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Sala: CTII 317

Tarefa Básica

1)

$$A = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \\ a_{31} & a_{32} \end{bmatrix}$$

$$a_{11} = 2 \cdot 1 + 3 \cdot 1 = 5$$

$$a_{12} = 2 \cdot 1 + 3 \cdot 2 = 8$$

$$a_{21} = 2 \cdot 2 + 3 \cdot 1 = 7$$

$$a_{22} = 2 \cdot 2 + 3 \cdot 2 = 10$$

$$a_{31} = 2 \cdot 3 + 3 \cdot 1 = 9$$

$$a_{32} = 2 \cdot 3 + 3 \cdot 2 = 12$$

$$R: A = \begin{bmatrix} 5 & 8 \\ 7 & 10 \\ 9 & 12 \end{bmatrix}$$

2)

$$A = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix}$$

$$a_{11} = 1^2 + 4 \cdot 1^2 = 1 + 4 = 5$$

$$a_{12} = 1^2 + 4 \cdot 2^2 = 1 + 16 = 17$$

$$a_{21} = 2^2 + 4 \cdot 1^2 = 4 + 4 = 8$$

$$a_{22} = 2^2 + 4 \cdot 2^2 = 4 + 16 = 20$$

$$R: A = \begin{bmatrix} 5 & 17 \\ 8 & 20 \end{bmatrix} \text{ letra "A"}$$

3)

$$\begin{bmatrix} 1 & x+2 \\ y-1 & z+1 \end{bmatrix} = \begin{bmatrix} 1 & -x \\ 2y & -2z \end{bmatrix}$$

$$1 = 1$$

$$x + 2 = -x$$

$$x = -1$$

$$x + 2 = -x$$

$$y - 1 = 2y$$

$$y = -1$$

$$y - 1 = 2y$$

$$z + 1 = -2z$$

$$z = -\frac{1}{3}$$

$$z + 1 = -2z$$

$$4) \begin{bmatrix} 3 & -x \\ 3x & x \end{bmatrix} = \begin{bmatrix} 3 & y \\ 2x+1 & z-1 \end{bmatrix}$$

$$\begin{cases} 3=3 \\ -x=y \\ 3x=2x+1 \\ x=2-1 \end{cases} \rightarrow \begin{cases} -x+y=0 \\ x=1 \\ x-z=-1 \end{cases} \rightarrow \begin{cases} 1+y=0 \\ 1-z=-1 \\ y=-1 \\ z=2 \end{cases} \rightarrow \begin{cases} x=1 \\ y=-1 \\ z=2 \end{cases}$$

$$\begin{cases} -x=y \\ 3x=2x+1 \\ x=2-1 \end{cases} \rightarrow \begin{cases} -x+y=0 \\ x=1 \\ x-z=-1 \end{cases} \rightarrow \begin{cases} y=-1 \\ z=2 \end{cases}$$

$$5) \begin{bmatrix} 11 & 12 & 13 & 14 \\ 21 & 22 & 23 & 24 \\ 31 & 32 & 33 & 34 \\ 41 & 42 & 43 & 44 \end{bmatrix}$$

$$a_{11} = 0 \rightarrow \text{Distância entre } i \text{ e } j$$

$$a_{12} = 1$$

$$a_{13} = \sqrt{2}$$

$$a_{14} = 1$$

$$a_{21} = 1$$

$$a_{22} = 0$$

$$a_{23} = 1$$

$$a_{24} = \sqrt{2}$$

$$a_{31} = \sqrt{2}$$

$$a_{32} = 1$$

$$a_{33} = 0$$

$$a_{34} = 1$$

$$a_{41} = 1$$

$$a_{42} = \sqrt{2}$$

$$a_{43} = 1$$

$$a_{44} = 0$$

$$A = \begin{bmatrix} 0 & 1 & \sqrt{2} & 1 \\ 1 & 0 & 1 & \sqrt{2} \\ \sqrt{2} & 1 & 0 & 1 \\ 1 & \sqrt{2} & 1 & 0 \end{bmatrix}$$

letra "B"

$$6) 2. \begin{bmatrix} -1 \\ 2 \\ 3 \end{bmatrix} - \begin{bmatrix} 0 \\ -2 \\ 1 \end{bmatrix} = \begin{bmatrix} -2 \\ 4+2 \\ 6-1 \end{bmatrix}$$

$$\begin{bmatrix} -2 \\ 4 \\ 6 \end{bmatrix} - \begin{bmatrix} 0 \\ -2 \\ 1 \end{bmatrix} = \begin{bmatrix} -2 \\ 6 \\ 5 \end{bmatrix} \text{ letra "D"}$$

