TABLE A.1 Cumulative binomial distribution

$$F(x) = P(X \le x) = \sum_{k=0}^{x} \frac{n!}{k!(n-k)!} p^k (1-p)^{(n-k)}$$

		p												
n	***x***	**0.05**	**0.10**	**0.20**	**0.25**	**0.30**	**0.40**	**0.50**	**0.60**	**0.70**	**0.75**	**0.80**	**0.90**	**0.95**
2	**0**	0.902	0.810	0.640	0.562	0.490	0.360	0.250	0.160	0.090	0.062	0.040	0.010	0.003
	1	0.997	0.990	0.960	0.938	0.910	0.840	0.750	0.640	0.510	0.438	0.360	0.190	0.098
	2	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
3	**0**	0.857	0.729	0.512	0.422	0.343	0.216	0.125	0.064	0.027	0.016	0.008	0.001	0.000
	1	0.993	0.972	0.896	0.844	0.784	0.648	0.500	0.352	0.216	0.156	0.104	0.028	0.007
	2	1.000	0.999	0.992	0.984	0.973	0.936	0.875	0.784	0.657	0.578	0.488	0.271	0.143
	3	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
4	**0**	0.815	0.656	0.410	0.316	0.240	0.130	0.062	0.026	0.008	0.004	0.002	0.000	0.000
	1	0.986	0.948	0.819	0.738	0.652	0.475	0.313	0.179	0.084	0.051	0.027	0.004	0.000
	2	1.000	0.996	0.973	0.949	0.916	0.821	0.688	0.525	0.348	0.262	0.181	0.052	0.014
	3	1.000	1.000	0.998	0.996	0.992	0.974	0.938	0.870	0.760	0.684	0.590	0.344	0.185
	4	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
5	**0**	0.774	0.590	0.328	0.237	0.168	0.078	0.031	0.010	0.002	0.001	0.000	0.000	0.000
	1	0.977	0.919	0.737	0.633	0.528	0.337	0.187	0.087	0.031	0.016	0.007	0.000	0.000
	2	0.999	0.991	0.942	0.896	0.837	0.683	0.500	0.317	0.163	0.104	0.058	0.009	0.001
	3	1.000	1.000	0.993	0.984	0.969	0.913	0.812	0.663	0.472	0.367	0.263	0.081	0.023
	4	1.000	1.000	1.000	0.999	0.998	0.990	0.969	0.922	0.832	0.763	0.672	0.410	0.226
	5	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
6	**0**	0.735	0.531	0.262	0.178	0.118	0.047	0.016	0.004	0.001	0.000	0.000	0.000	0.000
	1	0.967	0.886	0.655	0.534	0.420	0.233	0.109	0.041	0.011	0.005	0.002	0.000	0.000
	2	0.998	0.984	0.901	0.831	0.744	0.544	0.344	0.179	0.070	0.038	0.017	0.001	0.000
	3	1.000	0.999	0.983	0.962	0.930	0.821	0.656	0.456	0.256	0.169	0.099	0.016	0.002
	4	1.000	1.000	0.998	0.995	0.989	0.959	0.891	0.767	0.580	0.466	0.345	0.114	0.033
	5	1.000	1.000	1.000	1.000	0.999	0.996	0.984	0.953	0.882	0.822	0.738	0.469	0.265
	6	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
7	**0**	0.698	0.478	0.210	0.133	0.082	0.028	0.008	0.002	0.000	0.000	0.000	0.000	0.000
	1	0.956	0.850	0.577	0.445	0.329	0.159	0.063	0.019	0.004	0.001	0.000	0.000	0.000
	2	0.996	0.974	0.852	0.756	0.647	0.420	0.227	0.096	0.029	0.013	0.005	0.000	0.000
	3	1.000	0.997	0.967	0.929	0.874	0.710	0.500	0.290	0.126	0.071	0.033	0.003	0.000
	4	1.000	1.000	0.995	0.987	0.971	0.904	0.773	0.580	0.353	0.244	0.148	0.026	0.004
	5	1.000	1.000	1.000	0.999	0.996	0.981	0.938	0.841	0.671	0.555	0.423	0.150	0.044
	6	1.000	1.000	1.000	1.000	1.000	0.998	0.992	0.972	0.918	0.867	0.790	0.522	0.302
	7	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000

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TABLE A.1 Cumulative binomial distribution (continued)

		p											
n	x	0.05	0.10	0.20	0.25	0.30	0.40	0.50	0.60	0.70	0.75	0.80	0.90	0.95
8	0	0.663	0.430	0.168	0.100	0.058	0.017	0.004	0.001	0.000	0.000	0.000	0.000	0.000
	1	0.943	0.813	0.503	0.367	0.255	0.106	0.035	0.009	0.001	0.000	0.000	0.000	0.000
	2	0.994	0.962	0.797	0.679	0.552	0.315	0.145	0.050	0.011	0.004	0.001	0.000	0.000
	3	1.000	0.995	0.944	0.886	0.806	0.594	0.363	0.174	0.058	0.027	0.010	0.000	0.000
	4	1.000	1.000	0.990	0.973	0.942	0.826	0.637	0.406	0.194	0.114	0.056	0.005	0.000
	5	1.000	1.000	0.999	0.996	0.989	0.950	0.855	0.685	0.448	0.321	0.203	0.038	0.006
	6	1.000	1.000	1.000	1.000	0.999	0.991	0.965	0.894	0.745	0.633	0.497	0.187	0.057
	7	1.000	1.000	1.000	1.000	1.000	0.999	0.996	0.983	0.942	0.900	0.832	0.570	0.337
	8	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
9	0	0.630	0.387	0.134	0.075	0.040	0.010	0.002	0.000	0.000	0.000	0.000	0.000	0.000
	1	0.929	0.775	0.436	0.300	0.196	0.071	0.020	0.004	0.000	0.000	0.000	0.000	0.000
	2	0.992	0.947	0.738	0.601	0.463	0.232	0.090	0.025	0.004	0.001	0.000	0.000	0.000
	3	0.999	0.992	0.914	0.834	0.730	0.483	0.254	0.099	0.025	0.010	0.003	0.000	0.000
	4	1.000	0.999	0.980	0.951	0.901	0.733	0.500	0.267	0.099	0.049	0.020	0.001	0.000
	5	1.000	1.000	0.997	0.990	0.975	0.901	0.746	0.517	0.270	0.166	0.086	0.008	0.001
	6	1.000	1.000	1.000	0.999	0.996	0.975	0.910	0.768	0.537	0.399	0.262	0.053	0.008
	7	1.000	1.000	1.000	1.000	1.000	0.996	0.980	0.929	0.804	0.700	0.564	0.225	0.071
	8	1.000	1.000	1.000	1.000	1.000	1.000	0.998	0.990	0.960	0.925	0.866	0.613	0.370
	9	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
10	0	0.599	0.349	0.107	0.056	0.028	0.006	0.001	0.000	0.000	0.000	0.000	0.000	0.000
	1	0.914	0.736	0.376	0.244	0.149	0.046	0.011	0.002	0.000	0.000	0.000	0.000	0.000
	2	0.988	0.930	0.678	0.526	0.383	0.167	0.055	0.012	0.002	0.000	0.000	0.000	0.000
	3	0.999	0.987	0.879	0.776	0.650	0.382	0.172	0.055	0.011	0.004	0.001	0.000	0.000
	4	1.000	0.998	0.967	0.922	0.850	0.633	0.377	0.166	0.047	0.020	0.006	0.000	0.000
	5	1.000	1.000	0.994	0.980	0.953	0.834	0.623	0.367	0.150	0.078	0.033	0.002	0.000
	6	1.000	1.000	0.999	0.996	0.989	0.945	0.828	0.618	0.350	0.224	0.121	0.013	0.001
	7	1.000	1.000	1.000	1.000	0.998	0.988	0.945	0.833	0.617	0.474	0.322	0.070	0.012
	8	1.000	1.000	1.000	1.000	1.000	0.998	0.989	0.954	0.851	0.756	0.624	0.264	0.086
	9	1.000	1.000	1.000	1.000	1.000	1.000	0.999	0.994	0.972	0.944	0.893	0.651	0.401
	10	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
11	0	0.569	0.314	0.086	0.042	0.020	0.004	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	1	0.898	0.697	0.322	0.197	0.113	0.030	0.006	0.001	0.000	0.000	0.000	0.000	0.000
	2	0.985	0.910	0.617	0.455	0.313	0.119	0.033	0.006	0.001	0.000	0.000	0.000	0.000
	3	0.998	0.981	0.839	0.713	0.570	0.296	0.113	0.029	0.004	0.001	0.000	0.000	0.000
	4	1.000	0.997	0.950	0.885	0.790	0.533	0.274	0.099	0.022	0.008	0.002	0.000	0.000
	5	1.000	1.000	0.988	0.966	0.922	0.753	0.500	0.247	0.078	0.034	0.012	0.000	0.000
	6	1.000	1.000	0.998	0.992	0.978	0.901	0.726	0.467	0.210	0.115	0.050	0.003	0.000
	7	1.000	1.000	1.000	0.999	0.996	0.971	0.887	0.704	0.430	0.287	0.161	0.019	0.002
	8	1.000	1.000	1.000	1.000	0.999	0.994	0.967	0.881	0.687	0.545	0.383	0.090	0.015

Continued on page 807

TABLE A.1 Cumulative binomial distribution (continued)

		p												
n	***x***	**0.05**	**0.10**	**0.20**	**0.25**	**0.30**	**0.40**	**0.50**	**0.60**	**0.70**	**0.75**	**0.80**	**0.90**	**0.95**
11	**9**	1.000	1.000	1.000	1.000	1.000	0.999	0.994	0.970	0.887	0.803	0.678	0.303	0.102
	10	1.000	1.000	1.000	1.000	1.000	1.000	1.000	0.996	0.980	0.958	0.914	0.686	0.431
	11	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
12	**0**	0.540	0.282	0.069	0.032	0.014	0.002	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	1	0.882	0.659	0.275	0.158	0.085	0.020	0.003	0.000	0.000	0.000	0.000	0.000	0.000
	2	0.980	0.889	0.558	0.391	0.253	0.083	0.019	0.003	0.000	0.000	0.000	0.000	0.000
	3	0.998	0.974	0.795	0.649	0.493	0.225	0.073	0.015	0.002	0.000	0.000	0.000	0.000
	4	1.000	0.996	0.927	0.842	0.724	0.438	0.194	0.057	0.009	0.003	0.001	0.000	0.000
	5	1.000	0.999	0.981	0.946	0.882	0.665	0.387	0.158	0.039	0.014	0.004	0.000	0.000
	6	1.000	1.000	0.996	0.986	0.961	0.842	0.613	0.335	0.118	0.054	0.019	0.001	0.000
	7	1.000	1.000	0.999	0.997	0.991	0.943	0.806	0.562	0.276	0.158	0.073	0.004	0.000
	8	1.000	1.000	1.000	1.000	0.998	0.985	0.927	0.775	0.507	0.351	0.205	0.026	0.002
	9	1.000	1.000	1.000	1.000	1.000	0.997	0.981	0.917	0.747	0.609	0.442	0.111	0.020
	10	1.000	1.000	1.000	1.000	1.000	1.000	0.997	0.980	0.915	0.842	0.725	0.341	0.118
	11	1.000	1.000	1.000	1.000	1.000	1.000	1.000	0.998	0.986	0.968	0.931	0.718	0.460
	12	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
13	**0**	0.513	0.254	0.055	0.024	0.010	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	1	0.865	0.621	0.234	0.127	0.064	0.013	0.002	0.000	0.000	0.000	0.000	0.000	0.000
	2	0.975	0.866	0.502	0.333	0.202	0.058	0.011	0.001	0.000	0.000	0.000	0.000	0.000
	3	0.997	0.966	0.747	0.584	0.421	0.169	0.046	0.008	0.001	0.000	0.000	0.000	0.000
	4	1.000	0.994	0.901	0.794	0.654	0.353	0.133	0.032	0.004	0.001	0.000	0.000	0.000
	5	1.000	0.999	0.970	0.920	0.835	0.574	0.291	0.098	0.018	0.006	0.001	0.000	0.000
	6	1.000	1.000	0.993	0.976	0.938	0.771	0.500	0.229	0.062	0.024	0.007	0.000	0.000
	7	1.000	1.000	0.999	0.994	0.982	0.902	0.709	0.426	0.165	0.080	0.030	0.001	0.000
	8	1.000	1.000	1.000	0.999	0.996	0.968	0.867	0.647	0.346	0.206	0.099	0.006	0.000
	9	1.000	1.000	1.000	1.000	0.999	0.992	0.954	0.831	0.579	0.416	0.253	0.034	0.003
	10	1.000	1.000	1.000	1.000	1.000	0.999	0.989	0.942	0.798	0.667	0.498	0.134	0.025
	11	1.000	1.000	1.000	1.000	1.000	1.000	0.998	0.987	0.936	0.873	0.766	0.379	0.135
	12	1.000	1.000	1.000	1.000	1.000	1.000	1.000	0.999	0.990	0.976	0.945	0.746	0.487
	13	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
14	**0**	0.488	0.229	0.044	0.018	0.007	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	1	0.847	0.585	0.198	0.101	0.047	0.008	0.001	0.000	0.000	0.000	0.000	0.000	0.000
	2	0.970	0.842	0.448	0.281	0.161	0.040	0.006	0.001	0.000	0.000	0.000	0.000	0.000
	3	0.996	0.956	0.698	0.521	0.355	0.124	0.029	0.004	0.000	0.000	0.000	0.000	0.000
	4	1.000	0.991	0.870	0.742	0.584	0.279	0.090	0.018	0.002	0.000	0.000	0.000	0.000
	5	1.000	0.999	0.956	0.888	0.781	0.486	0.212	0.058	0.008	0.002	0.000	0.000	0.000
	6	1.000	1.000	0.988	0.962	0.907	0.692	0.395	0.150	0.031	0.010	0.002	0.000	0.000
	7	1.000	1.000	0.998	0.990	0.969	0.850	0.605	0.308	0.093	0.038	0.012	0.000	0.000

