

# The Carnegie RR Lyrae Program: The Mid-Infrared RR Lyrae Period-Luminosity-Metallicity Relations in $\omega$ Cen

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Accepted XXX. Received YYY; in original form ZZZ

## ABSTRACT

**Key words:** keyword1 - keyword2 - keyword3

## 1 INTRODUCTION

$\omega$  Centauri (NGC 5139) is one of the most well-studied Galactic globular clusters

Although observing RRL at mid-IR wavelengths dramatically reduces the effects of reddening and extinction, the consequences of this shift to longer wavelengths on other parameters in the empirical RRL PL relation are yet to be determined; a particularly contested factor is the effect of metallicity. Both theory and observation have demonstrated that the position of the horizontal branch in the optical colour-magnitude diagram is dependent on metallicity (e.g. Marconi et al. 2015; Catelan et al. 2004; Bono et al. 2003; Nemec et al. 1994). However, the size of the metallicity contribution in the infrared PL relation is yet to be settled in the literature, either from a theoretical or empirical standpoint.

The most in-depth study of the effect of metallicity on the mid-IR PL relation to date comes from Dambis et al. (2014, 2015), who used the ALLWISE data release (Wright et al. 2010; Cutri et al. 2013) to examine possible changes in the RRL PL relation in globular clusters with different metallicities. They found a moderate dependence of the [W1] (approximately equivalent to *Spitzer* [3.6]) PL relation with [Fe/H] of  $\gamma_{W1} = 0.102 \text{ mag dex}^{-1}$ , slightly larger than their value for the near-IR, and approximately half that of the optical dependence ( $\gamma_K = 0.088 \text{ mag dex}^{-1}$ ,  $\gamma_V = 0.232 \text{ mag dex}^{-1}$ ). The observational work of Muraveva et al. (2015) appears to confirm this result, favouring a low value of  $\gamma_K$  for Milky Way and LMC RRL. However, the empirical study of Karczmarek et al. (2015) considers near-IR observations of RRL in the Carina dwarf Spheroidal (dSph) galaxy, this time testing different PL relations with a range of metallicity coefficients. Their results favour a larger value for  $\gamma_K$  than Dambis et al. (2015), with average values

of  $\gamma_K \approx 0.18 \text{ mag dex}^{-1}$ . This is consistent with the theoretical models by Marconi et al. (2015), who find that the metallicity dependence of the infrared PL relation is just as large as at optical wavelengths.

In this work we focus on the effects of metallicity on the RRL PL relation in the mid-IR using  $\omega$  Cen as a test case.  $\omega$  Cen is unique in that it exhibits a measurable spread in metallicity, with the most recent results estimating  $0.8 \leq \Delta [\text{Fe}/\text{H}] \leq 1.4 \text{ dex}$  (Villanova et al. 2014; Marino et al. 2012; Johnson & Pilachowski 2010). This makes  $\omega$  Cen the ideal site for a metallicity study, as all the RRL can be considered to be at the same distance, leaving the metallicities of the individual stars as the only free parameter.  $\omega$  Cen has been used previously for such studies, ranging from empirical tests in the optical (e.g. Olech et al. 2003; Lee 1991) and near-IR (e.g. Cacciari et al. 2006; Del Principe et al. 2006), to semi-empirical tests using population synthesis techniques (Tailo et al. 2016). Our study is unique as it is the first study to use  $\omega$  Cen to empirically measure the metallicity effect on the mid-IR RRL PL relation using metallicities of individual stars.

This work is part of the Carnegie RR Lyrae Program (CRRP), a *Spitzer* program (Freedman et al. 2012a, PID 90002) which aims to provide an independent, population II measurement of the Hubble constant ( $H_0$ ), tied to RR Lyrae variables with high precision geometric distances in the Milky Way. Similar to the Carnegie Hubble Program (CHP Freedman et al. 2011), CRRP will provide a single instrument measurement of  $H_0$ . It will provide important constraints on the external accuracy of the standard candle distance ladder, and the internal consistency of the distance measurements of Cepheids and RR Lyrae variables.

The paper is set out as follows: Section 2 details the observations and data reduction. Section 3 presents the photometry of the  $\omega$  Cen RRL. Section 4 describes the mid-IR

PL relations and Section 5 discusses the application of these to a distance measurement of  $\omega$  Cen. Section 6 examines the effects of metallicity on RRL magnitudes and distance estimates. Section 7 discusses the implications of this, and other systematic effects we consider in this work. In Section 8 we present our conclusions.

## 2 OBSERVATIONS & DATA REDUCTION

This work combines mid-IR observations from the *Spitzer* program [Freedman et al. \(2012a, PID 90002\)](#) with supporting near-IR observations from the FourStar instrument ([Persson et al. 2013](#)) on the Baade-Magellan telescope at Las Campanas Observatory. Figure 1 shows a  $K_s$ -band FourStar image with the *Spitzer* fields outlined, and the positions of known RRL from [Kaluzny et al. \(2004\)](#) indicated by circles (fundamental mode, R<sub>Rab</sub>) or triangles (first overtone, R<sub>Rc</sub>).

### 2.1 *Spitzer* Data

The *Spitzer* observations for this work were taken as part of the CRRP. Three fields in  $\omega$  Cen were chosen; their positions are shown in Figure 1. To obtain optimal RRL light curves we observed each field 12 times over approximately 16 hours (0.67 days), roughly corresponding to the longest period RRL we expected in the field and ensuring full phase coverage of all RRL. The observations of all three fields were taken on 2013 May 10 and 2013 May 11. Each field was observed using the *Spitzer* InfraRed Array Camera (IRAC) ([Fazio et al. 2004](#)) with a 30 s frame time with a medium scale, gaussian 5-point dither pattern to mitigate any image artefacts. Images were collected in both the 3.6 and 4.5  $\mu$ m channels. The elongated field shapes come from the design of IRAC; while the [3.6] channel is collecting on-target data, the [4.5] channel collects off target data “for free”, and vice versa. We chose to include these off-target fields to maximise the number of RRL in our final sample and to increase the legacy value of our data set to the community.

The science images were created using MOPEX ([Makovoz et al. 2006](#)), first running overlap correction on the corrected basic calibrated data frames (cBCDs) then mosaicking them at 0.6 arcsec pixel scale using the drizzle algorithm. Mosaicked location-correction images were created at the same time.

PSF photometry was performed on the mosaicked images using DAOPHOT and ALLFRAME ([Stetson 1987, 1994](#)). The PSF model was created for each field/filter combination using the first epoch data and was applied to every epoch. As the observations were taken temporally close together the effects of telescope rotation between epochs on the mosaicked PSF were minimal, so making a single good PSF model for each field/filter combination proved to be more efficient and just as accurate as creating one for every epoch.

Master star lists for ALLFRAME were created for each filter/field combination using a median mosaicked image created by MOPEX. We did not use the same single master star list for both filters as only a small proportion (1/3) of the [3.6] and [4.5] fields overlap each other. Instead we performed separate ALLFRAME reductions for each filter, and combined

the results after the fact using DAOMATCH and DAOMASTER. Our mid-IR photometry is calibrated to the standard system set by [Reach et al. \(2005\)](#).

### 2.2 FourStar Data

$J$ ,  $H$  and  $K_s$  data were taken with the FourStar instrument on the Baade-Magellan telescope at Las Campanas Observatory ([Persson et al. 2013](#)) on the nights of 2013 June 25, 2013 June 27, and 2013 June 28. Four epochs were obtained each night in each filter for a total of 12 epochs. A mosaic of  $5 \times 3$  slightly overlapping pointings (tiles), each with FourStar’s native  $10.9 \times 10.9$  arcminute field of view, covered a  $50 \times 30$  arcminute field of view centred on  $\omega$  Cen. Each tile consists of a 5 point dither pattern with a 5.8 second exposure time. Stacked mosaics of the entire field were made as well as individual tiles using a customised pipeline for FourStar data. The purpose of the individual tiles is to provide photometry with better time resolution than the large mosaic.

PSF photometry of the tiles was performed using DAOPHOT and ALLFRAME ([Stetson 1987, 1994](#)). A PSF model was created for each epoch/tile/filter combination. A master star list for ALLFRAME was created from the final  $K_s$  mosaic and the multi-wavelength/epoch results were combined using DAOMATCH and DAOMASTER. Our final photometry is calibrated to the 2MASS standard system ([Skrutskie et al. 2006](#)).

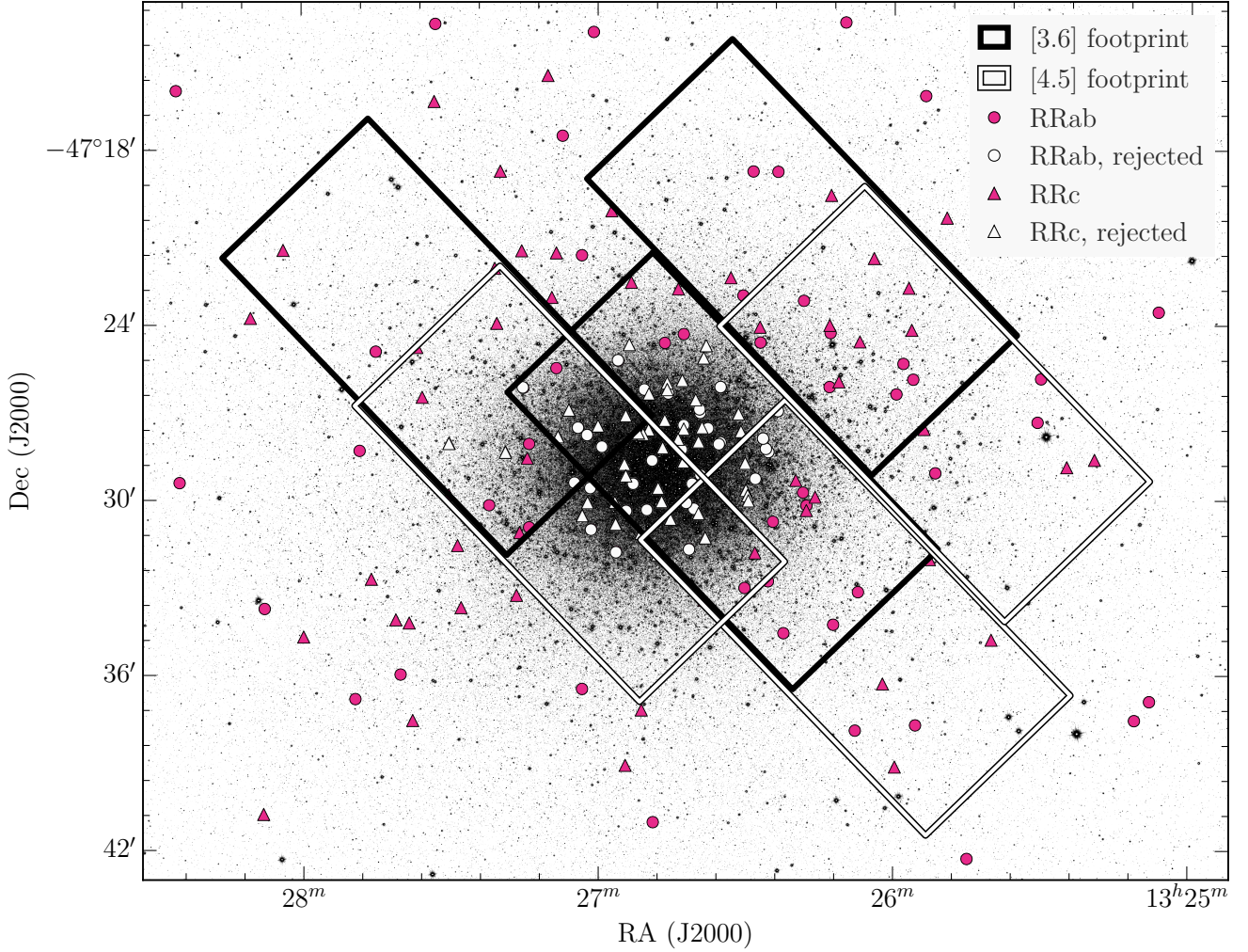
### 2.3 Crowding

The primary limiting factor in the photometric precision is crowding. To assess crowding for individual RRLs, we compared the *Spitzer* images to the higher resolution FourStar  $K_s$ -band image. The 0.159 arcsec/pixel scale of the  $K_s$ -band image compared to the 0.6 arcsec/pixel scale of the IRAC images enabled us to more accurately determine which stars were significantly contaminated. RRL were determined to be contaminated if there were one or more resolved stars in the  $K_s$ -band image within a 3.6 arcsecond (6 resampled IRAC pixels) radius of the RRL. 77 RRLs out of the original [Kaluzny et al. \(2004\)](#) catalog of 192 were rejected due to crowding. Another 13 were outside the FourStar mosaic field of view, and four more were found to be unusable due to other image artefacts.

