

The Carnegie RR Lyrae Program: The Mid-Infrared RR Lyrae Period-Luminosity Relation in ω Cen [working title]

Meredith J. Durbin^{1,2*} Victoria Scowcroft³ Wendy Freedman⁴ Barry Madore³
 Rachael Beaton³ Gurtina Besla⁵ Giuseppe Bono^{6,7} Vittorio Braga^{6,7}
 Maria-Rosa Cioni^{8,9,10} Gisella Clementini¹¹ Kathryn Johnston¹² Nitya Kallivayalil¹³
 Juna Kollmeier³ David Law¹ Steve Majewski¹³ Roeland van der Marel¹
 Massimo Marengo¹⁴ Andrew J. Monson¹⁵ Jill Neeley¹⁴ David Nidever¹⁶
 Grzegorz Pietrzynski^{17,18} George Preston³ Mark Seibert³ Horace Smith¹⁹
 Igor Soszynski¹⁷ Andrzej Udalski¹⁷

¹ Space Telescope Science Institute, 3700 San Martin Drive, Baltimore, MD 21218, USA

² Pomona College, Claremont, CA 91711, USA

³ Observatories of the Carnegie Institution of Washington, 813 Santa Barbara St., Pasadena, CA 91101, USA

⁴ Department of Astronomy and Astrophysics, University of Chicago, 5640 S Ellis Ave, Chicago, IL 60637, USA

⁵ Department of Astronomy and Steward Observatory, University of Arizona, 933 North Cherry Avenue, Tucson, AZ 85721, USA

⁶ Univ. Roma “Tor Vergata”, Via della Ricerca Scientifica, 1 - 00133, Roma, Italy

⁷ INAF-OAR, via Frascati 33 - 00040, Monte Porzio Catone (RM), Italy

⁸ Universitat Potsdam, Institut für Physik und Astronomie, Karl-Liebknecht-Str. 24/25, 14476 Potsdam, Germany

⁹ Leibniz-Institut für Astrophysik Potsdam, An der Sternwarte 16, 14482 Potsdam, Germany

¹⁰ University of Hertfordshire, Physics, Astronomy and Mathematics, College Lane, Hatfield AL10 9AB, United Kingdom

¹¹ INAF - Osservatorio Astronomico, Via Ranzani n. 1, 40127 Bologna, Italy

¹² Department of Astronomy, Columbia University, New York, NY 10027, USA

¹³ Department of Astronomy, University of Virginia, Charlottesville, VA 22904-0818, USA

¹⁴ Department of Physics and Astronomy, Iowa State University, Ames, IA, USA

¹⁵ Department of Astronomy and Astrophysics, The Pennsylvania State University, 403 Davey Lab, University Park, PA, 16802, USA

¹⁶ Department of Astronomy, University of Michigan, Ann Arbor, MI 48109, USA

¹⁷ Warsaw University Observatory Al. Ujazdowskie 4, 00-478 Warszawa, Poland

¹⁸ Departamento de Astronomia, Universidad de Concepcion, Casilla 160-C, Chile

¹⁹ Department of Physics and Astronomy, Michigan State University, East Lansing, MI, USA 48824

Accepted XXX. Received YYY; in original form ZZZ

ABSTRACT

Something something metallicity

Key words: keyword1 - keyword2 - keyword3

1 INTRODUCTION

The Carnegie RR Lyrae Program (CRRP) is a Warm *Spitzer* program (Freedman et al. 2012a, PID 90002) with the aim of calibrating the mid-infrared (mid-IR) RR Lyrae period-luminosity (PL) relation. Similar to the Carnegie Hubble Program (CHP) (Freedman et al. 2011), which used mid-IR observations of Cepheids to measure the Hubble constant (H_0 Freedman et al. 2012b), the results of the CRRP will be used to provide an independent, population II

calibration of the zero-point of the extragalactic distance scale, and hence an independent measurement of H_0 .

In recent years it has become increasingly important to obtain independent direct measurements of H_0 . The results of Riess et al. (2011) and Freedman et al. (2012b), both which use Cepheids and type Ia supernovae (SNe), agree very well at 74.4 ± 2.5 km s^{−1} Mpc^{−1} and 74.3 ± 2.6 km s^{−1} Mpc^{−1}, respectively. However, when we consider the latest results from *Planck*, who find 67.48 ± 0.98 km s^{−1} Mpc^{−1} (Planck Collaboration et al. 2015), there is tension. The *Planck* study derives their measurement from a model of the cosmic microwave background (CMB), so is completely independent of the Riess et al. and Freedman et al. results.

