

Embedded computing for scientific and industrial imaging applications

Lecture 4 - C demo, Newton's method

Outline

C demo with visual studio

- Computing square roots by Newton's method
- Incremental developing by using git

Computing square roots

Hardware arithmetic units can add, subtract, multiply, divide. Other mathematical functions usually take some software.

$$\sqrt{2} \approx 1.4142135623730951$$

In most languages, `sqrt(2)` computes this.

```
#include <math.h>
```

```
sqrt(2);
```

Newton's method

Problem: Find a solution of $f(s) = 0$ (zero or root of f)

Idea: Given approximation $s^{[k]}$,
approximate $f(s)$ by a linear function,
the tangent line at $(s^{[k]}, f(s^{[k]}))$.

Find unique zero of this function and use as $s^{[k+1]}$.

Updating formula:

$$s^{[k+1]} = s^{[k]} - \frac{f(s^{[k]})}{f'(s^{[k]})}$$

Approximate $s = \sqrt{x}$

Newton's method to find root of $s^2 - x = 0$.

```
double s = 1.;  
for (int i = 0; i < maxiter; i++)  
{  
    s = 0.5 * (s + x / s);  
}
```

where `maxiter` is some maximum number of iterations.

Demo

Goals:

- Develop our own version of sqrt function.
- Start simple and add complexity in stages.
- Illustrate some C programming.
- Illustrate use of git to track our development
- Get familiar with visual studio IDE

We will do this in codes/mysqrt directory so you can examine the various versions later.

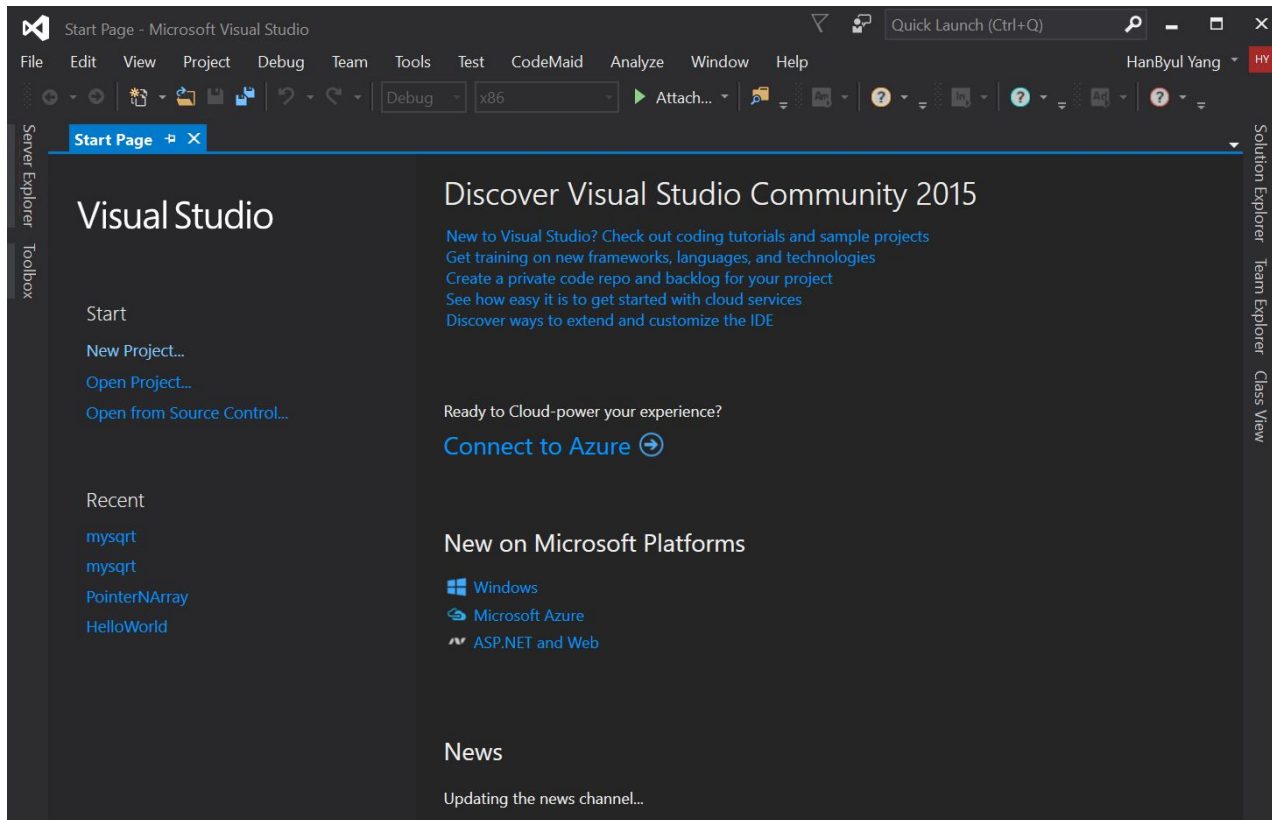
Demo : mysqrt.c

```
#include <stdio.h>
#include <math.h>

int main()
{
    double x = 2;
    double s = sqrt(x);
    printf("sqrt(%f) = %f\n", x, s);
}
```

Demo : visual studio

Start “New Project”

