

95+10  
105

### ① a) DFA and NFA.

They both have starting states, sets of accept states, transition functions, input alphabet.

Difference: - DFA takes an input and start states to produce the next possible state.

- NFA takes an input and starting states to produce a set of possible next states.

Terminals are character of alphabets that appears in the string generated by the grammar.

Ex: boys/girls laugh/cry.

Nonterminals are the place holder for strings or language patterns of terminal symbols.

Nonterminals can be used to generate terminal symbols. Ex: <NOUN> <VERB>

b). Pumping Lemma is used as a proof for irregularity of a language  $\Rightarrow$  if language is regular, it satisfies pumping lemma.

. Alphabet is a finite set of fundamental units (letters or symbols)

- String: over an alphabet is a finite sequence of symbols from the alphabet (no spaces or commas between symbols).
- Language: is a set of strings over an alphabet.
- Sequence is a list of objects in some order.
- $k$ -tuple: a finite sequence ~~that has  $k$  symbols from the alphabet~~ ( $k$  symbols <sup>(set of string)</sup> from alphabet).
- Ordered pair: ~~a pair of objects that its order is significant:  $(a, b) \neq (b, a)$  unless  $a = b$ .~~
- Unordered pair: ~~a pair of objects that its order is not significant:  $(a, b)$  can be equal  $(b, a)$ .~~
- ~~Domain~~ Ordered pair: a list of two elements.
- Unordered pair: a set with two members.
- Domain: The set of possible input to a function.
- Range: The set from which outputs of a function are drawn.

② CFG:

Context free grammar is a 4-tuple  $(V, \Sigma, R, S)$

$V$ : finite set called variable.

$\Sigma$ : finite set of variable  $V$ , called terminal.

$R$ : finite set of rules.

$S \in V$ : state variable.

PDA :

Push down automation is a 6-tuple  $(Q, \Sigma, \Gamma, \delta, q_0, F)$

$Q$ : set of states

$\Sigma$ : input alphabet

$\Gamma$ : ~~state~~ stack alphabet

$\delta: Q \times \Sigma_\epsilon \times \Gamma_\epsilon \rightarrow P(Q \times \Gamma_\epsilon)$  is the transition function.

$q_0 \in Q$ : start state

$F \subseteq Q$ : set of accept states.

~~Regular~~

Regular expression:

$R$  is regular expression if  $R$  is

1.  $a$  for some  $a$  in the alphabet  $\Sigma$ .

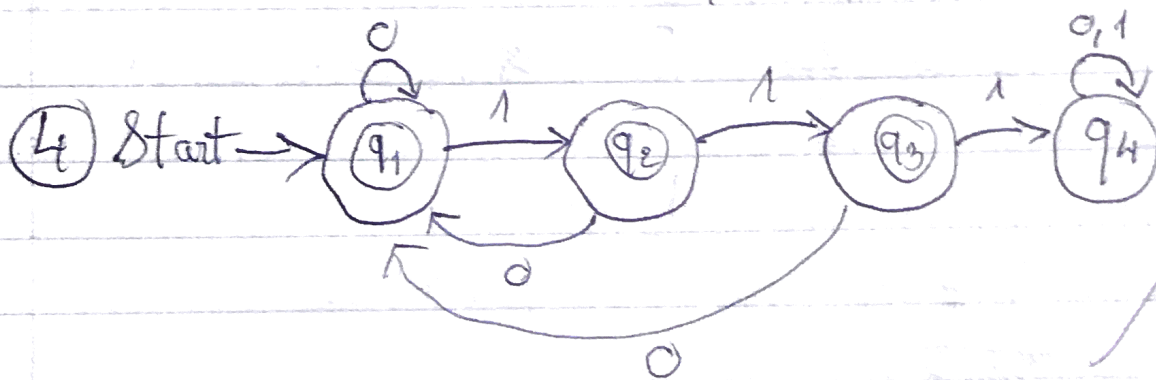
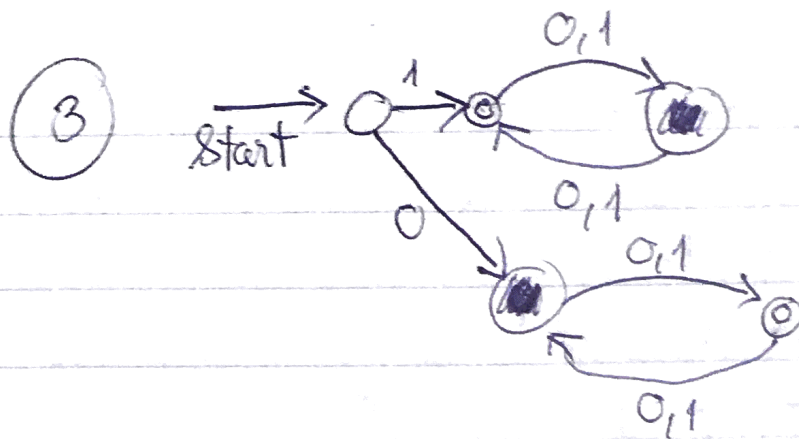
2.  $\epsilon$

3.  $\phi$

4.  $(R_1 \cup R_2)$ , where  $R_1$  and  $R_2$  are regular expressions

5.  $(R_1 \circ R_2)$ , where  $R_1$  and  $R_2$  are regular expressions.