* E-mail: mdurbin@stsci.edu

There have been several recent works that have investigated possible sources of uncertainty in the distance ladder that may contribute to the discrepancy between H_0 measurements. For example, [Rigault et al. \(2015\)](#) examine the differences in star formation rates in type Ia SNe host galaxies. They find that the intrinsic brightness of a SNe Ia may be affected by the local host environment; i.e. whether the SN occurs in a locally star forming or locally passive environment. [Efstathiou \(2014\)](#) reanalysed the Cepheid data from [Riess et al. \(2011\)](#), and found that different outlier rejection criteria lowered the resultant value of H_0 to $70.6 \pm 3.3 \text{ km s}^{-1} \text{ Mpc}^{-1}$, making it compatible with the value from *Planck*.

The CRRP assesses a systematic that was unreachable in the original CHP – the intrinsic accuracy of the mid-IR Cepheid standard candle distance scale when compared to the standard ruler distance scale of the CMB and Baryon Acoustic Oscillation (BAO) measurements. With only one “test candle” it was impossible to make any assessment of this accuracy. However, with two standard candles with similar precision we can make meaningful comparisons and assess their systematic accuracy.

RR Lyrae variables (hereafter RRL) are intrinsically fainter than Cepheids, and in the optical follow a much shallower, even horizontal, PL relation ([Catelan et al. 2004](#)). Determining an accurate distance to an RRL in the V band requires knowledge of its metallicity. However, [Longmore et al. \(1986\)](#) showed that the true power of RRL as distance indicators lies in the IR passbands. Several groups have been studying the populations of RRL in globular clusters and nearby dwarf spheroidal galaxies (e.g. [Garofalo et al. 2013](#); [Ordoñez et al. 2014](#); [Cusano et al. 2015](#); [Kains et al. 2015](#), and references therein), and *HST* parallaxes were obtained for several Galactic RRL calibrators ([Benedict et al. 2011](#)). **Should we assume people will understand “calibrator” in this context? It took me a while to pick up on it**

Distance measurements made in the mid-IR benefit from reduced extinction effects, where $A_{[3.6]}$ and $A_{[4.5]}$ are 16 to 20 times lower than A_V ([Cardelli et al. \(1989\)](#); [Indebetouw et al. \(2005\)](#)). Additionally, the precision of distances obtained from the RRL PL relation is increased. At the wavelengths observed by Warm *Spitzer* (3.6 and 4.5 μm) we do not see photospheric effects, but only the effects of temperature driving the pulsation; essentially, the mid-infrared light curve is tracing the change in radius of the star over a pulsation cycle. A by-product of this effect is that the intrinsic width of the RRL PL relation is also minimised in the mid-IR. The PL relation for pulsational variables can be thought of as a two-dimensional projection of the three-dimensional period-luminosity-colour relation (see figure 3 of [Madore & Freedman \(1991\)](#) for a graphical representation). As the colour-width decreases in the mid-IR, the width of the PL naturally decreases. As one moves from the optical to the mid-IR, the slope of the PL relation steepens and its dispersion dramatically decreases, and the slope should asymptotically approach the predicted slope of the period-radius relation, resulting in a slope between -2.4 and -2.8 , confirmed empirically by [Madore et al. \(2013\)](#). Through this decrease in dispersion we have found that the intrinsic width of the mid-IR PL for RRL is in fact smaller than for Cepheids – 0.05 mag compared to 0.10 mag ([Neeley et al. 2015](#)). This translates to an uncertainty on an individual RR Lyrae star of 2%, compared to 4% for Cepheids.

In this work we focus on the effects of metallicity on the RR Lyrae (RRL) PL relation. Several Galactic Globular Clusters are being observed as part of CRRP, but ω Cen is unique in that it exhibits a measurable spread in metallicity ([Freeman & Rodgers 1975](#); [Villanova et al. 2007, 2014](#)).

