

# CS 747, Autumn 2020: Week 7, Lecture 1

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Autumn 2020

# Reinforcement Learning

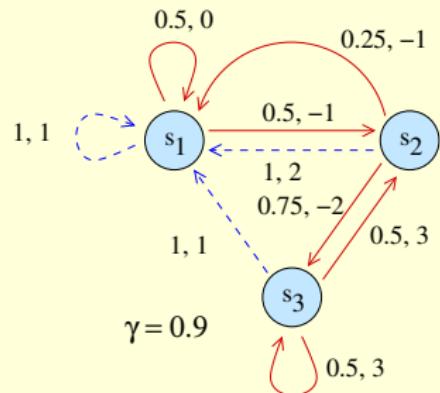
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2. Upcoming topics
3. Applications

# Reinforcement Learning

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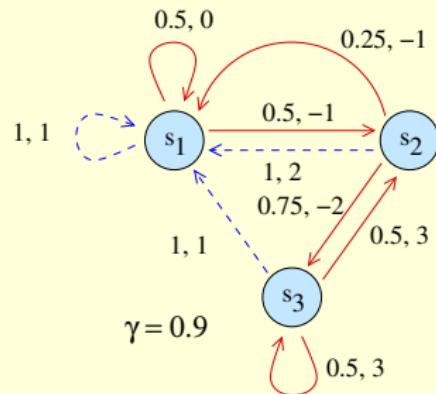
# The Learning Setting

Underlying MDP:

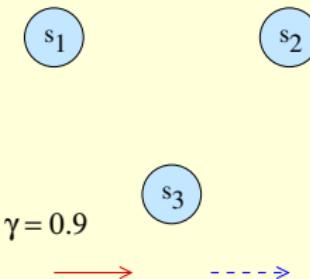


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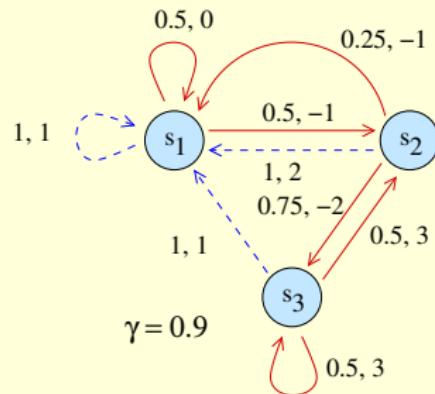


Agent's view:

