

Drawback of DDA :-

for every eq<sup>n</sup> we have to use Round fu<sup>n</sup>  
avoid

Bresenham's Algo :-

I : When  $m < 1$

$x$  - unit interval

$y_{k+1} \rightarrow ?$

II :  $m > 1$

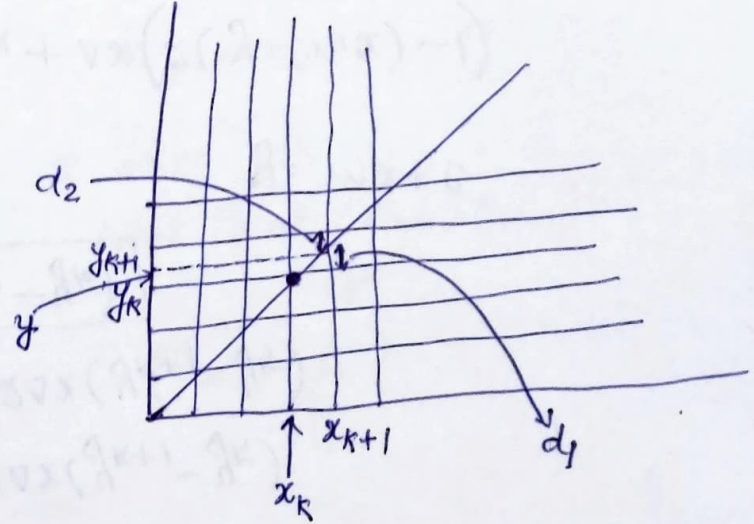
$y$  - unit interval

$x_{k+1} \rightarrow ?$

III :  $m = 1$

$x_{k+1} \rightarrow$  unit interval, and

$y_{k+1} \rightarrow$  unit interval



Let  $m < 1$  (case I)

$$y = mx + c$$

$$y_{k+1} = m(x_{k+1}) + c$$

$$\boxed{y = m(x_k + 1) + c} \quad \text{--- (1)}$$

Decision Parameter ( $P_k$ ) =  $\Delta x(d_1 - d_2)$  to select  $y_k$   
OR  
 $y_{k+1}$

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$$d_1 = y - y_k$$

$$d_1 = m(x_k + 1) + c - y_k$$

$$d_2 = y_{k+1} - y$$

$$d_2 = y_{k+1} - [m(x_k + 1) + c]$$

$$d_1 - d_2 = m(x_k + 1) + c - y_k - [y_{k+1} - m(x_k + 1) - c]$$

$$d_1 - d_2 = 2m(x_k + 1) - 2y_k + 2c - 1$$

$$\Delta x(d_1 - d_2) = \Delta x \left[ 2 \frac{\Delta y}{\Delta x} (x_k + 1) - 2y_k + 2c - 1 \right]$$

$$\text{Initial decision} = 2\Delta y(x_k + 1) - 2\Delta x y_k + 2\Delta x c - \Delta x$$

$$\text{Parameter } P_k = 2\Delta y x_k + 2\Delta y - 2\Delta x y_k + \Delta x(2c - 1)$$

$$P_{k+1} = 2\Delta y x_{k+1} + 2\Delta y - 2\Delta x y_{k+1} + \Delta x(2c - 1)$$

$$P_{k+1} - P_k = 2\Delta y x_{k+1} + 2\Delta y - 2\Delta x y_{k+1} + \Delta x(2c - 1) - 2\Delta y x_k - 2\Delta y + 2\Delta x y_k - \Delta x(2c - 1)$$

$$= 2\Delta y(x_{k+1} - x_k) - 2\Delta x(y_{k+1} - y_k)$$

$$= 2\Delta y(x_{k+1} - x_k) - 2\Delta x(y_{k+1} - y_k)$$

$$P_{k+1} = P_k + 2\Delta y - 2\Delta x(y_{k+1} - y_k)$$

put value of  $c$  in  $P_k$

$$y = mx + c$$

$$P_k = 2\Delta y x_k + 2\Delta y - 2\Delta x y_k + \Delta x(2(y - mx) - 1)$$

$$= 2\Delta y x_k + 2\Delta y - 2\Delta x y_k + 2\Delta x y - 2\Delta x m(x) - \Delta x$$

$$= 2\Delta y x_k + 2\Delta y - 2\Delta x y_k + 2\Delta x y - 2\Delta x \frac{\Delta y}{\Delta x} x - \Delta x$$

$$= 2\Delta y x_k + 2\Delta y - 2\Delta x y_k + 2\Delta x y - 2\Delta y x - \Delta x$$

$$= 2\Delta y x_k + 2\Delta y - 2\Delta x y_k + 2\Delta x y_k - 2\Delta y x_k - \Delta x$$



$$P_k = 2\Delta y - \Delta x \quad \text{Initially}$$

and

$$P_{k+1} = P_k + 2\Delta y - 2\Delta x(y_{k+1} - y_k)$$

Decision:

$$\text{If } P_k \geq 0$$

$$x_{k+1} = x_k + 1$$

$$\Rightarrow y_{k+1} = y_k + 1$$

Next point  $(x_{k+1}, y_{k+1})$  $\Downarrow$ 

$$(x_{k+1}, y_{k+1})$$

$$\text{If } P_k < 0$$

$$x_{k+1} = x_k + 1$$

$$\Rightarrow y_{k+1} = y_k$$

Next Point  $(x_{k+1}, y_{k+1})$  $\Downarrow$ 

$$(x_{k+1}, y_k)$$

Similarly if  $m$  is greater than 1 ( $m > 1$ )  
replace  $x \leftrightarrow y$