There are very few metallic or molecular transition lines in the

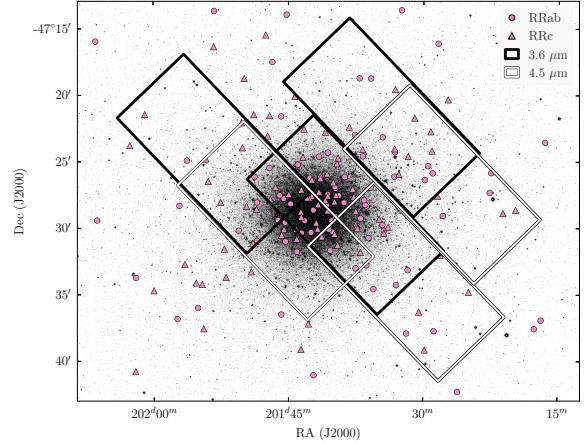


Figure 1. A K_s -band image of ω Cen from the FourStar camera, overlaid with a catalog of RRL from [Kaluzny et al. \(2004\)](#) and footprints of the *Spitzer* IRAC fields.

mid-IR at typical RRL temperatures, so the effects of metallicity on luminosity should be minimised. However, ω Cen provides the ideal test bed for any effect that we may not have predicted. Such an effect is not out of the realm of possibility; for example, the strength of the CO band head at 4.5 μm has been found to have a significant effect on Cepheid colours, and has such prevented the IRAC 4.5 μm Cepheid observations from being used for distance measurements in the CHP ([Scowcroft et al. 2011](#); [Monson et al. 2012](#); [Scowcroft et al. 2015](#)). As our concern in this program is systematic precision, we must ensure that similar effects do not plague the RRL distance scale.

The paper is set out as follows: Section 2 details the observations and data reduction. Section 3 presents the photometry of the ω Cen RRL. Section 4 describes the mid-IR PL relations and Section 5 discusses the application of these to a distance measurement of ω Cen. Section 6 examines the effects of metallicity on RRL magnitudes and distance estimates. Section 7 discusses the implications of this, and other systematic effects we consider in this work. In Section 8 we present our conclusions.

2 OBSERVATIONS & DATA REDUCTION

This work combines mid-IR observations from the Warm *Spitzer* mission, with supporting near-IR observations from the FourStar instrument on the Baade-Magellan telescope at Las Campanas Observatory ([Persson et al. 2013](#)). Figure 1 shows a K_s FourStar image with the *Spitzer* fields outlined, and the positions of known RRL plotted as circles.

2.1 Warm *Spitzer* Data

The Warm *Spitzer* observations for this work were taken as part of the Carnegie RR Lyrae Program. Three fields in ω Cen were chosen; their positions and the positions of known ω Cen RRLs are shown in Figure 1. To obtain optimal RRL light curves we observed each field 12 times over approximately 16 hours, roughly corresponding to the period of the longest period RRL we expected in the field.

The observations of all three fields were taken on 2013 May 10 and 2013 May 11. Each field was observed using *Spitzer* IRAC (Fazio et al. 2004) with a 30s frame time with a medium scale, gaussian 5-point dither pattern to mitigate any image artefacts. Images were collected in both the 3.6 and 4.5 μm channels. The elongated field shapes come from the design of IRAC; while the [3.6] channel is collecting on-target data, the [4.5] channel collects off target data “for free”, and vice versa. We chose to include these off-target fields to maximise the number of RRL in our final sample and to increase the legacy value of our data set to the community.

The science images were created using MOPEX (Makovoz et al. 2006), first running overlap correction on the basic calibrated data (cBCDs) then mosaicking them at 0.6 arcsec pixel scale using the drizzle algorithm. Mosaicked location-correction images were created at the same time.

PSF photometry was performed using DAOPHOT and ALLFRAME (Stetson 1987, 1994). The PSF model was created for each field/filter combination using the first epoch data. This was then applied to each other epoch. As the observations were taken temporally close together the effects of telescope rotation between epochs on the mosaicked PSF were minimal, so making a single good PSF model for each field/filter combination was much more efficient than creating one for every epoch.

Master star lists for ALLFRAME were created for each filter/field combination using a median mosaicked image created by MOPEX. We did not use the same single master star list for both filters as only a small proportion (1/3) of the 3.6 μm and 4.5 μm fields overlap each other. Instead we performed separate ALLFRAME reductions for each filter, and combined the results after the fact using DAOMATCH and DAOMASTER. Our mid-IR photometry is calibrated to the standard system set by Reach et al. (2005).