## 3 RESULTS

Our final photometry catalog, including magnitudes and uncertainties for  $JHK_s$ , [3.6], and [4.5], is presented in Table A1. The average magnitudes presented in Table A1 are flux averages, and the photometric uncertainties of the time series data are the error on the mean. **Note: this will not be an appendix in the final draft, we’re just putting it there for now because it’s huge.**

Our full, uncrowded RRL sample consists of 96 stars in  $J$  and  $H$ , 98 in  $K_s$ , 38 in [3.6], and 42 in [4.5]; the small number of RRL in the IRAC bands compared to the FourStar bands is due to the smaller coverage of the IRAC pointings (see Figure 1) and crowding effects due to IRAC’s lower resolution. For the PL fitting, detailed in Section 4, we use



**Figure 1.** A  $K_s$ -band image of  $\omega$  Cen from the FourStar camera, overlaid with a catalog of RRL from Kaluzny et al. (2004) and footprints of the *Spitzer* IRAC fields. The circular points are RRab's and the triangular points are RRC's; we adopt this convention throughout the paper. The three black rectangle outlines are the IRAC field of view for each pointing in the  $3.6\ \mu\text{m}$  channel, and the white rectangle outlines show the same for  $4.5\ \mu\text{m}$ .

only the stars for which we have photometry in all five band-passes, ensuring that the same range of periods and metallicities are sampled for each wavelength. This helps to reduce any biases that may be introduced by non-uniform sampling in the distance moduli fits in Section 5. Our final RRL sample consists of 24 stars, with 12 each of RRab's and RRC's.

#### 4 PERIOD-LUMINOSITY RELATIONS

We fit PL relations using the theoretical near-infrared PL relation parameters presented in Marconi et al. (2015) for the  $JHK_s$  bands, and the empirical PL relation parameters derived from photometry of RRLs in the globular cluster M4 (NGC 6121) from Neeley et al. (2015) for the IRAC bands. With the use of preexisting PL relation coefficients, the distance modulus becomes the only free parameter in our fit. We fit all distance moduli using an unweighted least-squares method, and fit the distance modulus to each pulsation mode in each wavelength separately. We also refine

the fit by sigma-clipping the residuals of the  $[3.6]$  fit at a  $2\sigma$  level, resulting in the rejection of two more stars.

For the mid-IR we use the PL relations from Neeley et al. (2015), as described in Table 1. These relations take the form

$$M = a + b \times (\log(P) - \log(P_0)) \quad (1)$$

where  $a$  and  $b$  are empirically derived coefficients and  $P_0$  is the absolute value of the logarithm of the mean period of the M4 RRL sample. We calculate the absolute PL zero-points,  $a$ , by adopting Neeley et al.'s M4 distance modulus of  $\mu = 11.399$  mag.

The  $JHK_s$  RRL PL relations are described in Table 2. The relations take the form

$$M = a + b \times \log P + c \times [\text{Fe}/\text{H}] \quad (2)$$

where  $a$ ,  $b$ , and  $c$  are theoretically derived coefficients.

The theoretical PL relations for the near-IR have a metallicity-dependent term; however, we do not have empirically measured metallicities for all RRL in our sample.



**Table 1.** Empirical mid-IR RRL period-luminosity relation coefficients (Neeley et al. 2015), for relations of the form  $M = a + b \times (\log(P) - \log(P_0))$  (Eqn. 1) with observed dispersion  $\sigma$ . These relations are derived from RRL in the globular cluster M4.

Band	Mode	$a$	$b$	$\log P_0$	$\sigma$
[3.6]	RRab	-0.558	-2.370	-0.260	0.040
	RRc	-0.192	-2.658	-0.550	0.079
[4.5]	RRab	-0.593	-2.355	-0.260	0.045
	RRc	-0.240	-2.979	-0.550	0.057

**Table 2.** Theoretical near-IR RRL period-luminosity relation coefficients (Marconi et al. 2015), for relations of the form  $M = a + b \times \log P + c \times [\text{Fe}/\text{H}]$  (Eqn. 2) with modeled dispersion  $\sigma$ .

Band	Mode	$a$	$b$	$c$	$\sigma$
$J$	RRab	-0.51	-1.98	0.17	0.06
	RRc	-1.07	-2.46	0.15	0.04
$H$	RRab	-0.76	-2.24	0.19	0.04
	RRc	-1.31	-2.70	0.16	0.02
$K_s$	RRab	-0.82	-2.27	0.18	0.03
	RRc	-1.37	-2.72	0.15	0.02

We therefore take the mean  $[\text{Fe}/\text{H}]$  of all 74 RRLs in Sollima et al. (2006), obtaining a mean  $[\text{Fe}/\text{H}]$  value of  $-1.677$ . The distribution of the  $[\text{Fe}/\text{H}]$  values for the  $\omega$  Cen RRL are shown in Figure 2, for both the spectroscopic measurements by Sollima et al. (2006) and the photometric determinations by Rey et al. (2000). The light blue shaded histograms indicate the full sample of stars for each catalogue, with the darker blue histograms denoting those in our sample. Figure 2 demonstrates that our sample of RRL is a representative sample of the metallicity distribution of the RRL in  $\omega$  Cen.

The fitted PL relations for all five bands are shown in Figure 3. Coloured points (purple, blue, green, yellow, red) represent the  $J$ ,  $H$ ,  $K_s$ , [3.6], and [4.5] data that was included in the PL fits. Grey points represent stars that were excluded from the fits due to a lack of data in all bands; this ensured that the fits are done with a uniform sampling of all periods and metallicities. The two white points indicate stars which were rejected after the sigma clipping procedure described above. The distance moduli derived from these PL fits, uncorrected for extinction, are given in Table 3.

## 5 DISTANCE MODULI

We combine the uncorrected distance moduli from each bandpass to obtain a mean reddening value and reddening-corrected distance modulus. We fit the near-infrared reddening law from Cardelli et al. (1989) to the  $JHK_s$  data and the mid-infrared law from Indebetouw et al. (2005) to [3.6] and [4.5] simultaneously, assuming a ratio of total to selective absorption  $R_V = 3.1$ . The resulting fit is shown in Figure 4. We derive a mean dereddened distance modulus of  $\langle \mu_0 \rangle = 13.789 \pm 0.018$  with  $E(B - V) = 0.084 \pm 0.030$  using the weighted mean RRab + RRc distance moduli. The in-

dividual uncorrected distance moduli  $\mu$ , corrected distance moduli  $\mu_0$ , and PL residuals are shown in Table 3.

It is apparent from Figure 4 that there are large discrepancies in the distance moduli in [3.6] and [4.5] for the two pulsation modes; these discrepancies contribute to the relatively low  $E(B - V)$  value and high dereddened distance modulus compared to previously determined values (e.g. Lub 2002; Del Principe et al. 2006). If we remove the RRc's and fit the extinction curve only to the RRab's, as shown in Figure 5, we obtain a better fit of all points to the extinction curve than when we use the mean. From these distance moduli we derive a dereddened distance modulus of  $\langle \mu_0 \rangle = 13.743 \pm 0.026$  with  $E(B - V) = 0.138 \pm 0.044$ , both of which are closer to accepted values than the values derived from the weighted mean distance moduli. All individual corrected distance moduli from this fit are shown in Table 4.

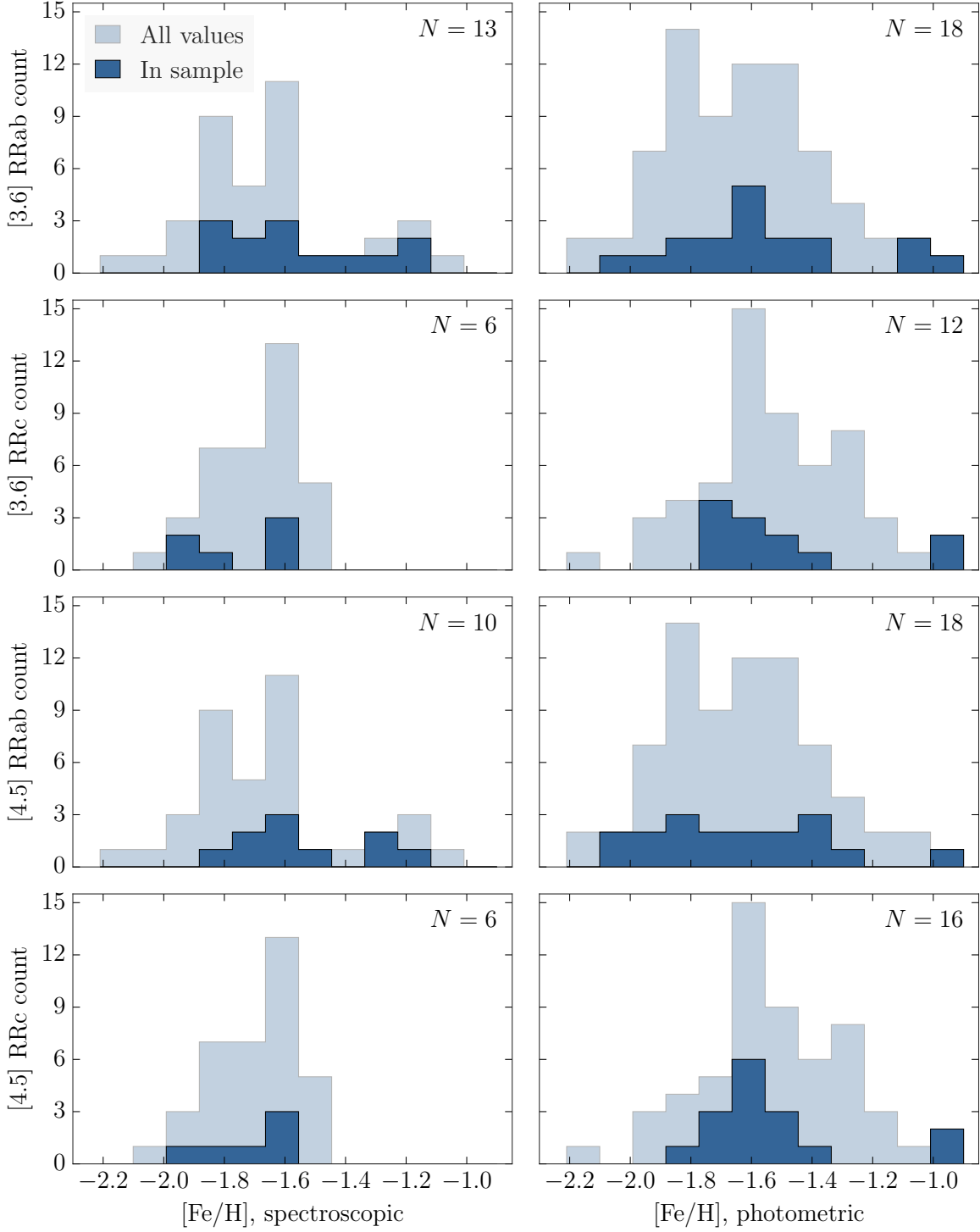
Given the large errors in the [4.5] distance moduli, we also fit the extinction curve to the  $JHK_s$  and [3.6] distances only, excluding [4.5] entirely; this was found to have a negligible effect on the final derived distance modulus and reddening for both the mean and RRab-only measurements.

