face classification starter

May 2, 2022

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[220]: import numpy as np
       import pandas as pd
       import matplotlib.pyplot as plt
       from scipy.io import loadmat
       from sklearn.metrics import accuracy_score
       from sklearn.model selection import cross val score
       from sklearn.model_selection import train_test_split
       dataset = loadmat('face emotion data.mat')
       X, y = dataset['X'], dataset['y']
       n, p = np.shape(X)
       y[y==-1] = 0 # use 0/1 for labels instead of -1/+1
       X = np.hstack((np.ones((n,1)), X)) # append a column of ones
      0.0.1 1)
[202]: \#Logistic\ function \Rightarrow f(z) = 1/(1+e^{-(-z)})
[205]: ## Train NN
       Xb = np.hstack((np.ones((n,1)), X))
       q = np.shape(y)[1] #number of classification problems
       M = 32 #number of hidden nodes
       ## initial weights
       V = np.random.randn(M, q);
       W = np.random.randn(p+2, M);
       def logsig(_x):
           return 1/(1+np.exp(-x))
       H = logsig(Xb@W)
       Yhat = logsig(H@V)
[194]: Yhat = [1 if i > 0.5 else 0 for i in Yhat]
       Yhat
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[194]: [1, 1, 1, 1, 1, Ο, 1, Ο, 1, Ο, 1, 1, 1, 1, 1, 1, 1, Ο, 1, 1, 1, 1, 1, Ο, Ο, 1, 1, 1, Ο, 1, Ο, 1, 1, 1, 1, 1, 1, Ο, 1, 1, Ο, 1, 1, 1, 1,

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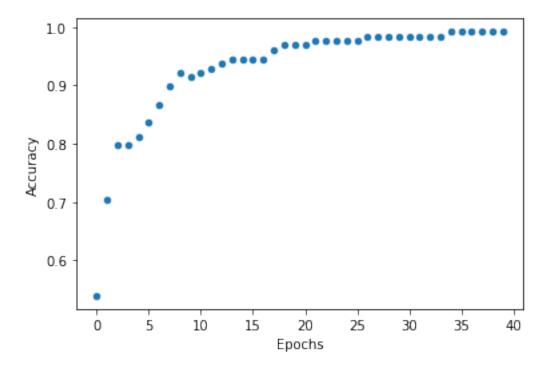
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      b)
[170]: L = 40
       ## initial weights
       V = np.random.randn(M+1, q);
       W = np.random.randn(p+2, M);
       alpha = 0.05
       accuracy = []
       epochs = []
       for epoch in range(L):
           ind = np.random.permutation(n)
           epochs.append(epoch)
```

