0.462	0.644	-11.282
6.979					
DummyMultiple	-76.0773	3.153	-24.130	0.000	-82.257
-69.897					
DummyOnlineSecurity	67.4949	2.830	23.850	0.000	61.948
73.042					
DummyOnlineBackup	-12.6597	2.931	-4.319	0.000	-18.406
-6.914					
DummyDeviceProtection	24.8879	2.807	8.867	0.000	19.386
30.390					
DummyTechSupport	-52.5816	2.857	-18.405	0.000	-58.182
-46.981					
DummyStreamingTV	30.4799	3.372	9.039	0.000	23.870

37.090					
DummyPaperlessBilling	-2.6415	2.752	-0.960	0.337	-8.035
2.752					
Tenure	81.9913	0.051	1600.655	0.000	81.891
82.092					
MonthlyCharge	4.7092	0.048	97.416	0.000	4.614
4.804					
TimelyResponse	-1.4340	1.939	-0.739	0.460	-5.236
2.368					
Fixes	1.6837	1.817	0.927	0.354	-1.878
5.245					
Replacements	-2.4128	1.666	-1.448	0.148	-5.679
0.853					
Reliability	-1.5594	1.489	-1.047	0.295	-4.479
1.360					
Options	0.5285	1.547	0.342	0.733	-2.504
3.561					
Respectfulness	1.2322	1.593	0.774	0.439	-1.890
4.354					
Courteous	0.4649	1.507	0.308	0.758	-2.490
3.419					
Listening	3.1708	1.434	2.212	0.027	0.361
5.981					
intercept	33.1742	16.379	2.025	0.043	1.069
65.280					
=====					
Omnibus:	871.245	Durbin-Watson:	1.970		
Prob(Omnibus):	0.000	Jarque-Bera (JB):	697.849		
Skew:	-0.559	Prob(JB):	2.91e-152		
Kurtosis:	2.349	Cond. No.	5.95e+05		
=====					

Warnings:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 5.95e+05. This might indicate that there are strong multicollinearity or other numerical problems.

1.3.5 Initial Multiple Linear Regression Model

With 30 independent variables (17 continuous & 13 categorical): $y = 104.85 + 30.86 * \text{Children} - 3.31 * \text{Age} + 0.00 * \text{Income} - 0.26 * \text{Outage_sec_perweek} - 0.31 * \text{Email} + 2.95 * \text{Contacts} + 0.67 * \text{Yearly_equip_failure} + 0.62 * \text{DummyTechie} + 3.93 * \text{DummyContract} + 0.47 * \text{DummyPort_modem} - 1.98 * \text{DummyTablet} - 373.71 * \text{DummyInternetService} - 2.15 * \text{DummyPhone} - 76.08 * \text{DummyMultiple} + 67.49 * \text{DummyOnlineSecurity} - 12.66 * \text{DummyOnlineBackup} + 24.89 * \text{DummyDeviceProtection} - 52.58 * \text{DummyTechSupport} + 30.48 * \text{DummyStreamingTV} - 2.64 * \text{DummyPaperlessBilling} + 82.01 * \text{Tenure} + 3.28 * \text{MonthlyCharge} - 8.9 * \text{TimelyResponse} + 3.47 * \text{Fixes} - 0.18 * \text{Replacements} - 0.27 * \text{Reliability} + 2.72 * \text{Options} + 1.72 * \text{Respectfulness} - 1.35 *$

