



# Flow transition over surface gaps in 2D incompressible laminar boundary layers

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# Motivation



Figure: Wing of a Boeing 737-800

# Setup

BL profile  
 $u = u_{\text{BL}},$   
 $v = v_{\text{BL}}$

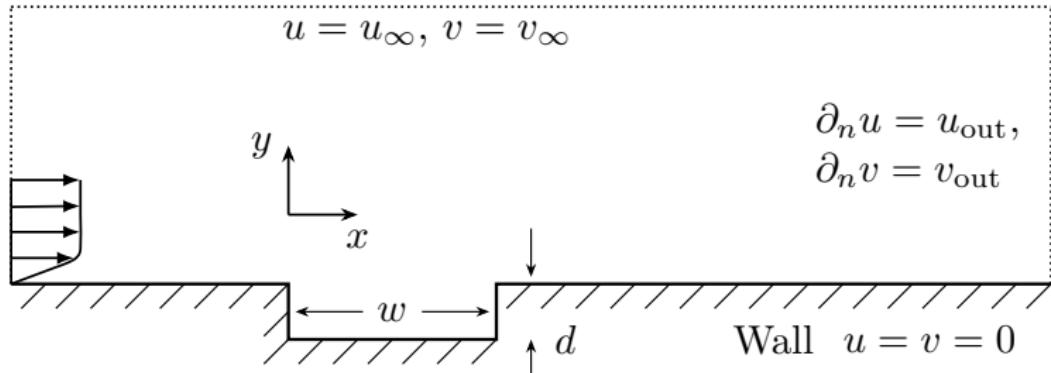
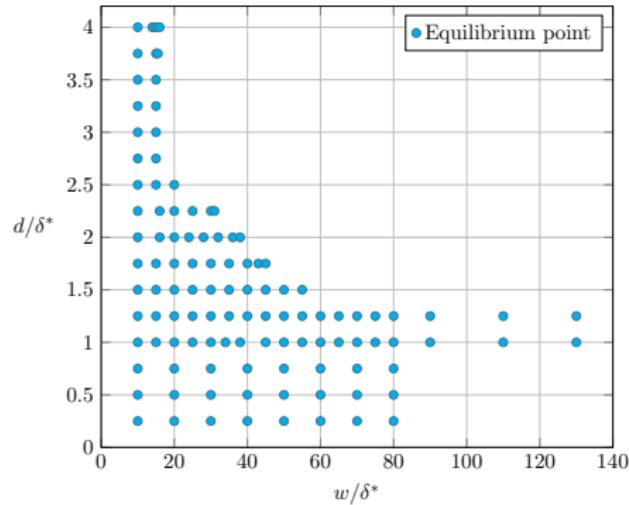


Figure: Domain setup for the steady-state finder

- **Aim:** Study the stability of the system as a function of the depth  $d$  and width  $w$  of the gap.
- 2D incompressible NS
- $\text{Re}_{\delta^*} = 1000 \implies \text{Re}_x = 3.38 \times 10^5$

