



Flow transition over surface gaps in 2D incompressible laminar boundary layers

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2 July 2025

IMPERIAL



Motivation



Figure: Wing of a Boeing 737-800

Setup

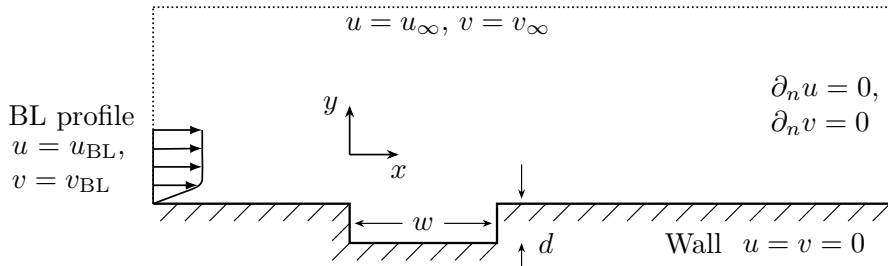


Figure: Domain setup for the steady-state finder

- **Aim:** Study the stability of the system as a function of the depth d and width w of the gap.
- 2D incompressible NS
- $\text{Re}_{\delta^*} = 1000 \implies \text{Re}_x = 3.38 \times 10^5$

Stability results

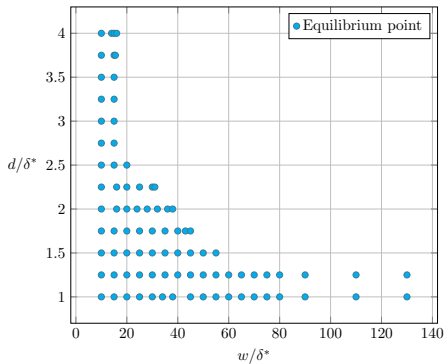
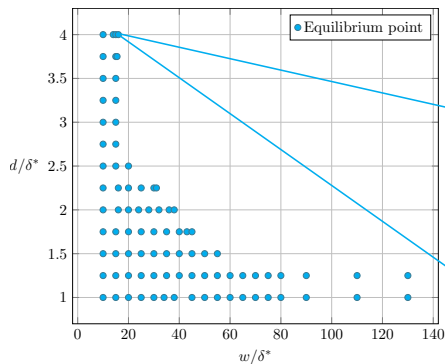


Figure: Classification of the stability of points downstream of the gap.

Stability results



$$d/\delta^* = 4, \quad w/\delta^* = 15$$

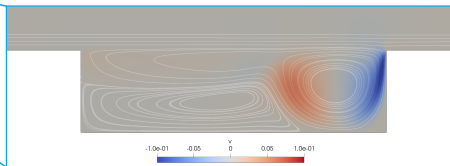


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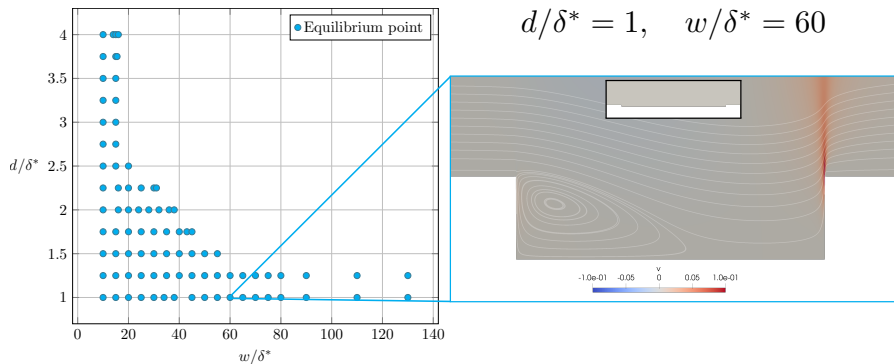


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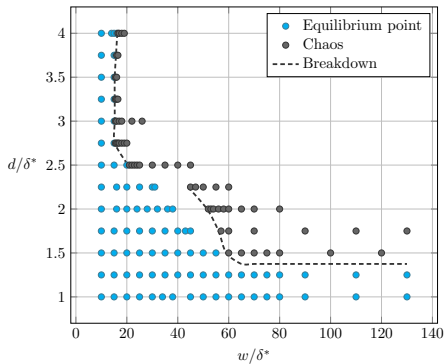