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TABLE A.1 Cumulative binomial distribution (continued)

		p												
n	x	0.05	0.10	0.20	0.25	0.30	0.40	0.50	0.60	0.70	0.75	0.80	0.90	0.95
14	8	1.000	1.000	1.000	0.998	0.992	0.942	0.788	0.514	0.219	0.112	0.044	0.001	0.000
	9	1.000	1.000	1.000	1.000	0.998	0.982	0.910	0.721	0.416	0.258	0.130	0.009	0.000
	10	1.000	1.000	1.000	1.000	1.000	0.996	0.971	0.876	0.645	0.479	0.302	0.044	0.004
	11	1.000	1.000	1.000	1.000	1.000	0.999	0.994	0.960	0.839	0.719	0.552	0.158	0.030
	12	1.000	1.000	1.000	1.000	1.000	1.000	0.999	0.992	0.953	0.899	0.802	0.415	0.153
	13	1.000	1.000	1.000	1.000	1.000	1.000	1.000	0.999	0.993	0.982	0.956	0.771	0.512
	14	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
15	0	0.463	0.206	0.035	0.013	0.005	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	1	0.829	0.549	0.167	0.080	0.035	0.005	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	2	0.964	0.816	0.398	0.236	0.127	0.027	0.004	0.000	0.000	0.000	0.000	0.000	0.000
	3	0.995	0.944	0.648	0.461	0.297	0.091	0.018	0.002	0.000	0.000	0.000	0.000	0.000
	4	0.999	0.987	0.836	0.686	0.515	0.217	0.059	0.009	0.001	0.000	0.000	0.000	0.000
	5	1.000	0.998	0.939	0.852	0.722	0.403	0.151	0.034	0.004	0.001	0.000	0.000	0.000
	6	1.000	1.000	0.982	0.943	0.869	0.610	0.304	0.095	0.015	0.004	0.001	0.000	0.000
	7	1.000	1.000	0.996	0.983	0.950	0.787	0.500	0.213	0.050	0.017	0.004	0.000	0.000
	8	1.000	1.000	0.999	0.996	0.985	0.905	0.696	0.390	0.131	0.057	0.018	0.000	0.000
	9	1.000	1.000	1.000	0.999	0.996	0.966	0.849	0.597	0.278	0.148	0.061	0.002	0.000
	10	1.000	1.000	1.000	1.000	0.999	0.991	0.941	0.783	0.485	0.314	0.164	0.013	0.001
	11	1.000	1.000	1.000	1.000	1.000	0.998	0.982	0.909	0.703	0.539	0.352	0.056	0.005
	12	1.000	1.000	1.000	1.000	1.000	1.000	0.996	0.973	0.873	0.764	0.602	0.184	0.036
	13	1.000	1.000	1.000	1.000	1.000	1.000	1.000	0.995	0.965	0.920	0.833	0.451	0.171
	14	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	0.995	0.987	0.965	0.794	0.537
	15	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
16	0	0.440	0.185	0.028	0.010	0.003	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	1	0.811	0.515	0.141	0.063	0.026	0.003	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	2	0.957	0.789	0.352	0.197	0.099	0.018	0.002	0.000	0.000	0.000	0.000	0.000	0.000
	3	0.993	0.932	0.598	0.405	0.246	0.065	0.011	0.001	0.000	0.000	0.000	0.000	0.000
	4	0.999	0.983	0.798	0.630	0.450	0.167	0.038	0.005	0.000	0.000	0.000	0.000	0.000
	5	1.000	0.997	0.918	0.810	0.660	0.329	0.105	0.019	0.002	0.000	0.000	0.000	0.000
	6	1.000	0.999	0.973	0.920	0.825	0.527	0.227	0.058	0.007	0.002	0.000	0.000	0.000
	7	1.000	1.000	0.993	0.973	0.926	0.716	0.402	0.142	0.026	0.007	0.001	0.000	0.000
	8	1.000	1.000	0.999	0.993	0.974	0.858	0.598	0.284	0.074	0.027	0.007	0.000	0.000
	9	1.000	1.000	1.000	0.998	0.993	0.942	0.773	0.473	0.175	0.080	0.027	0.001	0.000
	10	1.000	1.000	1.000	1.000	0.998	0.981	0.895	0.671	0.340	0.190	0.082	0.003	0.000
	11	1.000	1.000	1.000	1.000	1.000	0.995	0.962	0.833	0.550	0.370	0.202	0.017	0.001
	12	1.000	1.000	1.000	1.000	1.000	0.999	0.989	0.935	0.754	0.595	0.402	0.068	0.007
	13	1.000	1.000	1.000	1.000	1.000	1.000	0.998	0.982	0.901	0.803	0.648	0.211	0.043
	14	1.000	1.000	1.000	1.000	1.000	1.000	1.000	0.997	0.974	0.937	0.859	0.485	0.189
	15	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	0.997	0.990	0.972	0.815	0.560
	16	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000

Continued on page 809

TABLE A.1 Cumulative binomial distribution (continued)

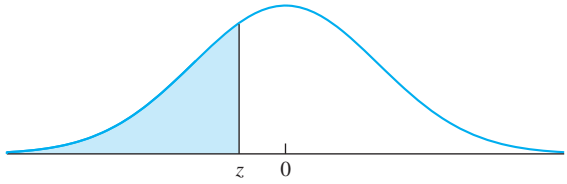
		p												
n	***x***	**0.05**	**0.10**	**0.20**	**0.25**	**0.30**	**0.40**	**0.50**	**0.60**	**0.70**	**0.75**	**0.80**	**0.90**	**0.95**
17	**0**	0.418	0.167	0.023	0.008	0.002	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	1	0.792	0.482	0.118	0.050	0.019	0.002	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	2	0.950	0.762	0.310	0.164	0.077	0.012	0.001	0.000	0.000	0.000	0.000	0.000	0.000
	3	0.991	0.917	0.549	0.353	0.202	0.046	0.006	0.000	0.000	0.000	0.000	0.000	0.000
	4	0.999	0.978	0.758	0.574	0.389	0.126	0.025	0.003	0.000	0.000	0.000	0.000	0.000
	5	1.000	0.995	0.894	0.765	0.597	0.264	0.072	0.011	0.001	0.000	0.000	0.000	0.000
	6	1.000	0.999	0.962	0.893	0.775	0.448	0.166	0.035	0.003	0.001	0.000	0.000	0.000
	7	1.000	1.000	0.989	0.960	0.895	0.641	0.315	0.092	0.013	0.003	0.000	0.000	0.000
	8	1.000	1.000	0.997	0.988	0.960	0.801	0.500	0.199	0.040	0.012	0.003	0.000	0.000
	9	1.000	1.000	1.000	0.997	0.987	0.908	0.685	0.359	0.105	0.040	0.011	0.000	0.000
	10	1.000	1.000	1.000	0.999	0.997	0.965	0.834	0.552	0.225	0.107	0.038	0.001	0.000
	11	1.000	1.000	1.000	1.000	0.999	0.989	0.928	0.736	0.403	0.235	0.106	0.005	0.000
	12	1.000	1.000	1.000	1.000	1.000	0.997	0.975	0.874	0.611	0.426	0.242	0.022	0.001
	13	1.000	1.000	1.000	1.000	1.000	1.000	0.994	0.954	0.798	0.647	0.451	0.083	0.009
	14	1.000	1.000	1.000	1.000	1.000	1.000	0.999	0.988	0.923	0.836	0.690	0.238	0.050
	15	1.000	1.000	1.000	1.000	1.000	1.000	1.000	0.998	0.981	0.950	0.882	0.518	0.208
	16	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	0.998	0.992	0.977	0.833	0.582
	17	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
18	**0**	0.397	0.150	0.018	0.006	0.002	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	1	0.774	0.450	0.099	0.039	0.014	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	2	0.942	0.734	0.271	0.135	0.060	0.008	0.001	0.000	0.000	0.000	0.000	0.000	0.000
	3	0.989	0.902	0.501	0.306	0.165	0.033	0.004	0.000	0.000	0.000	0.000	0.000	0.000
	4	0.998	0.972	0.716	0.519	0.333	0.094	0.015	0.001	0.000	0.000	0.000	0.000	0.000
	5	1.000	0.994	0.867	0.717	0.534	0.209	0.048	0.006	0.000	0.000	0.000	0.000	0.000
	6	1.000	0.999	0.949	0.861	0.722	0.374	0.119	0.020	0.001	0.000	0.000	0.000	0.000
	7	1.000	1.000	0.984	0.943	0.859	0.563	0.240	0.058	0.006	0.001	0.000	0.000	0.000
	8	1.000	1.000	0.996	0.981	0.940	0.737	0.407	0.135	0.021	0.005	0.001	0.000	0.000
	9	1.000	1.000	0.999	0.995	0.979	0.865	0.593	0.263	0.060	0.019	0.004	0.000	0.000
	10	1.000	1.000	1.000	0.999	0.994	0.942	0.760	0.437	0.141	0.057	0.016	0.000	0.000
	11	1.000	1.000	1.000	1.000	0.999	0.980	0.881	0.626	0.278	0.139	0.051	0.001	0.000
	12	1.000	1.000	1.000	1.000	1.000	0.994	0.952	0.791	0.466	0.283	0.133	0.006	0.000
	13	1.000	1.000	1.000	1.000	1.000	0.999	0.985	0.906	0.667	0.481	0.284	0.028	0.002
	14	1.000	1.000	1.000	1.000	1.000	1.000	0.996	0.967	0.835	0.694	0.499	0.098	0.011
	15	1.000	1.000	1.000	1.000	1.000	1.000	0.999	0.992	0.940	0.865	0.729	0.266	0.058
	16	1.000	1.000	1.000	1.000	1.000	1.000	1.000	0.999	0.986	0.961	0.901	0.550	0.226
	17	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	0.998	0.994	0.982	0.850	0.603
	18	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
19	**0**	0.377	0.135	0.014	0.004	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	1	0.755	0.420	0.083	0.031	0.010	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000

Continued on page 810

TABLE A.1 Cumulative binomial distribution (continued)

		p											
n	x	0.05	0.10	0.20	0.25	0.30	0.40	0.50	0.60	0.70	0.75	0.80	0.90	0.95
19	2	0.933	0.705	0.237	0.111	0.046	0.005	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	3	0.987	0.885	0.455	0.263	0.133	0.023	0.002	0.000	0.000	0.000	0.000	0.000	0.000
	4	0.998	0.965	0.673	0.465	0.282	0.070	0.010	0.001	0.000	0.000	0.000	0.000	0.000
	5	1.000	0.991	0.837	0.668	0.474	0.163	0.032	0.003	0.000	0.000	0.000	0.000	0.000
	6	1.000	0.998	0.932	0.825	0.666	0.308	0.084	0.012	0.001	0.000	0.000	0.000	0.000
	7	1.000	1.000	0.977	0.923	0.818	0.488	0.180	0.035	0.003	0.000	0.000	0.000	0.000
	8	1.000	1.000	0.993	0.971	0.916	0.667	0.324	0.088	0.011	0.002	0.000	0.000	0.000
	9	1.000	1.000	0.998	0.991	0.967	0.814	0.500	0.186	0.033	0.009	0.002	0.000	0.000
	10	1.000	1.000	1.000	0.998	0.989	0.912	0.676	0.333	0.084	0.029	0.007	0.000	0.000
	11	1.000	1.000	1.000	1.000	0.997	0.965	0.820	0.512	0.182	0.077	0.023	0.000	0.000
	12	1.000	1.000	1.000	1.000	0.999	0.988	0.916	0.692	0.334	0.175	0.068	0.002	0.000
	13	1.000	1.000	1.000	1.000	1.000	0.997	0.968	0.837	0.526	0.332	0.163	0.009	0.000
	14	1.000	1.000	1.000	1.000	1.000	0.999	0.990	0.930	0.718	0.535	0.327	0.035	0.002
	15	1.000	1.000	1.000	1.000	1.000	1.000	0.998	0.977	0.867	0.737	0.545	0.115	0.013
	16	1.000	1.000	1.000	1.000	1.000	1.000	1.000	0.995	0.954	0.889	0.763	0.295	0.067
	17	1.000	1.000	1.000	1.000	1.000	1.000	1.000	0.999	0.990	0.969	0.917	0.580	0.245
	18	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	0.999	0.996	0.986	0.865	0.623
	19	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
20	0	0.358	0.122	0.012	0.003	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	1	0.736	0.392	0.069	0.024	0.008	0.001	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	2	0.925	0.677	0.206	0.091	0.035	0.004	0.000	0.000	0.000	0.000	0.000	0.000	0.000
	3	0.984	0.867	0.411	0.225	0.107	0.016	0.001	0.000	0.000	0.000	0.000	0.000	0.000
	4	0.997	0.957	0.630	0.415	0.238	0.051	0.006	0.000	0.000	0.000	0.000	0.000	0.000
	5	1.000	0.989	0.804	0.617	0.416	0.126	0.021	0.002	0.000	0.000	0.000	0.000	0.000
	6	1.000	0.998	0.913	0.786	0.608	0.250	0.058	0.006	0.000	0.000	0.000	0.000	0.000
	7	1.000	1.000	0.968	0.898	0.772	0.416	0.132	0.021	0.001	0.000	0.000	0.000	0.000
	8	1.000	1.000	0.990	0.959	0.887	0.596	0.252	0.057	0.005	0.001	0.000	0.000	0.000
	9	1.000	1.000	0.997	0.986	0.952	0.755	0.412	0.128	0.017	0.004	0.001	0.000	0.000
	10	1.000	1.000	0.999	0.996	0.983	0.872	0.588	0.245	0.048	0.014	0.003	0.000	0.000
	11	1.000	1.000	1.000	0.999	0.995	0.943	0.748	0.404	0.113	0.041	0.010	0.000	0.000
	12	1.000	1.000	1.000	1.000	0.999	0.979	0.868	0.584	0.228	0.102	0.032	0.000	0.000
	13	1.000	1.000	1.000	1.000	1.000	0.994	0.942	0.750	0.392	0.214	0.087	0.002	0.000
	14	1.000	1.000	1.000	1.000	1.000	0.998	0.979	0.874	0.584	0.383	0.196	0.011	0.000
	15	1.000	1.000	1.000	1.000	1.000	1.000	0.994	0.949	0.762	0.585	0.370	0.043	0.003
	16	1.000	1.000	1.000	1.000	1.000	1.000	0.999	0.984	0.893	0.775	0.589	0.133	0.016
	17	1.000	1.000	1.000	1.000	1.000	1.000	1.000	0.996	0.965	0.909	0.794	0.323	0.075
	18	1.000	1.000	1.000	1.000	1.000	1.000	1.000	0.999	0.992	0.976	0.931	0.608	0.264
	19	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	0.999	0.997	0.988	0.878	0.642
	20	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000

