Black Holes and Limiting Curvature Gravity (LCG) Theory

Main Concepts

Black Holes:

- Formation of New Universes: Inside a black hole.
- **Bouncing Cosmological Solutions:** Describing oscillating universes.
- Mass Inflation Problem: Addressing growth of mass in certain scenarios.

Limiting Curvature Gravity (LCG) Theory:

- Covariant action imposing constraints on curvature invariants.
- Subcritical Regime:
 - \circ \$Q < 0\$ \rightarrow \rightarrow \$\text{symbol}^2 = -Q\$, \$X = 0\$.
- Supercritical Regime:
 - $\circ $Q = 0$ \rightarrow \text{rightarrow } \text{symbol} = 0$, $X \neq 0$.$

Mathematical Framework

- Lagrangian: $L(q,q')=L(q,q')+Z[Q(q,q')+symbol2].L(q,q')=L(q,q')+Z[Q(q,q')+text{symbol}^2].$
- Constraints: Q(q,q')+symbol2=0,X×symbol=0.Q(q,q') + \text{symbol}^2 = 0, \quad X \times \text{symbol} = 0.

2D Limiting Curvature Gravity Model

• Action:

```
ILCG=IDG+Ix,Ix=12 \int d2x \mid g \mid X'(R-A+symbol2),I_{\text{LCG}} = I_{\text{LCG}} + I_x, \quad I_x = \frac{1}{2} \int x \mid g \mid X'(R-A+symbol2),I_{\text{LCG}} = I_{\text{LCG}} + I_x, \quad I_x = \frac{1}{2} \int x \mid g \mid X'(R-A+symbol2),I_{\text{LCG}} = I_{\text{LCG}} + I_x, \quad I_x = \frac{1}{2} \int x \mid g \mid X'(R-A+symbol2),I_{\text{LCG}} = I_{\text{LCG}} + I_x, \quad I_x = \frac{1}{2} \int x \mid g \mid X'(R-A+symbol2),I_{\text{LCG}} = I_{\text{LCG}} + I_x, \quad I_x = \frac{1}{2} \int x \mid g \mid X'(R-A+symbol2),I_{\text{LCG}} = I_{\text{LCG}} + I_x, \quad I_x = \frac{1}{2} \int x \mid g \mid X'(R-A+symbol2),I_{\text{LCG}} = I_{\text{LCG}} + I_x, \quad I_x = \frac{1}{2} \int x \mid g \mid X'(R-A+symbol2),I_{\text{LCG}} = I_{\text{LCG}} + I_x, \quad I_x = \frac{1}{2} \int x \mid g \mid X'(R-A+symbol2),I_{\text{LCG}} = I_{\text{LCG}} + I_x, \quad I_x = \frac{1}{2} \int x \mid g \mid X'(R-A+symbol2),I_{\text{LCG}} = I_{\text{LCG}} + I_x, \quad I_x = \frac{1}{2} \int x \mid g \mid X'(R-A+symbol2),I_{\text{LCG}} = I_x + I_x, \quad I_x = \frac{1}{2} \int x \mid g \mid X'(R-A+symbol2),I_{\text{LCG}} = I_x + I
```

• Subcritical Regime:

```
X=0,C2=A-R.X=0, \quad C^2=A-R.
```

• Equation for \$\epsilon\$:

```
-\epsilon(\gamma 2+14R)\epsilon=0.-\exp(\log(\alpha^2 + \frac{1}{4}R)\epsilon=0.
Solution: \epsilon=\exp(-\text{text}\{\text{symbol}\} 0)$.
```

• Metric for a Static 2D Black Hole:

```
 ds2 = -fdt2 + f - 1dr2, f = 1 - m\gamma e - 2\gamma r. ds^2 = -f dt^2 + f^{-1} dr^2, \quad f = 1 - frac\{m\} {\gamma amma} e^{-2\gamma amma}.
```

• Boundary Conditions:

```
P(\pm\pi2)=\pm\pi2, Q(\pm\pi2)=\pm\pi2. \\ P(\pm\frac{\pi}{2}) = \pm\frac{\pi}{2}, \qquad Q(\pm\frac{\pi}{2}) = \pm\frac{\pi}{2}.
```

Key Variables

- \$q, q'\$: Coordinates and derivatives.
- \$X, \text{symbol}\$: Lagrange multipliers.
- \$A, R\$: Parameters in curvature equations.
- \$\gamma, \beta\$: Scaling constants.
- \$P, Q\$: Null coordinates.

Formulas for Curvature Metrics

- Boundary Value Condition: RA-RH= $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=4\gamma 2A<1$. R_A R_H = $12\gamma \ln \beta$, $\beta=1\gamma 2\alpha$, $\beta=$
- Temperature: $T-A=1\gamma \arccos \beta . T \{-A\} = \frac{1}{\gamma \alpha \beta } \arccos \sqrt{\beta \beta }.$

Python Script

```
import numpy as np
import matplotlib.pyplot as plt
def metric function(r, m, gamma):
    return 1 - (m / gamma) * np.exp(-2 * gamma * r)
# Parameters
m = 1.0  # Mass parameter
gamma = 0.5 # Scaling constant
r = np.linspace(0, 10, 500)
# Metric computation
f = metric function(r, m, gamma)
# Plotting the metric
plt.plot(r, f, label="Metric function f(r)")
plt.axhline(0, color='red', linestyle='--', label="Event Horizon")
plt.xlabel("r")
plt.ylabel("f(r)")
plt.title("Metric Function of a Static 2D Black Hole")
plt.legend()
```

```
plt.grid()
plt.show()
```

GNU Octave Script

```
% Parameters
m = 1.0; % Mass parameter
gamma = 0.5; % Scaling constant
r = linspace(0, 10, 500);
% Metric function
f = 1 - (m / gamma) * exp(-2 * gamma * r);
% Plot
figure;
plot(r, f, 'b', 'LineWidth', 1.5);
hold on;
line([0, 10], [0, 0], 'color', 'red', 'linestyle', '--', 'linewidth',
1.5);
xlabel('r');
ylabel('f(r)');
title('Metric Function of a Static 2D Black Hole');
grid on;
hold off;
```

Summary

This document outlines the theoretical framework of black holes in the context of Limiting Curvature Gravity (LCG) theory. Python and Octave scripts are provided for simulating the metric of a static 2D black hole, which serves as a foundation for understanding the behavior of curvature and associated metrics in this model.