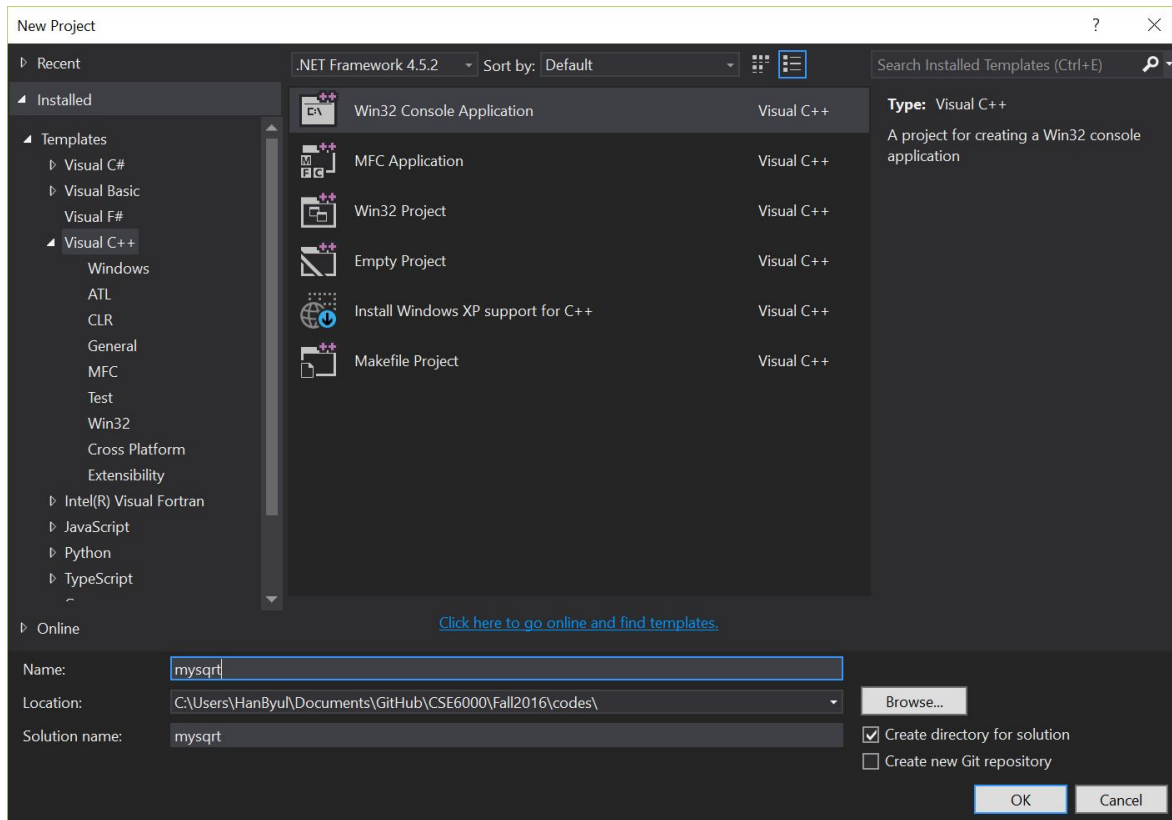


Demo : new project

Visual c++

Win32 Console application

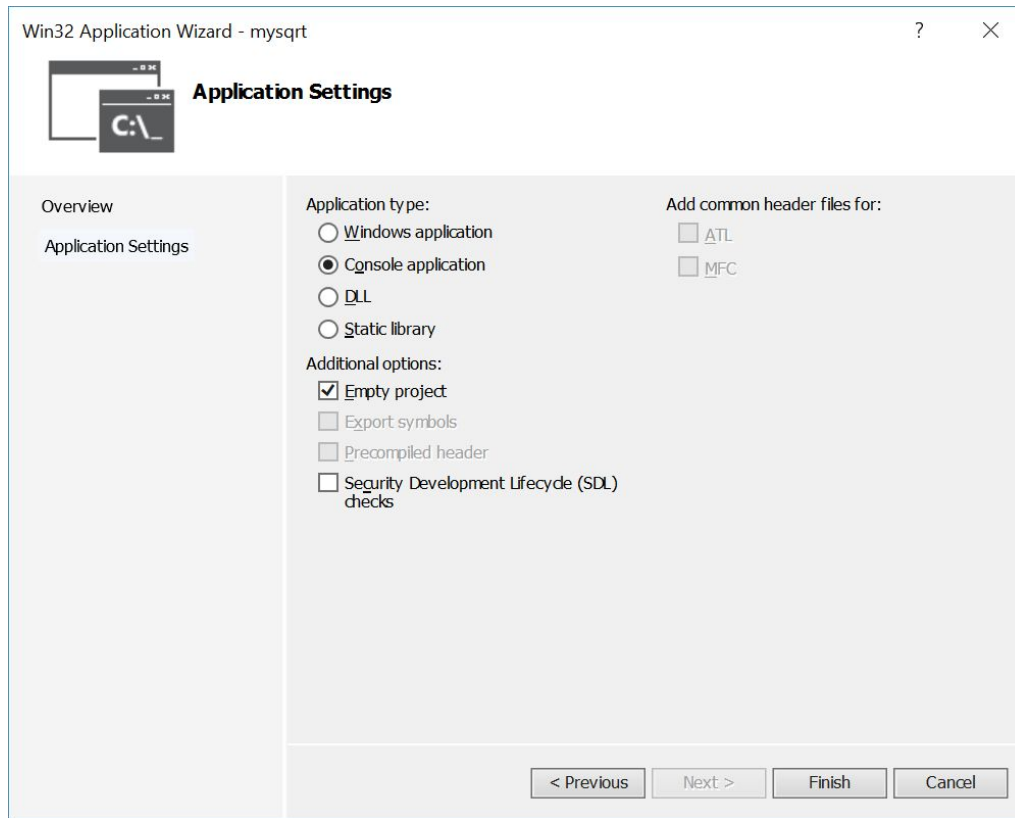
“mysql”



