

**CMPSC 623 Problem Set 1**  
**by Prof. Honggang Zhang**

**Out: September 12, 2006**  
**Due: September 19, 2006, before class.**

**Problem 1.** Exercise 1.2-2 on page 13. In addition, how might one rewrite the merge sort pseudocode to make it even faster on small inputs?

**Problem 2.** Rank the following functions by order of growth; that is, find an arrangement  $g_1, g_2, \dots, g_{23}$  of the functions satisfying  $g_1 = \Omega, g_2 = \Omega(g_3), \dots, g_{22} = \Omega(g_{23})$ . Partition your list into equivalent classes such that  $f(n)$  and  $g(n)$  are in the same class if and only if  $f(n) = \Theta(g(n))$ .

$$(3/2)^n, (\sqrt{2})^{\lg n}, \lg^* n, n^2, n^3, \lg^2 n, \lg(n!), 2^{2^n}, n^{1/\lg n}, \lg \lg n, n \cdot 2^n, n^{\lg \lg n} \\ \ln n, 2^n, 2^{\lg n}, (\lg n)^{\lg n}, 4^{\lg n}, (n+1)!, \sqrt{\lg n}, n!, n, n \lg n, 1$$

**Problem 3.** Problem 2-1 on page 37.

**Problem 4.** Exercise 3.1-1 on page 50.

**Problem 5.** Exercise 3.1-3 on page 50.

**Problem 6.** Exercise 3.1-8 on page 50.