2.2 FourStar Data

J , H and K_s data were taken with the FourStar instrument on the Baade-Magellan telescope at Las Campanas Observatory (Persson et al. 2013) on the nights of 2013 June 25, 2013 June 27, and 2013 June 28. Four epochs were obtained each night in each filter for a total of 12 epochs. A mosaic of 5×3 (slightly overlapping) pointings (tiles) covered a 50×30 arcminute field of view centered on ω Cen. Each tile consists of a 5 point dither pattern with a 5.8 second exposure time. Stacked mosaics of the entire field were made as well as individual tiles using a customized pipeline for FourStar data. The purpose of the individual tiles is to provide photometry with better time resolution than the large mosaic.

PSF photometry of the tiles was performed using DAOPHOT and ALLFRAME (Stetson 1987, 1994). A PSF model was created for each epoch/tile/filter combination. A master star list for ALLFRAME was created from the final K_s mosaic and the multi-wavelength/epoch results were combined using DAOMATCH and DAOMASTER. Our final photometry is calibrated to the 2MASS standard system (Skrutskie et al. 2006).

2.3 Crowding

The primary limiting factor in the data is crowding: 77 RRLs out of the original catalog of 192 (Kaluzny et al. 2004) were rejected due to crowding. We compared the *Spitzer* images to the FourStar K_s -band image. The 0.159 arcsec/pixel resolution of the K_s band image enabled us to assess which stars were significantly contaminated. Our full, uncrowded RRL sample consists of 97 stars in J and H , 99 in K_s , 37 in 3.6 μm , and 43 in 4.5 μm .

Table 1. Theoretical near-IR RRL period-luminosity relation coefficients for ω Cen (Marconi et al. 2015), for relations of the form $M = a + b \times \log P + c \times [\text{Fe}/\text{H}]$ with predicted dispersion σ .

Band	Mode	a	b	c	σ
J	RRab	-0.510	-1.980	0.170	0.060
	RRc	-1.070	-2.460	0.150	0.040
H	RRab	-0.760	-2.240	0.190	0.040
	RRc	-1.310	-2.700	0.160	0.020
K_s	RRab	-0.820	-2.270	0.180	0.030
	RRc	-1.370	-2.720	0.150	0.020

3 RESULTS

Our final photometry catalog, including magnitudes and uncertainties for JHK_s , [3.6], and [4.5], is presented in Table ?? . The average magnitudes presented in Table ?? are flux averages, and the photometric uncertainties of the time series data are the error on the mean.

Our full, uncrowded RRL sample consists of 96 stars in J and H , 98 in K_s , 36 in [3.6], and 43 in [4.5]. For the PL fitting, detailed in the next section, we use only the stars for which we have photometry in all five bandpasses, ensuring that the same range of periods and metallicities are sampled for each wavelength. Our final RRL sample consists of 24 stars, or 12 in each pulsation mode.

4 PERIOD-LUMINOSITY RELATIONS

We use the theoretical near-infrared PL relation parameters presented in Marconi et al. (2015) for the JHK bands, and the empirical PL relation parameters derived from photometry of RRLs in the globular cluster M4 (NGC 6121) from Neeley et al. (2015) for the IRAC bands. With the use of preexisting PL relation coefficients, the distance modulus becomes the only free parameter in our fit. We fit all distance moduli using an unweighted least-squares method, and fit the distance modulus to each pulsation mode in each wavelength separately.

The JHK RRL PL relations are described in Table 1. The relations take the form

$$M = a + b \times \log P + c \times [\text{Fe}/\text{H}] \quad (1)$$

where a , b , and c are theoretically derived coefficients.

For the mid-IR we use the PL relations from Neeley et al. (2015), as described in Table 2. These relations take the form

$$M = a + b \times (\log(P) + P_0) \quad (2)$$

where a and b are empirically derived coefficients and P_0 is the absolute value of the logarithm of the mean period of the M4 RRL sample. We calculate the PL zero-points assuming Neeley et al.’s M4 distance modulus of $\mu = 11.399$ mag.

