

STATISTICAL MODELING OF EARTH'S PLASMASPHERE

by

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Dedication

I dedicate this dissertation to ... I dedicate this dissertation to ... I dedicate this dissertation to ... I dedicate this dissertation to ... I dedicate this dissertation to ... I dedicate this dissertation to ... I dedicate this dissertation to ...

Acknowledgments

I would like to thank the following people who made this possible ... I would like to thank the following people who made this possible ...

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Abstract

STATISTICAL MODELLING OF EARTH'S PLASMASPHERE

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George Mason University, 2016

Dissertation Director: Robert Weigel

This dissertation intends to first: be a survey of current forecasting capabilities of statistical and magnetohydrodynamic (MHD) methods of Earth's magnetosphere, and second: attempt to improve upon forecasting methods by investigating the usefulness of various new models on both real and modeled data. The forecasting will be separated into two parts: that focusing on rare, but significant events (e.g. geomagnetic storms), and that focusing on general day-to-day predictions. It will encompass three main methods of forecasting: impulse response functions (IRF), nonlinear methods, and statistical methods that attempt to forecast MHD.

Chapter 1: Introduction

1.1 Background

1.1.1 Magnetosphere

Discovery

The dynamic processes of Earth's magnetosphere and their various impacts on the planet and its inhabitants have been studied for centuries: from Celsius and Hiorter who noted a correlation between compass orientation and aurora Soon and Yaskell [2003], and the Carrington event in 1859 established the connection between solar output and electromagnetic effects on Earth Carrington [1859].

It wasn't until Van Allen did his rocket sounding and satellite measurements of high altitude cosmic rays, finding the eponymous Van Allen Radiation Belt, that the structure of the magnetosphere was generally accepted to be more complex than that of a basic dipole magnet Newell [2011]. Showing that charged particles in solar wind plasma could be broken into constituent parts and directed into currents led to a deeper understanding of the behavior the magnetosphere and its interconnectivity with structures both inwards and outwards, which in turn allowed for better forecasting of ground-based effects based on solar wind conditions.

Our current computational technology, combined with over 50 years' worth of satellite and ground based measurements Snare, allows for a much stronger statistics-based forecasting method to be performed and long-term analyses of the capabilities of computationally intensive forecasting methods.

Processes

The complex structure of the magnetosphere and plasmasphere lead to a number of distinct behaviors and processes such as ring currents, geomagnetic storms, and magnetospheric substorms.

The Ring Current, shown in Figure 1.1 is a formed when the magnetosphere splits the neutral solar wind into positive and negative components, where they circle the earth moving along magnetic field lines until they either connect with particles in the upper atmosphere/ionosphere and fall out, or remain trapped in the magnetosphere and slowly drift in opposing directions around the magnetic equator. With enough energetic particles drifting together, a current is generated that can significantly affect the Earth's magnetic field and is labeled the ring current. These particles in the current are injected into the magnetosphere via conditions that cause the solar wind's magnetic field to connect with that of Earth, which is often exacerbated by the surge of energy created by geomagnetic storms.

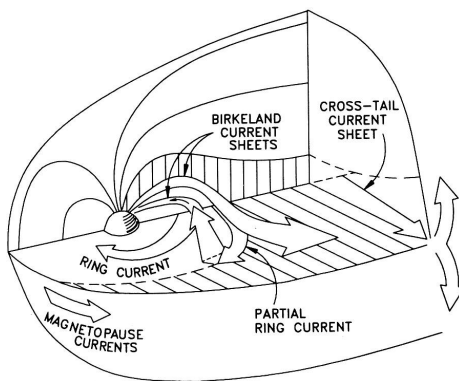


Figure 1.1: Currents in/around the magnetosphere Stern [1994]

Geomagnetic storms occur when the solar wind interacts with the Earth's magnetosphere in such a way as to produce significant disruptions in its normal, quiet-time, behavior. It is generally defined by a significant change to the magnetic field measured by multiple ground-based magnetometer measurements from stations spread around the world, in the case of the K_P index, or around the geomagnetic equator in the case of the disturbance

storm-time (D_{st}) index. By using these indices, storms can be classified into categories of severity Oceanic and Administration [2005]. The definition of storms in the literature varies slightly between authors Yermolaev and Yermolaev [2006], but most agree that sustained and abnormally perturbed near-earth magnetic field strengths over several hours or more constitutes a geomagnetic storm Gosling et al. [1991].

Geomagnetic substorms, in contrast with storms, are much shorter; typically only existing for an hour or two, and potentially happening soon after one another. They tend to have a less appreciable effect on the amount of particles/energy in the ring current, and are associated with sudden changes in energy coming from the tail of the magnetosphere rather than the dayside reconnections associated with storms, and is often directly injected into the polar regions.

Geomagnetic storms and substorms can have significant impacts on Earth and space systems, from inducing currents in large power grids to harming satellite circuitry and on-board data Allen et al. [1989]. Because of the potential damage of such events, any ability to forecast a storm could allow operators to prevent or mitigate problems in their systems. Because of the large correlation of CMEs with geomagnetic storms Yermolaev and Yermolaev [2006], it can be estimated that our forewarning time is the difference between observing a CME (via visual or X-ray methods) and its propagation time plus magnetospheric interaction time. This time can be anywhere from one to five days, depending on the speed of the CME and how it interacts with the interplanetary medium Zhang et al. [2007]. With a light delay of only eight minutes, this is ample time to see a storm approaching Earth and for operators to react, but a problem lies in the fact that storms are poorly predicted with such lead times Weigel et al. [2006]. Some storms have slow onsets, some spike suddenly; some have high velocities, and some coincide with large amounts of high-energy particles; no single factor has yet proven to be a good predictor for storms, and while prediction has gradually improved over the years, there remains room for further study.

All of these processes tend to couple earthwards with the plasmasphere, by transferring plasma and radiation from the interplanetary medium down into the Earth's magnetic

influence.

1.1.2 Plasmasphere

Discovery

The plasmasphere was largely unknown until the beginning of the space age, being found both through analyses of very low frequency radio waves and in-situ spacecraft measurements. Previously it was believed that electron density decreased continuously from the ionosphere to the interplanetary medium. These experiments showed that the Earth had an envelope of cold plasma around it that ended in an abrupt boundary, and varied in location and density gradient with geomagnetic activity Lemaire [1998].

Processes

The plasmasphere is interconnected with the rest of the magnetosphere, the radiation belts, and the ionosphere. While many of the specifics of this interaction are still not fully understood, some parts have been observed and explained to a reliable degree of accuracy.

At the lowest level, photoionization of oxygen in the ionosphere produces excess electrons that get transferred up into the plasmasphere along magnetic field lines bringing energy/heat along with it. There is also an upward daily "refilling" flux until a saturation point is reached, bringing the lower bounds of the plasmasphere into equilibrium with the upper ionosphere. This flux also typically reverses on the night side, sending electrons back down into the ionosphere.

During periods where the location of the plasmopause is quickly brought earthwards, or a new plasmopause is established, plasma caught outside the plasmopause is known to be magnetically convected outwards and sunwards [Carpenter and Lemaire, 1997], termed "eroding".

At times, the plasmasphere becomes distorted at the plasmopause due to dayside reconnection, causing bulges that can become elongated and detached during co-rotation, usually across the dusk side. These extended segments of plasma are known as "plumes" and show

up as a peak in density in a normally empty plasmatrough. These plumes also often occur with, and possible because of, enhanced magnetospheric activity [Elphic et al., 1996].

Leave off with list of things that are not well understood and how work in thesis approaches them.

1.1.3 Radiation Belts

Discovery

The radiation belts that surround Earth, known as the Van Allen Radiation Belts, are two (occasionally three Darrouzet et al. [2013]) bands of energetic particles encircling the planet. The existence of such bands was theorized based on knowledge of magnetically trapped motion, and results from rocket soundings that found more radiation in the auroral regions than at the equator. The beginning of the space age allowed particle counters to be sent up on Explorer 1 and Explorer 3, finding radiation far beyond what was anticipated, but concentrated into bands of high density Newell [2011].

Processes

The outer radiation belt is filled with particles (mostly electrons) pulled from the solar wind and trapped by the magnetosphere, and occasionally lost when the magnetopause moves back inward. The inner belt tends to be filled by heavier particles (electrons and protons) coming up from the ionosphere, and is overall less variable than the outer belt Darrouzet et al. [2013]. The slot region between the two is formed by the interaction of energetic particles with very low frequency (VLF) waves, leading to particle loss to the atmosphere Fung et al. [2006].

