	 neural_network.py All you will have to do is to copprovided you different .py files lines. Note that these are the office. You are allowed to make as masseparately, therefore it can semight have an issue. For the "HW4 - Non-program" 	the autograder on "HW4 - Bonus-Programming" in the following format: by your implementations of the classes "dlnet" and "RandomForest" onto the respective file and we added libraries in those files please DO NOT remove those lines and add your code only allowed libraries that you can use for the homework. any submissions until the deadline as you like. Additionally, note that the autograder tests enve as a useful tool to help you debug your code if you are not sure of what part of your implementary part, you will download your jupyter notbook as HTML, print it as a PDF from year. To download the notebook as html, click on "File" on the top left corner of this page		
: ii	and submit it on Gradescope. To download the notebook as html, click on "File" on the top left corner of this page and "Download as > HTML". The non-programming part corresponds to Q1, Q2, Q3.3, Q4 Environment Setup import numpy as np import matplotlib.pyplot as plt from sklearn.datasets import load_breast_cancer from sklearn.model_selection import train_test_split from sklearn.model_selection import train_test_split from sklearn.metrics import classification_report from sklearn.metrics import plot_confusion_matrix from collections import Counter from scipy import stats from math import log2, sqrt import pandas as pd import time from sklearn.model_selection import train_test_split from sklearn.model_selection import train_test_split from sklearn.preprocessing import LabelEncoder from sklearn.preprocessing import LabelEncoder from sklearn.tree import DecisionTreeClassifier			
f f f f i i f				
f	rom sklearn.datasets imporrom sklearn.metrics imporrom sklearn import svm . Two Layer Neural I	_		
	Neuron or b_1 node θ_{11}	Bias $1 \qquad b^{2}_{1}$ 0_{11} 0^{2}_{11}		
	feature x_1 θ^{1}_{2d} θ^{1}_{2d} θ^{1}_{2d} feature x_d θ^{1}_{m1} θ^{1}_{m}	relu or $tanh$ 0_{12} 0_{22} 0_{22} 0_{22}		
		clarification – θ^1_{21} – theta of 1 st layer connecting 2 nd hidden unit of 1 st layer with 1 st input unit θ^2_{12} - theta of 2 nd layer connecting 1 st unit of 2 nd layer with 2 nd hidden unit of 1 st layer b ¹ ₁ – bias for 1 st hidden unit of 1 st layer		
Α	single layer perceptron can be th	nought of as a linear hyperplane as in logistic regression followed by a non-linear activation follow		
b c F T d	$x \in R$ is the bias element for the embination of the features in x we will be connected Layer pically, a modern neural network different configurations such as cast which comprises multiple parallel products and the comprises of the comprise o	contains millions of perceptrons as the one shown in the previous image. Perceptrons interscaded or parallel. In this part, we describe a fully connected layer configuration in a neural perceptrons forming one layer.		
ir n ω ο θ c	put/hidden/output units cascaded demotes the number of hidden under $u^{[l]} \in R^m$ is a m-dimension perations. Similarly, $o^{[l-1]}$ is the number of $R^m \in R^m \times R^m$ is the weight matrix of presponds to one hidden unit of the presponds of the presponds $R^m \times R^m \times R^m$	describe a fully connected layer. Each layer in a fully connected network has a number of d in parallel. Let us a define a single layer of the neural net as follows: units in a single layer l whereas n denotes the number of units in the previous layer $l-1$. $u^{[l]} = \theta^{[l]} o^{[l-1]} + b^{[l]}$ hal vector pertaining to the hidden units of the l^{th} layer of the neural network after applying l^{th} dimensional output vector corresponding to the hidden units of the $(l-1)^{th}$ activation lay if the l^{th} layer where each row of $\theta^{[l]}$ is analogous to θ_l described in the previous section i.e. the l^{th} layer. $b^{[l]} \in R^m$ is the bias vector of the layer where each element of b pertains to only be dement wise non-linear activation function $o^{[l]} = \phi(u^{[l]})$. The whole operation can be $o^{[l]} = \phi(\theta^{[l]} o^{[l-1]} + b^{[l]})$		
T F	Relu			
Т	he derivative of relu function is given	$\operatorname{ven as} o' = \phi'(u) = \begin{cases} 0 & u \leq 0 \\ 1 & u > 0 \end{cases}$ $\operatorname{relu}(u)$		
	8 - 6 - 4 -			
S	2 - 0 Sigmoid	-10 -5 0 5 10 u		
0	utput is between 0 and 1. The ma	In-linear function with S-shaped curve. This function is useful in the case of binary classifical athematical form of the function is $o = \phi(u) = \frac{1}{1+e^{-u}}$ tion has a nice form and is given as $o' = \phi'(u) = \frac{1}{1+e^{-u}} \left(1 - \frac{1}{1+e^{-u}}\right) = \phi(u)(1-\phi(u))$		
	0.8 -	Sigmoid(u)		
	0.6 -			