$$\begin{bmatrix} -2-0 \\ 4-(-2) \\ 6-1 \end{bmatrix}$$

$$7) A-B = \begin{bmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{bmatrix} - \begin{bmatrix} -1 & 2 \\ 3 & 0 \\ 2 & 1 \end{bmatrix}$$

$$A-B = \begin{bmatrix} 1-(-1) & 2-2 \\ 3-3 & 4-0 \\ 5-2 & 6-1 \end{bmatrix}$$

$$A-B = \begin{bmatrix} 2 & 0 \\ 0 & 4 \\ 3 & 5 \end{bmatrix} \text{ letra "B"}$$

8)

$$A = \begin{bmatrix} 2 & -1 & 2y \\ x & 0 & -2 \\ 4 & 3 & 2 \end{bmatrix}$$

$$A^T = \begin{bmatrix} 2 & x & 4 \\ -1 & 0 & 3 \\ 2y & -2 & 2 \end{bmatrix}$$

$$A = A^T$$

$$\begin{cases} x = -1 \\ 2y = 4 \\ -2 = 3 \end{cases} \Rightarrow \begin{cases} y = 2 \\ z = 4 \end{cases}$$

$$\begin{aligned} x+y+z &= -1 + 2 + 4 \\ x+y+z &= 5 \end{aligned}$$

$$9) \quad A = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \\ a_{31} & a_{32} \end{bmatrix} \quad B = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \\ a_{31} & a_{32} \end{bmatrix}$$

$$\begin{aligned} a_{11} &= 1 \\ a_{12} &= 3 \\ a_{21} &= 3 \\ a_{22} &= 1 \end{aligned}$$

$$A = \begin{bmatrix} 1 & 3 \\ 3 & 1 \\ 4 & 5 \end{bmatrix} + \begin{bmatrix} 1 & 0 \\ 0 & 2 \\ 0 & 0 \end{bmatrix}$$

$$\begin{aligned} a_{11} &= 1 \\ a_{12} &= 0 \\ a_{21} &= 0 \\ a_{22} &= 2 \\ a_{31} &= 0 \\ a_{32} &= 0 \end{aligned}$$

$$\begin{aligned} a_{31} &= 4 \\ a_{32} &= 5 \end{aligned}$$

$$A + B = \begin{bmatrix} 2 & 3 \\ 3 & 3 \\ 4 & 5 \end{bmatrix} \quad \text{linha "C"}$$

$$10) \quad M = \begin{bmatrix} x & 8 \\ 10 & y \end{bmatrix} \quad N = \begin{bmatrix} y & 6 \\ 12 & x+14 \end{bmatrix} \quad P = \begin{bmatrix} 7 & 16 \\ 23 & 13 \end{bmatrix}$$

$$\frac{3}{2}M + \frac{2}{3}N = P$$

$$\frac{3}{2} \cdot \begin{bmatrix} x & 8 \\ 10 & y \end{bmatrix} + \frac{2}{3} \cdot \begin{bmatrix} y & 6 \\ 12 & x+14 \end{bmatrix}$$

$$\begin{bmatrix} \frac{3x}{2} & 12 \\ 15 & \frac{3y}{2} \end{bmatrix} + \begin{bmatrix} \frac{2y}{3} & 4 \\ 8 & \frac{2x+8}{3} \end{bmatrix}$$

$$\begin{bmatrix} \frac{3x}{2} & 12 \\ 15 & \frac{3y}{2} \end{bmatrix} + \begin{bmatrix} \frac{2y}{3} & 4 \\ 8 & \frac{2x+8}{3} \end{bmatrix}$$

$$\begin{bmatrix} \frac{3x}{2} + \frac{2y}{3} & 12 + 4 \\ 15 + 8 & \frac{3y}{2} + \frac{2x+8}{3} \end{bmatrix}$$

$$\frac{3x}{2} + \frac{2y}{3} = 7$$

$$\frac{2x+8}{3} + \frac{3y}{2} = 13$$

$$\frac{9x}{6} + 2 \cdot \frac{2y}{6} = \frac{42}{6}$$

$$\frac{2(2x+8)}{6} + 3 \cdot \frac{2y}{6} = 13 \cdot 6$$

$$9x + 4y = 42$$

$$4x + 16 + 9y = 78$$

$$9x + 4y = 42$$

$$4x + 9y = 62$$

$$9x - 4x + 4y - 9y = 42 - 62$$

$$5x - 5y = -20$$

$$x - y = -4$$

$$y - x = 4 \quad \text{linha "B"}$$