The various forms of particle movement are shown in Figure 1.2. The primary components being the drift motion leading to the ring current, and the bounce motion leading to the existence of belts of radiation. As particles approach the "Mirror point", a slight angle between the motion and the curvature of the magnetic field line lead to a force opposing

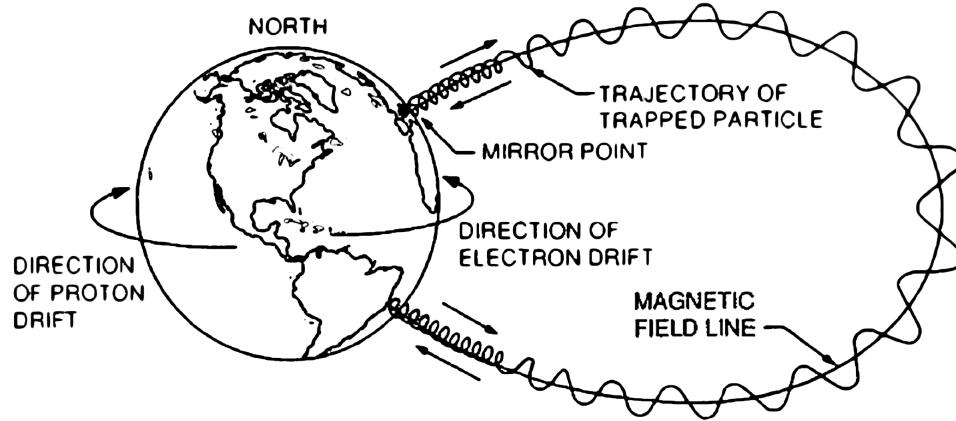


Figure 1.2: Motion of magnetically trapped particles Walt [1994]

the motion along the line, eventually mirroring the particle back in the direction it came from. Since this applies to all particles within a certain range of energies and pitch angles, the collective sum of trapped particles forms the radiation belts. By modeling the particle mass, momentum, and the magnetic field strength of a given dipole magnetic field, approximations can be made regarding what amount of particles will become trapped in the field, and what amount will be lost to scattering [Young et al., 2008].

The azimuthal (equatorial) drift of ions in the radiation belts is what leads to the ring current. When increased geomagnetic activity causes a change in particles in the radiation belts, this leads to a change in the ring current, which perturbs the Earth’s magnetic field noticeably. This perturbation is the basis for the D_{st} index used to gauge magnetic activity.

The radiation belts also have an impact on the plasmasphere by acting as an occasional source of low energy particles and a sink for high energy particles. The plasmasphere also acts on the radiation belts via the VLF waves, energizing electrons out of the plasmasphere and into the radiation belts, or providing particles already in the belts the energy needed to become untrapped Darrouzet et al. [2013]. While the outer limits of the plasmasphere and the outer radiation belt often coincide and react similarly to geomagnetic activity, they can become separated during geomagnetically active times Darrouzet et al. [2013]. An example of this variation in relative position is shown in Figure 1.3.

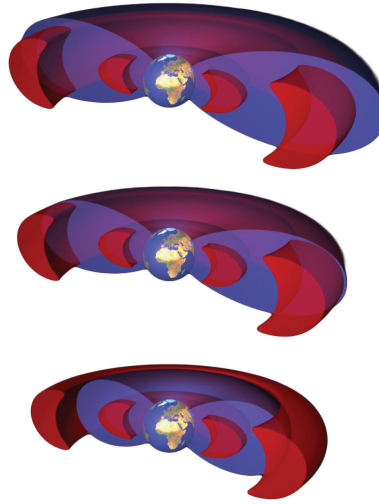


Figure 1.3: Relative position of plasmasphere (blue) and radiation belts (red) with varying geomagnetic activity levels Carreau [2013].

Another source/sink of energy for particles in the radiation belts (or general magnetospheric plasma) is via Alfvén waves [Keiling, 2009]. These waves are composed of oscillations of particles traveling along magnetic field lines, carrying both energy and field-aligned currents as they propagate. By moving energy along the field lines, Alfvén waves also couple the various distinct sections of plasma around Earth.

denton paper for plasmasphere bounce motion [Young et al., 2008] and density along field line (cite?)
correlation with plasmasphere? Mention radiation belt in ring current section and how they're independent.

1.1.4 Statistical Modeling of Magnetosphere and Plasmasphere

Initial forecasts were based on an observed time delay between sunspots and geomagnetic storms [Richardson, 1936]. It then advanced to a basic theory involving electromagnetic interactions in the magnetosphere Chapman and Ferraro [1931]. There now exist entire services dedicated to executing MHD-based models of the magnetosphere CCMC, as well

as multi-year, multi-institution efforts to survey the general statistics of modeling and forecasting of extreme events Ghil et al. [2011].

The convergence of the advancement in both statistical and MHD-based simulation has led to a situation where the scientific community has the capacity for monitoring space weather in real time, and forecasting the near-Earth effects. There have been efforts to test the forecast performance of select models over a small number of geomagnetic events [Bala and Reiff, 2012, Tsyganenko and Sitnov, 2005, Zhang et al., 2006, Yermolaev and Yermolaev, 2006]. However no research has been done that involves the analysis of long-term forecasting performance of these models and comparison of the results with existing methods.

Three main metrics of magnetospheric activity are seen throughout the literature; the K_p index: a measure of magnetosphere convection caused by currents induced by a changing plasma sheet (and indirectly from the global convection field strength) [Thomsen, 2004]; the AE index: a measure of electrojet activity based on the maximum and minimum field strength measurements from stations at auroral latitudes [Davis and Sugiura, 1966]; and the previously mentioned D_{st} index based on field perturbations caused by a changing ring current.

Models specific to the plasmasphere and plasmatrough include Carpenter and Anderson’s ISEE/Whistler Model of Equatorial Electron Density in the Magnetosphere, which empirically derives the location and density of the saturated plasmasphere and plasmatrough [Carpenter and Anderson, 1992]. Looking at ISEE 1 data for drops in number density of at least a factor of 5 across half an L-shell, they state that the inner edge of the plasmopause is located at $L_{ppi} = 5.6 - 0.46K_{pmax}$, with K_{pmax} as the maximum value of K_p (an index averaging 11 mid-latitude stations in the previous 24 hours, and L being the set of magnetic field lines at a distance of L Earth radii at the magnetic equator. This specifies the outer boundary of the plasmasphere, and from there the density is defined inwards as $n_e = n_{eL_{ppi}} \cdot 10^{-(L-L_{ppi})/\Delta pp}$, where $n_{eL_{ppi}}$ relates day number, sunspot number, whistler profiles, and multiple year long perturbations in an exponential fashion shown as

$n_e(L, d, \bar{R}) = 10^{\Sigma x_i}$. L_{ppi} and Δpp are empirically derived plasmopause location and width, respectively. x_1 is a whistler reference profile, and indices 2-4 represent perturbation values for annual, semiannual, and solar cycle variations. The exact numbers in the density profiles vary slightly between a midnight-06 MLT model, and a 06-15 MLT model, based on the passes selected for each section.

Gallagher et al. [2000] create a Global Core Plasma Model which combines empirically derived models of the ionosphere, plasmasphere, and magnetosphere. For the plasmasphere it links plasma density and magnetosphere conditions by fitting Carpenter's equation, but replacing their piecewise dependence on MLT with a sinusoidal term along with extra factors to account for the post-dusk bulge while still keeping the plasmasphere model continuous. At the most basic level, the plasmasphere component reduces to an exponential equation of the form $n_{ps} = 10^{gh} - 1$, where g and h are terms relating to the inner plasmasphere and plasmopause, combining sunspot number, day of year, and a plasmopause gradient term that accounts for the MLT dependence in the form of $\Delta_{pp} = 0.036 \cdot \sin(\frac{2\pi(MLT-6)}{24}) + 0.14$. They also link plasmasphere filling time to K_p , stating it starts at 3.5 MLT and fills until a time of $\Phi_{TP} = 0.145K_p^2 - 2.63K_p + 21.86$ hours Gallagher et al. [1995].

Moldwin et al. [2002] build on Carpenter's model by taking CRRES data and the same plasmopause detection parameters as Carpenter, finding 969 plasmopause detections compared to the 40 used to derive the model in [Carpenter and Anderson, 1992]. Using the abundance of data they do statistical analyses such as showing a least squares linear fit between increasing K_p and decreasing L-shell of the plasmopause of the form $L_{pp} = (5.39 \pm 0.072) - (0.382 \pm 0.019) \cdot K_p(max)$ with a correlation of 0.548. They also find that if they limit this to plasmopause crossings between 09 and 15 MLT, the linear correlation increases to 0.727.