The theoretical PL relations for the near-IR have a metallicity-dependent term; however, we do not have known metallicities for all RRL in our sample. We therefore use the average $[\text{Fe}/\text{H}]$ of the RRLs for which there are known metallicities. Using spectroscopic metallicities from Sollima et al. (2006), we obtain an average $[\text{Fe}/\text{H}]$ of -1.567 . The effect of our choice of mean abundance is discussed further in Section 6.

Table 2. Empirical mid-IR RRL period-luminosity relation coefficients for ω Cen (Neeley et al. 2015), for relations of the form $M = a + b \times (\log(P) + P_0)$ with measured σ dispersion σ .

Band	Mode	a	b	P_0	σ
[3.6]	RRab	-0.558	-2.370	0.260	0.035
	RRc	-0.192	-2.658	0.550	0.021
[4.5]	RRab	-0.593	-2.355	0.260	0.036
	RRc	-0.240	-2.979	0.550	0.021

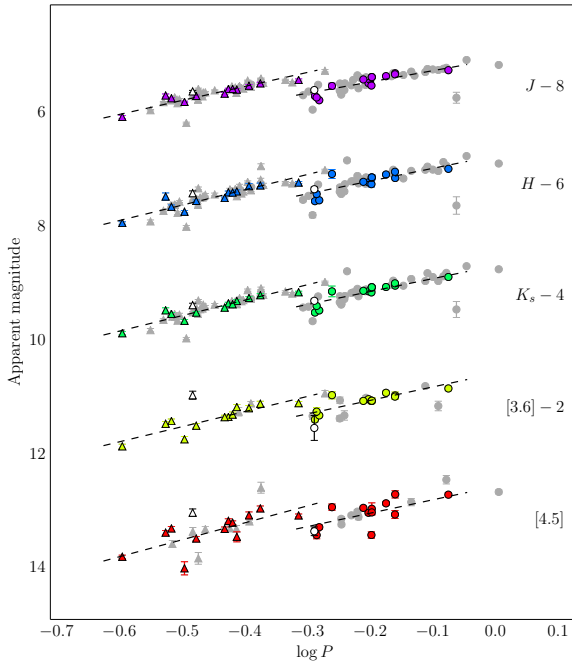


Figure 2. PL relations for JHK_s , [3.6], and [4.5] photometry assuming $[\text{Fe}/\text{H}] = -1.567$. Here circles represent RRab stars, triangles represent RRcs, colored points are the final consistent sample, grey points are stars that did not appear in all bands, and the unfilled points are stars rejected from the final sample based on 2σ clipping of the residuals of $3.6 \mu\text{m}$ vs. the residuals of H and K .

5 DISTANCE MODULI

We combine the uncorrected distance moduli from each bandpass to obtain a mean reddening-corrected distance modulus. We fit the near-infrared reddening law from Cardelli et al. (1989) and mid-infrared law from Indebetouw et al. (2005) simultaneously, assuming a ratio of total to selective absorption $R_V = 3.1$. The resulting fit is shown in Figure 3. We derive a dereddened distance modulus of $\langle \mu_0 \rangle = 13.781 \pm 0.018$ with $E(B - V) = 0.066 \pm 0.030$ using the weighted mean RRab + RRc distances.

It is apparent from Figure 3 that there are large discrepancies in the distance moduli in 3.6 and $4.5 \mu\text{m}$ for the two pulsation modes; these contribute to the relatively low $E(B - V)$ value and high dereddened distance modulus. If we remove the RRc's and fit the extinction curve only to the RRab's, as shown in Figure 4, we obtain a better fit of all points to the extinction curve than when we use the mean. From these distance moduli we derive a dereddened distance modulus of $\langle \mu_0 \rangle = 13.739 \pm 0.024$ with $E(B - V) = 0.110 \pm 0.042$,