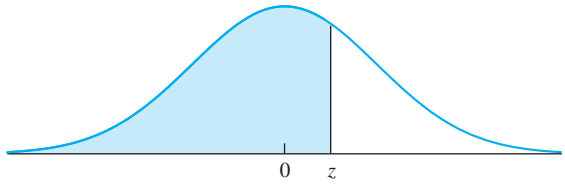
TABLE A.2 Cumulative normal distribution (z table)



z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
−3.6	.0002	.0002	.0001	.0001	.0001	.0001	.0001	.0001	.0001	.0001
−3.5	.0002	.0002	.0002	.0002	.0002	.0002	.0002	.0002	.0002	.0002
−3.4	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0002
−3.3	.0005	.0005	.0005	.0004	.0004	.0004	.0004	.0004	.0004	.0003
−3.2	.0007	.0007	.0006	.0006	.0006	.0006	.0006	.0005	.0005	.0005
−3.1	.0010	.0009	.0009	.0009	.0008	.0008	.0008	.0008	.0007	.0007
−3.0	.0013	.0013	.0013	.0012	.0012	.0011	.0011	.0011	.0010	.0010
−2.9	.0019	.0018	.0018	.0017	.0016	.0016	.0015	.0015	.0014	.0014
−2.8	.0026	.0025	.0024	.0023	.0023	.0022	.0021	.0021	.0020	.0019
−2.7	.0035	.0034	.0033	.0032	.0031	.0030	.0029	.0028	.0027	.0026
−2.6	.0047	.0045	.0044	.0043	.0041	.0040	.0039	.0038	.0037	.0036
−2.5	.0062	.0060	.0059	.0057	.0055	.0054	.0052	.0051	.0049	.0048
−2.4	.0082	.0080	.0078	.0075	.0073	.0071	.0069	.0068	.0066	.0064
−2.3	.0107	.0104	.0102	.0099	.0096	.0094	.0091	.0089	.0087	.0084
−2.2	.0139	.0136	.0132	.0129	.0125	.0122	.0119	.0116	.0113	.0110
−2.1	.0179	.0174	.0170	.0166	.0162	.0158	.0154	.0150	.0146	.0143
−2.0	.0228	.0222	.0217	.0212	.0207	.0202	.0197	.0192	.0188	.0183
−1.9	.0287	.0281	.0274	.0268	.0262	.0256	.0250	.0244	.0239	.0233
−1.8	.0359	.0351	.0344	.0336	.0329	.0322	.0314	.0307	.0301	.0294
−1.7	.0446	.0436	.0427	.0418	.0409	.0401	.0392	.0384	.0375	.0367
−1.6	.0548	.0537	.0526	.0516	.0505	.0495	.0485	.0475	.0465	.0455
−1.5	.0668	.0655	.0643	.0630	.0618	.0606	.0594	.0582	.0571	.0559
−1.4	.0808	.0793	.0778	.0764	.0749	.0735	.0721	.0708	.0694	.0681
−1.3	.0968	.0951	.0934	.0918	.0901	.0885	.0869	.0853	.0838	.0823
−1.2	.1151	.1131	.1112	.1093	.1075	.1056	.1038	.1020	.1003	.0985
−1.1	.1357	.1335	.1314	.1292	.1271	.1251	.1230	.1210	.1190	.1170
−1.0	.1587	.1562	.1539	.1515	.1492	.1469	.1446	.1423	.1401	.1379
−0.9	.1841	.1814	.1788	.1762	.1736	.1711	.1685	.1660	.1635	.1611
−0.8	.2119	.2090	.2061	.2033	.2005	.1977	.1949	.1922	.1894	.1867
−0.7	.2420	.2389	.2358	.2327	.2296	.2266	.2236	.2206	.2177	.2148
−0.6	.2743	.2709	.2676	.2643	.2611	.2578	.2546	.2514	.2483	.2451
−0.5	.3085	.3050	.3015	.2981	.2946	.2912	.2877	.2843	.2810	.2776
−0.4	.3446	.3409	.3372	.3336	.3300	.3264	.3228	.3192	.3156	.3121
−0.3	.3821	.3783	.3745	.3707	.3669	.3632	.3594	.3557	.3520	.3483
−0.2	.4207	.4168	.4129	.4090	.4052	.4013	.3974	.3936	.3897	.3859
−0.1	.4602	.4562	.4522	.4483	.4443	.4404	.4364	.4325	.4286	.4247
−0.0	.5000	.4960	.4920	.4880	.4840	.4801	.4761	.4721	.4681	.4641

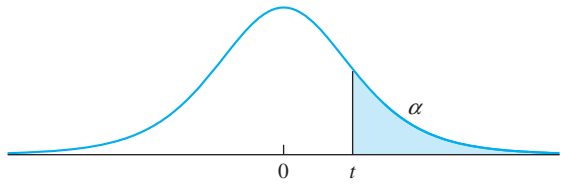
Continued on page 812

TABLE A.2 Cumulative normal distribution (continued)



z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	.5000	.5040	.5080	.5120	.5160	.5199	.5239	.5279	.5319	.5359
0.1	.5398	.5438	.5478	.5517	.5557	.5596	.5636	.5675	.5714	.5753
0.2	.5793	.5832	.5871	.5910	.5948	.5987	.6026	.6064	.6103	.6141
0.3	.6179	.6217	.6255	.6293	.6331	.6368	.6406	.6443	.6480	.6517
0.4	.6554	.6591	.6628	.6664	.6700	.6736	.6772	.6808	.6844	.6879
0.5	.6915	.6950	.6985	.7019	.7054	.7088	.7123	.7157	.7190	.7224
0.6	.7257	.7291	.7324	.7357	.7389	.7422	.7454	.7486	.7517	.7549
0.7	.7580	.7611	.7642	.7673	.7704	.7734	.7764	.7794	.7823	.7852
0.8	.7881	.7910	.7939	.7967	.7995	.8023	.8051	.8078	.8106	.8133
0.9	.8159	.8186	.8212	.8238	.8264	.8289	.8315	.8340	.8365	.8389
1.0	.8413	.8438	.8461	.8485	.8508	.8531	.8554	.8577	.8599	.8621
1.1	.8643	.8665	.8686	.8708	.8729	.8749	.8770	.8790	.8810	.8830
1.2	.8849	.8869	.8888	.8907	.8925	.8944	.8962	.8980	.8997	.9015
1.3	.9032	.9049	.9066	.9082	.9099	.9115	.9131	.9147	.9162	.9177
1.4	.9192	.9207	.9222	.9236	.9251	.9265	.9279	.9292	.9306	.9319
1.5	.9332	.9345	.9357	.9370	.9382	.9394	.9406	.9418	.9429	.9441
1.6	.9452	.9463	.9474	.9484	.9495	.9505	.9515	.9525	.9535	.9545
1.7	.9554	.9564	.9573	.9582	.9591	.9599	.9608	.9616	.9625	.9633
1.8	.9641	.9649	.9656	.9664	.9671	.9678	.9686	.9693	.9699	.9706
1.9	.9713	.9719	.9726	.9732	.9738	.9744	.9750	.9756	.9761	.9767
2.0	.9772	.9778	.9783	.9788	.9793	.9798	.9803	.9808	.9812	.9817
2.1	.9821	.9826	.9830	.9834	.9838	.9842	.9846	.9850	.9854	.9857
2.2	.9861	.9864	.9868	.9871	.9875	.9878	.9881	.9884	.9887	.9890
2.3	.9893	.9896	.9898	.9901	.9904	.9906	.9909	.9911	.9913	.9916
2.4	.9918	.9920	.9922	.9925	.9927	.9929	.9931	.9932	.9934	.9936
2.5	.9938	.9940	.9941	.9943	.9945	.9946	.9948	.9949	.9951	.9952
2.6	.9953	.9955	.9956	.9957	.9959	.9960	.9961	.9962	.9963	.9964
2.7	.9965	.9966	.9967	.9968	.9969	.9970	.9971	.9972	.9973	.9974
2.8	.9974	.9975	.9976	.9977	.9977	.9978	.9979	.9979	.9980	.9981
2.9	.9981	.9982	.9982	.9983	.9984	.9984	.9985	.9985	.9986	.9986
3.0	.9987	.9987	.9987	.9988	.9988	.9989	.9989	.9989	.9990	.9990
3.1	.9990	.9991	.9991	.9991	.9992	.9992	.9992	.9992	.9993	.9993
3.2	.9993	.9993	.9994	.9994	.9994	.9994	.9994	.9995	.9995	.9995
3.3	.9995	.9995	.9995	.9996	.9996	.9996	.9996	.9996	.9996	.9997
3.4	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9998
3.5	.9998	.9998	.9998	.9998	.9998	.9998	.9998	.9998	.9998	.9998
3.6	.9998	.9998	.9999	.9999	.9999	.9999	.9999	.9999	.9999	.9999

TABLE A.3 Upper percentage points for the Student's t distribution

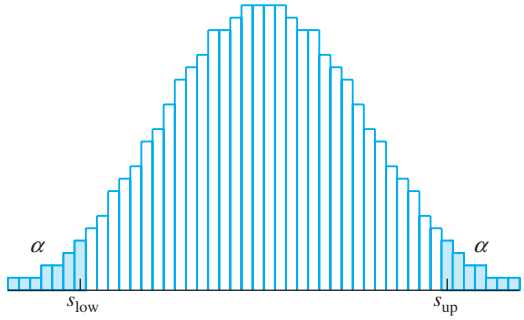


	α								
ν	**0.40**	**0.25**	**0.10**	**0.05**	**0.025**	**0.01**	**0.005**	**0.001**	**0.0005**
1	0.325	1.000	3.078	6.314	12.706	31.821	63.657	318.309	636.619
2	0.289	0.816	1.886	2.920	4.303	6.965	9.925	22.327	31.599
3	0.277	0.765	1.638	2.353	3.182	4.541	5.841	10.215	12.924
4	0.271	0.741	1.533	2.132	2.776	3.747	4.604	7.173	8.610
5	0.267	0.727	1.476	2.015	2.571	3.365	4.032	5.893	6.869
6	0.265	0.718	1.440	1.943	2.447	3.143	3.707	5.208	5.959
7	0.263	0.711	1.415	1.895	2.365	2.998	3.499	4.785	5.408
8	0.262	0.706	1.397	1.860	2.306	2.896	3.355	4.501	5.041
9	0.261	0.703	1.383	1.833	2.262	2.821	3.250	4.297	4.781
10	0.260	0.700	1.372	1.812	2.228	2.764	3.169	4.144	4.587
11	0.260	0.697	1.363	1.796	2.201	2.718	3.106	4.025	4.437
12	0.259	0.695	1.356	1.782	2.179	2.681	3.055	3.930	4.318
13	0.259	0.694	1.350	1.771	2.160	2.650	3.012	3.852	4.221
14	0.258	0.692	1.345	1.761	2.145	2.624	2.977	3.787	4.140
15	0.258	0.691	1.341	1.753	2.131	2.602	2.947	3.733	4.073
16	0.258	0.690	1.337	1.746	2.120	2.583	2.921	3.686	4.015
17	0.257	0.689	1.333	1.740	2.110	2.567	2.898	3.646	3.965
18	0.257	0.688	1.330	1.734	2.101	2.552	2.878	3.610	3.922
19	0.257	0.688	1.328	1.729	2.093	2.539	2.861	3.579	3.883
20	0.257	0.687	1.325	1.725	2.086	2.528	2.845	3.552	3.850
21	0.257	0.686	1.323	1.721	2.080	2.518	2.831	3.527	3.819
22	0.256	0.686	1.321	1.717	2.074	2.508	2.819	3.505	3.792
23	0.256	0.685	1.319	1.714	2.069	2.500	2.807	3.485	3.768
24	0.256	0.685	1.318	1.711	2.064	2.492	2.797	3.467	3.745
25	0.256	0.684	1.316	1.708	2.060	2.485	2.787	3.450	3.725
26	0.256	0.684	1.315	1.706	2.056	2.479	2.779	3.435	3.707
27	0.256	0.684	1.314	1.703	2.052	2.473	2.771	3.421	3.690
28	0.256	0.683	1.313	1.701	2.048	2.467	2.763	3.408	3.674
29	0.256	0.683	1.311	1.699	2.045	2.462	2.756	3.396	3.659
30	0.256	0.683	1.310	1.697	2.042	2.457	2.750	3.385	3.646
35	0.255	0.682	1.306	1.690	2.030	2.438	2.724	3.340	3.591
40	0.255	0.681	1.303	1.684	2.021	2.423	2.704	3.307	3.551
60	0.254	0.679	1.296	1.671	2.000	2.390	2.660	3.232	3.460
120	0.254	0.677	1.289	1.658	1.980	2.358	2.617	3.160	3.373
∞	0.253	0.674	1.282	1.645	1.960	2.326	2.576	3.090	3.291