O'Brien and Moldwin [2003] finds that using auroral electrojet (AE) or disturbance storm time (D_{st}) indices work better than K_p for determining plasmopause location. They use the same plasmopause crossings as [Moldwin et al., 2002] and model them against hourly

changes in the ring current (via D_{st}) or 1-minute changes in the auroral electrojet currents (AE). They take the maximum (or minimum, as required) of each index over a varying range of hours, from a start of up to 72 hours before crossing up to end of at least 6 hours before crossing, and fit a basic linear model. Their three best models were a basic linear fit of L_{pp} to $\max_{-36,-2} K_p$, $\max_{-36,0} AE$, and $\log_{10}(\min_{-24,0} D_{st})$. Using a bootstrap analysis for significance, all three models were indistinguishably similar in the root mean square error (RMSE) of their respective models, except for AE having significantly less error in the night sector than D_{st} . Making the model slightly more advanced by including a MLT dependence and periodic terms allows a bulge to be approximated, and finds that the allowing local time to be accounted for significantly (at the 95% confidence level) reduces the error of the model, but still shows no significant difference between models of the same complexity.

As for models specifically of the plasmatrough, Loto'aniu et al. [1999] take ground based Ultra Low Frequency (ULF) wave measurements, then map them to plasma mass densities between $L = 4.5$ and $L = 10$ via the Tsyganenko T89 magnetic field model and an R^{-4} plasma mass density profile. These estimated values were then compared to in-situ measurements from the CRRES satellite and found that this technique can, under specific conditions, accurately measure plasmatrough mass density.

Takahashi et al. [2006] take a similar approach, but approximate ULF waves from the CRRES satellite directly, instead of using ground stations, and then map that to mass density values. By using the electric field spectra on the satellite and finding a fundamental frequency of the toroidal waves, they estimate mass density with a combination of theoretical model and empirical observations. The magnetic field model used is either T89 or T96, dependent on K_p or D_{st} respectively. Instead of an R^{-4} dependence for the mass density model, they use $\rho = \rho_{eq}(LR_E/R)^{0.5}$, and then combine with frequency observations via $\rho_{eq_est} = \rho_{eq_theory}(f_{1_theory}/f_{1_obs})^2$.

Takahashi (2010), Kondrashov 2014, Denton (2006, 2015), Min 2013, Tsyganenko models

King and Papitshvili OMNI data reference

Discuss current results based on plasmopause but current study focused on plasmatrough (Denton and Takahashi show most data in plasmatrough)

Make connection to each paper with a section in chapter 2.

Chapter 2: Methods

This work utilized a number of linear and nonlinear methods of analysis and modeling, including Auto-Regressive Moving Average models with eXogenous inputs (ARMAX) and neural net models. No single method is ideal, and using many methods is better for insight, especially for nonlinear/complex systems. The details of their application will be expanded upon in their respective sections.

2.1 Linear

2.1.1 Overview

Due to its simplicity and ease of application, linear models are used in practically all fields as a first attempt to discover information about the data and any potential relationships. In Space Physics, where the underlying behavior of a complex system is not theoretically known, and in-situ measurements are sparse, linear models are often the first step towards understanding what components are related and to what degree. Sometimes this leads to understanding unexpected complexities in a system. **Example. Lemaire p.183 heavier ions in outer plasmasphere than inner plasmasphere? Correlation between plasmopause and radiation belt boundary?**

2.1.2 ARX

Impulse response systems are systems in which the output (a response) is driven by a linear sum of coefficients of an input (a series of impulses). A simple example would be making a loud noise in a concert hall. The response will be the unique echoes and reverberations

created by the initial driving sound, and with enough signal, a statistical model can be generated that will map the input sound to a response echo. In the magnetosphere, the most used example is an impulse of v_{Bs} driving the Auroral Electrojet (AE/AL) index Bargatze et al. [1985], or the Disturbance Storm Time (D_{st}) index Clauer et al. [1981], also shown in Figure 2.1.

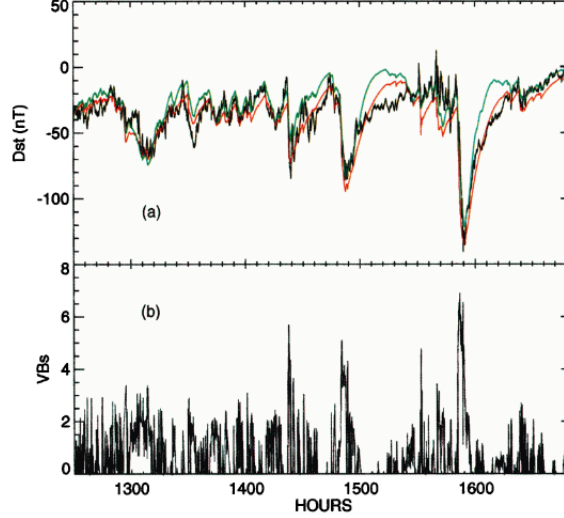


Figure 2.1: DST (black), nonlinear autoregressive exogenous (ARX) model (red), Burton et al 1975 model (green). (b) v_{Bs} impulse as input. Klimas et al. [1998]

This plot shows how different models are used to predict magnetospheric variables with varying amounts of success. In this proposal, what starts as a simple Box-Jenkins model of the form Weigel [2007]:

$$x(t) = c + \sum_{j=0}^m a_j f(t - j\Delta t)$$

can be modified with an auto-regressive component to be an autoregressive model with exogenous inputs (ARX) such as that used in Klimas et al. [1998], taking the form:

$$\hat{x}(t + \Delta t) = \sum_{i=0}^l a_i \cdot x(t - i\Delta t) + \sum_{j=0}^m b_j \cdot f(t - j\Delta t) + c \quad (2.1)$$

Where m and l are the number of coefficients desired for including previous data points in the prediction, and c is a factor to remove the mean offset from the data. Note that in some cases the starting value of the iterators can be individually increased if there is a known delay in response time or there is a desire to predict further into the future. In Klimas et al. [1998], second order equations ($m = 2$) were used with anywhere from one to four driving coefficients, but in practice any number of coefficients and any number of driving variables can be used up to some fraction of the number of data points that allows the coefficient matrices to be solved for.

There generally is a limit to the usefulness of large-lag data Ghil et al. [2011]. By looking at a plot of the cross correlation relative to the number of coefficients, a limit will generally be seen where adding more coefficients no longer reduces error in the model. By creating a threshold of change in fit per coefficient added (perhaps via a bootstrap method), the minimum number of coefficients needed to optimally model the system can be determined.

By constructing a linear system of equations from Equation 2.1, the coefficients can be solved for in a general matrix form (where, in this case, $l = m$):

$$\begin{pmatrix} x_0 & \dots & x_{l-1} & f_0 & \dots & f_{l-1} & 1 \\ x_1 & & x_l & f_l & & f_l & 1 \\ \dots & & & & & & \\ x_{N-l} & \dots & x_{N-1} & f_{N-l} & \dots & f_{N-1} & 1 \end{pmatrix} \begin{pmatrix} a_0 \\ \dots \\ a_{l-1} \\ b_0 \\ \dots \\ b_{l-1} \\ c \end{pmatrix} = \begin{pmatrix} x_l \\ x_{l+1} \\ \dots \\ x_N \end{pmatrix}$$

This is a linear model for the behavior of a system. However, it has been shown that the set of coefficients describing the response of a system can change with storm intensity Klimas et al. [1998], the time scale modeled Vassiliadis et al. [2004], and even the time of day Bargatze et al. [1985]. This creates a very large number of possible directions for research,

from predicting storm onsets, to predicting storm intensities, to modeling the overall shape and behavior of a storm, as well as all of the other possible interactions outside of storm-time.

2.1.3 ARMAX

A class of model known as an Auto-Regressive Moving Average with eXogenous inputs model (ARMAX) is often used in time series analysis to combine the effects of persistence, linear dependence, and an average that changes with time. It makes a slight change on the ARX model in Equation 2.1, adding the moving average term:

$$\hat{x}(t + \Delta t) = \sum_{i=0}^l a_i \cdot x(t - i\Delta t) + \sum_{j=0}^m b_j \cdot f(t - j\Delta t) + \sum_{k=0}^n c_k \cdot g(t - k\Delta t) + c_{t+\Delta t} \quad (2.2)$$

Clean up notation (c_t or c_n ? All go 0 to t ?)