## 6 METALLICITY

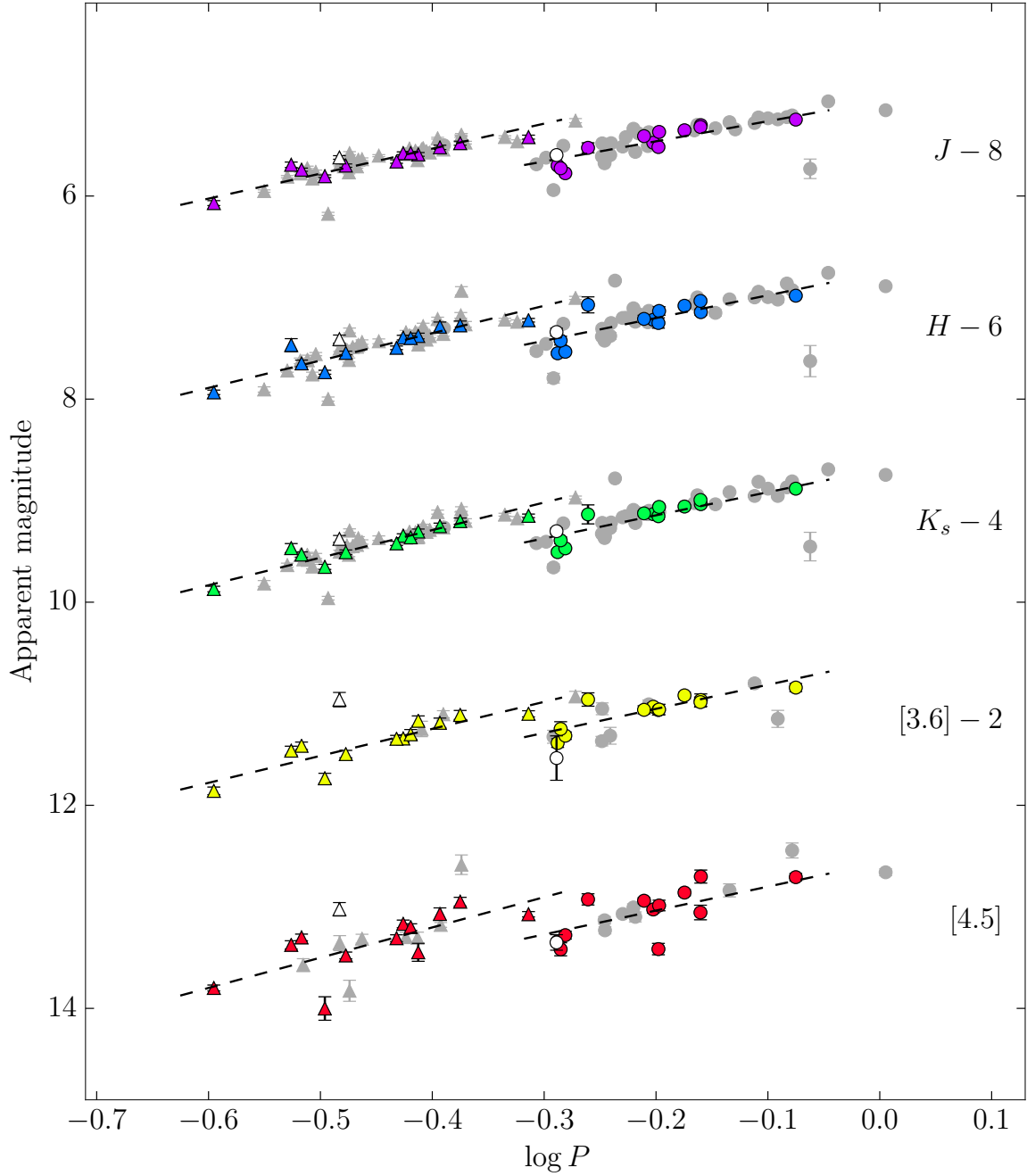
In principle, moving from the optical to the mid-infrared in uncrowded systems should bring the advantage of a steeper PL relation with decreased dispersion. However, theoretical works suggest that the metallicity coefficient in the infrared PL relations should be comparable to the metallicity coefficient at optical wavelengths (Bono et al. 2001; Catelan et al. 2004; Marconi et al. 2015).  $\omega$  Cen is ideal for assessing the contribution of metallicity to the mid-IR RRL PL relation, because it is known to have a large spread in metallicity ( $0.8 \leq \Delta [\text{Fe}/\text{H}] \leq 1.4$  dex Villanova et al. 2014; Marino et al. 2012; Johnson & Pilachowski 2010). A metallicity spread this wide is not found in any other Galactic globular cluster.

One of the advantages of using globular clusters to calibrate PL coefficients is that all stars in a cluster can be considered to be at the same distance. The dispersion in the PL relation is a combination of the a) the intrinsic dispersion of the PL relation, b) the photometric uncertainties, and c) dispersion induced by other complicating factors such as the spread in metallicity. Since we have a measured “intrinsic” dispersion of the RRL PL in [3.6] and [4.5] from the cluster M4 (Neeley et al. 2015) and the photometric uncertainties are well understood, we can isolate the remaining scatter due to astrophysical sources such as metallicity.

It has been shown with mid-IR spectra that a significant CO feature sits within the IRAC [4.5] filter. In the case of Cepheids, Scowcroft et al. (2016) have shown that this has a significant effect on the [4.5] magnitudes, and is metallicity dependent. However, this effect decreases with increasing temperatures, turning off completely above 6000 K where all the CO has been destroyed (Scowcroft et al. 2016). As even the coolest RRL have temperatures over 6000 K (Iben 1971), we expect to see no such CO absorption affecting the [4.5] PL relation, nor do we expect any other temperature dependent (hence period dependent) metallicity effects. However, we can directly and empirically test this prediction.



**Figure 2.** Histograms of spectroscopic (Sollima et al. 2006, left column) and photometric (Rey et al. 2000, right column) [Fe/H] values for R/Rab (top row) and R/Rc (bottom row). The light blue histograms represent all known metallicity values for each type, and the dark blue are the metallicity values for our final RRL sample in each passband. The number  $N$  at the top right corner of each subplot is the number of stars in our final sample that have known metallicity values for the given type, wavelength, and metallicity catalog.



**Figure 3.** PL relations for  $JHK_s$ ,  $[3.6]$ , and  $[4.5]$  photometry assuming  $[\text{Fe}/\text{H}] = -1.677$ . Here circles represent RRab stars and triangles represent RRc's. Coloured points are the final consistent sample with photometry in all 5 wavebands that are used for PL fitting. Grey points are stars that did not appear in all bands and are not used for PL fitting. The unfilled points are stars rejected from the final sample based on  $2\sigma$  clipping of the PL residuals in  $[3.6]$ , where sigma clipping was performed only on the consistent sample.

### 6.1 Metallicity Contribution to the Overall Dispersion

We can place an upper limit on the contribution of metallicity to the  $\omega$  Cen PL dispersion using the known variances of the individual components: the observed distribution of  $\omega$  Cen PL residuals  $\sigma_{\text{observed}}^2$ , the intrinsic PL width  $\sigma_{\text{intrinsic}}^2$ , and the dispersion induced by photometric error  $\sigma_{\text{phot}}^2$ . The

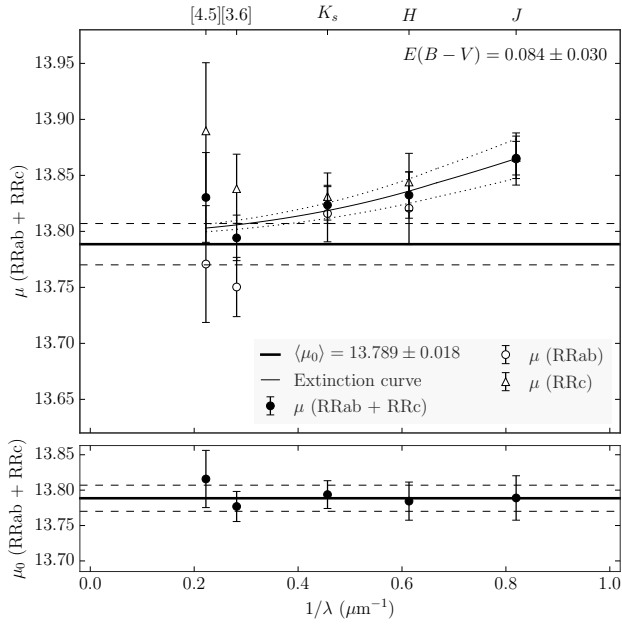
dispersion contributed by metallicity can therefore be constrained as follows:

$$\sigma_{[\text{Fe}/\text{H}]} \leq \sqrt{\sigma_{\text{observed}}^2 - \sigma_{\text{intrinsic}}^2 - \sigma_{\text{phot}}^2} \quad (3)$$

The calculated  $\sigma_{[\text{Fe}/\text{H}]}$  values for all IRAC PL relations are shown in Table 5, along with  $\sigma_{\text{observed}}$  and the other scatter components.

**Table 3.** Uncorrected distance moduli  $\mu$ , corrected distance moduli  $\mu_0$ , and the measured PL dispersion  $\sigma$  for all wavelengths and pulsation modes. The corrected distance moduli  $\mu_0$  are equal to  $\mu - A_\lambda A_V$ , where  $A_V$  is derived from fitting the reddening laws to the mean distance moduli.