TABLE A.4 Tolerance factors for the normal distribution

Sample Size n	Confidence Level 95% — Percent of Population Contained 90%	95%	99%	Confidence Level 99% — Percent of Population Contained 90%	95%	99%
2	32.0187	37.6746	48.4296	160.1940	188.4915	242.3004
3	8.3795	9.9158	12.8613	18.9304	22.4009	29.0553
4	5.3692	6.3699	8.2993	9.3984	11.1501	14.5274
5	4.2749	5.0787	6.6338	6.6118	7.8550	10.2602
6	3.7123	4.4140	5.7746	5.3366	6.3453	8.3013
7	3.3686	4.0074	5.2481	4.6129	5.4877	7.1868
8	3.1358	3.7317	4.8907	4.1473	4.9355	6.4683
9	2.9670	3.5317	4.6310	3.8223	4.5499	5.9660
10	2.8385	3.3794	4.4330	3.5821	4.2647	5.5943
11	2.7372	3.2592	4.2766	3.3970	4.0449	5.3075
12	2.6550	3.1617	4.1496	3.2497	3.8700	5.0792
13	2.5868	3.0808	4.0441	3.1295	3.7271	4.8926
14	2.5292	3.0124	3.9549	3.0294	3.6081	4.7371
15	2.4799	2.9538	3.8785	2.9446	3.5073	4.6053
16	2.4371	2.9029	3.8121	2.8717	3.4207	4.4920
17	2.3995	2.8583	3.7538	2.8084	3.3453	4.3934
18	2.3662	2.8188	3.7022	2.7527	3.2792	4.3068
19	2.3366	2.7835	3.6560	2.7034	3.2205	4.2300
20	2.3099	2.7518	3.6146	2.6594	3.1681	4.1614
25	2.2083	2.6310	3.4565	2.4941	2.9715	3.9039
30	2.1398	2.5494	3.3497	2.3848	2.8414	3.7333
35	2.0899	2.4900	3.2719	2.3063	2.7479	3.6107
40	2.0516	2.4445	3.2122	2.2468	2.6770	3.5177
45	2.0212	2.4083	3.1647	2.1998	2.6211	3.4443
50	1.9964	2.3787	3.1259	2.1616	2.5756	3.3846
60	1.9578	2.3328	3.0657	2.1029	2.5057	3.2929
70	1.9291	2.2987	3.0208	2.0596	2.4541	3.2251
80	1.9068	2.2720	2.9859	2.0260	2.4141	3.1725
90	1.8887	2.2506	2.9577	1.9990	2.3819	3.1303
100	1.8738	2.2328	2.9343	1.9768	2.3555	3.0955
200	1.7981	2.1425	2.8158	1.8651	2.2224	2.9207
300	1.7670	2.1055	2.7671	1.8199	2.1685	2.8499
400	1.7492	2.0843	2.7392	1.7940	2.1377	2.8094
500	1.7373	2.0701	2.7206	1.7769	2.1173	2.7826
600	1.7287	2.0598	2.7071	1.7644	2.1024	2.7631
700	1.7220	2.0519	2.6967	1.7549	2.0911	2.7481
800	1.7167	2.0456	2.6884	1.7473	2.0820	2.7362
900	1.7124	2.0404	2.6816	1.7410	2.0746	2.7264
1000	1.7087	2.0361	2.6759	1.7358	2.0683	2.7182

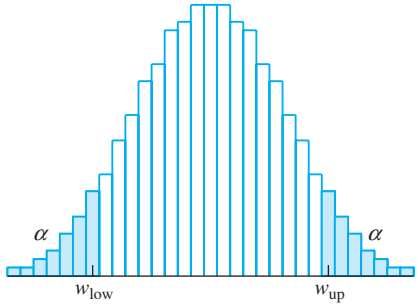
TABLE A.5 Critical points for the Wilcoxon signed-rank test



n	s_{low}	s_{up}	α
4	1	9	0.1250
	0	10	0.0625
5	3	12	0.1562
	2	13	0.0938
	1	14	0.0625
	0	15	0.0312
6	4	17	0.1094
	3	18	0.0781
	2	19	0.0469
	1	20	0.0312
	0	21	0.0156
7	6	22	0.1094
	5	23	0.0781
	4	24	0.0547
	3	25	0.0391
	2	26	0.0234
	1	27	0.0156
	0	28	0.0078
8	9	27	0.1250
	8	28	0.0977
	6	30	0.0547
	5	31	0.0391
	4	32	0.0273
	3	33	0.0195
	2	34	0.0117
	1	35	0.0078
	0	36	0.0039
9	11	34	0.1016
	10	35	0.0820
	9	36	0.0645
	8	37	0.0488
	6	39	0.0273
	5	40	0.0195
	4	41	0.0137
	3	42	0.0098
	2	43	0.0059
	1	44	0.0039
10	15	40	0.1162
	14	41	0.0967
	11	44	0.0527
	10	45	0.0420
	9	46	0.0322
	8	47	0.0244
	6	49	0.0137
	5	50	0.0098
	4	51	0.0068
	3	52	0.0049
11	18	48	0.1030
	17	49	0.0874
	14	52	0.0508
	13	53	0.0415
	11	55	0.0269
	10	56	0.0210
	8	58	0.0122
	7	59	0.0093
	6	60	0.0068
	5	61	0.0049
12	22	56	0.1018
	21	57	0.0881
	18	60	0.0549
	17	61	0.0461
	14	64	0.0261
	13	65	0.0212
	10	68	0.0105
	9	69	0.0081
	8	70	0.0061
	7	71	0.0046
13	27	64	0.1082
	26	65	0.0955
	22	69	0.0549
	21	70	0.0471
	18	73	0.0287
	17	74	0.0239
	13	78	0.0107
	12	79	0.0085
	10	81	0.0052
	9	82	0.0040
14	32	73	0.1083
	31	74	0.0969
	26	79	0.0520
	25	80	0.0453
	22	83	0.0290
	21	84	0.0247
	16	89	0.0101
	15	90	0.0083
	13	92	0.0054
	12	93	0.0043
15	37	83	0.1039
	36	84	0.0938
	31	89	0.0535
	30	90	0.0473
	26	94	0.0277
	25	95	0.0240
	20	100	0.0108
	19	101	0.0090
	16	104	0.0051
	15	105	0.0042
16	43	93	0.1057
	42	94	0.0964
	36	100	0.0523
	35	101	0.0467
	30	106	0.0253
	29	107	0.0222
	24	112	0.0107
	23	113	0.0091
	20	116	0.0055
	19	117	0.0046
17	49	104	0.1034
	48	105	0.0950
	42	111	0.0544
	41	112	0.0492
	35	118	0.0253
	34	119	0.0224
	28	125	0.0101
	27	126	0.0087
	24	129	0.0055
	23	130	0.0047
18	56	115	0.1061
	55	116	0.0982
	48	123	0.0542
	47	124	0.0494
	41	130	0.0269
	40	131	0.0241
	33	138	0.0104
	32	139	0.0091
	28	143	0.0052
	27	144	0.0045
19	63	127	0.1051
	62	128	0.0978
	54	136	0.0521
	53	137	0.0478
	47	143	0.0273
	46	144	0.0247
	38	152	0.0102
	37	153	0.0090
	33	157	0.0054
	32	158	0.0047
20	70	140	0.1012
	69	141	0.0947
	61	149	0.0527
	60	150	0.0487
	53	157	0.0266
	52	158	0.0242
	44	166	0.0107
	43	167	0.0096
	38	172	0.0053
	37	173	0.0047

For $n > 20$, compute $z = \frac{S_+ - n(n+1)/4}{\sqrt{n(n+1)(2n+1)/24}}$ and use the z table (Table A.2).

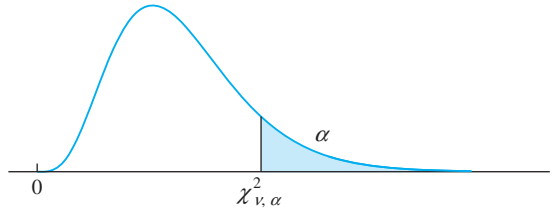
TABLE A.6 Critical points for the Wilcoxon rank-sum test



m	n	w_{low}	w_{up}	α
2	5	4	12	0.0952
		3	13	0.0476
	6	4	14	0.0714
		3	15	0.0357
	7	4	16	0.0556
		3	17	0.0278
	8	5	17	0.0889
		4	18	0.0444
		3	19	0.0222
3	4	7	17	0.0571
		6	18	0.0286
	5	8	19	0.0714
		7	20	0.0357
		6	21	0.0179
	6	9	21	0.0833
		8	22	0.0476
		7	23	0.0238
	7	9	24	0.0583
		8	25	0.0333
		7	26	0.0167
		6	27	0.0083
	8	10	26	0.0667
		9	27	0.0424
		8	28	0.0242
		7	29	0.0121
		6	30	0.0061
4	4	12	24	0.0571
		11	25	0.0286
		10	26	0.0143
	5	13	27	0.0556
		12	28	0.0317
		11	29	0.0159
		10	30	0.0079
	6	14	30	0.0571
		13	31	0.0333
		12	32	0.0190
		11	33	0.0095
		10	34	0.0048
	7	15	33	0.0545
		14	34	0.0364
		13	35	0.0212
		12	36	0.0121
		11	37	0.0061
		10	38	0.0030
	8	16	36	0.0545
		15	37	0.0364
		14	38	0.0242
		13	39	0.0141
		12	40	0.0081
		11	41	0.0040
5	5	20	35	0.0754
		19	36	0.0476
		18	37	0.0278
		17	38	0.0159
		16	39	0.0079
		15	40	0.0040
	6	21	39	0.0628
		20	40	0.0411
		19	41	0.0260
		18	42	0.0152
		17	43	0.0087
		16	44	0.0043
	7	22	43	0.0530
		21	44	0.0366
		20	45	0.0240
		19	46	0.0152
		18	47	0.0088
		17	48	0.0051
		16	49	0.0025
	8	24	46	0.0637
		23	47	0.0466
		22	48	0.0326
		21	49	0.0225
		20	50	0.0148
		19	51	0.0093
		18	52	0.0054
		17	53	0.0031
6	6	29	49	0.0660
		28	50	0.0465
		27	51	0.0325
		26	52	0.0206
		25	53	0.0130
		24	54	0.0076
		23	55	0.0043
	7	30	54	0.0507
		29	55	0.0367
		28	56	0.0256
		27	57	0.0175
		26	58	0.0111
		25	59	0.0070
		24	60	0.0041
	8	32	58	0.0539
		31	59	0.0406
		30	60	0.0296
		29	61	0.0213
		28	62	0.0147
		27	63	0.0100
		26	64	0.0063
		25	65	0.0040
7	7	40	65	0.0641
		39	66	0.0487
		37	68	0.0265
		36	69	0.0189
		35	70	0.0131
		34	71	0.0087
		33	72	0.0055
		32	73	0.0035
	8	42	70	0.0603
		41	71	0.0469
		39	73	0.0270
		38	74	0.0200
		36	76	0.0103
		35	77	0.0070
		34	78	0.0047
8	8	52	84	0.0524
		51	85	0.0415
		50	86	0.0325
		49	87	0.0249
		46	90	0.0103
		45	91	0.0074
		44	92	0.0052
		43	93	0.0035

When m and n are both greater than 8, compute $z = \frac{W - m(m+n+1)/2}{\sqrt{mn(m+n+1)/12}}$ and use the z table (Table A.2).