Courteous + 5.78 * Listening

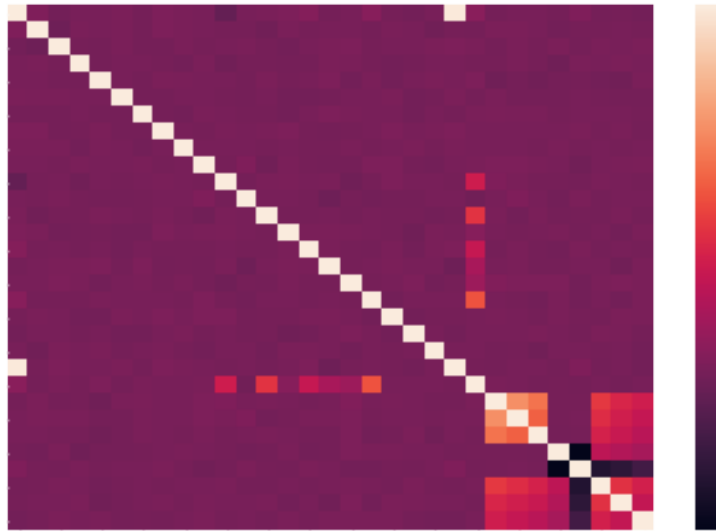
1.3.6 Based on an R2 value = 0.989. So, 99% of the variation is explained by this model. The condition number is large which might suggest strong multicollinearity. Apparently, we do not need all of these variables to explain the variance. So, let's run a heatmap for bivariate analysis & a principal component analysis in order to reduce variables.

1.3.7 D2. Justification of Model Reduction

Justify a statistically based variable selection procedure and a model evaluation metric to reduce the initial model in a way that aligns with the research question.

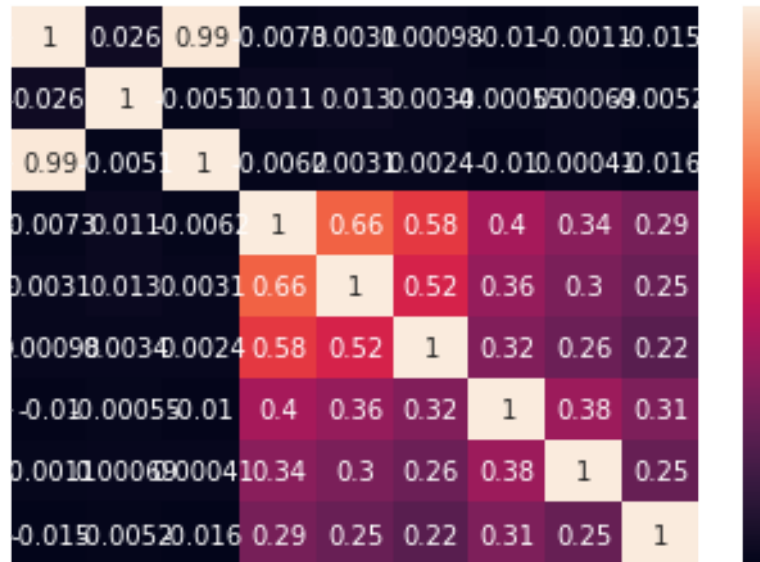
```
[38]: # Create dataframe for heatmap bivariate analysis of correlation
churn_bivariate = churn_df[['Bandwidth_GB_Year', 'Children', 'Age', 'Income',
                             'Outage_sec_perweek', 'Yearly equip_failure',
                             '→'DummyTechie', 'DummyContract',
                             'DummyPort_modem', 'DummyTablet',
                             '→'DummyInternetService',
                             'DummyPhone', 'DummyMultiple',
                             '→'DummyOnlineSecurity',
                             'DummyOnlineBackup', 'DummyDeviceProtection',
                             'DummyTechSupport', 'DummyStreamingTV',
                             'DummyPaperlessBilling', 'Email', 'Contacts',
                             'Tenure', 'MonthlyCharge', 'TimelyResponse',
                             '→'Fixes',
                             'Replacements', 'Reliability', 'Options',
                             '→'Respectfulness',
                             'Courteous', 'Listening']]
```

```
[39]: # Run Seaborn heatmap
sns.heatmap(churn_bivariate.corr(), annot=False)
plt.show()
```



