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1. Given the following input (3412, 3413, 1741, 3269, 2909, 6291, 6373, 5129) and the hash function $h(k) = k \bmod 10$, which of the following statement(s) true? Choose all correct ones.

- ☒ A. 3269, 2909, 5129 hash to the same value
- ☐ B. 3412 and 3413 hash to the same value
- ☒ C. 1741, 6291 hash to the same value
- ☐ D. 3413, 3269, 6291, 6373 each hashes to a different value

2. The keys 14, 18, 33, 4, 3, 23, 25 and 5 are inserted into an initially empty hash table in this given order. The hash table has 10 slots and uses chaining with hash function $h(k) = k \bmod 10$. What is the hash table after inserting all keys? (multiple numbers in the same slot represents a linked list to chain the numbers together in that order)

0	
1	
2	
3	3, 23, 33
4	4, 14
5	5, 25
6	
7	
8	18
9	

A

0	
1	
2	
3	23, 3, 33
4	4, 14
5	5, 25
6	
7	
8	18
9	

☒ B

0	
1	
2	
3	33, 23, 3
4	14, 4
5	25, 5
6	
7	
8	18
9	

C

0	
1	
2	
3	33, 3, 23
4	14, 4
5	25, 5
6	
7	
8	18
9	

D

$$h(14) = 14 \bmod 10 = 4$$

$$h(18) = 18 \bmod 10 = 8$$

$$h(33) = 33 \bmod 10 = 3$$

$$h(4) = 4 \bmod 10 = 4 \text{ (collision)}$$

$$h(3) = 3 \bmod 10 = 3 \text{ (collision)}$$

$$h(23) = 23 \bmod 10 = 3 \text{ (collision)}$$

$$h(25) = 25 \bmod 10 = 5$$

$$h(5) = 5 \bmod 10 = 5 \text{ (collision)}$$

3. The keys 14, 18, 33, 4, 3, 23, 25 and 5 are inserted into an initially empty hash table in this given order. The hash table has 10 slots and uses open addressing with hash function $h(k) = k \bmod 10$ and linear probing. What is the hash table after inserting all keys?

0	
1	
2	
3	23
4	4
5	5
6	
7	
8	18
9	

A

0	
1	
2	5
3	33
4	14
5	4
6	3
7	23
8	18
9	25

B

0	
1	
2	
3	33
4	14
5	25
6	
7	
8	18
9	

C

0	5
1	
2	
3	33
4	14
5	4
6	3
7	23
8	18
9	25

(D)

$$\begin{aligned}
 h(14, 0) &= 14 \bmod 10 = 4 \\
 h(18, 0) &= 18 \bmod 10 = 8 \\
 h(33, 0) &= 33 \bmod 10 = 3 \\
 h(4, 0) &= 4 \bmod 10 = 4 \text{ (collision)} \\
 h(4, 1) &= (4+1) \bmod 10 = 5 \\
 h(3, 0) &= 3 \bmod 10 = 3 \text{ (collision)} \\
 h(3, 1) &= 4 \text{ (collision)}; h(3, 2) = 5 \text{ (collision)}; h(3, 3) = 6
 \end{aligned}$$

4. (1) What is the load factor in Problem 2 above?

$$\alpha = \frac{8}{10} = \frac{4}{5}$$

$$h(23, 0) = 23 \bmod 10 = 3 \text{ (collision)}$$

$$h(23, 1) = 4 \text{ (collision)}$$

$$\vdots$$

$$h(23, 4) = 7$$

$$h(25, 0) = 25 \bmod 10 = 5 \text{ (collision)}$$

$$\vdots$$

$$h(25, 4) = 9$$

$$h(5, 0) = 5 \bmod 10 = 5 \text{ (collision)} \dots h(5, 5) = 0$$

(2) What is the load factor in Problem 3 above?

$$\alpha = \frac{8}{10} = \frac{4}{5}$$