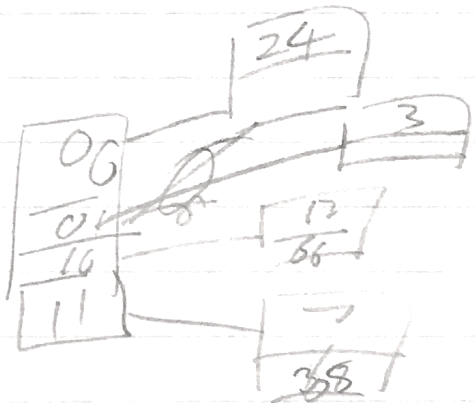
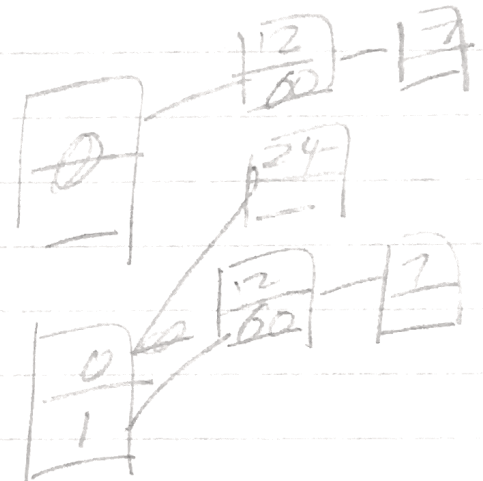
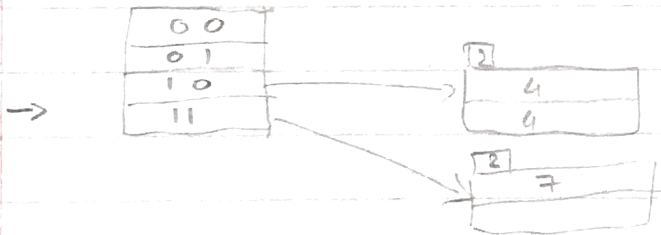


2 search / bucket.

Hash index.

$x \bmod 8$

12	4	100
60	4	100
7	7	111
24	0	000
38	6	110
99	3	011
53	5	101
2	2	010
25	1	001
29	5	101



$$\left\lceil \frac{250}{n} \right\rceil + 1 + n \leq 100$$

$$\frac{250}{n} + \frac{n}{n} + \frac{n^2}{n} \leq 100$$

$$250 + n + n^2 \leq 100n$$

$$n^2 + n - 100n \leq -250$$

$$n^2 - 99n \leq -250$$

$$n \neq n \quad (n)$$

$$n^2 - 99n + 250 \leq 0$$

$$n_1 = 5, \quad n_2 = 96$$

4> hash join.

taken \bowtie taught

$$\# \text{ of passes for hashing} = \lceil \log_{M-1} b_s \rceil - 1 = \lceil \log_{99} 197 \rceil - 1 = 1$$

$$\begin{aligned} \text{Cost} &= 2 * (100,000 + 197) + (100,000 + 197) \\ &= 300,591 \end{aligned}$$

taught \bowtie taken

$$\# \text{ of passes for hashing} = \lceil \log_{99} 100,000 \rceil - 1 = 3 - 1 = 2$$

$$\begin{aligned} \text{Cost} &= 2 * 2 * (100,000 + 197) + 100,000 + 197 \\ &= 500,985 \end{aligned}$$

T₁

T₂

T₃

T₄

T₅

s.lock(A)
read(A)

s.lock(B)
read(B)
x.lock(B)
write(B)
s.lock(C)
read(C)

s.lock(A)
read(A)

s.lock(C)
read C
unlock(A,C)
commit

s.lock(C)
read C

x.lock(A)
write A
unlock(A)
commit

s.lock(C)
read C

wait
after T₄
write C
unlock C
commit.

x.lock(A)
write A
unlock(A,B,C)
commit

s.lock(B)
read B
unlock(B,C)
commit

T₃ → T₂ → T₁ → T₄ → T₅
T

1. salary > 60.