6.  $(R_1^*)$  where  $R_1$  is a regular expression.



$$M = \{Q, \Sigma, \delta, q_0, F\}$$

$$Q = \{q_1, q_2, q_3, q_4\}$$

$$\Sigma = \{0, 1\}$$

$$\delta =$$

	0	1
$q_1$	$q_1$	$q_2$
$q_2$	$q_1$	$q_3$
$q_3$	$q_1$	$q_4$
$q_4$	$q_4$	$q_4$

$$q_0 = q_1 \text{ (start state)}$$

$$F = (q_1, q_2, q_3) \text{ (final accept states)}$$



$L = \{ w \mid w \text{ has at most 2 consecutive 1's} \}$

(5) PDA uses stack alphabet  $\Gamma$ , which allows PDA to recognize non-regular languages.

Limit:

PDA<sub>\*</sub> has a transition function that takes an input and a state or <sup>an</sup> empty string; DFA needs to have input and state to produce next state. (cannot take empty string)

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(1)

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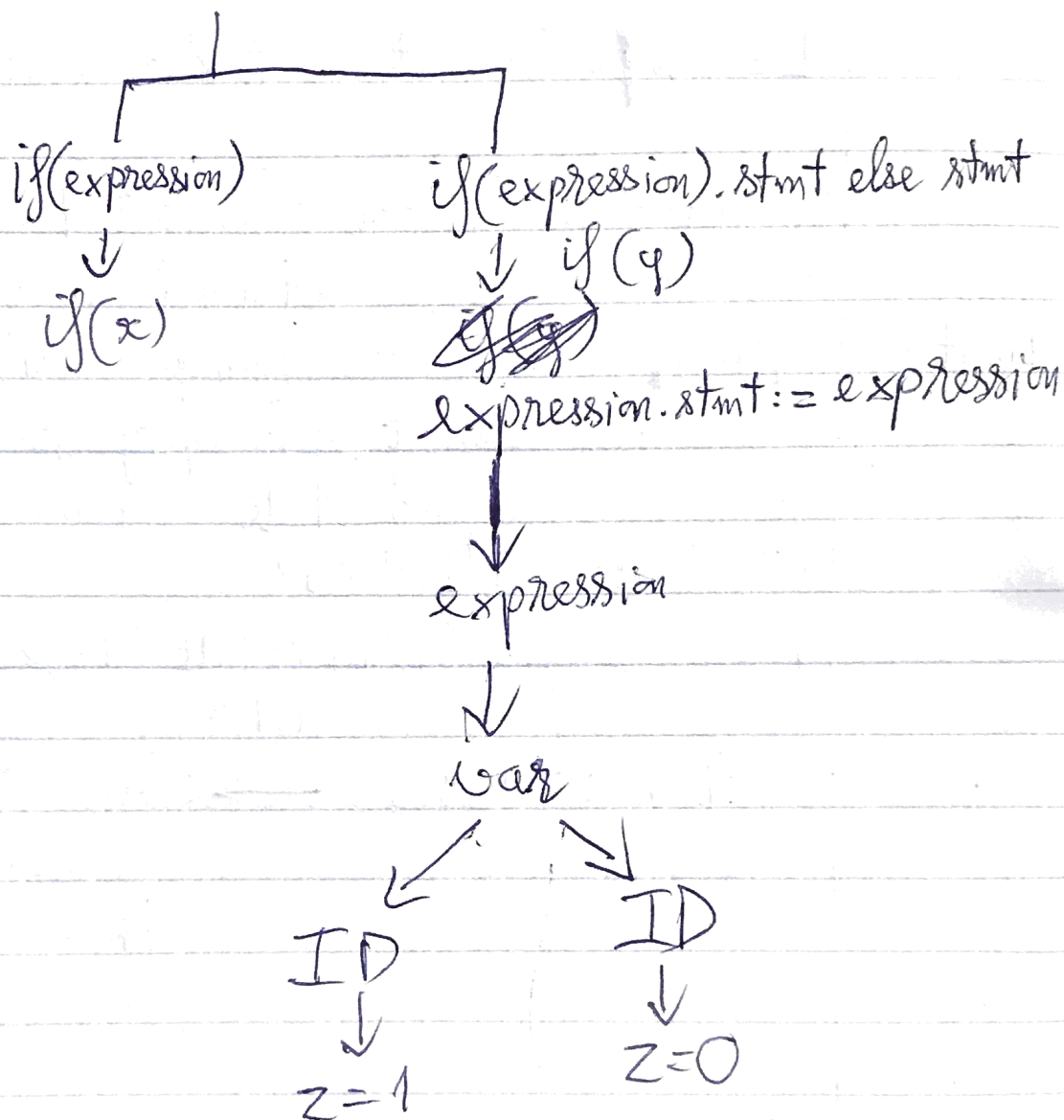
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(C) ~~comp~~  
~~comp~~ compound

b)



a) compound-stmt C-S

selection-stmt S-S

iteration-stmt ~~i-i~~ i-S

return-stmt R-S

break-stmt b-S

expression-stmt e-S → e  
:= expression

selection-stmt ::= if(expression) stmt / s- s if(e) s if(expression) stmt else stmt expression-stmt ::= expression; var <del>+</del> += expression <del>assign</del> var = expression simple-expression var ::= ID ID(expression)	if( <del>e</del> )(e) s else s $e \rightarrow \text{var} = e$ $\text{var}(+) = e$ $\text{var} = e$ $e(s)$ $\text{var} = \text{ID}$ $\text{ID}(e)$
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-10

1	0
2	0
3	0
4	0
5	5