T a	anh anh also known as hyperbolic tang ways proves to be better than the	gent is like a shifted version of sigmoid activation function with its range going from -1 to 1. e sigmoid function since the mean of the activations are closer to zero. Tanh has an effect of ext layer a bit easier. The mathematical form of tanh is given as		
	ata that makes learning for the ne he derivative of tanh is given as	ext layer a bit easier. The mathematical form of tanh is given as $o = \phi(u) = tanh(u) = \frac{e^u - e^{-u}}{e^u + e^{-u}}$ $o' = \phi'(u) = 1 - \left(\frac{e^u - e^{-u}}{e^u + e^{-u}}\right)^2 = 1 - o^2$ $\tanh(u)$		
	1.00 - 0.75 - 0.50 - 0.25 - -0.25 -			
	-0.50 - -0.75 - -1.00 -	-3 -2 -1 0 1 2 3		
n le w	etwork parameters that minimizes vel the distance between true dat ill be looking for network paramet E loss is given by	aral network is the loss function. The whole purpose of gradient descent algorithm is to find a the loss function. In this exercise, we minimize Cross Entropy (CE) loss that represents on the distribution and estimated distribution by neural network. So during training of the neural ters that minimizes the distance between true and estimated distribution. The mathematical $CE(p,q) = -\sum_i p(x_i) \log q(x_i)$		
I I	nplementation details	and $q(x)$ is the estimated distribution. as in this exercise, we have probability distribution of a label y_i given by $y_i = \begin{cases} 1 & \text{with probability } p(x_i) \\ 0 & \text{with probability } 1 - p(x_i) \end{cases}$ be written as $p(x_i) = \sum_{i=1}^{N} \frac{y_i}{N}$		
v F	Forward Propagation /e start by initializing the weights	hary estimation can be written as $CE(y_i, \mathring{y_i}) = -\frac{1}{N} \sum_{i=1}^N \left(y_i \log(\mathring{y_i}) + (1-y_i) \log(1-\mathring{y_i}) \right)$ and $\mathring{y_i} \in [0, 1]$ is the estimated label. 1 of the fully connected layer using Xavier initialization Xavier initialization. During training, we		
b	elow.	37		
Д	•	$\theta^{[2]}:= heta^{[2]}-lr imesrac{\partial l}{\partial heta^{[2]}}$		
		$b^{[2]} := b^{[2]} - lr \times \frac{\partial l}{\partial b^{[2]}}$ $\theta^{[1]} := \theta^{[1]} - lr \times \frac{\partial l}{\partial \theta^{[1]}}$ $b^{[1]} := b^{[1]} - lr \times \frac{\partial l}{\partial b^{[1]}}$ sides the step size we want to take in the direction of the negative gradient. $\frac{\partial l}{\partial \theta^{[2]}} = \frac{\partial l}{\partial o^{[2]}} \frac{\partial o^{[2]}}{\partial u^{[2]}} \frac{\partial u^{[2]}}{\partial \theta^{[2]}}$		
â	o, $\frac{\partial l}{\partial o^{[2]}}$ is the differentiation of the $\frac{o^{[2]}}{u^{[2]}}$ is the differentiation of the Sig $\frac{u^{[2]}}{g^{[2]}}$ is equal to $o^{[1]}$	$\frac{\partial l}{\partial b^{[2]}} = \frac{\partial l}{\partial o^{[2]}} \frac{\partial o^{[2]}}{\partial u^{[2]}} \frac{\partial u^{[2]}}{\partial b^{[2]}}$ e cross entropy loss function at point $o^{[2]}$		
T v d	ariables during forward propagation erivatives, we store the values we	$2^{1}\&o^{[1]}$ which are calculated during forward propagation. So we need to store these values on to be able to access them during backward propagation. Similarly for calculating other pull be needing for chain rule in cache. These values are obtained from the forward propagation is implemented as a dictionary here where the keys are the variable names and the value		
Д	lso, the functional form of the CE	differentiation and Sigmoid differentiation are given by $\frac{\partial l}{\partial o^{[2]}} = \frac{-1}{N} \left(\frac{y}{o^{[2]}} - \frac{1-y}{1-o^{[2]}} \right)$ $\frac{\partial o^{[2]}}{\partial u^{[2]}} = \frac{1}{1+e^{-u^{[2]}}} \left(1 - \frac{1}{1+e^{-u^{[2]}}} \right) = o^{[2]} (1-o^{[2]})$		
		$\frac{\partial u^{[2]}}{\partial \theta^{[2]}} = o^{[1]}$		
	his completes the differentiation or which are given as follows:			
for V	or which are given as follows:	$\frac{\partial u^{[2]}}{\partial \theta^{[2]}} = o^{[1]}$ $\frac{\partial u^{[2]}}{\partial b^{[2]}} = 1$ of loss function w.r.t to parameters in the second layer. We now move on to the first layer, the $\frac{\partial l}{\partial \theta^{[1]}} = \frac{\partial l}{\partial o^{[2]}} \frac{\partial o^{[2]}}{\partial u^{[2]}} \frac{\partial u^{[2]}}{\partial o^{[1]}} \frac{\partial o^{[1]}}{\partial u^{[1]}} \frac{\partial u^{[1]}}{\partial \theta^{[1]}}$ $\frac{\partial l}{\partial b^{[1]}} = \frac{\partial l}{\partial o^{[2]}} \frac{\partial o^{[2]}}{\partial u^{[2]}} \frac{\partial u^{[2]}}{\partial u^{[1]}} \frac{\partial o^{[1]}}{\partial u^{[1]}} \frac{\partial u^{[1]}}{\partial b^{[1]}}$ $\frac{\partial u^{[2]}}{\partial o^{[1]}} = \theta^{[2]}$ $\frac{\partial o^{[1]}}{\partial u^{[1]}} = \begin{cases} 0 & \text{if } u^{[1]} \leq 0 \\ 1 & \text{if } u^{[1]} > 0 \end{cases}$ $\frac{\partial u^{[1]}}{\partial \theta^{[1]}} = x$ $\frac{\partial u^{[1]}}{\partial \theta^{[1]}} = 1$ To of the Relu function at $u^{[1]}$. In order the same process can be extended to different neural net with reluction expression.		