• B+ tree

The size of a tuple is $20 * 5 = 100$

A page size is 4096 bytes

The number of tuples per page is $\frac{4096}{100} = 40$

The number of pointers per page is $\frac{4096 - 4}{20 + 4} + 1 = 171$

The height of B+ tree is $\lceil \log_{171} 25000 \rceil = 2$

The number of leaf pages is $\frac{1000000}{40} / \left(\frac{171 - 1}{2} \right) * \frac{100 - 60}{100 - 51}$

$$= 9604$$

The number of qualifying tuples = $1000000 * \frac{100 - 60}{100 - 51}$

$$= 816327$$

$$\text{Cost} = (2 - 1) + 9604 + 816327 = 825933$$

• File scan.

Size of tuple = 100

The number of fit in a page $\frac{4096}{100} = 40$

$$\text{Cost} = 25000$$

$$\Rightarrow \text{Cost} = 25000$$

Assume if we have primary index on (courses) in taken

of pages in taken qualifies in search is

$$\left\lceil \frac{800}{40} \right\rceil = 20 \text{ pages}$$

$$\begin{aligned} \text{total} &= 197 + 20000 * (2 + 20) \\ &= 440.197 \end{aligned}$$

③ merge-join.

cost of external merge join.

$$2 \text{ br} \left[\lg_{\frac{M}{M-1}} \frac{\text{br}}{M} \right] + \text{br}$$

sort taken.

$$2 * 100000 * \left[\lg_{99} \frac{100000}{100} \right] + 100000 = 500,000$$

sort taught:

$$2 * 197 * \left[\lg_{99} \frac{197}{100} + 197 = 591 \right]$$

$$\begin{aligned} \text{total cost} &= 500000 + 591 + (100000 + 197) + (100000 + 197) \\ &\quad \text{(final) + (merge)} \\ &= 700,985 \end{aligned}$$

+ assume if we have primary index on (course) in taken

$$\text{cost of external merge join} = 591 + 197 + 100197 = 100,985$$

taken (~~mid~~ name, course, score, semester, year)

taught (course, instructor)

taken has 4,000,000 tuples, 100,000 pages

taught has 20,000 tuples, 197 pages

$$M = 100 \text{ pages.}$$

① block-nested loop join.

taken \bowtie taught.

$$\left\lceil \frac{100000}{100-2} \right\rceil * 197 + 100000 = 301,137$$

(M)

taught \bowtie taken.

$$\left\lceil \frac{197}{100-2} \right\rceil * 100000 + 197 = 300,197.$$

② indexed-nested loop join.

assume secondary index on <course> in both relations.

taken \bowtie taught

height of B-tree on course in taught.

$$h = \left\lceil \log_{\frac{171}{2}} \frac{5000}{(5000 \text{ course index base})} \right\rceil = 2$$

of tuple in taught that qualifies the equality search is $\frac{\lceil 20000 \rceil}{5000} = 4$

cost to retrieve the tuples = 2 + 4 = 6 pages

$$\text{total} = 100000 + 4 \cdot 4,000,000 * 6 = 24,100,000 \text{ pages}$$

taught \bowtie taken

$$h = \left\lceil \log_{\frac{171}{2}} 5000 \right\rceil = 2.$$

of tuple in taken qualifies the search. $\frac{4,000,000}{5000} = 800$

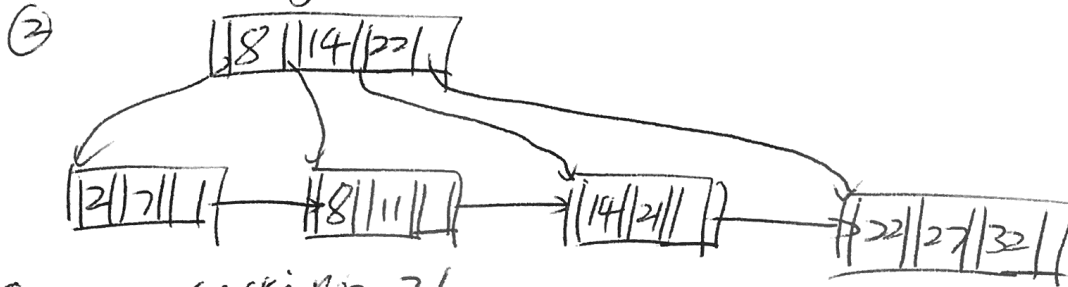
$$\text{total cost} = 197 + 20000 * (2 + 800)$$

2, 7, 8, 11, 14, 21, 22, 27, 32, 36

①

2	7	8
---	---	--------------

inserting 11. . . .



③ inserting 36