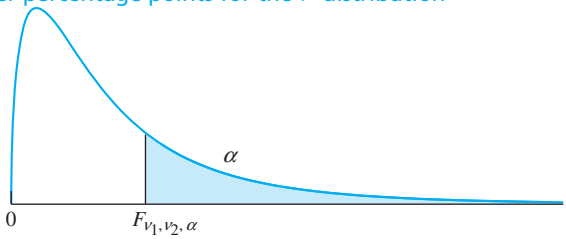
TABLE A.7 Upper percentage points for the χ^2 distribution



	α									
ν	0.995	0.99	0.975	0.95	0.90	0.10	0.05	0.025	0.01	0.005
1	0.000	0.000	0.001	0.004	0.016	2.706	3.841	5.024	6.635	7.879
2	0.010	0.020	0.051	0.103	0.211	4.605	5.991	7.378	9.210	10.597
3	0.072	0.115	0.216	0.352	0.584	6.251	7.815	9.348	11.345	12.838
4	0.207	0.297	0.484	0.711	1.064	7.779	9.488	11.143	13.277	14.860
5	0.412	0.554	0.831	1.145	1.610	9.236	11.070	12.833	15.086	16.750
6	0.676	0.872	1.237	1.635	2.204	10.645	12.592	14.449	16.812	18.548
7	0.989	1.239	1.690	2.167	2.833	12.017	14.067	16.013	18.475	20.278
8	1.344	1.646	2.180	2.733	3.490	13.362	15.507	17.535	20.090	21.955
9	1.735	2.088	2.700	3.325	4.168	14.684	16.919	19.023	21.666	23.589
10	2.156	2.558	3.247	3.940	4.865	15.987	18.307	20.483	23.209	25.188
11	2.603	3.053	3.816	4.575	5.578	17.275	19.675	21.920	24.725	26.757
12	3.074	3.571	4.404	5.226	6.304	18.549	21.026	23.337	26.217	28.300
13	3.565	4.107	5.009	5.892	7.042	19.812	22.362	24.736	27.688	29.819
14	4.075	4.660	5.629	6.571	7.790	21.064	23.685	26.119	29.141	31.319
15	4.601	5.229	6.262	7.261	8.547	22.307	24.996	27.488	30.578	32.801
16	5.142	5.812	6.908	7.962	9.312	23.542	26.296	28.845	32.000	34.267
17	5.697	6.408	7.564	8.672	10.085	24.769	27.587	30.191	33.409	35.718
18	6.265	7.015	8.231	9.390	10.865	25.989	28.869	31.526	34.805	37.156
19	6.844	7.633	8.907	10.117	11.651	27.204	30.144	32.852	36.191	38.582
20	7.434	8.260	9.591	10.851	12.443	28.412	31.410	34.170	37.566	39.997
21	8.034	8.897	10.283	11.591	13.240	29.615	32.671	35.479	38.932	41.401
22	8.643	9.542	10.982	12.338	14.041	30.813	33.924	36.781	40.289	42.796
23	9.260	10.196	11.689	13.091	14.848	32.007	35.172	38.076	41.638	44.181
24	9.886	10.856	12.401	13.848	15.659	33.196	36.415	39.364	42.980	45.559
25	10.520	11.524	13.120	14.611	16.473	34.382	37.652	40.646	44.314	46.928
26	11.160	12.198	13.844	15.379	17.292	35.563	38.885	41.923	45.642	48.290
27	11.808	12.879	14.573	16.151	18.114	36.741	40.113	43.195	46.963	49.645
28	12.461	13.565	15.308	16.928	18.939	37.916	41.337	44.461	48.278	50.993
29	13.121	14.256	16.047	17.708	19.768	39.087	42.557	45.722	49.588	52.336
30	13.787	14.953	16.791	18.493	20.599	40.256	43.773	46.979	50.892	53.672
31	14.458	15.655	17.539	19.281	21.434	41.422	44.985	48.232	52.191	55.003
32	15.134	16.362	18.291	20.072	22.271	42.585	46.194	49.480	53.486	56.328
33	15.815	17.074	19.047	20.867	23.110	43.745	47.400	50.725	54.776	57.648
34	16.501	17.789	19.806	21.664	23.952	44.903	48.602	51.966	56.061	58.964
35	17.192	18.509	20.569	22.465	24.797	46.059	49.802	53.203	57.342	60.275
36	17.887	19.233	21.336	23.269	25.643	47.212	50.998	54.437	58.619	61.581
37	18.586	19.960	22.106	24.075	26.492	48.363	52.192	55.668	59.893	62.883
38	19.289	20.691	22.878	24.884	27.343	49.513	53.384	56.896	61.162	64.181
39	19.996	21.426	23.654	25.695	28.196	50.660	54.572	58.120	62.428	65.476
40	20.707	22.164	24.433	26.509	29.051	51.805	55.758	59.342	63.691	66.766

For $\nu > 40$, $\chi^2_{\nu,\alpha} \approx 0.5(z_\alpha + \sqrt{2\nu - 1})^2$.

TABLE A.8 Upper percentage points for the F distribution



		ν_1								
ν_2	α	1	2	3	4	5	6	7	8	9
1	0.100	39.86	49.50	53.59	55.83	57.24	58.20	58.91	59.44	59.86
	0.050	161.45	199.50	215.71	224.58	230.16	233.99	236.77	238.88	240.54
	0.010	4052.18	4999.50	5403.35	5624.58	5763.65	5858.99	5928.36	5981.07	6022.47
	0.001	405284	500012	540382	562501	576405	585938	592874	598144	603040
2	0.100	8.53	9.00	9.16	9.24	9.29	9.33	9.35	9.37	9.38
	0.050	18.51	19.00	19.16	19.25	19.30	19.33	19.35	19.37	19.38
	0.010	98.50	99.00	99.17	99.25	99.30	99.33	99.36	99.37	99.39
	0.001	998.50	999.00	999.17	999.25	999.30	999.33	999.36	999.37	999.39
3	0.100	5.54	5.46	5.39	5.34	5.31	5.28	5.27	5.25	5.24
	0.050	10.13	9.55	9.28	9.12	9.01	8.94	8.89	8.85	8.81
	0.010	34.12	30.82	29.46	28.71	28.24	27.91	27.67	27.49	27.35
	0.001	167.03	148.50	141.11	137.10	134.58	132.85	131.58	130.62	129.86
4	0.100	4.54	4.32	4.19	4.11	4.05	4.01	3.98	3.95	3.94
	0.050	7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	6.00
	0.010	21.20	18.00	16.69	15.98	15.52	15.21	14.98	14.80	14.66
	0.001	74.14	61.25	56.18	53.44	51.71	50.53	49.66	49.00	48.47
5	0.100	4.06	3.78	3.62	3.52	3.45	3.40	3.37	3.34	3.32
	0.050	6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.77
	0.010	16.26	13.27	12.06	11.39	10.97	10.67	10.46	10.29	10.16
	0.001	47.18	37.12	33.20	31.09	29.75	28.83	28.16	27.65	27.24
6	0.100	3.78	3.46	3.29	3.18	3.11	3.05	3.01	2.98	2.96
	0.050	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.10
	0.010	13.75	10.92	9.78	9.15	8.75	8.47	8.26	8.10	7.98
	0.001	35.51	27.00	23.70	21.92	20.80	20.03	19.46	19.03	18.69
7	0.100	3.59	3.26	3.07	2.96	2.88	2.83	2.78	2.75	2.72
	0.050	5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.68
	0.010	12.25	9.55	8.45	7.85	7.46	7.19	6.99	6.84	6.72
	0.001	29.25	21.69	18.77	17.20	16.21	15.52	15.02	14.63	14.33
8	0.100	3.46	3.11	2.92	2.81	2.73	2.67	2.62	2.59	2.56
	0.050	5.32	4.46	4.07	3.84	3.69	3.58	3.50	3.44	3.39
	0.010	11.26	8.65	7.59	7.01	6.63	6.37	6.18	6.03	5.91
	0.001	25.41	18.49	15.83	14.39	13.48	12.86	12.40	12.05	11.77
9	0.100	3.36	3.01	2.81	2.69	2.61	2.55	2.51	2.47	2.44
	0.050	5.12	4.26	3.86	3.63	3.48	3.37	3.29	3.23	3.18
	0.010	10.56	8.02	6.99	6.42	6.06	5.80	5.61	5.47	5.35
	0.001	22.86	16.39	13.90	12.56	11.71	11.13	10.70	10.37	10.11

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TABLE A.8 Upper percentage points for the F distribution (continued)

		ν_1								
ν_2	α	10	12	15	20	25	30	40	50	60
1	0.100	60.19	60.71	61.22	61.74	62.05	62.26	62.53	62.69	62.79
	0.050	241.88	243.91	245.95	248.01	249.26	250.10	251.14	251.77	252.20
	0.010	6055.85	6106.32	6157.29	6208.73	6239.83	6260.65	6286.78	6302.52	6313.03
	0.001	606316	611276	616292	621362	624430	626486	659725	660511	6610390
2	0.100	9.39	9.41	9.42	9.44	9.45	9.46	9.47	9.47	9.47
	0.050	19.40	19.41	19.43	19.45	19.46	19.46	19.47	19.48	19.48
	0.010	99.40	99.42	99.43	99.45	99.46	99.47	99.47	99.48	99.48
	0.001	999.40	999.42	999.43	999.45	999.46	999.47	999.47	999.48	999.48
3	0.100	5.23	5.22	5.20	5.18	5.17	5.17	5.16	5.15	5.15
	0.050	8.79	8.74	8.70	8.66	8.63	8.62	8.59	8.58	8.57
	0.010	27.23	27.05	26.87	26.69	26.58	26.50	26.41	26.35	26.32
	0.001	129.25	128.32	127.37	126.42	125.84	125.45	124.96	124.66	124.47
4	0.100	3.92	3.90	3.87	3.84	3.83	3.82	3.80	3.80	3.79
	0.050	5.96	5.91	5.86	5.80	5.77	5.75	5.72	5.70	5.69
	0.010	14.55	14.37	14.20	14.02	13.91	13.84	13.75	13.69	13.65
	0.001	48.05	47.41	46.76	46.10	45.70	45.43	45.09	44.88	44.75
5	0.100	3.30	3.27	3.24	3.21	3.19	3.17	3.16	3.15	3.14
	0.050	4.74	4.68	4.62	4.56	4.52	4.50	4.46	4.44	4.43
	0.010	10.05	9.89	9.72	9.55	9.45	9.38	9.29	9.24	9.20
	0.001	26.92	26.42	25.91	25.39	25.08	24.87	24.60	24.44	24.33
6	0.100	2.94	2.90	2.87	2.84	2.81	2.80	2.78	2.77	2.76
	0.050	4.06	4.00	3.94	3.87	3.83	3.81	3.77	3.75	3.74
	0.010	7.87	7.72	7.56	7.40	7.30	7.23	7.14	7.09	7.06
	0.001	18.41	17.99	17.56	17.12	16.85	16.67	16.44	16.31	16.21
7	0.100	2.70	2.67	2.63	2.59	2.57	2.56	2.54	2.52	2.51
	0.050	3.64	3.57	3.51	3.44	3.40	3.38	3.34	3.32	3.30
	0.010	6.62	6.47	6.31	6.16	6.06	5.99	5.91	5.86	5.82
	0.001	14.08	13.71	13.32	12.93	12.69	12.53	12.33	12.20	12.12
8	0.100	2.54	2.50	2.46	2.42	2.40	2.38	2.36	2.35	2.34
	0.050	3.35	3.28	3.22	3.15	3.11	3.08	3.04	3.02	3.01
	0.010	5.81	5.67	5.52	5.36	5.26	5.20	5.12	5.07	5.03
	0.001	11.54	11.19	10.84	10.48	10.26	10.11	9.92	9.80	9.73
9	0.100	2.42	2.38	2.34	2.30	2.27	2.25	2.23	2.22	2.21
	0.050	3.14	3.07	3.01	2.94	2.89	2.86	2.83	2.80	2.79
	0.010	5.26	5.11	4.96	4.81	4.71	4.65	4.57	4.52	4.48
	0.001	9.89	9.57	9.24	8.90	8.69	8.55	8.37	8.26	8.19

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TABLE A.8 Upper percentage points for the F distribution (continued)

		ν_1								
ν_2	α	1	2	3	4	5	6	7	8	9
10	0.100	3.29	2.92	2.73	2.61	2.52	2.46	2.41	2.38	2.35
	0.050	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	3.02
	0.010	10.04	7.56	6.55	5.99	5.64	5.39	5.20	5.06	4.94
	0.001	21.04	14.91	12.55	11.28	10.48	9.93	9.52	9.20	8.96
11	0.100	3.23	2.86	2.66	2.54	2.45	2.39	2.34	2.30	2.27
	0.050	4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.90
	0.010	9.65	7.21	6.22	5.67	5.32	5.07	4.89	4.74	4.63
	0.001	19.69	13.81	11.56	10.35	9.58	9.05	8.66	8.35	8.12
12	0.100	3.18	2.81	2.61	2.48	2.39	2.33	2.28	2.24	2.21
	0.050	4.75	3.89	3.49	3.26	3.11	3.00	2.91	2.85	2.80
	0.010	9.33	6.93	5.95	5.41	5.06	4.82	4.64	4.50	4.39
	0.001	18.64	12.97	10.80	9.63	8.89	8.38	8.00	7.71	7.48
13	0.100	3.14	2.76	2.56	2.43	2.35	2.28	2.23	2.20	2.16
	0.050	4.67	3.81	3.41	3.18	3.03	2.92	2.83	2.77	2.71
	0.010	9.07	6.70	5.74	5.21	4.86	4.62	4.44	4.30	4.19
	0.001	17.82	12.31	10.21	9.07	8.35	7.86	7.49	7.21	6.98
14	0.100	3.10	2.73	2.52	2.39	2.31	2.24	2.19	2.15	2.12
	0.050	4.60	3.74	3.34	3.11	2.96	2.85	2.76	2.70	2.65
	0.010	8.86	6.51	5.56	5.04	4.69	4.46	4.28	4.14	4.03
	0.001	17.14	11.78	9.73	8.62	7.92	7.44	7.08	6.80	6.58
15	0.100	3.07	2.70	2.49	2.36	2.27	2.21	2.16	2.12	2.09
	0.050	4.54	3.68	3.29	3.06	2.90	2.79	2.71	2.64	2.59
	0.010	8.68	6.36	5.42	4.89	4.56	4.32	4.14	4.00	3.89
	0.001	16.59	11.34	9.34	8.25	7.57	7.09	6.74	6.47	6.26
16	0.100	3.05	2.67	2.46	2.33	2.24	2.18	2.13	2.09	2.06
	0.050	4.49	3.63	3.24	3.01	2.85	2.74	2.66	2.59	2.54
	0.010	8.53	6.23	5.29	4.77	4.44	4.20	4.03	3.89	3.78
	0.001	16.12	10.97	9.01	7.94	7.27	6.80	6.46	6.19	5.98
17	0.100	3.03	2.64	2.44	2.31	2.22	2.15	2.10	2.06	2.03
	0.050	4.45	3.59	3.20	2.96	2.81	2.70	2.61	2.55	2.49
	0.010	8.40	6.11	5.18	4.67	4.34	4.10	3.93	3.79	3.68
	0.001	15.72	10.66	8.73	7.68	7.02	6.56	6.22	5.96	5.75
18	0.100	3.01	2.62	2.42	2.29	2.20	2.13	2.08	2.04	2.00
	0.050	4.41	3.55	3.16	2.93	2.77	2.66	2.58	2.51	2.46
	0.010	8.29	6.01	5.09	4.58	4.25	4.01	3.84	3.71	3.60
	0.001	15.38	10.39	8.49	7.46	6.81	6.35	6.02	5.76	5.56
19	0.100	2.99	2.61	2.40	2.27	2.18	2.11	2.06	2.02	1.98
	0.050	4.38	3.52	3.13	2.90	2.74	2.63	2.54	2.48	2.42
	0.010	8.18	5.93	5.01	4.50	4.17	3.94	3.77	3.63	3.52
	0.001	15.08	10.16	8.28	7.27	6.62	6.18	5.85	5.59	5.39
20	0.100	2.97	2.59	2.38	2.25	2.16	2.09	2.04	2.00	1.96
	0.050	4.35	3.49	3.10	2.87	2.71	2.60	2.51	2.45	2.39
	0.010	8.10	5.85	4.94	4.43	4.10	3.87	3.70	3.56	3.46
	0.001	14.82	9.95	8.10	7.10	6.46	6.02	5.69	5.44	5.24