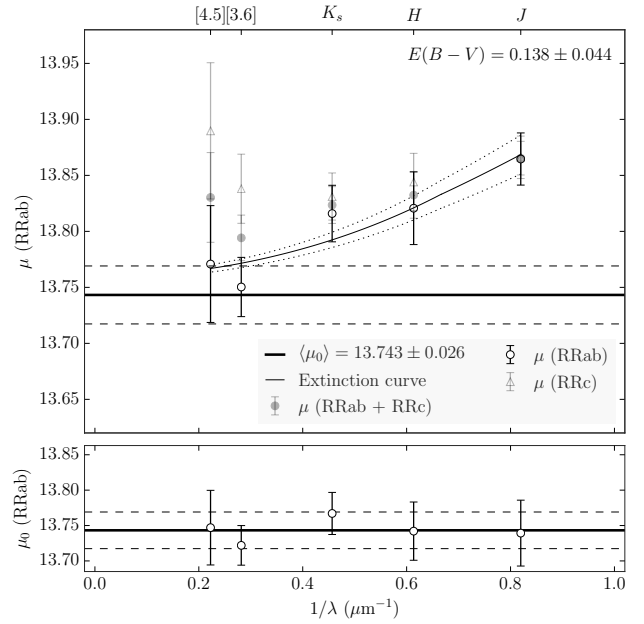
Band	$\mu$ , RRab	$\mu$ , RRc	$\mu$ , RRab + RRc	$\mu_0$ , RRab	$\mu_0$ , RRc	$\mu_0$ , RRab + RRc	$\sigma_{\text{PL}}$ , RRab	$\sigma_{\text{PL}}$ , RRc
<i>J</i>	$13.865 \pm 0.023$	$13.866 \pm 0.019$	$13.865 \pm 0.015$	$13.788 \pm 0.036$	$13.790 \pm 0.033$	$13.789 \pm 0.031$	0.127	0.082
<i>H</i>	$13.821 \pm 0.032$	$13.844 \pm 0.026$	$13.832 \pm 0.021$	$13.773 \pm 0.037$	$13.796 \pm 0.031$	$13.784 \pm 0.027$	0.170	0.107
<i>K_s</i>	$13.816 \pm 0.025$	$13.831 \pm 0.021$	$13.824 \pm 0.016$	$13.786 \pm 0.027$	$13.801 \pm 0.024$	$13.794 \pm 0.020$	0.147	0.089
[3.6]	$13.750 \pm 0.026$	$13.838 \pm 0.031$	$13.794 \pm 0.020$	$13.733 \pm 0.027$	$13.821 \pm 0.031$	$13.777 \pm 0.021$	0.124	0.096
[4.5]	$13.771 \pm 0.052$	$13.890 \pm 0.061$	$13.830 \pm 0.040$	$13.756 \pm 0.052$	$13.875 \pm 0.061$	$13.816 \pm 0.040$	0.154	0.219



**Figure 4.** Top: Uncorrected distance moduli for the final sample of *JHK<sub>s</sub>*, [3.6], and [4.5] photometry. Filled circles are the mean distance moduli using both RRab and RRc stars, open circles are the distance moduli using only RRab stars, and open triangles are distance moduli using only RRc stars. Here the NIR and MIR reddening laws are fit to the mean distance moduli. The solid and dashed horizontal lines are the mean corrected distance modulus and its  $1\sigma$  errors respectively. Bottom: reddening-corrected distance moduli and mean corrected distance modulus. Errors on the corrected distance moduli are the quadrature sum of the uncorrected distance moduli errors and the reddening error at the requisite wavelength.

**Table 4.** Corrected distance moduli  $\mu_0$  using the  $A_V$  value derived from fitting the reddening laws to only the RRab distance moduli.

Band	$\mu_0$ , RRab	$\mu_0$ , RRc	$\mu_0$ , RRab + RRc
<i>J</i>	$13.739 \pm 0.047$	$13.741 \pm 0.045$	$13.740 \pm 0.043$
<i>H</i>	$13.742 \pm 0.041$	$13.766 \pm 0.036$	$13.754 \pm 0.033$
<i>K_s</i>	$13.767 \pm 0.030$	$13.782 \pm 0.026$	$13.775 \pm 0.023$
[3.6]	$13.722 \pm 0.028$	$13.810 \pm 0.032$	$13.766 \pm 0.022$
[4.5]	$13.747 \pm 0.053$	$13.866 \pm 0.061$	$13.806 \pm 0.041$



**Figure 5.** Same as Figure 4, with the reddening laws fit to the RRab distances only instead of the mean. RRc distance moduli and mean distance moduli are greyed out.

**Table 5.** The standard deviation of the observed spread of the PL residuals  $\sigma_{\text{observed}}$  ( $\sigma_{\text{PL}}$  in Table 3) and its components:  $\sigma_{\text{intrinsic}}$  ( $\sigma$  in Table 1),  $\sigma_{\text{phot}}$ , and  $\sigma_{[\text{Fe}/\text{H}]}$  for all IRAC PL relations.

Band	Mode	$\sigma_{\text{observed}}$	$\sigma_{\text{intrinsic}}$	$\sigma_{\text{phot}}$	$\sigma_{[\text{Fe}/\text{H}]}$
<i>J</i>	RRab	0.127	0.060	0.018	0.111
	RRc	0.082	0.040	0.015	0.070
<i>H</i>	RRab	0.170	0.040	0.028	0.163
	RRc	0.107	0.020	0.024	0.102
<i>K<sub>s</sub></i>	RRab	0.147	0.030	0.023	0.142
	RRc	0.089	0.020	0.021	0.084
[3.6]	RRab	0.124	0.040	0.052	0.106
	RRc	0.096	0.079	0.044	0.034
[4.5]	RRab	0.154	0.045	0.046	0.140
	RRc	0.219	0.057	0.054	0.205

We use these estimates of  $\sigma_{[\text{Fe}/\text{H}]}$  to assess the  $\gamma$  parameter for  $\omega$  Cen, where

$$\gamma = \frac{\Delta \text{mag}}{\Delta [\text{Fe}/\text{H}]} \text{ mag dex}^{-1}, \quad (4)$$

**Table 6.** Metallicity standard deviations and  $\gamma$  values.

Band	Mode	$\sigma_{\text{spect}}[\text{Fe}/\text{H}]$	$\sigma_{\text{phot}}[\text{Fe}/\text{H}]$	$\gamma_{\text{spect}}$	$\gamma_{\text{phot}}$
<i>J</i>	RRab	0.215	0.262	0.515	0.423
	RRc	0.132	0.245	0.529	0.285
<i>H</i>	RRab	0.215	0.260	0.760	0.627
	RRc	0.132	0.245	0.773	0.416
<i>K<sub>s</sub></i>	RRab	0.215	0.258	0.659	0.549
	RRc	0.132	0.242	0.636	0.347
[3.6]	RRab	0.232	0.275	0.455	0.385
	RRc	0.145	0.266	0.237	0.129
[4.5]	RRab	0.215	0.285	0.653	0.492
	RRc	0.107	0.244	1.904	0.837

similar to  $\gamma$  used to quantify the effect of metallicity on the zero-point of the Cepheid PL relation (Kennicutt et al. 1998; Scowcroft et al. 2009). Here we calculate  $\gamma$  in units of  $\text{mag dex}^{-1}$  by dividing the standard deviation of the metallicity component of the PL scatter by the standard deviation of the metallicity distribution for both (Sollima et al. 2006) and photometric (Rey et al. 2000) metallicities; the results for each PL are shown in Table 6. We use all available metallicity values for each pulsation mode when taking the standard deviation, as we do not have metallicity values for all the stars in our samples, although the metallicity values we do have trace the overall metallicity distributions fairly well (see Figure 2).

For [3.6] we find  $\gamma \leq 0.455 \text{ mag dex}^{-1}$  for RRab's, and  $\gamma \leq 0.237 \text{ mag dex}^{-1}$  for RRc's. These values are upper limits, and as we will show in Sections 6.2 and 7, the size of the effect that can be attributed to metallicity effects alone may be much smaller.

## 6.2 PL Residuals and Individual Metallicities

$\omega$  Cen provides a second approach to testing for a metallicity effect on the RRL PL relation. The cluster is well studied and many of its RRL have spectroscopic or photometric metallicities in the literature (e.g. Sollima et al. 2006; Rey et al. 2000).

Theory predicts a linear metallicity term in the PLZ relation in the optical and infrared,  $c \times [\text{Fe}/\text{H}]$ . We thus fit a relation of the form

$$\Delta\text{mag} = \gamma \times [\text{Fe}/\text{H}] + d \quad (5)$$

to the [3.6] and [4.5] PL residuals and metallicity values for stars with known metallicity values, as shown in Figures 6, 7, 8, 9, and 10. The scatter in the [3.6] and [4.5] PL relations is higher for  $\omega$  Cen than it is for M4 (Neeley et al. 2015; Braga et al. 2015); however, when we examine  $[\text{Fe}/\text{H}]$  vs. the residuals of each PL relation,  $\gamma$  is within  $2\sigma$  of zero for all fits, indicating that there is no significant metallicity dependence in the PL residuals. The flatness of these relations hints that the source of additional dispersion in the  $\omega$  Cen PL relations may not be due to metallicity, but in fact due to other evolutionary effects such as the spread in age of its multiple populations. This is discussed further in Section 7.

However, the dominant source of uncertainty in these fits is the metallicity measurements, with typical errors approaching  $\sim 0.5$  dex, and systematic offsets between the

photometric and spectroscopic systems that make them unsuitable for use as one catalogue. More accurate metallicities will be required to constrain any potential effect more precisely.

## 7 DISCUSSION

While we find high upper bounds on the contribution of metallicity to the PL scatter in all infrared passbands, it is unlikely that this scatter is due to metallicity alone. Gratton et al. (1986) and Lee (1991) demonstrate that RRL luminosity is dependent on the horizontal branch morphology as well as metallicity; it is also well known that  $\omega$  Cen contains RRLs in multiple evolutionary states (Sollima et al. 2008; Navarrete et al. 2015).

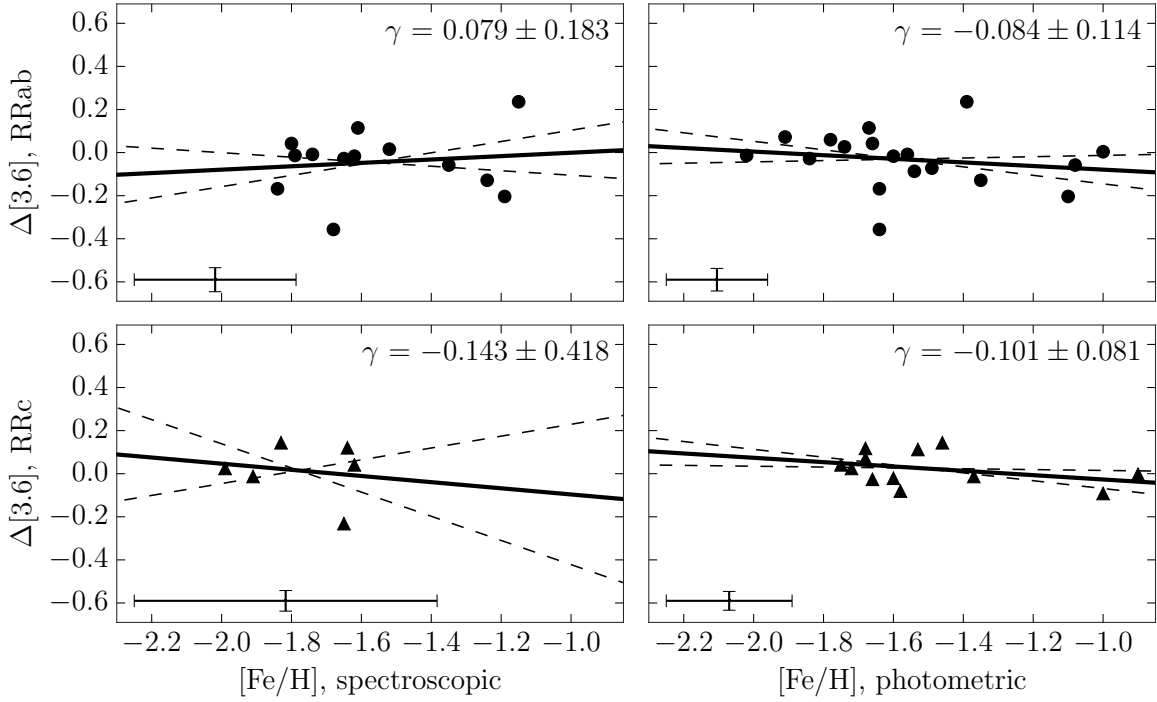
Marconi et al. (2015) performed extensive theoretical studies of the effects of both RRL composition and evolutionary state on the position of the horizontal branch in the Hertzsprung–Russell (HR) diagram. In their figure 2 they present the HR diagram for a selection of models at a fixed composition for a range of evolutionary states, demonstrating a spread in 0.3 dex in bolometric luminosity between the least evolved, zero-age horizontal branch (ZAHB) mass RRL and the most evolved RRL. The RRL population in  $\omega$  Cen is thought to be comprised of (at least) two different populations — the metal rich population being the less evolved ZAHB phase stars, with the more metal poor population in an advanced evolutionary state (Tailo et al. 2016). This spread in evolutionary state *in addition to* the spread in metallicity could create the additional dispersion observed in the  $\omega$  Cen PL relations.