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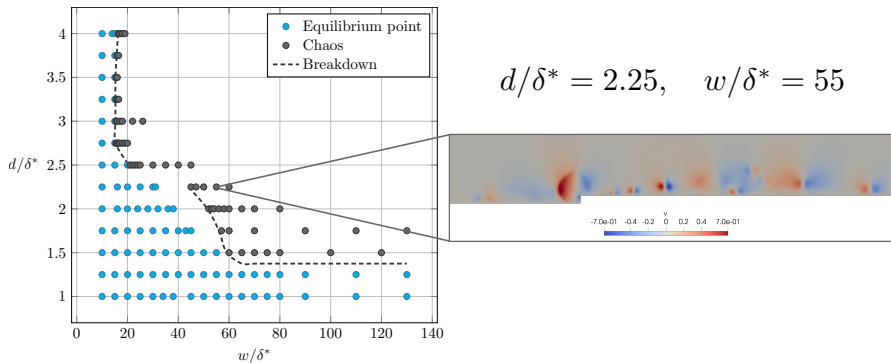


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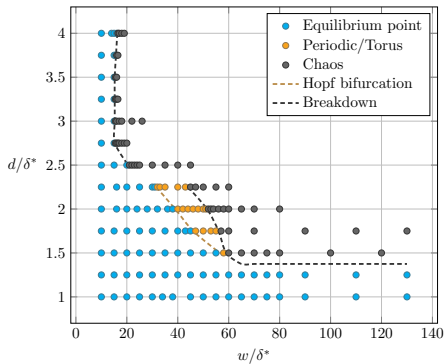
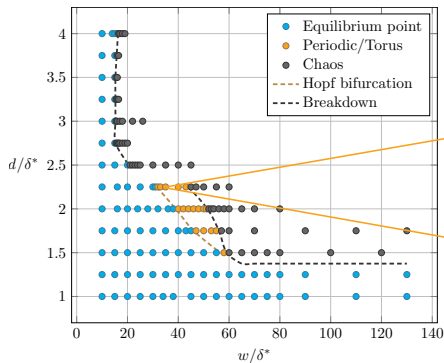


Figure: Classification of the stability of points downstream of the gap.

Stability results



$$d/\delta^* = 2.25, \quad w/\delta^* = 35$$

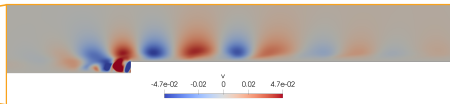


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Framework for the LST (TS-wave transition)

- We linearize the flow around a steady baseflow:

$$\mathbf{u}(x, y, t) = \mathbf{U}(x, y) + \tilde{\mathbf{u}}(x, y, t)$$

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- But this is a local representation! To account for streamwise growth in the BL we use the e^N -method. Fixing $\omega \in \mathbb{R}$:

$$n(x, \omega) = - \int_{x_0}^x \alpha_i(s, \omega) \, ds = \log \left(\frac{|\tilde{\mathbf{u}}(x, \omega)|}{|\tilde{\mathbf{u}}_0|} \right)$$
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\implies Disturbances of amplitude A_0 satisfy $A(x) \leq A_0 e^{N(x)}$.

Previous Work

Flow (2022), 2 E8
doi:10.1017/fo.2022.1

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Characterizing surface-gap effects on boundary-layer transition dominated by Tollmien–Schlichting instability

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Received: 7 July 2021; Revised: 24 January 2022; Accepted: 24 January 2022

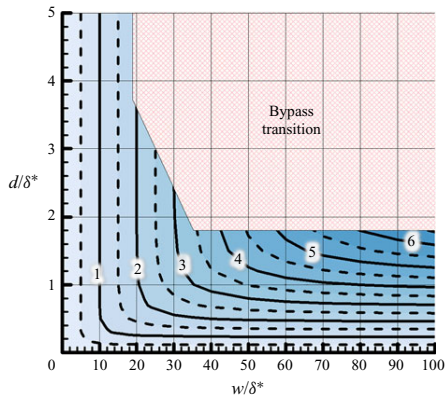


Figure: $\Delta N = N - N_{\text{ref}}$ for different gap dimensions

Crouch JD, Kosorygin VS, Sutanto MI, Miller GD. Characterizing surface-gap effects on boundary-layer transition dominated by Tollmien–Schlichting instability. *Flow*. 2022;2:E8.