2.1.4 Applicability

As implied by the name, an ARMAX model is suitable for analysis of a time-dependent linear system where the value of a measurement is determined by its own persistence, an external variable, and some factor that contributes to a moving average with time. Most linear systems can be encapsulated by this framework, some even being overspecified with this level of accounting for variability.

2.1.5 Caveats and Biases

There will be a number of things that, ideally, must come together to make this kind of data prediction work. For one: ARX methods can often be heavily dependent on a concept known as "persistence", whereby the best prediction for a variable at any time is that same variable at the last measured time step. For example, if the high temperature today is 70°, it is fairly likely that the high temperature tomorrow will be near 70°. Too much

reliance on persistence forecasting, though, and predictions can lose their usefulness. Figure 2.2, for example, shows how a model can achieve high correlation with persistence, but be almost entirely useless for predicting events before they happen since the spikes are never anticipated, just modeled after they’ve already been seen.

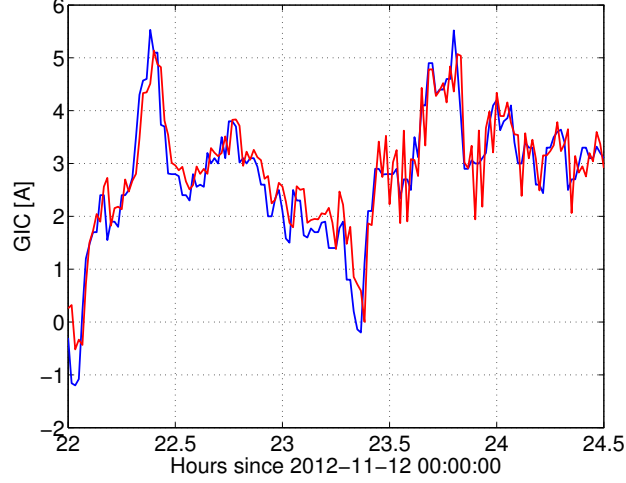


Figure 2.2: Persistence forecast; model in red

In this case, it is clear that the most recent measurement has the most weight in a forecast. For day-to-day behavior, this is acceptable as being part of the behavior of the system. For the forecasting of extreme events, however, another metric must be used that measures the ability of the model to predict events at or before their actual occurrence, while simultaneously avoiding predicting events that do not happen. One method for comparing models in this fashion is by using the Heidke Skill Score Heidke [1926], Brier and Allen [1951], which is based on the quantity:

$$S = \frac{R - E}{T - E}$$

where R is the number of correct forecasts, T is the total number of forecasts, and E is the number expected to be correct by, in this case, a persistence forecast. This can be adapted to either consider a range of "correctness", or a binary threshold to be met. It may also be desired to assign a cost-weighting to success rates. If, say, it costs \$1 million to prepare

a power grid for a storm, 10 false alarms to every one storm gets costly unless successfully preparing for that one storm saves \$1 billion. To do this, a measure of the utility of a forecast can be quantified Weigel et al. [2006]:

$$U_F \equiv BN_H - CN_{\bar{H}} > 0$$

Where N_H is the number of correct forecasts, $N_{\bar{H}}$ is the number of false alarms, C is the cost of taking mitigating action, and B is the benefit from correctly taking mitigating action. This method has caveats discussed in Weigel et al. [2006], but is a useful metric for forecast utility when costs are known, and some measure of success can be determined.

The other major problem in forecasting is that of lead time. Being able to forecast a storm one minute in advance is generally not enough time for operators to take mitigating action.

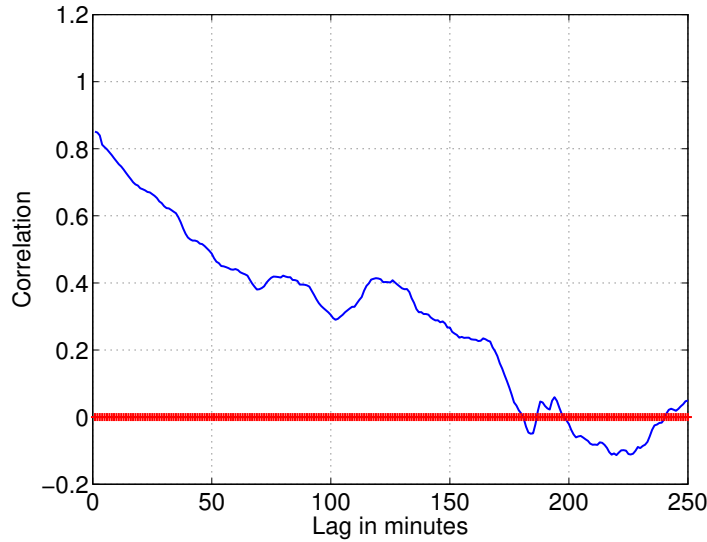


Figure 2.3: Correlation vs lags

Figure 2.3 shows a set of predictions made for autocorrelation in geomagnetically-induced currents (GIC). This metric is a measure of how much electric currents in the magnetosphere induce currents in ground-based electrical systems. The predictions were made further and further in time from the current magnetic field and GIC measurements,

with decreasing accuracy as the predicted time got further from the current time. While an accurate prediction can be made one minute in advance, a prediction 3 hours in advance has almost no correlation with what actually happens. This is the main problem that this dissertation hopes to address.

Mean vs Median

The question of whether to use means or medians for analysis is based on what facets of the data are most important to the research. Since means biased towards outliers and medians biased against them, the decision rests on how much weight should be given to outliers (or extreme values) in a study. For example, when looking at long-term solar wind variables, intermittent spikes may not be relevant to the overall pattern of behavior being analyzed, but knowing that on a short time scale a certain day had a noticeable spike may be important. In the former case, using the median would likely be best, and using the mean for the latter. However, space physics often deals with skewed distributions and sparse data, leading to an uncertainty of which method is best, so both are and analyzed with their respective traits in mind. [Numerically specific result](#)

Effects of time averaging

Similarly to the mean vs median question, the decision on if/how much to average the data over time will affect the resulting time series to be biased against intermittent spikes in value. The more time added to any particular average, the less impact any short-term changes will have on the final value.

2.1.6 Summary

reiterate relevance

2.2 Nonlinear

2.2.1 Overview

While many nonlinear systems are approximated by a number of localized linear models for the sake of simplicity and ease of interpretation, the design and implementation of nonlinear models has become greatly simplified in recent years. Their use allows for determining nonlinear structure without pre-assuming any localization of the data, and as such were used to attempt forecasting in this dissertation. The first choice was a model based on neural networks Hernandez et al. [1993], Bala and Reiff [2012] which approximates a non-linear system given a set of training data. The usefulness of this is apparent in a few key points: the weights of contribution of any particular variable to a system will likely be nonlinear in some fashion (e.g. a ground station's measurements will depend on sunlight heating the ionosphere which depends on latitude, time of year, and time of day), and allowing for the non-linear effects of saturation where perhaps the magnetosphere will behave differently after reaching certain levels of particle density or electric potential, rather than directly scaling regardless of limits.

Another algorithm known as Principal Component Analysis (PCA) can be used to take the large number of possible variables and define an orthogonal set of vectors that most efficiently encapsulate the variance in the data. By doing this, the number of variables needed for computing any linear or non-linear algorithm can be reduced and optimized, making predictions quicker while maintaining most of the predictive benefits of using all possible data, as well as indicating which variables contain the most information relevant to the predictions.

2.2.2 Neural Networks

2.2.3 Applicability

Nonlinear models are applicable when a system has more complexity than can be encapsulated by a linear model. Since they're usually a class of model that trains adaptive weights

that can be tuned by known inputs and outputs, they're especially useful for systems where a large amount of training data are available.

2.2.4 Caveats and Biases

Nonlinear models can be susceptible to overfitting, since they inherently attempt to fit more complexity than a linear model, but can also be controlled via the number of inputs and weights used. They also may suggest more structure than might truly exist. Both of these problems are lessened by training with more data, if available. Figure 2.4 shows a comparison of predicting equatorial mass density (ρ_{eq}) with the $F_{10.7}$ index and solar wind velocity (V_{sw}). The neural net model shows much more structure than the linear model despite being given the same data. Whether that structure reflects any real physical phenomenon, however, is a difficult problem to answer.