Demo : application setting

Console application

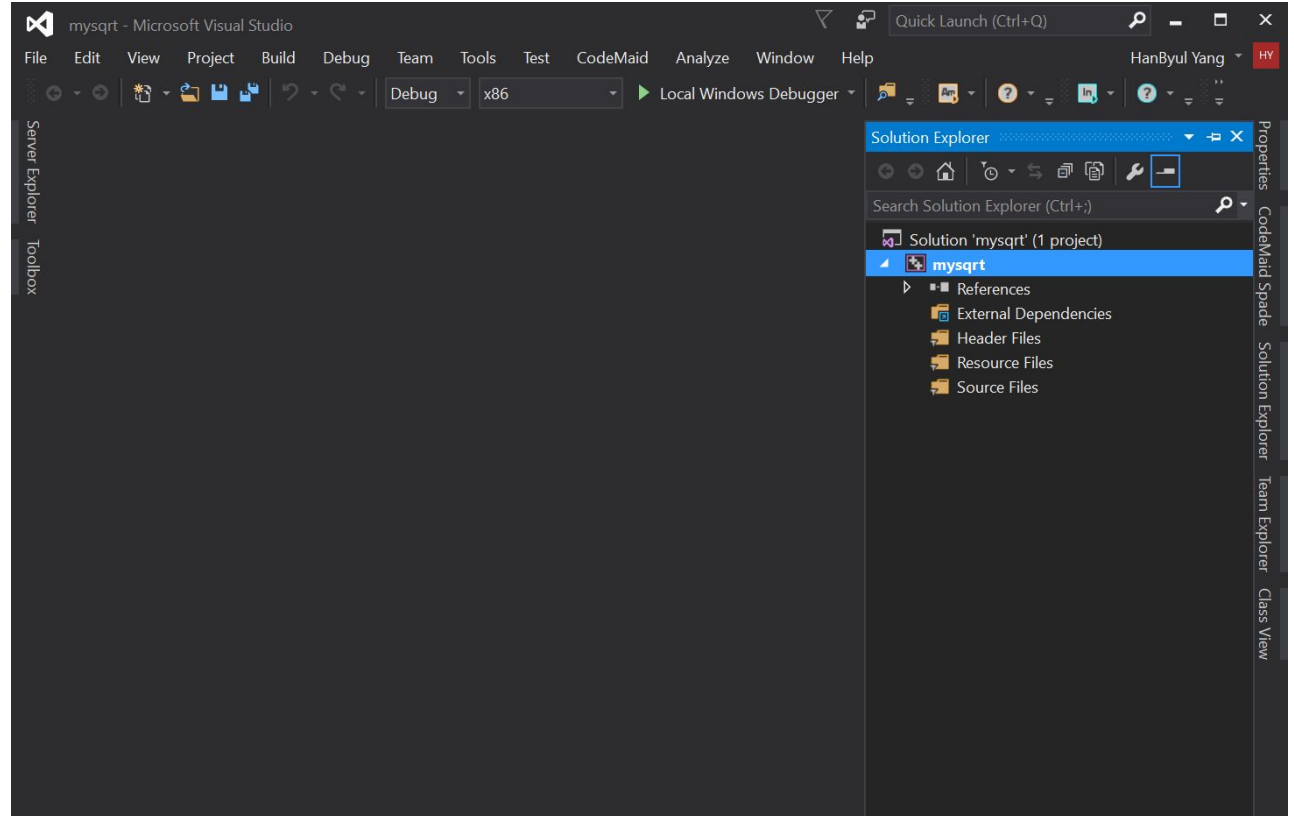
Empty project



Demo : Solution Explorer

Solution

Project

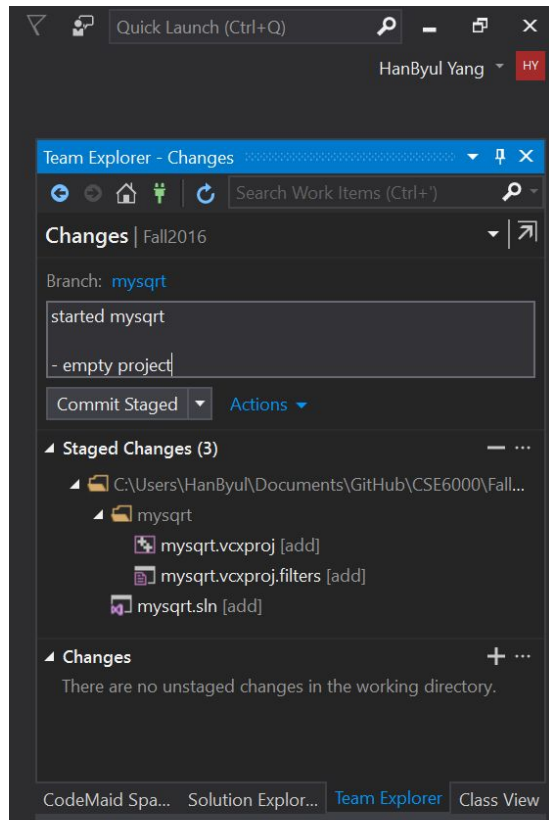