N Talala (ote that $\frac{\partial e^{[1]}}{\partial u^{[1]}}$ is the differentiation the above equations outline the forestivation layer and sigmoid has the yers like tanh. Code Implementation This question, you will implement and optimization techniques. Functions here - Relu, Tanh and Signih activation followed by sigmoid indicativation followed by sigmoid igmoid. The pu'll also implement gradient descender graduate students. The litrain these neural nets on bread outlier to have a properties of the properties of	$\frac{\partial u^{(2)}}{\partial \theta^{(2)}} = o^{[1]}$ $\frac{\partial u^{(2)}}{\partial \theta^{(2)}} = 1$ of loss function w.r.t to parameters in the second layer. We now move on to the first layer, the of loss function w.r.t to parameters in the second layer. We now move on to the first layer, the of loss function w.r.t to parameters in the second layer. We now move on to the first layer, the of loss function w.r.t to parameters in the second layer. We now move on to the first layer, the of loss function w.r.t to parameters in the second layer. We now move on to the first layer, the of loss function w.r.t to parameters in the second layer. We now move on to the first layer, the of layer is a constant. $\frac{\partial l}{\partial \theta^{[1]}} = \frac{\partial l}{\partial o^{[2]}} \frac{\partial o^{[2]}}{\partial u^{[2]}} \frac{\partial o^{[1]}}{\partial u^{[1]}} \frac{\partial u^{[1]}}{\partial u^{[1]}} \frac{\partial u^{[1]}}{\partial u^{[1]}} > 0$ $\frac{\partial u^{[2]}}{\partial u^{[1]}} = \theta^{[2]}$ $\frac{\partial u^{[1]}}{\partial \theta^{[1]}} = 1$ of the Relu function at $u^{[1]}$. In or the Relu function at $u^{[1]}$. In order the Relu function at $u^{[1]}$. In order the Relu function at $u^{[1]}$. In order to the Relu function at $u^{[1]}$. In order to the Relu function at $u^{[1]}$. In order to the Relu function at $u^{[1]}$. In order to the Relu function at $u^{[1]}$ and		
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In [7]:	Training the Neural Network, you do not need to modify this cell We are going to use Breast Cancer Wisconsin (Diagnostic) Data Set provided by sklearn https://scikit-learn.org/stable/modules/generated/sklearn.datasets.load_breast_cancer.html ''' dataset = load_breast_cancer() # load the dataset x, y = dataset.data, dataset.target x = MinMaxScaler().fit_transform(x) #normalize data x_train, x_test, y_train, y_test = train_test_split(x, y, random_state=1) #split data x_train, x_test, y_train, y_test = x_train.T, x_test.T, y_train.reshape(1,-1), y_test #condition data nn = dlnet(x_train,y_train,lr=0.1) # initalize neural net class nn.stochastic_gradient_descent(x_train, y_train, iter = 66000) #train
	<pre># create figure fig = plt.plot(np.array(nn.loss).squeeze()) plt.title(f'Training: {nn.neural_net_type}') plt.xlabel("Epoch") plt.ylabel("Loss") Loss after iteration 2000: 0.001772 Loss after iteration 4000: 0.000119 Loss after iteration 6000: 0.019489 Loss after iteration 8000: 1.313548 Loss after iteration 10000: 0.001398 Loss after iteration 12000: 0.000014 Loss after iteration 14000: 0.000057</pre>
	Loss after iteration 16000: 0.000012 Loss after iteration 18000: 0.000004 Loss after iteration 20000: 0.067969 Loss after iteration 22000: 0.000238 Loss after iteration 24000: 0.001232 Loss after iteration 26000: 0.014399 Loss after iteration 28000: 0.000140 Loss after iteration 30000: 0.000063 Loss after iteration 32000: 0.001527 Loss after iteration 34000: 0.000117 Loss after iteration 36000: 0.000391 Loss after iteration 38000: 0.000000 Loss after iteration 40000: 0.000003 Loss after iteration 40000: 0.000003 Loss after iteration 40000: 0.000003
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Out[7]:	Text(0, 0.5, 'Loss') Training: Tanh -> Sigmoid 12 -
In [8]:	<pre>"" "" Testing Neural Network "" y_predicted = nn.predict(x_test) # predict #plot print(f"Classification Report for {nn.neural_net_type}\n\n")</pre>
	<pre>print(classification_report(y_test, y_predicted, target_names=dataset.target_names)) plot_confusion_matrix(nn, x_test, y_test, cmap=plt.cm.Blues, display_labels=dataset.target_names) plt.show() Classification Report for Tanh -> Sigmoid precision recall f1-score support malignant 0.95 0.96 0.95 55 benign 0.98 0.97 0.97 88 accuracy 0.97 143</pre>
	macro avg
	2: (Bounus for all) Image Classification based on Convolutional Neural Networks [15pts] **[W]** Keras is a deep learning API written in Python, running on top of the machine learning platform TensorFlow. It was developed with a focus on enabling fast experimentation. Being able to go from idea to result as fast as possible is key to doing good research. In this part, you
	will build a convolutional neural network based on Keras to solve the image classification task for MINIST. If you haven't installed TensorFlow, you can install the package by pip command or train your model by uploading HW4 notebook to Colab directly. Colab contains all packages you need for this section. Hint1: First contact with Keras Hint2: How to Install Keras Hint3: CS231n Tutorial (Layers used to build ConvNets)
In [9]:	<pre>fromfuture import print_function import keras from keras.datasets import mnist from keras.models import Sequential from keras.layers import Dense, Dropout, Flatten from keras.layers import Conv2D, MaxPooling2D from keras import backend as K import matplotlib.pyplot as plt</pre> Load MINIST dataset