Continued on page 821

TABLE A.8 Upper percentage points for the F distribution (continued)

		ν_1								
ν_2	α	10	12	15	20	25	30	40	50	60
10	0.100	2.32	2.28	2.24	2.20	2.17	2.16	2.13	2.12	2.11
	0.050	2.98	2.91	2.85	2.77	2.73	2.70	2.66	2.64	2.62
	0.010	4.85	4.71	4.56	4.41	4.31	4.25	4.17	4.12	4.08
	0.001	8.75	8.45	8.13	7.80	7.60	7.47	7.30	7.19	7.12
11	0.100	2.25	2.21	2.17	2.12	2.10	2.08	2.05	2.04	2.03
	0.050	2.85	2.79	2.72	2.65	2.60	2.57	2.53	2.51	2.49
	0.010	4.54	4.40	4.25	4.10	4.01	3.94	3.86	3.81	3.78
	0.001	7.92	7.63	7.32	7.01	6.81	6.68	6.52	6.42	6.35
12	0.100	2.19	2.15	2.10	2.06	2.03	2.01	1.99	1.97	1.96
	0.050	2.75	2.69	2.62	2.54	2.50	2.47	2.43	2.40	2.38
	0.010	4.30	4.16	4.01	3.86	3.76	3.70	3.62	3.57	3.54
	0.001	7.29	7.00	6.71	6.40	6.22	6.09	5.93	5.83	5.76
13	0.100	2.14	2.10	2.05	2.01	1.98	1.96	1.93	1.92	1.90
	0.050	2.67	2.60	2.53	2.46	2.41	2.38	2.34	2.31	2.30
	0.010	4.10	3.96	3.82	3.66	3.57	3.51	3.43	3.38	3.34
	0.001	6.80	6.52	6.23	5.93	5.75	5.63	5.47	5.37	5.30
14	0.100	2.10	2.05	2.01	1.96	1.93	1.91	1.89	1.87	1.86
	0.050	2.60	2.53	2.46	2.39	2.34	2.31	2.27	2.24	2.22
	0.010	3.94	3.80	3.66	3.51	3.41	3.35	3.27	3.22	3.18
	0.001	6.40	6.13	5.85	5.56	5.38	5.25	5.10	5.00	4.94
15	0.100	2.06	2.02	1.97	1.92	1.89	1.87	1.85	1.83	1.82
	0.050	2.54	2.48	2.40	2.33	2.28	2.25	2.20	2.18	2.16
	0.010	3.80	3.67	3.52	3.37	3.28	3.21	3.13	3.08	3.05
	0.001	6.08	5.81	5.54	5.25	5.07	4.95	4.80	4.70	4.64
16	0.100	2.03	1.99	1.94	1.89	1.86	1.84	1.81	1.79	1.78
	0.050	2.49	2.42	2.35	2.28	2.23	2.19	2.15	2.12	2.11
	0.010	3.69	3.55	3.41	3.26	3.16	3.10	3.02	2.97	2.93
	0.001	5.81	5.55	5.27	4.99	4.82	4.70	4.54	4.45	4.39
17	0.100	2.00	1.96	1.91	1.86	1.83	1.81	1.78	1.76	1.75
	0.050	2.45	2.38	2.31	2.23	2.18	2.15	2.10	2.08	2.06
	0.010	3.59	3.46	3.31	3.16	3.07	3.00	2.92	2.87	2.83
	0.001	5.58	5.32	5.05	4.78	4.60	4.48	4.33	4.24	4.18
18	0.100	1.98	1.93	1.89	1.84	1.80	1.78	1.75	1.74	1.72
	0.050	2.41	2.34	2.27	2.19	2.14	2.11	2.06	2.04	2.02
	0.010	3.51	3.37	3.23	3.08	2.98	2.92	2.84	2.78	2.75
	0.001	5.39	5.13	4.87	4.59	4.42	4.30	4.15	4.06	4.00
19	0.100	1.96	1.91	1.86	1.81	1.78	1.76	1.73	1.71	1.70
	0.050	2.38	2.31	2.23	2.16	2.11	2.07	2.03	2.00	1.98
	0.010	3.43	3.30	3.15	3.00	2.91	2.84	2.76	2.71	2.67
	0.001	5.22	4.97	4.70	4.43	4.26	4.14	3.99	3.90	3.84
20	0.100	1.94	1.89	1.84	1.79	1.76	1.74	1.71	1.69	1.68
	0.050	2.35	2.28	2.20	2.12	2.07	2.04	1.99	1.97	1.95
	0.010	3.37	3.23	3.09	2.94	2.84	2.78	2.69	2.64	2.61
	0.001	5.08	4.82	4.56	4.29	4.12	4.00	3.86	3.77	3.70

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TABLE A.8 Upper percentage points for the F distribution (continued)

		ν_1								
ν_2	α	1	2	3	4	5	6	7	8	9
21	0.100	2.96	2.57	2.36	2.23	2.14	2.08	2.02	1.98	1.95
	0.050	4.32	3.47	3.07	2.84	2.68	2.57	2.49	2.42	2.37
	0.010	8.02	5.78	4.87	4.37	4.04	3.81	3.64	3.51	3.40
	0.001	14.59	9.77	7.94	6.95	6.32	5.88	5.56	5.31	5.11
22	0.100	2.95	2.56	2.35	2.22	2.13	2.06	2.01	1.97	1.93
	0.050	4.30	3.44	3.05	2.82	2.66	2.55	2.46	2.40	2.34
	0.010	7.95	5.72	4.82	4.31	3.99	3.76	3.59	3.45	3.35
	0.001	14.38	9.61	7.80	6.81	6.19	5.76	5.44	5.19	4.99
23	0.100	2.94	2.55	2.34	2.21	2.11	2.05	1.99	1.95	1.92
	0.050	4.28	3.42	3.03	2.80	2.64	2.53	2.44	2.37	2.32
	0.010	7.88	5.66	4.76	4.26	3.94	3.71	3.54	3.41	3.30
	0.001	14.20	9.47	7.67	6.70	6.08	5.65	5.33	5.09	4.89
24	0.100	2.93	2.54	2.33	2.19	2.10	2.04	1.98	1.94	1.91
	0.050	4.26	3.40	3.01	2.78	2.62	2.51	2.42	2.36	2.30
	0.010	7.82	5.61	4.72	4.22	3.90	3.67	3.50	3.36	3.26
	0.001	14.03	9.34	7.55	6.59	5.98	5.55	5.23	4.99	4.80
25	0.100	2.92	2.53	2.32	2.18	2.09	2.02	1.97	1.93	1.89
	0.050	4.24	3.39	2.99	2.76	2.60	2.49	2.40	2.34	2.28
	0.010	7.77	5.57	4.68	4.18	3.85	3.63	3.46	3.32	3.22
	0.001	13.88	9.22	7.45	6.49	5.89	5.46	5.15	4.91	4.71
26	0.100	2.91	2.52	2.31	2.17	2.08	2.01	1.96	1.92	1.88
	0.050	4.23	3.37	2.98	2.74	2.59	2.47	2.39	2.32	2.27
	0.010	7.72	5.53	4.64	4.14	3.82	3.59	3.42	3.29	3.18
	0.001	13.74	9.12	7.36	6.41	5.80	5.38	5.07	4.83	4.64
27	0.100	2.90	2.51	2.30	2.17	2.07	2.00	1.95	1.91	1.87
	0.050	4.21	3.35	2.96	2.73	2.57	2.46	2.37	2.31	2.25
	0.010	7.68	5.49	4.60	4.11	3.78	3.56	3.39	3.26	3.15
	0.001	13.61	9.02	7.27	6.33	5.73	5.31	5.00	4.76	4.57
28	0.100	2.89	2.50	2.29	2.16	2.06	2.00	1.94	1.90	1.87
	0.050	4.20	3.34	2.95	2.71	2.56	2.45	2.36	2.29	2.24
	0.010	7.64	5.45	4.57	4.07	3.75	3.53	3.36	3.23	3.12
	0.001	13.50	8.93	7.19	6.25	5.66	5.24	4.93	4.69	4.50
29	0.100	2.89	2.50	2.28	2.15	2.06	1.99	1.93	1.89	1.86
	0.050	4.18	3.33	2.93	2.70	2.55	2.43	2.35	2.28	2.22
	0.010	7.60	5.42	4.54	4.04	3.73	3.50	3.33	3.20	3.09
	0.001	13.39	8.85	7.12	6.19	5.59	5.18	4.87	4.64	4.45
30	0.100	2.88	2.49	2.28	2.14	2.05	1.98	1.93	1.88	1.85
	0.050	4.17	3.32	2.92	2.69	2.53	2.42	2.33	2.27	2.21
	0.010	7.56	5.39	4.51	4.02	3.70	3.47	3.30	3.17	3.07
	0.001	13.29	8.77	7.05	6.12	5.53	5.12	4.82	4.58	4.39
31	0.100	2.87	2.48	2.27	2.14	2.04	1.97	1.92	1.88	1.84
	0.050	4.16	3.30	2.91	2.68	2.52	2.41	2.32	2.25	2.20
	0.010	7.53	5.36	4.48	3.99	3.67	3.45	3.28	3.15	3.04
	0.001	13.20	8.70	6.99	6.07	5.48	5.07	4.77	4.53	4.34

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TABLE A.8 Upper percentage points for the F distribution (continued)