```
for i in ind:
        # Forward-propagate
        H = logsig(np.hstack((np.ones((1,1)), Xb[[i],:]@W)))
        Yhat = logsig(H@V)
         # Backpropagate
        delta = (Yhat-y[[i],:])*Yhat*(1-Yhat)
        Vnew = V-alpha*H.T@delta
        gamma = delta@V[1:,:].T*H[:,1:]*(1-H[:,1:])
        Wnew = W - alpha*Xb[[i],:].T@gamma
        V = Vnew
        W = Wnew
    H = logsig(np.hstack((np.ones((n,1)), Xb@W)))
    Yhat = logsig(H@V)
    Yhat = [1 \text{ if } i > 0.5 \text{ else } 0 \text{ for } i \text{ in } Yhat ]
    accuracy_append(accuracy_score( Yhat, y ))
df = pd.DataFrame({"Epochs":epochs, "Accuracy":accuracy})
df.plot.scatter("Epochs", "Accuracy")
```

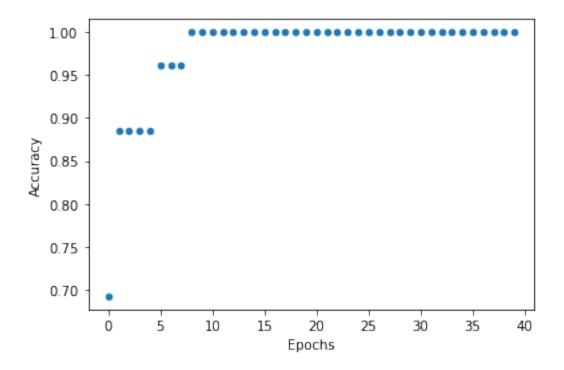
[170]: <AxesSubplot:xlabel='Epochs', ylabel='Accuracy'>

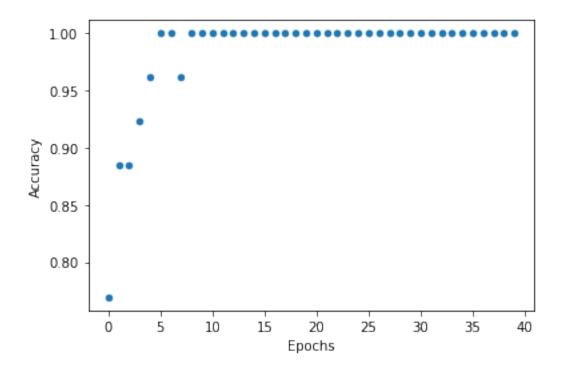


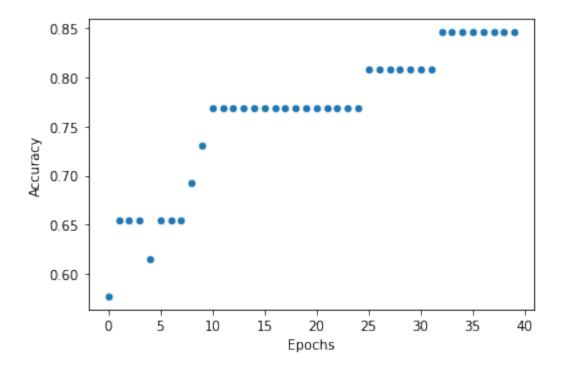
It takes about 35 epochs to reach 0% of error in the training set.

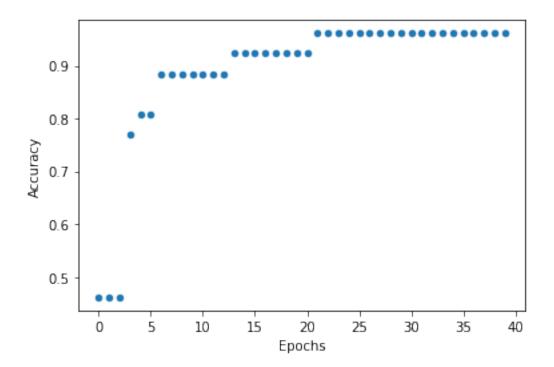
c)

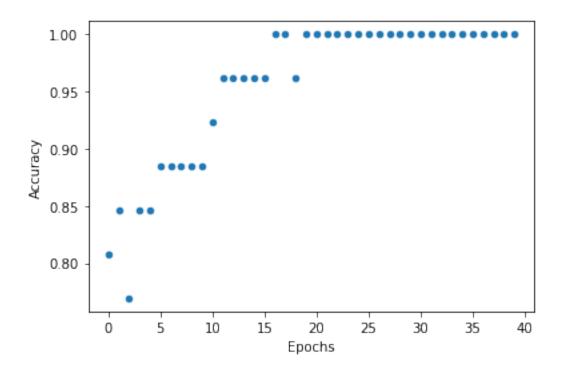
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[224]: L = 40
       alpha = 0.05
       for j in range(0,8):
           X_train, X_test, Y_train, Y_test = train_test_split(Xb, y, test_size = 0.2)
           q = np.shape(Y_train)[1]
           M = 32
           V = np.random.randn(M+1, q);
           W = np.random.randn(p+2, M);
           accuracy = []
           epochs = []
           for epoch in range(L):
                ind = np.random.permutation(len(X_train))
               epochs.append(epoch)
               for i in ind:
                    # Forward-propagate
                    H = logsig(np.hstack((np.ones((1,1)), X_train[[i],:]@W)))
                    Yhat = logsig(H@V)
                     # Backpropagate
                    delta = (Yhat-Y_train[[i],:])*Yhat*(1-Yhat)
                    Vnew = V-alpha*H.T@delta
                    gamma = delta@V[1:,:].T*H[:,1:]*(1-H[:,1:])
                    Wnew = W - alpha*X_train[[i],:].T@gamma
                    V = Vnew
                    W = Wnew
               H = logsig(np.hstack((np.ones((len(X_test),1)), X_test@W)))
               Yhat = logsig(H@V)
               Yhat = [1 \text{ if } i > 0.5 \text{ else } 0 \text{ for } i \text{ in } Yhat ]
                accuracy.append(accuracy_score( Yhat, Y_test ))
           df = pd.DataFrame({"Epochs":epochs,"Accuracy":accuracy})
           df.plot.scatter("Epochs", "Accuracy")
```

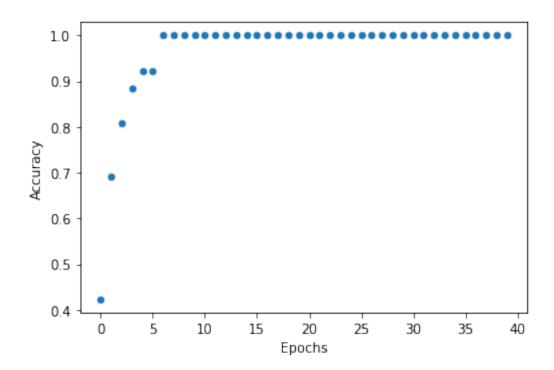


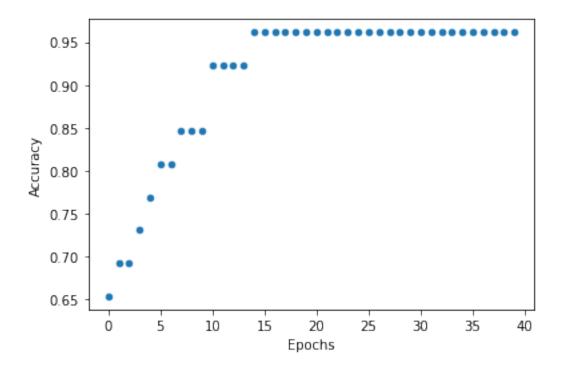


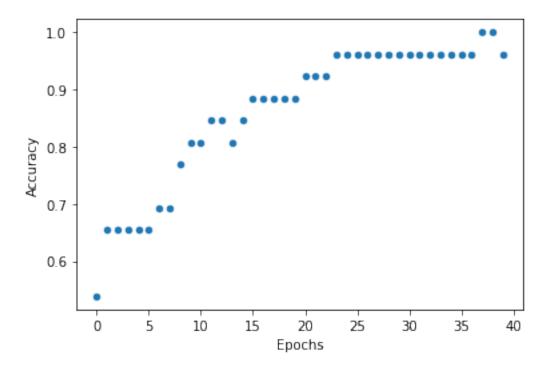












Now as wee can see on the graphs, that the amount of epochs variates depending on the way we select the training and the testing set.