Q1 Combining Factors

16 Points

Given the factors $P(A \mid C)$ and $P(B \mid A, C)$ what is the resulting factor after joining over C?

- OP(A, B, C)
- $OP(A \mid B, C)$
- $\bigcirc P(A, B \mid C)$
- O None of the above.

Given the factors P(A|B) and P(B|C) and P(C) which factor will be created after joining on C and summing out over C?

- OP(B,C)
- \bullet P(B)
- OP(C)
- O None of the above

Given the factors P(A|C) and P(B|A,C) what is the resulting factor after joining over A and summing over A?

- OP(C)
- OP(B)
- OP(B,C)
- $OP(A \mid C)$
- $\bigcirc P(B \mid C)$
- O None of the above.

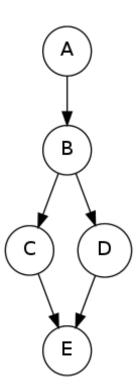
Given the factors P(C|A), P(D|A,B,C), P(B|A,C), what is the resulting factor after joining over C and summing over C?

- $OP(D \mid A)$
- $OP(C,D \mid A)$
- $OP(B,C,D\mid A)$
- $\bigcirc P(B,D \mid A)$
- $\bigcirc P(C, B \mid A, D) * P(A \mid D)$
- O None of the above.

Q2 Variable Elimination Tables

20 Points

Assume the following Bayes Net and corresponding CPTs. In this exercise, we are given the query $P(C\mid e=1)$, and we will complete the tables for each factor generated during the elimination process.



After introducing evidence, we have the following probability tables.



B	A	P(B A)
0	0	0.500
1	0	0.500
0	1	0.400
1	1	0.600

C	В	P(C B)
0	0	0.400
1	0	0.600
0	1	0.300
1	1	0.700

D	В	P(D B)
0	0	0.600
1	0	0.400
0	1	0.900
1	1	0.100

C	D	P(e=1 C,D)
0	0	0.600
1	0	0.200
0	1	0.600
1	1	0.200

Q2.1

15 Points

Three steps are required for elimination, with the resulting factors listed below:

Step 1: eliminate A. We get the factor $f_1(B) = \sum_a P(a) P(B|a)$

Step 2: eliminate B. We get the factor $f_2(C,D) = \sum_b P(C|b)P(D|b)f_1(b)$

Step 3: eliminate D. We get the factor $f_3(C,e=1) = \sum_d P(e=1|C,d) f_2(C,d)$.

Fill in the missing quantities. (some of the quantities are computed for you)

$$f_1(B=0) =$$

.41

$$f_1(B=1) =$$

.59

$$f_2(C=0, D=0) =$$

.2577

$$f_2(C=1, D=0) =$$

.5193

$$f_2(C=0,D=1)=0.083$$

$$f_2(C=1, D=1) = 0.14$$

$$f_3(C=0,e=1) =$$
 .20442

$$f_3(C=1,e=1)=0.132$$

Q2.2

5 Points

After getting the final factor $f_3(C,e=1)$, a final renormalization step needs to be carried out to obtain the conditional probability P(C|e=1). Fill in the final conditional probabilities below.

$$P(C=0 \mid e=1) =$$

.608

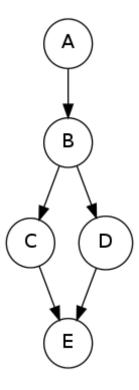
$$P(C = 1 \mid e = 1) =$$

.392

Q3 Rejection Sampling

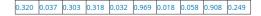
16 Points

We will work with a Bayes' net of the following structure.



In this question, we will perform rejection sampling to estimate $P(C=1\mid B=1,E=1)$. Perform one round of rejection sampling, using the random samples given in the table below. Variables are sampled in the order A,B,C,D,E. In the boxes below, choose the value (0 or 1) that each variable gets assigned to. Note that the sampling attempt should stop as soon as you discover that the sample will be rejected. In that case mark the assignment of that variable and write none for the rest of the variables.

When generating random samples, use as many values as needed from the table below, which we generated independently and uniformly at random from [0,1). Use numbers from left to right. To sample a binary variable W with probability P(W=0)=p and P(W=1)=1-p using a value a from the table, choose W=0 if a< p and W=1 if $a\geq p$.