In [10]:	We use MINIST dataset to train our model. MINIST is a subset of a larger set available from NIST. MNIST database of handwritten digits has a training set of 60,000 examples, and a test set of 10,000 examples. Each example is 28 × 28 pixel grayscale image of handwritten digits between 0 to 9. # Helper function, You don't need to modify it # split data between train and test sets (x_train, y_train), (x_test, y_test) = mnist.load_data() # input image dimensions img_rows, img_cols = 28, 28 #set num of classes num_classes = 10
	<pre>if K.image_data_format() == 'channels_first': x_train = x_train.reshape(x_train.shape[0], 1, img_rows, img_cols) x_test = x_test.reshape(x_test.shape[0], 1, img_rows, img_cols) input_shape = (1, img_rows, img_cols) else: x_train = x_train.reshape(x_train.shape[0], img_rows, img_cols, 1) x_test = x_test.reshape(x_test.shape[0], img_rows, img_cols, 1) input_shape = (img_rows, img_cols, 1) x_train = x_train.astype('float32') x_test = x_test.astype('float32') x_train /= 255 x_test /= 255 print('x_train_shape:', x_train.shape)</pre>
	<pre>print('x_test shape:', x_test.shape) print(x_train.shape[0], 'train samples') print(x_test.shape[0], 'test samples') # convert class vectors to binary class matrices y_train = keras.utils.to_categorical(y_train, num_classes) y_test = keras.utils.to_categorical(y_test, num_classes) x_train shape: (60000, 28, 28, 1) x_test shape: (10000, 28, 28, 1) 60000 train samples 10000 test samples</pre> Load some images from MINIST
In [11]:	<pre># Helper function, You don't need to modify it # Show some images from MINIST for i in range(0,25): plt.subplot(5,5,i+1) image=x_train[i].reshape((28,28)) plt.imshow(image,cmap='gray') plt.show()</pre>
	As you can see from above, the MINIST dataset contains handwritten digits from 0 to 9. The digits have been size-normalized and centered in fixed-size images.
	Build convolutional neural network model In this part, you need to build a convolutional neural network that contains 2 convolutional layers. The architecture of thie model is: [INPUT - CONV - RELU - MAXPOOL - CONV - RELU - MAXPOOL - FC1 - FC2] [1] INPUT: [28 × 28 × 1] will hold the raw pixel values of the image, in this case, an image of width 28, height 28, and with only one color channels.
	CONV: Conv. layer will compute the output of neurons that are connected to local regions in the input, each computing a dot product between their weights and a small region they are connected to the input volume. We decide to set the kernel_size 3×3 for the both Conv. layers. For example, the output of the Conv. layer may like $[26 \times 26 \times 32]$ if we use 32 filters. RELU: As we mentioned in the previous section, the Relu layer will apply an elementwise activation function, such as the max(0,x) thresholding at zero, which leaves the size of the volume unchanged. MAXPOOL: MAXPOOL layer will perform a downsampling operation along the spatial dimensions (width, hight). FC1: First Fully-Connected layer, we use ReLu as the activation function. The dimension of the output space is 128. FC2: Second Fully-Connected layer will compute the class scores. We use Softmax as the activation function. The
In [12]:	dimension of the output space is the number of class. Loss function: Crossentropy (mentioned in the previous section) optimizer: Stochastic gradient descent(SGD) [1] CS231n: https://cs231n.github.io/convolutional-networks/ # Helper function, You don't need to modify it # Show the architecture of the model achi=plt.imread('Architecture.png') fig = plt.figure(figsize=(10,10)) plt.imshow(achi)
Out[12]:	<pre>Model: "sequential_1" Layer (type)</pre>
	max_pooling2d_3 (MaxPooling2 (None, 5, 5, 64) 0 flatten_1 (Flatten)
In [13]:	0 100 200 300 400 500 600 Defining Variables
In [14]:	<pre>Defining model def create_net():</pre>
	<pre># Add first convolution layer with activation function Relu() model.add(Conv2D(32, kernel_size=(3, 3), activation='relu', input_shape=(28, 28, 1))) # Add first max pooling layer with pool size 2X2 model.add(MaxPooling2D(pool_size=(2, 2))) # Add second convolution layer with activation function Relu() model.add(Conv2D(64, kernel_size=(3, 3), activation='relu', input_shape=(13, 13, 1))) # Add second max pooling layer with pool size 2X2 model.add(MaxPooling2D(pool_size=(2, 2))) # Flatten output model.add(Flatten()) # Add first fully connected layer with 128 nodes model.add(Dense(128, activation='relu'))</pre>
In [15]:	<pre># Add second fully connected layer with 10 nodes model.add(Dense(10, activation='softmax')) # Compile model SDG = keras.optimizers.SGD(learning_rate=lr) model.compile(optimizer = SDG, loss='categorical_crossentropy', metrics=['accuracy']) # Return model return model # Helper function, You don't need to modify it # model.summary() gives you details of your architecture. #You can compare your architecture with the 'Architecture.png' model=create net()</pre>
	Model: "sequential" Layer (type) Output Shape Param # conv2d (Conv2D) (None, 26, 26, 32) 320 max_pooling2d (MaxPooling2D) (None, 13, 13, 32) 0 conv2d_1 (Conv2D) (None, 11, 11, 64) 18496 max_pooling2d_1 (MaxPooling2 (None, 5, 5, 64) 0
	flatten (Flatten) (None, 1600) 0 dense (Dense) (None, 128) 204928 dense_1 (Dense) (None, 10) 1290 ===================================