# Stability results



**Figure:** Classification of the stability of points downstream of the gap.

# Stability results

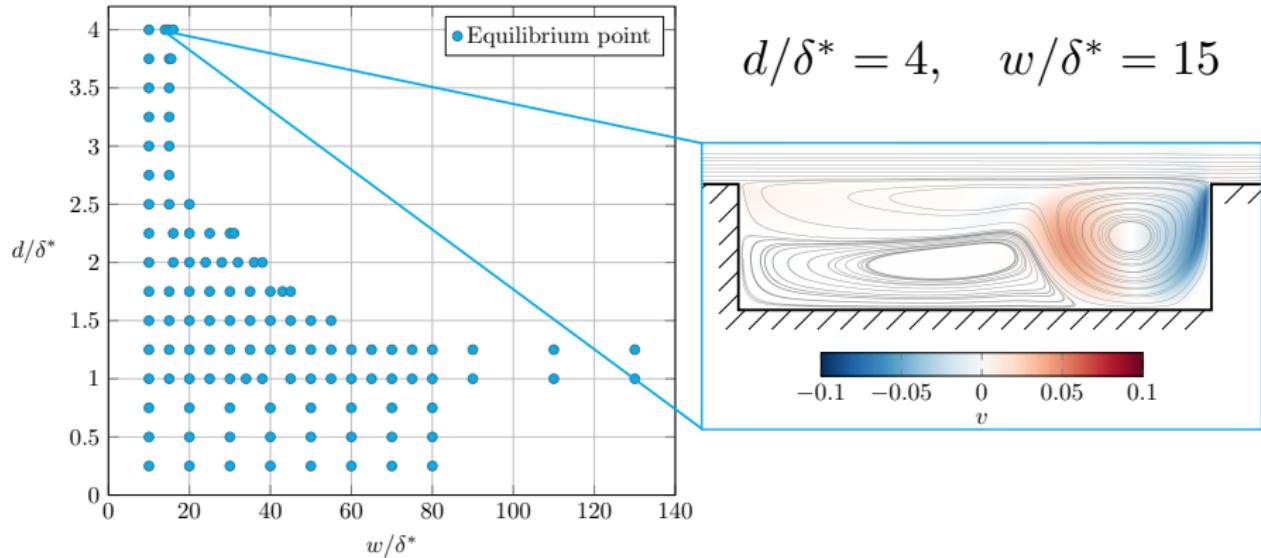


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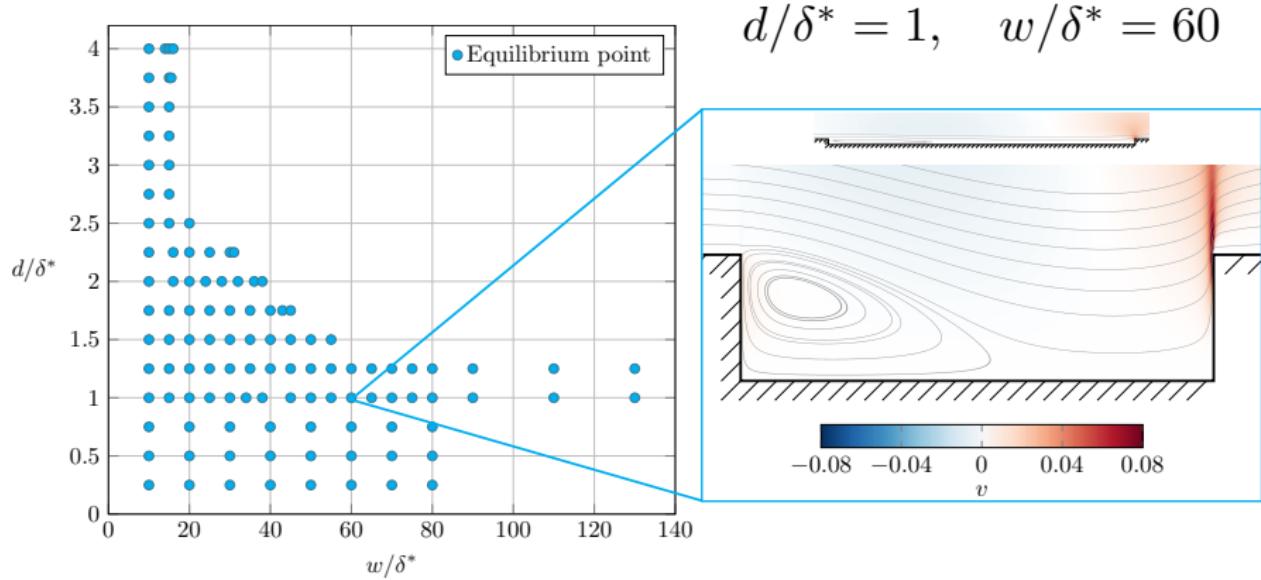
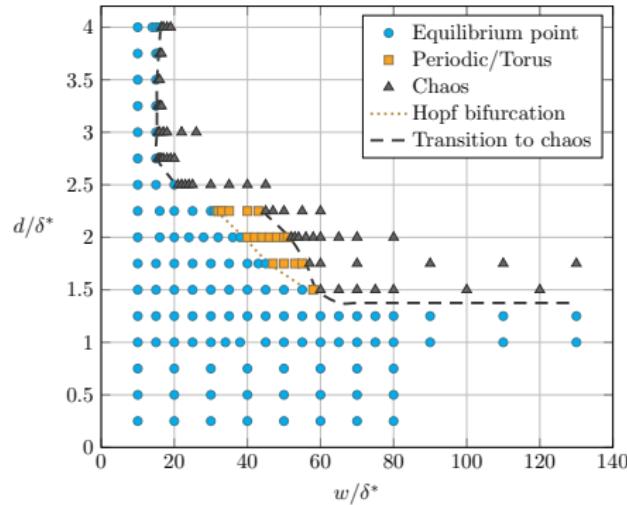


