

## Analysis of Algorithms Learning Outcomes 91.404 (Section 201)

(adapted from *ACM Computer Science Computing Curricula 2001, Steelman Draft, August, 2001*)

- 1) Use big O, omega and theta notation to give asymptotic upper, lower, and tight bounds on time and space complexity of algorithms.
- 2) Determine the time complexity of simple algorithms.
- 3) Express simple algorithms using pseudocode conventions.
- 4) Justify the correctness of an algorithm
  - a) “Mechanical”: e.g. no infinite loops or recursion, remaining within array bounds
  - b) “As advertised”: the algorithm solves the given problem: e.g. sorting algorithm results in correct ordering of elements.
- 5) Given a computational problem begin to learn how to:
  - a) Recognize its underlying structure
  - b) Identify aspects of the problem relevant to time & space complexity (e.g. problem size, distribution of inputs)
  - c) Develop intuition about it using worst-case, best-case and average-case inputs
  - d) Determine if a known solution exists
  - e) Adapt a solution to a closely related problem
  - f) Design an algorithm from scratch by appropriately selecting an algorithmic paradigm and making of abstract data type and implementation choices.
- 6) Given a list of functions of a single variable, order them according to asymptotic growth.
- 7) Perform worst-case, best-case and average case asymptotic analysis.
- 8) Deduce the recurrence relations that describe the time complexity of recursive algorithms, and solve simple recurrence relations using Master Theorem, recursion trees and induction/ substitution.
- 9) Design and analyze simple randomized algorithms.
- 10) Solve problems using sorting algorithms:
  - a) Comparison-based sorting algorithms
    - i) Insertion Sort
    - ii) Merge Sort
    - iii) Heap Sort: Execute operations that preserve the heap property
    - iv) Quick Sort
  - b) Non-comparison and/or hybrid sorting algorithms.
    - i) Counting Sort
    - ii) Radix Sort
    - iii) Bucket Sort
- 11) Assess the impact of choices of abstract data type and implementation on running time and storage requirements
  - a) Stacks
  - b) Queues
  - c) Linked Lists
  - d) Trees: Binary search trees and balanced binary search trees
    - i) Apply left and right rotations that preserve the binary search tree property
  - e) Hash Tables, including collision avoidance strategies
  - f) Graphs, including both adjacency matrix and adjacency list representations
- 12) Understand the operation of the following graph algorithms
  - a) Depth-First Search
  - b) Breadth-First Search
  - c) Topological Sort
- 13) Understand how a multi-threaded Merge Sort works (time permitting)