		ν_1								
ν_2	α	10	12	15	20	25	30	40	50	60
21	0.100	1.92	1.87	1.83	1.78	1.74	1.72	1.69	1.67	1.66
	0.050	2.32	2.25	2.18	2.10	2.05	2.01	1.96	1.94	1.92
	0.010	3.31	3.17	3.03	2.88	2.79	2.72	2.64	2.58	2.55
	0.001	4.95	4.70	4.44	4.17	4.00	3.88	3.74	3.64	3.58
22	0.100	1.90	1.86	1.81	1.76	1.73	1.70	1.67	1.65	1.64
	0.050	2.30	2.23	2.15	2.07	2.02	1.98	1.94	1.91	1.89
	0.010	3.26	3.12	2.98	2.83	2.73	2.67	2.58	2.53	2.50
	0.001	4.83	4.58	4.33	4.06	3.89	3.78	3.63	3.54	3.48
23	0.100	1.89	1.84	1.80	1.74	1.71	1.69	1.66	1.64	1.62
	0.050	2.27	2.20	2.13	2.05	2.00	1.96	1.91	1.88	1.86
	0.010	3.21	3.07	2.93	2.78	2.69	2.62	2.54	2.48	2.45
	0.001	4.73	4.48	4.23	3.96	3.79	3.68	3.53	3.44	3.38
24	0.100	1.88	1.83	1.78	1.73	1.70	1.67	1.64	1.62	1.61
	0.050	2.25	2.18	2.11	2.03	1.97	1.94	1.89	1.86	1.84
	0.010	3.17	3.03	2.89	2.74	2.64	2.58	2.49	2.44	2.40
	0.001	4.64	4.39	4.14	3.87	3.71	3.59	3.45	3.36	3.29
25	0.100	1.87	1.82	1.77	1.72	1.68	1.66	1.63	1.61	1.59
	0.050	2.24	2.16	2.09	2.01	1.96	1.92	1.87	1.84	1.82
	0.010	3.13	2.99	2.85	2.70	2.60	2.54	2.45	2.40	2.36
	0.001	4.56	4.31	4.06	3.79	3.63	3.52	3.37	3.28	3.22
26	0.100	1.86	1.81	1.76	1.71	1.67	1.65	1.61	1.59	1.58
	0.050	2.22	2.15	2.07	1.99	1.94	1.90	1.85	1.82	1.80
	0.010	3.09	2.96	2.81	2.66	2.57	2.50	2.42	2.36	2.33
	0.001	4.48	4.24	3.99	3.72	3.56	3.44	3.30	3.21	3.15
27	0.100	1.85	1.80	1.75	1.70	1.66	1.64	1.60	1.58	1.57
	0.050	2.20	2.13	2.06	1.97	1.92	1.88	1.84	1.81	1.79
	0.010	3.06	2.93	2.78	2.63	2.54	2.47	2.38	2.33	2.29
	0.001	4.41	4.17	3.92	3.66	3.49	3.38	3.23	3.14	3.08
28	0.100	1.84	1.79	1.74	1.69	1.65	1.63	1.59	1.57	1.56
	0.050	2.19	2.12	2.04	1.96	1.91	1.87	1.82	1.79	1.77
	0.010	3.03	2.90	2.75	2.60	2.51	2.44	2.35	2.30	2.26
	0.001	4.35	4.11	3.86	3.60	3.43	3.32	3.18	3.09	3.02
29	0.100	1.83	1.78	1.73	1.68	1.64	1.62	1.58	1.56	1.55
	0.050	2.18	2.10	2.03	1.94	1.89	1.85	1.81	1.77	1.75
	0.010	3.00	2.87	2.73	2.57	2.48	2.41	2.33	2.27	2.23
	0.001	4.29	4.05	3.80	3.54	3.38	3.27	3.12	3.03	2.97
30	0.100	1.82	1.77	1.72	1.67	1.63	1.61	1.57	1.55	1.54
	0.050	2.16	2.09	2.01	1.93	1.88	1.84	1.79	1.76	1.74
	0.010	2.98	2.84	2.70	2.55	2.45	2.39	2.30	2.25	2.21
	0.001	4.24	4.00	3.75	3.49	3.33	3.22	3.07	2.98	2.92
31	0.100	1.81	1.77	1.71	1.66	1.62	1.60	1.56	1.54	1.53
	0.050	2.15	2.08	2.00	1.92	1.87	1.83	1.78	1.75	1.73
	0.010	2.96	2.82	2.68	2.52	2.43	2.36	2.27	2.22	2.18
	0.001	4.19	3.95	3.71	3.45	3.28	3.17	3.03	2.94	2.87

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TABLE A.8 Upper percentage points for the F distribution (continued)

		ν_1								
ν_2	α	1	2	3	4	5	6	7	8	9
32	0.100	2.87	2.48	2.26	2.13	2.04	1.97	1.91	1.87	1.83
	0.050	4.15	3.29	2.90	2.67	2.51	2.40	2.31	2.24	2.19
	0.010	7.50	5.34	4.46	3.97	3.65	3.43	3.26	3.13	3.02
	0.001	13.12	8.64	6.94	6.01	5.43	5.02	4.72	4.48	4.30
33	0.100	2.86	2.47	2.26	2.12	2.03	1.96	1.91	1.86	1.83
	0.050	4.14	3.28	2.89	2.66	2.50	2.39	2.30	2.23	2.18
	0.010	7.47	5.31	4.44	3.95	3.63	3.41	3.24	3.11	3.00
	0.001	13.04	8.58	6.88	5.97	5.38	4.98	4.67	4.44	4.26
34	0.100	2.86	2.47	2.25	2.12	2.02	1.96	1.90	1.86	1.82
	0.050	4.13	3.28	2.88	2.65	2.49	2.38	2.29	2.23	2.17
	0.010	7.44	5.29	4.42	3.93	3.61	3.39	3.22	3.09	2.98
	0.001	12.97	8.52	6.83	5.92	5.34	4.93	4.63	4.40	4.22
35	0.100	2.85	2.46	2.25	2.11	2.02	1.95	1.90	1.85	1.82
	0.050	4.12	3.27	2.87	2.64	2.49	2.37	2.29	2.22	2.16
	0.010	7.42	5.27	4.40	3.91	3.59	3.37	3.20	3.07	2.96
	0.001	12.90	8.47	6.79	5.88	5.30	4.89	4.59	4.36	4.18
36	0.100	2.85	2.46	2.24	2.11	2.01	1.94	1.89	1.85	1.81
	0.050	4.11	3.26	2.87	2.63	2.48	2.36	2.28	2.21	2.15
	0.010	7.40	5.25	4.38	3.89	3.57	3.35	3.18	3.05	2.95
	0.001	12.83	8.42	6.74	5.84	5.26	4.86	4.56	4.33	4.14
37	0.100	2.85	2.45	2.24	2.10	2.01	1.94	1.89	1.84	1.81
	0.050	4.11	3.25	2.86	2.63	2.47	2.36	2.27	2.20	2.14
	0.010	7.37	5.23	4.36	3.87	3.56	3.33	3.17	3.04	2.93
	0.001	12.77	8.37	6.70	5.80	5.22	4.82	4.53	4.30	4.11
38	0.100	2.84	2.45	2.23	2.10	2.01	1.94	1.88	1.84	1.80
	0.050	4.10	3.24	2.85	2.62	2.46	2.35	2.26	2.19	2.14
	0.010	7.35	5.21	4.34	3.86	3.54	3.32	3.15	3.02	2.92
	0.001	12.71	8.33	6.66	5.76	5.19	4.79	4.49	4.26	4.08
39	0.100	2.84	2.44	2.23	2.09	2.00	1.93	1.88	1.83	1.80
	0.050	4.09	3.24	2.85	2.61	2.46	2.34	2.26	2.19	2.13
	0.010	7.33	5.19	4.33	3.84	3.53	3.30	3.14	3.01	2.90
	0.001	12.66	8.29	6.63	5.73	5.16	4.76	4.46	4.23	4.05
40	0.100	2.84	2.44	2.23	2.09	2.00	1.93	1.87	1.83	1.79
	0.050	4.08	3.23	2.84	2.61	2.45	2.34	2.25	2.18	2.12
	0.010	7.31	5.18	4.31	3.83	3.51	3.29	3.12	2.99	2.89
	0.001	12.61	8.25	6.59	5.70	5.13	4.73	4.44	4.21	4.02
50	0.100	2.81	2.41	2.20	2.06	1.97	1.90	1.84	1.80	1.76
	0.050	4.03	3.18	2.79	2.56	2.40	2.29	2.20	2.13	2.07
	0.010	7.17	5.06	4.20	3.72	3.41	3.19	3.02	2.89	2.78
	0.001	12.22	7.96	6.34	5.46	4.90	4.51	4.22	4.00	3.82
60	0.100	2.79	2.39	2.18	2.04	1.95	1.87	1.82	1.77	1.74
	0.050	4.00	3.15	2.76	2.53	2.37	2.25	2.17	2.10	2.04
	0.010	7.08	4.98	4.13	3.65	3.34	3.12	2.95	2.82	2.72
	0.001	11.97	7.77	6.17	5.31	4.76	4.37	4.09	3.86	3.69
120	0.100	2.75	2.35	2.13	1.99	1.90	1.82	1.77	1.72	1.68
	0.050	3.92	3.07	2.68	2.45	2.29	2.18	2.09	2.02	1.96
	0.010	6.85	4.79	3.95	3.48	3.17	2.96	2.79	2.66	2.56
	0.001	11.38	7.32	5.78	4.95	4.42	4.04	3.77	3.55	3.38

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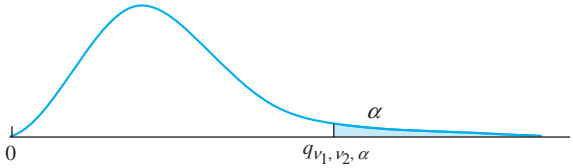
TABLE A.8 Upper percentage points for the F distribution (continued)

		ν_1								
ν_2	α	10	12	15	20	25	30	40	50	60
32	0.100	1.81	1.76	1.71	1.65	1.62	1.59	1.56	1.53	1.52
	0.050	2.14	2.07	1.99	1.91	1.85	1.82	1.77	1.74	1.71
	0.010	2.93	2.80	2.65	2.50	2.41	2.34	2.25	2.20	2.16
	0.001	4.14	3.91	3.66	3.40	3.24	3.13	2.98	2.89	2.83
33	0.100	1.80	1.75	1.70	1.64	1.61	1.58	1.55	1.53	1.51
	0.050	2.13	2.06	1.98	1.90	1.84	1.81	1.76	1.72	1.70
	0.010	2.91	2.78	2.63	2.48	2.39	2.32	2.23	2.18	2.14
	0.001	4.10	3.87	3.62	3.36	3.20	3.09	2.94	2.85	2.79
34	0.100	1.79	1.75	1.69	1.64	1.60	1.58	1.54	1.52	1.50
	0.050	2.12	2.05	1.97	1.89	1.83	1.80	1.75	1.71	1.69
	0.010	2.89	2.76	2.61	2.46	2.37	2.30	2.21	2.16	2.12
	0.001	4.06	3.83	3.58	3.33	3.16	3.05	2.91	2.82	2.75
35	0.100	1.79	1.74	1.69	1.63	1.60	1.57	1.53	1.51	1.50
	0.050	2.11	2.04	1.96	1.88	1.82	1.79	1.74	1.70	1.68
	0.010	2.88	2.74	2.60	2.44	2.35	2.28	2.19	2.14	2.10
	0.001	4.03	3.79	3.55	3.29	3.13	3.02	2.87	2.78	2.72
36	0.100	1.78	1.73	1.68	1.63	1.59	1.56	1.53	1.51	1.49
	0.050	2.11	2.03	1.95	1.87	1.81	1.78	1.73	1.69	1.67
	0.010	2.86	2.72	2.58	2.43	2.33	2.26	2.18	2.12	2.08
	0.001	3.99	3.76	3.51	3.26	3.10	2.98	2.84	2.75	2.69
37	0.100	1.78	1.73	1.68	1.62	1.58	1.56	1.52	1.50	1.48
	0.050	2.10	2.02	1.95	1.86	1.81	1.77	1.72	1.68	1.66
	0.010	2.84	2.71	2.56	2.41	2.31	2.25	2.16	2.10	2.06
	0.001	3.96	3.73	3.48	3.23	3.07	2.95	2.81	2.72	2.66
38	0.100	1.77	1.72	1.67	1.61	1.58	1.55	1.52	1.49	1.48
	0.050	2.09	2.02	1.94	1.85	1.80	1.76	1.71	1.68	1.65
	0.010	2.83	2.69	2.55	2.40	2.30	2.23	2.14	2.09	2.05
	0.001	3.93	3.70	3.45	3.20	3.04	2.92	2.78	2.69	2.63
39	0.100	1.77	1.72	1.67	1.61	1.57	1.55	1.51	1.49	1.47
	0.050	2.08	2.01	1.93	1.85	1.79	1.75	1.70	1.67	1.65
	0.010	2.81	2.68	2.54	2.38	2.29	2.22	2.13	2.07	2.03
	0.001	3.90	3.67	3.43	3.17	3.01	2.90	2.75	2.66	2.60
40	0.100	1.76	1.71	1.66	1.61	1.57	1.54	1.51	1.48	1.47
	0.050	2.08	2.00	1.92	1.84	1.78	1.74	1.69	1.66	1.64
	0.010	2.80	2.66	2.52	2.37	2.27	2.20	2.11	2.06	2.02
	0.001	3.87	3.64	3.40	3.14	2.98	2.87	2.73	2.64	2.57
50	0.100	1.73	1.68	1.63	1.57	1.53	1.50	1.46	1.44	1.42
	0.050	2.03	1.95	1.87	1.78	1.73	1.69	1.63	1.60	1.58
	0.010	2.70	2.56	2.42	2.27	2.17	2.10	2.01	1.95	1.91
	0.001	3.67	3.44	3.20	2.95	2.79	2.68	2.53	2.44	2.38
60	0.100	1.71	1.66	1.60	1.54	1.50	1.48	1.44	1.41	1.40
	0.050	1.99	1.92	1.84	1.75	1.69	1.65	1.59	1.56	1.53
	0.010	2.63	2.50	2.35	2.20	2.10	2.03	1.94	1.88	1.84
	0.001	3.54	3.32	3.08	2.83	2.67	2.55	2.41	2.32	2.25
120	0.100	1.65	1.60	1.55	1.48	1.44	1.41	1.37	1.34	1.32
	0.050	1.91	1.83	1.75	1.66	1.60	1.55	1.50	1.46	1.43
	0.010	2.47	2.34	2.19	2.03	1.93	1.86	1.76	1.70	1.66
	0.001	3.24	3.02	2.78	2.53	2.37	2.26	2.11	2.02	1.95

