

*Note:* All questions below refer to lexicographic order (e.g. “smallest” means “smallest with respect to lexicographic order”).

1. Put the following permutations in lexicographic order: 43521, 14523, 43152, 43512, 21345
2. (a) What is the smallest permutation of  $\{1, 2, \dots, 7\}$  that begins with 315? What's the next permutation in lexicographic order?  
(b) What is the largest permutation of  $\{1, 2, \dots, 7\}$  that begins with 315? What's the next permutation in lexicographic order?
3. Consider the permutation 7263541.
  - (a) Find the next permutation in lexicographic order.
  - (b) Fill in the following blank:  
7263541 is the largest permutation of  $\{1, 2, \dots, 7\}$  in lexicographic order which begins with the string \_\_\_\_\_.  
(Find the shortest such string that works. What are other strings that would also work?)
4. Find the next three permutations in lexicographic order after 465321.
5. What's the largest 4-combination of  $\{1, 2, \dots, 9\}$  which contains both of the elements 1, 4? What's the next 4-combination in lexicographic order?
6. Find the next three 4-combinations of  $\{1, 2, \dots, 9\}$  after  $\{2, 5, 7, 9\}$ .
7. Find the next three 5-combinations of  $\{1, 2, \dots, 7\}$  after  $\{2, 3, 4, 6, 7\}$ .

Answers:

1. 14523, 21345, 43152, 43512, 43521
2. (a) 3152467. The next permutation is 3152476.  
(b) 3157642. The next permutation is 3162457.
3. (a) 7264135  
(b) 7263
4. 512346, 512364, 512436
5.  $\{1, 4, 8, 9\}$ ; next 4-combination is  $\{1, 5, 6, 7\}$
6.  $\{2, 5, 8, 9\}$ ,  $\{2, 6, 7, 8\}$ ,  $\{2, 6, 7, 9\}$
7.  $\{2, 3, 5, 6, 7\}$ ,  $\{2, 4, 5, 6, 7\}$ ,  $\{3, 4, 5, 6, 7\}$