

Signed Numbers

The rules for combining signed numbers are described below.

I. ADDITION

First, ask, "*do the numbers being added have the same sign?*"

If your answer is Yes, use rule 1.

If your answer is No, use rule 2.

Rule 1: When adding numbers with the same sign, add the numbers and keep the sign.

Rule 2: When adding numbers with different signs, subtract the smaller number from the larger number, and keep the sign of the larger number.

Example 1:
 $(+3) + (+7) = +10$

Example 2:
 $(-5) + (-9) = -14$

Example 3:
 $(-4) + (+2) = -2$

Example 4:
 $(+28) + (-5) = +23$

Note: The previous examples can also be written as follows:

Example 1:
 $3 + 7 = 10$

Example 2:
 $-5 - 9 = -14$

Example 3:
 $-4 + 2 = -2$

Example 4:
 $28 - 5 = 23$

Examples 1 and 2 used Rule 1.

Examples 3 and 4 used Rule 2.

How would you do the following problem?

Example 5: $(+21) + (-14) + (-15) + (+9)$

Using Rule 1, combine all the positives:	$(+21) + (+9) = +30$
Then combine all the negatives:	$(-14) + (-15) = -29$
Next, use Rule 2 to combine the sum of the positives and the sum of the negatives	$(+30) + (-29) = +1$

II. SUBTRACTION

Every subtraction problem of signed numbers is really an addition problem that follows these two rules:

Rule 1: Change the subtraction sign to an addition sign, and change the sign of the number that was being subtracted.

Rule 2: Use the addition rules to solve the problem.

Example 1:

$$(+75) - (+30) =$$

$$(+75) + (-30) = +45$$

Example 2:

$$(-58) - (-33) =$$

$$(-58) + (+33) = -25$$

Example 3:

$$(-39) - (+39) =$$

$$(-39) + (-39) = -78$$

Note: The previous examples can also be written as follows:

Example 1:

$$75 - 30 = 45$$

Example 2:

$$-58 + 33 = -25$$

Example 3:

$$-39 - 39 = -78$$

II. MULTIPLICATION AND DIVISION

Both Multiplication and Division have the same sign rules. Ask, "*do the numbers being multiplied or divided have the same sign?*"

If your answer is Yes, use Rule 1.

If your answer is No, use Rule 2.

Rule 1: When multiplying or dividing numbers with the same signs, the answer is always positive.

Rule 2: When multiplying or dividing numbers with different signs, the answer is always negative.

Example 1:

$$(-3) \cdot (-5) = +15$$

Example 2:

$$\frac{-24}{+6} = -4$$

Example 3:

$$\frac{-33}{-3} = +11$$

Example 4:

$$-(x + 1) = -x - 1$$

Example 5:

$$-(x - 1) = -x + 1$$

Whenever there is a negative sign in front of the parenthesis, the signs of **all** the terms on the inside becomes the opposite of what they are. See example 4 and 5.