Demo : Team Explorer

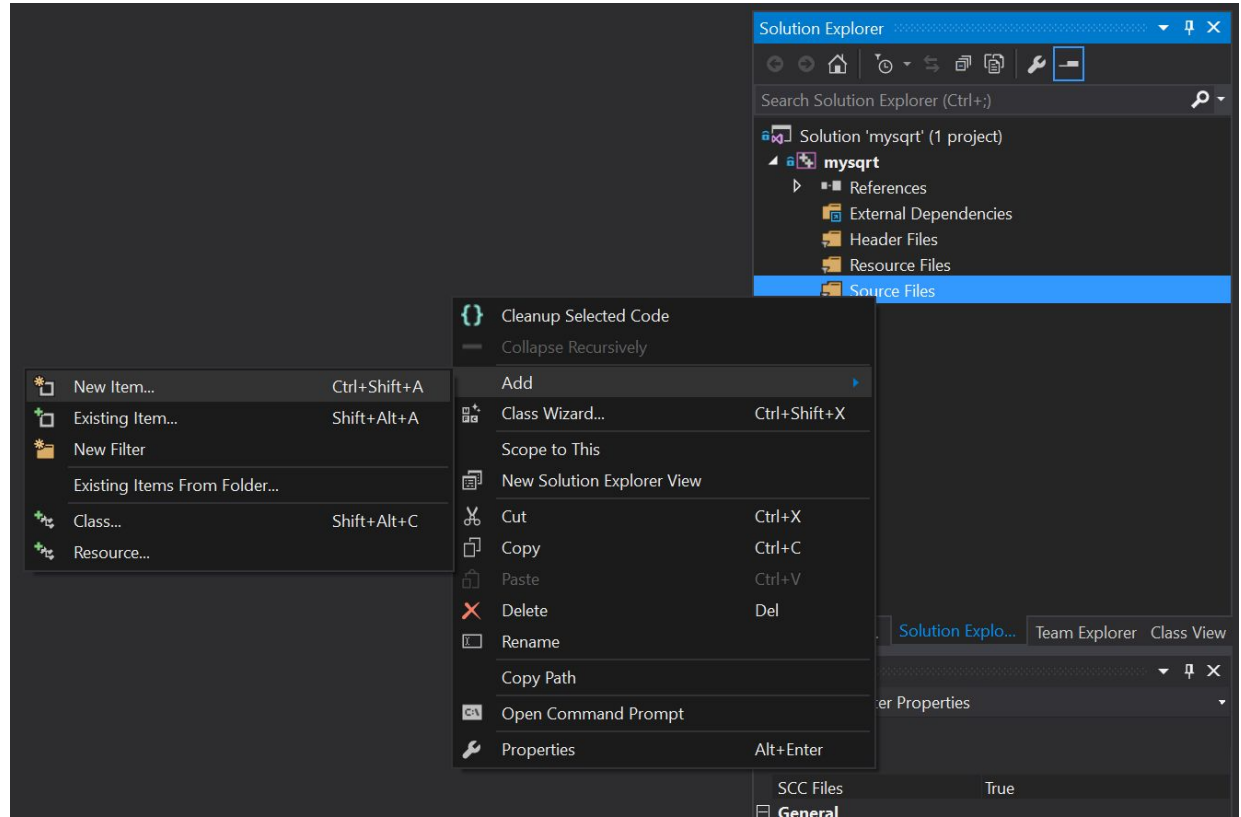
Branch : mysqlt

Commit 3 files

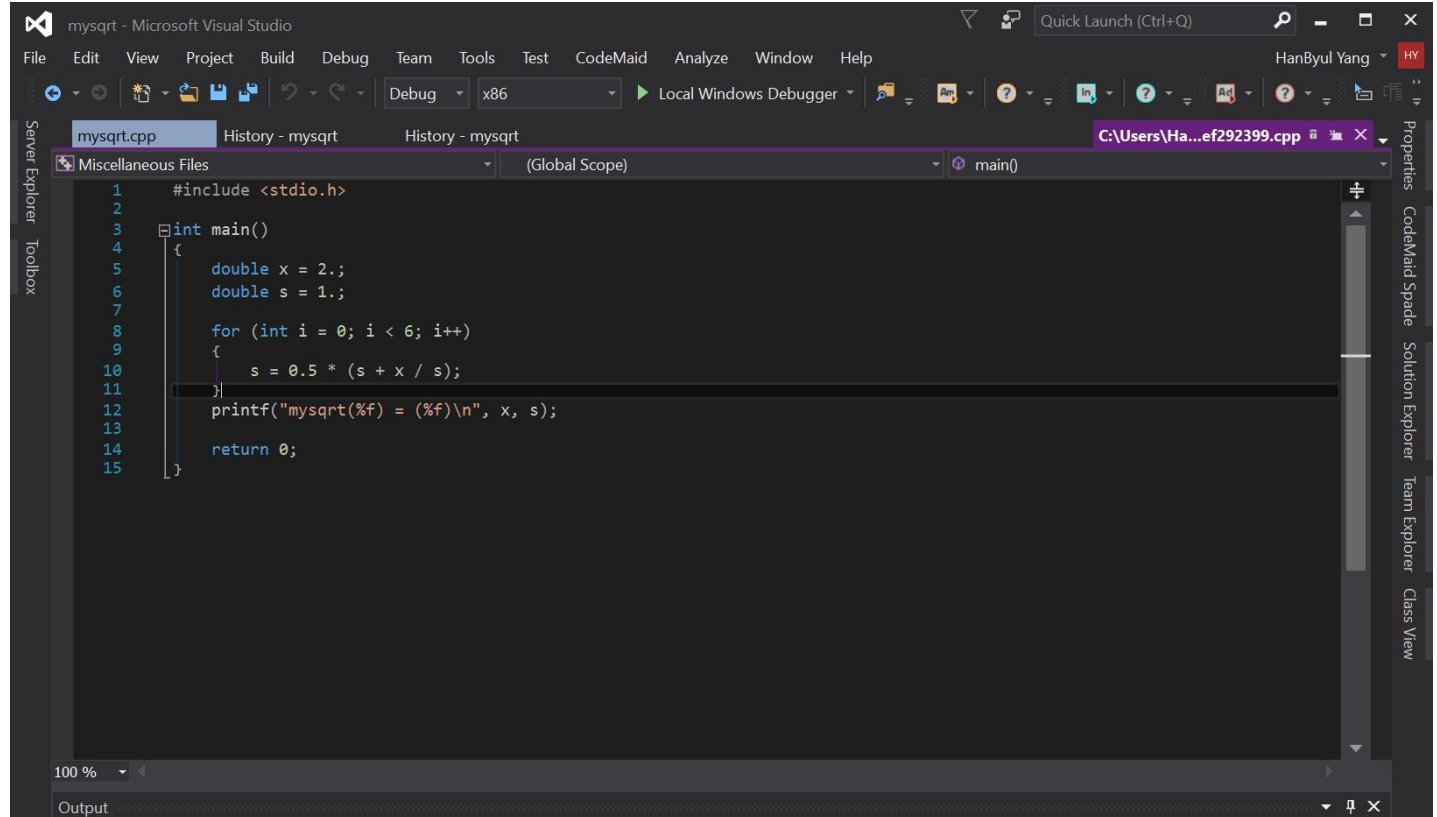
- mysqlt.sln
- mysqlt.vcxproj
- mysqlt.vcxproj.filters



Add “New Item”



