

20/08/2021

CS 6160 Cryptology Lecture 1: Overview of the Field of Cryptography

Maria Francis

August 20, 2021

20/08/2021

The need for cryptography



Alice

Insecure Channel



Bob

The need for cryptography



Alice

Insecure Channel



Bob



Passive Adversary (Eve)

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The need for cryptography



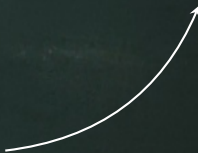
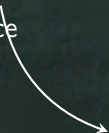
Alice



Bob



Active Adversary (Mallory)



The need for cryptography

- Communicating or computing over a channel where there are adversaries.
- There are **information systems**(PCs, cellphones, network of computers, ATMs, cars, smart grids, etc.)
- Our aim is to **control access** to the information – we are looking to see if we can control who **sees** and **modifies** the information.
- Some examples of such rules :
 - ▶ Only XX can read the contents of the file
 - ▶ The contents of this file has not been changed after XX send it.
 - ▶ The recipient of this email can authenticate the sender.

Our Aims and the Tools at Hand

What we aim to achieve:

- Data Confidentiality
- Data Integrity
- Authentication –
- Non-repudiation – the sender cannot claim that she/he did not send it

How do we achieve them? Tools such as:

- Encryption
- Hash Functions
- Digital Signatures
- Zero knowledge Proofs

What about the Adversary?

- Could be anybody – insider/outsider
- Assume he knows system design including implementation details
- Resources – powerful computers, ability to intercept messages, ability to collude with some participants
- Generally **generous** assumptions about adversary's abilities but we assume a **computationally bounded** adversary.

A Simple Solution



Alice

Key k
Encryption Algorithm Enc
Decryption Algorithm Dec



Bob

All previously agreed upon

A Simple Solution



Alice

$$c = \text{Enc}_k(m)$$



Bob

Retrieving the message:
 $m = \text{Dec}_k(c)$

A Simple Solution



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Retrieving the message:

$$m = Dec_k(c)$$

Questions: Which of these are secret here?

How are the secrets agreed upon? Parties may not even have met before?

Formalizing the Solution

Symmetric key encryption (SKE) scheme consists of:

- \mathcal{M} : a set of possible **plaintexts**
- \mathcal{C} : a set of possible **ciphertexts**
- \mathcal{K} : a set of possible **keys**.
- **Gen** (called the **key generation algorithm**) is a **randomized algorithm** that returns a key k such that $k \in \mathcal{K}$.
- A family of encryption functions, $Enc_k : \mathcal{M} \rightarrow \mathcal{C}, \forall k \in \mathcal{K}$
- A family of decryption functions, $Dec_k : \mathcal{C} \rightarrow \mathcal{M}, \forall k \in \mathcal{K}$, such that **$Dec_k(Enc_k(m)) = m$** for all $m \in \mathcal{M}$ and $k \in \mathcal{K}$

Timeline of Cryptography as a field

0 2021



Ancient times to 1900s:
Classical
Ciphers

1900s :
Mechanical
Ciphers

1970s:
Modern Ciphers
- Symmetric keys
/Public Key Crypto

Classical Ciphers

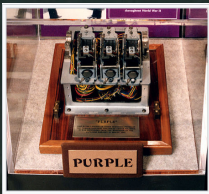
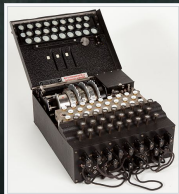
The first idea that comes up when you need secret communication.
Popular upto 1900s :

- Shift/Ceaser cipher
- Substitution cipher
- Vigenère cipher, etc

S	E	N	D	R	E	I	N	F	O	R	C	E	M	E	N	T	S
V	I	G	E	N	E	R	E	V	I	G	E	N	E	R	E	V	I
N	M	T	H	E	I	Z	R	A	W	X	G	R	Q	V	R	O	A

Mechanical Ciphers - Enigma, Purple, etc

- Motor devices
- Electromechanical devices
- Cryptography performed by (typically, rotor) machines.
- Alan Turing and others at Bletchley Park, William Friedman and others in the USA – all helped break these ciphers



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- Less information we give to the adversary, the harder it is to break the scheme, right??
- Not really! – Kerchoff's principle (1884)



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- Conservative approach – guarantees that security is preserved even if everything but the key is known to the adversary.
- First step to formally defining the security of encryption schemes.

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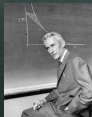
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- If so, then Eve would be able to compute everything that Alice and Bob could compute and would thus be able to decrypt anything that Bob can decrypt.

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- If so, then Eve would be able to compute everything that Alice and Bob could compute and would thus be able to decrypt anything that Bob can decrypt.
- *To prevent this we require Gen to be randomized.*

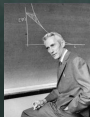
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Perfect Secrecy (C. Shannon (1916 - 2001))



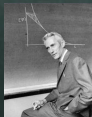
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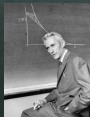
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- **One Time Pad**/ Vernam Cipher - unbreakable!

