

Theory of Automata & Formal Languages ①

Section-A (Short answers question)

- 1) Write a regular expression to denote a language L , which accepts all the strings that begin or end with either 00 or 11. (2018-19)
- 2) For the given language $L_1 = \epsilon$, $L_2 = \{a\}$, $L_3 = \phi$, Compute $L_1 L_2^* \cup L_3^*$ (2018-19)
- 3) Write regular expression for set of all strings such that the number of a 's divisible by 3 over $\Sigma = \{a, b\}$ (2018-19)
- 4) Design a regular expression that accepts all the strings for input alphabet $\{a, b\}$ containing exactly 2 a 's. (2017-18)
- 5) Define and give the difference between positive closure and Kleene closure. (2017-18)
- 6) Give the regular expression for set of all strings $\{0, 1\}$ containing exactly three 0's. (2017-18)
- 7) State the pumping lemma theorem for regular languages. (2016-17)
- 8) Differentiate between L^* and L^+ . (2015-16)
- 9) Write regular expression for set of all strings such that number of 0's is odd. (2015-16)

(2)

10) Write the regular expression for the language containing the strings over $\{0,1\}$ in which there are at least two occurrences of 1's between any two occurrences of 0's. (2014-15)

11) Describe the language of the given regular expression $(1+01)^*(0+01)^*$ (2014-15)

Section - B (Long answer questions)

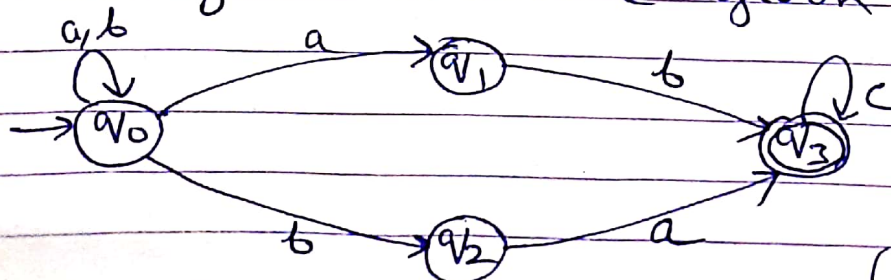
1) State Arden's theorem and construct regular expression for the following FA using Arden's theorem. (2018-19)

State	Input	
	0	1
A	$\{A, B\}$	\emptyset
B	C	$\{A, B\}$
C	B	\emptyset

A is the initial state and C is final state

2) Using pumping lemma, prove that the language $L = \{a^{i^2} \mid i \geq 1\}$ is not regular. (2018-19)

3) Find the regular expression corresponding to the finite automata given below.



(2018-19)

4) Prove that the language $L = \{a^n b^n\}$ is not regular.

(2018-19)

5) Explain the closure properties of regular expression

(2018-19)

6) State recursive definition of regular expression and construct a regular expression corresponding to the state transition diagram as shown in Fig 1.

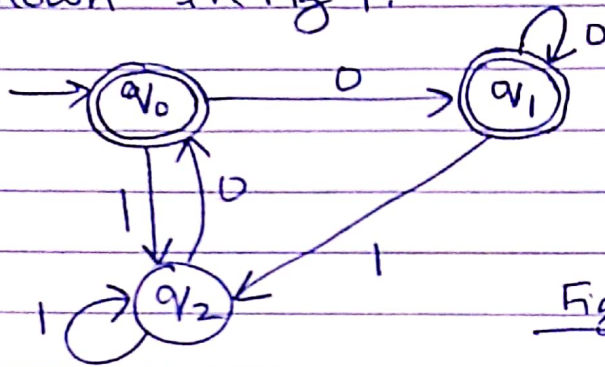


Fig-1

(2017-18)