Figures 12 and 13 demonstrate the need for an additional evolutionary parameter. Both the *H* and [3.6] bands show additional scatter in the  $\omega$  Cen PL relations above that which can be explained by the intrinsic dispersion and photometric uncertainties alone. Figures 12 and 13 show the PL relations with the stars colour coded by metallicity. If metallicity were the dominant factor in the additional dispersion we would expect that the high metallicity points would sit on one side of the mean PL, with the low metallicity points on the other. This is not the case in either the *H* or [3.6] bands; the metallicities appear to be randomly distributed about the mean PLs. This is a clear suggestion that the dominant effect contributing to the dispersion in the  $\omega$  Cen PL relation is a spread in evolutionary state (i.e. age), rather than composition.

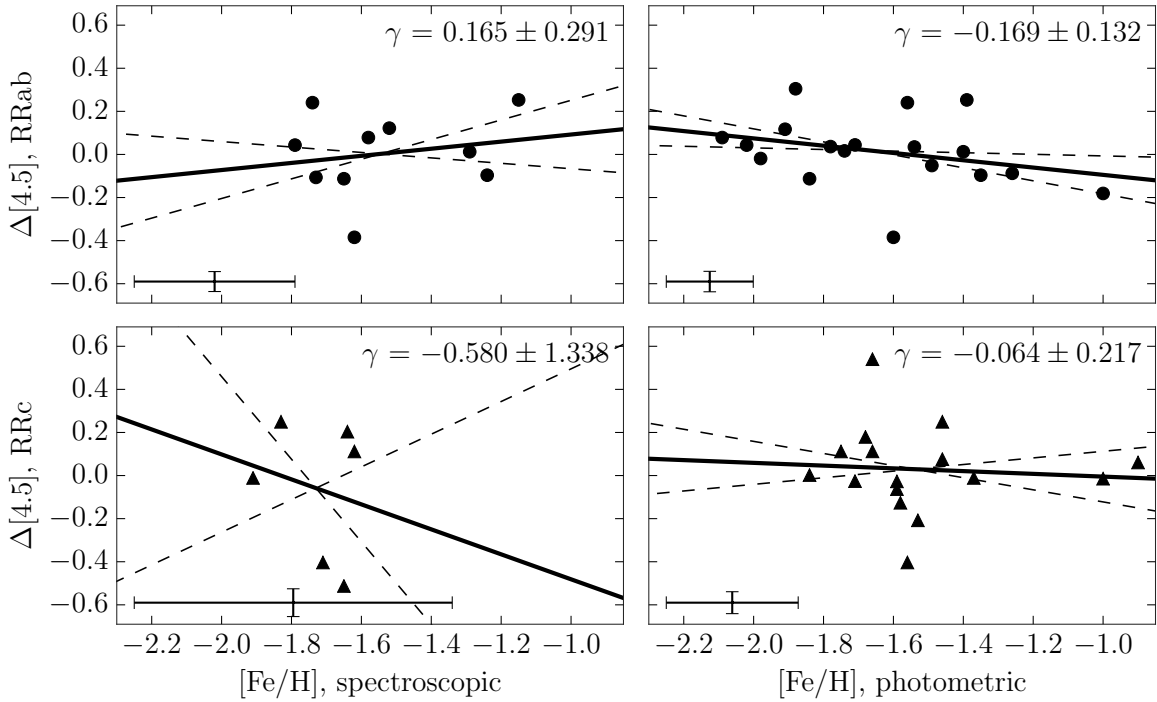
Results from the Gaia mission (Lindgren & Perryman 1996) are expected to improve the overall characterisation of the RRL PL relation dramatically. Trigonometric parallaxes and spectrophotometric metallicities of Galactic RRLs from Gaia will increase the number of high quality calibrators for the infrared PL relations by an order of magnitude (Liu et al. 2012, Scowcroft et al. 2016b, in prep., Beaton et al. 2016, in prep.).

In addition to the calibration of the slope and absolute zero-point of the RRL PL relation, Gaia will also provide important insights regarding  $\omega$  Cen. Gaia will observe many of the RRL in  $\omega$  Cen (Babusiaux et al. 2002), providing 0.2% parallaxes and spectrophotometric metallicities for the individual stars. Combining the photometric data presented here with the Gaia sample of high-quality parallaxes and

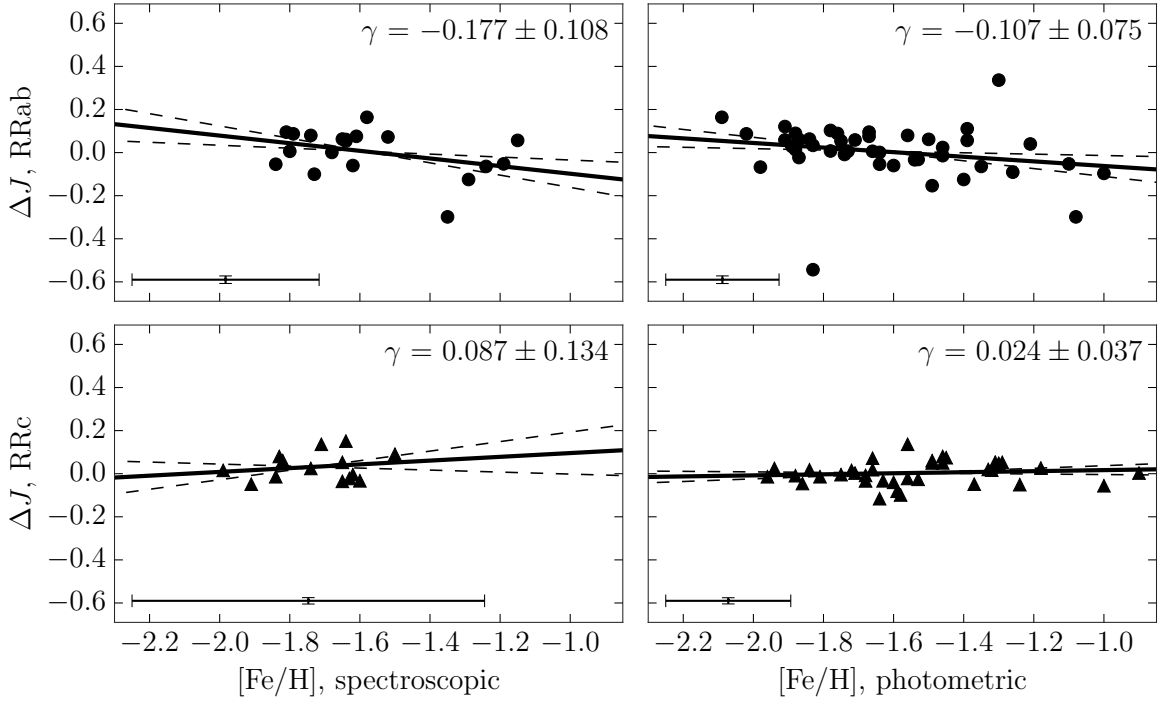




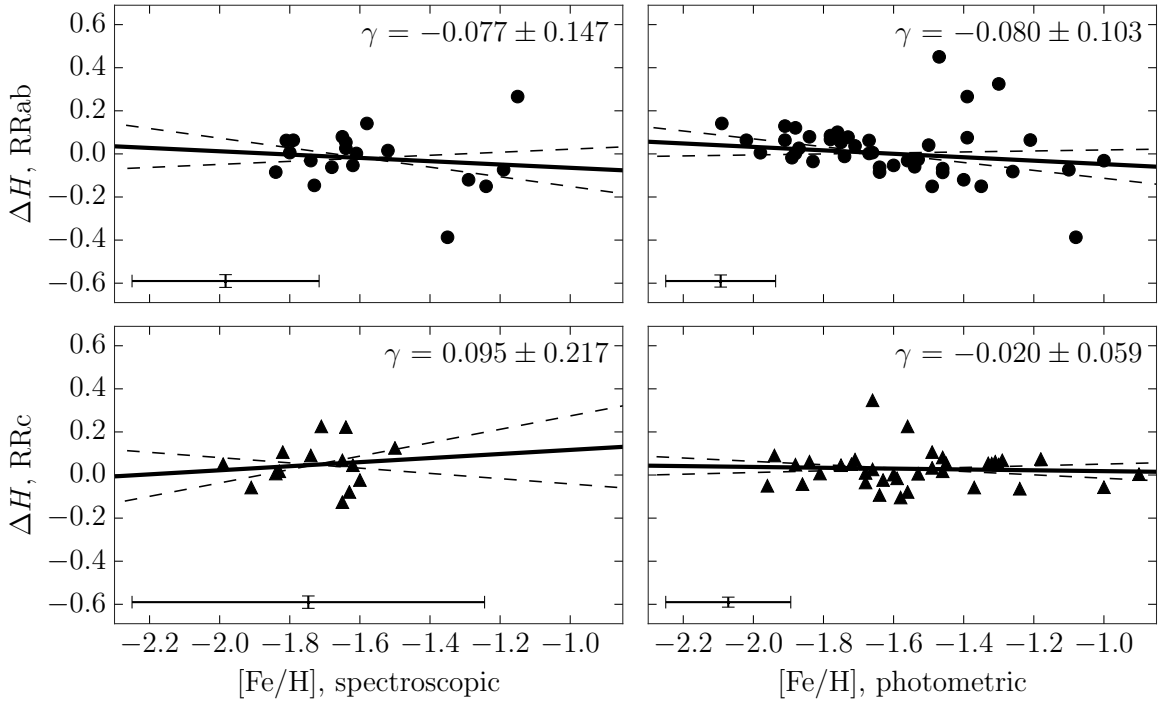
**Figure 6.** Spectroscopic (Sollima et al. 2006, left column) and photometric (Rey et al. 2000, right column)  $[\text{Fe}/\text{H}]$  values vs. period-luminosity residuals for RRAb (top row) and RRc (bottom row) in  $[3.6]$ . Solid lines are the line of best fit with slope  $\gamma$ , and dashed lines are the  $1\sigma$  confidence intervals. The crossed lines at the bottom left corner of each subplot represent average errors in  $[\text{Fe}/\text{H}]$  and  $\Delta\text{mag}$ . The  $\gamma$  parameter from equation 4 is shown in the top right corner of each subplot. All  $\gamma$  values are consistent with zero within  $2\sigma$ , and most are consistent within  $1\sigma$ .