Computational Complexity Theory

- A systematic study of what computationally bounded parties can and cannot do
- Started with Alan Turing but formal study with Cook (Turing Award '82), Karp (Turing Award '85) and Blum (Turing Award '95)
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- Many ideas are still “conjectured” or believed
- The foundation of modern cryptography



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Definition (**Polynomial Time Algorithm**)

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Definition (Probabilistic Polynomial Time Algorithm (PPT))

It is a polynomial time algorithm A that is randomized.

- What does that mean? We flip coins during the computation of the algorithm and the output depends on the coin toss outcome.
- $y \leftarrow A(x)$ is the random variable y , the randomized output of A on input x , i.e. r was chosen at random and $y = A(x; r)$ was computed.

Probabilistic Polynomial Time

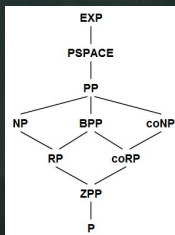
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A negl function is one that is **asymptotically smaller** than **any inverse poly. function**.

2^{-k} , $k^{-\log k}$ are negl but $1/k^{1000}$ is not.

Negligible function stays negligible even after poly. attempts :
 $\text{poly}(k) \cdot \text{negl}(k) = \text{negl}(k)$.

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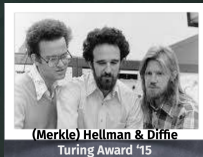
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- Alice and Bob and the adversary are assumed to run in time polynomial in k and the adversary can break the system with probability negligible in k .
- Increasing k we get higher security but a degraded efficiency. What is the correct value of k ?

1970s - Public Key Revolution

- Merkle, and independently Hellman and Diffie, invented the notion of public-key cryptography.
- In November 1976, Diffie and Hellman published *New Directions in Cryptography*, proclaiming *We are at the brink of a revolution in cryptography.*



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- **Digital Signatures** – sign with SK_A and verify with PK_A .

Public Key Encryption



Alice



Bob

Encrypting
using Bob's public key:
$$c = \text{Enc}_{PK_B}(m)$$

Decrypting
using Bob's private key:
$$m = \text{Dec}_{SK_B}(c)$$

Digital Signatures using Public Keys



Bob

(m, s)



Alice

Signing
using Bob's private key:
 $s = \text{Sign}_{SK_B}(m)$

Verifying
using Bob's public key:
 $\text{Verify}_{PK_B}(s, m)$

Public Key Encryption – RSA

How to implement Diffie/Hellman ideas? – Rivest, Shamir, Adleman in 1977 came with the RSA algorithm.



Shamir, Rivest & Adleman
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Note: In 1999, it was revealed that Ellis, Cocks and Williamson had invented PKC in the British secret service, before their invention outside.

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- Idea : **reduce** the problem of finding the secret key to some known **hard** mathematical problem.
- RSA security relies (in part) on the **conjectured hardness of factoring** n , a product of two very large primes p, q .
- What we look for in any PKC are **one-way functions with a trapdoor**:
 - ▶ Function f must be **invertible** so as to decrypt encrypted messages.
 - ▶ **Efficient** to encrypt
 - ▶ **Difficult to invert** so that Eve cannot compute m knowing $f(m)$
 - ▶ Has a **trapdoor**: given some information (SK_A) finding m is easy given $f(m)$.

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- More Turing award winners in theoretical crypto - Goldwasser & Micali (2012)
- More interesting ideas like for e.g:
 - ▶ **secret sharing** : collaboration between distrusting parties
 - ▶ **zero knowledge proofs (ZKPs)** : revealing nothing but the validity of the statement
 - ▶ **fully homomorphic encryption** : computation on encrypted data
- IACR - Intl. Assn. for Crypto Research. Sponsors the big crypto conferences – Crypto, Eurocrypt and Asiacrypt

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You do not want to work with intuitive ideas.
- It helps analyze and evaluate the scheme and some cases prove security too!

Formal Definitions - An example

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- **What is prior knowledge? What is leak?**

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- They are not proven but conjectured to be true.
- This means the assumptions should be examined and tested to be true.
- If it is not refuted for many years our confidence in it is increased. **This means precisely and simply stating it or else no one will study it!**

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- If an assumption is broken (like factoring on a quantum computer) the schemes built on the assumption (such as RSA, ECDSA) will break!

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- Pegasus shows us that well-resourced targeted attack is still impossible to prevent! Read :
<https://blog.cryptographyengineering.com/2021/07/20/a-case-against-security-nihilism/>.

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- Attacks on different cryptographic primitives like hash functions.

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- And of course, there is **cryptanalysis!**