MACHINE INTELLIGENCE UNIT-5

Regularization

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VIBHA MASTI

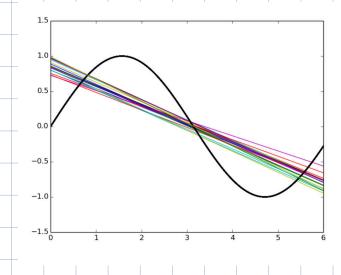
1. Bias-Variance Trade-off

- Sample: 25 points out of 100 for the function $f(x) = \sin x$
- · Train simple model

· Train complex model

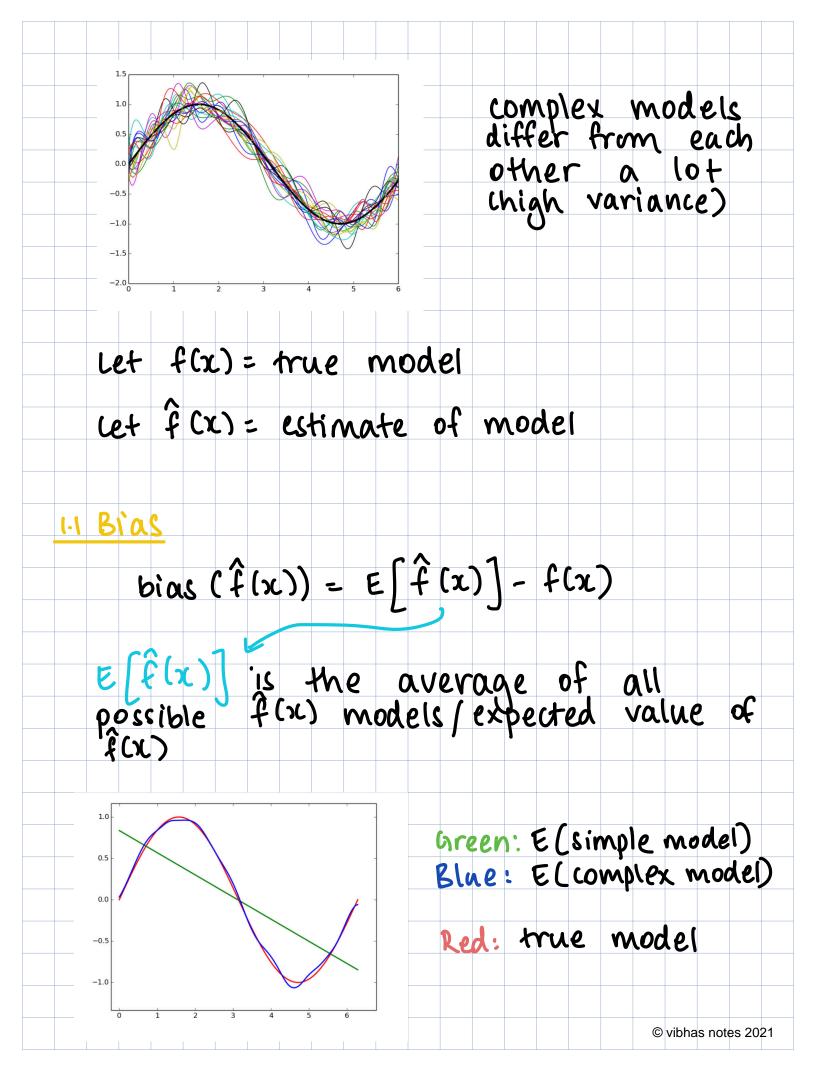
$$y = f(x) = \sum_{i=1}^{25} w_i x^i + w_0$$