Perturbed system setup

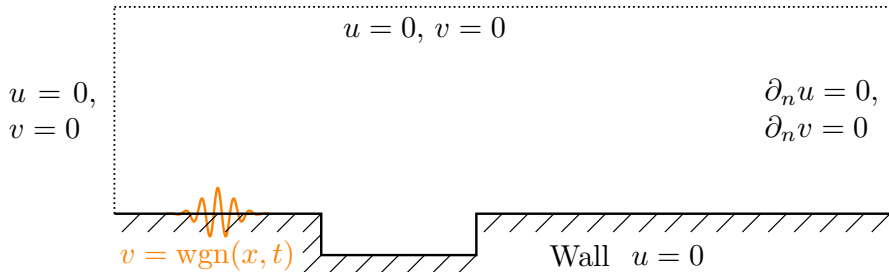


Figure: Domain setup for the perturbed system

e^N -method results

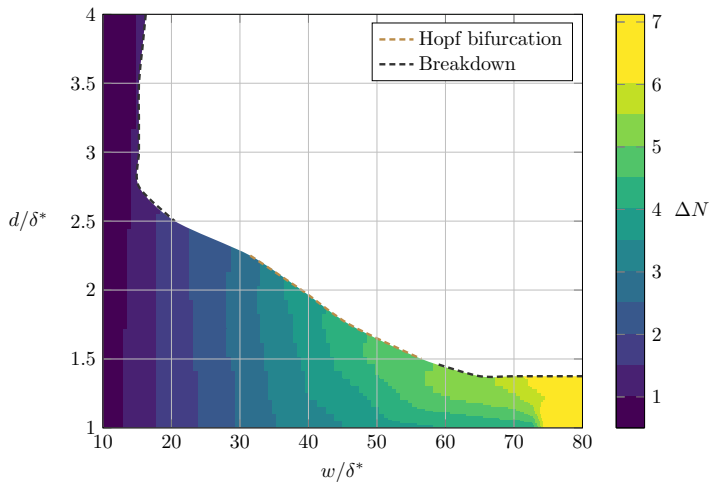


Figure: Interpolated $\Delta N = N - N_{\text{ref}}$ in the globally-stable region.

e^N -method results

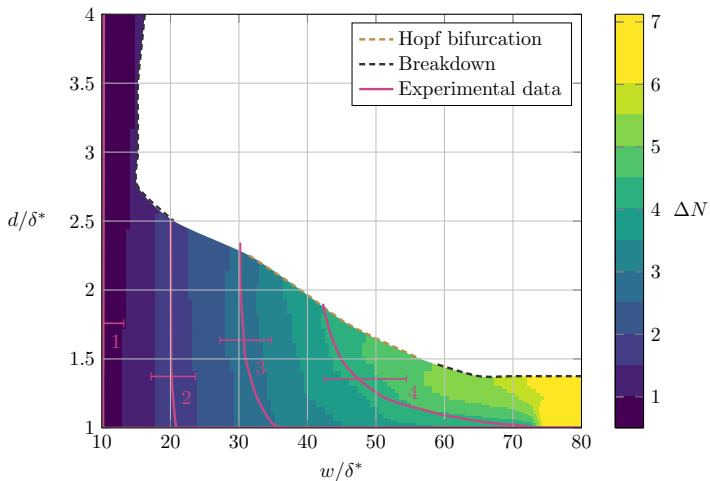


Figure: Interpolated $\Delta N = N - N_{\text{ref}}$ in the equilibria region. Magenta lines indicate the contour levels of the experimental data.

Future Work

- Go to higher Ma (compressible regime).

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- Account for spanwise effects (quasi-3d simulations).