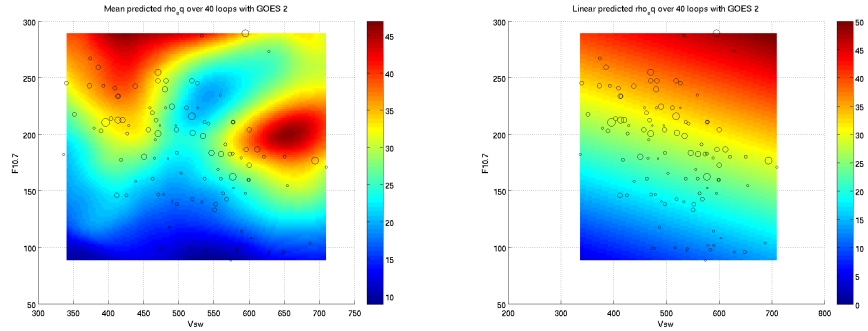


Figure 2.4: Nonlinear model vs linear model of ρ_{eq}

Fix figure to be showing the same scales

2.2.5 Comparison to Linear Model

Nonlinear models differ from linear models by incorporating some method for accounting for effects within a domain that are not seen across the entire domain. Though both models can be given the same inputs, and trained on the same outputs, the models themselves can fundamentally differ. Linear models are also generally simple to interpret (e.g. $y = 2 * x$

means for every change in x , y changes by double that amount.) Nonlinear models, on the other hand, often have no simple interpretation and must be approached by testing for a range of parameters in the model to map out resulting outputs and make some interpretation of the underlying structure.

Nonlinear models can be compared to a linear model of the same data in order to assess the usefulness of accounting for nonlinear features. If both models result in similar correlation values, it can be said that the nonlinear model offers no extra insight into the structure of the system and the relationships therein.

2.2.6 Summary

reiterate relevance

Chapter 3: Measurements

The measurements can, to a certain extent, be broken into three main components: those pertaining to the solar wind, those from the magnetosphere in general, and those specific to the plasmasphere. An example of all the combined data sources is shown in Figure 3.1, providing solar wind variables B_z , V_{SW} ; solar variable $F_{10.7}$, plasmatrough variable ρ_{eq} , and magnetosphere/plasmasphere variable D_{st} .

Similarly, Figure 3.2 shows the same variables before, during, and after the March 1989 geomagnetic storm as seen by GOES 6. This makes it clearer how the variables are interrelated, notably how short-timescale effects such as drops in B_z and D_{st} are connected, or longer time scale changes on $F_{10.7}$ and V_{SW} are related. This figure also shows how the sparse availability of ρ_{eq} created challenges for this study, as discussed later.

3.1 Solar Wind

Solar wind is the largest driver of particle density in the magnetosphere [cite](#), and as such is an important input for a plasmatrough model. Conditions such as magnetic field orientation and particle velocity are important considerations for whether the plasmasphere is expected to be compressed, saturated, or experiencing high variability. By adding these to a model that account for time delayed inputs, their effects can be accounted for and aid in categorizing the state of the plasmatrough.

3.1.1 Source

Solar wind data for this dissertation is provided by the OMNIWeb service [cite](#), a combination of many satellites' data to create a uniform, high resolution, near-Earth set of solar wind measurements. The one-hour resolution dataset was used since the study is concerned

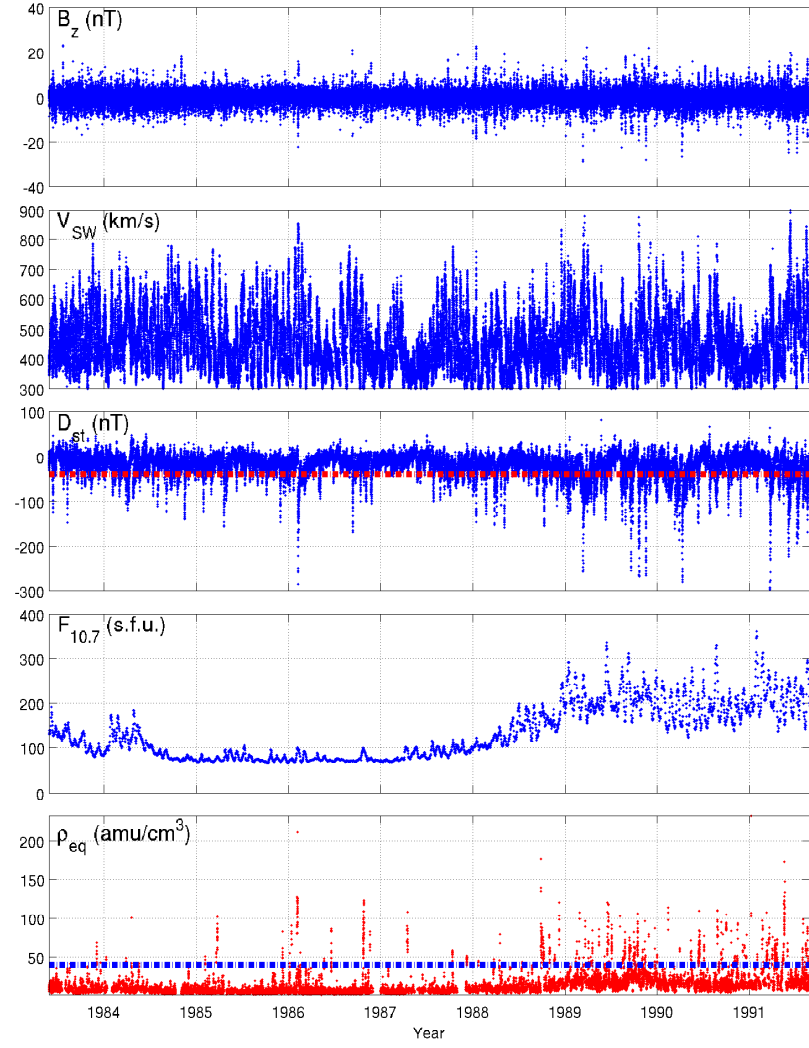


Figure 3.1: Data from GOES 6 with dashed lines indicating default storm thresholds

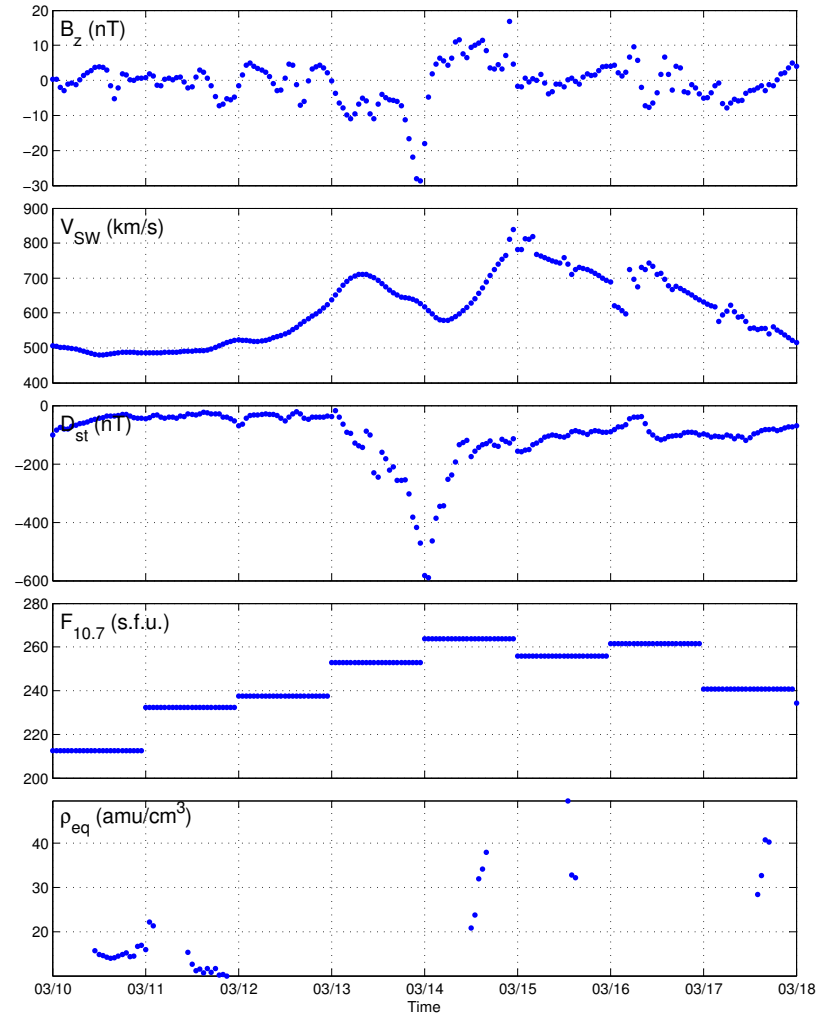


Figure 3.2: Data from GOES 6 around March 1989 geomagnetic storm

with effects on timescales of longer than an hour, and to more easily compare to the other data sources used.

