## CMPSC 623 Problem Set 1 by Prof. Honggang Zhang

Out: September 6, 2007 Due: September 13, 2007, before class.

**Problem 1.** Exercise 1.2-2 on page 13. In addition, how might one rewrite the merge sort pseudocode to make it even faster on small inputs?

**Problem 2.** Rank the following functions by order of growth; that is, find an arrangement  $g_1, g_2, ..., g_{23}$  of the functions satisfying  $g_1 = \Omega, g_2 = \Omega(g_3), ..., g_{22} = \Omega(g_{23})$ . Partition your list into equivalent classes such that f(n) and g(n) are in the same class if and only if  $f(n) = \Theta(g(n))$ .

$$(3/2)^{n}, (\sqrt{2})^{\lg n}, \lg^{*} n, n^{2}, n^{3}, \lg^{2} n, \lg(n!), 2^{2^{n}}, n^{1/\lg n}, \lg\lg n, n \cdot 2^{n}, n^{\lg\lg n}$$

$$\ln n, 2^{n}, 2^{\lg n}, (\lg n)^{\lg n}, 4^{\lg n}, (n+1)!, \sqrt{\lg n}, n!, n, n \lg n, 1$$

**Problem 3.** Problem 2-1 on page 37.

Problem 4. Exercise 3.1-1 on page 50.

**Problem 5.** Exercise 3.1-3 on page 50.

**Problem 6.** Exercise 3.1-8 on page 50.