To [16].	Tuning: Training the network is the next thing to try. You can set your parameter at the Defining Variable section. If your parameters are set properly, you should see the loss of the validation set decreased and the value of accuracy increased. It may take more than 20 minutes to train your model. Expected Result: You should be able to achieve more than 90% accuracy on the test set to get full 15 points. If you achieve accuracy between 80% to 90%, you will only get half points of this part. Train your own CNN model
In [16]:	<pre># Helper function, You don't need to modify it # Train the model history = model.fit(x_train, y_train,</pre>
	469/469 [====================================
	s: 0.5349 - val_accuracy: 0.8593 Epoch 7/12 469/469 [====================================
In [17]:	469/469 [====================================
	<pre>plt.title('model accuracy') plt.ylabel('accuracy') plt.xlabel('epoch') plt.legend(['train', 'test'], loc='upper left') plt.show() # summary plt.plot(history.history['loss']) plt.plot(history.history['val_loss']) plt.title('model loss') plt.ylabel('loss') plt.xlabel('epoch') plt.legend(['train', 'test'], loc='upper left') plt.show()</pre>
	dict_keys(['loss', 'accuracy', 'val_loss', 'val_accuracy']) model accuracy 0.9 train 0.8 0.7 0.6 0.5 0.4
	0.3 - 0.2 - 0 2 4 6 8 10 epoch model loss 2.25 - train test 1.50 - 1.50
	3: Random Forests [40pts] **[P]** **[W]** NOTE: Please use sklearn's DecisionTreeClassifier in your Random Forest implementation. You can find more details about this classifier
	3.1 Random Forest Implementation (30 pts) **[P]** The decision boundaries drawn by decision trees are very sharp, and fitting a decision tree of unbounded depth to a list of examples almost inevitably leads to overfitting. In an attempt to decrease the variance of a decision tree, we're going to use a technique called 'Bootstrap Aggregating' (often abbreviated 'bagging'). This stems from the idea that a collection of weak learners can learn decision boundaries as well as a strong learner. This is commonly called a Random Forest. We can build a Random Forest as a collection of decision trees, as follows: 1) For every tree in the random forest, we're going to
	a) Subsample the examples with replacement. Note that in this question, the size of the subsample data is equal to the original dataset. b) From the subsamples in a), choose attributes at random to learn on in accordance with a provi ded attribute subsampling rate. Based on what it was mentioned in the class, we randomly pick fe atures in each split. We use a more general approach here to make the programming part easier. Let's randomly pick some features (70% percent of features) and grow the tree based on the pre-determined randomly selected features. Therefore, there is no need to find random features in each split. c) Fit a decision tree to the subsample of data we've chosen to a certain depth.
	Classification for a random forest is then done by taking a majority vote of the classifications yielded by each tree in the forest after it classifies an example. In RandomForest Class, 1. X is assumed to be a matrix with num_training rows and num_features columns where num_training is the number of total records and num_features is the number of features of each record. 2. y is assumed to be a vector of labels of length num_training. NOTE: Lookout for TODOs for the parts that needs to be implemented.
In [18]:	<pre>import math import sklearn import time import pdb class RandomForest(object): definit(self, n_estimators=50, max_depth=None, max_features=0.7): # helper function. You don't have to modify it # Initialization done here self.n_estimators = n_estimators self.max_depth = max_depth self.max_features = max_features</pre>
	<pre>self.bootstraps_row_indices = [] self.feature_indices = [] self.out_of_bag = [] self.decision_trees = [sklearn.tree.DecisionTreeClassifier(max_depth=max_depth, criterion='entr opy') for i in range(n_estimators)] defbootstrapping(self, num_training, num_features, random_seed = None): """ TODO: - Randomly select indices of size num_training with replacement corresponding to row locations of selected samples in the original dataset. - Randomly select indices without replacement corresponding the column locations of selected fe atures in the original feature</pre>
	list (num_features denotes the total number of features in the training set, max_features de notes the percentage of features that are used to fit each decision tree). Reference: https://en.wikipedia.org/wiki/Bootstrapping_(statistics) Args: - num_training: an integer N representing the total number of training instances num_features: an integer D representing the total number of features. Returns: - row_idx: (N,) numpy array of row indices corresponding to the row locations of the selected s amples in the original dataset col_idx: 1-D array of column indices corresponding to the column locations of selected featur
	<pre>es in the original feature list. Hint: Consider using np.random.choice. """ np.random.seed(seed=random_seed) row_idx = np.random.choice(num_training, num_training, replace=True) col_idx = list(np.random.choice(num_features, math.floor(num_features * self.max_features), rep lace=False)) return row_idx, col_idx def bootstrapping(self, num_training, num_features): """ Args: - num training: an integer N representing the total number of training instances.</pre>
	<pre>- num_features: an integer D representing the total number of features. Returns: - None """ # helper function. You don't have to modify it # Initializing the bootstap datasets for each tree for i in range(self.n_estimators): total = set(list(range(num_training))) row_idx, col_idx = selfbootstrapping(num_training, num_features) total = total - set(row_idx) self.bootstraps_row_indices.append(row_idx) self.feature_indices.append(col_idx)</pre>