Demo : First version of mysqlt

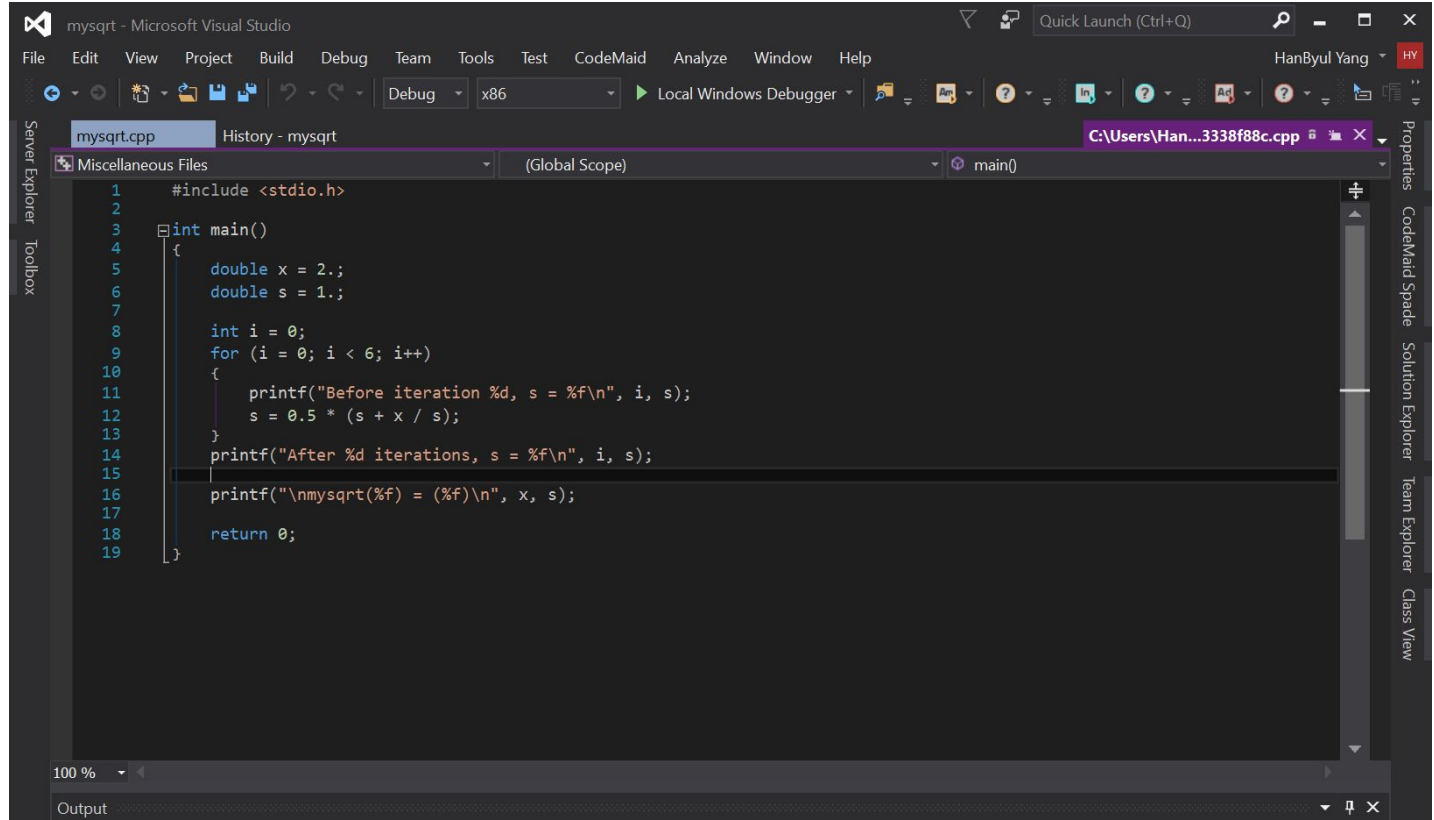


The screenshot shows the Microsoft Visual Studio IDE with the file 'mysqlt.cpp' open. The code is as follows:

```
1  #include <stdio.h>
2
3  int main()
4  {
5      double x = 2.;
6      double s = 1.;
7
8      for (int i = 0; i < 6; i++)
9      {
10         s = 0.5 * (s + x / s);
11     }
12     printf("mysqlt(%f) = (%f)\n", x, s);
13
14     return 0;
15 }
```

The interface includes a menu bar (File, Edit, View, Project, Build, Debug, Team, Tools, Test, CodeMaid, Analyze, Window, Help), a toolbar with icons for file operations and debugging, and a sidebar with 'Server Explorer' and 'Toolbox'. The bottom status bar shows '100 %' zoom and an 'Output' window.