TABLE A.9 Upper percentage points for the Studentized range q_{ν_1,ν_2}



		ν_1													
ν_2	α	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	0.10	8.93	13.44	16.36	18.49	20.15	21.51	22.64	23.62	24.48	25.24	25.92	26.54	27.10	27.62
	0.05	17.97	26.98	32.82	37.08	40.41	43.12	45.40	47.36	49.07	50.59	51.96	53.20	54.33	55.36
	0.01	90.02	135.0	164.3	185.6	202.2	215.8	227.2	237.0	245.6	253.2	260.0	266.2	271.8	277.0
2	0.10	4.13	5.73	6.77	7.54	8.14	8.63	9.05	9.41	9.72	10.01	10.26	10.49	10.70	10.89
	0.05	6.08	8.33	9.80	10.88	11.74	12.44	13.03	13.54	13.99	14.39	14.75	15.08	15.38	15.65
	0.01	14.04	19.02	22.29	24.72	26.63	28.20	29.53	30.68	31.69	32.59	33.40	34.13	34.81	35.43
3	0.10	3.33	4.47	5.20	5.74	6.16	6.51	6.81	7.06	7.29	7.49	7.67	7.83	7.98	8.12
	0.05	4.50	5.91	6.82	7.50	8.04	8.48	8.85	9.18	9.46	9.72	9.95	10.15	10.35	10.52
	0.01	8.26	10.62	12.17	13.33	14.24	15.00	15.64	16.20	16.69	17.13	17.53	17.89	18.22	18.52
4	0.10	3.01	3.98	4.59	5.04	5.39	5.68	5.93	6.14	6.33	6.49	6.65	6.78	6.91	7.02
	0.05	3.93	5.04	5.76	6.29	6.71	7.05	7.35	7.60	7.83	8.03	8.21	8.37	8.52	8.66
	0.01	6.51	8.12	9.17	9.96	10.58	11.10	11.55	11.93	12.27	12.57	12.84	13.09	13.32	13.53
5	0.10	2.85	3.72	4.26	4.66	4.98	5.24	5.46	5.65	5.82	5.97	6.10	6.22	6.34	6.44
	0.05	3.64	4.60	5.22	5.67	6.03	6.33	6.58	6.80	6.99	7.17	7.32	7.47	7.60	7.72
	0.01	5.70	6.98	7.80	8.42	8.91	9.32	9.67	9.97	10.24	10.48	10.70	10.89	11.08	11.24
6	0.10	2.75	3.56	4.07	4.44	4.73	4.97	5.17	5.34	5.50	5.64	5.76	5.87	5.98	6.07
	0.05	3.46	4.34	4.90	5.31	5.63	5.90	6.12	6.32	6.49	6.65	6.79	6.92	7.03	7.14
	0.01	5.24	6.33	7.03	7.56	7.97	8.32	8.61	8.87	9.10	9.30	9.49	9.65	9.81	9.95
7	0.10	2.68	3.45	3.93	4.28	4.55	4.78	4.97	5.14	5.28	5.41	5.53	5.64	5.74	5.83
	0.05	3.34	4.16	4.68	5.06	5.36	5.61	5.82	6.00	6.16	6.30	6.43	6.55	6.66	6.76
	0.01	4.95	5.92	6.54	7.01	7.37	7.68	7.94	8.17	8.37	8.55	8.71	8.86	9.00	9.12
8	0.10	2.63	3.37	3.83	4.17	4.43	4.65	4.83	4.99	5.13	5.25	5.36	5.46	5.56	5.64
	0.05	3.26	4.04	4.53	4.89	5.17	5.40	5.60	5.77	5.92	6.05	6.18	6.29	6.39	6.48
	0.01	4.75	5.64	6.20	6.63	6.96	7.24	7.47	7.68	7.86	8.03	8.18	8.31	8.44	8.55
9	0.10	2.59	3.32	3.76	4.08	4.34	4.54	4.72	4.87	5.01	5.13	5.23	5.33	5.42	5.51
	0.05	3.20	3.95	4.42	4.76	5.02	5.24	5.43	5.59	5.74	5.87	5.98	6.09	6.19	6.28
	0.01	4.60	5.43	5.96	6.35	6.66	6.91	7.13	7.33	7.49	7.65	7.78	7.91	8.03	8.13
10	0.10	2.56	3.27	3.70	4.02	4.26	4.47	4.64	4.78	4.91	5.03	5.13	5.23	5.32	5.40
	0.05	3.15	3.88	4.33	4.65	4.91	5.12	5.31	5.46	5.60	5.72	5.83	5.93	6.03	6.11
	0.01	4.48	5.27	5.77	6.14	6.43	6.67	6.88	7.05	7.21	7.36	7.49	7.60	7.71	7.81
11	0.10	2.54	3.23	3.66	3.96	4.20	4.40	4.57	4.71	4.84	4.95	5.05	5.15	5.23	5.31
	0.05	3.11	3.82	4.26	4.57	4.82	5.03	5.20	5.35	5.49	5.61	5.71	5.81	5.90	5.99
	0.01	4.39	5.15	5.62	5.97	6.25	6.48	6.67	6.84	6.99	7.13	7.25	7.36	7.46	7.56
12	0.10	2.52	3.20	3.62	3.92	4.16	4.35	4.51	4.65	4.78	4.89	4.99	5.08	5.16	5.24
	0.05	3.08	3.77	4.20	4.51	4.75	4.95	5.12	5.27	5.40	5.51	5.62	5.71	5.80	5.88
	0.01	4.32	5.05	5.50	5.84	6.10	6.32	6.51	6.67	6.81	6.94	7.06	7.17	7.26	7.36

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TABLE A.9 Upper percentage points for the Studentized range q_{ν_1,ν_2} (continued)

		ν_1													
ν_2	α	2	3	4	5	6	7	8	9	10	11	12	13	14	15
13	0.10	2.50	3.18	3.59	3.88	4.12	4.30	4.46	4.60	4.72	4.83	4.93	5.02	5.10	5.18
	0.05	3.06	3.73	4.15	4.45	4.69	4.88	5.05	5.19	5.32	5.43	5.53	5.63	5.71	5.79
	0.01	4.26	4.96	5.40	5.73	5.98	6.19	6.37	6.53	6.67	6.79	6.90	7.01	7.10	7.19
14	0.10	2.49	3.16	3.56	3.85	4.08	4.27	4.42	4.56	4.68	4.79	4.88	4.97	5.05	5.12
	0.05	3.03	3.70	4.11	4.41	4.64	4.83	4.99	5.13	5.25	5.36	5.46	5.55	5.64	5.72
	0.01	4.21	4.89	5.32	5.63	5.88	6.08	6.26	6.41	6.54	6.66	6.77	6.87	6.96	7.05
15	0.10	2.48	3.14	3.54	3.83	4.05	4.23	4.39	4.52	4.64	4.75	4.84	4.93	5.01	5.08
	0.05	3.01	3.67	4.08	4.37	4.60	4.78	4.94	5.08	5.20	5.31	5.40	5.49	5.58	5.65
	0.01	4.17	4.84	5.25	5.56	5.80	5.99	6.16	6.31	6.44	6.55	6.66	6.76	6.84	6.93
16	0.10	2.47	3.12	3.52	3.80	4.03	4.21	4.36	4.49	4.61	4.71	4.81	4.89	4.97	5.04
	0.05	3.00	3.65	4.05	4.33	4.56	4.74	4.90	5.03	5.15	5.26	5.35	5.44	5.52	5.59
	0.01	4.13	4.79	5.19	5.49	5.72	5.92	6.08	6.22	6.35	6.46	6.56	6.66	6.74	6.82
17	0.10	2.46	3.11	3.50	3.78	4.00	4.18	4.33	4.46	4.58	4.68	4.77	4.86	4.93	5.01
	0.05	2.98	3.63	4.02	4.30	4.52	4.71	4.86	4.99	5.11	5.21	5.31	5.39	5.47	5.55
	0.01	4.10	4.74	5.14	5.43	5.66	5.85	6.01	6.15	6.27	6.38	6.48	6.57	6.66	6.73
18	0.10	2.45	3.10	3.49	3.77	3.98	4.16	4.31	4.44	4.55	4.65	4.75	4.83	4.90	4.98
	0.05	2.97	3.61	4.00	4.28	4.49	4.67	4.82	4.96	5.07	5.17	5.27	5.35	5.43	5.50
	0.01	4.07	4.70	5.09	5.38	5.60	5.79	5.94	6.08	6.20	6.31	6.41	6.50	6.58	6.65
19	0.10	2.44	3.09	3.47	3.75	3.97	4.14	4.29	4.42	4.53	4.63	4.72	4.80	4.88	4.95
	0.05	2.96	3.59	3.98	4.25	4.47	4.65	4.79	4.92	5.04	5.14	5.23	5.32	5.39	5.46
	0.01	4.05	4.67	5.05	5.33	5.55	5.73	5.89	6.02	6.14	6.25	6.34	6.43	6.51	6.58
20	0.10	2.44	3.08	3.46	3.74	3.95	4.12	4.27	4.40	4.51	4.61	4.70	4.78	4.85	4.92
	0.05	2.95	3.58	3.96	4.23	4.45	4.62	4.77	4.90	5.01	5.11	5.20	5.28	5.36	5.43
	0.01	4.02	4.64	5.02	5.29	5.51	5.69	5.84	5.97	6.09	6.19	6.29	6.37	6.45	6.52
24	0.10	2.42	3.05	3.42	3.69	3.90	4.07	4.21	4.34	4.45	4.54	4.63	4.71	4.78	4.85
	0.05	2.92	3.53	3.90	4.17	4.37	4.54	4.68	4.81	4.92	5.01	5.10	5.18	5.25	5.32
	0.01	3.96	4.55	4.91	5.17	5.37	5.54	5.69	5.81	5.92	6.02	6.11	6.19	6.26	6.33
30	0.10	2.40	3.02	3.39	3.65	3.85	4.02	4.16	4.28	4.38	4.47	4.56	4.64	4.71	4.77
	0.05	2.89	3.49	3.85	4.10	4.30	4.46	4.60	4.72	4.82	4.92	5.00	5.08	5.15	5.21
	0.01	3.89	4.45	4.80	5.05	5.24	5.40	5.54	5.65	5.76	5.85	5.93	6.01	6.08	6.14
40	0.10	2.38	2.99	3.35	3.60	3.80	3.96	4.10	4.21	4.32	4.41	4.49	4.56	4.63	4.69
	0.05	2.86	3.44	3.79	4.04	4.23	4.39	4.52	4.63	4.74	4.82	4.90	4.98	5.05	5.11
	0.01	3.82	4.37	4.70	4.93	5.11	5.27	5.39	5.50	5.60	5.69	5.76	5.83	5.90	5.96
60	0.10	2.36	2.96	3.31	3.56	3.75	3.91	4.04	4.16	4.25	4.34	4.42	4.49	4.56	4.62
	0.05	2.83	3.40	3.74	3.98	4.16	4.31	4.44	4.55	4.65	4.73	4.81	4.88	4.94	5.00
	0.01	3.76	4.28	4.59	4.82	4.99	5.13	5.25	5.36	5.45	5.53	5.60	5.67	5.73	5.79
120	0.10	2.34	2.93	3.28	3.52	3.71	3.86	3.99	4.10	4.19	4.28	4.35	4.42	4.48	4.54
	0.05	2.80	3.36	3.68	3.92	4.10	4.24	4.36	4.47	4.56	4.64	4.71	4.78	4.84	4.90
	0.01	3.70	4.20	4.50	4.71	4.87	5.01	5.12	5.21	5.30	5.38	5.44	5.50	5.56	5.61
∞	0.10	2.33	2.90	3.24	3.48	3.66	3.81	3.93	4.04	4.13	4.21	4.28	4.35	4.41	4.47
	0.05	2.77	3.31	3.63	3.86	4.03	4.17	4.29	4.39	4.47	4.55	4.62	4.68	4.74	4.80
	0.01	3.64	4.12	4.40	4.60	4.76	4.88	4.99	5.08	5.16	5.23	5.29	5.35	5.40	5.45

TABLE A.10 Control chart constants

n	A_2	A_3	B_3	B_4	D_3	D_4	c_4	d_2
2	1.880	2.659	0.000	3.267	0.000	3.267	0.7979	1.128
3	1.023	1.954	0.000	2.568	0.000	2.575	0.8862	1.693
4	0.729	1.628	0.000	2.266	0.000	2.282	0.9213	2.059
5	0.577	1.427	0.000	2.089	0.000	2.114	0.9400	2.326
6	0.483	1.287	0.030	1.970	0.000	2.004	0.9515	2.534
7	0.419	1.182	0.118	1.882	0.076	1.924	0.9594	2.704
8	0.373	1.099	0.185	1.815	0.136	1.864	0.9650	2.847
9	0.337	1.032	0.239	1.761	0.184	1.816	0.9693	2.970
10	0.308	0.975	0.284	1.716	0.223	1.777	0.9727	3.078
11	0.285	0.927	0.321	1.679	0.256	1.744	0.9754	3.173
12	0.266	0.866	0.354	1.646	0.283	1.717	0.9776	3.258
13	0.249	0.850	0.382	1.618	0.307	1.693	0.9794	3.336
14	0.235	0.817	0.406	1.594	0.328	1.672	0.9810	3.407
15	0.223	0.789	0.428	1.572	0.347	1.653	0.9823	3.472
16	0.212	0.763	0.448	1.552	0.363	1.637	0.9835	3.532
17	0.203	0.739	0.466	1.534	0.378	1.622	0.9845	3.588
18	0.194	0.718	0.482	1.518	0.391	1.609	0.9854	3.640
19	0.187	0.698	0.497	1.503	0.403	1.597	0.9862	3.689
20	0.180	0.680	0.510	1.490	0.415	1.585	0.9869	3.735
21	0.173	0.663	0.523	1.477	0.425	1.575	0.9876	3.778
22	0.167	0.647	0.534	1.466	0.434	1.566	0.9882	3.819
23	0.162	0.633	0.545	1.455	0.443	1.557	0.9887	3.858
24	0.157	0.619	0.555	1.445	0.452	1.548	0.9892	3.895
25	0.153	0.606	0.565	1.435	0.459	1.541	0.9896	3.931

For $n > 25$: $A_3 \approx 3/\sqrt{n}$, $B_3 \approx 1 - 3/\sqrt{2n}$, and $B_4 \approx 1 + 3/\sqrt{2n}$.