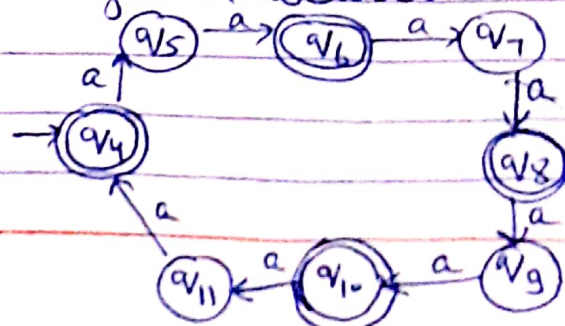
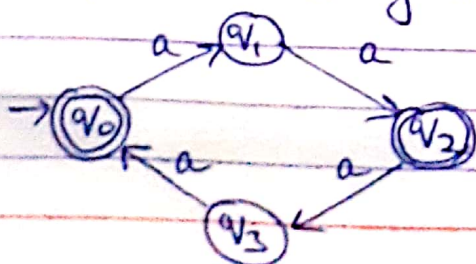
7) State pumping lemma for regular sets. Show that the set $L = \{a^p \mid p \text{ is a prime}\}$ is not regular.

(2017-18)

8) Discuss closure properties i.e. concatenation, union, intersection, complement of regular languages.

(2017-18)

9) Check with the comparison method for testing equivalence of two FA given below.



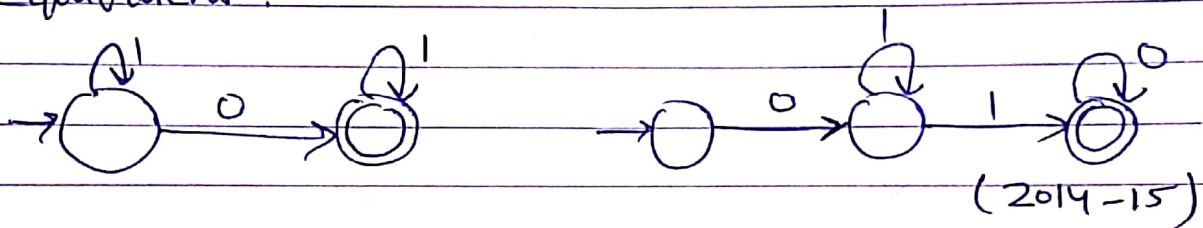
(2016-17)

(4)

10) Prove that the complement, homomorphism and inverse homomorphism closure of a regular language is regular. (2016-17)

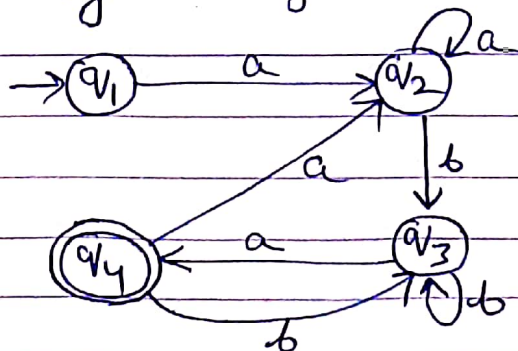
11) State and prove Kleen's theorem with an example. (2016-17)

12) Explain the condition in which two machines M_1 and M_2 are said to be equivalent. Show that the following automata's are not equivalent.



13) State and prove Pumping lemma of RE. Show that $L = \{a^p : p \text{ is prime}\}$ is not regular. (2015-16)

14) Find the regular expression using Arden's theorem of F.A given below.



(2015-15)

- 15) Prove that the language $L = \{0^n \mid n \text{ is perfect cube}\}$ is not regular. (2014-15)
- 16) Let L_1 be some language over Σ and $L_2 = \phi$.
Then prove that
(i) $L_1 L_2 \neq L_1$ (ii) $L_1 + L_2 \neq \phi$ (2014-15)
- 17) For regular expression prove that:
 $(a+b)^* \neq a^* + b^*$ (2014-15)
- 18) What is regular expression? Construct a DFA for the regular expression
 $(00+001)^*1$ (2014-15)
- 19) Prove that the given set of languages is not regular
 $L = \{0^n \mid 0^n \mid n \geq 1\}$ (2014-15)
- 20) Describe the closure properties of regular languages. Prove that regular languages are closed under complementation. (2014-15)