	<pre>def fit(self, X, y): """ TODO: Train decision trees using the bootstrapped datasets. Note that you need to use the row indices and column indices. Args: -X: NxD numpy array, where N is number</pre>
	<pre>Returns: - None """ self.bootstrapping(X.shape[0], X.shape[1]) i = 0 for decision_tree in self.decision_trees: xs = np.take(np.take(X, self.bootstraps_row_indices[i], axis=0), self.feature_indices[i], a xis=1) ys = np.take(y, self.bootstraps_row_indices[i], axis=0) decision_tree.fit(xs, ys) i += 1</pre>
	<pre>def 00B_score(self, X, y): # helper function. You don't have to modify it # This function computes the accuracy of the random forest model predicting y given x. accuracy = [] for i in range(len(X)): predictions = [] for t in range(self.n_estimators): if i in self.out_of_bag[t]:</pre>
	3.2 Hyperparameter Tuning with a Random Forest (5pts) **[P]** In machine learning, hyperparameters are parameters that are set before the learning process begins. The max_depth, num_estimators, or max_features variables from 3.1 are examples of different hyperparameters for a random forest model. In this section, you will tune your random forest model on an e-commerce dataset to achieve a high accuracy on a classifying revenue sessions (whether a customer will purchase a product) from user behavior. Let's first review the dataset in a bit more detail. Dataset Objective
	Imagine that we are the founders of a new e-commerce company that uses machine learning to optimize the user experience. We are tasked with the responsibility of coming up with a method for determining the likelihood of a shopping session ending in a purchase being made. We will then use this information to adjust pricing and services to encourage more purchasing. After much deliberation amongst the team, you come to a conclusion that we can use past online shopping data to predict the future occurence of revenue sessions. We will use our random forest algorithm from Q3.1 to predict if a shopping session ends in a purchase. You can find more information on the dataset here.
	The dataset that the company has collected has the following features: 1. Administrative : continuous variable 2. Administrative_Duration : continuous variable 3. Informational : continuous variable 4. Informational_Duration : continuous variable 5. ProductRelated : continuous variable 6. ProductRelated_Duration : continuous variable 7. BounceRates : continuous variable 8. ExitRates : continuous variable 9. PageValues : continuous variable 10. SpecialDay : continuous variable
	 Month: categorical variable OperatingSystems: continuous variable Browser: continuous variable Region: continuous variable TrafficType: continuous variable VisitorType: categorical variable Weekend: continuous variable Revenue: target variable> Your random forest model will try to predict this variable. A "True" value in this column means a shopper purchased an item given their user behavior described by features 1-17, while a "False" label indicates that a shopper did not purchase an item.
In [19]:	<pre># Logic for loading in datasets. DO NOT MODIFY anything in this block. from sklearn import preprocessing preprocessor = preprocessing.LabelEncoder() data_train = pd.read_csv("datasets/hw4_fall2020_data_train.csv") data_test = pd.read_csv("datasets/hw4_fall2020_data_test.csv") X_train = data_train.drop(columns = 'Revenue') y_train = data_train['Revenue'] X_test = np.array(data_test.drop(columns = 'Revenue')) y_test = np.array(data_test['Revenue']) X_train, y_train, X_test, y_test = np.array(X_train), np.array(y_train), np.array(X_test), np.array(y_test)</pre>
	#The following lines of code converts columns holding categorical or boolean variables into integers. X_train[:,10] = preprocessor.fit_transform(X_train[:,10]) X_test[:,10] = preprocessor.fit_transform(X_test[:,10]) X_train[:,-2] = preprocessor.fit_transform(X_train[:,-2]) X_test[:,-2] = preprocessor.fit_transform(X_test[:,-2]) In the following codeblock, train your random forest model with different values for max_depth, n_estimators, or max_features and evaluate each model on the held-out test set. Try to choose a combination of hyperparameters that maximizes your prediction accuracy on the test set (aim for 92%+). Once you are satisfied with your chosen parameters, change the default values for max_depth, n_estimators, and max_features in the init function of your RandomForest class in random_forest.py to your chosen values, and then submit this file to Gradescope. You must achieve at least a 92% accuracy against a hidden test set (this will NOT the same as the test set provided here) in Gradescope to receive full credit for this section.
In [20]:	n_estimators defines how many decision trees are fitted for the random forest. max_depth defines a stop condition when the tree reaches to a certain depth. max_features controls the percentage of features that are used to fit each decision tree. Tune these three parameters to achieve a better accuracy. While you can use the provided test set to evaluate your implementation, you will need to obtain 92% on a hidden test set to receive full credit for this section. """ import sklearn.ensemble n_estimators = 12 #Hint: Consider values between 5-12.