**Figure 7.** Same as Figure 6, but for  $[4.5]$ .



**Figure 8.** Same as Figure 6, but for  $J$ .



**Figure 9.** Same as Figure 6, but for  $H$ .

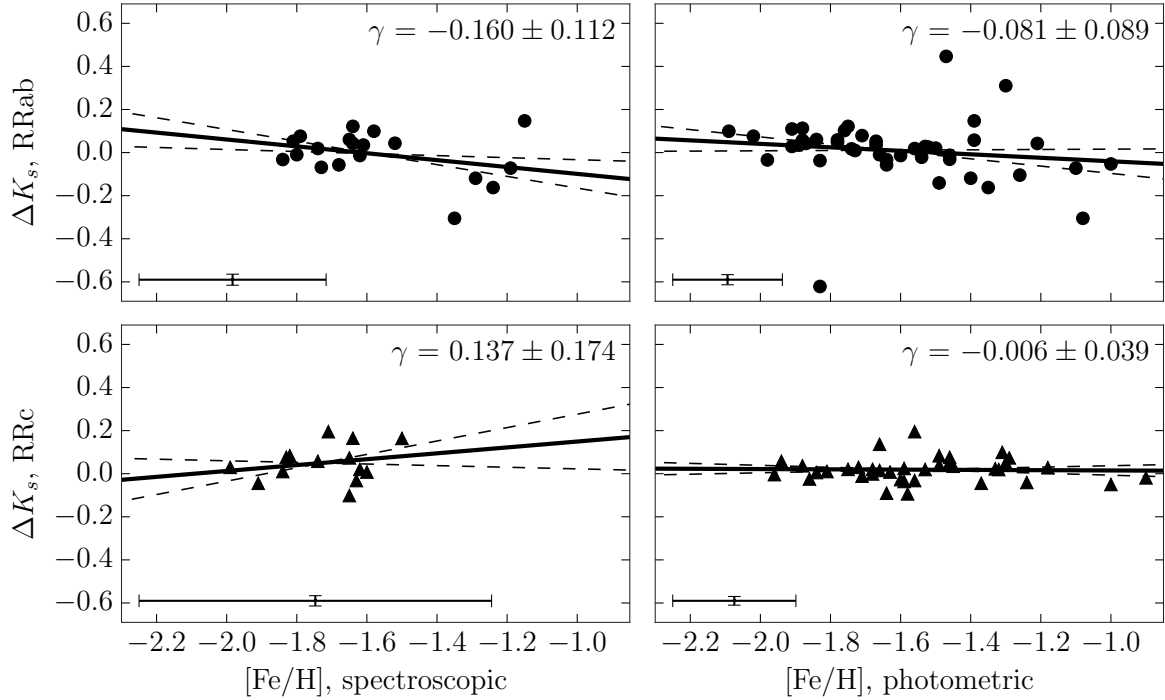


Figure 10. Same as Figure 6, but for  $K_s$ .

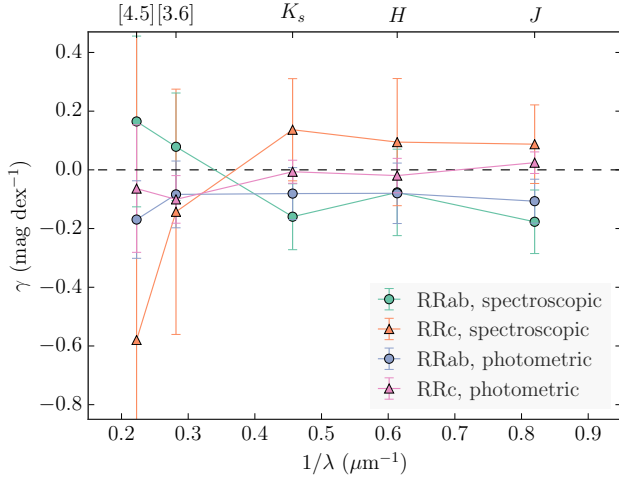


Figure 11. .

consistent metallicities we will be able to further constrain the effect on the mid-IR PL relation.

We also anticipate that the NIRCcam instrument on *JWST* (Burriesci 2005; Gardner et al. 2006) will provide substantial improvements over IRAC for investigations of this nature. The NIRCcam filters F356W and F444W will provide data in passbands comparable to IRAC's [3.6] and [4.5] at an order of magnitude higher resolution (0.065 arc-sec/pixel), which will significantly decrease photometric error due to crowding and therefore allow us to obtain data for

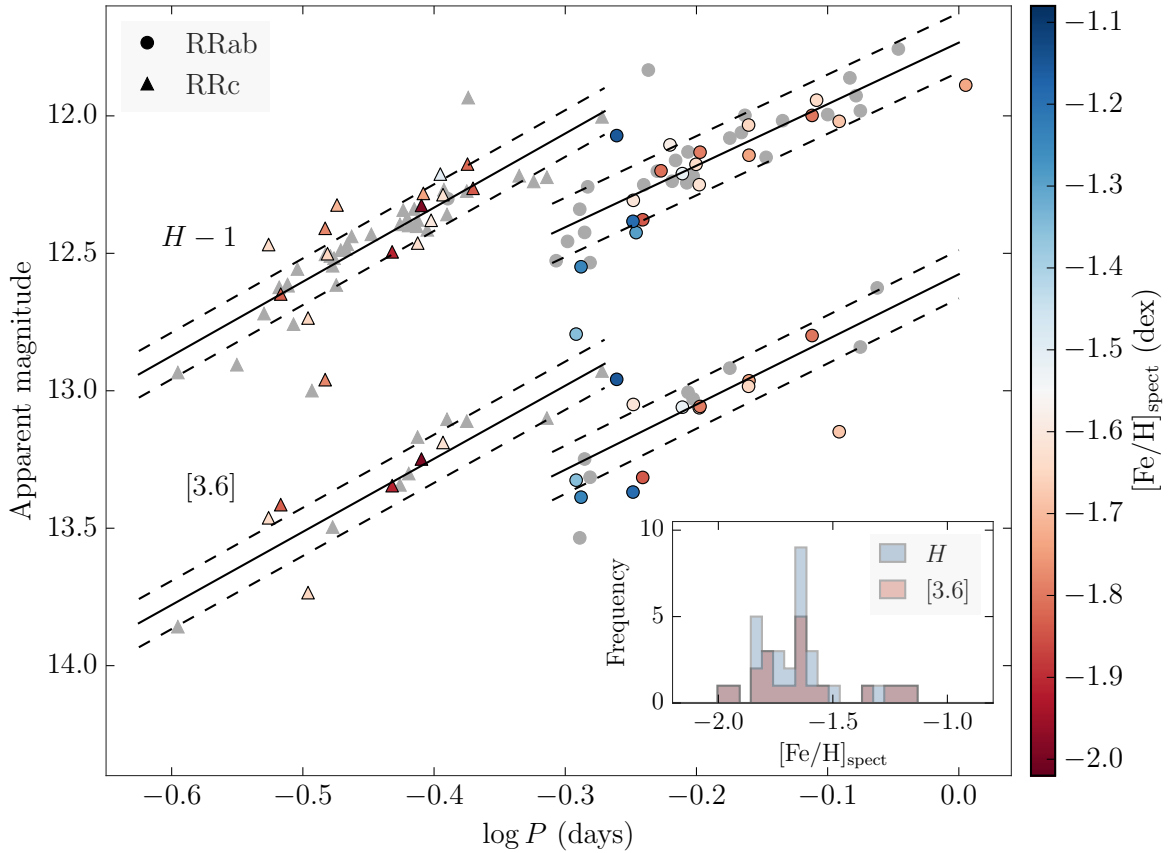
the full sample of RRL in  $\omega$  Cen. With the parallaxes and differential metallicities from Gaia, and the high precision photometry from *JWST*, studies of  $\omega$  Cen will allow us to explore the effects of metallicity and evolutionary effects on the RRL populations of globular clusters.

## 8 CONCLUSIONS

We derive a mean dereddened distance modulus for  $\omega$  Cen of  $\langle\mu_0\rangle = 13.743 \pm 0.026$  with reddening  $E(B - V) = 0.138 \pm 0.044$  using distance moduli derived from RRL PL relations in  $JHK_s$ , [3.6], and [4.5]. Using the mean of RRLab and RRLc distance moduli in the same passbands, we derive a mean dereddened distance modulus of  $\langle\mu_0\rangle = 13.789 \pm 0.018$  with reddening  $E(B - V) = 0.084 \pm 0.030$ . The value found using RRLab alone is in better agreement with those in the literature (e.g. Lub 2002; Del Principe et al. 2006).

We also constrain the contribution of metallicity on the dispersion of the RRL PL relations by considering the variances associated with each component of the PL relation. We find that at most metallicity contributes 0.106 and 0.140 mag in dispersion to the [3.6] and [4.5] RRLab PL relations respectively. Converting these values into  $\gamma$ , the PL relation metallicity coefficient, we find high upper limits compared to theoretical predictions for all infrared wavelengths.

When deriving  $\gamma$  empirically using the residuals from the RRL PL relations and the individual metallicities of the stars, we find  $\gamma$  values consistent with zero at all infrared wavelengths. We thus conclude that the upper limits derived in Section 6.1 are likely a combination of metallicity and



**Figure 12.**  $H$  and  $[3.6]$  PL relations, with colour indicating spectroscopic (Sollima et al. 2006) metallicity values. Grey points have no known metallicity values. There is no trend between direction of deviation from the PL with metallicity in either the  $H$  or  $[3.6]$  relation, demonstrating that the increased dispersion must have an additional evolutionary component.

evolutionary effects due to the evolutionary spread of the populations in  $\omega$  Cen.

under contract with the National Aeronautics and Space Administration.

## ACKNOWLEDGEMENTS

We thank Eric Persson for his many contributions to this project.

This work is based on observations made with the Spitzer Space Telescope, which is operated by the Jet Propulsion Laboratory, California Institute of Technology under a contract with NASA. Support for this work was provided by NASA through an award issued by JPL/Caltech.

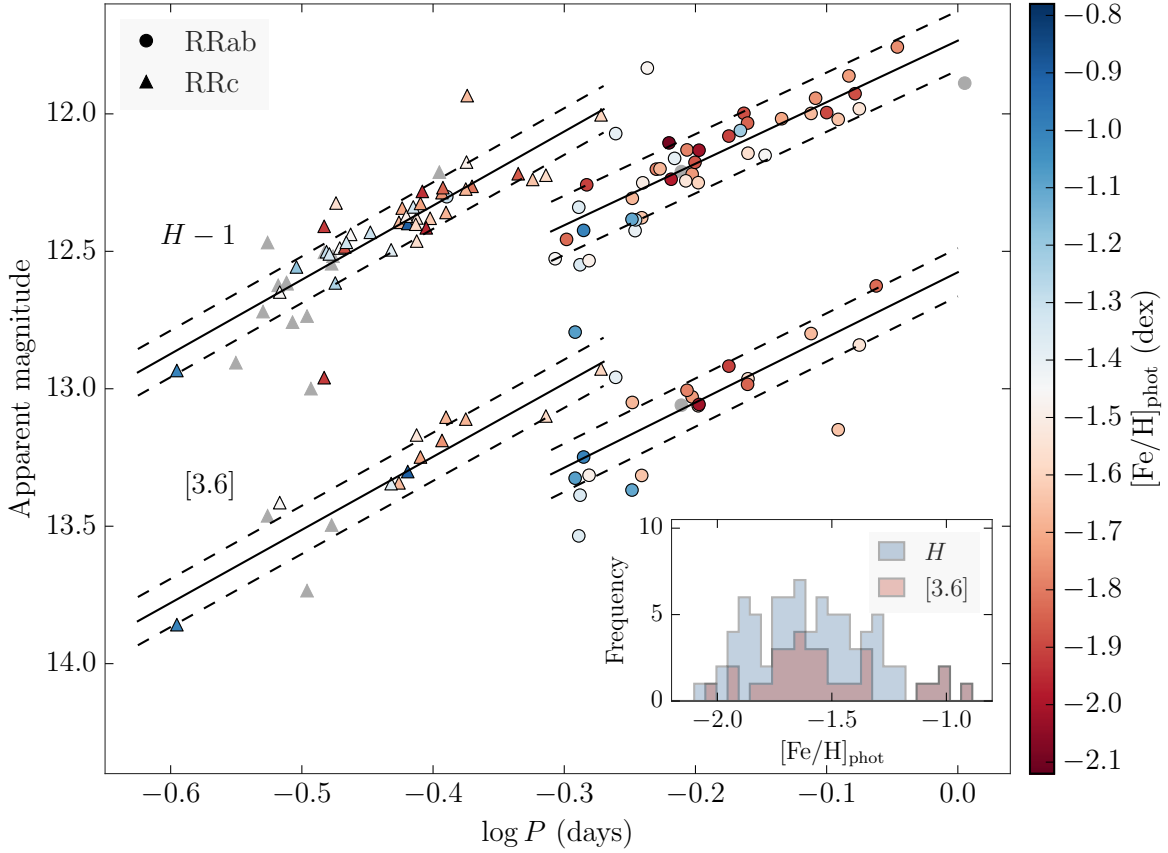
This work was also supported in part by the Claremont-Carnegie Astrophysics Research Program.

