

COMP 4040 Analysis of Algorithms
Homework 4

1. QuickSort Algorithm (20 points)

Using the PARTITION and QUICKSORT routines in textbook 171, what value of q does each PARTITION return for the following cases? Justify your answer for each case.

- (1) when all elements in $A[p..r]$ are distinct and sorted in descending order?
- (2) when all elements in $A[p..r]$ are distinct and sorted in ascending order?

2 QuickSort Algorithm Running Time (20 points)

Provide tight upper and lower bounds on the running time of the QUICKSORT algorithm (p171) for above two cases? Show your answer (the running time) in recurrence and solve the recurrence. Justify your answer.

3. QuickSort and Substitution (20 points)

Use the substitution method to prove your answer in 2.

4. QuickSort Analysis (20 points)

Assume the partitioning algorithm always produces a 7-to-3 proportional split, write the recurrence of the running time of QuickSort in this case. Solve the recurrence by using a recursion tree.

5. QuickSort Analysis (20 points)

Exercise 7.2-5 (p178)