

Department of Computer Science
University of Massachusetts Lowell
COMP.3040 Foundations of Computer Science
Spring 2017
Quiz 2 [5%]
4/13/2017

1. Give the formal definition of a Turing Machine (TM)

A Turing Machine is a 7-tuple, $(Q, \Sigma, \Gamma, \delta, q_0, q_{accept}, q_{reject})$

• Q is a finite set of states

• Σ is the input alphabet not containing the blank symbol

• Γ is the tape alphabet, δ is transition function, q_0 is the start state, q_{accept} is the accept state, q_{reject} is the reject state

2. What is an Enumerator?

Enumerator is a Turing machine with an attached printer.

3. What is Church Turing Thesis?

Church-Turing Thesis is the intuitive notion of algorithms equals the Turing machine algorithms.

4. A multi-tape TM is more powerful than a single tape TM.

• True
• False

5. A Non-deterministic TM is more powerful than a Deterministic TM.

• True
• False

6. Order the class of languages in increasing order of power

• Context Free
• Regular
• Turing Recognizable
• Turing Decidable

7. $A = \{ 0^n 1^n \mid n \geq 0 \}$ is a decidable/recognizable language

• Decidable
• Recognizable

8. $A_{DFA} = \{ (B, w) \mid B \text{ is a DFA that accepts input string } w, \text{ is a decidable/recognizable language} \}$

- Decidable
- Recognizable

9. $A_{REG} = \{ (R, w) \mid R \text{ is a Regular Expression that generates string } w, \text{ is a decidable/recognizable language} \}$

- Decidable
- Recognizable

10. $A_{CFG} = \{ (G, w) \mid G \text{ is a CFG that generates string } w, \text{ is a decidable/recognizable language} \}$

- Decidable
- Recognizable

11. [20 points] Sketch an algorithm using a single tape TM to recognize the language L — contains matching parenthesis; for example $((()))$ and $((()()))$

For $((()))$ and $((()()))$

- ① At start, the input string appears on the tape and it will start parsing left to right.
- ② Mark the symbol and remember if it's "("
- ③ Move to the right and find the ")" if there is another "(", keep looking until found ")". the first ")" will be matched with the last "(".
- ④ repeat the process until it found all completed pair of parenthesis

— 15