This publication makes use of data products from the Two Micron All Sky Survey, which is a joint project of the University of Massachusetts and the Infrared Processing and Analysis Center/California Institute of Technology, funded by the National Aeronautics and Space Administration and the National Science Foundation.

This research has made use of the NASA/IPAC Extragalactic Database (NED), which is operated by the Jet Propulsion Laboratory, California Institute of Technology,

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**Figure 13.**  $H$  and  $[3.6]$  PL relations, with colour indicating photometric (Rey et al. 2000) metallicity values. Grey points have no known metallicity values. There is no trend between direction of deviation from the PL with metallicity in either the  $H$  or  $[3.6]$  relation, demonstrating that the increased dispersion must have an additional evolutionary component.

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**APPENDIX A: RRL PHOTOMETRY**

Table A1: Parameters for 99 RRLs in  $\omega$  Cen. First five columns are star ID, right ascension and declination, pulsation mode, and period in days from [Kaluzny et al. \(2004\)](#). Columns 6 through 11 are  $JHK_s$  apparent magnitudes and errors from FourStar data. Columns 12 through 17 are  $3.6\ \mu\text{m}$  and  $4.5\ \mu\text{m}$  apparent magnitudes, errors, and PL residuals ( $\Delta[3.6]$  and  $\Delta[4.5]$ ) from IRAC data. Columns 18-21 are photometric ([Fe/H],  $p$ ) and spectroscopic ([Fe/H],  $s$ ) metallicities and errors from [Rey et al. \(2000\)](#) and [Sollima et al. \(2006\)](#) respectively.

ID	RA (J2000)	Dec (J2000)	Mode	$P$ (days)	$J$	$\sigma_J$	$H$	$\sigma_H$	$K_s$	$\sigma_{K_s}$	[3.6]	$\sigma_{[3.6]}$	$\Delta[3.6]$	[4.5]	$\sigma_{[4.5]}$	$\Delta[4.5]$	[Fe/H], $p$	$\sigma_{[\text{Fe}/\text{H}]}, p$	[Fe/H], $s$	$\sigma_{[\text{Fe}/\text{H}]}, s$
3	13:25:56.15	-47:25:53.8	RRab	0.841	13.247	0.017	12.982	0.018	12.882	0.017	12.841	0.039	-0.087	12.708	0.036	0.035	-1.540	0.050	—	—
4	13:26:12.93	-47:24:18.8	RRab	0.627	13.475	0.016	13.219	0.021	13.133	0.020	13.030	0.036	0.026	13.026	0.035	0.016	-1.740	0.050	—	—
5	13:26:18.33	-47:23:12.4	RRab	0.515	13.700	0.017	13.549	0.020	13.507	0.027	13.387	0.043	-0.129	13.340	0.030	-0.096	-1.350	0.080	-1.240	0.110
7	13:27:00.90	-47:14:00.5	RRab	0.713	13.333	0.009	13.151	0.031	13.036	0.018	—	—	—	—	—	—	-1.460	0.080	—	—
8	13:27:48.45	-47:28:20.3	RRab	0.521	13.505	0.015	13.258	0.017	13.223	0.014	—	—	—	—	—	—	-1.910	0.280	—	—
9	13:25:59.58	-47:26:24.0	RRab	0.523	13.776	0.017	13.534	0.021	13.470	0.016	13.315	0.036	-0.072	13.279	0.039	-0.051	-1.490	0.060	—	—
10	13:26:06.99	-47:24:36.6	RRc	0.375	13.579	0.014	13.395	0.023	13.345	0.019	13.342	0.037	-0.026	13.168	0.037	0.112	-1.660	0.100	—	—
11	13:26:30.59	-47:23:01.6	RRab	0.565	13.481	0.014	13.307	0.028	13.219	0.025	13.050	0.058	—	—	—	—	-1.670	0.130	-1.610	0.220
12	13:26:27.21	-47:24:06.2	RRc	0.387	13.590	0.018	13.379	0.028	13.305	0.025	13.168	0.048	0.112	13.448	0.088	-0.208	-1.530	0.140	—	—
13	13:25:58.18	-47:25:21.6	RRab	0.669	13.353	0.019	13.081	0.022	13.058	0.017	12.918	0.032	0.072	12.860	0.031	0.117	-1.910	0.000	—	—
14	13:25:59.74	-47:39:09.6	RRc	0.377	13.588	0.011	13.343	0.020	13.365	0.016	—	—	—	13.299	0.045	—	-1.710	0.130	—	—
15	13:26:27.11	-47:24:38.0	RRab	0.811	13.245	0.018	13.020	0.031	12.954	0.025	13.149	0.084	—	—	—	—	-1.640	0.390	-1.680	0.180
16	13:27:37.69	-47:37:34.8	RRc	0.330	13.680	0.015	13.502	0.022	13.437	0.018	—	—	—	—	—	—	-1.290	0.080	-1.650	0.460
18	13:27:45.11	-47:24:56.6	RRab	0.622	13.371	0.010	13.131	0.024	13.100	0.016	13.006	0.043	—	—	—	—	-1.780	0.280	—	—
20	13:27:14.05	-47:28:06.3	RRab	0.616	13.410	0.015	13.210	0.036	13.125	0.025	13.060	0.039	0.016	12.940	0.029	0.122	—	—	-1.520	0.340
21	13:26:11.17	-47:25:58.8	RRc	0.381	13.578	0.016	13.399	0.027	13.361	0.020	13.301	0.047	-0.003	13.200	0.032	0.061	-0.900	0.110	—	—
22	13:27:41.04	-47:34:07.6	RRc	0.396	13.572	0.012	13.380	0.016	13.288	0.017	—	—	—	—	—	—	-1.630	0.170	-1.600	0.990
23	13:26:46.50	-47:24:39.5	RRab	0.511	13.941	0.025	13.794	0.048	13.658	0.033	13.325	0.064	—	—	—	—	-1.080	0.140	-1.350	0.580
24	13:27:38.32	-47:34:14.5	RRc	0.462	13.419	0.012	13.218	0.014	13.138	0.014	—	—	—	—	—	—	-1.860	0.030	—	—
30	13:26:15.94	-47:29:56.0	RRc	0.404	13.521	0.021	13.287	0.046	13.251	0.030	13.188	0.047	0.041	13.071	0.060	0.112	-1.750	0.170	-1.620	0.280
32	13:27:03.32	-47:21:38.9	RRab	0.620	13.508	0.009	13.244	0.018	13.132	0.018	—	—	—	—	—	—	-1.530	0.160	—	—
33	13:25:51.60	-47:29:05.8	RRab	0.602	13.338	0.015	13.106	0.022	13.091	0.019	—	—	—	13.006	0.035	—	-2.090	0.230	-1.580	0.420
34	13:26:07.21	-47:33:10.4	RRab	0.734	13.273	0.014	13.018	0.014	12.916	0.013	—	—	—	12.838	0.065	—	-1.710	0.000	—	—
35	13:26:53.21	-47:22:34.7	RRc	0.387	13.586	0.012	13.463	0.024	13.356	0.023	—	—	—	—	—	—	-1.560	0.080	-1.630	0.360
36	13:27:10.11	-47:15:29.8	RRc	0.380	13.534	0.007	13.372	0.019	13.307	0.014	—	—	—	—	—	—	-1.490	0.230	—	—
38	13:27:03.30	-47:36:30.2	RRab	0.779	13.226	0.015	12.943	0.019	12.814	0.018	—	—	—	—	—	—	-1.750	0.180	-1.640	0.400
39	13:27:59.77	-47:34:42.3	RRc	0.393	13.560	0.009	13.415	0.014	13.308	0.014	—	—	—	—	—	—	-1.960	0.290	—	—
40	13:26:24.56	-47:30:46.2	RRab	0.634	13.517	0.022	13.250	0.051	13.153	0.033	13.062	0.049	-0.017	13.416	0.056	-0.385	-1.600	0.080	-1.620	0.190
44	13:26:22.39	-47:34:35.3	RRab	0.568	13.677	0.014	13.425	0.023	13.368	0.018	—	—	—	13.132	0.036	—	-1.400	0.120	-1.290	0.350
45	13:25:30.88	-47:27:21.0	RRab	0.589	13.513	0.015	13.201	0.015	13.164	0.014	—	—	—	13.070	0.028	—	-1.780	0.250	—	—
46	13:25:30.23	-47:25:51.8	RRab	0.687	13.299	0.016	12.998	0.017	12.947	0.014	—	—	—	—	—	—	-1.880	0.170	—	—
47	13:25:56.46	-47:24:12.0	RRc	0.485	13.420	0.020	13.223	0.018	13.150	0.018	13.099	0.030	-0.080	13.073	0.026	-0.126	-1.580	0.310	—	—
49	13:26:07.78	-47:37:55.5	RRab	0.605	13.566	0.012	13.238	0.019	13.220	0.016	—	—	—	13.099	0.049	—	-1.980	0.110	—	—
50	13:25:53.94	-47:27:35.8	RRc	0.386	13.647	0.014	13.402	0.015	13.362	0.014	—	—	—	13.305	0.056	—	-1.590	0.190	—	—
51	13:26:42.66	-47:24:21.4	RRab	0.574	13.597	0.014	13.378	0.033	13.270	0.029	13.315	0.083	—	—	—	—	-1.640	0.210	-1.840	0.230
54	13:26:23.54	-47:18:47.7	RRab	0.773	13.281	0.016	12.998	0.017	12.954	0.015	12.799	0.030	—	—	—	—	-1.660	0.120	-1.800	0.230
56	13:25:55.53	-47:37:44.1	RRab	0.568	13.643	0.009	13.386	0.022	13.353	0.017	—	—	—	13.232	0.035	—	-1.260	0.150	—	—
57	13:27:49.38	-47:36:50.5	RRab	0.794	13.234	0.015	12.995	0.018	12.882	0.014	—	—	—	—	—	—	-1.890	0.140	—	—
58	13:26:13.05	-47:24:03.0	RRc	0.370	13.660	0.017	13.495	0.018	13.421	0.021	13.345	0.033	-0.013	13.309	0.034	-0.011	-1.370	0.180	-1.910	0.310
59	13:26:18.43	-47:29:46.7	RRab	0.519	13.727	0.023	13.424	0.043	13.391	0.033	13.248	0.071	0.004	13.418	0.064	-0.181	-1.000	0.280	—	—
63	13:25:07.96	-47:36:54.1	RRab	0.826	13.223	0.017	12.862	0.017	12.869	0.012	—	—	—	—	—	—	-1.730	0.090	—	—
64	13:26:02.22	-47:36:19.2	RRc	0.344	13.638	0.013	13.438	0.022	13.407	0.022	—	—	—	13.314	0.044	—	-1.460	0.230	—	—
66	13:26:33.08	-47:22:25.2	RRc	0.407	13.542	0.011	13.359	0.022	13.264	0.020	13.103	0.035	—	—	—	—	-1.680	0.340	—	—
67	13:26:28.62	-47:18:46.9	RRab	0.564	13.610	0.014	13.384	0.016	13.326	0.015	13.368	0.047	—	—	—	—	-1.100	0.000	-1.190	0.230
68	13:26:12.80	-47:19:35.7	RRc	0.535	13.258	0.021	13.004	0.015	12.970	0.015	12.928	0.050	—	—	—	—	-1.600	0.010	—	—
69	13:25:11.02	-47:37:33.5	RRab	0.635	—	—	—	—	13.112	0.014	—	—	—	—	—	—	-1.520	0.140	—	—
70	13:27:27.76	-47:33:42.7	RRc	0.391	13.529	0.013	13.282	0.029	13.254	0.022	—	—	—	—	—	—	-1.940	0.150	-1.740	0.300
72	13:27:33.11	-47:16:22.9	RRc	0.385	13.554	0.010	13.339	0.017	13.311	0.014	—	—	—	—	—	—	-1.320	0.220	—	—
73	13:25:53.75	-47:16:10.8	RRab	0.575	13.480	0.018	13.251	0.017	13.215	0.016	—	—	—	—	—	—	-1.500	0.090	—	—
74	13:27:07.22	-47:17:33.9	RRab	0.503	13.622	0.008	13.457	0.016	13.405	0.015	—	—	—	—	—	—	-1.830	0.360	—	—
75	13:27:19.70	-47:18:46.5	RRc	0.422	13.410	0.011	13.175	0.028	13.137	0.025	—	—	—	—	—	—	-1.490	0.080	-1.820	0.990
76	13:26:57.23	-47:20:07.7	RRc	0.338	13.634	0.012	13.488	0.017	13.449	0.020	—	—	—	—	—	—	-1.450	0.130	—	—
77	13:27:20.89	-47:22:05.6	RRc	0.426	13.474	0.013	13.264	0.028	13.199	0.021	—	—	—	—	—	—	-1.810	0.000	-1.840	0.430