- Train k different simple & complex models on different samples of training data
- Each model gets its own sample



simple models do not differ from each other much

however, they are underfitting Chigh bias) - very far

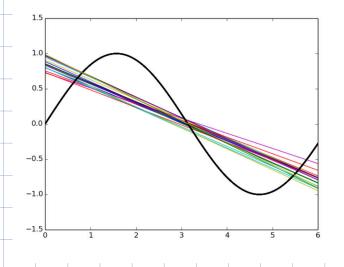


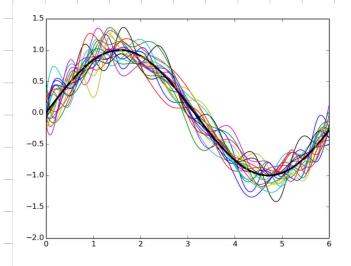
- · Simple model has high bias
- · Complex model has low bias

1.2 Variance

variance
$$(\hat{f}(x)) = E[(\hat{f}(x) - E[\hat{f}(x)])^2]$$

E[(f(x)-E[f(x)])] is the variance of every possible model wrt the average model

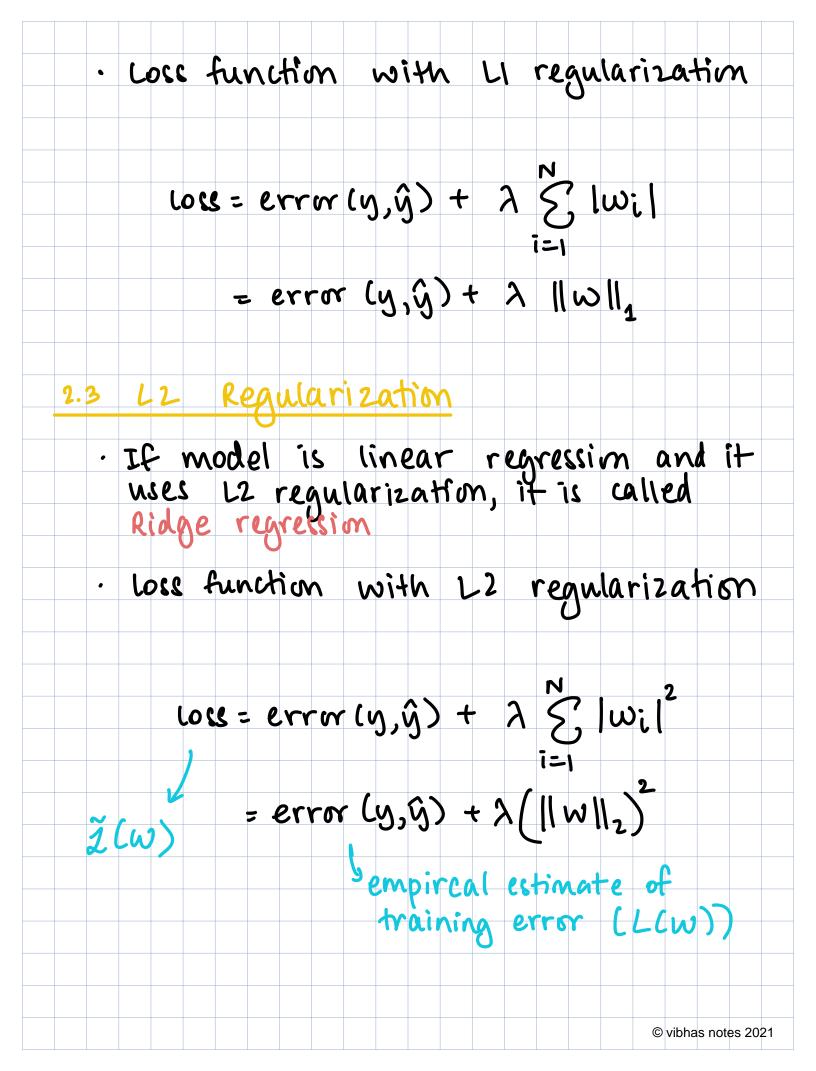


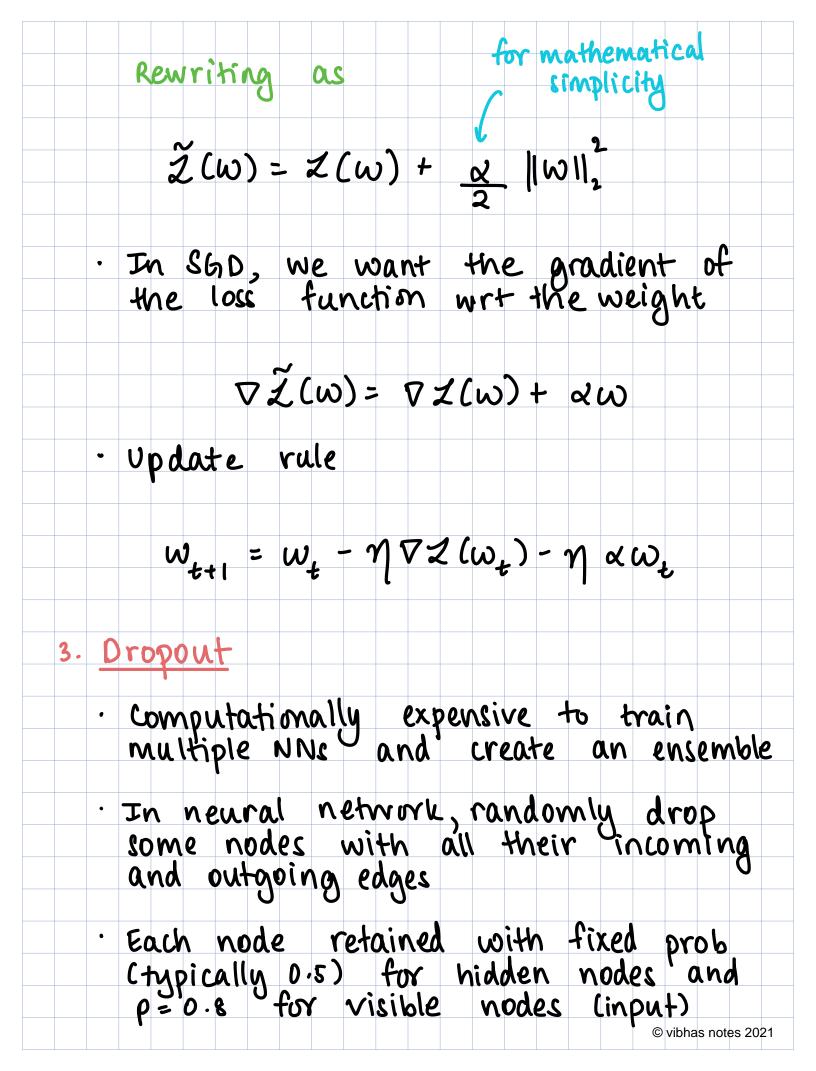


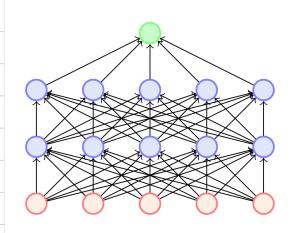
- · simple model has low variance
- complex model has high variance

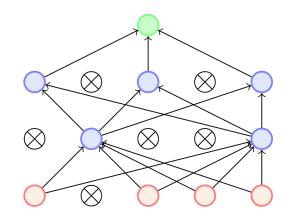
1.3 Train-Test Error Coverfitting · As model complexity increases, train error decreases but test error increases High bias error High variance Blue: train err Sweet spot--perfect tradeoff Red: test err -ideal model complexity/ model complexity Data D= {x;,y;} split into train(n) and test(m) For any point (xi, yi), yi = f(xi) + Ei enoise Cacsume white) $\varepsilon \sim N(0, \sigma^2)$ · f is unknown, only f known after training such that $yi = \hat{f}(xi) \forall (x_i, y_i) \in D_{train}$

2.	Regul	lari	<u> 201</u>	im														
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- · If n nodes present, total possible no of thinned networks = an
- · Probability p is a hyperparameter
- · Combining all models: use full NN and scale output of each node by the fraction of times it was on during training

4. Dataset Augmentation

- · Another technique to reduce overfitting without having to fetch more training data
- · Transform training data so that the labels do not change (eg: shifting, scaling, rotating an image)