	<pre>n_estimators = 12 #Hint: Consider values between 5-12. max_depth = 12 # Hint: Consider values betweeen 3-12 max_features = 0.9 # Hint: Consider values betweeen 0.7-1.0. random_forest = RandomForest(n_estimators, max_depth, max_features) random_forest.fit(X_train, y_train) accuracy=random_forest.OOB_score(X_test, y_test) print("accuracy: %.4f" % accuracy) accuracy: 0.9312</pre>
	3.3 Plotting Feature Importance (5pts) **[W]** While building tree-based models, it's common to quantify how well splitting on a particular feature in a decision tree helps with predicting the target label in a dataset. Machine learning practicioners typically use "Gini importance", or the (normalized) total reduction in entropy brought by that feature to evaluate how important that feature is for predicting the target variable. Gini importance is typically calculated as the reduction in entropy from reaching a split in a decision tree weighted by the probability of reaching that split in the decision tree. Sklearn internally computes the probability for reaching a split by finding the total number of samples that reaches it during the training phase divided by the total number of samples in the dataset. This weighted value is our feature importance. Let's think about what this metric means with an example. A high probability of reaching a split on "TrafficType" in a decision tree trained on
	our e-commerce dataset (many samples will reach this split for a decision) and a large reduction in entropy from splitting on "TrafficType" will result in a high feature importance value for "TrafficType". This could mean "TrafficType" is a very important feature for predicting a customer's revenue session. On the other hand, a low probability of reaching a split on "Month" in a decision tree (few samples will reach this split for a decision) and a low reduction in entropy from splitting on "Month" will result in a low feature importance value. This could mean "Month" is not a very informative feature for predicting the revenue session in our decision tree. Thus, the higher the feature importance value, the more important the feature is to predicting the target label. Fortunately for us, fitting a sklearn. DecisionTreeClassifier to a dataset auomatically computes the Gini importance for every feature in the decision tree and stores these values in a feature importances variable. Review the docs for more details on how to access this variable. In the function below, display a bar plot that shows the feature importance values for at least one decision tree in your tuned random forest from Q3.2, and briefly comment on whether any features have noticeably higher / or lower importance weights than others. [Note that there
In [21]:	<pre>isn't a "correct" answer here. We simply want you to investigate how different features in your random forest contribute to predicting the target variable]. from matplotlib import pyplot as plt def plot_feature_importance(random_forest): """ TODO: -Display a bar plot showing the feature importance of every feature in at least one decision tree from the tuned random_forest from Q3.2. Args: random_forest: This is your implemented and tuned random forest from Q3.2.</pre>
	Returns: None. Calling this function should simply display the aforementioned feature importance bar cha rt """ i = 8 sort_idx = np.argsort(random_forest.decision_trees[i].feature_importances_)[::-1] importance = random_forest.decision_trees[i].feature_importances_[sort_idx] idx = random_forest.feature_indices[i] features = data_train.columns.drop('Revenue')[idx] features = features[sort_idx] plt.xticks(rotation='vertical') plt.title('Feature Importance for predicting Positive Revenue Sessions') plt.xlabel('Feature Importance')
	PageValues ProductRelated Duration Month Administrative_Duration BounceRates ProductRelated TafficType Region OperatingSystems Weekend SpecialDay American SpecialDay Informational SpecialDay Approach SpecialDay SpecialDay SpecialDay SpecialDay
	4: SVM (30 Pts) **[W]**

	Consider a dataset with 2 points in 1-dimensional space: $(x_1=-3,y_1=-1)$ and $(x_2=2,y_2=1)$. Here x are the point coordinates and y are the classes. Consider mapping each point to 3-dimensional space using the feature vector $\phi(x)=[1,2x,x^2]$. (This is equivalent to using a second order polynomial kernel.) The max margin classifier has the form $\min \theta ^2 s. t.$ $y_1(\phi(x_1)\theta+b) \geq 1$ $y_2(\phi(x_2)\theta+b) \geq 1$ Hint: $\phi(x_1)$ and $\phi(x_2)$ are the suppport vectors. We have already given you the solution for the suppport vectors and you need to calculate back the parameters. Margin is equal to $\frac{1}{ \theta }$ and full margin is equal to $\frac{2}{ \theta }$.
	(1) Find a vector parallel to the optimal vector θ . (4pts) $Z_1 = \phi(x_1) = [1, 2x_1, x_1^2] = [1, -6, 9] \text{and} Z_2 = \phi(x_1) = [1, 2x_2, x_2^2] = [1, 4, 4]$ $v = Z_2 - Z_1 \Rightarrow v = [1, 4, 4] - [1, -6, 9] \Rightarrow v = [0, 10, -5]$ $\hat{v} = \frac{v}{\ v\ } \Rightarrow \hat{v} = \frac{[0, 10, -5]}{\sqrt{(10)^2 + (-5)^2}} \Rightarrow \hat{v} = [0, \frac{2\sqrt{5}}{5}, -\frac{\sqrt{5}}{5}]$ (2) Calculate the value of the margin achieved by this θ ? (4pts) $margin = \frac{\ v\ }{2} \Rightarrow margin = \frac{5\sqrt{5}}{2}$ (3) Solve for θ , given that the margin is equal to $1/ \theta $. (4pts)