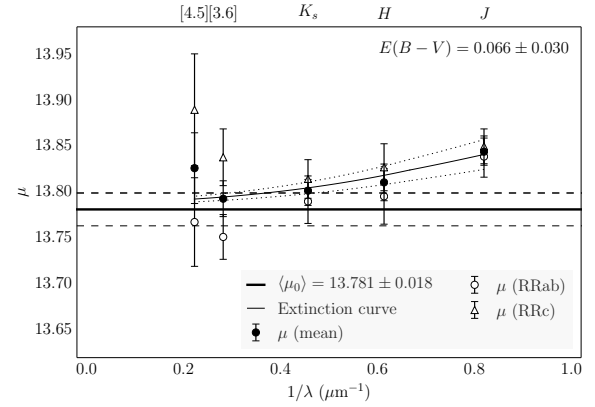


Figure 3. Distance moduli for the final sample of JHK_s , $3.6 \mu\text{m}$, and $4.5 \mu\text{m}$ photometry. The filled circles are the mean distance moduli using both RRab and RRc stars, the unfilled circles are the distance moduli using only RRab stars, and the filled triangles are distance moduli using only RRc stars. The reddening laws are fit to the mean distance moduli.

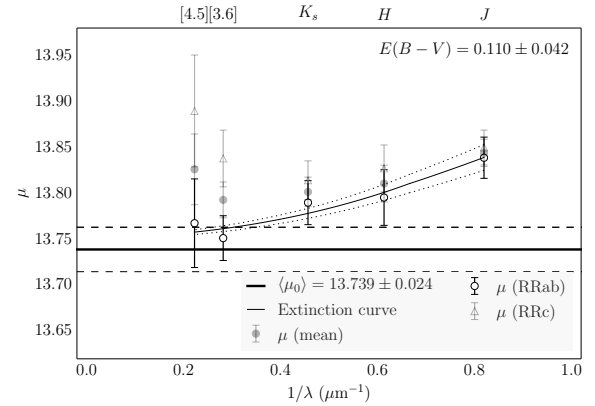


Figure 4. Distance moduli for the final sample of JHK_s , $3.6 \mu\text{m}$, and $4.5 \mu\text{m}$ photometry, with the reddening laws fit to the distances from RRab only.

both of which are closer to accepted values [CITE] than the values derived from the weighted mean distance moduli.

6 METALLICITY

ω Cen is ideal for examining the RRL period-luminosity-metallicity relation, because [is there a better canonical metallicity spread than the one Giuseppe sent us like 2 years ago] A metallicity spread this wide is not found in any other Galactic globular cluster. One of the advantages of using globular clusters to calibrate PL coefficients is that all stars in a cluster can be considered to be at the same distance from Earth. We can therefore assume that any dispersion in the PL relation is a combination of the a) the intrinsic dispersion of the PL relation, b) the photometric uncertainties, and c) dispersion induced by the spread in metallicity of the RRL. Since we have measured the intrinsic dispersion of the RRL PL from the cluster M4, Neeley et al. (2015) and our photometric uncertainties are well understood,

the only unknown in this problem is the dispersion due to the spread in metallicity of the cluster.

ω Cen is unique in that we can also take a second approach to establishing the metallicity effect on the RRL PL relation. As it is such an interesting system, ω Cen is extremely well studied and many of its RRL have spectroscopic or photometric metallicities in the literature (e.g. Sollima et al. 2006; Rey et al. 2000). As another test of the effect of metallicity, we use these measurements to assess the γ parameter for ω Cen, where

$$\gamma = \frac{\Delta \text{mag}}{[\text{Fe}/\text{H}]}, \quad (3)$$

similar to γ used to quantify the effect of metallicity on the zero-point of the Cepheid PL relation (Kennicutt et al. 1998).

Theoretical models suggest that the metallicity dependence of the RRL PL relation should decrease monotonically from the optical to the near-infrared (Bono et al. 2001; Catelan et al. 2004). Observational evidence corroborates this; previous investigations performed on WISE data suggest no obvious metallicity dependence in the mid-IR PL relations (Madore et al. 2013).

In the case of Cepheids, Scowcroft et al. (2011) and Scowcroft et al. (2015) have shown that in the $4.5 \mu\text{m}$ bandpass there is absorption due to a CO bandhead at $4.65 \mu\text{m}$, which strengthens the metallicity dependence of the PL relation in this bandpass. However, this effect is due to the low temperature of Cepheid atmospheres and disappears in the hottest, shortest-period Cepheids, as the CO dissociates at temperatures above 6000 K (Monson et al. 2012). As even the coolest RRL have temperatures over 6000 K (Iben 1971), we expect to see no such CO absorption in the $4.5 \mu\text{m}$ PL relation. If there are any other unanticipated metallicity effects, they must be smaller than the dispersion of the PL relations themselves.