1.3.8 Alrighty, let's try that without some demographic, contacting-customer & options variables, basically purple or darker.

```
[40]: churn_bivariate = churn_df[['Bandwidth_GB_Year', 'Children',  
                                'Tenure', 'TimelyResponse', 'Fixes',  
                                'Replacements', 'Respectfulness',  
                                'Courteous', 'Listening']]  
  
sns.heatmap(churn_bivariate.corr(), annot=True)  
plt.show()
```



1.3.9 That looks a lot better.

Again, it appears that Tenure is the predictor for most of the variance. There is clearly a direct linear relationship between customer tenure with the telecom company & the amount of data (in GBs) that is being used. Let's run a multiple linear regression model on those variables with 0.50 or above & children because of its high coefficient (30.86) on the original OLS model. I also add children intuitively because children always add cost & using the p-value for children is 0.000, & therefore statistically significant.

1.3.10 So, the reduced regression equation will include the continuous variable of tenure & the categorical of children as well as the ordinal categorical independent variables of fixes & replacements.

1.3.11 D3. Reduced Multiple Regression Model

```
[41]: # Run reduced OLS multiple regression
churn_df['intercept'] = 1
lm_bandwidth_reduced = sm.OLS(churn_df['Bandwidth_GB_Year'],
    churn_df[['Children', 'Tenure', 'Fixes', 'Replacements', 'intercept']]).fit()
print(lm_bandwidth_reduced.summary())
```

OLS Regression Results

=====						
Dep. Variable:	Bandwidth_GB_Year	R-squared:	0.984			
Model:	OLS	Adj. R-squared:	0.984			
Method:	Least Squares	F-statistic:	1.537e+05			
Date:	Thu, 15 Jul 2021	Prob (F-statistic):	0.00			
Time:	00:48:57	Log-Likelihood:	-70407.			
No. Observations:	10000	AIC:	1.408e+05			
Df Residuals:	9995	BIC:	1.409e+05			
Df Model:	4					
Covariance Type:	nonrobust					
=====						
	coef	std err	t	P> t	[0.025	0.975]

Children	31.1763	1.288	24.211	0.000	28.652	33.700
Tenure	81.9518	0.105	783.845	0.000	81.747	82.157
Fixes	1.0728	3.129	0.343	0.732	-5.061	7.206
Replacements	-3.6585	3.149	-1.162	0.245	-9.831	2.514
intercept	506.7695	11.949	42.413	0.000	483.348	530.191
=====						
Omnibus:	380.733	Durbin-Watson:	1.978			
Prob(Omnibus):	0.000	Jarque-Bera (JB):	295.369			
Skew:	0.334	Prob(JB):	7.27e-65			
Kurtosis:	2.488	Cond. No.	191.			
=====						

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

1.3.12 Well, there it is. Removing all those other predictor variables & our model still explains 98% of the variance.

1.3.13 Reduced Multiple Linear Regression Model

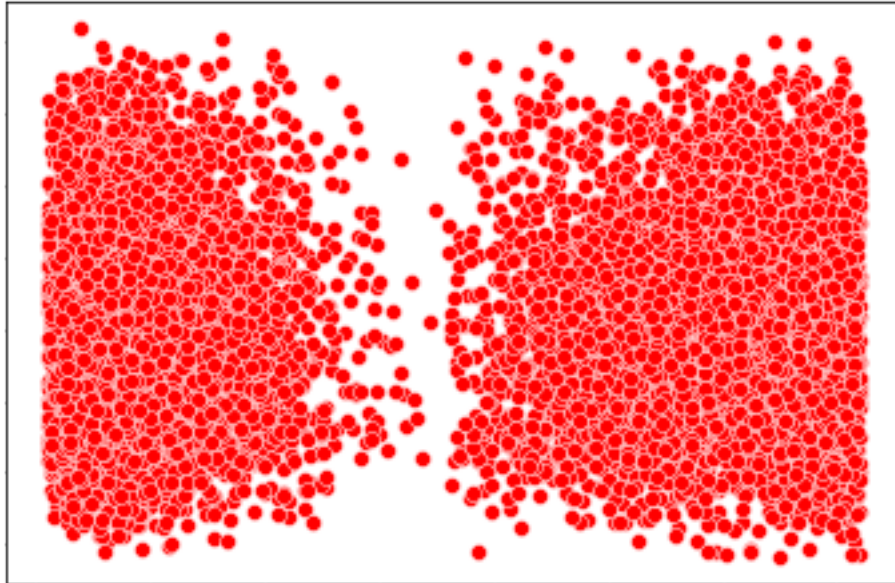
With 4 independent variables: $y = 497.78 + 31.18 * \text{Children} + 81.94 * \text{Tenure} + 1.07 * \text{Fixes} - 3.66 * \text{Replacements}$