Demo : Print each iteration

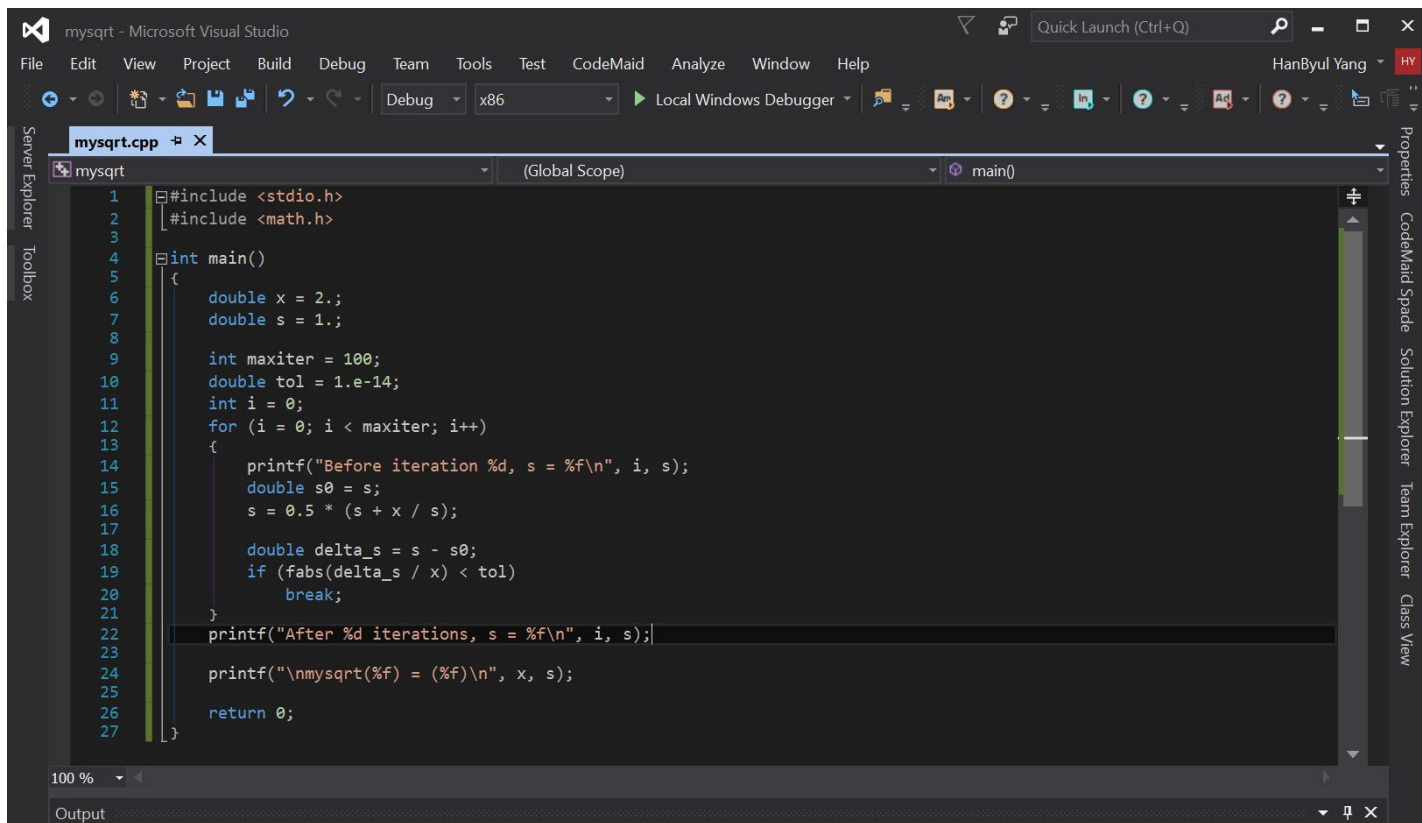


The screenshot shows the Microsoft Visual Studio IDE with a C++ file named `mysqrt.cpp` open. The code implements a function to calculate the square root of a number using the Newton-Raphson method. The program prints the state of variables before and after each iteration of the loop.

```
1  #include <stdio.h>
2
3  int main()
4  {
5      double x = 2.;
6      double s = 1.;
7
8      int i = 0;
9      for (i = 0; i < 6; i++)
10     {
11         printf("Before iteration %d, s = %f\n", i, s);
12         s = 0.5 * (s + x / s);
13     }
14     printf("After %d iterations, s = %f\n", i, s);
15
16     printf("\nmysqrt(%f) = (%f)\n", x, s);
17
18     return 0;
19 }
```

The interface includes the menu bar (File, Edit, View, Project, Build, Debug, Team, Tools, Test, CodeMaid, Analyze, Window, Help), the toolbar, the Solution Explorer showing the project structure, and the Output window at the bottom.

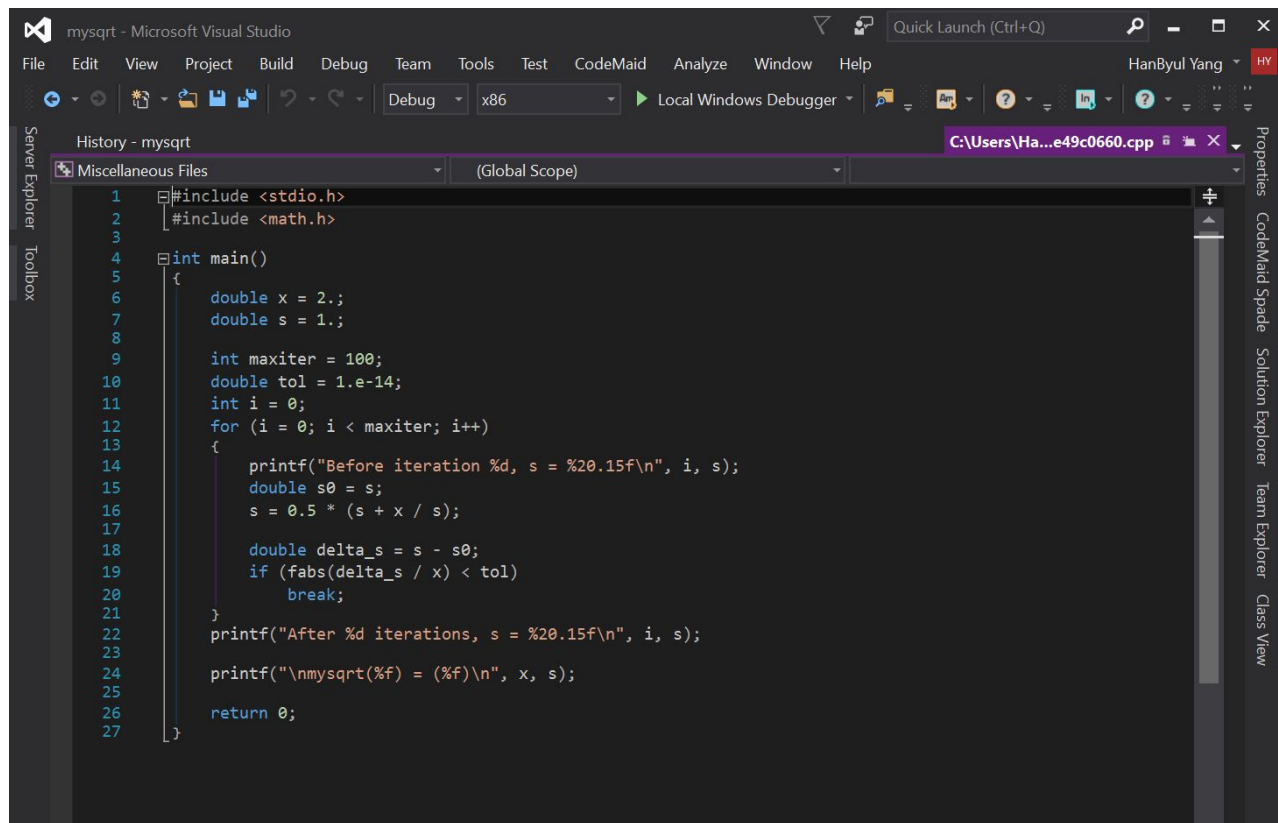
Demo : Add convergence test



The screenshot shows the Microsoft Visual Studio IDE with a C++ project named 'mysqrt'. The code in 'mysqrt.cpp' implements a Newton-Raphson method for finding the square root of a number 'x'. It includes a convergence test that stops the iteration when the relative error is small enough.

```
1  #include <stdio.h>
2  #include <math.h>
3
4  int main()
5  {
6      double x = 2.;
7      double s = 1.;
8
9      int maxiter = 100;
10     double tol = 1.e-14;
11     int i = 0;
12     for (i = 0; i < maxiter; i++)
13     {
14         printf("Before iteration %d, s = %f\n", i, s);
15         double s0 = s;
16         s = 0.5 * (s + x / s);
17
18         double delta_s = s - s0;
19         if (fabs(delta_s / x) < tol)
20             break;
21     }
22     printf("After %d iterations, s = %f\n", i, s);
23
24     printf("\nmysqrt(%f) = (%f)\n", x, s);
25
26     return 0;
27 }
```