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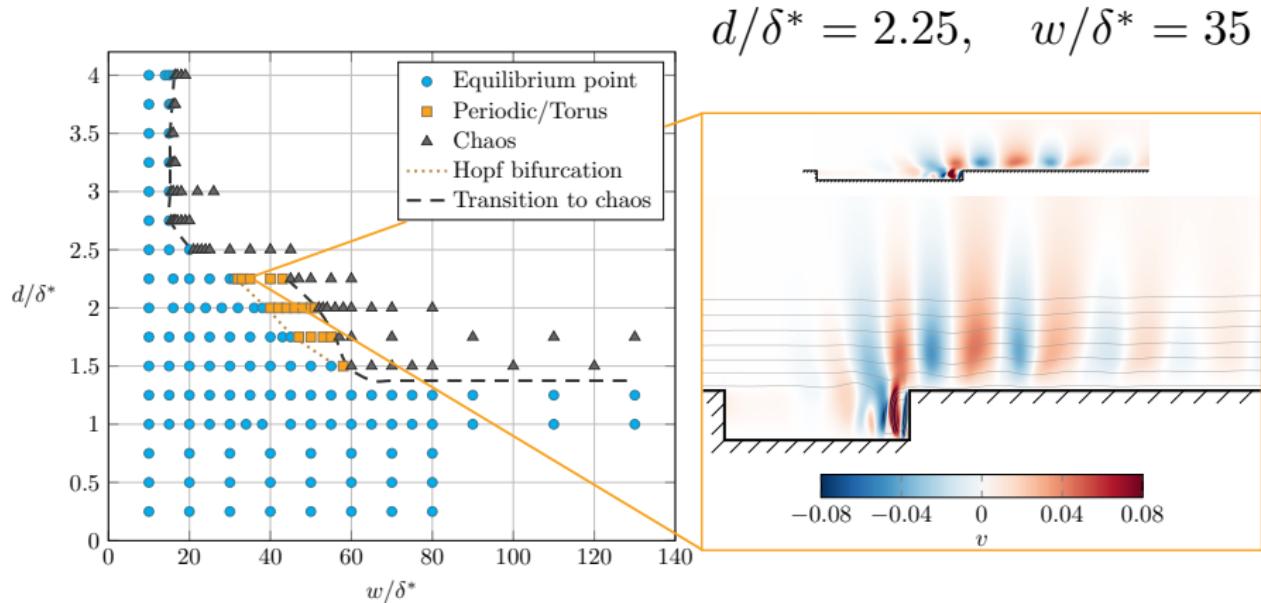


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## Framework for the LST (TS-wave transition)

- We linearize the flow around a steady baseflow:

$$\mathbf{u}(x, y, t) = \mathbf{U}(x, y) + \tilde{\mathbf{u}}(x, y, t).$$

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- We add a disturbance of characteristic amplitude  $A_0$  upstream of the gap and we track its evolution through

$$A(x) := A_0 e^{n(x)} \implies n(x) = \log \left( \frac{A(x)}{A_0} \right).$$

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- To compare between gaps, we define  $n_{\text{ref}}(x)$  as the *n-factor* of a reference case (flat plate) and we compute