	Because θ and \hat{v} are parallel, we know that $\theta = k * \hat{v}$. Lets solve for θ $margin = \frac{1}{\ \theta\ } \Rightarrow \ \theta\ = \frac{1}{margin} \Rightarrow \ \theta\ = \frac{2\sqrt{5}}{25}$ $\theta = k * \hat{v} \Rightarrow \theta = [0, \frac{2\sqrt{5}}{5}k, \frac{-\sqrt{5}}{5}k]$ $\ \theta\ = \sqrt{(\frac{2\sqrt{5}}{5}k)^2 + (\frac{-\sqrt{5}}{5}k)^2} = \frac{2\sqrt{5}}{25} \Rightarrow (\frac{2\sqrt{5}}{5}k)^2 + (\frac{-\sqrt{5}}{5}k)^2 = \frac{4}{125} \Rightarrow k^2(\frac{4}{5} + \frac{1}{5}) = \frac{4}{125} \Rightarrow \sqrt{k^2} = \sqrt{\frac{4}{125}} \Rightarrow k = \pm \frac{2\sqrt{5}}{25}$ $\theta = [0, 0.16, -0.08] \text{or} \theta = [0, -0.16, 0.08]$
	(4) Solve for b using your value for θ . (4pts) To find b, we must plug in our two options for θ into the two constraint inequalities. The correct one will yield a result where $b \leq b'$ and $b \geq b'$ Lets try $\theta = [0, 0.16, -0.08]$ first: $y_1(Z_1\theta + b) \geq 1 => -1((0 - 6(0.16) - 9(0.08)) + b) \geq 1 => (-0.96 - 0.72) + b \leq -1 => -1.68 + b \leq -1 => b \leq 0.68$ $y_2(Z_2\theta + b) \geq 1 => 1((0 + 4(0.16) - 4(0.08)) + b) \geq 1 => (0.64 - 0.32) + b \geq 1 => 0.32 + b \geq 1 => b \geq 0.68$ We can conclude that: $b = 0.68$ and that the correct θ in question 3 is: $\theta = [0, 0.16, -0.08]$
Jr	We can conclude that: $b = 0.68$ and that the correct θ in question 3 is: $\theta = [0, 0.16, -0.08]$ (5) Write down the form of the discriminant function $f(x) = \phi(x)\theta + b$ as an explicit function of x . $f(x) = \phi(x)\theta + b = \sum f(x) = -0.08x^2 + 0.32x + 0.68$ 4.2 Feature Mapping (10 Pts) **[W]** Let's look at a dataset where the datapoint can't be classified with a good accuracy using a linear classifier. Run the below cell to generate the dataset. We will also see what happens when we try to fit a linear classifier to the dataset.
in [33]:	<pre># Generate dataset random_state = 1 X, y = make_moons(n_samples=1000, noise=.05) y = np.where(y == 0, -1, y) X_train, X_test, y_train, y_test = train_test_split(X, y,</pre>
	plt.scatter(X[:, 0], X[:, 1], c = y, marker = '.') plt.show() 100 - 0.75 - 0.50 - 0.00 -
In [34]:	def visualize_decision_boundary(X, y, feature_new=None, h=0.02): ''' You don't have to modify this function Function to vizualize decision boundary feature_new is a function to get X with additional features ''' This will make a Visualize to large() and visualize t
	<pre>x1_min, x1_max = X[:, 0].min() - 1, X[:, 0].max() + 1 x2_min, x2_max = X[:, 1].min() - 1, X[:, 1].max() + 1 xx_1, xx_2 = np.meshgrid(np.arange(x1_min, x1_max, h),</pre>
In [351	<pre>f, ax = plt.subplots(nrows=1, ncols=1, figsize=(5,5)) plt.contourf(xx_1, xx_2, Z, cmap=plt.cm.coolwarm, alpha=0.8) plt.scatter(X[:, 0], X[:, 1], c=y, cmap=plt.cm.coolwarm) plt.xlabel('X_1') plt.ylabel('X_2') plt.xlim(xx_1.min(), xx_1.max()) plt.ylim(xx_2.min(), xx_2.max()) plt.xticks(()) plt.yticks(())</pre> # DO NOT CHANGE
u ÷	<pre># Try to fit a linear classifier to the dataset svm_cls = svm.LinearSVC() svm_cls.fit(X_train, y_train) y_test_predicted = svm_cls.predict(X_test) print("Accuracy on test dataset: {}".format(accuracy_score(y_test, y_test_predicted))) visualize_decision_boundary(X_train, y_train) Accuracy on test dataset: 0.865</pre>
	X1
In [36]:	We can see that we need a non-linear boundary to be able to successfully classify data in this dataset. By mapping the current feature x to a higher space with more features, linear SVM could be performed on the features in the higher space to learn a non-linear decision boundary. In the function below add additional features which can help classify in the above dataset. After creating the additional features use code in the further cells to see how well the features perform on the test set. (Hint: Think of the shape of the decision boundary that would best separate the above points. What additional features could help map the linear boundary to the non-linear one? Look at this for a detailed analysis of doing the same for points separable with a circular boundary) def create_nl_feature(X): TODO - Create additional features and add it to the dataset
In [37]:	<pre>returns: X_new - (N, d + num_new_features) array with additional features added to X such that it can classify the points in the dataset. ''' # Delete this line when you implement the function # (x1, x2, exp(-((x1)^2+(x2)^2))) X_new = np.asarray((X[:,0], X[:,1], np.exp(-(X[:,0]**2 + X[:,1]**2)))).T return X_new # DO NOT CHANGE # Create new features</pre>
In [38]:	<pre>X_new = create_nl_feature(X) X_train, X_test, y_train, y_test = train_test_split(X_new, y,</pre>
	<pre>print("Accuracy on test dataset: {}".format(accuracy_score(y_test, y_test_predicted))) visualize_decision_boundary(X_train, y_train, create_nl_feature) Accuracy on test dataset: 0.93</pre>
In []:	X_{-1}

4.1 Fitting an SVM classifier by hand (20 Pts) **[W]**