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1. Consider the belief network shown below:

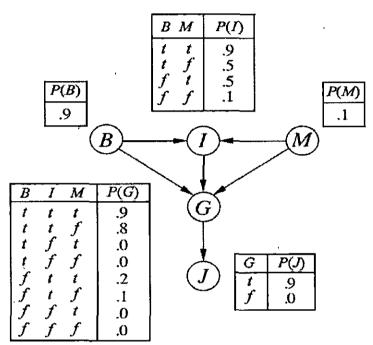


Fig 1: A simple Bayes net with Boolean variables B =BrokeElectionLaw, $I = Indicted\ M = PoliticallyMotivatedProsecutor\ ,\ G = FoundGuilty\ ,\ J = Jailed$

- a) (4 points) Which of the following are asserted by the network structure?
 - (i) P(B, I,M) = P(B)P(I)P(M).
 - (ii) P(J|G) = P(J|G, I).
 - (iii) $P(M \mid G,B, I) = P(M \mid G,B, I, J).$
- b) (5 points) Calculate the value of P(b, i, ¬m, g, j).
- c) (6 points) Calculate the probability that someone goes to jail given that they broke the law, have been indicted, and face a politically motivated prosecutor.
- d) (5 points) Suppose we want to add the variable P = Presidential Pardon to the network; draw the new network and briefly explain any links you add.

1 a) (ii) and (iii). bl. p(bii, migu): = P(b). P(-1m). P(i/b,-m) P(g/b,i,-1m) P(s/g) = 0.9 × 0.9 × 0.5 × 0.9 = 0.29/6 c). p(J16,i,m) $= 2 \sum_{g} P(f_{ig}) = 2 \left[P(5_{ig}) + P(5_{ig}) \right]$ $= 2 \sum_{g} P(f_{ig}) = 2 \left[P(5_{ig}) + P(5_{ig}) \right]$ $= 2 \sum_{g} P(f_{ig}) = 2 \left[P(5_{ig}) + P(5_{ig}) \right]$ · P(j,g)= P(J/g)-P(g) = 0-9 ,0-9=0.81 P(71,9) = P(71,9). P(g)=0.1,0.9 =0.09. P(J1-9)=P(J|99). P(79)=0x0.1=0 P(-15,-19) = P(-15,-19)-P(-18) = 1x0.1=0.1 =1 (0 = L[(0.81,0.09)+(0,0.4)]=(0.81,0.09) =) The person bility of gots to soul is 0.81

A pandon is not recessary if the person is not Indided on not found quilty = I and Grave parent of P. P is the parent of 5 since pander means get and of Sail.

2. (10 points) Given the Bayes net shown in the Figure below; A, B, C, D, and E are all Boolean variables. P(A="T") is simply denoted as P(A).

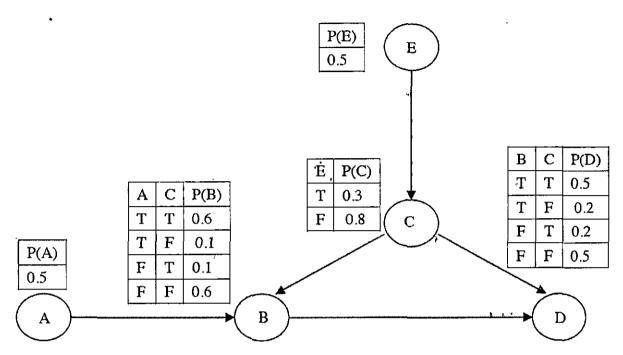


Fig 2: Bayes Net

Note: In the following, the notations: $A \perp B$ means A is independent of B; $A \perp B \mid C$ means A is conditionally independent of B given C.

a. Please judge if the following independence assumptions are correct or not:

3. Consider the Bayesian network below

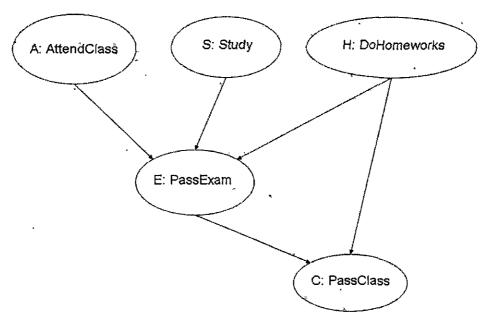


Fig 3: Bayes net for studying and passing

- a) (5points) Write down the joint distribution as it factorizes according to the graph below.
- b) (5 points) Use variable elimination and your result from (a) above to write down the expression for the probability of passing the class, given that you attend class and study, but don't do the home works.
- c) (10 points) Use the following CPTs for the graph of question 1 to compute P (A|C,H).

$$P(A) = 0.5, P(S) = 0.7, P(H) = 0.9$$

A	S	H	P (E A, S,
0	0	0	0.2
0	0	1	0.5
0	1	0	0.4
0	1	1	0.8
1	0	0	0.3
1	0	1	0.7
1	1	0	0.6
1	1	1	0.9

Е	H	P (C E, H)
0	0	0.1
0	1	0.4
1	0	0.3
1	1	0.9

3a) P(A,S, H,E,C) = P(A).P(S).P(H).P(ElA,S,H).P(C|E,H) b) P(C(A,S, ¬H) = P(C,A,S, ¬H) P (A15,74) = = = P(A,S,¬H,E=e,C=c) = \(\begin{align*} P(A) \, P(S) \, P(\sigma H) \, P(E=e|A \, S, \sigma H) \, P(C=e|E=e, \sigma H) \\ e c \, P(A) \, P(S) \, P(\sigma H) \, P(E=e|A \, S, \sigma H) \, P(C=e|E=e, \sigma H) \\ e c \, P(A) \, P(B) \, = P(A).P(S).P(nH). & P(E=e/A,S,nH).P(C/E=e,nH) P(A)-P(S), P(7H). & P(E=e)A,S,7H) & P(C=c)E=e,7H) = P(A). P(S).P(7H) & P(E=e) A,S,7H) . P(C|E=e,7H) P(A) p(s) -P(7H) = &P(E=e/A,S,7H). P(C/E=e,7H) c) P(A)(H) = P(A, (,H) = \frac{\xi \xi P(A; S=S, H, E=e, C)}{\xi \xi \xi \xi P(A=a, S=S, H, E=e, C)} = \ P(A). P(S=s). P(H). P(E=el A,S=s;H). P(C| E=e|H) ₹ € P(A) P(S=S).P(H) -P(E=e|A=a,S=S,H).P((|E=e,H) = P(A).P(H) & P(S=s) . & P(E=e | A, S=s, H) P(C| E=e, H) P(H) . & P(A=0) . \$ P(S=5) . & P(E=e1A=0, S=3,H) P(C|E=e,H) = PCA). & P(S=S) & P(E=e, IA, S=S, H). PCC| E=e, H) ≥ P(A=a) ≥ P(S=s) ≥ P(E=elA=a,S=s,H) P(C|E=e,H) 0.5 [0.7(0.9.0.9 + 0.1/0.4) + 0.3(0.7,0.9+0.3,0.4)] 0,5[0.7(0.9',0.9+0.1x0.4)+0.3(0.7x0.9+0.3x0.4)]+0.5[0.7(0.8x0.9+02x0.4)+0.3(0.5x0.9+0.5x0.4)

 $\frac{5[6.7(0.9],0.9+0.1,0.4)+0.3(0.7,0.9+0.3,6.4)]+0.5[0.7(0.8],0.9+0.4,0.5)+0.3(0.5,0.9+0.4)}{0.7875}$