$$\Delta n_{\text{gap}} = n_{\text{gap}} - n_{\text{ref}}.$$

## Perturbed system setup

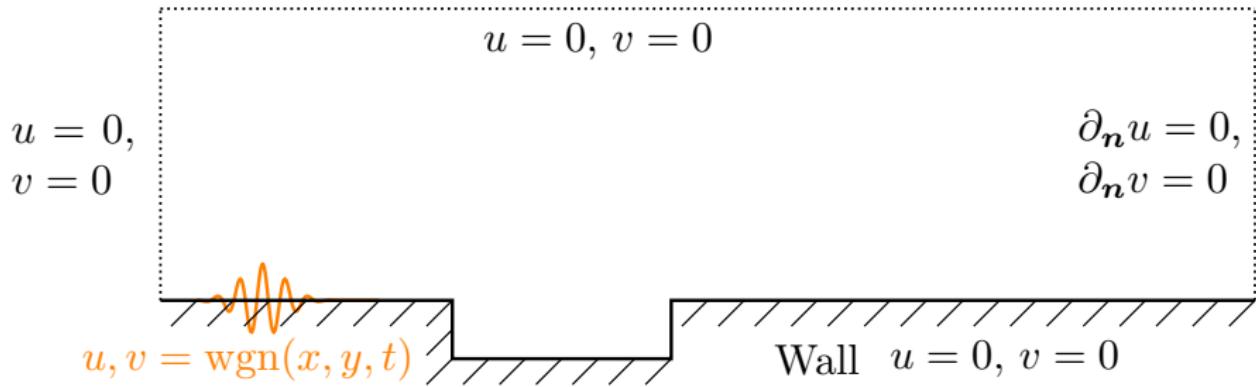


Figure: Domain setup for the perturbed system

# Previous Work

Flow (2022), 2 E8  
doi:10.1017/flo.2022.1

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## Characterizing surface-gap effects on boundary-layer transition dominated by Tollmien–Schlichting instability

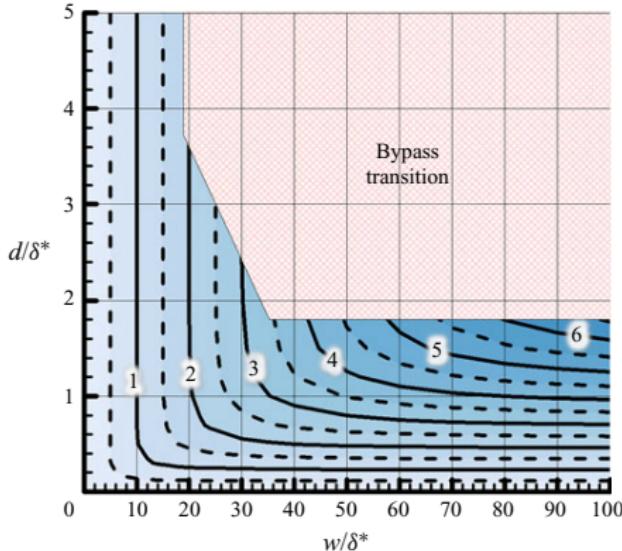
J. D. Crouch<sup>1,\*</sup> , V. S. Kosorygin<sup>2</sup>, M. I. Sutanto<sup>1</sup> and G. D. Miller<sup>1</sup>

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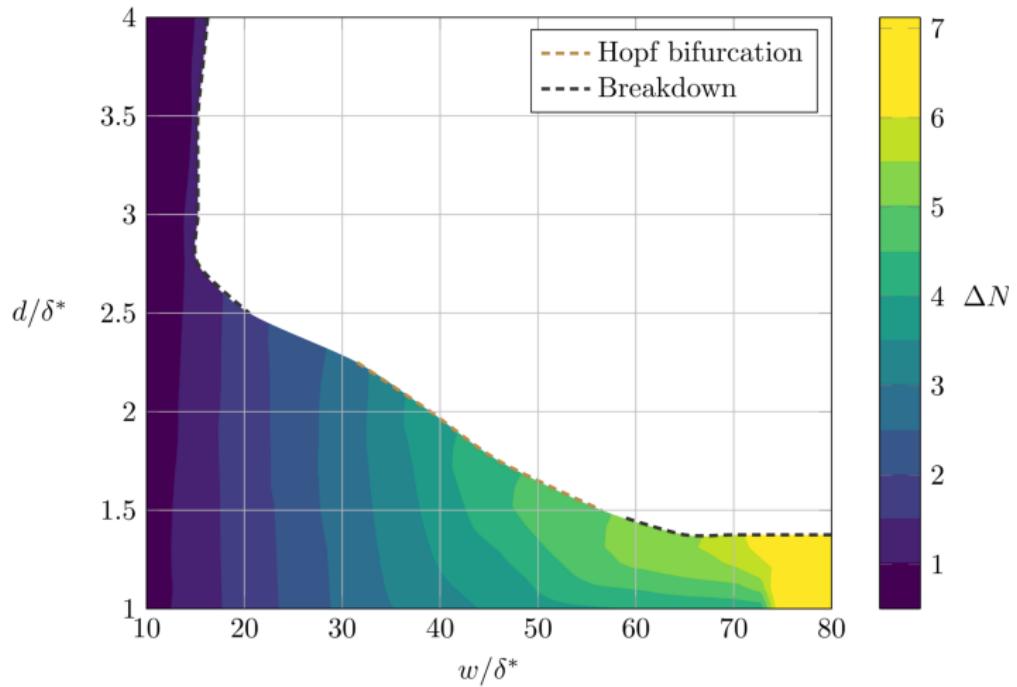
Received: 7 July 2021; Revised: 24 January 2022; Accepted: 24 January 2022



