2019 ES 156 Problem Set 6

Announcements

• Submission of your solution to this problem set are made electronically via Canvas no later than 10 am on Friday, March 29th, 2019 Late problem sets will be penalized (see syllabus).

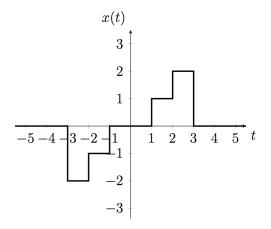
Problems

- 1. [25 points] Given the following continuous-time signals $x_1(t) = e^{-2t}u(t-1)$ and $x_2(t) = e^{-3t}u(t+1)$.
 - (a) Compute the convolution of the two signals $y(t) = x_1(t) * x_2(t)$.
 - (b) Compute the Fourier transform of $x_1(t)$ and $x_2(t)$.
 - (c) Suppose $\hat{Y}(j\omega) = X_1(j\omega)X_2(j\omega)$. Compute the associated continuous-time signal $\hat{y}(t)$. Are y(t) from part (a) and $\hat{y}(t)$ equal?
- 2. [25 points] Suppose a continuous-time signal x(t) has the following Fourier transform

$$X(j\omega) = \frac{d}{d\omega} \left(\frac{e^{-3j\omega}}{(2 + j(\omega - \frac{\pi}{3}))(2 + j(\omega + \frac{\pi}{3}))} \right).$$

Using the Fourier properties, determine the signal x(t). At each juncture, indicate the properties you use.

3. [10 points] Consider the following signal



Compute the integral $\int_{-\infty}^{\infty} |X(j(\omega - \pi)) + X(j(\omega + \pi))|^2 d\omega$.

4. [40 points+5 points] Voice Recognition lab See the Jupyter notebook on Canvas for details.