However, since the OMNIWeb data has gaps for some of the variables, Kondrashov et al. [2014] was used as they reliably reconstruct gaps to make a continuous, uniform data set. They used Singular Spectrum Analysis with synthetic gaps created by shifting real gaps from 1984-1995 data onto 1996-2007 data so that verification data would exist to test the effectiveness of their model.

3.1.2 Coverage

Low resolution OMNI data is available from 1963 to present, but only the years of 1983-1992 were considered as they overlapped with the other data sets of interest. The data covers, but is not limited to: magnetic field strength in all three dimensions; solar wind proton density and temperature; the K_p , AE , $F_{10.7}$, and D_{st} indices; and varying levels of proton flux.

3.1.3 Data preparation

The only data cleaning required on the OMNI dataset was to convert fill values of 999.9 and 9999 to NaN, to be appropriate for use in data analysis. Of the variables included (see Coverage), B , B_z (GSE and GSM), and Solar wind proton density and plasma speed all were missing about 35% of their data. The AE index was missing about 7% of its data, and all other variables were provided complete.

3.2 Geomagnetic

Geomagnetic data cover everything inside the magnetopause, but in this study will tend to refer specifically to information in the magnetosphere but not in the plasmasphere or ionosphere.

3.2.1 Source

The data come from Takahashi et al. [2010], which takes data from the Geostationary Operational Environmental Satellites (GOES) and uses a set of magnetic field models to relate Alfvén waves to equatorial mass density (ρ_{eq}). By taking magnetic field vectors and applying spectral analysis, they find a set of fundamental harmonic frequencies of toroidal waves. Through testing, they find a strong linear dependence of the 27-day average third toroidal frequency ($f_{T3.27d}$) on the similarly averaged $F_{10.7}$ index, of the form: $f_{T3.27d}(mHz) = 37.5 - 0.0972F_{10.7.27d}(sfu)$. From there, they also find a linear relationship to the averaged ρ_{eq} in the form $\log(\rho_{eq.27d}) = 0.421 + 0.00390F_{10.7.27d}$, effectively linking the derived toroidal frequency to ρ_{eq} .

3.2.2 Coverage

The GOES satellites used in this study cover the years from 1980 to the end of 1991, often with overlapping years between satellites. The satellites themselves held a geostationary orbit at around $6.62 R_E$ and collected data on a roughly 3-second cadence [GOE], which was then transformed onto a 10-minute cadence. Their position means they’re almost always measuring properties of the plasmatrough, the region devoid of dense plasma just outside the plasmasphere.

3.2.3 Data preparation

The data were prepared by replacing fill values of 9999 with NaN and then narrowing results to only one satellite at a time to ideally remove any effects of satellite position or calibration from the results. These data still had many temporal gaps, so they were scaled onto a uniform 10-minute grid leaving missing points as NaN, but allowing for easier data analysis and comparison to other data sets.

In order to align the GOES data with the OMNI 1-hour cadence, the median of all existing values within 30 minutes on either side of each hour was taken. For hours with no existing values, a NaN was inserted to keep the cadence uniform. Two other methods were

attempted: using the mean of each hour, centered on the hour, and using the median of the data on or within an hour after each time point (e.g. 7:00-7:59 would be combined into the 7:00 point). Both were found to have minimal effect on results.

3.3 Plasmasphere

Plasmasphere data covers the inner regions of the magnetosphere, bounded by the plasma-pause on the outer edge and the ionosphere on the inner edge. This puts it at a typical distance of $L = 3 - 5R_E$.

3.3.1 Source

Data for the plasmasphere also comes from the GOES and OMNI datasets previously discussed, but are often calculated as extensions of directly measured data either onboard the satellites or from ground stations, depending on the current extent of the plasmasphere and location of the satellite.

3.3.2 Coverage

Since the data come from the same sources as that of the magnetosphere, the coverage is largely the same with specifics covered in Takahashi et al. [2010], where any error associated with temporary conditions is overshadowed by the variance in effectiveness of the model itself.

3.3.3 Data preparation

The same preparation done for the magnetosphere applied to the plasmasphere data. Some specific analysis done in Takahashi et al. [2010] discusses how the spacecraft’s geomagnetic location affected their ability to detect the necessary toroidal frequency, and thus estimate ρ_{eq} , so for some of the long-timescale averages, only certain MLTs were included. They also show that ρ_{eq} does correlate with geomagnetic activity (and, by extension, plasmapause

location), so during long periods of no activity the plasmasphere extends beyond geosynchronous orbit, leading to measurements of ρ_{eq} reflecting density in the plasmasphere and not the plasmatrough.

Chapter 4: Analysis

4.1 Overview

While Figure 3.1 shows an overview of the most pertinent variables used in this study, some further analysis was done to determine any potential biases introduced by specifics of the satellite motion or derivations used. For example, Figure 4.1 shows that not only did data availability vary significantly with local time, but the values themselves vary significantly.

Cite that this is known (dawn vs dusk, etc)

This trend similarly holds for Magnetic Local Time (MLT), a time basis where "noon" points directly magnetically upstream in the solar wind. **Does it even make sense to compare ρ_{eq} to local time?**

4.2 $F_{10.7}$ Dependence

Takahashi et al. [2010] showed a strong correlation between the 27-day averaged $F_{10.7}$ index of solar activity and the averaged equatorial mass density (ρ_{eq}). This was chosen as a starting place for verifying the data analysis routines developed for this dataset, so as to show that data input, averaging, and interpolation were all done in a reasonable and reproducible manner. Figure 4.2 shows the strong correlation seen previously, and reasonably reproduces Figure 13.b from Takahashi et al. [2010] for the years covered by GOES 6.

4.3 Linear Correlations

This dependence was further investigated, and extended, by creating a simple one-time-lag linear model for each major variable in the database as well as combinations of some to

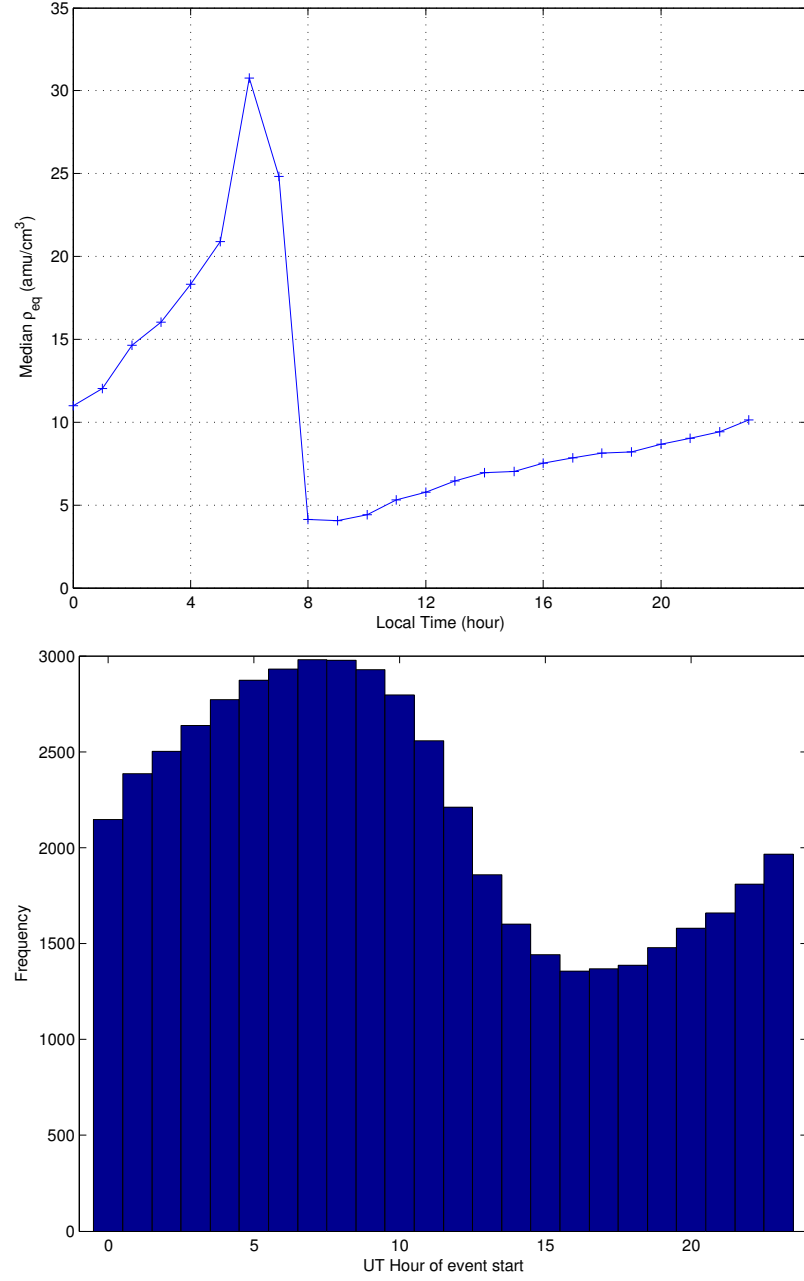


Figure 4.1: Median ρ_{eq} binned by local time, and availability of ρ_{eq} with local time.

