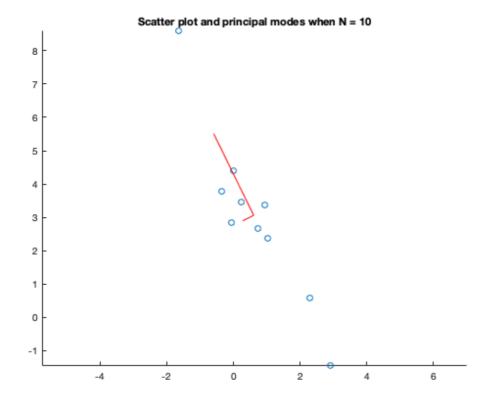
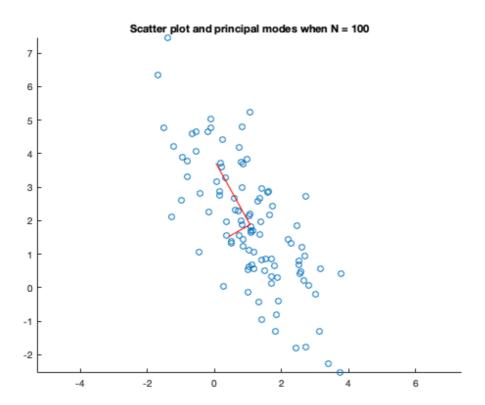
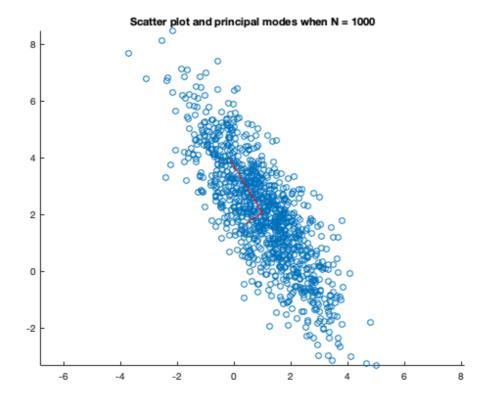
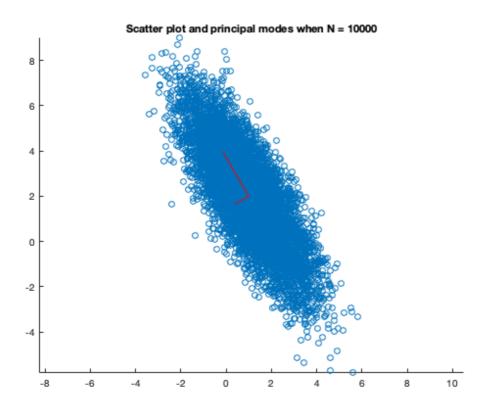
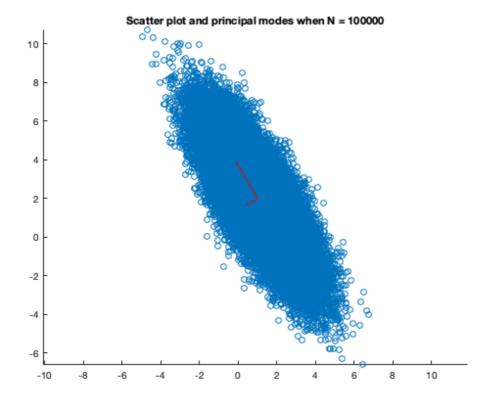
```
clear;
close all;
rng(190050128);
mu = [1; 2];
C = [1.6250, -1.9486; -1.9486, 3.8750]; % Given covariance matrix
[U, D2] = eig(C);
A = U*sqrt(D2)*U';
samples = [10 100 1000 10000 100000];
for i = 1:5
   N = samples(i);
   % Part (b) and (c)
   for trial = 1:100
       W = randn([2 N]);
       X = A*W + mu;
                                    % Generated sample with required mean and covariance matrix
                                     % ML estimate of mean
       mu = sum(X, 2)/N;
       mu_error = sqrt((mu - mu_)' * (mu - mu_) / (mu' * mu));
       mean_error(trial, i) = mu_error;
       C_{-} = (X - mu_{-}) * (X - mu_{-})' / N;
                                                % ML estimate of covariance matrix
       C_error = sqrt(sum((C - C_) .^2, 'all') / sum(C .^2, 'all'));
       cov_error(trial, i) = C_error;
   end
   % Part (d)
   [U_, D_] = eig(C_);
   l = diag(sqrt(D_));
                            % 2x1 vector containing eigenvalues
   figure;
   scatter(X(1, :), X(2, :));
   axis equal;
   hold on;
   X1 = [mu_(1) mu_(1)];
   Y1 = [mu_(2) mu_(2)];
   X2 = X1 + [1(1)*U_(1, 1) 1(2)*U_(1, 2)];
   Y2 = Y1 + [1(1)*U_(2, 1) 1(2)*U_(2, 2)];
   plot([X1; X2], [Y1; Y2], 'r');
   hold off;
   title(['Scatter plot and principal modes when N = ', num2str(N)]);
end
figure;
boxplot(mean error);
title('Error between true mean and ML estimate of mean');
xlabel('log_{10}(N)');
figure;
boxplot(cov error);
title('Error between true cov and ML estimate of cov matrix');
xlabel('log_{10}(N)');
```

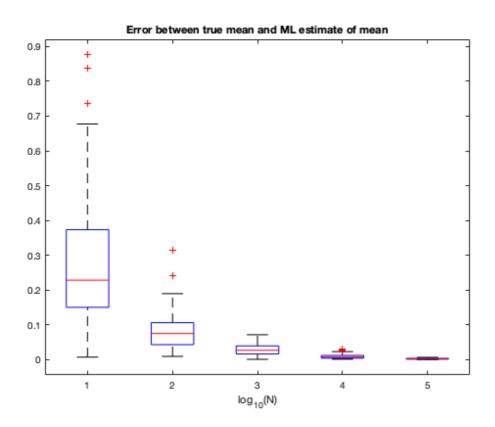


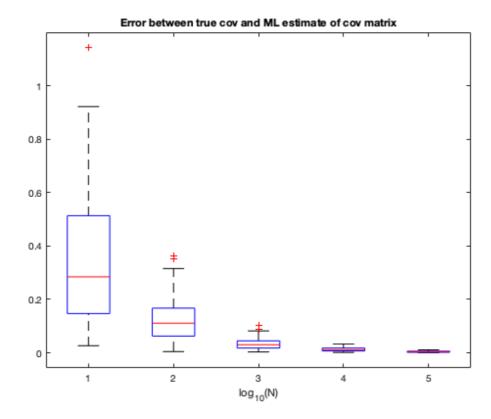












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