If there is any correlation between $[\text{Fe}/\text{H}]$ and the PL residuals, we expect it to be a linear one, consistent with the theoretical metallicity terms in the PL relation, $c \times [\text{Fe}/\text{H}]$; we fit a relation of the form

$$\Delta \text{mag} = \gamma \times [\text{Fe}/\text{H}] + d \quad (4)$$

to the $3.6 \mu\text{m}$ and $4.5 \mu\text{m}$ PL residuals and metallicity values for stars with known individual metallicity values, as shown in Figure 6. We find that although the scatter in the $3.6 \mu\text{m}$ and $4.5 \mu\text{m}$ PL relations is higher for ω Cen than it is for M4 (Neeley et al. 2015; Braga et al. 2015), there is no evidence that it is due to metallicity. When we examine $[\text{Fe}/\text{H}]$ vs. $\Delta 3.6 \mu\text{m}$ and $\Delta 4.5 \mu\text{m}$, γ is within 1σ of zero for all fits, indicating that there is no significant metallicity dependence in the PL residuals.

7 DISCUSSION

8 CONCLUSIONS

Trigonometric parallaxes of Galactic RRLs from the *GAIA* mission will increase the number of calibrators for the absolute RRL PL relations by an order of magnitude [cite overview paper].

ACKNOWLEDGEMENTS

We thank Eric Persson for his many contributions to this project.

This work is based on observations made with the Spitzer Space Telescope, which is operated by the Jet Propulsion Laboratory, California Institute of Technology under a contract with

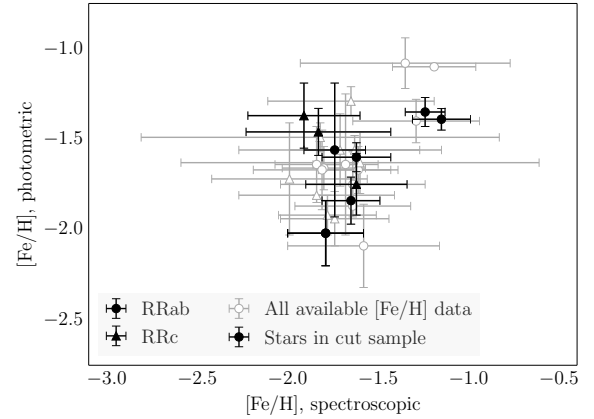


Figure 5. Spectroscopic vs. photometric measurements of $[\text{Fe}/\text{H}]$ for RRLs in ω Cen.

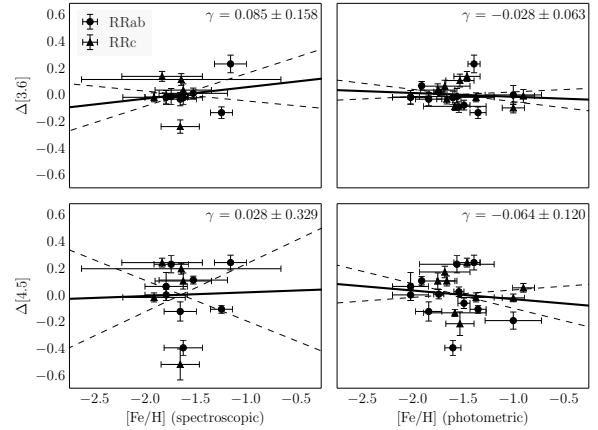


Figure 6. Photometric and spectroscopic $[\text{Fe}/\text{H}]$ values vs. period-luminosity residuals in $3.6 \mu\text{m}$ and $4.5 \mu\text{m}$, with the γ parameter from equation 4 in the top right corner of each subplot.

NASA. Support for this work was provided by NASA through an award issued by JPL/Caltech.

This publication makes use of data products from the Two Micron All Sky Survey, which is a joint project of the University of Massachusetts and the Infrared Processing and Analysis Center/California Institute of Technology, funded by the National Aeronautics and Space Administration and the National Science Foundation.

This research has made use of the NASA/IPAC Extragalactic Database (NED), which is operated by the Jet Propulsion Laboratory, California Institute of Technology, under contract with the National Aeronautics and Space Administration.