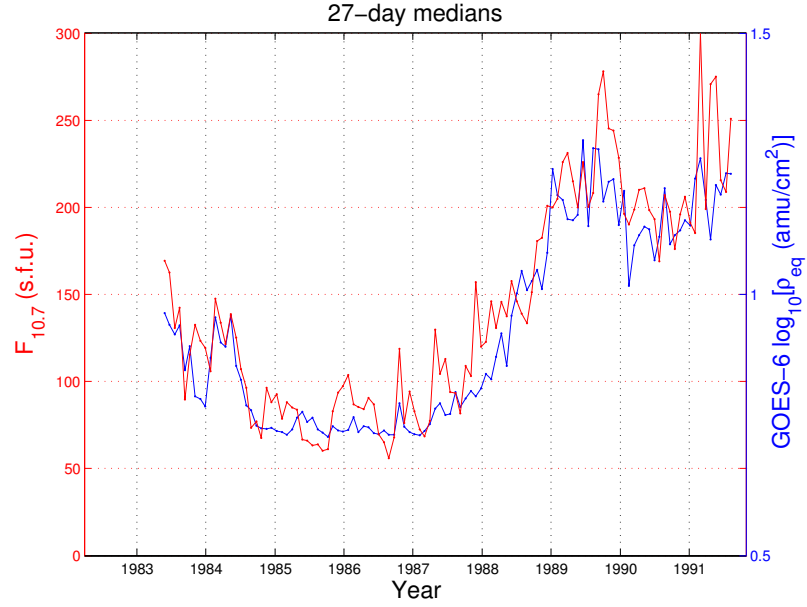


Figure 4.2: Comparing $F_{10.7,27d}$ and $\log(\rho_{eq,27d})$ using GOES 6 data

test for independent contributions to the correlation. The models were trained on half of the dataset and tested on the other half for each satellite, and this was repeated with new random samples 100 times and then the median correlation values were taken. The results are shown in Table 4.1.

| | GOES 2 | GOES 5 | GOES 6 | GOES 7 |
|----------|--------|--------|--------|--------|
| doy | -0.08 | +0.10 | -0.05 | +0.06 |
| MLT | -0.09 | -0.09 | -0.04 | -0.05 |
| Bz | +0.17 | -0.12 | +0.08 | -0.08 |
| Vsw | -0.04 | +0.29 | +0.06 | -0.06 |
| Dst | +0.27 | +0.66 | +0.06 | +0.22 |
| Rhosw | +0.34 | +0.63 | +0.07 | +0.34 |
| F107 | +0.42 | +0.14 | +0.49 | +0.42 |
| Bz+Vsw | +0.09 | +0.19 | +0.12 | -0.11 |
| Dst+F107 | +0.45 | +0.69 | +0.53 | +0.47 |
| All | -0.10 | +0.34 | +0.61 | +0.39 |

Table 4.1: Table of linear model correlations showing the median of 100 random samples. Each sample trained on half of the data (via randomly selected rows of the least squares matrix) and tested on the other half

Look at making this (along with figures) a git submodule

It can be seen that $F_{10.7}$ almost always correlates the most with ρ_{eq} , but that there is significant variance between data from different satellites. **Including training correlations?**
Make model a 12 hour model to smooth it out a bit?

4.4 Nonlinear Correlations

Similarly for a simple neural net model with one time lag, Table 4.2

| | GOES 2 | GOES 5 | GOES 6 | GOES 7 |
|----------|--------|--------|--------|--------|
| doy | +0.20 | +0.31 | +0.13 | +0.11 |
| MLT | +0.18 | +0.12 | +0.16 | +0.10 |
| Bz | +0.14 | +0.23 | +0.07 | +0.05 |
| Vsw | +0.14 | +0.24 | +0.07 | +0.06 |
| Dst | +0.16 | +0.05 | +0.11 | +0.10 |
| Rhosw | +0.17 | +0.17 | +0.32 | +0.14 |
| F107 | +0.33 | +0.29 | +0.50 | +0.38 |
| Bz+Vsw | +0.17 | +0.26 | +0.10 | -0.04 |
| Dst+F107 | +0.22 | +0.20 | +0.45 | +0.34 |
| All | | | | |

Table 4.2: Table of nonlinear model correlations showing the median of 100 random samples. Each sample trained on half of the data (via randomly selected rows of the least squares matrix) and tested on the other half

Appendix A: An Appendix

This is an appendix. Here is a numbered appendix equation:

$$a^2 + b^2 = c^2. \tag{A.1}$$

Bibliography

- Access to GOES SEM data. URL <https://www.ngdc.noaa.gov/stp/satellite/goes/dataaccess.html>.
- J. Allen, L. Frank, H. Sauer, and P. Reiff. Effects of the March 1989 solar activity. *EOS Transactions*, 70:1479, November 1989. doi: 10.1029/89EO00409.
- R. Bala and P. Reiff. Improvements in short-term forecasting of geomagnetic activity. *Space Weather*, 10:S06001, June 2012. doi: 10.1029/2012SW000779.
- L. F. Bargatze, D. N. Baker, E. W. Hones, Jr., and R. L. McPherron. Magnetospheric impulse response for many levels of geomagnetic activity. *Journal of Geophysical Research*, 90:6387–6394, July 1985. doi: 10.1029/JA090iA07p06387.
- G. Brier and R. Allen. Verification of Weather Forecasts. *Compendium of Meteorology*, pages 841–848, 1951. URL <http://archive.org/stream/compendiumofmete00amer#page/840/mode/2up>.
- D. L. Carpenter and R. R. Anderson. An ISEE/Whistler model of equatorial electron density in the magnetosphere. *J. Geophys. Res.*, 97:1097–1108, February 1992. doi: 10.1029/91JA01548.
- D. L. Carpenter and J. Lemaire. Erosion and Recovery of the Plasmasphere in the Plasmapause Region. *Space Science Reviews*, 80:153–179, April 1997. doi: 10.1023/A:1004981919827.
- C. Carreau. Earth’s plasmasphere and the Van Allen belts, September 2013. URL <http://sci.esa.int/cluster/52831-earth-plasmasphere-and-the-van-allen-belts/>.

- R. C. Carrington. Description of a Singular Appearance seen in the Sun on September 1, 1859. *Monthly Notices of the Royal Astronomical Society*, 20:13–15, November 1859.
- CCMC. Community coordinated modeling center. URL <http://ccmc.gsfc.nasa.gov/>.
- S. Chapman and V. C. A. Ferraro. A new theory of magnetic storms. *Terrestrial Magnetism and Atmospheric Electricity (Journal of Geophysical Research)*, 36:77, 1931. doi: 10.1029/TE036i002p00077.
- C. R. Clauer, R. L. McPherron, C. Searls, and M. G. Kivelson. Solar wind control of auroral zone geomagnetic activity. *Geophysical Research Letters*, 8:915–918, August 1981. doi: 10.1029/GL008i008p00915.
- F. Darrouzet, V. Pierrard, S. Benck, G. Lointier, J. Cabrera, K. Borremans, N. Y. Ganushkina, and J. D. Keyser. Links between the plasmopause and the radiation belt boundaries as observed by the instruments CIS, RAPID, and WHISPER onboard Cluster. *Journal of Geophysical Research (Space Physics)*, 118:4176–4188, July 2013. doi: 10.1002/jgra.50239.
- T. N. Davis and M. Sugiura. Auroral electrojet activity index AE and its universal time variations. *J. Geophys. Res.*, 71:785–801, February 1966. doi: 10.1029/JZ071i003p00785.
- R. C. Elphic, L. A. Weiss, M. F. Thomsen, D. J. McComas, and M. B. Moldwin. Evolution of plasmaspheric ions at geosynchronous orbit during times of high geomagnetic activity. *Geophysical Research Letters*, 23:2189–2192, 1996. doi: 10.1029/96GL02085.
- S. F. Fung, X. Shao, and L. C. Tan. Long-term variations of the electron slot region and global radiation belt structure. *Geophys. Res. Lett.*, 33:L04105, February 2006. doi: 10.1029/2005GL024891.
- D. L. Gallagher, P. D. Craven, R. H. Comfort, and T. E. Moore. On the azimuthal variation of core plasma in the equatorial magnetosphere. *J. Geophys. Res.*, 100:23597–23606, December 1995. doi: 10.1029/95JA02100.