В	A	P(B A)
0	0	0.800
1	0	0.200
0	1	0.400
1	1	0.600

C	В	P(C B)
0	0	0.600
1	0	0.400
0	1	0.400
1	1	0.600

D	B	P(D B)
0	0	0.800
1	0	0.200
0	1	0.600
1	1	0.400

E	C	D	P(E C,D)
0	0	0	0.800
1	0	0	0.200
0	1	0	0.600
1	1	0	0.400
0	0	1	0.400
1	0	1	0.600
0	1	1	0.400
1	1	1	0.600

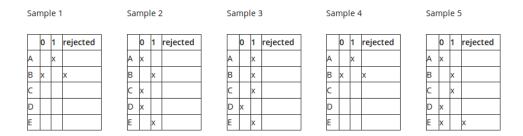
Enter either a 0 or 1 for each variable that you assign a value to. Upon rejecting a sample, enter its assigned value, and enter none for the remaining variables. For example, if C gets rejected, fill in none for D and E.

A:	
	1
B:	
	0
C:	
	none
D:	
	none
E:	
r -	none
r -	none
	none nich variable will get rejected?
	nich variable will get rejected?
WI	nich variable will get rejected?
WI	nich variable will get rejected? A B
WI O	nich variable will get rejected? A B C
Wi O	nich variable will get rejected? A B C

Q4 Estimating Probabilities from Samples

16 Points

Below are a set of samples obtained by running rejection sampling for the Bayes' net from the previous question. Use them to estimate $P(C=1\mid B=1,E=1)$. The estimation cannot be made whenever all samples were rejected. In this case, input -1 into the box below.



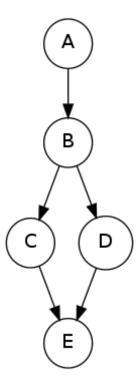
Estimation:

.5

Q5 Likelihood Weighting

16 Points

We will work with a Bayes' net of the following structure.



In this question, we will perform likelihood weighting to estimate $P(C=1\mid B=1,E=1)$. Generate a sample and its weight, using the random samples given in the table below. Variables are sampled in the order A, B, C, D, E. In the table below, select the assignments to the variables you sampled.

When generating random samples, use as many values as needed from the table below, which we generated independently and uniformly at random from [0,1). Use numbers from left to right. To sample a binary variable W with probability P(W=0)=p and P(W=1)=1-p using a value a from the table, choose W=0 if a< p and W=1 if $a\geq p$.



A P(A)
0 0.200
1 0.800

B	A	P(B A)
0	0	0.400
1	0	0.600
0	1	0.200
1	1	0.800

C	B	P(C B)
0	0	0.600
1	0	0.400
0	1	0.600
1	1	0.400

D	B	P(D B)
0	0	0.800
1	0	0.200
0	1	0.600
1	1	0.400

E	C	D	P(E C,D)
0	0	0	0.200
1	0	0	0.800
0	1	0	0.600
1	1	0	0.400
0	0	1	0.800
1	0	1	0.200
0	1	1	0.800
1	1	1	0.200

Input Answers Here

A:

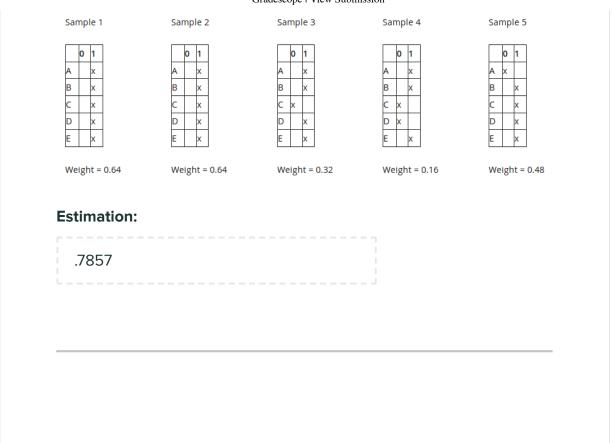
1	
B:	
1	
C :	
0	
D:	
0	
E :	
1	
What is the weight for the sample you ob .64	taine

Q6 Estimating Probabilities from Weighted Samples

16 Points

Below are a set of weighted samples obtained by running likelihood weighting for the Bayes' net from the previous question. Use them to estimate $P(C=1\mid B=1,E=1)$. Input -1 in the box below if the estimation cannot be made.

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HW 7 (Electronic Component)

GRADED

STUDENT

TOTAL POINTS

100 / 100 pts

QUESTION 1

Combining Factors 16 / 16 pts

QUESTION 2

Variable Elimination Tables 20 pts

2.1 (no title) 15 / 15 pts

2.2 (no title) **5** / 5 pts

QUESTION 3

Rejection Sampling 16 / 16 pts

QUESTION 4

Estimating Probabilities from Samples 16 / 16 pts

QUESTION 5

Likelihood Weighting 16 / 16 pts

QUESTION 6

Estimating Probabilities from Weighted Samples 16 / 16 pts