Continued on next page

Table A1 - Continued from previous page

ID	RA (J2000)	Dec (J2000)	Mode	$P$ (days)	$J$	$\sigma_J$	$H$	$\sigma_H$	$K_s$	$\sigma_{K_s}$	[3.6]	$\sigma_{[3.6]}$	$\Delta[3.6]$	[4.5]	$\sigma_{[4.5]}$	$\Delta[4.5]$	[Fe/H], p	$\sigma_{[\text{Fe}/\text{H}]}$ , p	[Fe/H], s	$\sigma_{[\text{Fe}/\text{H}]}$ , s
79	13:28:24.99	-47:29:25.2	RRab	0.608	13.382	0.010	13.162	0.016	13.123	0.015	—	—	—	—	—	—	-1.390	0.180	—	—
81	13:27:36.68	-47:24:48.3	RRc	0.389	13.542	0.013	13.326	0.033	13.286	0.025	13.248	0.076	—	—	—	—	-1.720	0.310	-1.990	0.430
82	13:27:35.61	-47:26:30.3	RRc	0.336	13.579	0.016	13.324	0.024	13.296	0.018	—	—	—	13.827	0.104	—	-1.560	0.200	-1.710	0.560
83	13:27:08.42	-47:21:34.1	RRc	0.357	13.603	0.010	13.431	0.024	13.370	0.022	—	—	—	—	—	—	-1.300	0.220	—	—
84	13:24:47.45	-47:29:56.5	RRab	0.580	—	—	12.833	0.017	12.781	0.016	—	—	—	—	—	—	-1.470	0.100	—	—
85	13:25:06.49	-47:23:34.0	RRab	0.743	13.344	0.011	—	—	—	—	—	—	—	—	—	—	-1.870	0.310	—	—
94	13:25:57.06	-47:22:46.1	RRc	0.254	14.070	0.024	13.934	0.022	13.870	0.027	13.858	0.038	-0.092	13.799	0.029	-0.014	-1.000	0.110	—	—
95	13:25:24.95	-47:28:53.2	RRc	0.405	13.497	0.015	13.269	0.017	13.264	0.017	—	—	—	13.178	0.024	—	-1.840	0.550	—	—
97	13:27:08.49	-47:25:30.9	RRab	0.692	13.302	0.010	13.143	0.029	13.034	0.022	12.964	0.061	-0.008	12.702	0.064	0.240	-1.560	0.370	-1.740	0.170
101	13:27:30.24	-47:29:51.0	RRc	0.341	13.708	0.016	13.484	0.030	13.436	0.023	—	—	—	—	—	—	-1.880	0.320	—	—
102	13:27:22.11	-47:30:12.3	RRab	0.691	13.320	0.012	13.033	0.022	12.993	0.020	12.984	0.049	-0.028	13.056	0.072	-0.113	-1.840	0.130	-1.650	0.160
103	13:27:14.29	-47:28:36.3	RRc	0.329	13.620	0.018	13.409	0.040	13.377	0.034	12.960	0.071	—	13.024	0.066	—	-1.920	0.110	-1.780	0.270
104	13:28:07.76	-47:33:44.9	RRab	0.867	13.732	0.096	13.626	0.154	13.452	0.141	—	—	—	—	—	—	-1.830	0.180	—	—
105	13:27:46.02	-47:32:43.9	RRc	0.335	13.768	0.014	13.615	0.020	13.533	0.018	—	—	—	—	—	—	-1.240	0.180	—	—
107	13:27:14.05	-47:30:57.9	RRab	0.514	13.597	0.017	13.340	0.038	13.301	0.030	13.535	0.219	—	13.351	0.076	—	-1.360	0.110	—	—
115	13:26:12.30	-47:34:17.5	RRab	0.630	13.401	0.012	13.176	0.017	13.103	0.013	—	—	—	—	—	—	-1.870	0.010	-1.640	0.320
117	13:26:19.91	-47:29:21.0	RRc	0.422	13.480	0.020	13.274	0.043	13.202	0.031	13.110	0.044	0.071	12.949	0.043	0.179	-1.680	0.250	—	—
120	13:26:25.52	-47:32:48.6	RRab	0.549	13.525	0.049	13.072	0.079	13.135	0.094	12.958	0.066	0.236	12.927	0.055	0.253	-1.390	0.060	-1.150	0.160
121	13:26:28.17	-47:31:50.5	RRc	0.304	13.741	0.016	13.648	0.033	13.531	0.026	13.414	0.037	0.144	13.302	0.033	0.249	-1.460	0.130	-1.830	0.400
122	13:26:30.31	-47:33:02.2	RRab	0.635	13.369	0.018	13.132	0.042	13.062	0.024	13.057	0.052	-0.013	12.987	0.052	0.043	-2.020	0.180	-1.790	0.210
123	13:26:51.17	-47:37:13.2	RRc	0.474	13.462	0.016	13.239	0.019	13.174	0.017	—	—	—	—	—	—	-1.640	0.010	—	—
124	13:26:54.49	-47:39:07.5	RRc	0.332	13.708	0.013	13.510	0.018	13.482	0.023	—	—	—	—	—	—	-1.330	0.230	—	—
125	13:26:48.92	-47:41:03.7	RRab	0.593	13.420	0.015	13.200	0.016	13.153	0.015	—	—	—	—	—	—	-1.670	0.220	-1.810	0.380
126	13:28:08.03	-47:40:46.7	RRc	0.342	13.642	0.011	13.467	0.017	13.370	0.016	—	—	—	—	—	—	-1.310	0.130	—	—
127	13:25:19.36	-47:28:37.6	RRc	0.305	—	—	—	—	13.579	0.018	—	—	—	13.573	0.063	—	-1.590	0.080	—	—
128	13:26:17.75	-47:30:13.0	RRab	0.835	13.207	0.018	12.927	0.032	12.810	0.020	—	—	—	12.445	0.074	—	-1.880	0.040	—	—
130	13:26:09.93	-47:13:40.0	RRab	0.493	13.688	0.021	13.527	0.032	13.418	0.025	—	—	—	—	—	—	-1.460	0.170	—	—
147	13:27:15.86	-47:31:09.2	RRc	0.423	13.397	0.012	12.934	0.041	13.083	0.022	—	—	—	12.585	0.096	—	-1.660	0.140	—	—
149	13:27:32.94	-47:13:43.6	RRab	0.683	13.354	0.015	13.061	0.035	13.024	0.024	—	—	—	—	—	—	-1.210	0.240	—	—
150	13:27:40.21	-47:36:00.1	RRab	0.899	13.068	0.019	12.757	0.025	12.692	0.018	—	—	—	—	—	—	-1.760	0.340	—	—
151	13:28:25.40	-47:16:00.2	RRab	0.408	13.501	0.013	13.301	0.020	13.265	0.016	—	—	—	—	—	—	-1.300	0.240	—	—
163	13:25:49.42	-47:20:21.5	RRc	0.313	13.763	0.019	13.557	0.016	13.545	0.025	—	—	—	—	—	—	-1.180	0.270	—	—
168	13:25:52.78	-47:32:02.9	RRc	0.321	14.176	0.015	14.000	0.020	13.960	0.018	—	—	—	—	—	—	—	—	—	—
169	13:27:20.47	-47:23:59.1	RRc	0.319	13.805	0.013	13.735	0.019	13.652	0.025	13.734	0.050	-0.232	14.001	0.116	-0.512	—	—	-1.650	0.190
184	13:27:28.50	-47:31:35.4	RRc	0.303	13.778	0.012	13.624	0.028	13.536	0.019	—	—	—	—	—	—	—	—	—	—
185	13:26:04.13	-47:21:45.0	RRc	0.333	13.701	0.016	13.545	0.018	13.508	0.023	13.496	0.036	-0.043	13.479	0.033	-0.046	—	—	—	—
261	13:27:15.41	-47:21:29.5	RRc	0.403	13.431	0.009	13.212	0.019	13.113	0.020	—	—	—	—	—	—	—	—	-1.500	0.350
263	13:26:13.13	-47:26:09.7	RRab	1.012	13.155	0.017	12.888	0.017	12.746	0.016	—	—	—	12.660	0.034	—	—	—	-1.730	0.190
274	13:26:43.73	-47:22:48.2	RRc	0.311	13.828	0.011	13.758	0.023	13.650	0.022	—	—	—	—	—	—	—	—	—	—
276	13:27:16.51	-47:33:17.6	RRc	0.308	13.727	0.021	13.614	0.046	13.533	0.024	—	—	—	—	—	—	—	—	—	—
280	13:27:09.33	-47:23:05.7	RRc	0.282	13.951	0.012	13.905	0.026	13.816	0.029	—	—	—	—	—	—	—	—	—	—
285	13:25:40.20	-47:34:48.4	RRc	0.329	13.687	0.017	13.504	0.027	13.503	0.015	—	—	—	13.358	0.074	—	—	—	—	—
288	13:28:10.32	-47:23:47.8	RRc	0.295	13.809	0.011	13.719	0.016	13.635	0.019	—	—	—	—	—	—	—	—	—	—
289	13:28:03.68	-47:21:27.9	RRc	0.308	13.743	0.013	13.618	0.015	13.584	0.022	—	—	—	—	—	—	—	—	—	—
291	13:26:38.52	-47:33:28.0	RRc	0.334	13.674	0.018	13.518	0.044	13.444	0.026	—	—	—	—	—	—	—	—	—	—
357	13:26:17.77	-47:30:23.4	RRc	0.298	13.692	0.027	13.468	0.064	13.468	0.045	13.462	0.044	0.120	13.375	0.041	0.204	—	—	-1.640	0.990

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