- D. L. Gallagher, P. D. Craven, and R. H. Comfort. Global core plasma model. *J. Geophys. Res.*, 105:18, August 2000. doi: 10.1029/1999JA000241.
- M. Ghil, P. Yiou, S. Hallegatte, B. D. Malamud, P. Naveau, A. Soloviev, P. Friederichs, V. Keilis-Borok, D. Kondrashov, V. Kossobokov, O. Mestre, C. Nicolis, H. W. Rust, P. Shebalin, M. Vrac, A. Witt, and I. Zaliapin. Extreme events: dynamics, statistics and prediction. *Nonlinear Processes in Geophysics*, 18:295–350, May 2011. doi: 10.5194/npg-18-295-2011.
- J. T. Gosling, D. J. McComas, J. L. Phillips, and S. J. Bame. Geomagnetic activity associated with earth passage of interplanetary shock disturbances and coronal mass ejections. *Journal Of Geophysical Research*, 96:7831–7839, May 1991. doi: 10.1029/91JA00316.
- P. Heidke. Berechnung des Erfolges und der Güte der Windstärkevorhersagen im Sturmwarungsdienst. *Geografiska Annaler*, 8:310–349, 1926. URL <http://www.jstor.org/stable/519729?seq=4>.
- J. V. Hernandez, T. Tajima, and W. Horton. Neural net forecasting for geomagnetic activity. *Geophysical Research Letters*, 20:2707–2710, December 1993. doi: 10.1029/93GL02848.
- A. Keiling. Alfvén Waves and Their Roles in the Dynamics of the Earth’s Magnetotail: A Review. *Space Sci. Rev.*, 142:73–156, February 2009. doi: 10.1007/s11214-008-9463-8.
- A. J. Klimas, D. Vassiliadis, and D. N. Baker. Dst index prediction using data-derived analogues of the magnetospheric dynamics. *Journal of Geophysical Research*, 103:20435–20448, September 1998. doi: 10.1029/98JA01559.
- D. Kondrashov, R. Denton, Y. Y. Shprits, and H. J. Singer. Reconstruction of gaps in the past history of solar wind parameters. *Geophys. Res. Lett.*, 41:2702–2707, April 2014. doi: 10.1002/2014GL059741.
- J Lemaire. *The Earth’s Plasmasphere*. Cambridge University Press, Cambridge, U.K. New York, 1998. ISBN 9780521430913.

- T. M. Loto'aniu, C. L. Waters, B. J. Fraser, and J. C. Samson. Plasma mass density in the plasmatrough: Comparison using ULF waves and CRRES. *Geophys. Res. Lett.*, 26: 3277–3280, 1999. doi: 10.1029/1999GL003641.
- M. B. Moldwin, L. Downward, H. K. Rassoul, R. Amin, and R. R. Anderson. A new model of the location of the plasmapause: CRRES results. *Journal of Geophysical Research (Space Physics)*, 107:1339, November 2002. doi: 10.1029/2001JA009211.
- Homer Newell. *Beyond the Atmosphere Early Years of Space Science*. Dover Publications, City, 2011. ISBN 0486135659. URL <http://history.nasa.gov/SP-4211/contents.htm>.
- T. P. O'Brien and M. B. Moldwin. Empirical plasmapause models from magnetic indices. *Geophys. Res. Lett.*, 30:1152, February 2003. doi: 10.1029/2002GL016007.
- National Oceanic and Atmospheric Administration. NOAA Space Weather Scales, 2005. URL <http://www.swpc.noaa.gov/NOAAscales/>.
- R. S. Richardson. Sun-Spots and Magnetic Storms. *Leaflet of the Astronomical Society of the Pacific*, 2:133, 1936.
- R. Snare. A History of Vector Magnetometry in Space. URL <http://www-ssc.igpp.ucla.edu/personnel/russell/ESS265/History.html>.
- Willie Soon and Steven H. Yaskell. *The Maunder Minimum and the Variable Sun-earth Connection*. World Scientific, 2003. ISBN 9789812382757.
- David P. Stern. The art of mapping the magnetosphere. *Journal of Geophysical Research: Space Physics*, 99(A9):17169–17198, 1994. ISSN 2156-2202. doi: 10.1029/94JA01239. URL <http://dx.doi.org/10.1029/94JA01239>.
- K. Takahashi, R. E. Denton, R. R. Anderson, and W. J. Hughes. Mass density inferred from toroidal wave frequencies and its comparison to electron density. *Journal of Geophysical Research (Space Physics)*, 111:A01201, January 2006. doi: 10.1029/2005JA011286.

- K. Takahashi, R. E. Denton, and H. J. Singer. Solar cycle variation of geosynchronous plasma mass density derived from the frequency of standing Alfvén waves. *Journal of Geophysical Research (Space Physics)*, 115:A07207, July 2010. doi: 10.1029/2009JA015243.
- M. F. Thomsen. Why Kp is such a good measure of magnetospheric convection. *Space Weather*, 2:S11004, November 2004. doi: 10.1002/2004SW000089.
- N. A. Tsyganenko and M. I. Sitnov. Modeling the dynamics of the inner magnetosphere during strong geomagnetic storms. *Journal of Geophysical Research (Space Physics)*, 110:A03208, March 2005. doi: 10.1029/2004JA010798.
- D. Vassiliadis, R. S. Weigel, D. N. Baker, S. G. Kanekal, and A. J. Klimas. Probing the solar wind-inner magnetospheric coupling: validation of relativistic electron flux models. *Journal of Atmospheric and Solar-Terrestrial Physics*, 66:1399–1409, October 2004. doi: 10.1016/j.jastp.2004.03.025.
- Martin Walt. *Introduction to Geomagnetically Trapped Radiation*. Cambridge University Press, Cambridge New York, 1994. ISBN 9780521431439.
- R. S. Weigel. Solar wind time history contribution to the day-of-year variation in geomagnetic activity. *Journal of Geophysical Research (Space Physics)*, 112:A10207, October 2007. doi: 10.1029/2007JA012324.
- R. S. Weigel, T. Detman, E. J. Rigler, and D. N. Baker. Decision theory and the analysis of rare event space weather forecasts. *Space Weather*, 4:05002, May 2006. doi: 10.1029/2005SW000157.
- Y. I. Yermolaev and M. Y. Yermolaev. Statistic study on the geomagnetic storm effectiveness of solar and interplanetary events. *Advances in Space Research*, 37:1175–1181, 2006. doi: 10.1016/j.asr.2005.03.130.
- S. L. Young, R. E. Denton, B. J. Anderson, and M. K. Hudson. Magnetic field line curvature

- induced pitch angle diffusion in the inner magnetosphere. *Journal of Geophysical Research (Space Physics)*, 113:A03210, March 2008. doi: 10.1029/2006JA012133.
- J. Zhang, M. W. Liemohn, J. U. Kozyra, M. F. Thomsen, H. A. Elliott, and J. M. Weygand. A statistical comparison of solar wind sources of moderate and intense geomagnetic storms at solar minimum and maximum. *Journal of Geophysical Research (Space Physics)*, 111: A01104, January 2006. doi: 10.1029/2005JA011065.
- J. Zhang, I. G. Richardson, D. F. Webb, N. Gopalswamy, E. Huttunen, J. C. Kasper, N. V. Nitta, W. Poomvises, B. J. Thompson, C.-C. Wu, S. Yashiro, and A. N. Zhukov. Solar and interplanetary sources of major geomagnetic storms ($Dst \leq -100$ nT) during 1996-2005. *Journal of Geophysical Research (Space Physics)*, 112:A10102, October 2007. doi: 10.1029/2007JA012321.

Curriculum Vitae

Include your *curriculum vitae* here detailing your background, education, and professional experience.