1.3.14 E1. Model Comparison

1.3.15 Residual Plot

```
[42]: churn_df = pd.read_csv('churn_prepared.csv')
churn_df['intercept'] = 1
residuals = churn_df['Bandwidth_GB_Year'] - lm_bandwidth_reduced.
    ↳ predict(churn_df[['Children', 'Tenure', 'Fixes', '
    ↳ 'Replacements', 'intercept']])
sns.scatterplot(x=churn_df['Tenure'], y=residuals, color='red')
```

```
plt.show();
```



1.3.16 E2. Output & Calculations

Calculations & code output above.

1.3.17 E3. Code

All code for analysis include above.

1.3.18 F1. Results

Discuss the results of your data analysis, including the following elements:

The final multiple regression equation with 4 independent variables:

$$y = 497.78 + 31.18 * \text{Children} + 81.94 * \text{Tenure} + 1.07 * \text{Fixes} - 3.66 * \text{Replacements}$$

The coefficients suggest that for every 1 unit of:

Children - Bandwidth_GB_Year will increase 31.18 units

Tenure - Bandwidth_GB_Year will increase 81.94 units

Fixes - Bandwidth_GB_Year will increase 1.07 units

Grus, J. (2015). Data Science from Scratch. O'Reilly.
 Massaron, L. & Boschetti, A. (2016). Regression Analysis with Python. Packt Publishing.
 McKinney, W. (2018). Python for Data Analysis. O'Reilly.
 Rossant, C. (2018). IPython Interactive Computing & Visualization Cookbook, 2nd Edition. Packt Publishing.
 Rossant, C. (2015). Learning IPython Interactive Computing & Visualization, 2nd Edition. Packt Publishing.
 VanderPlas, J. (2017). Python Data Science Handbook. O'Reilly.

```
[ ]: !wget -nc https://raw.githubusercontent.com/brpy/colab-pdf/master/colab_pdf.py
from colab_pdf import colab_pdf
colab_pdf('D208_Performance_Assessment_NBM2_Task_1.ipynb')
```

```
--2021-07-15 00:50:15-- https://raw.githubusercontent.com/brpy/colab-
pdf/master/colab_pdf.py
Resolving raw.githubusercontent.com (raw.githubusercontent.com)...
185.199.111.133, 185.199.108.133, 185.199.109.133, ...
Connecting to raw.githubusercontent.com
(raw.githubusercontent.com)|185.199.111.133|:443... connected.
HTTP request sent, awaiting response... 200 OK
Length: 1864 (1.8K) [text/plain]
Saving to: colab_pdf.py
```

```
colab_pdf.py          100%[=====>]    1.82K  --.-KB/s    in 0s
```

```
2021-07-15 00:50:15 (25.9 MB/s) - colab_pdf.py saved [1864/1864]
```

```
Mounted at /content/drive/
```

```
WARNING: apt does not have a stable CLI interface. Use with caution in scripts.
```

```
WARNING: apt does not have a stable CLI interface. Use with caution in scripts.
```

```
Extracting templates from packages: 100%
```

```
[ ]:
```