$$P_k = 2\Delta x - \Delta y$$

$$P_{k+1} = P_k + 2\Delta x - 2\Delta y(x_{k+1} - x_k)$$

Decision:

$$\text{If } P_k \geq 0$$

$$y_{k+1} = y_k + 1$$

$$\Rightarrow x_{k+1} = x_k + 1$$

Next point

$$(x_{k+1}, y_{k+1})$$

 $\Downarrow$ 

$$(x_{k+1}, y_{k+1})$$

$$\text{If } P_k < 0$$

$$y_{k+1} = y_k + 1$$

$$x_{k+1} = x_k$$

Next Point

$$(x_{k+1}, y_{k+1})$$

 $\Downarrow$ 

$$(x_k, y_{k+1})$$

ex-  $m > 1$

(1,1) ————— (6,7)

$$m = \frac{7-1}{6-1} = \frac{6}{5} = 1.2 > 1$$

$$\Delta x = 6-1 = 5 \quad 2\Delta x = 10$$

$$\Delta y = 7-1 = 6 \quad 2\Delta y = 12$$

When  $m > 1$

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$$P_k = 2\Delta x - \Delta y$$

$$P_{k+1} = P_k + 2\Delta x - 2\Delta y(x_{k+1} - x_k)$$

$$\text{If } P_k > 0 \Rightarrow x_{k+1} = x_k + 1$$

$$\text{If } P_k < 0 \Rightarrow x_{k+1} = x_k$$

$$P_k = 2\Delta x - \Delta y$$

$$= 10 - 6 = 4 > 0$$

k(iteration)	$(x_k, y_k)$	$P_k$	$(x_{k+1}, y_{k+1})$
1:	(1,1)	4	(2,2)

$$\begin{aligned} P_{k+1} &= P_k + 2\Delta x - 2\Delta y(x_{k+1} - x_k) \\ &= 4 + 10 - 12(2-1) \\ &= 14 - 12 \\ &= 2 > 0 \end{aligned}$$

2:	(2,2)	2	(3,3)
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$$\begin{aligned} P_{k+1} &= 2 + 10 - 12(3-2) \\ &= 12 - 12 = 0 \end{aligned}$$

3:	(3,3)	0	(4,4)
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$$\begin{aligned} P_{k+1} &= 0 + 10 - 12(4-3) \\ &= -2 < 0 \end{aligned}$$

4:	(4,4)	-2	(4,5)
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$$\begin{aligned} P_{k+1} &= -2 + 10 - 12(4-4) \\ &= 8 > 0 \end{aligned}$$

5:	(4,5)	8	(5,6)
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$$P_{k+1} = 8 + 10 - 12(5-4)$$

$$= 18 - 12$$

$$= 6 > 0$$

6: (5,6)                      6      (6,7)

(1,1)(2,2)(3,3)(4,4)(4,5)(5,6)(6,7)

Que: (1,1) — (8,6)

ex- (35,40) — (43,45)

$$m = \frac{45-40}{43-35} = \frac{5}{8} = 0.6 < 1$$

$$\text{So } P_k = 2\Delta y - \Delta x$$

$$P_{k+1} = P_k + 2\Delta y - 2\Delta x(y_{k+1} - y_k)$$

$$\text{If } P_k \geq 0 \Rightarrow y_{k+1} = y_k + 1$$

$$\text{N.C.} = (x_{k+1}, y_{k+1})$$

$$P_k < 0 \Rightarrow y_{k+1} = y_k$$

$$\text{N.C.} = (x_{k+1}, y_k)$$

Initial Parameter

$$P_k = 2\Delta y - \Delta x = 10 - 8 = 2 > 0$$

$k$	$(x_k, y_k)$	$P_k$	$(x_{k+1}, y_{k+1})$
1	(35, 40)	2	(36, 41)

$$P_{k+1} = P_k + 2\Delta y - 2\Delta x(y_{k+1} - y_k)$$

$$= 2 + 10 - 16(41-40)$$

$$= 12 - 16 = -4 < 0$$

2	(36, 41)	-4	(37, 41)
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$$P_{k+1} = -4 + 10 - 16(41-41)$$

$$= 6 > 0$$

3	(37, 41)	6	(38, 42)
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$$\Delta x = 43 - 35$$

$$= 8$$

$$2\Delta x = 16$$

$$\Delta y = 45 - 40$$

$$= 5$$

$$2\Delta y = 10$$

$$P_{k+1} = 6 + 10 - 16(42 - 41) \\ = 16 - 16 = 0$$

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4. (38, 42)                      0                      (39, 43)

$$P_{k+1} = 0 + 10 - 16(43 - 42) \\ = 10 - 16 = -6 > 0$$

5 (39, 43)                      -6                      (40, 43)

$$P_{k+1} = -6 + 10 - 16(43 - 43) \\ = -6 + 10 = 4 > 0$$

6 (40, 43)                      4                      (41, 44)

$$P_{k+1} = 4 + 10 - 16(44 - 43) \\ = 14 - 16 \\ = -2 < 0$$

7 (41, 44)                      -2                      (42, 44)

$$P_{k+1} = -2 + 10 - 16(44 - 44) \\ = 8 > 0$$

8 (42, 44)                      8                      (43, 45)

~~40, 43~~ (35, 40)(36, 41)(37, 41)(38, 42)(39, 43)(40, 43)(41, 44) \\ (42, 44)(43, 45)

Que:- Generate the intermediate points using BLDA b/w two end points (3, 2) and (4, 6)