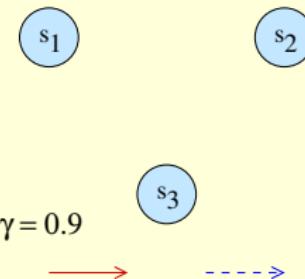


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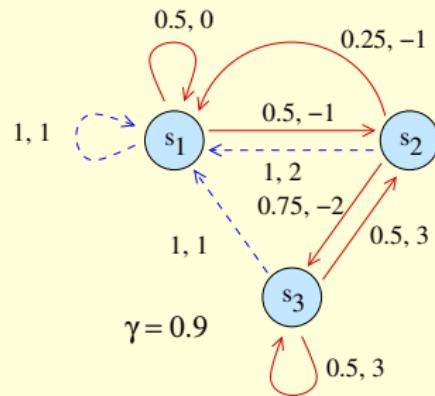
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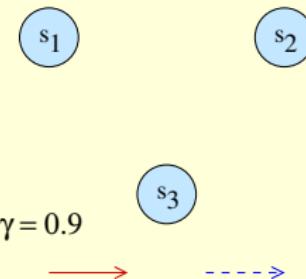
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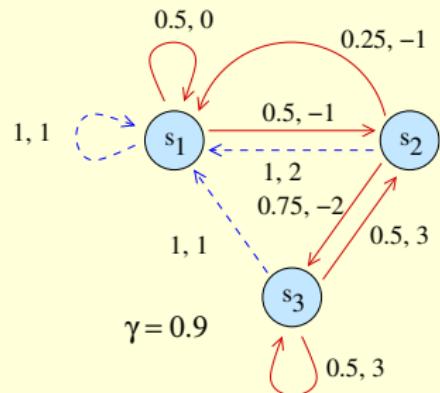
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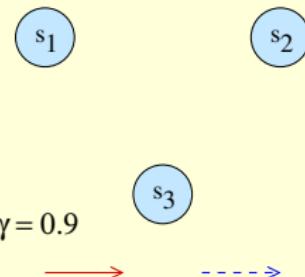
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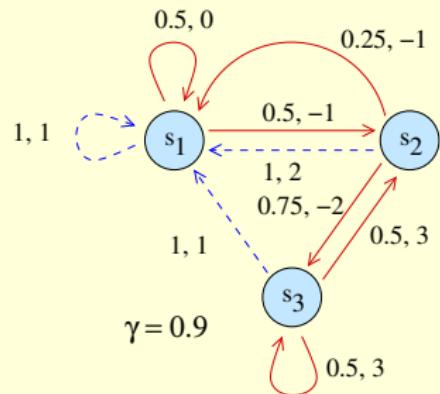
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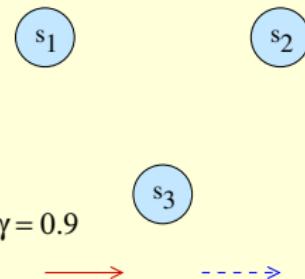
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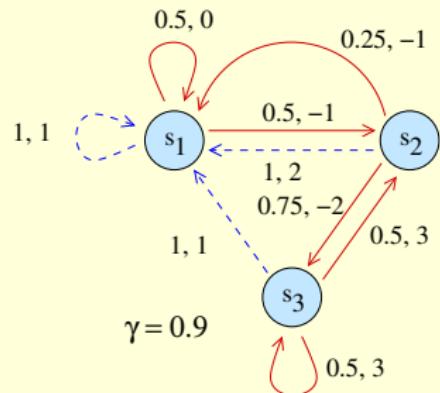
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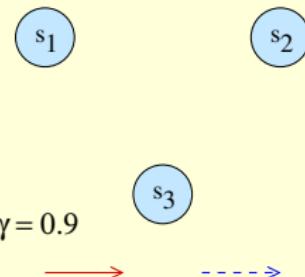
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Can the agent eventually take optimal actions?

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- A learning algorithm  $L$  is a mapping from the set of all histories to the set of all (probability distributions over) arms.
- **Learning problem:** Can we construct  $L$  such that

$$\lim_{T \rightarrow \infty} \frac{1}{T} \left( \sum_{t=0}^{T-1} \mathbb{P}\{a^t \sim L(h^t) \text{ is an optimal action for } s^t\} \right) = 1?$$

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- Applications
  - ▶ ATARI games (Mnih *et al.* (2015)), Go (Silver *et al.* (2016)).

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# Board Games

Backgammon



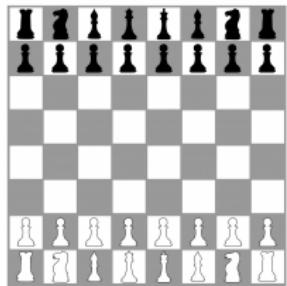
[1]

Go



[2]

Chess



[3]

References: Tesauro (1992), Silver *et al.* (2018).

1. <https://www.publicdomainpictures.net/pictures/60000/velka/backgammon.jpg>.
2. <https://www.publicdomainpictures.net/pictures/170000/velka/finished-go-game.jpg>.
3. <https://www.publicdomainpictures.net/pictures/80000/velka/chess-board-and-pieces.jpg>.

# Robotics and Control

## Helicopter control



[1]

Reference: Ng *et al.* (2003).

1. <https://www.publicdomainpictures.net/pictures/20000/velka/police-helicopter-8712919948643Mk.jpg>

# Video Games



[1]

Reference: Mnih *et al.* (2015).

1. <https://www.publicdomainpictures.net/pictures/30000/velka/arcade-gaming.jpg>.

# Computer Systems

## Optimising a memory controller



[1]

- Reference: İpek *et al.* (2008).

1. <https://www.publicdomainpictures.net/pictures/100000/velka/motherboard.jpg>.

# Healthcare

## Adaptive treatment of epilepsy



[1]

- Reference: Guez *et al.* (2008).

1. <https://www.publicdomainpictures.net/pictures/140000/velka/brain-signals.jpg>.

# Finance

## Stock trading



- Reference: Moody and Saffell (2001).

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