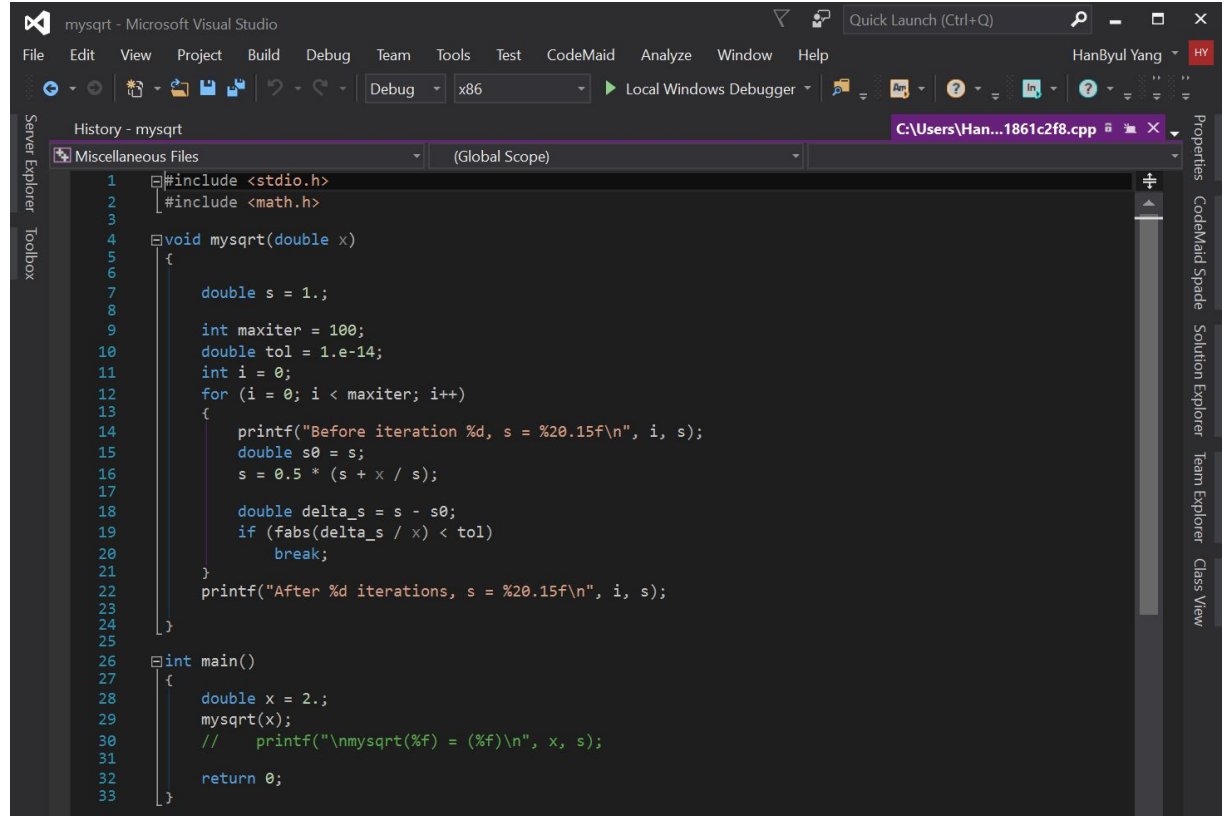

Demo : Refinement of printing floating point number



The screenshot shows the Microsoft Visual Studio IDE with a C++ project named 'mysqrt'. The code is written in a dark-themed editor and implements a function to calculate the square root of a number using the Newton-Raphson method. The code includes standard headers, defines constants for maximum iterations and tolerance, and prints the results at each iteration and at the end.

```
1  #include <stdio.h>
2  #include <math.h>
3
4  int main()
5  {
6      double x = 2.;
7      double s = 1.;
8
9      int maxiter = 100;
10     double tol = 1.e-14;
11     int i = 0;
12     for (i = 0; i < maxiter; i++)
13     {
14         printf("Before iteration %d, s = %20.15f\n", i, s);
15         double s0 = s;
16         s = 0.5 * (s + x / s);
17
18         double delta_s = s - s0;
19         if (fabs(delta_s / x) < tol)
20             break;
21     }
22     printf("After %d iterations, s = %20.15f\n", i, s);
23
24     printf("\nmysqrt(%f) = (%f)\n", x, s);
25
26     return 0;
27 }
```