REFERENCES

- Benedict G. F., et al., 2011, *AJ*, **142**, 187
- Bono G., Caputo F., Castellani V., Marconi M., Storm J., 2001, *MNRAS*, **326**, 1183
- Braga V. F., et al., 2015, *ApJ*, **799**, 165
- Cardelli J. A., Clayton G. C., Mathis J. S., 1989, *ApJ*, **345**, 245

- Catelan M., Pritzl B. J., Smith H. A., 2004, *ApJS*, **154**, 633
- Cusano F., et al., 2015, *ApJ*, **806**, 200
- Efstathiou G., 2014, *MNRAS*, **440**, 1138
- Fazio G. G., et al., 2004, *ApJS*, **154**, 10
- Freedman W. L., et al., 2011, *AJ*, **142**, 192
- Freedman W., et al., 2012a, The Carnegie RR Lyrae Program, Spitzer Proposal
- Freedman W. L., Madore B. F., Scowcroft V., Burns C., Monson A., Persson S. E., Seibert M., Rigby J., 2012b, *ApJ*, **758**, 24
- Freeman K. C., Rodgers A. W., 1975, *ApJ*, **201**, L71
- Garofalo A., et al., 2013, *ApJ*, **767**, 62
- Iben Jr. I., 1971, *PASP*, **83**, 697
- Indebetouw R., et al., 2005, *ApJ*, **619**, 931
- Kains N., et al., 2015, *A&A*, **578**, A128
- Kaluzny J., Olech A., Thompson I. B., Pych W., Krzemiński W., Schwarzenberg-Czerney A., 2004, *A&A*, **424**, 1101
- Kennicutt Jr. R. C., et al., 1998, *ApJ*, **498**, 181
- Longmore A. J., Fernley J. A., Jameson R. F., 1986, *MNRAS*, **220**, 279
- Madore B. F., Freedman W. L., 1991, *PASP*, **103**, 933
- Madore B. F., et al., 2013, *ApJ*, **776**, 135
- Makovoz D., Roby T., Khan I., Booth H., 2006, in Society of Photo-Optical Instrumentation Engineers (SPIE) Conference Series. p. 0, doi:10.1117/12.672536
- Marconi M., et al., 2015, *ApJ*, **808**, 50
- Monson A. J., Freedman W. L., Madore B. F., Persson S. E., Scowcroft V., Seibert M., Rigby J. R., 2012, *ApJ*, **759**, 146
- Neeley J. R., et al., 2015, preprint, ([arXiv:1505.07858](https://arxiv.org/abs/1505.07858))
- Ordoñez A. J., Yang S.-C., Sarajedini A., 2014, *ApJ*, **786**, 147
- Persson S. E., et al., 2013, *PASP*, **125**, 654
- Planck Collaboration et al., 2015, preprint, ([arXiv:1502.01589](https://arxiv.org/abs/1502.01589))
- Reach W. T., et al., 2005, *PASP*, **117**, 978
- Rey S.-C., Lee Y.-W., Joo J.-M., Walker A., Baird S., 2000, *AJ*, **119**, 1824
- Riess A. G., et al., 2011, *ApJ*, **730**, 119
- Rigault M., et al., 2015, *ApJ*, **802**, 20
- Scowcroft V., Freedman W. L., Madore B. F., Monson A. J., Persson S. E., Seibert M., Rigby J. R., Sturch L., 2011, *ApJ*, **743**, 76
- Scowcroft V., Freedman W. L., Madore B. F., Monson A., Persson S. E., Rich J., Seibert M., Rigby J. R., 2015, preprint, ([arXiv:1502.06995](https://arxiv.org/abs/1502.06995))
- Skrutskie M. F., et al., 2006, *AJ*, **131**, 1163
- Sollima A., Borissova J., Catelan M., Smith H. A., Minniti D., Cacciari C., Ferraro F. R., 2006, *ApJ*, **640**, L43
- Stetson P. B., 1987, *PASP*, **99**, 191
- Stetson P. B., 1994, *PASP*, **106**, 250
- Villanova S., et al., 2007, *ApJ*, **663**, 296
- Villanova S., Geisler D., Gratton R. G., Cassisi S., 2014, *ApJ*, **791**, 107

This paper has been typeset from a \LaTeX file prepared by the author.