**Figure:**  $\Delta n_{\text{gap}} = n_{\text{gap}} - n_{\text{ref}}$  for different gap dimensions

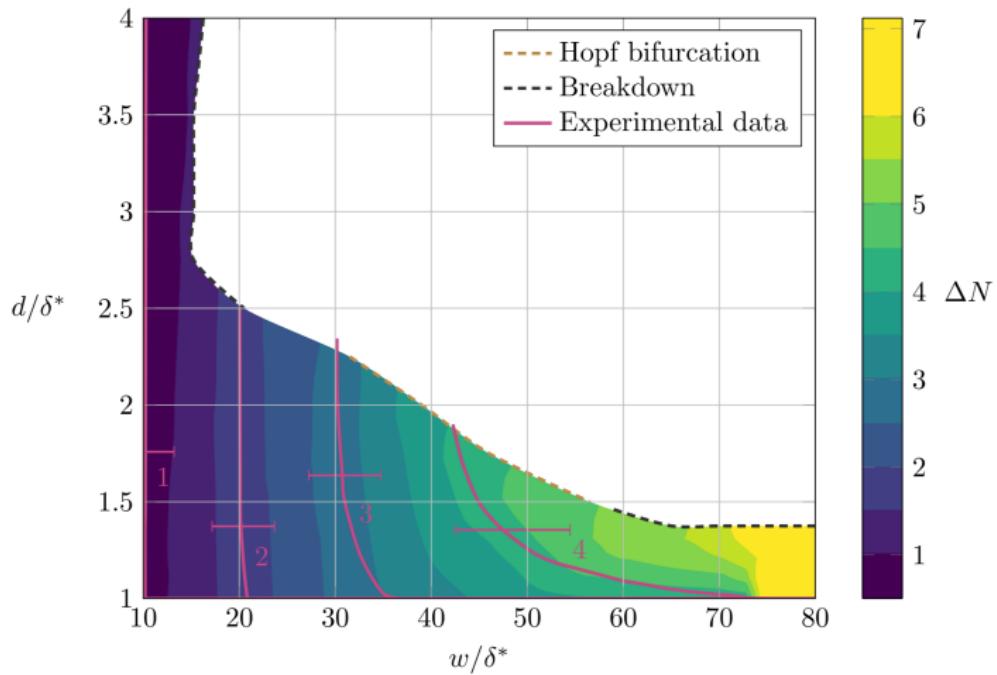
Crouch JD, Kosorygin VS, Sutanto MI, Miller GD. Characterizing surface-gap effects on boundary-layer transition dominated by Tollmien–Schlichting instability. *Flow.* 2022;2:E8.

## e<sup>N</sup>-method results



**Figure:** Interpolated  $\Delta n_{\text{gap}} = n_{\text{gap}} - n_{\text{ref}}$  in the globally-stable region.

## $e^N$ -method results



**Figure:** Interpolated  $\Delta n_{\text{gap}} = n_{\text{gap}} - n_{\text{ref}}$  in the equilibria region. Magenta lines indicate the contour levels of the experimental data.

## Future Work

- Go to higher Ma (compressible regime).

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- Account for spanwise effects (quasi-3d simulations).