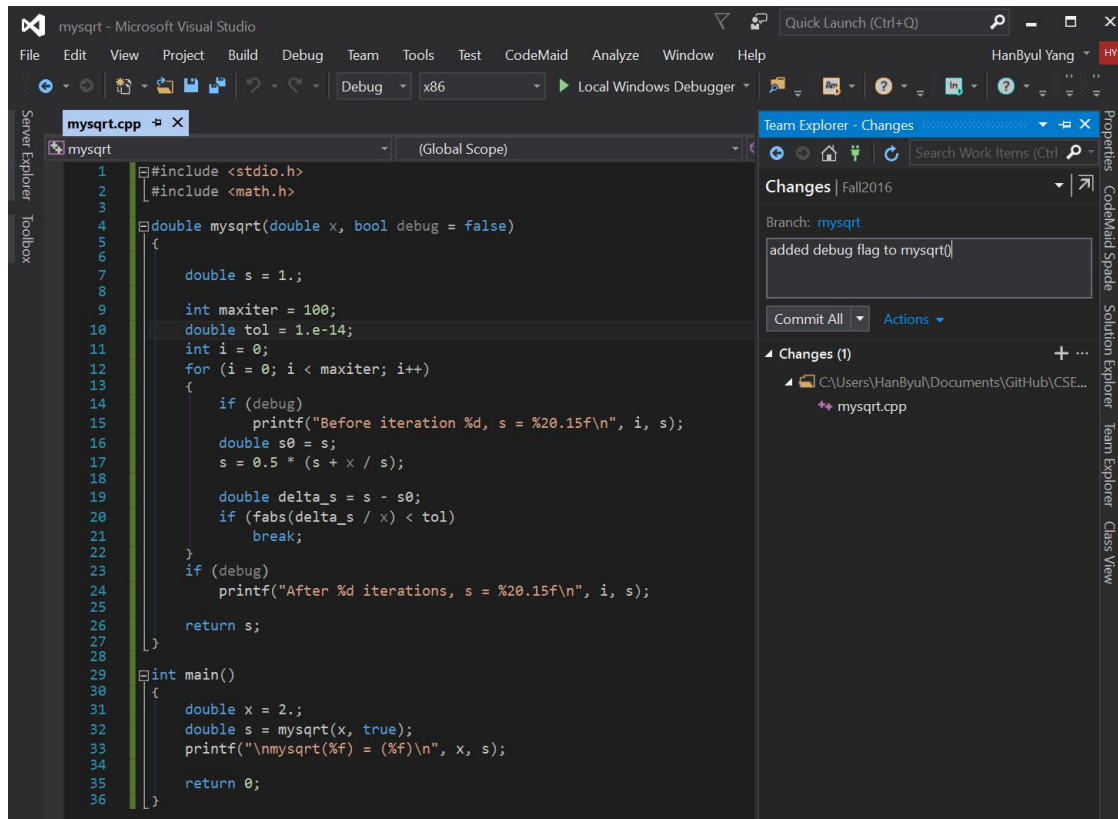
Demo : mysqrt() function



The screenshot shows the Microsoft Visual Studio IDE with a C++ project named 'mysqrt'. The code is written in a dark-themed editor. The file explorer on the left shows 'Miscellaneous Files' and '(Global Scope)'. The code defines a 'mysqrt' function that uses the Newton-Raphson method to calculate the square root of a number 'x'. It includes headers for <stdio.h> and <math.h>. The function takes a 'double x' as input and returns a 'double'. The main function calls 'mysqrt(2.0)' and prints the result.

```
1 #include <stdio.h>
2 #include <math.h>
3
4 void mysqrt(double x)
5 {
6     double s = 1.;
7
8     int maxiter = 100;
9     double tol = 1.e-14;
10    int i = 0;
11    for (i = 0; i < maxiter; i++)
12    {
13        printf("Before iteration %d, s = %20.15f\n", i, s);
14        double s0 = s;
15        s = 0.5 * (s + x / s);
16
17        double delta_s = s - s0;
18        if (fabs(delta_s / x) < tol)
19            break;
20    }
21    printf("After %d iterations, s = %20.15f\n", i, s);
22
23 }
24
25
26 int main()
27 {
28     double x = 2.;
29     mysqrt(x);
30     // printf("\nmysqrt(%f) = (%f)\n", x, s);
31
32     return 0;
33 }
```

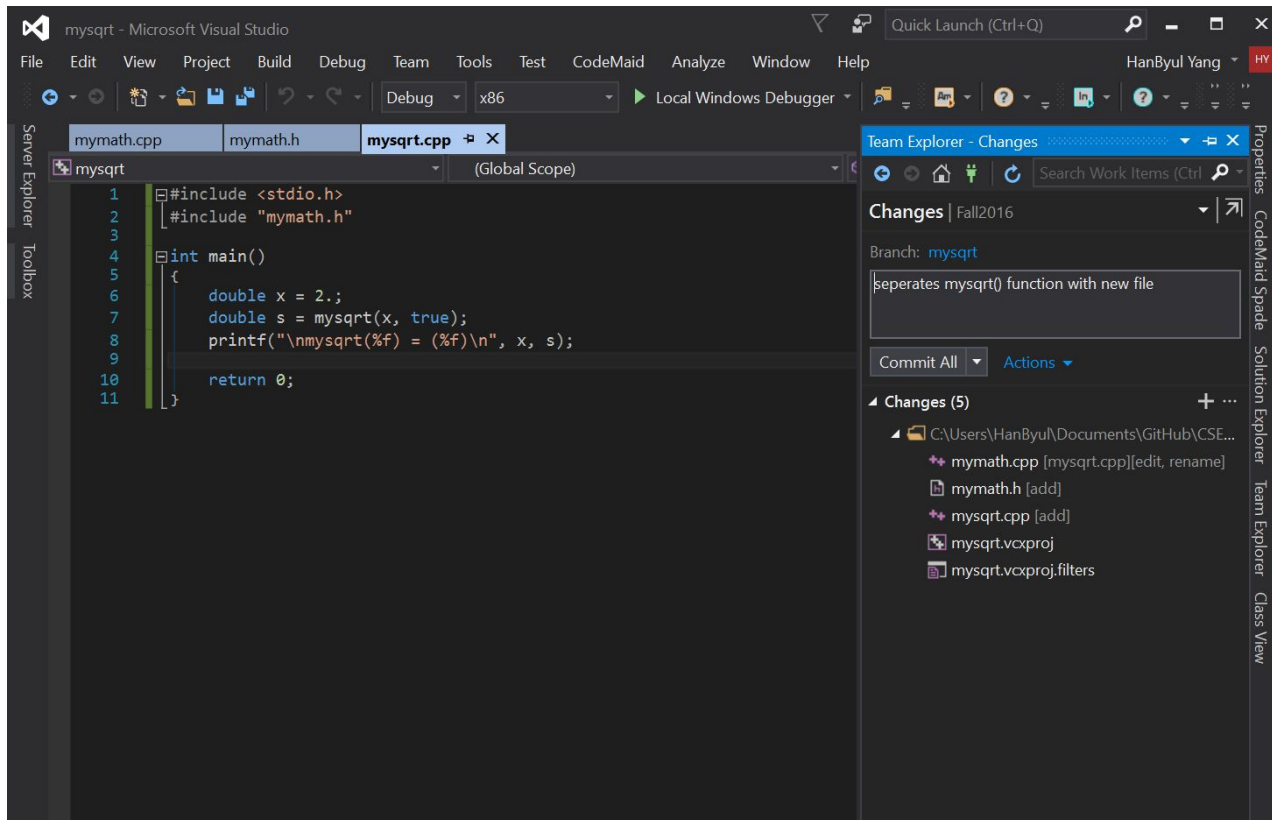
Demo : mysqrt() function with debug flag



Demo : separates mysqrt()

New files

- mymath.h
- mymath.cpp



Links

- [Getting Started with C++ in Visual Studio](#)
- [Visual C++ in Visual Studio 2015](#)
- [C++ Language Reference](#)