

## Homework #5

### 1. (10 points) Exercise 6.1-5 (page 154):

Ans:

Yes. For an array with sorted order, we have  $A[i] \leq A[j]$  for  $i < j$ , and satisfies that  $A[\text{PARENT}(i)] \leq A[i]$  since  $\text{PARENT}(i) < i$ .

### 2. (10 points) Exercise 6.1-6 (page 154):

Ans:

No. In the heap, the “6” is the parent of “5” and “7”, which violates the max-heap property  $A[\text{PARENT}(i)] \geq A[i]$ .

### 3. (10 points) Problem 6.2-4 (page 156) :

Ans:

There is no effect, because the element  $A[i]$  for  $i > A.\text{heapsize}/2$  are leaves.

### 4. (10 points) Problem 6.3-2 (page 159) :

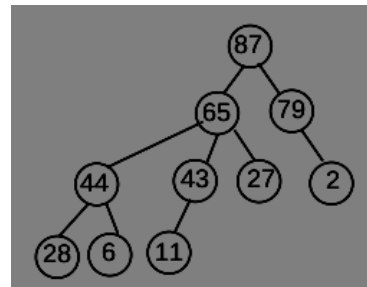
Ans:

Because the procedure BUILD-MAX-HEAP is working in a bottom-up manner by using MAX-HEAPIFY which compares the node and its children. The procedure assumes that the sub-trees under the current node are already max-heaps. Because the nodes  $A[i]$  with  $i > \text{heapsize}/2$  are leaves, so the loop starts from and finally ends at the top node of the entire heap ( $i=1$ ).

### 5. (10 points) Does the tree on the right represent a MAX HEAP?

Ans:

No, the tree is not a MAX HEAP. The (binary) heap in this chapter is an array object that we can view as a nearly complete binary tree, but the node with value 65 has three children.



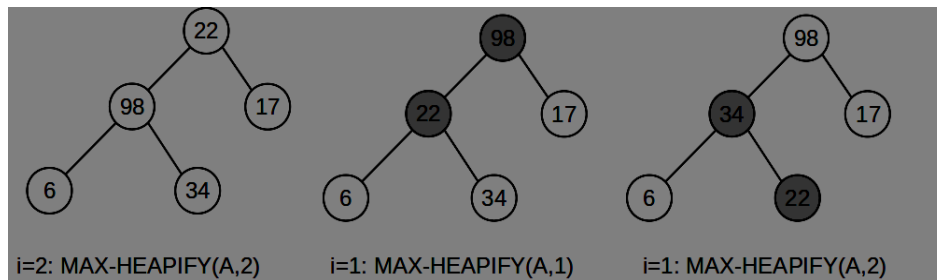
6. (20 points) **Given the array  $A = \langle 22, 98, 17, 6, 34 \rangle$  :**

(a) Illustrate the operation of **HeapSort** using Figure 6.4 on p. 161 as a model. Sort the numbers into non-decreasing order.

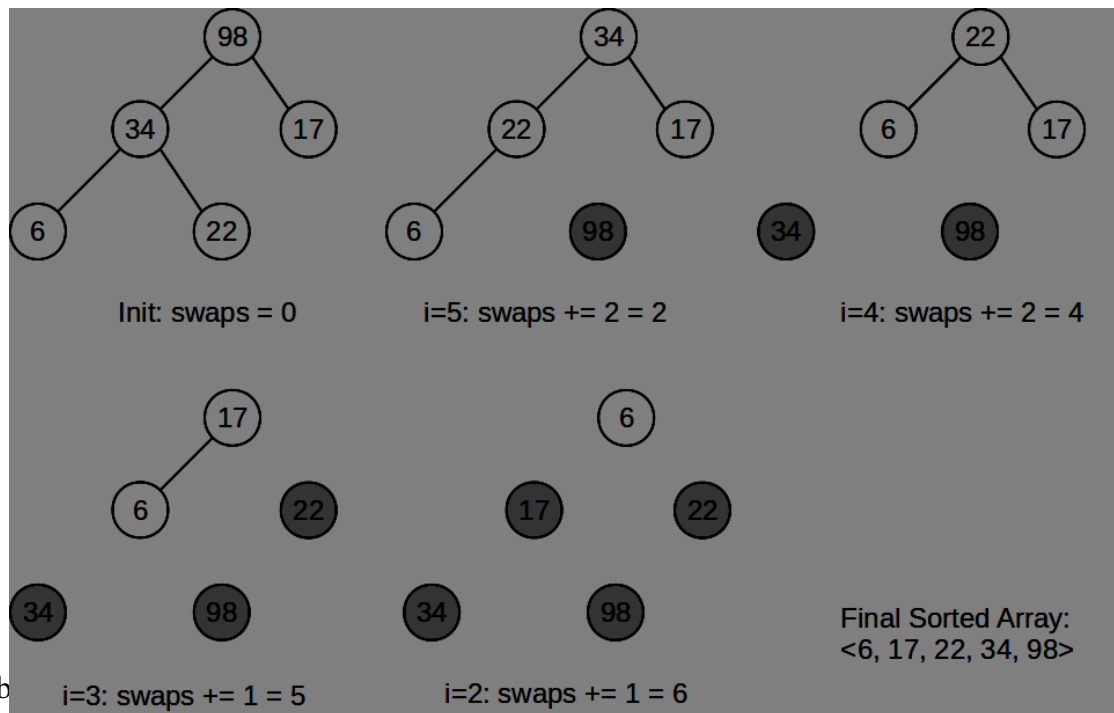
(b) A swap is an exchange of two elements in the array:  $A[i] \leftrightarrow A[j]$  . How many swaps are performed by **HeapSort** to sort the array  $A$ ? Note: Include the swaps used to build the heap.

Ans:

(a)  $A.length = 5$ , so the BUILD-MAX-HEAP will use MAX-HEAPIFY from  $i=2$  to 1. For iteration  $i=2$ , MAX-HEAPIFY does nothing, and there is two exchange at the iteration  $i=1$  where 22 and 98 are swapped and then 22 and 34 are changed.



For sorting part, the loop is from  $i=5$  to 2 and each iteration there is an exchange between  $A[1]$  and  $A[i]$  and maybe another exchange for MAX-HEAPIFY.



(b)